

Theory meets experiment 2025

New frontiers in particle cosmology

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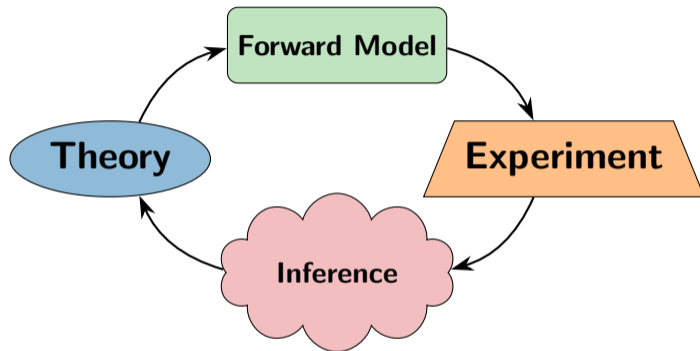


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TMEX: Theory meets experiment

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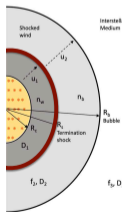
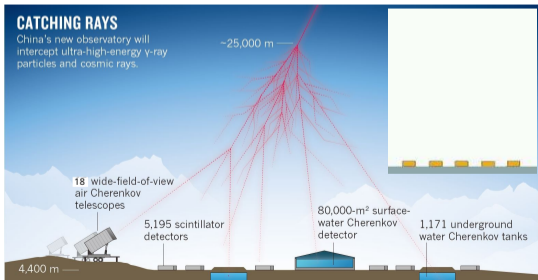
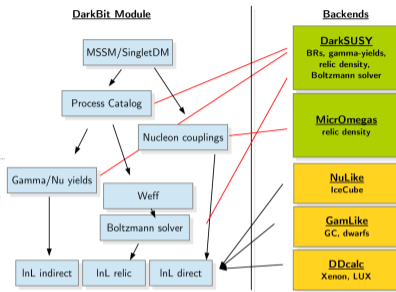
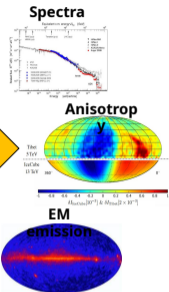
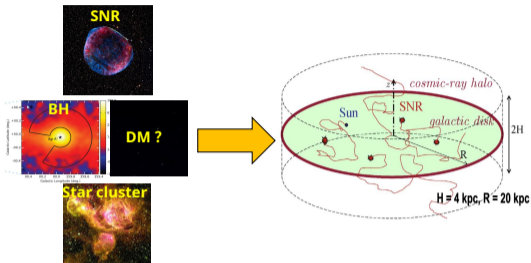


- ▶ Inference sits at the interface between theory and experiment
- ▶ Also called “inverse problems”
- ▶ Process is direct: “measurement”

▶ This talk focuses on **frontiers**:

1. Simulation-based inference
2. GPU-accelerated inference

Examples of forward models from Monday



Time-stationary transport equation in spherical geometry:

$$\frac{\partial}{\partial r} \left[r^2 D(r, p) \frac{\partial f}{\partial r} \right] - r^2 u(r) \frac{\partial f}{\partial r} + \frac{d}{dr} \left[\frac{r^2 u}{3} p \frac{\partial f}{\partial p} \right] + r^2 Q(r, p) = 0$$

- Arbitrary diffusion coefficient $D(r, p)$
- Injection only at the termination shock $Q(r, p) \propto \delta(p - p_{inj}) \delta(r - R_s)$
- Wind velocity profile: $u(r) = \begin{cases} u_1 = v_w & \text{for } r < R_s, \\ \frac{u_1}{\sigma} \left(\frac{R_s}{r} \right)^2 & \text{for } R_s < r < R_b, \\ 0 & \text{for } r > R_b; \end{cases}$

- Boundary conditions:
- No net flux at the cluster center: $r^2 [D \partial_r f - u f]_{r=R_c} = 0$
 - Matching the Galactic distribution: $f(r \rightarrow \infty, p) = f_{gal}(p)$

Morino et al., MNRAS 504 (2021) 4

Bayesian & frequentist data combination

Multimessenger approaches

Frequentist

- ▶ Preferred by particle physicists & mathematicians
- ▶ Probability/stochasticity only in the data D

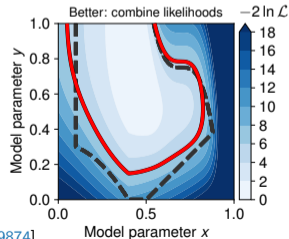
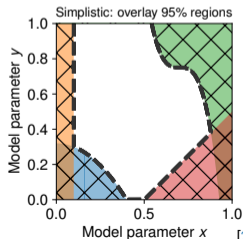
- ▶ Whether Bayesian or frequentist, If you have a model M with parameters θ , multiple datasets combine at the likelihood level:

$$P(D_1, D_2 | \theta, M) = P(D_1 | \theta, M) P(D_2 | \theta, M)$$

$$\mathcal{L}_{\text{joint}} = \mathcal{L}_1 \times \mathcal{L}_2 \times \dots \times \mathcal{L}_n$$

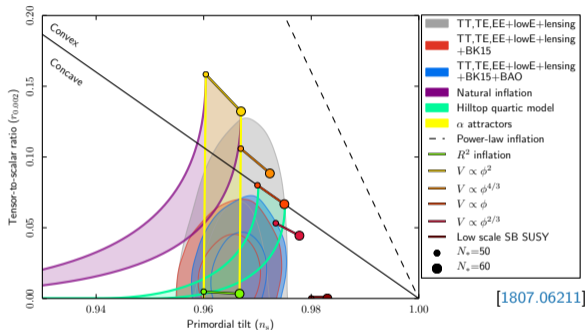
Bayesian

- ▶ Preferred by astronomers & machine learning/information theorists
- ▶ Quantifies all uncertainties in data & model (D, θ, M) using probability.

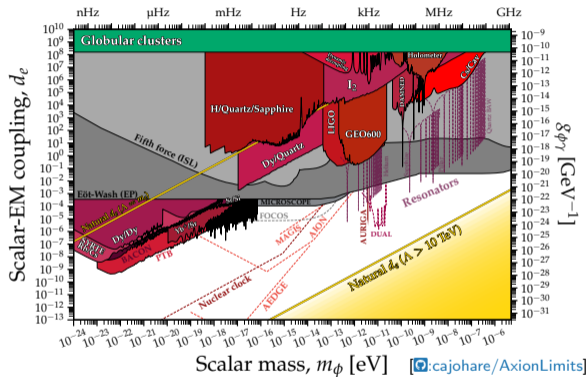


An aside: difference in plotting

Exclusion vs. posterior plots



- ▶ Contours indicate **allowed** regions
- ▶ Preferred in astro/cosmology

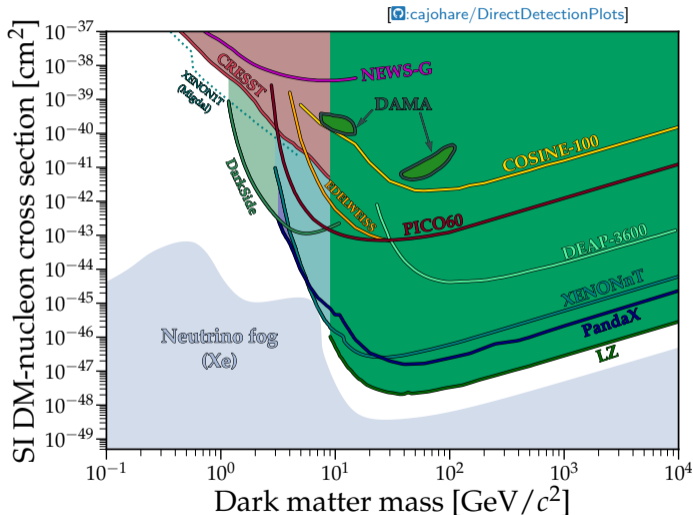


- ▶ Contours indicate **excluded** regions
- ▶ Preferred in particle physics

An aside: difference in plotting

Exclusion vs. posterior plots

- ▶ Beware this kind of particularly confusing plot, which uses both!
- ▶ Here almost all of these are 2σ exclusion plots
- ▶ But 'DAMA' are (controversial & conflicting) superimposed constraints/allowed regions.



The three pillars of (Bayesian) inference

Parameter estimation

What do the data tell us about the parameters of a model?

e.g. the size or age of a Λ CDM universe

$$P(\theta|D, M) = \frac{P(D|\theta, M)P(\theta|M)}{P(D|M)}$$

$$\mathcal{P} = \frac{\mathcal{L} \times \pi}{\mathcal{Z}}$$

$$\text{Posterior} = \frac{\text{Likelihood} \times \text{Prior}}{\text{Evidence}}$$

Model comparison

How much does the data support a particular model?

e.g. Λ CDM vs a dynamic dark energy cosmology

$$P(M|D) = \frac{P(D|M)P(M)}{P(D)}$$

$$\frac{\mathcal{Z}_M \Pi_M}{\sum_m \mathcal{Z}_m \Pi_m}$$

$$\text{Posterior} = \frac{\text{Evidence} \times \text{Prior}}{\text{Normalisation}}$$

Tension quantification

Do different datasets make consistent predictions from the same model? *e.g. CMB vs Type IA supernovae data*

$$\mathcal{R} = \frac{\mathcal{Z}_{AB}}{\mathcal{Z}_A \mathcal{Z}_B}$$

$$\begin{aligned} \log \mathcal{S} &= \langle \log \mathcal{L}_{AB} \rangle_{\mathcal{P}_{AB}} \\ &\quad - \langle \log \mathcal{L}_A \rangle_{\mathcal{P}_A} \\ &\quad - \langle \log \mathcal{L}_B \rangle_{\mathcal{P}_B} \end{aligned}$$

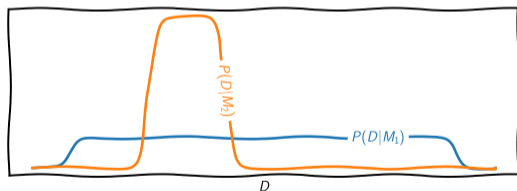
Model comparison $\mathcal{Z} = P(D|M)$

- ▶ Bayesian model comparison allows mathematical derivation of key philosophical principles.

Viewed from data-space D :

Popper's falsificationism

- ▶ Prefer models that make bold predictions.
- ▶ if proven true, model more likely correct.



- ▶ Falsificationism comes from normalisation

Viewed from parameter-space θ :

Occam's razor

- ▶ Models should be as simple as possible
- ▶ ... but no simpler

- ▶ Occam's razor equation:

$$\log \mathcal{Z} = \langle \log \mathcal{L} \rangle_{\mathcal{P}} - \mathcal{D}_{\text{KL}}$$

- ▶ "Occam penalty": KL divergence between prior π and posterior \mathcal{P} .

$$\mathcal{D}_{\text{KL}} \sim \log \frac{\text{Prior volume}}{\text{Posterior volume}}$$

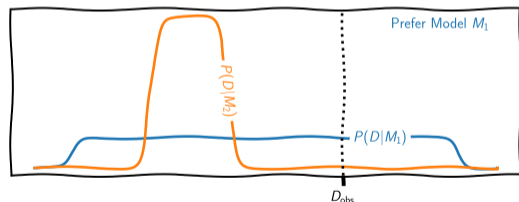
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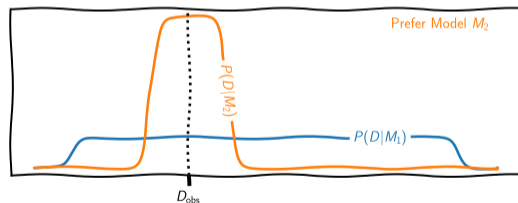
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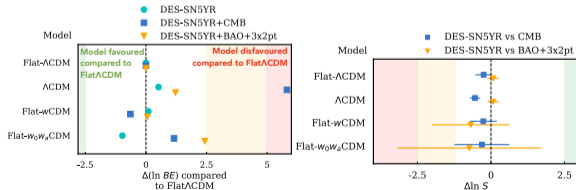
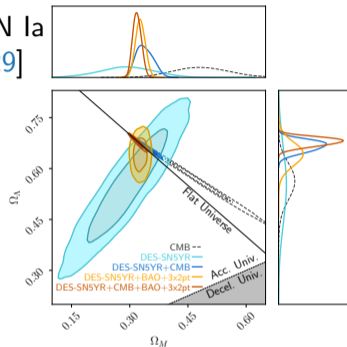
LBI: Likelihood-based inference

The standard approach if you are fortunate enough to have a likelihood function $P(D|\theta)$:

$$P(\theta|D) = \frac{P(D|\theta)P(\theta)}{P(D)}$$

1. Define **prior** $\pi(\theta)$
 - ▶ spend some time being philosophical
2. Sample **posterior** $\mathcal{P}(\theta|D)$
 - ▶ use out-of-the-box MCMC tools such as emcee or MultiNest
 - ▶ make some triangle plots
3. Optionally compute **evidence** $\mathcal{Z}(D)$
 - ▶ e.g. nested sampling or parallel tempering
 - ▶ do some model comparison (i.e. science)
 - ▶ talk about tensions

DES Y5 SN Ia
[2401.02929]



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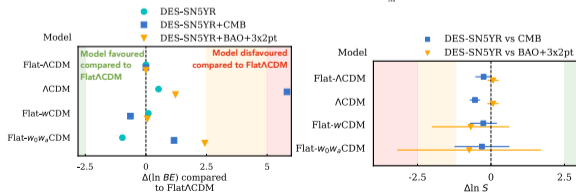
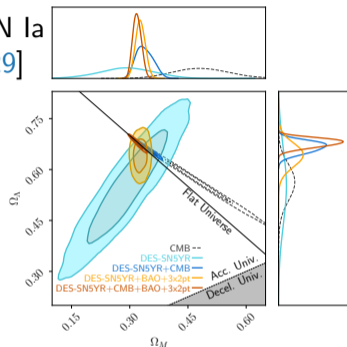
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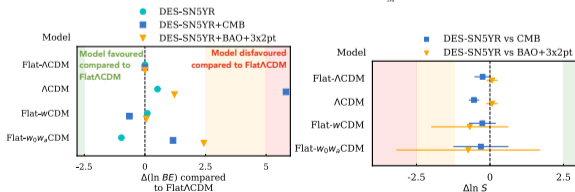
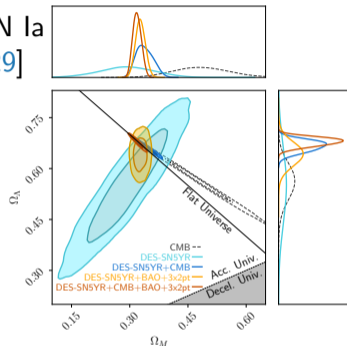
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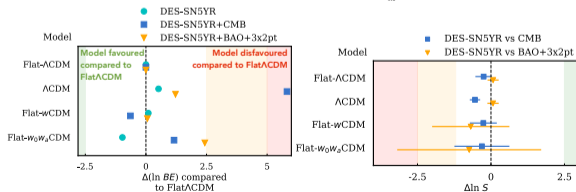
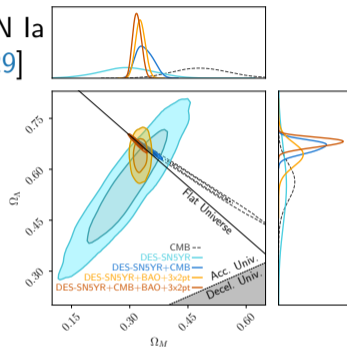
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$$\mathcal{P} \times \mathcal{Z} = \mathcal{J} = \mathcal{L} \times \pi, \quad \text{Joint} = \mathcal{J} = P(\theta, D)$$

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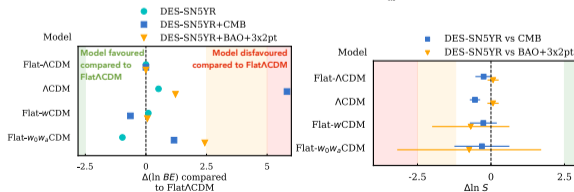
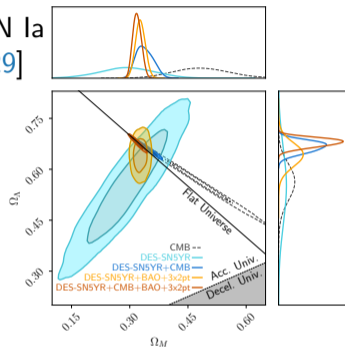
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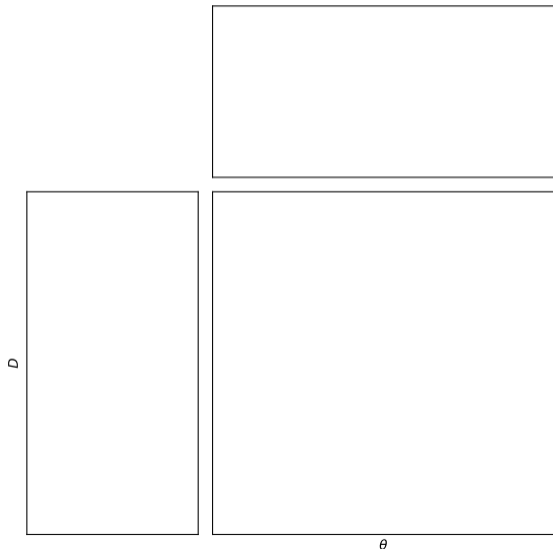
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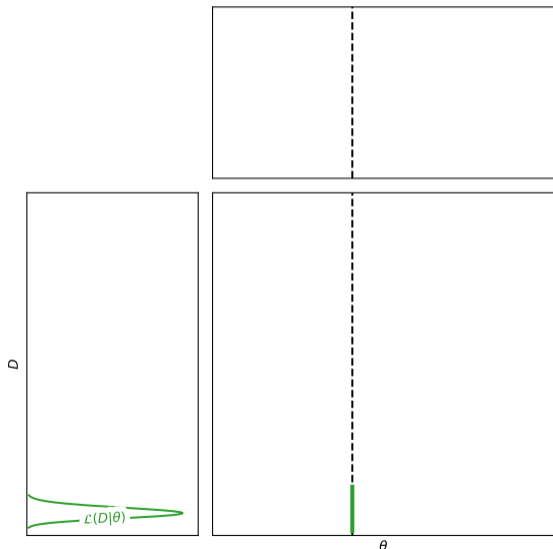
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- ▶ Simulator generates samples from $\mathcal{L}(\cdot|\theta)$.
- ▶ With a prior $\pi(\theta)$ can generate samples from *joint distribution* $\mathcal{J}(\theta, D) = \mathcal{L}(D|\theta)\pi(\theta)$ the “probability of everything”.
- ▶ Task of SBI is take joint \mathcal{J} samples and learn *posterior* $\mathcal{P}(\theta|D)$ and *evidence* $\mathcal{Z}(D)$ and possibly *likelihood* $\mathcal{L}(D|\theta)$.
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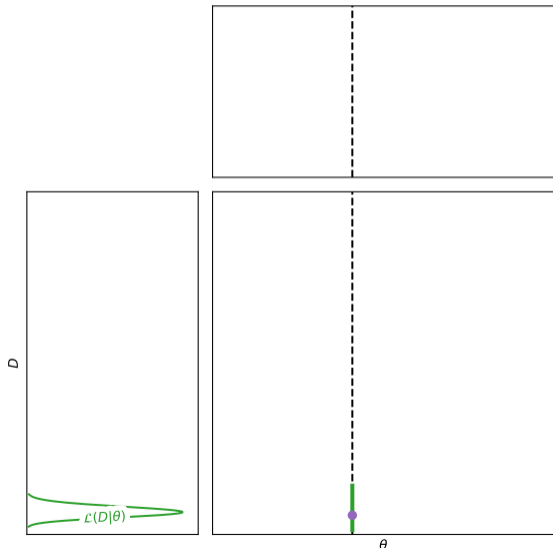
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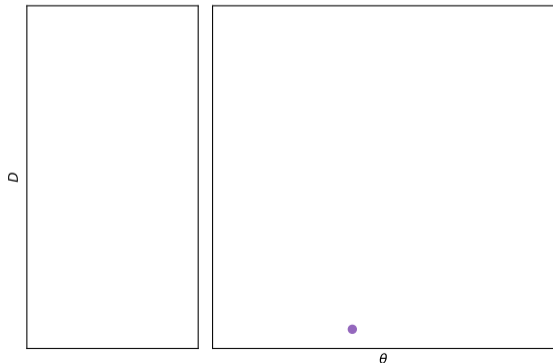
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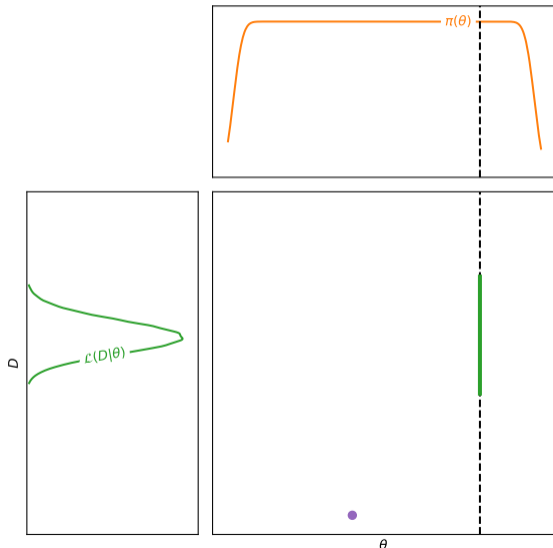
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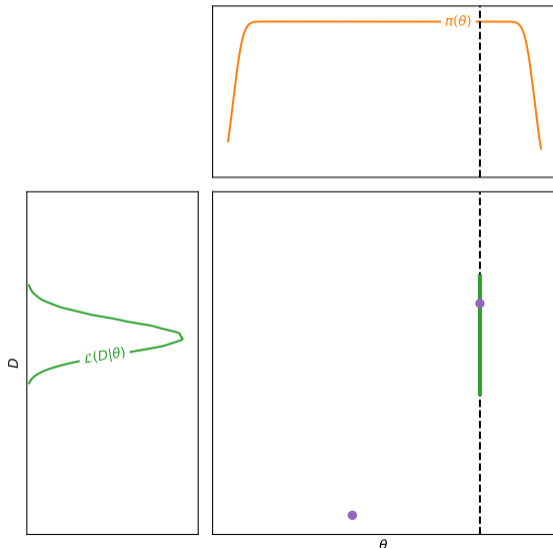
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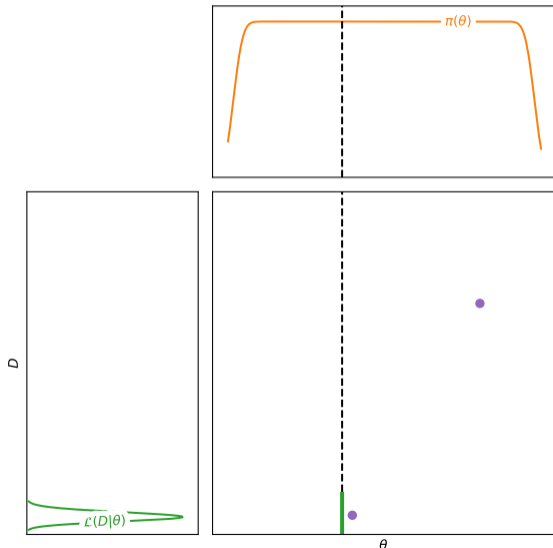
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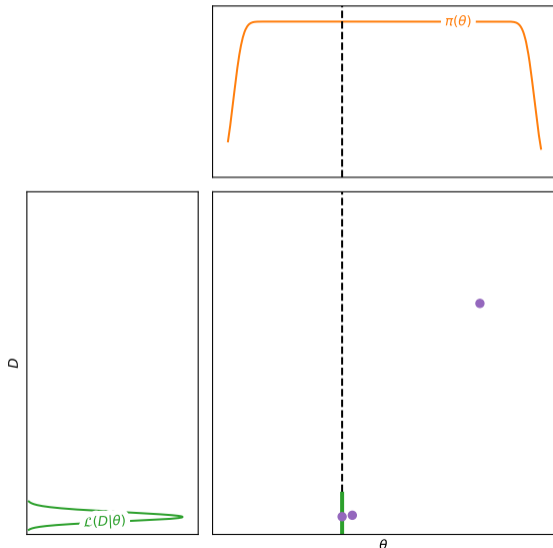
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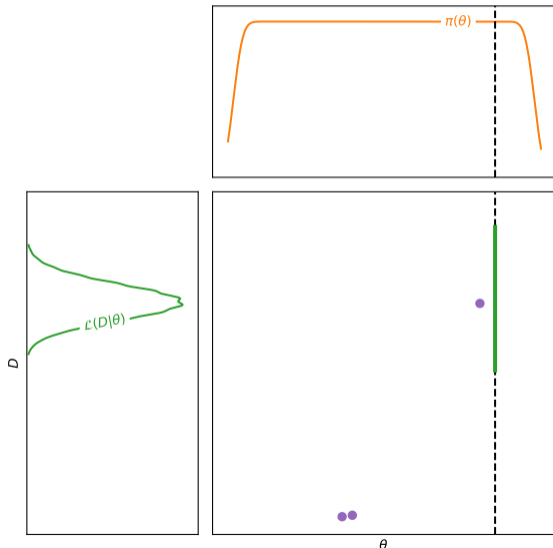
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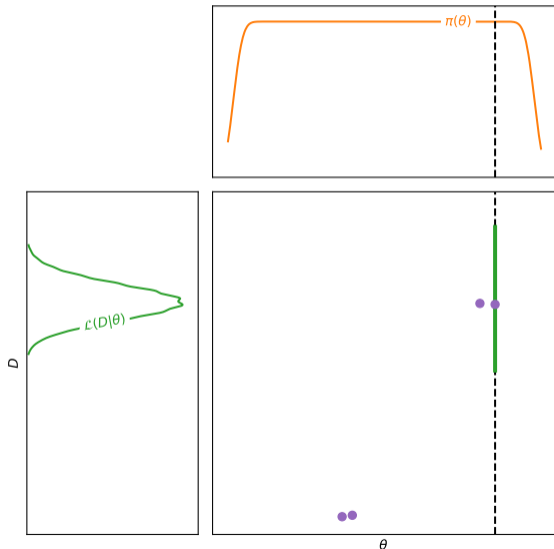
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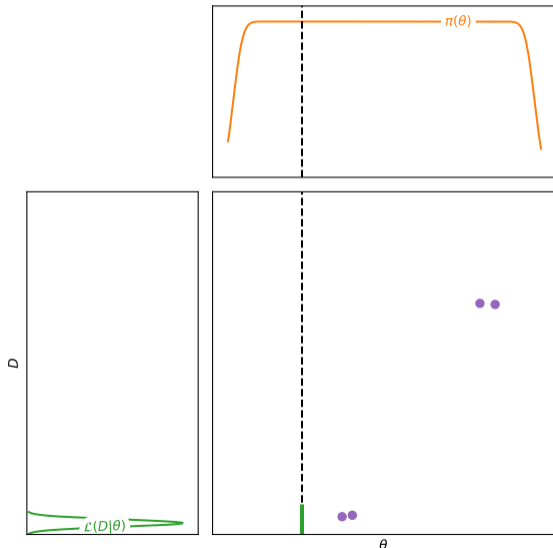
SBI: Simulation-based inference

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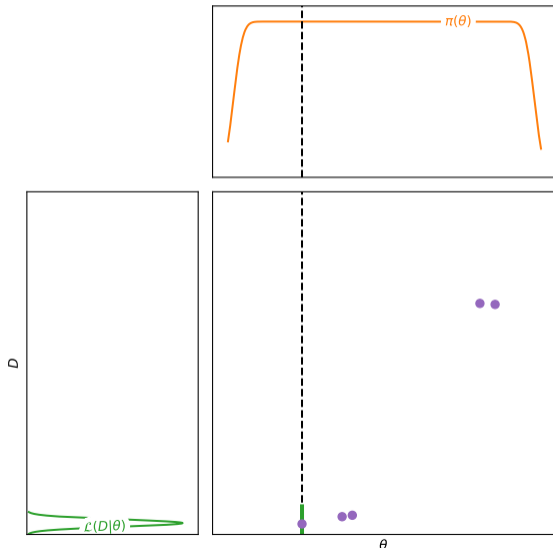
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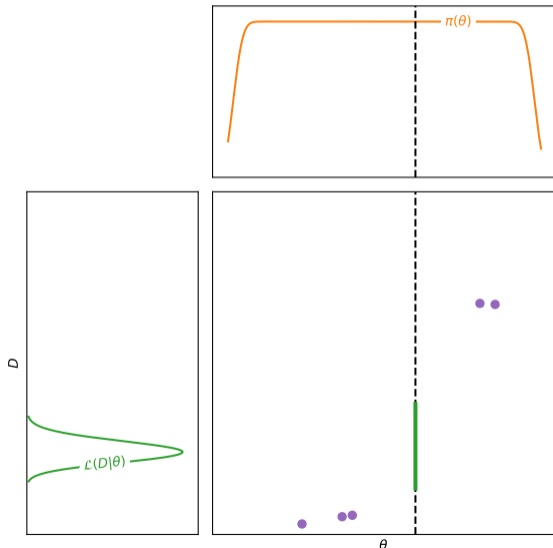
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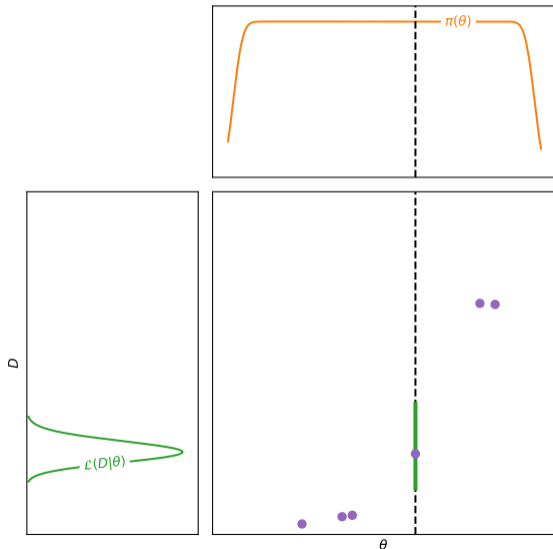
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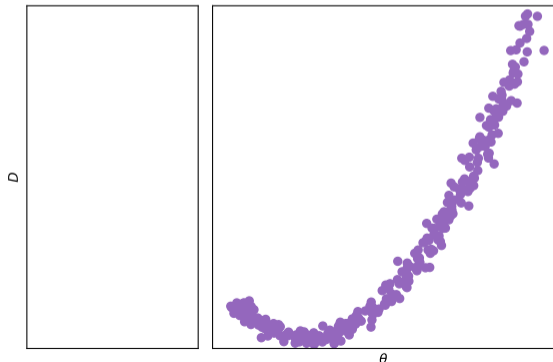
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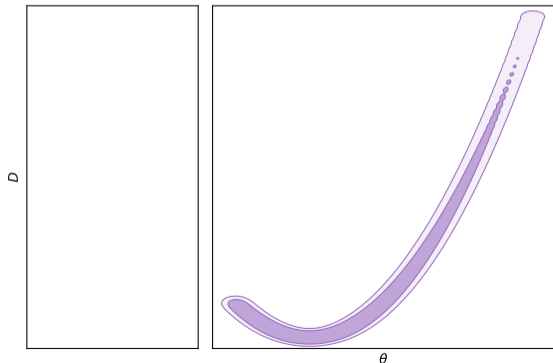
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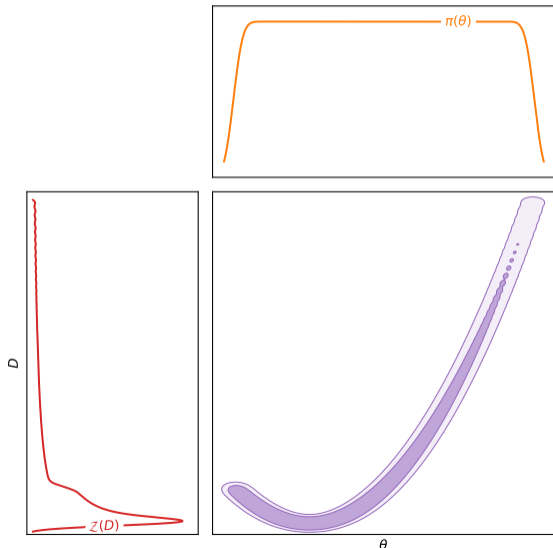
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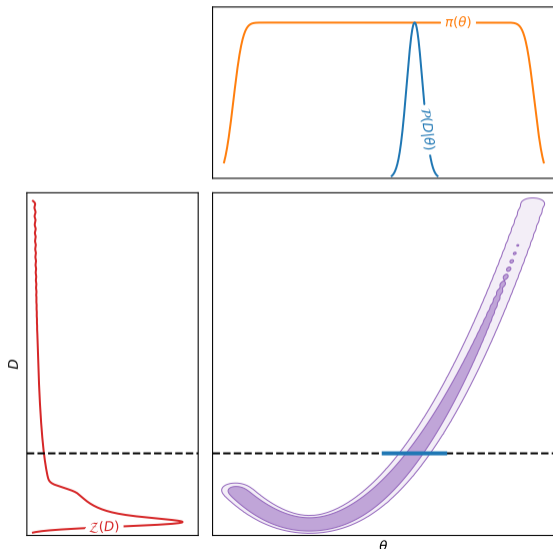
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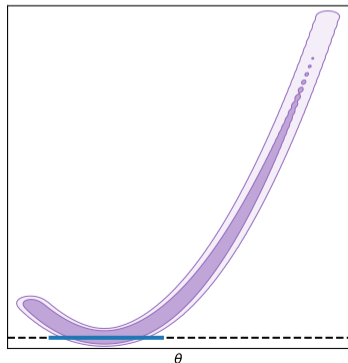
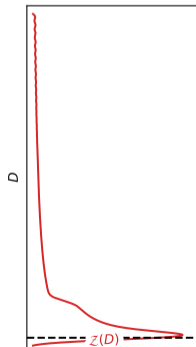
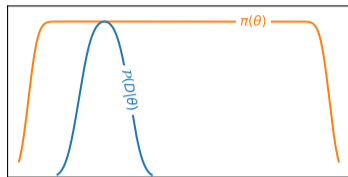
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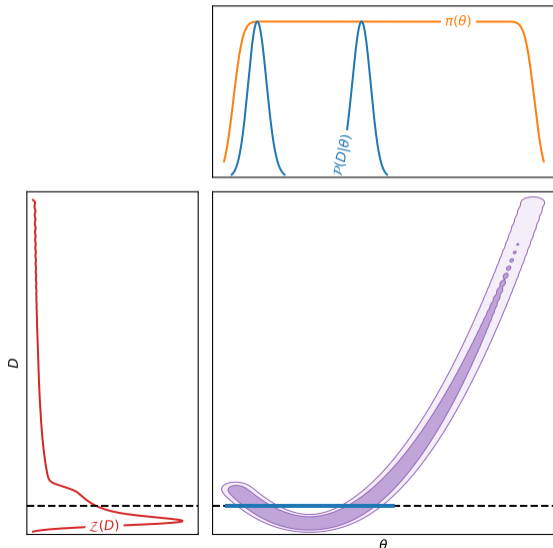
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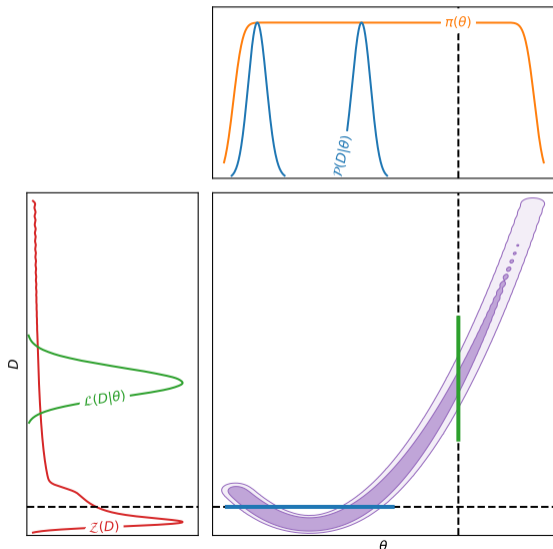
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Why SBI?

SBI is useful because:

1. If you don't have a likelihood, you can still do inference
 - ▶ This is the usual case beyond CMB cosmology
2. Faster than LBI
 - ▶ emulation – also applies to LBI in principle
3. No need to pragmatically encode fiducial cosmologies
 - ▶ Covariance computation implicitly encoded in simulations
 - ▶ Highly relevant for disentangling tensions & systematics
4. Equips AI/ML with Bayesian interpretability
5. Lower barrier to entry than LBI
 - ▶ Much easier to forward model a systematic
 - ▶ Emerging set of plug-and-play packages
 - ▶ For this reason alone, it will come to dominate scientific inference



A screenshot of a GitHub repository page for 'sbi: simulation-based inference'. The repository is owned by 'sbi-dev'. The main content shows the README file, which describes 'sbi' as a Python toolbox for simulation-based inference. It lists key features like 'No likelihood required', 'Supports arbitrary models', and 'Supports arbitrary data'. The repository has 1,000 stars and 100 forks.

[\[sbi-dev\]](#)



[\[undark-lab/swyft\]](#)



[\[florent-leclercq/pyself\]](#)



[\[justinalising/pydelfi\]](#)

- ▶ 2024 has been the year it has started to be applied to real data.
- ▶ Mostly for weak lensing
- ▶ However: SBI requires mock data generation code
- ▶ Most data analysis codes were built before the generative paradigm.
- ▶ It's still a lot of work to upgrade cosmological likelihoods to be able to do this (e.g. plik & camspec).
- ▶ [\[📄:smsharma/awesome-neural-sbi\]](https://github.com/smsharma/awesome-neural-sbi)

Investigating the turbulent hot gas in X-COP galaxy clusters

S. Dupourqu¹, N. Clerc¹, E. Pointecouteau¹, D. Eckert², S. Ettori¹, and F. Vazza^{4,5,6}

Dark Energy Survey Year 3 results: simulation-based cosmological inference with wavelet harmonics, scattering transforms, and moments of weak lensing mass maps II. Cosmological results

M. Gatti^{1,*}, G. Campailla², N. Jeffrey³, L. Whiteway³, A. Porceddu⁴, J. Prat⁵, J. Williamson⁵, M. Raveri², B.

Neural Posterior Estimation with guaranteed exact coverage: the ringdown of GW150914

Marco Crisostomi^{1,2}, Kallol Dey³, Enrico Barausse^{1,2}, Roberto Trotta^{1,2,4,5}

Applying Simulation-Based Inference to Spectral and Spatial Information from the Galactic Center Gamma-Ray Excess

Katharena Christy^a, Eric J. Baxter^b, Jason Kumar^a

KiDS-1000 and DES-Y1 combined: Cosmology from peak count statistics

Joachim Harnois-Déraps^{1*}, Sven Heydenreich², Benjamin Giblin³, Nicolas Martinet⁴, Tilman Tröster⁵, Marika Asgari^{1,6,7}, Pierre Burger^{8,9,10}, Tiago Castro^{11,12,13,14}, Klaus Dolag¹⁵, Catherine Heymans^{3,16}, Hendrik Hildebrandt¹⁶, Benjamin Joachimi¹⁷ & Angus H. Wright¹⁶

KiDS-SBI: Simulation-Based Inference Analysis of KiDS-1000 Cosmic Shear

Maximilian von Wietersheim-Kramat^{1,2,3}, Kiyam Lin¹, Nicolas Tessore¹, Benjamin Joachimi¹, Arthur Loureiro^{4,5}, Robert Reischke^{6,7}, and Angus H. Wright⁷

Simulation-based inference of deep fields: galaxy population model and redshift distributions

Beatrice Moser,^{a,1} Tomasz Kacprzak,^{a,b} Silvan Fischbacher,^a Alexandre Refregier,^a Dominic Grimm,^a Luca Tortorelli^c

SBI-BIG: Cosmological Constraints using Simulation-Based Inference of Galaxy Clustering with Marked Power Spectra

ELENA MARRARA^{1,2,*}, CHANGHOON HAN³, MICHAEL ECKENBERG⁴, SHIRLEY HO⁵, JIAMIN HOU^{6,7}, PARAG LEMON^{8,9,10}, CHIRAG MODI^{4,11}, AJASHH MOHAMMEDRAB DEBARI^{12,13}, LIAM PARKER^{14,15} AND BRUNO RECALDO-SANTY BLANCAID¹⁶

Cosmology from HSC Y1 Weak Lensing with Combined Higher-Order Statistics and Simulation-based Inference

Camila P. Novaes^{1,2,3,*}, Leander Thiele^{2,3,1}, Joaquin Armijo^{2,3}, Sihao Cheng^{4,5}, Jessica A. Cowell^{2,3,6}, Gabriela A. Marques^{7,8}, Elisa G. M. Ferreira^{2,9}, Masato Shirasaki^{10,10}, Ken Osato^{11,12,2}, and Jia Liu^{2,3}

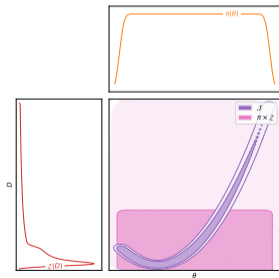
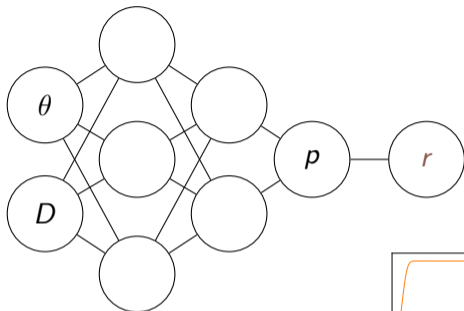
Neural Ratio Estimation

► SBI flavours: github.com/sbi-dev/sbi

- NPE Neural posterior estimation
- NLE Neural likelihood estimation
- NJE Neural joint estimation
- NRE Neural ratio estimation

► NRE recap:

1. Generate joint samples $(\theta, D) \sim \mathcal{J}$
 - straightforward if you have a simulator:
 $\theta \sim \pi(\cdot)$, $D \sim \mathcal{L}(\cdot|\theta)$
2. Generate separated samples $\theta \sim \pi$, $D \sim \mathcal{Z}$
 - aside: can shortcut step 2 by scrambling the (θ, D) pairings from step 1
3. Train probabilistic classifier p to distinguish whether (θ, D) came from \mathcal{J} or $\pi \times \mathcal{Z}$.
4. $\frac{p}{1-p} = r = \frac{P(\theta, D)}{P(\theta)P(D)} = \frac{\mathcal{J}}{\pi \times \mathcal{Z}} = \frac{\mathcal{L}}{\mathcal{Z}} = \frac{\mathcal{P}}{\pi}$.
5. Use ratio r for parameter estimation $\mathcal{P} = r \times \pi$



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Bayesian proof

► Let $M_{\mathcal{J}}: (\theta, D) \sim \mathcal{J}$, $M_{\pi \mathcal{Z}}: (\theta, D) \sim \pi \times \mathcal{Z}$

► Classifier gives

$$p(\theta, D) = P(M_{\mathcal{J}}|\theta, D) = 1 - P(M_{\pi \mathcal{Z}}|\theta, D)$$

► Bayes theorem then shows

$$\frac{p}{1-p} = \frac{P(M_{\mathcal{J}}|\theta, D)}{P(M_{\pi \mathcal{Z}}|\theta, D)} = \frac{P(\theta, D|M_{\mathcal{J}})P(M_{\mathcal{J}})}{P(\theta, D|M_{\pi \mathcal{Z}})P(M_{\pi \mathcal{Z}})} = \frac{\mathcal{J}}{\pi \mathcal{Z}},$$

where we have assumed

► $P(M_{\mathcal{J}}) = P(M_{\pi \mathcal{Z}})$,

and by definition

► $\mathcal{J}(\theta, D) = P(\theta, D|M_{\mathcal{J}})$

► $\pi(\theta)\mathcal{Z}(D) = P(\theta, D|M_{\pi \mathcal{Z}})$.

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Why I like NRE

- The link between classification and inference is profound.
- Density estimation is hard – Dimensionless r divides out the hard-to-calculate parts.

Why I don't like NRE

- Practical implementations require marginalisation [2107.01214], or autoregression [2308.08597].
- Model comparison and parameter estimation are separate [2305.11241].

I want (my student) to get started with SBI...

... where should I send them?

the swyft package

- ▶ Ratio estimation
- ▶ astro/cosmology specific examples

swyft.readthedocs.io/en/stable

the pydelfi package

- ▶ Neural density estimation
- ▶ astro/cosmology specific examples

justinalsing.github.io/pydelfi

the sbi package

- ▶ General package
- ▶ Not domain specific
- ▶ A lot of (opaquely named) methods

sbi-dev.github.io/sbi/latest/tutorials

All methods generally require:

- ▶ A forward simulator
- ▶ A data compressor

All methods either:

- ▶ “Amortized” over data D
- ▶ “Sequential” tuning to D_{obs}

GPU-accelerated inference

CMB cosmopower [2106.03846]

CMB candl [2401.13433]

SNe BayesSN [2401.08755]

SGW Eryn [2303.02164]

GW redback [2308.12806]

GW ripple [2302.05329]

EP ExoJAX [2105.14782]

X jaxspec [2409.05757]

[:JAXtronomy]

- ▶ Increase in the number of cosmological codes written for GPUs (particularly jax).
- ▶ Over the next few years, more and more analyses will be done on GPUs.
- ▶ Several trends trigger this
 - ▶ the rise of machine learning, whose linear algebra is well-suited to GPUs
 - ▶ the creation of usable languages for GPU programming (e.g. jax, pytorch, tensorflow)
 - ▶ the rise of large language models, which ease writing codes for GPUs
- ▶ Prediction: low-power GPUs (likely ARM-based) will become the norm for scientific computing.



- ▶ **very** recent work over the past month
- ▶ Have implemented a nested slice sampler in blackjax [[GitHub: blackjax-devs/blackjax/pull/755](https://github.com/blackjax-devs/blackjax/pull/755)].

```
1 pip install git+https://github.com/handleylab/blackjax@nested_sampling
2 import blackjax.ns.adaptive
```

- ▶ Think MultiNest for jax.
- ▶ Plugs into jim [[GitHub: kazewong/jim](https://github.com/kazewong/jim)] and ripple [[2302.05329](https://arxiv.org/abs/2302.05329)]

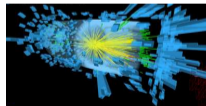
Conclusions

:handley-lab

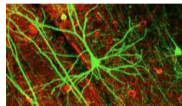


- ▶ **Inference** bridges theory and experiment, crucial for extracting information from data.
- ▶ **Simulation-Based Inference (SBI)** enables inference when the likelihood is intractable, using simulations and machine learning. SBI is becoming increasingly popular for complex astrophysical analyses.
- ▶ **GPU-accelerated inference** is transforming the field, allowing faster and more complex computations. Tools like `jax` are empowering a new generation of GPU-ready inference codes.

Frontiers of simulation based inference [1911.01429]



Particle colliders



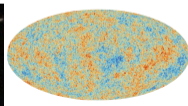
Neuron activity



Epidemics



Gravitational lensing



Evolution of the Universe

