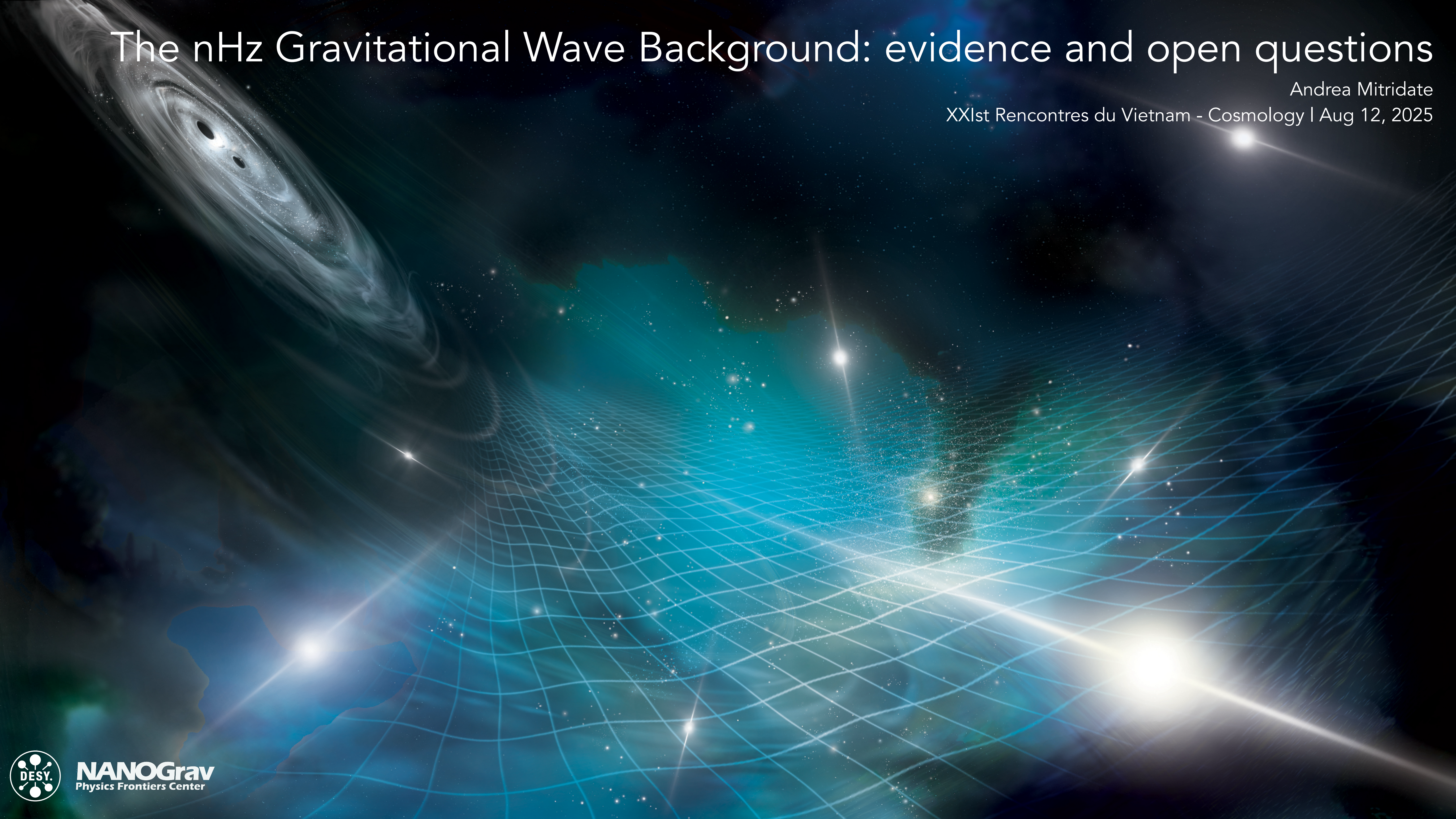


The nHz Gravitational Wave Background: evidence and open questions

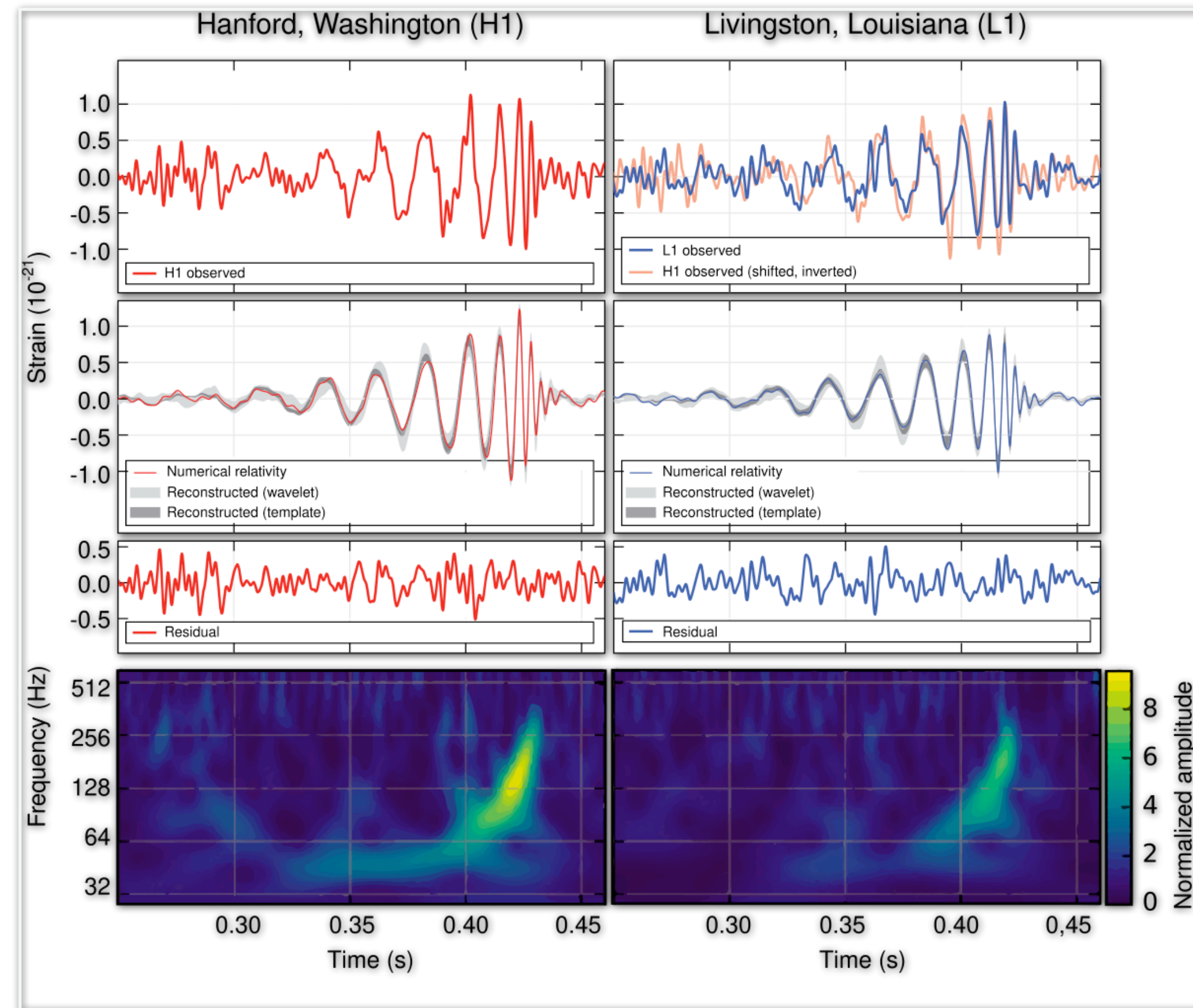
Andrea Mitridate

XXIst Rencontres du Vietnam - Cosmology I Aug 12, 2025



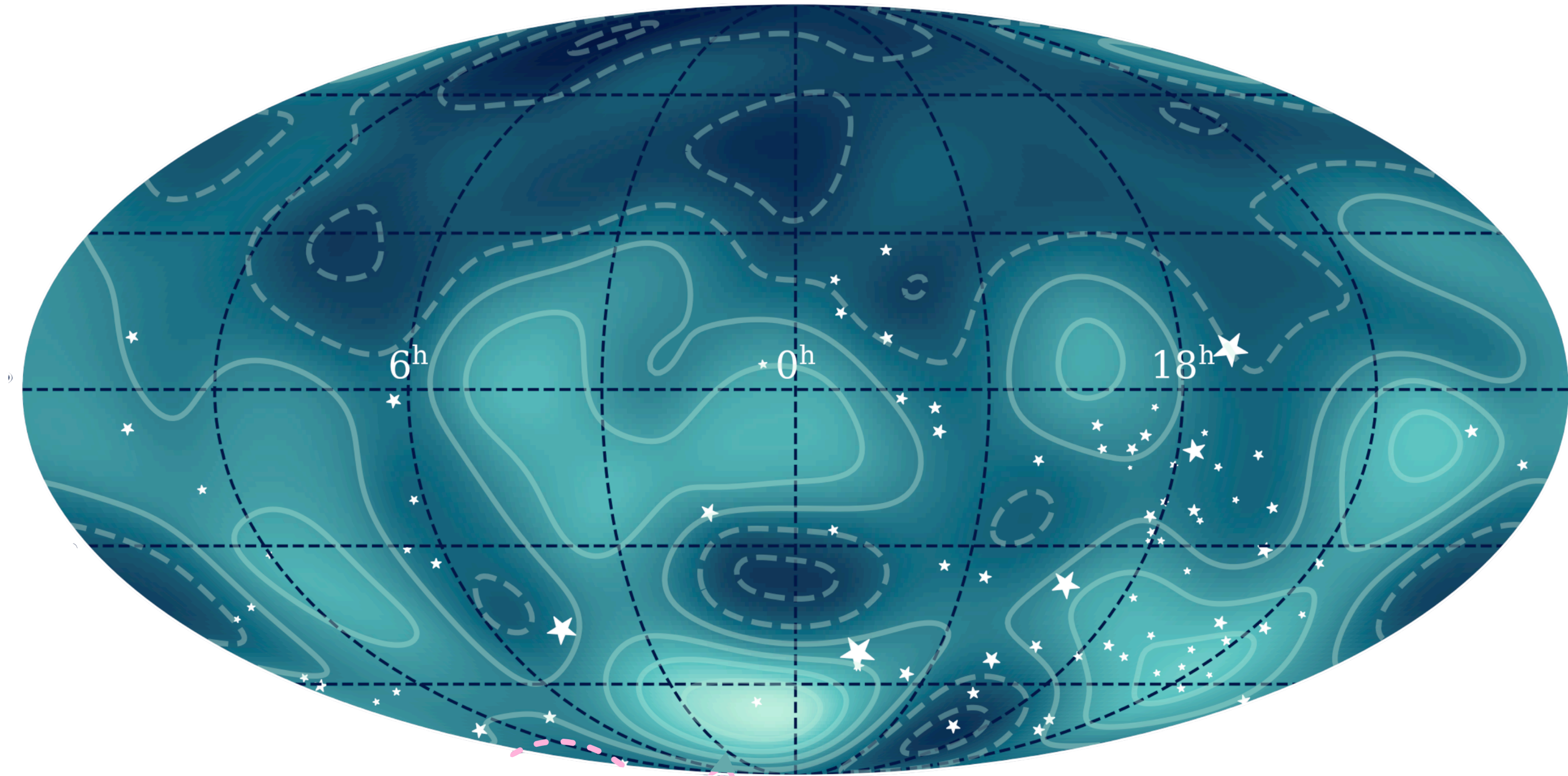
NANOGrav
Physics Frontiers Center

INITIAL DISCLAIMER



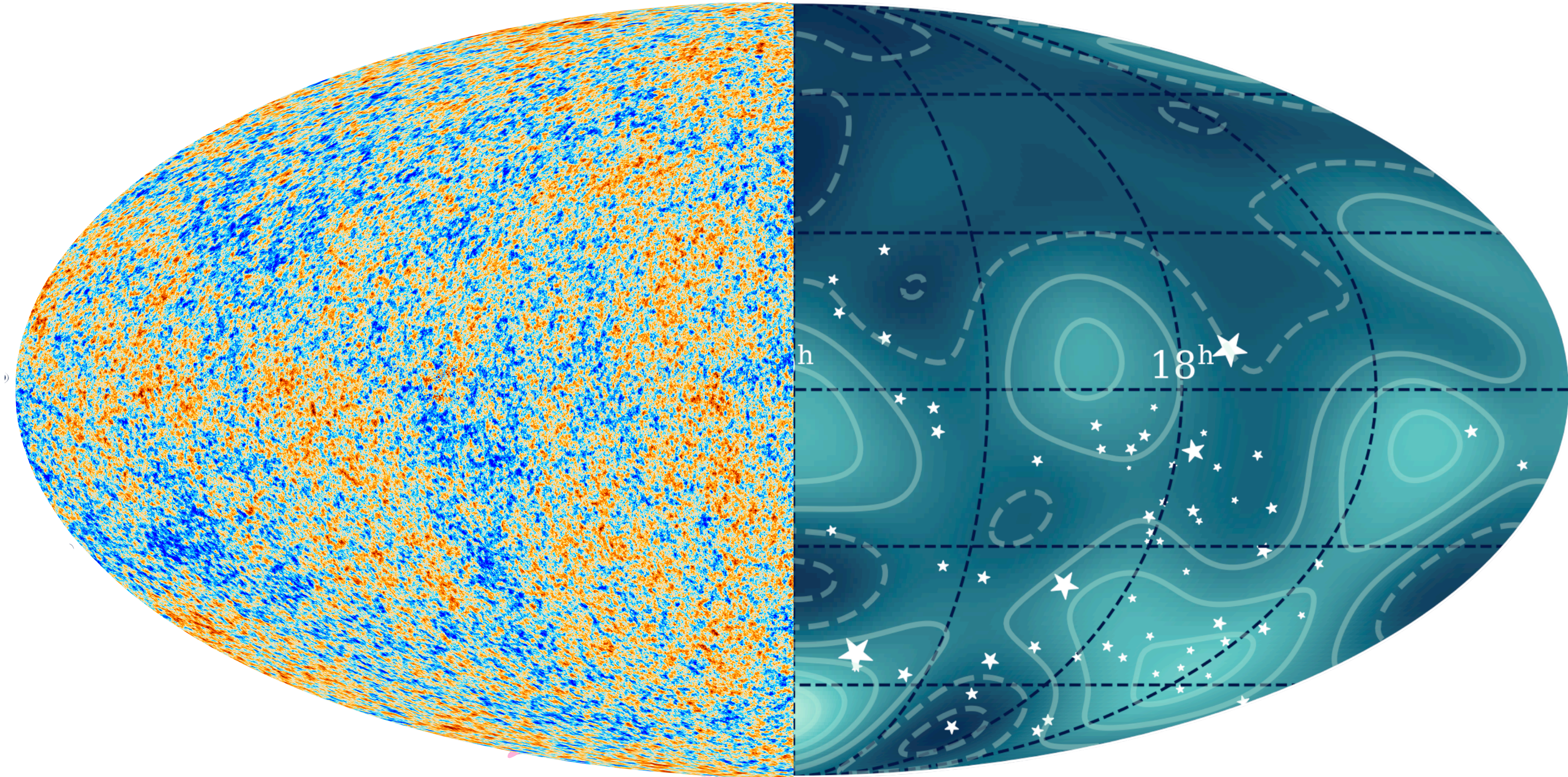
localized and **transient** events

INITIAL DISCLAIMER



persistent and **all-sky**

INITIAL DISCLAIMER



persistent and **all-sky**

PULSARS

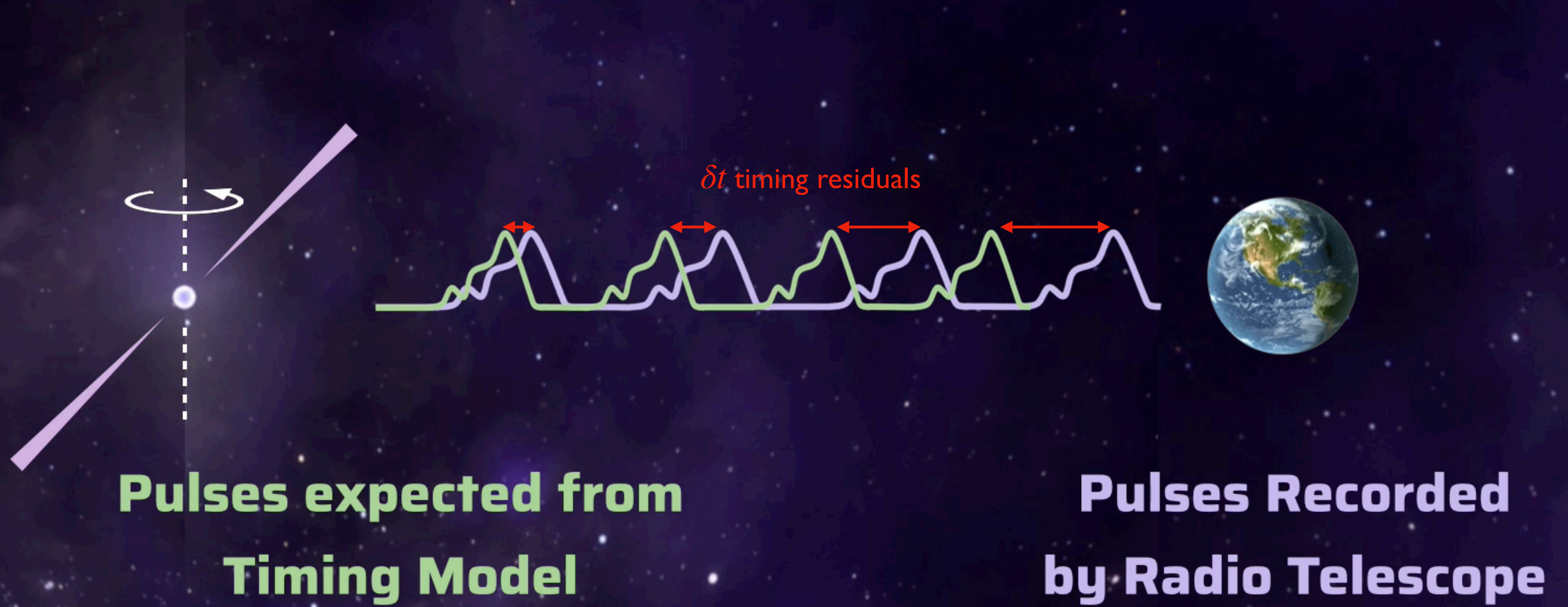
**Rotation
Axis**



**Magnetic
Field Axis**

Radiation Beams

TIMING RESIDUALS





A GALAXY-SIZE DETECTOR FOR GW_s

A GALAXY-SIZE DETECTOR FOR GWs

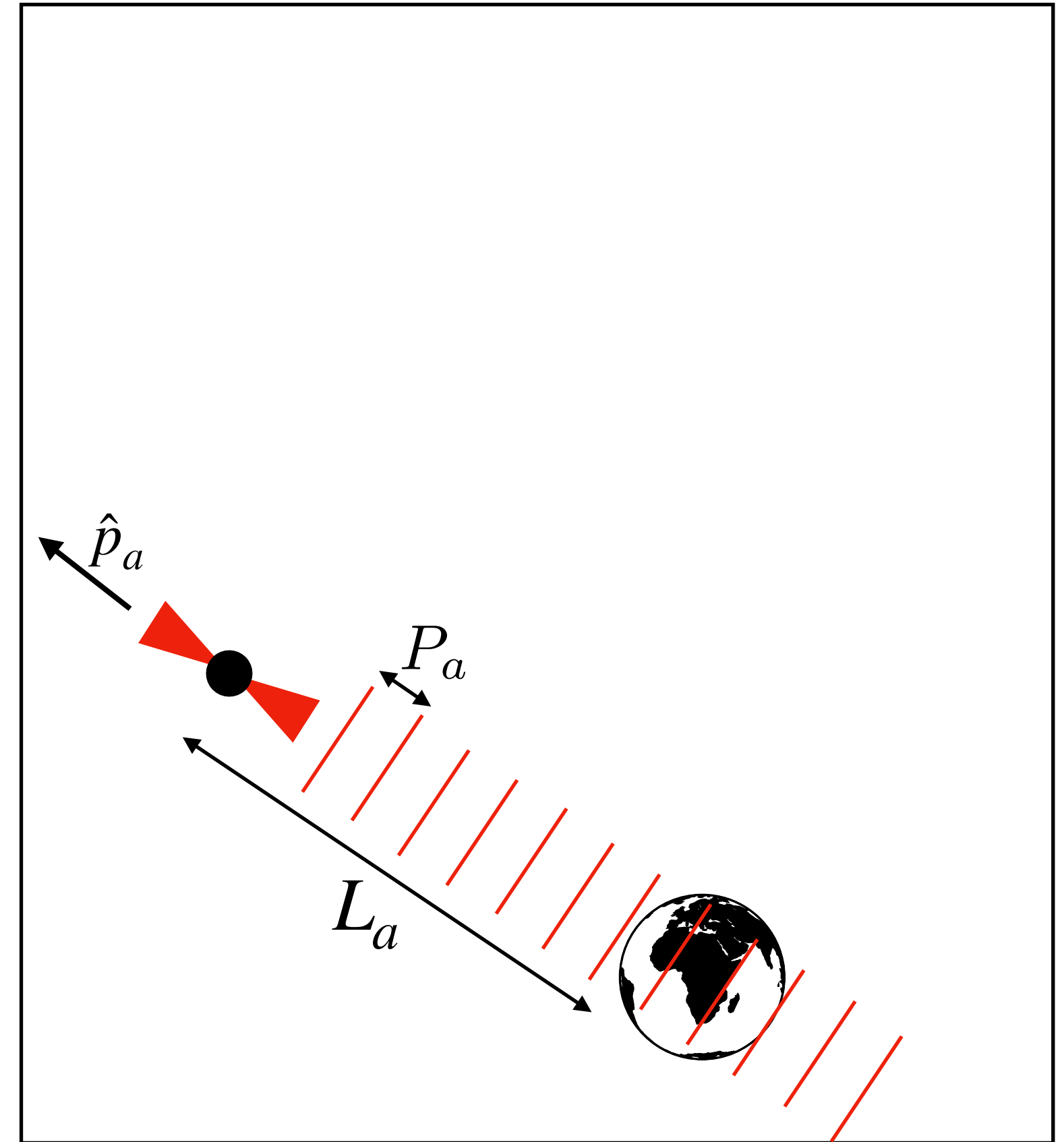
68 pulsars observed
by NG

observing
baseline of 15 yrs

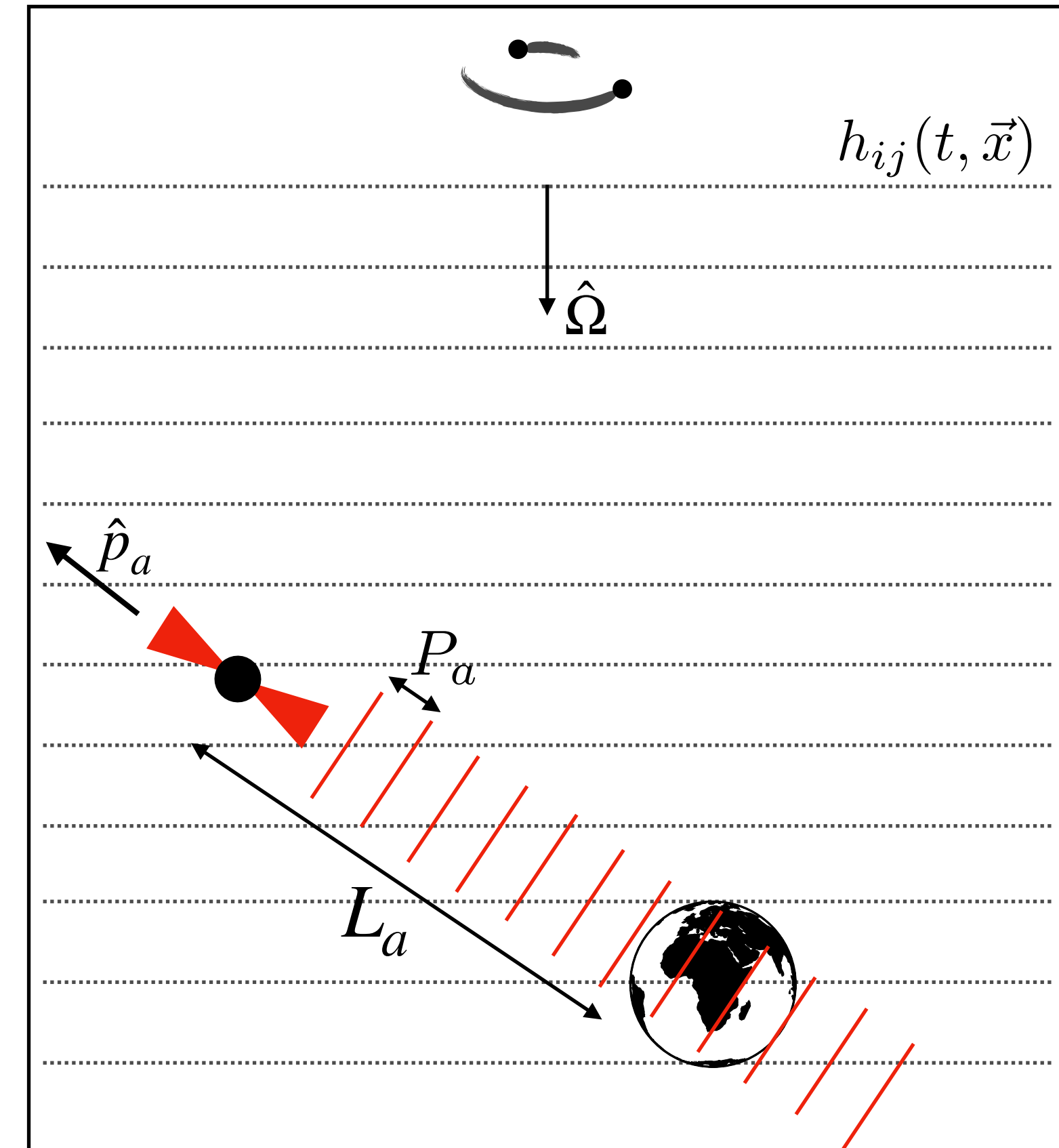
distance to pulsars up
to ~kpc

IPTA DR3 will contain
>100 pulsars

GW SIGNALS

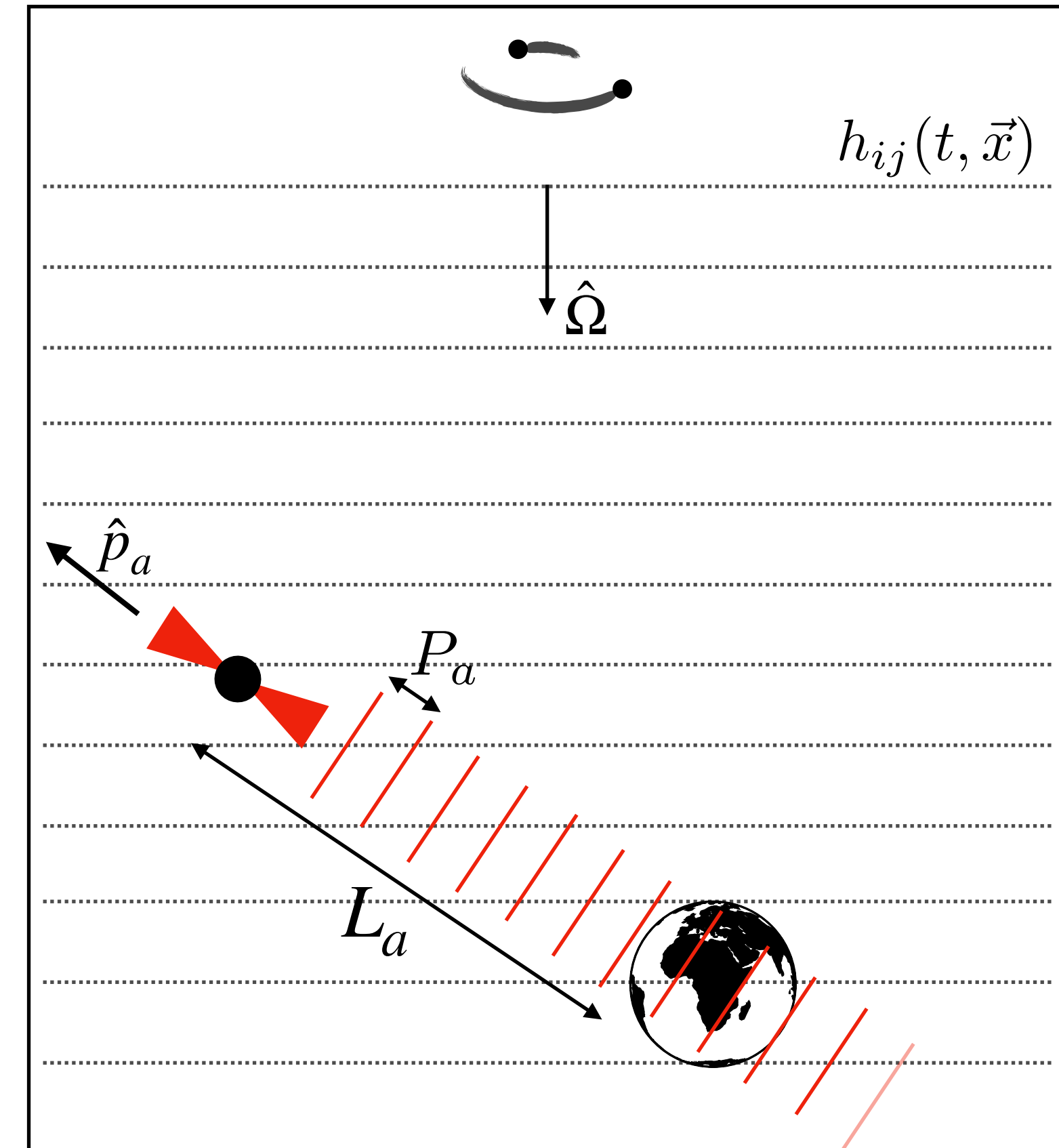


GW SIGNALS



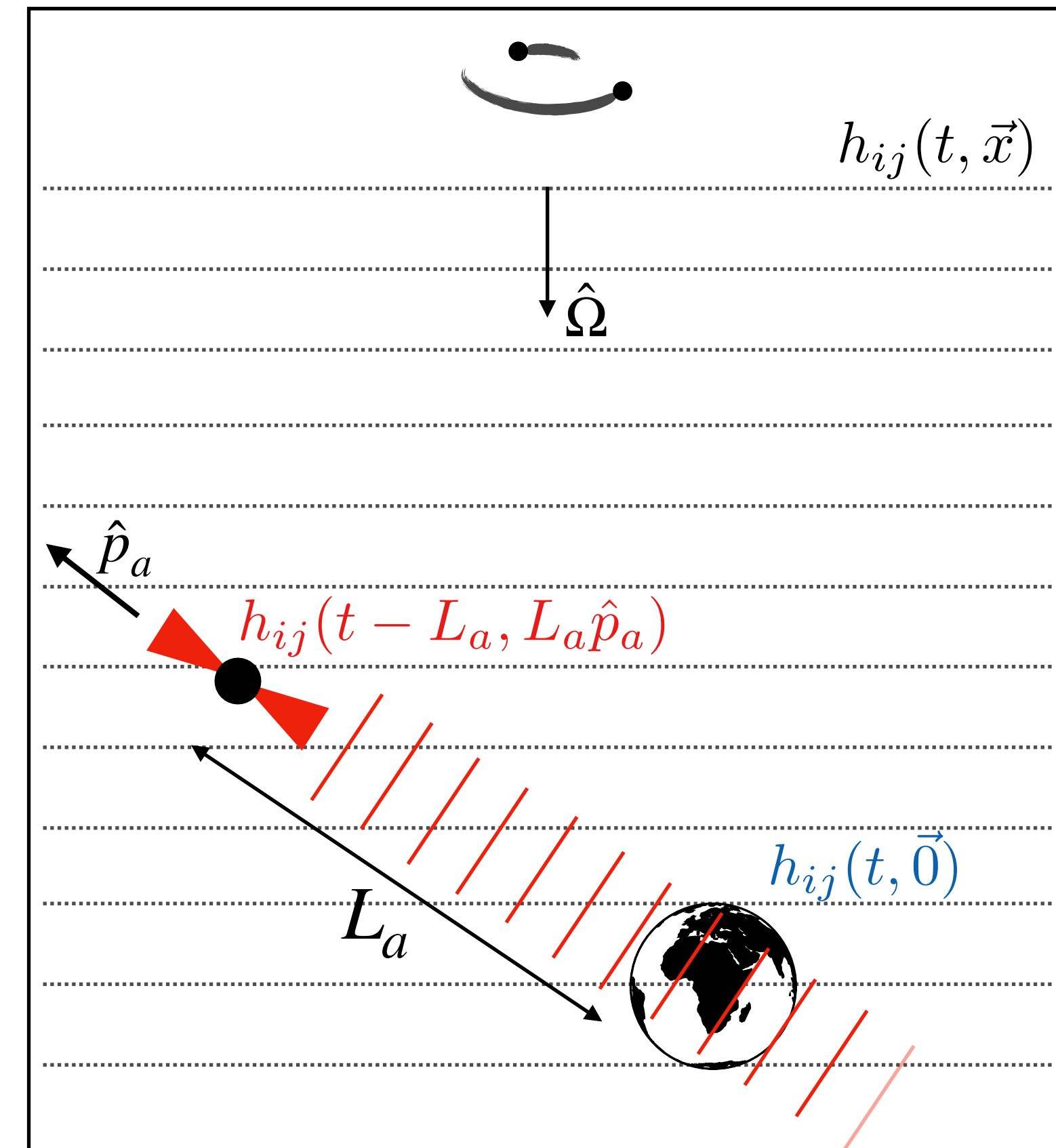
GW SIGNALS

$$\frac{\delta P_a(t)}{P_a} = \frac{\hat{p}_a^i \hat{p}_a^j}{2(1 + \hat{\Omega} \cdot \hat{p}_a)} \left[h_{ij}(t, \vec{0}) - h_{ij}(t - L_a, L_a \hat{p}_a) \right]$$



GW SIGNALS

$$\frac{\delta P_a(t)}{P_a} = \frac{\hat{p}_a^i \hat{p}_a^j}{2(1 + \hat{\Omega} \cdot \hat{p}_a)} \left[\underbrace{h_{ij}(t, \vec{0})}_{\text{Earth term}} - \underbrace{h_{ij}(t - L_a, L_a \hat{p}_a)}_{\text{pulsar term}} \right]$$



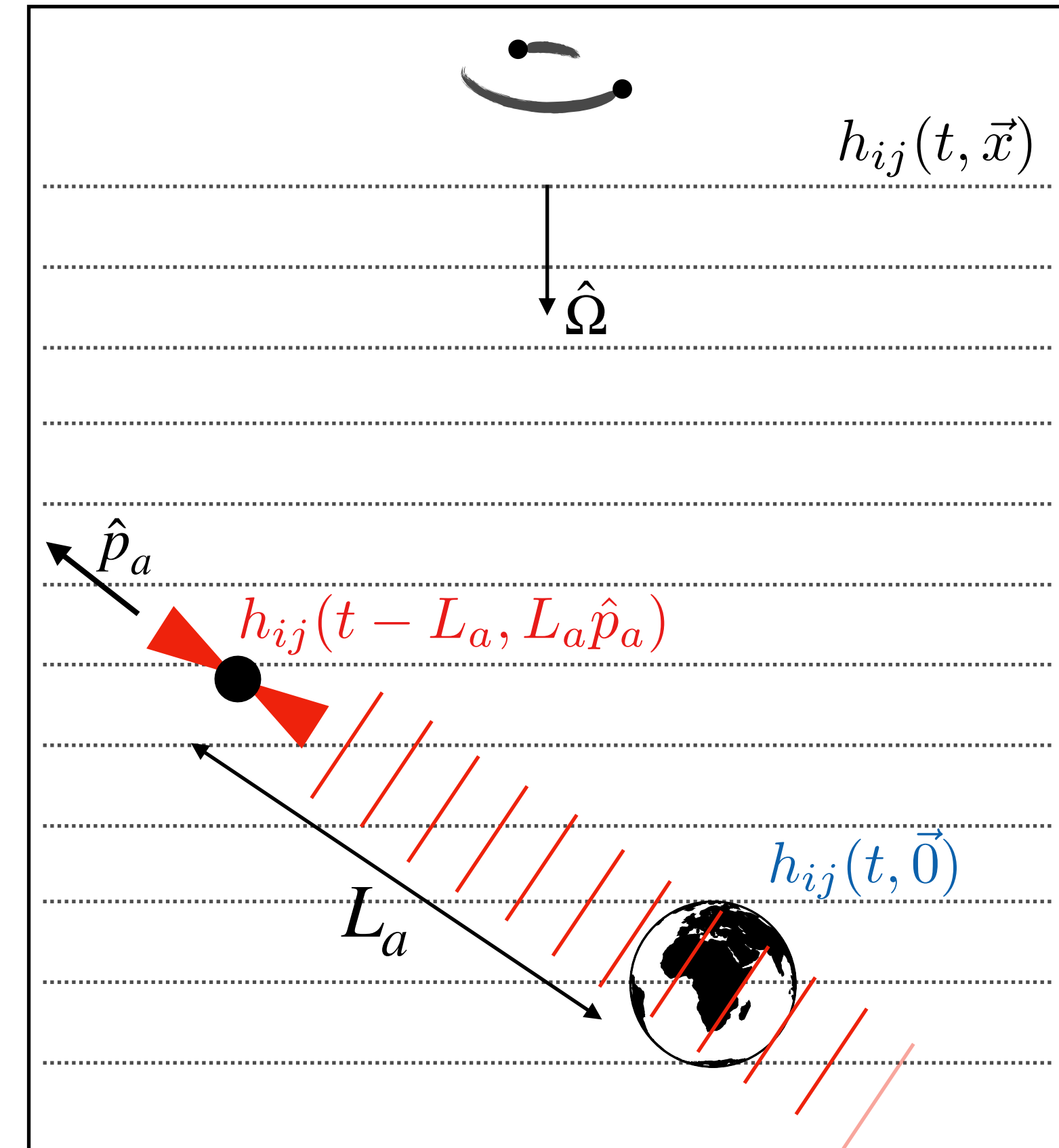
GW SIGNALS

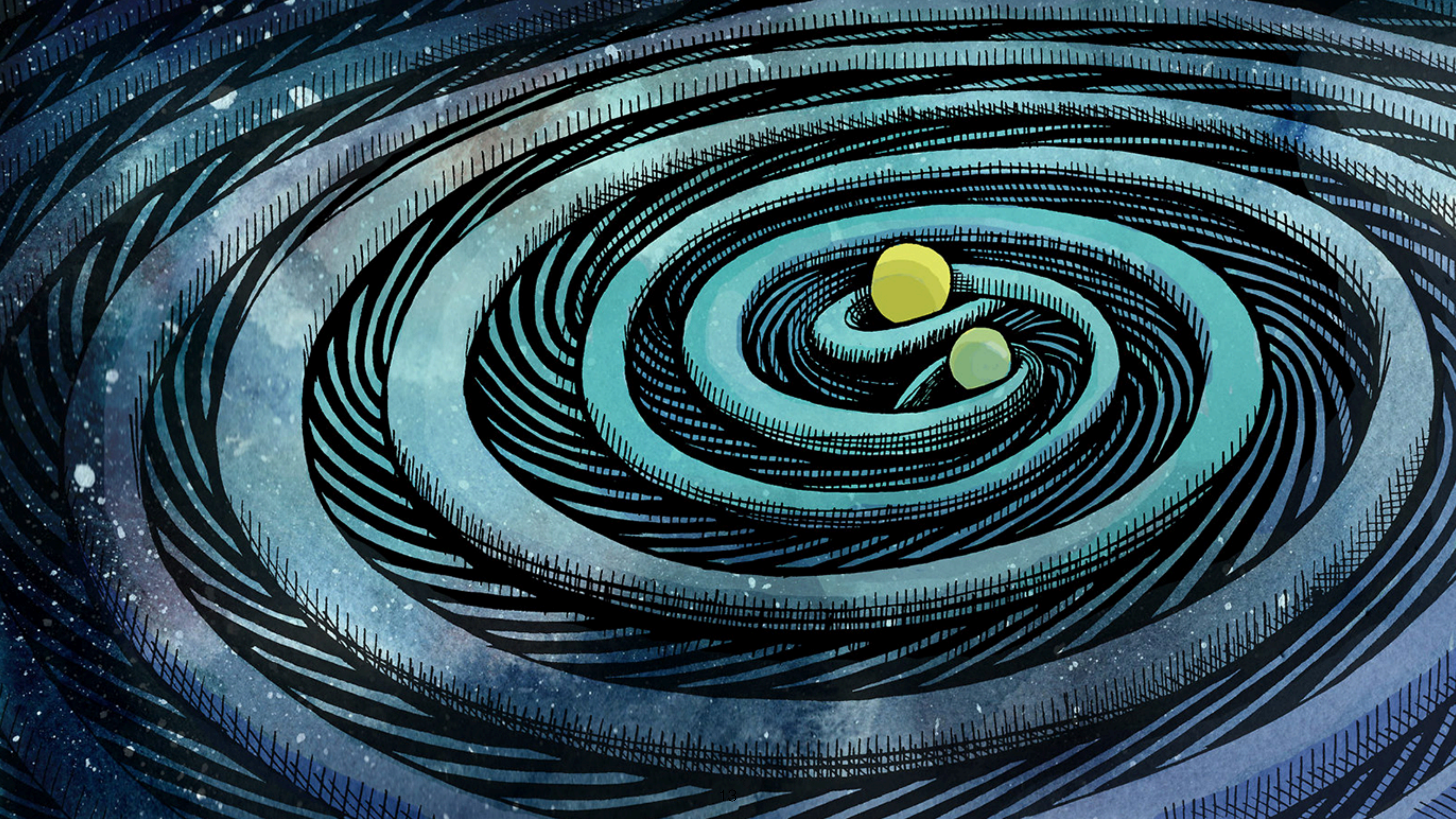
$$\frac{\delta P_a(t)}{P_a} = \frac{\hat{p}_a^i \hat{p}_a^j}{2(1 + \hat{\Omega} \cdot \hat{p}_a)} \left[h_{ij}(t, \vec{0}) - h_{ij}(t - L_a, L_a \hat{p}_a) \right]$$

Earth term

pulsar term

geometric response





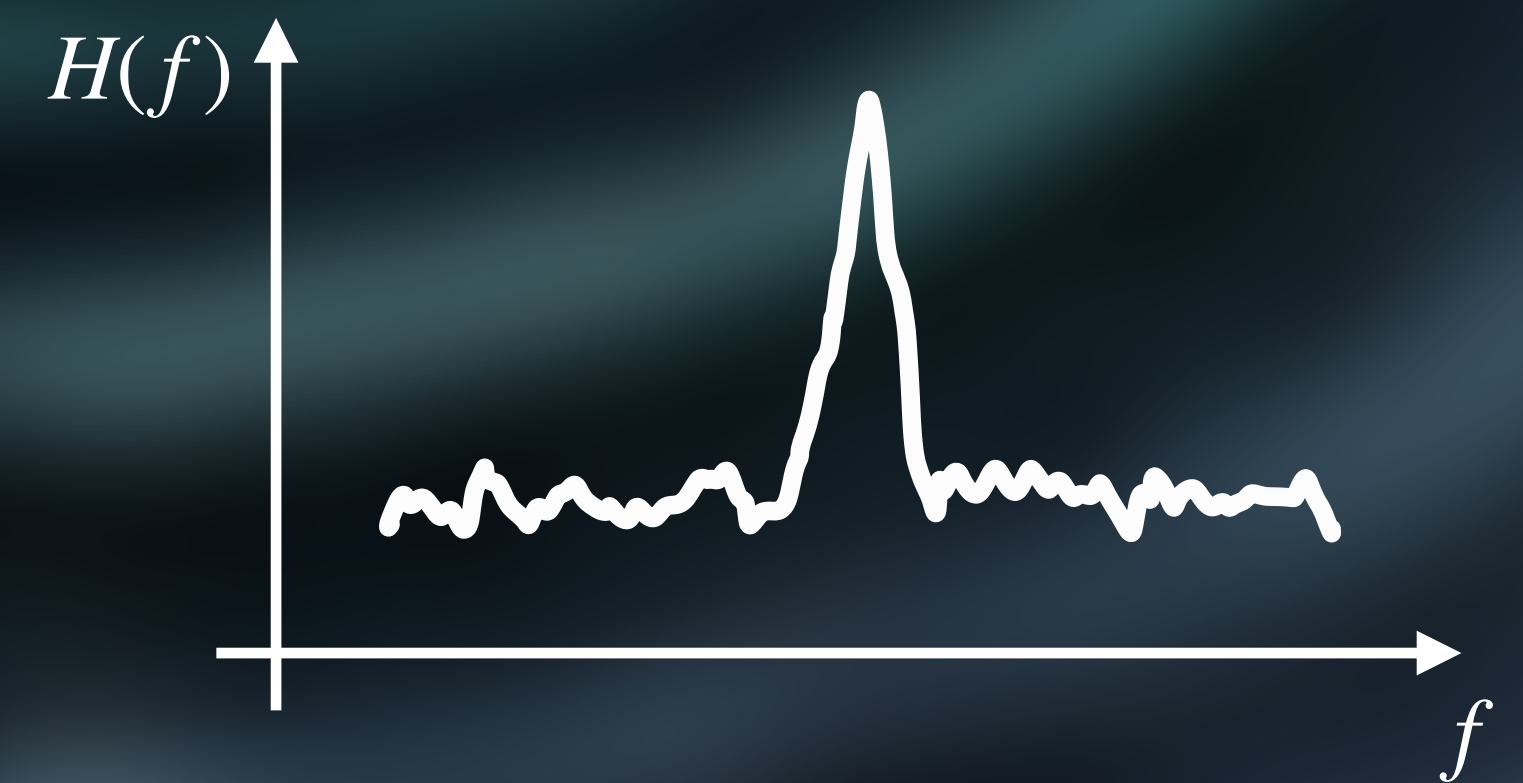
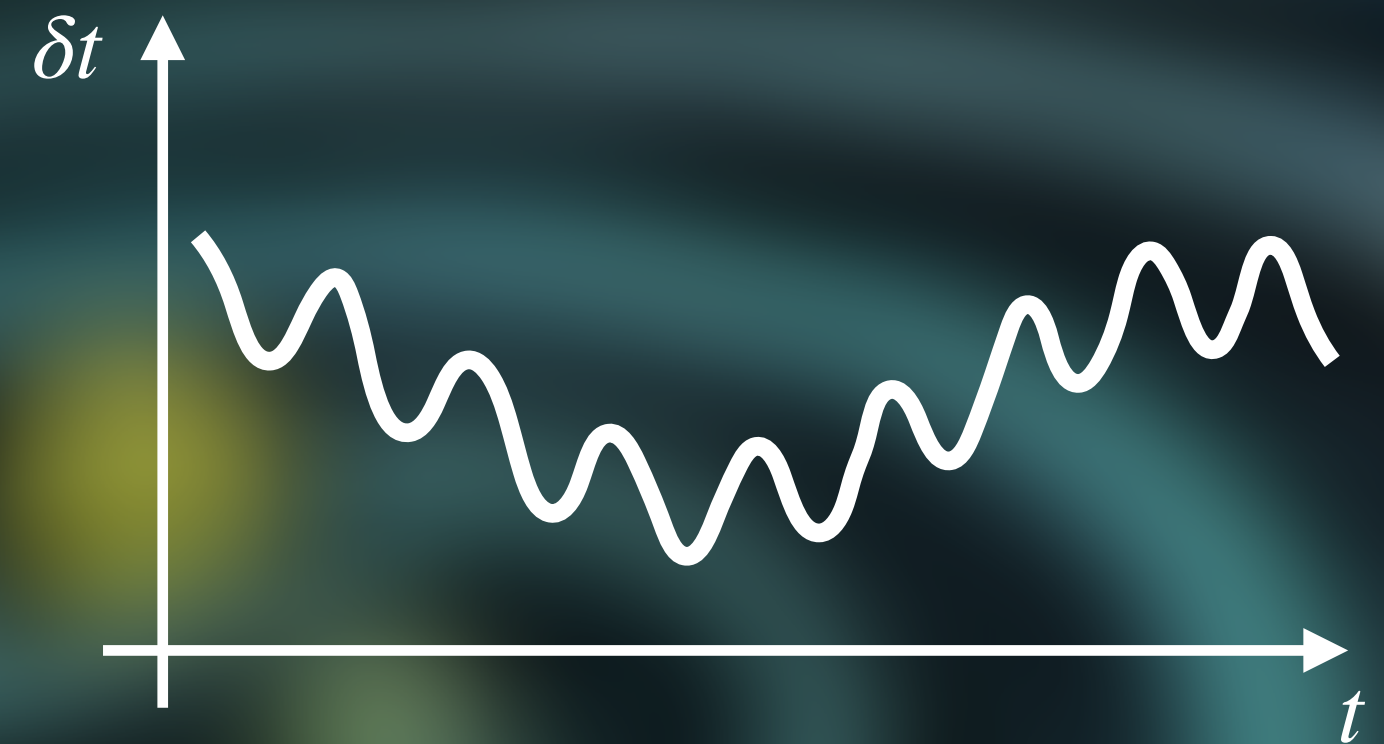
CONTINUOUS WAVE

$$h_{ij}(t, \vec{x}) \sim h_0 \sin \left[\omega \left(t - \hat{\Omega} \cdot \vec{x} \right) \right] e_{ij}(\hat{\Omega})$$



CONTINUOUS WAVE

$$h_{ij}(t, \vec{x}) \sim h_0 \sin \left[\omega \left(t - \hat{\Omega} \cdot \vec{x} \right) \right] e_{ij}(\hat{\Omega})$$





GW BACKGROUND

$$h_{ij}(t, \vec{x}) = \sum_A \int df \int d\hat{\Omega} \tilde{h}_A(f, \hat{\Omega}) e_{ij}^A(\hat{\Omega}) e^{-2\pi i f(t - \hat{\Omega} \cdot \vec{x})}$$

GW BACKGROUND

$$h_{ij}(t, \vec{x}) = \sum_A \int df \int d\hat{\Omega} \underbrace{\tilde{h}_A(f, \hat{\Omega})}_{\substack{\text{"Fourier" components} \\ \text{treated as random variables}}} \underbrace{e_{ij}^A(\hat{\Omega})}_{\text{polarization tensors}} \underbrace{e^{-2\pi i f(t - \hat{\Omega} \cdot \vec{x})}}_{\text{plane waves}}$$

GW BACKGROUND

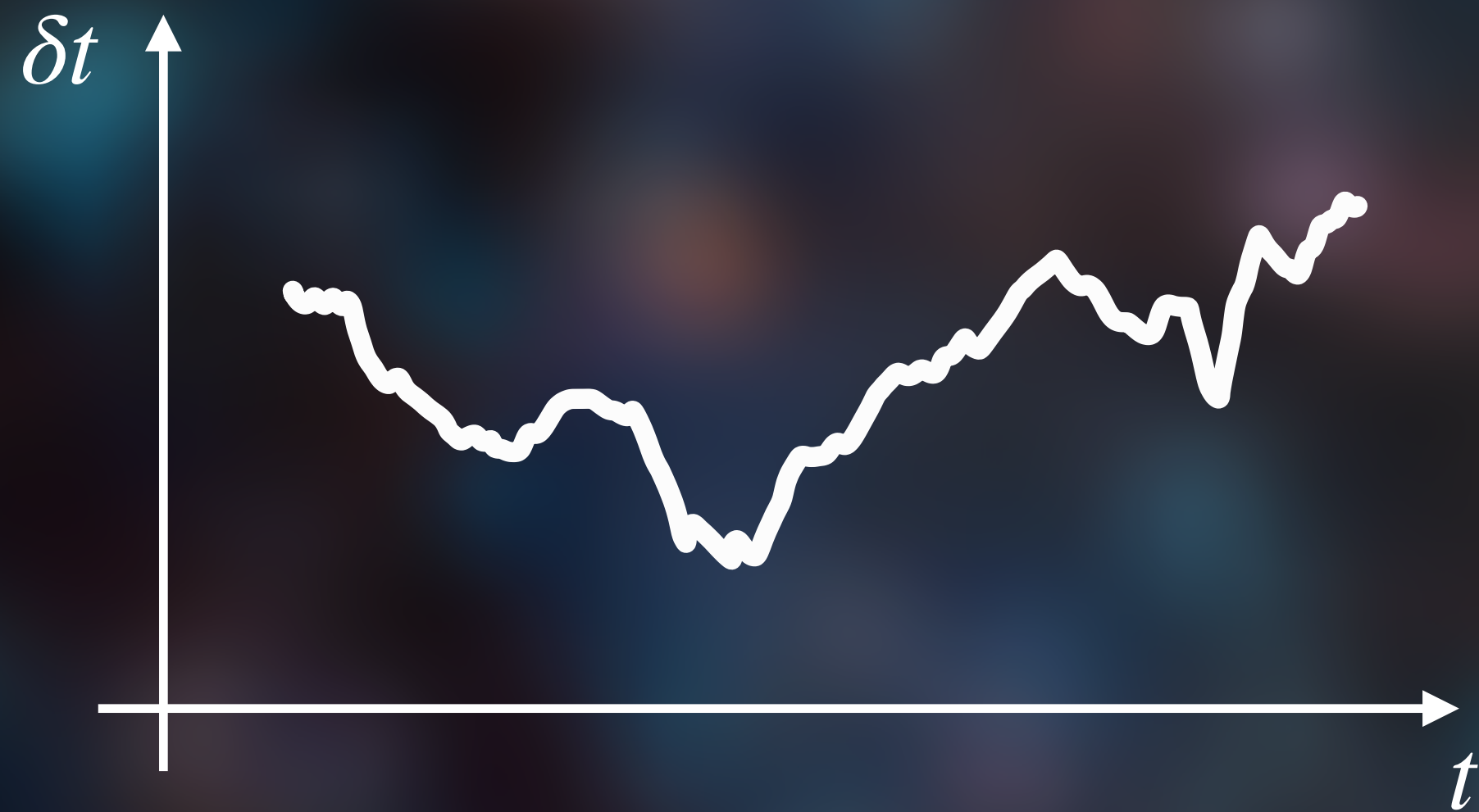
$$h_{ij}(t, \vec{x}) = \sum_A \int df \int d\hat{\Omega} \underbrace{\tilde{h}_A(f, \hat{\Omega})}_{\substack{\text{"Fourier" components} \\ \text{treated as random variables}}} \underbrace{e_{ij}^A(\hat{\Omega})}_{\text{polarization tensors}} \underbrace{e^{-2\pi i f(t - \hat{\Omega} \cdot \vec{x})}}_{\text{plane waves}}$$



$$\langle \tilde{h}_A(f, \hat{\Omega})^* \tilde{h}_A(f', \hat{\Omega}') \rangle \propto \delta(f - f') H(f)$$

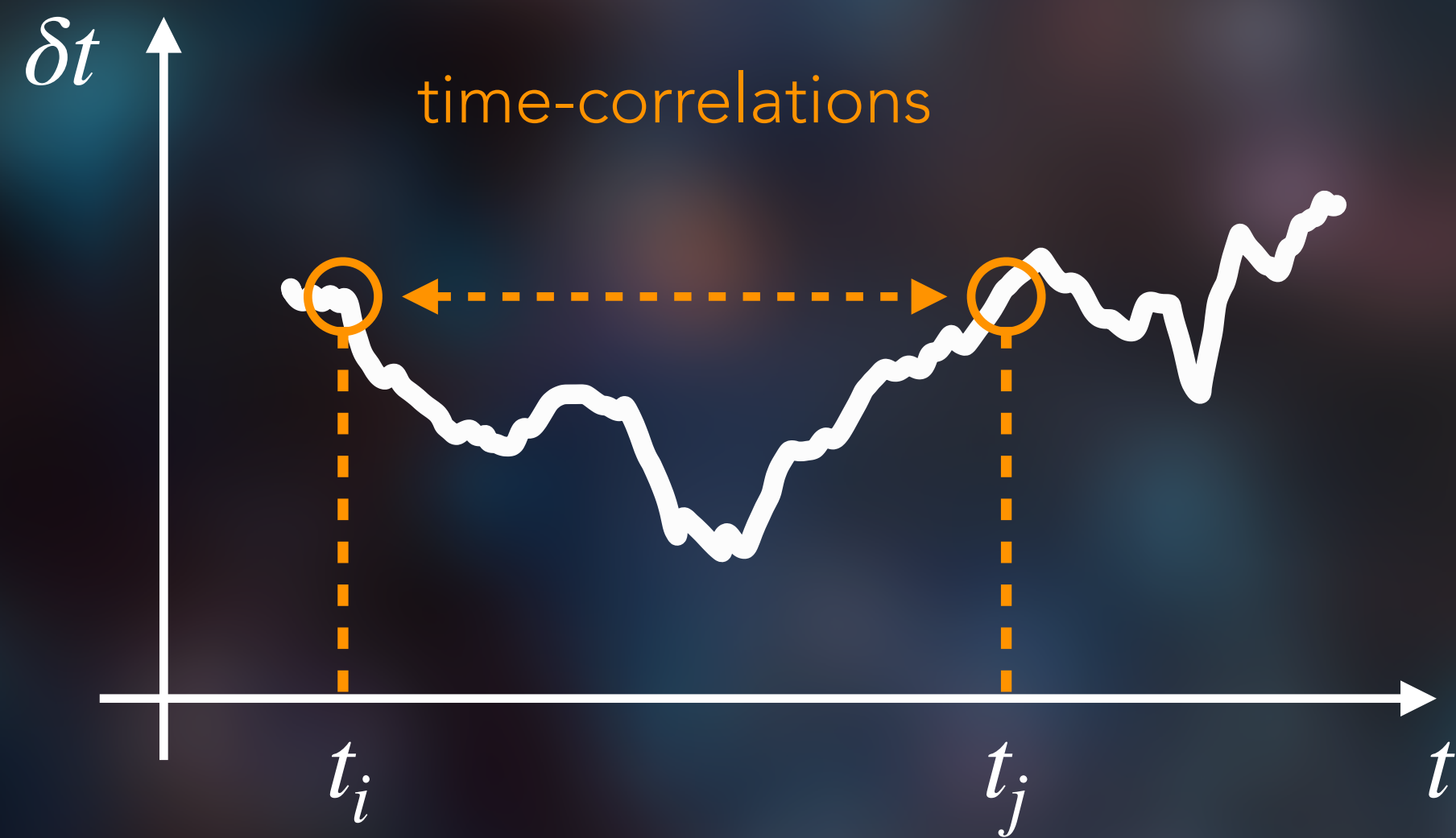
GW BACKGROUND

$$h_{ij}(t, \vec{x}) = \sum_A \int df \int d\hat{\Omega} \tilde{h}_A(f, \hat{\Omega}) e_{ij}^A(\hat{\Omega}) e^{-2\pi i f(t - \hat{\Omega} \cdot \vec{x})}$$



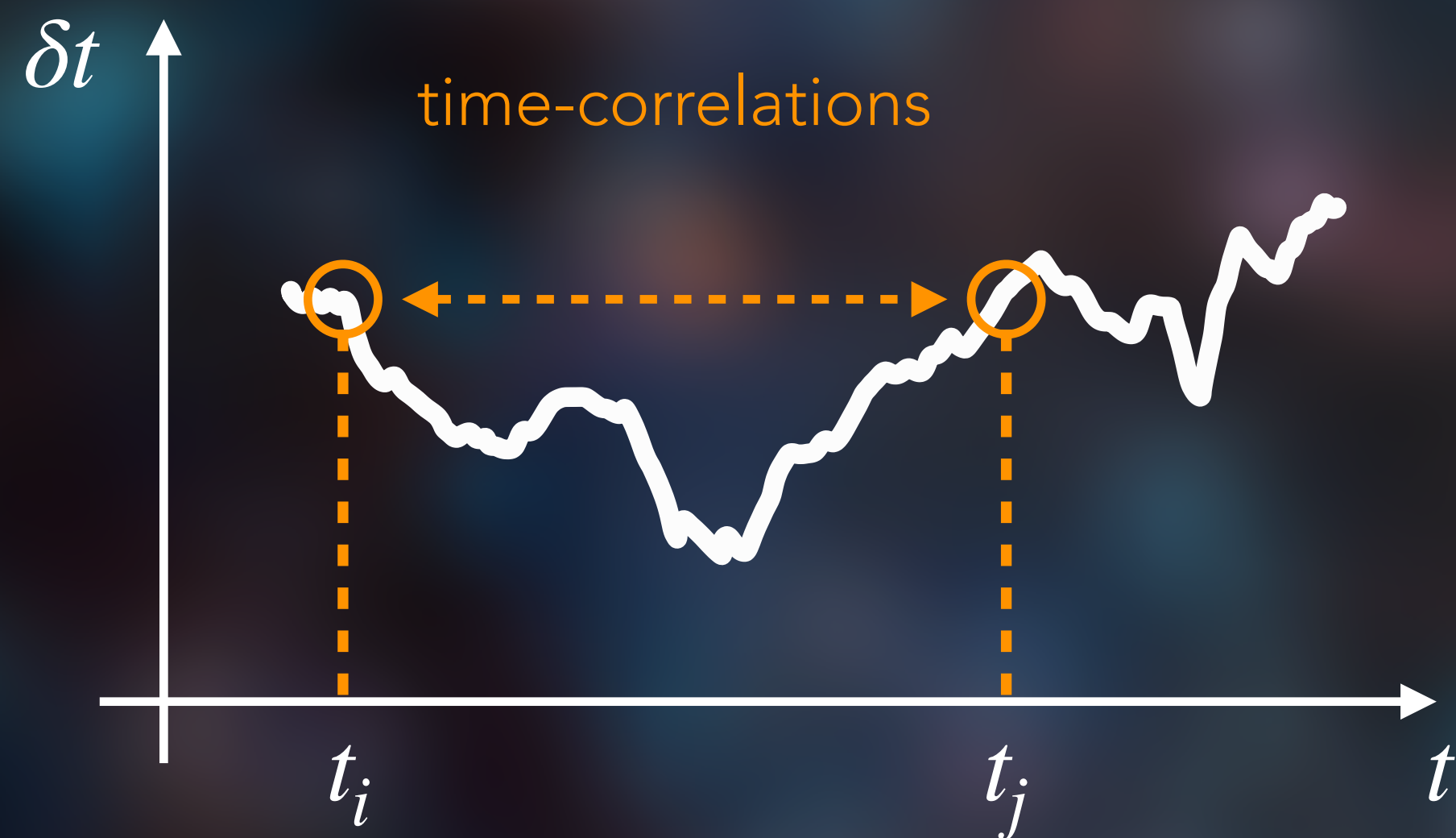
GW BACKGROUND

$$h_{ij}(t, \vec{x}) = \sum_A \int df \int d\hat{\Omega} \tilde{h}_A(f, \hat{\Omega}) e_{ij}^A(\hat{\Omega}) e^{-2\pi i f(t - \hat{\Omega} \cdot \vec{x})}$$



GW BACKGROUND

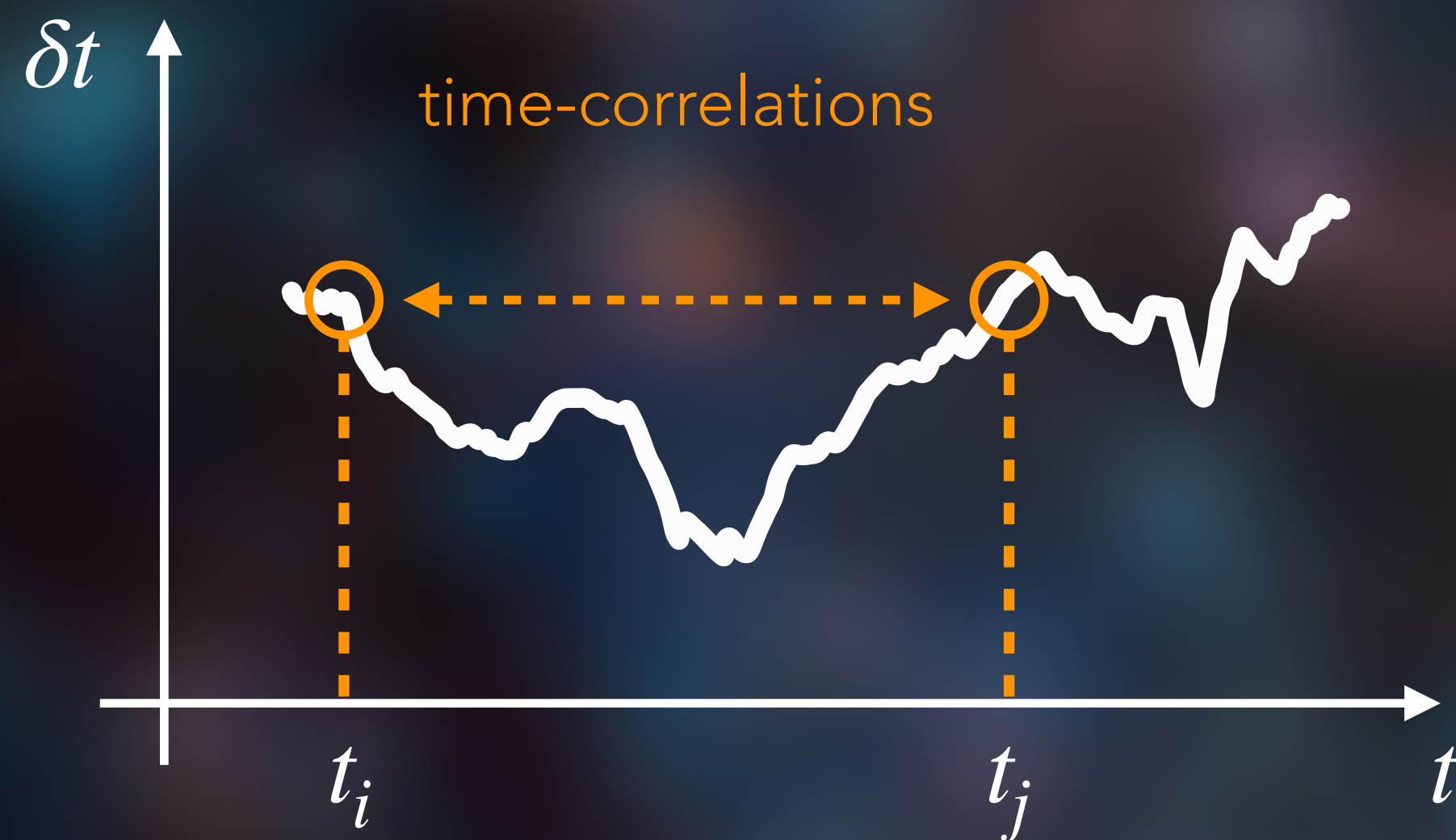
$$h_{ij}(t, \vec{x}) = \sum_A \int df \int d\hat{\Omega} \tilde{h}_A(f, \hat{\Omega}) e_{ij}^A(\hat{\Omega}) e^{-2\pi i f(t - \hat{\Omega} \cdot \vec{x})}$$



$$\langle \delta t(t_i) \delta t(t_j) \rangle$$

GW BACKGROUND

$$h_{ij}(t, \vec{x}) = \sum_A \int df \int d\hat{\Omega} \tilde{h}_A(f, \hat{\Omega}) e_{ij}^A(\hat{\Omega}) e^{-2\pi i f(t - \hat{\Omega} \cdot \vec{x})}$$



GWB power spectrum

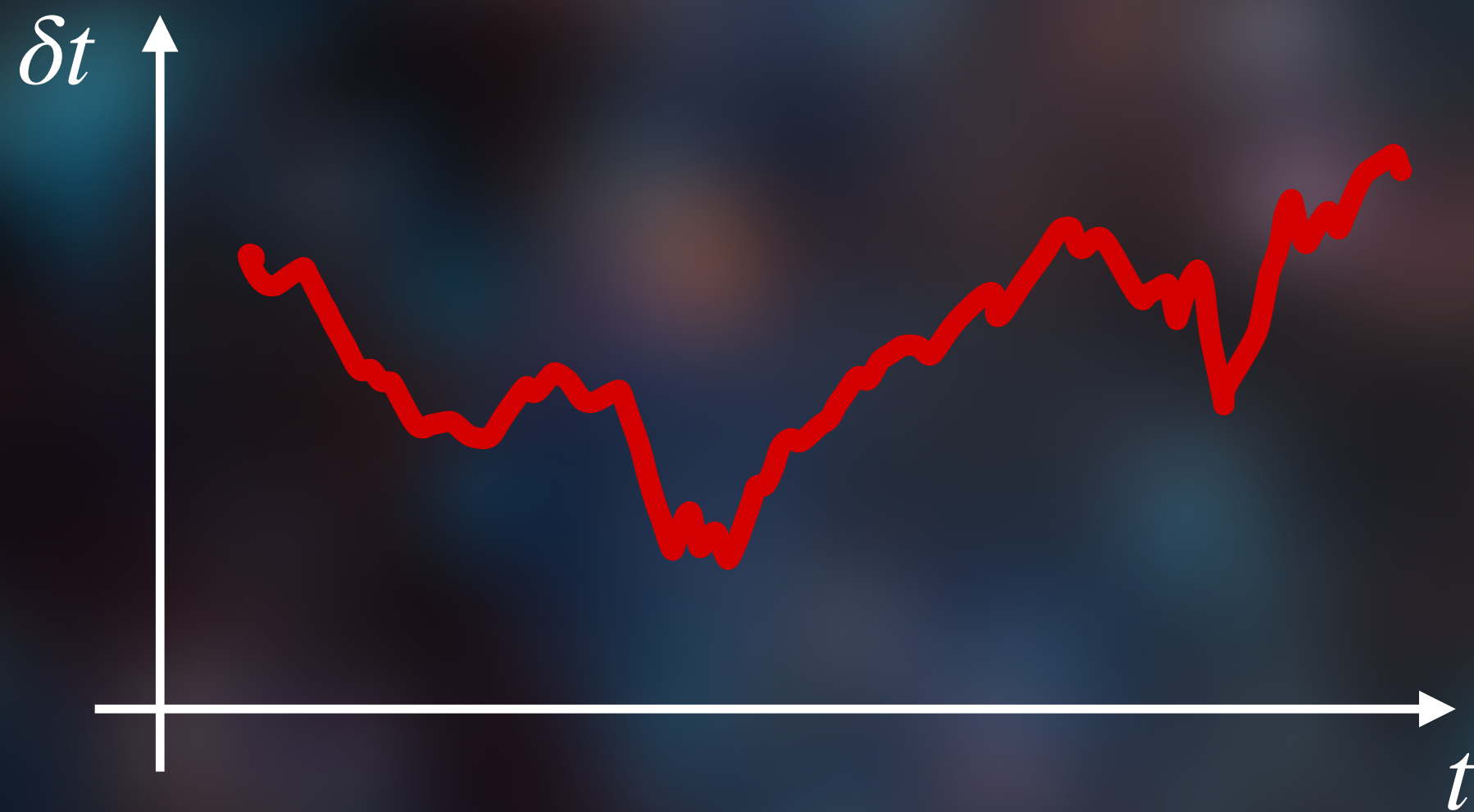
$$\langle \delta t(t_i) \delta t(t_j) \rangle \propto \int df \boxed{H(f)} e^{2\pi i f(t_i - t_j)}$$

$$\langle \tilde{h}_A(f, \hat{\Omega})^* \tilde{h}_A(f', \hat{\Omega}') \rangle \propto \delta(f - f') H(f)$$

time-correlations of the signal are controlled by the
GWB power spectrum

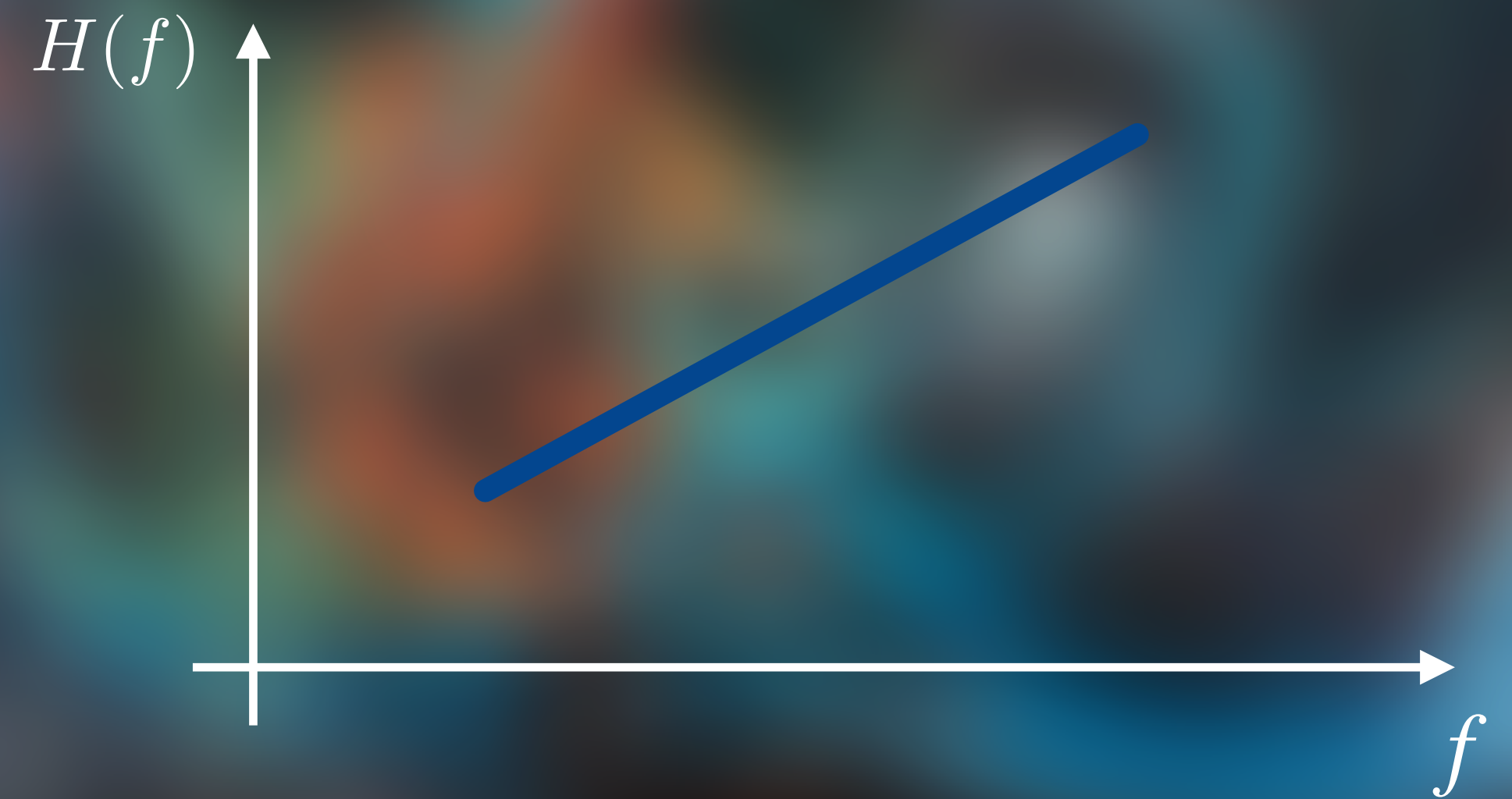
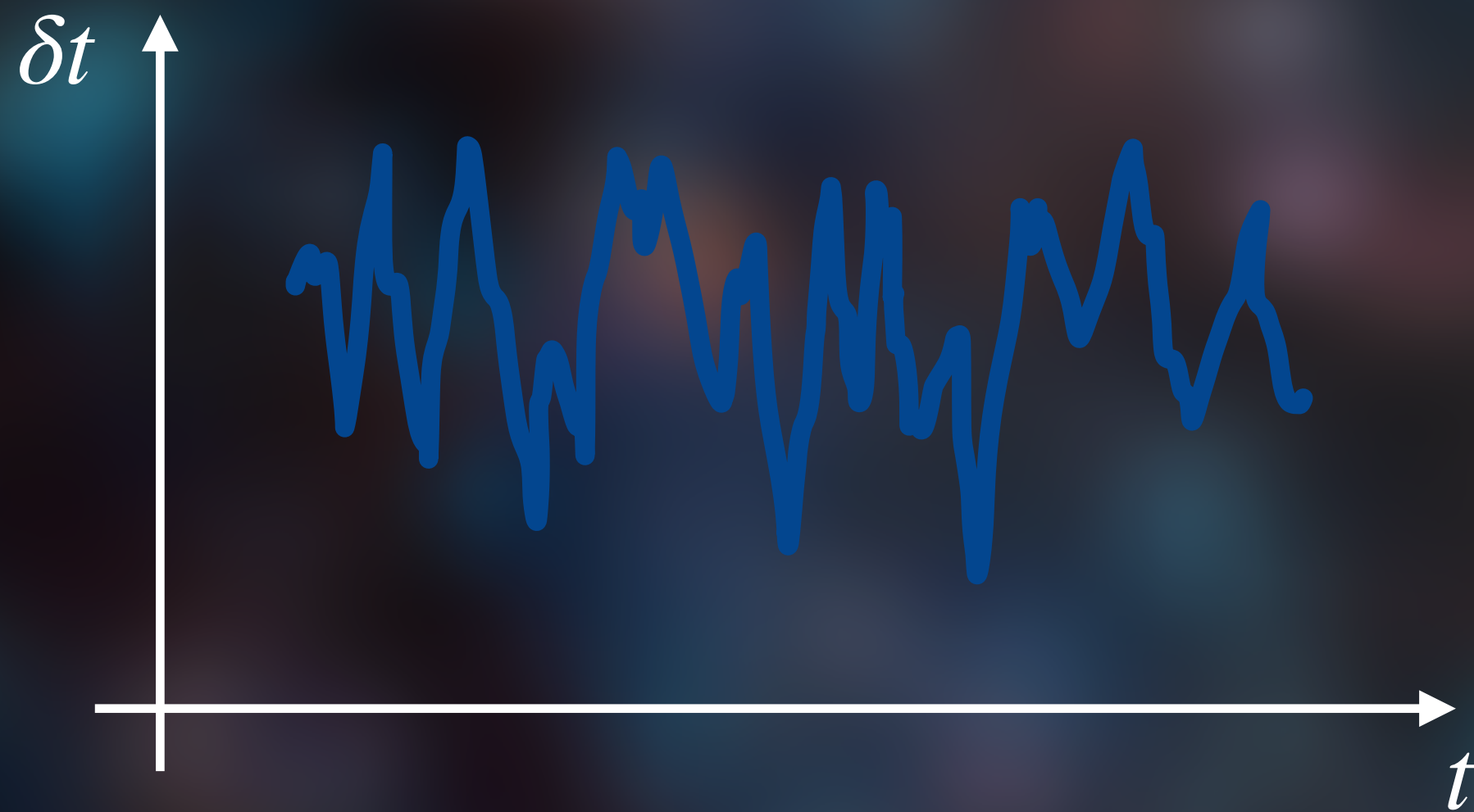
GW BACKGROUND

$$h_{ij}(t, \vec{x}) = \sum_A \int df \int d\hat{\Omega} \tilde{h}_A(f, \hat{\Omega}) e_{ij}^A(\hat{\Omega}) e^{-2\pi i f(t - \hat{\Omega} \cdot \vec{x})}$$



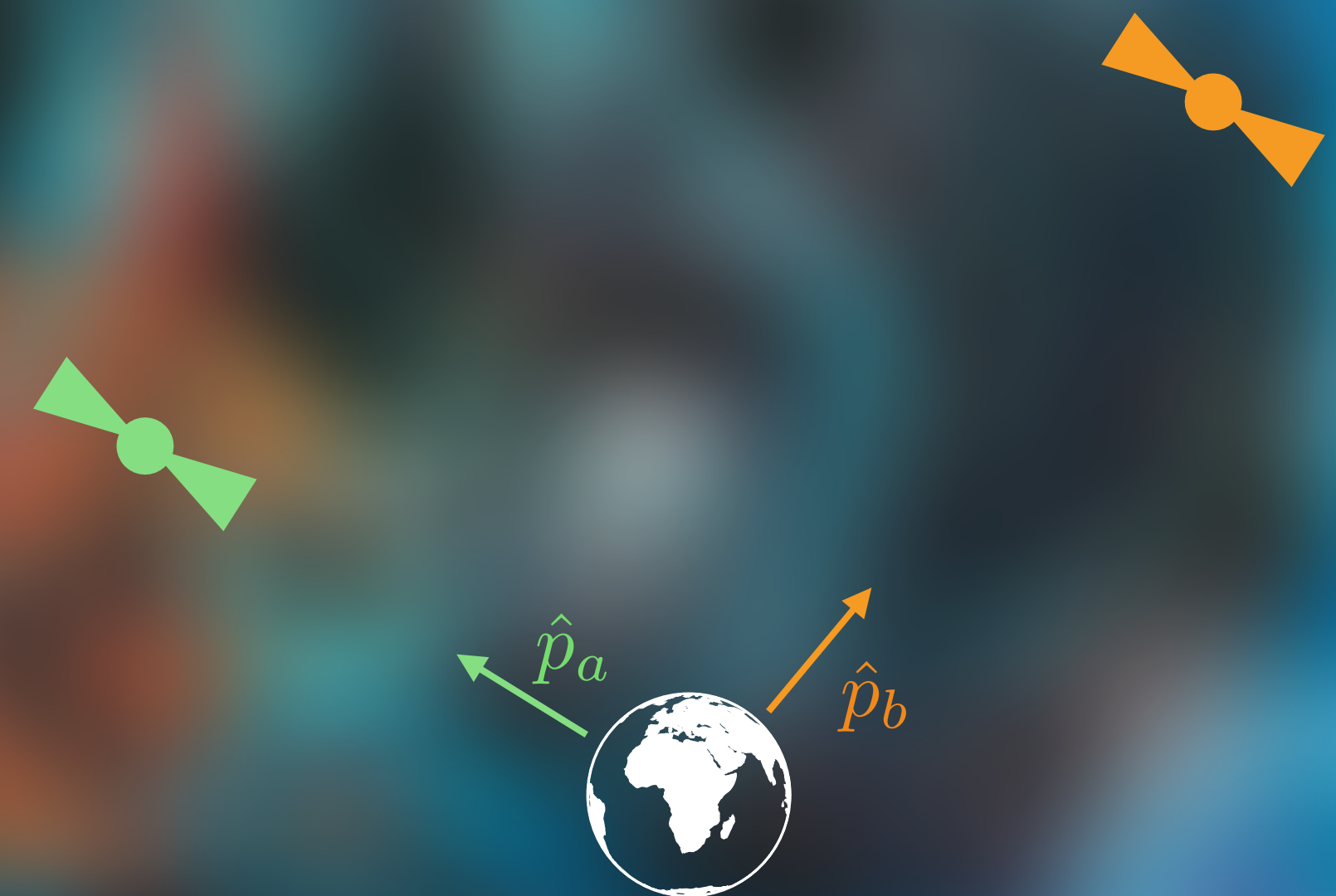
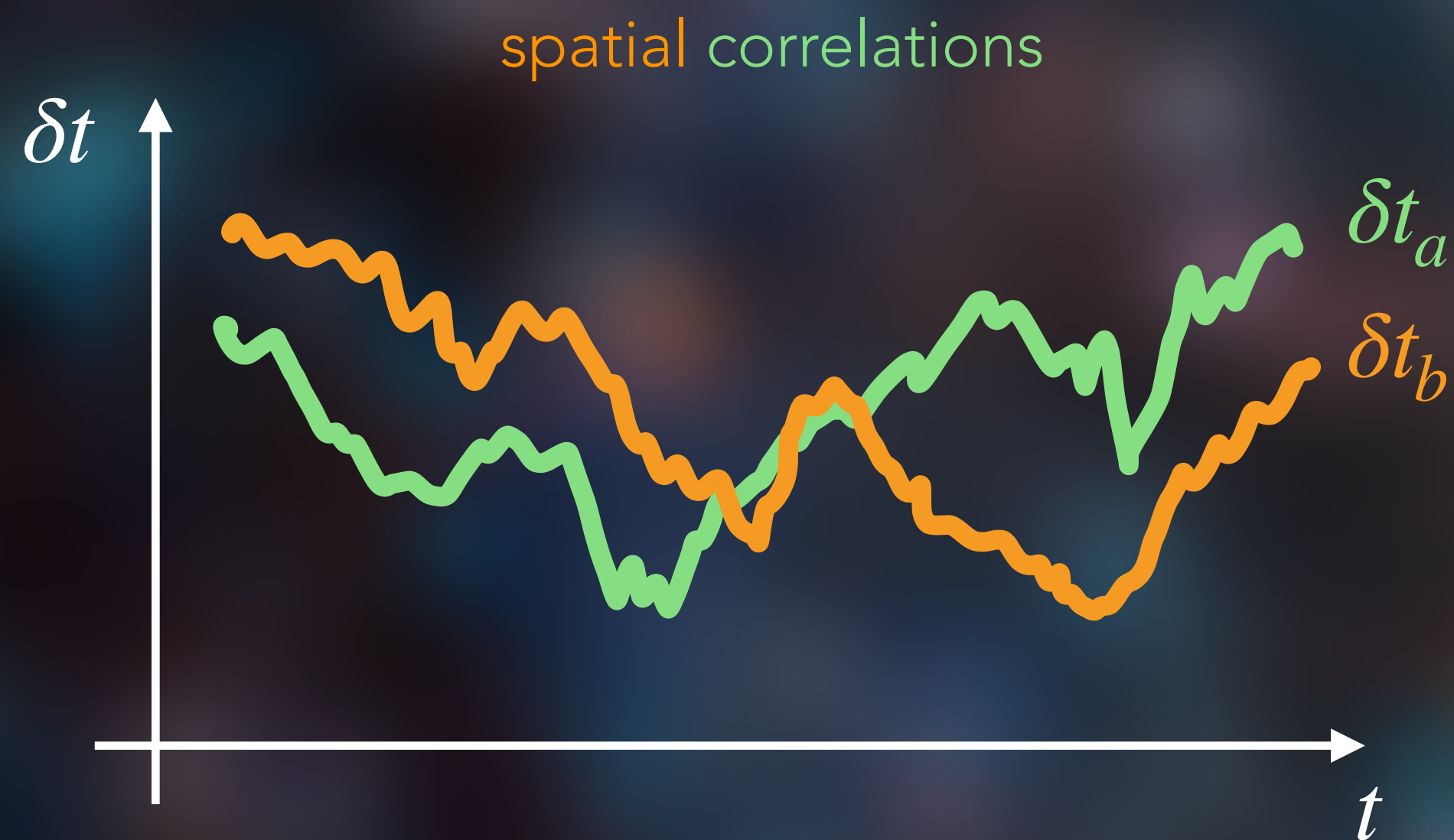
GW BACKGROUND

$$h_{ij}(t, \vec{x}) = \sum_A \int df \int d\hat{\Omega} \tilde{h}_A(f, \hat{\Omega}) e_{ij}^A(\hat{\Omega}) e^{-2\pi i f(t - \hat{\Omega} \cdot \vec{x})}$$



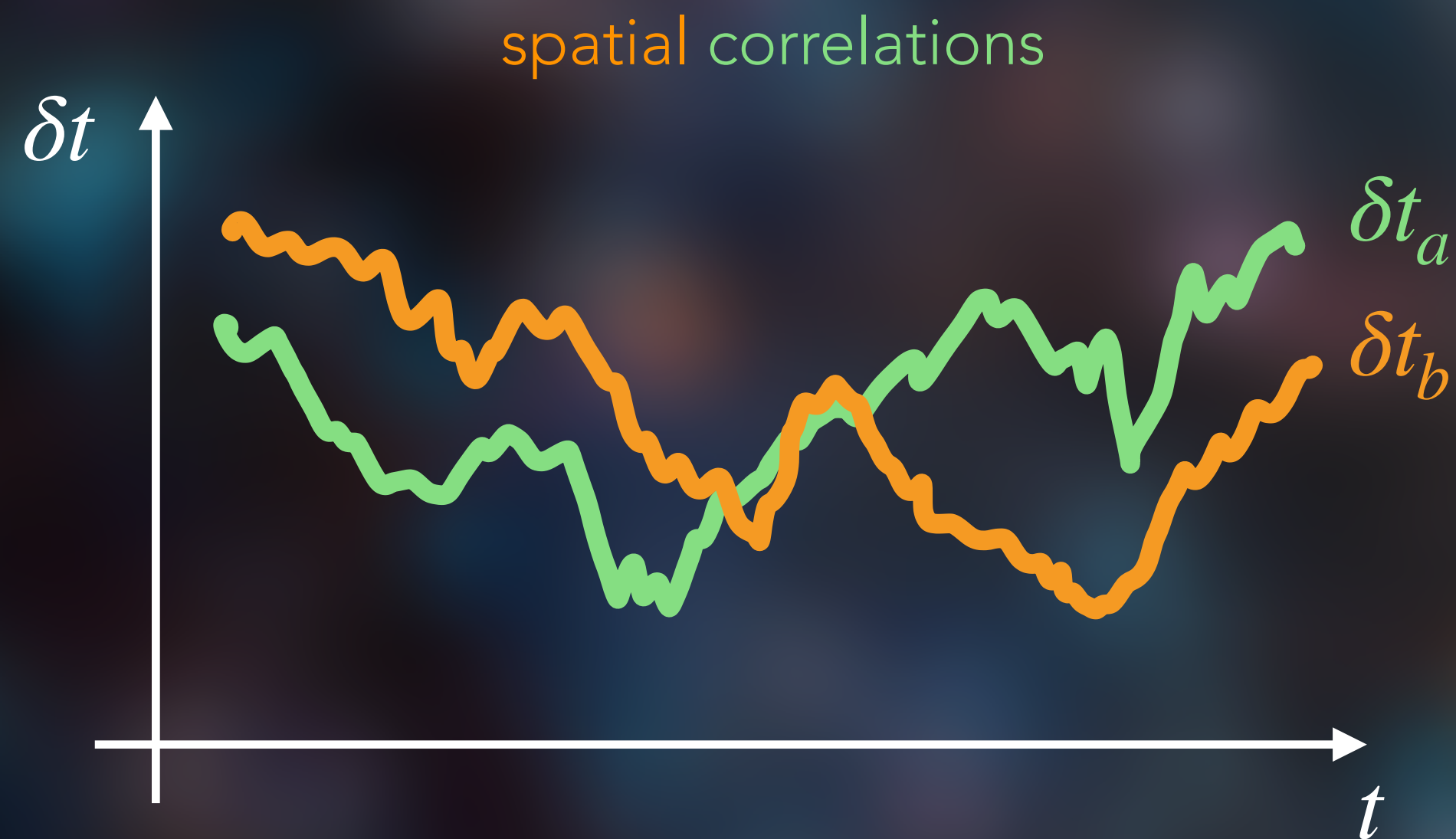
GW BACKGROUND

$$h_{ij}(t, \vec{x}) = \sum_A \int df \int d\hat{\Omega} \tilde{h}_A(f, \hat{\Omega}) e_{ij}^A(\hat{\Omega}) e^{-2\pi i f(t - \hat{\Omega} \cdot \vec{x})}$$



GW BACKGROUND

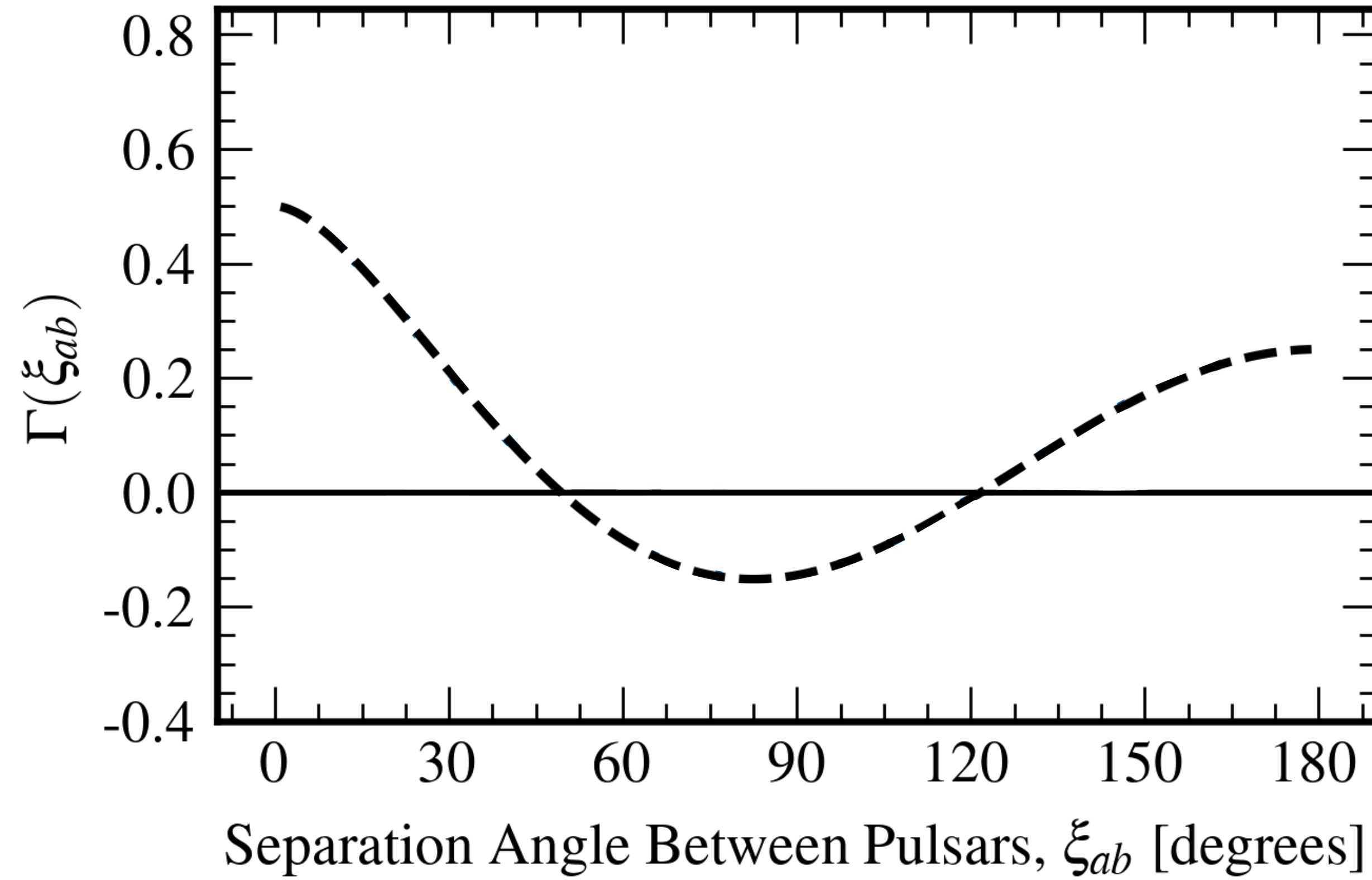
$$h_{ij}(t, \vec{x}) = \sum_A \int df \int d\hat{\Omega} \tilde{h}_A(f, \hat{\Omega}) e_{ij}^A(\hat{\Omega}) e^{-2\pi i f(t - \hat{\Omega} \cdot \vec{x})}$$



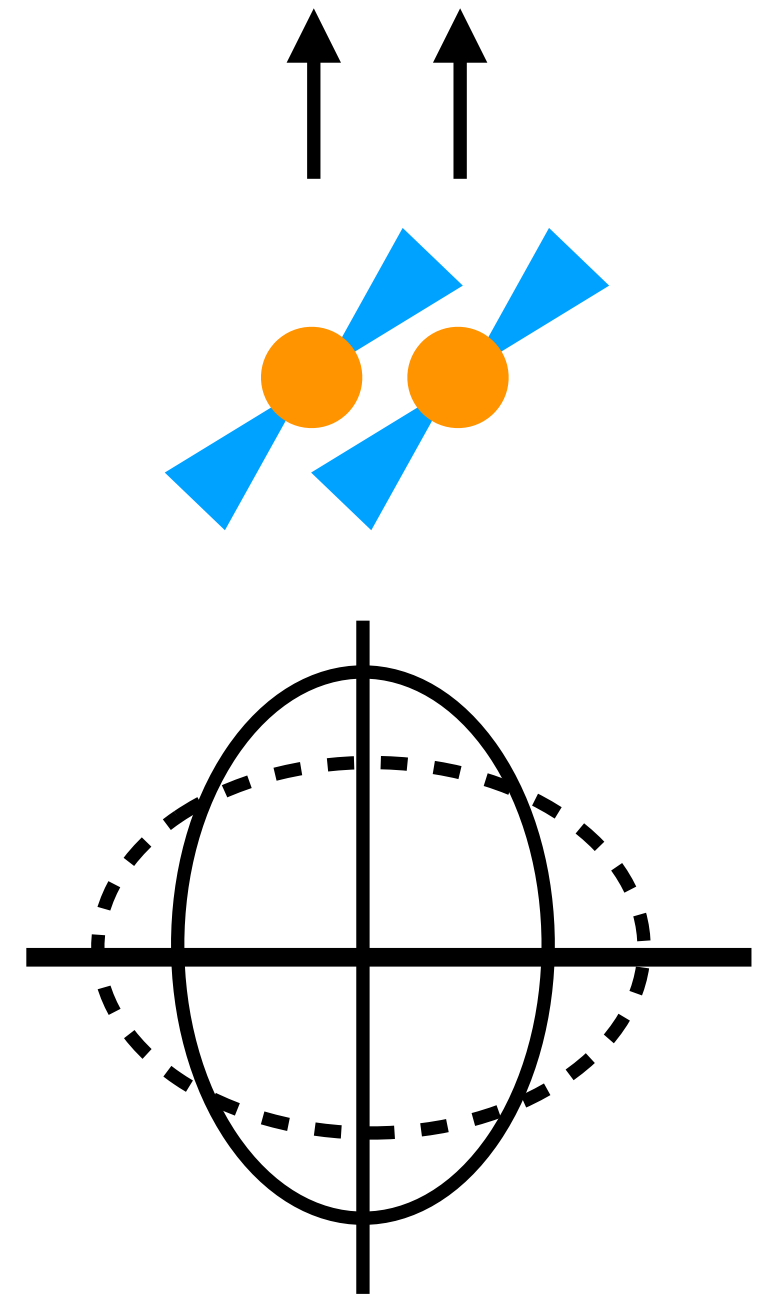
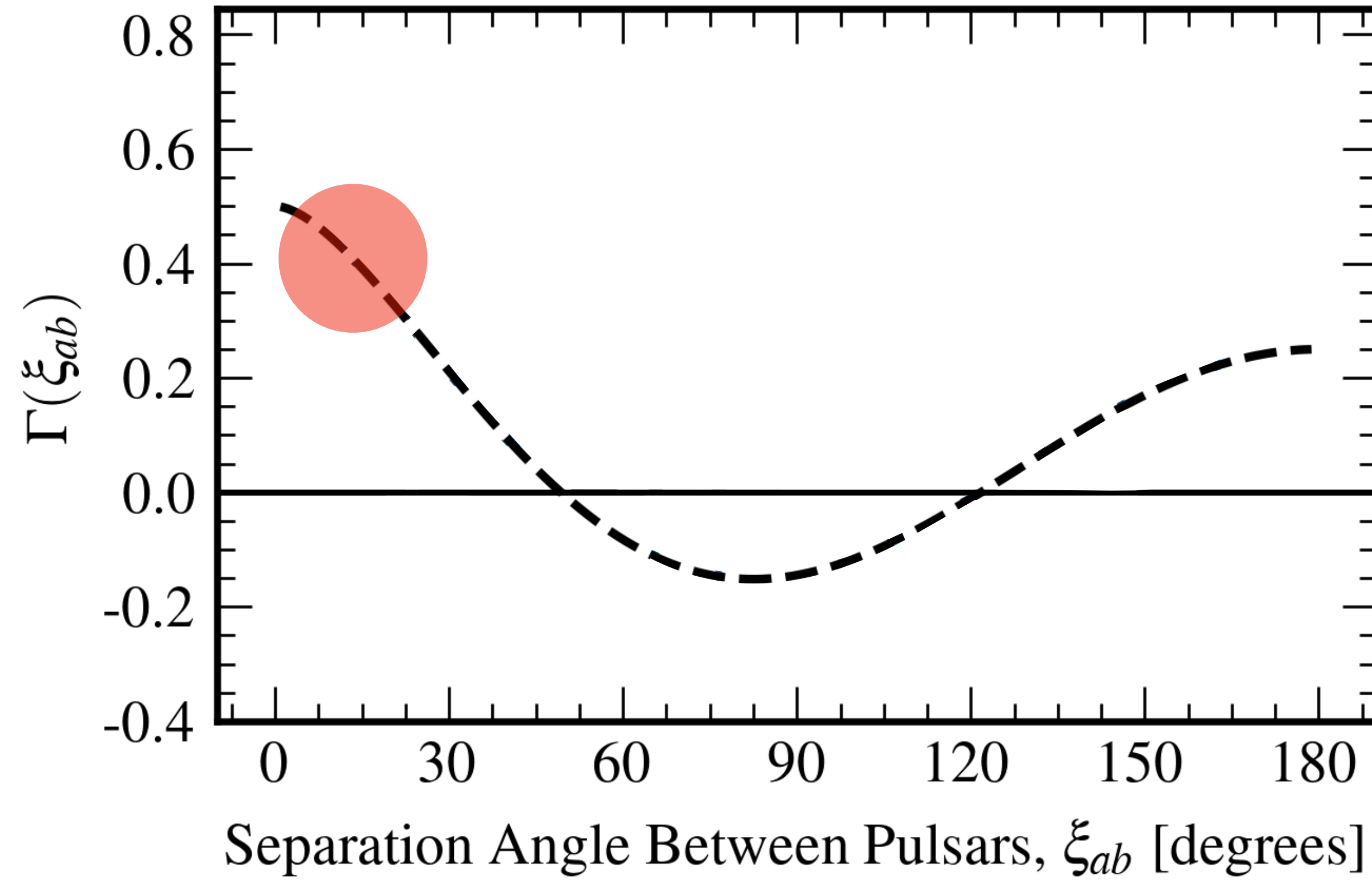
$$\langle \delta t_a \delta t_b \rangle \propto \Gamma_{ab}$$

$$\Gamma_{ab} = \int d\hat{\Omega} \sum_A F_a^A(\hat{\Omega}) F_b^A(\hat{\Omega}) [1 + \delta_{ab}]$$

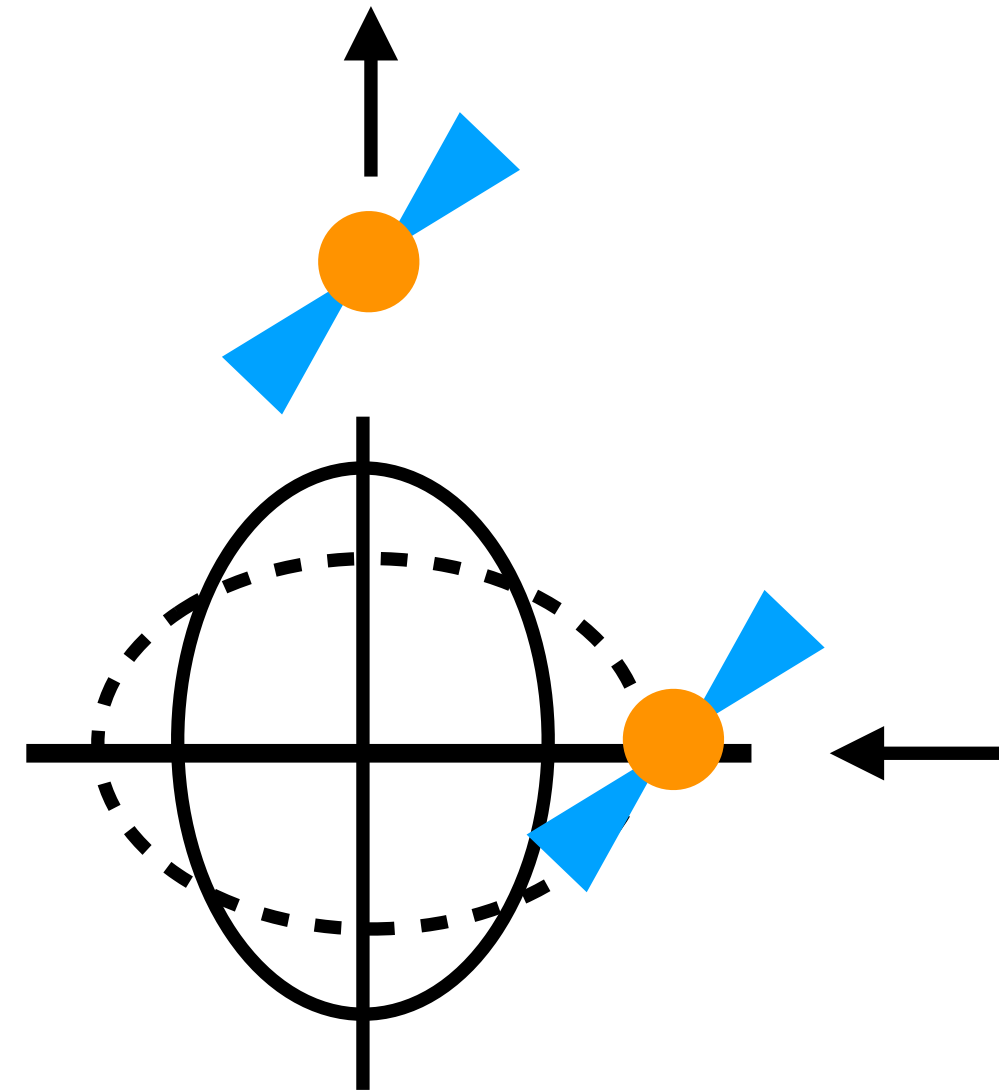
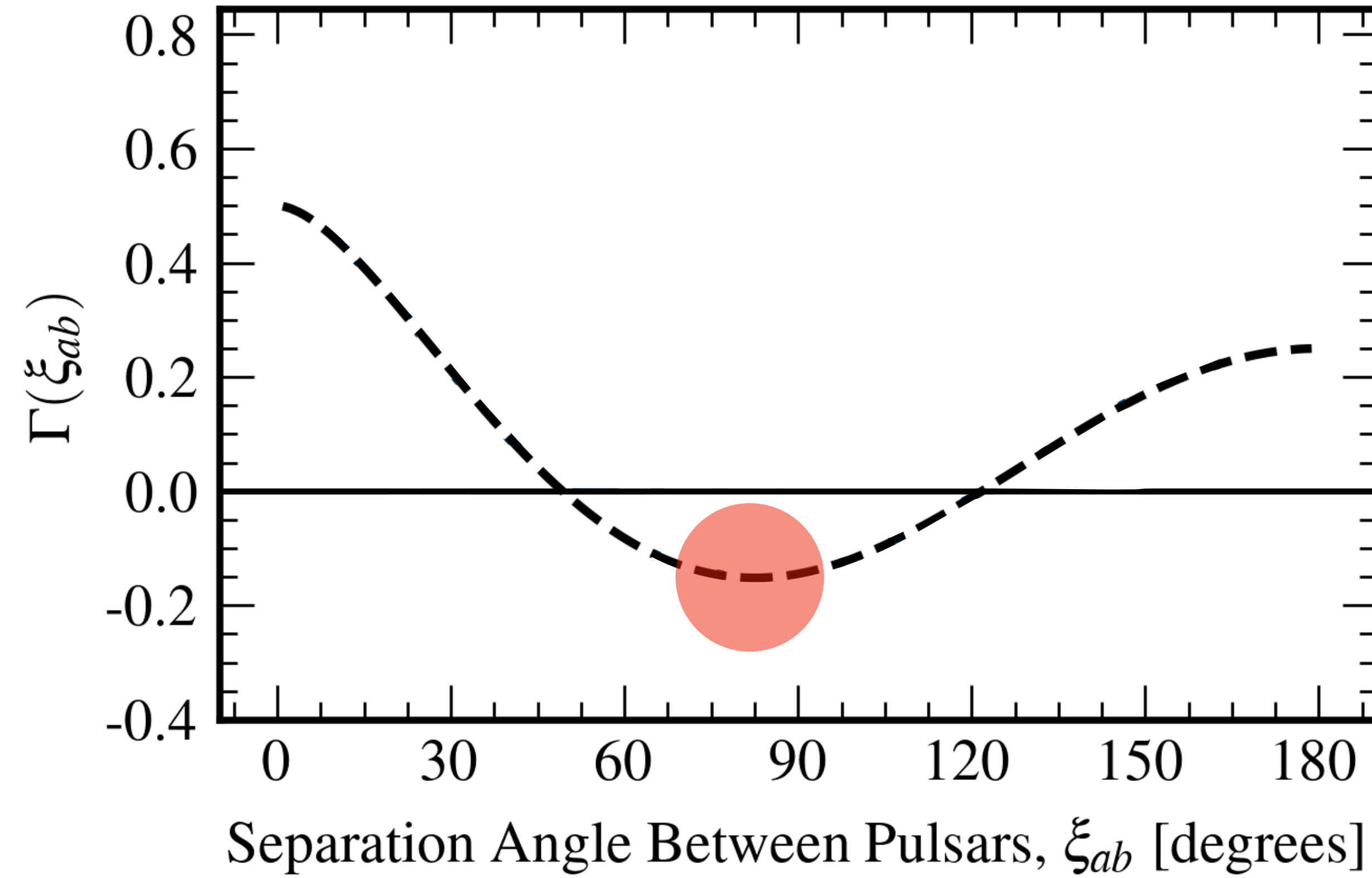
HELLINGS & DOWNS CURVE



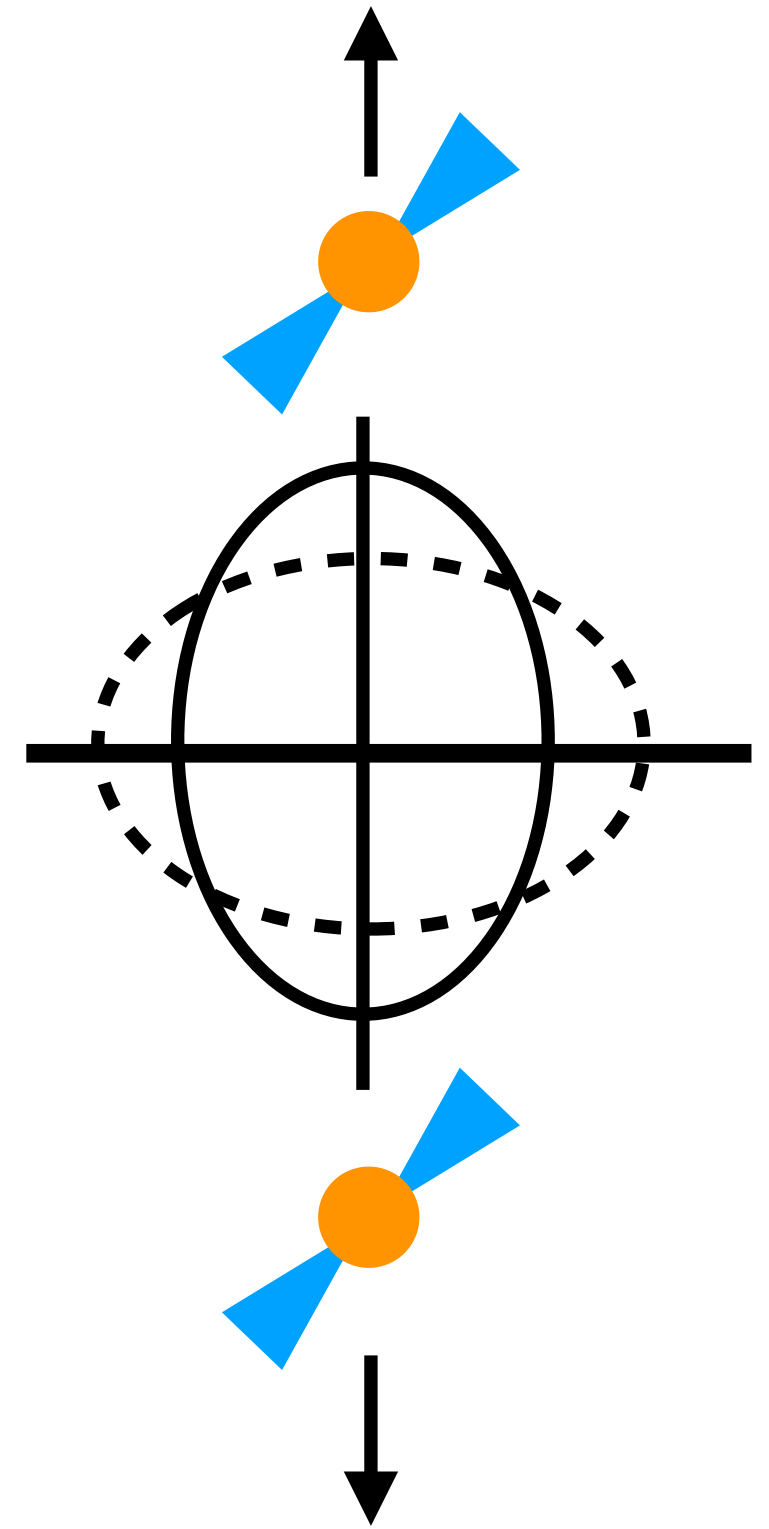
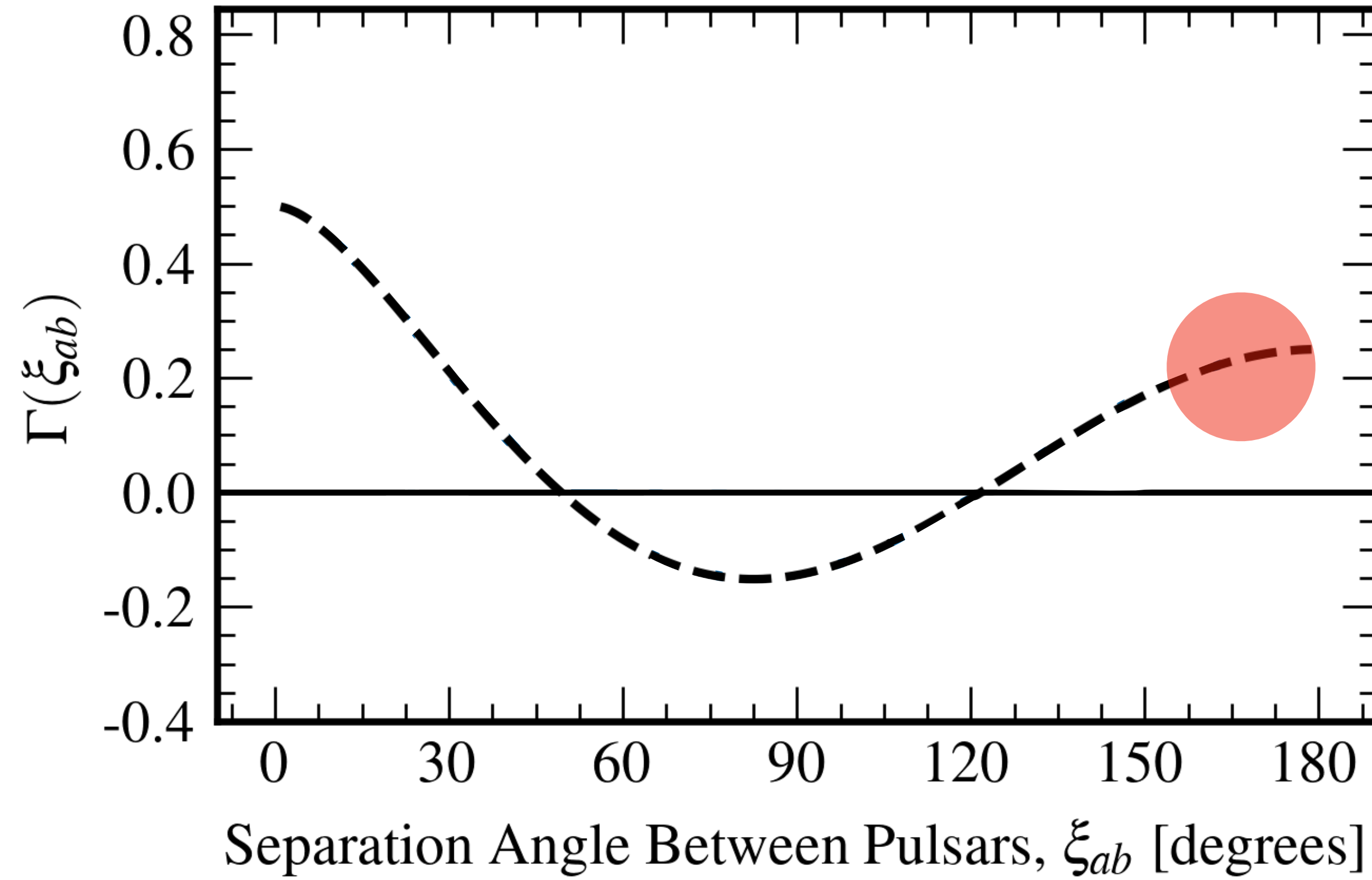
HELLINGS & DOWNS CURVE



HELLINGS & DOWNS CURVE



HELLINGS & DOWNS CURVE



searching for a GWB means searching for **stochastic delays** in the TOAs that are **common across pulsars** and **spatially correlated**

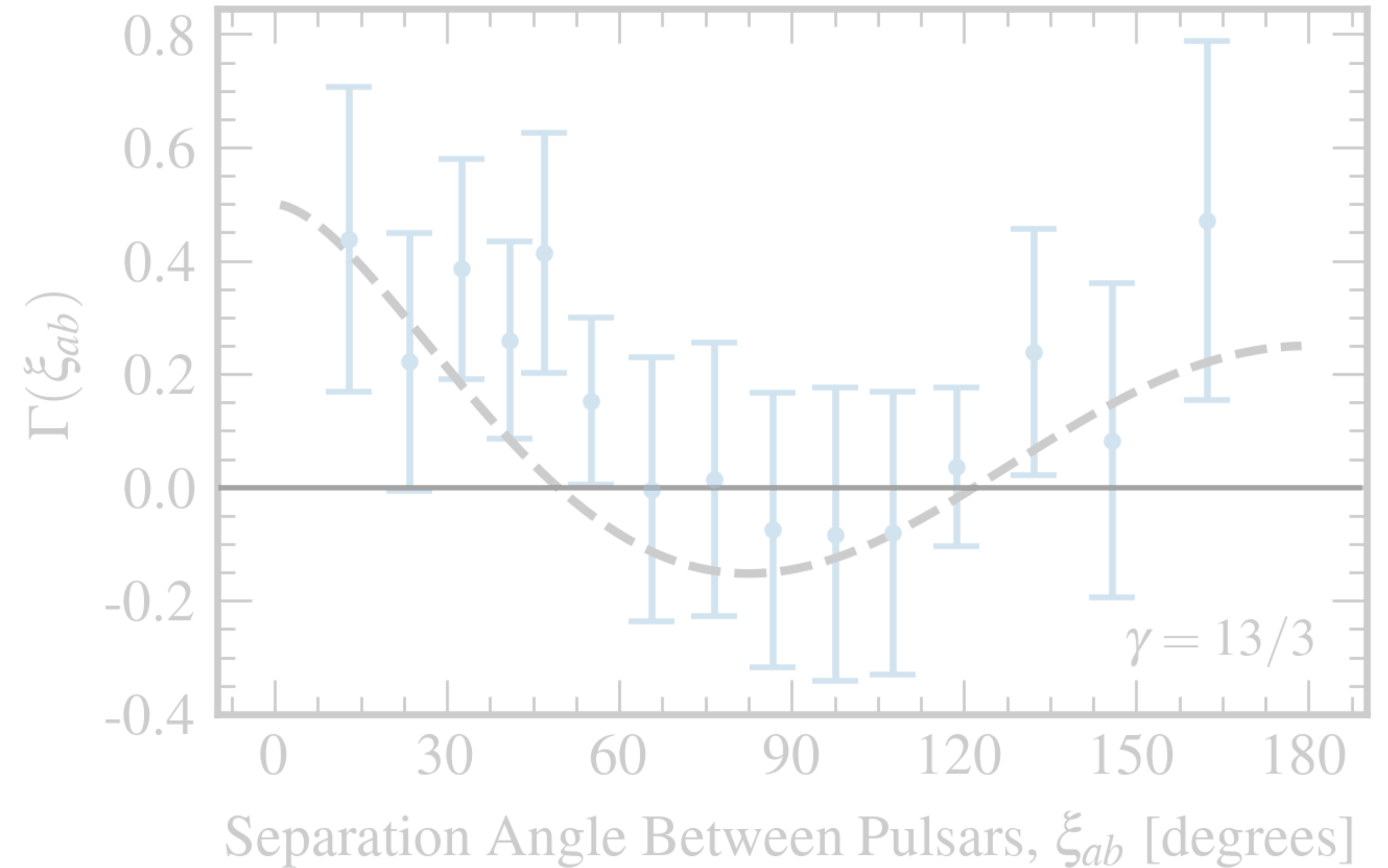
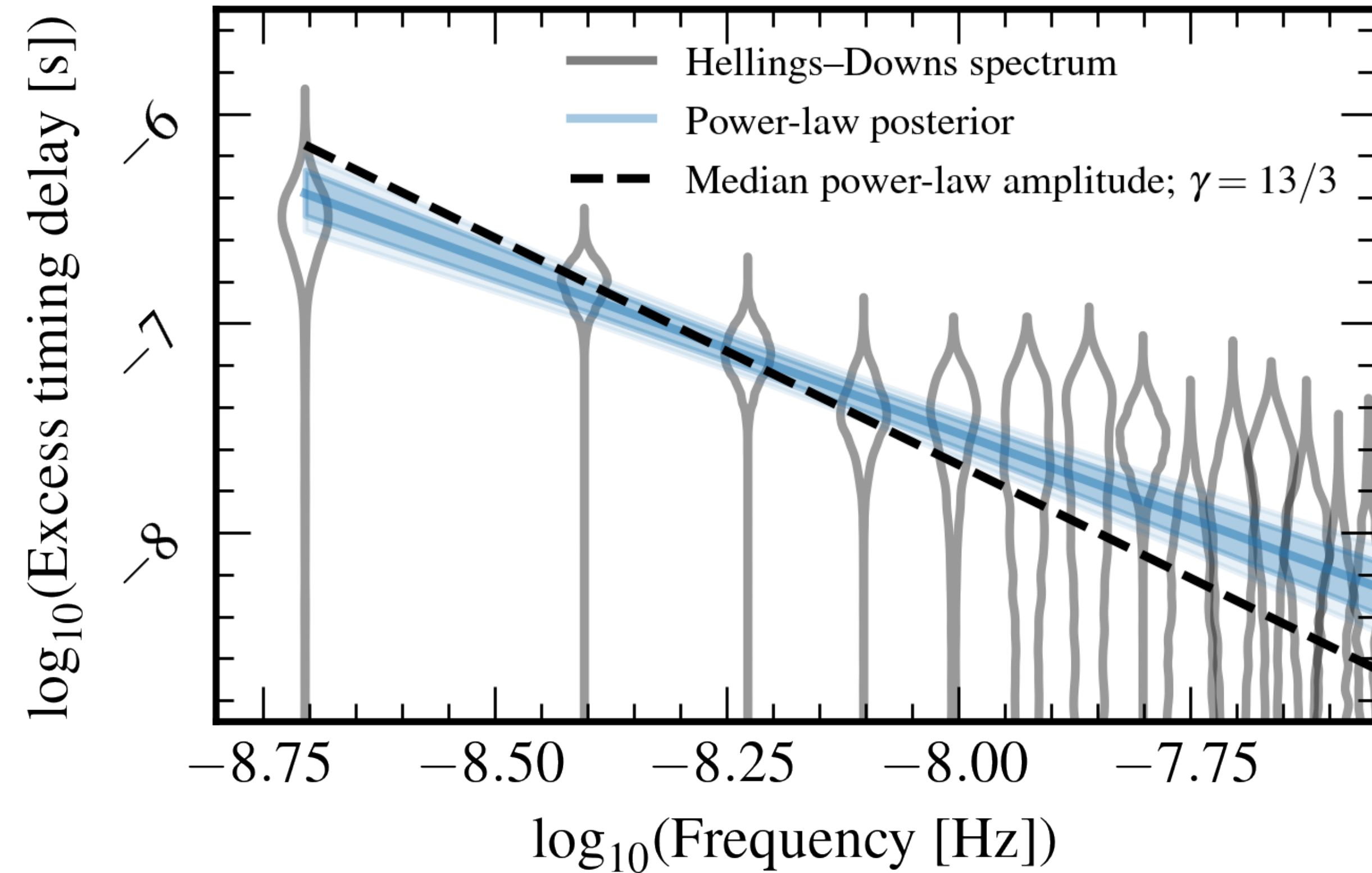
The NANOGrav 15-year Data Set: Evidence for a Gravitational-Wave Background

ABSTRACT

We report multiple lines of evidence for a stochastic signal that is correlated among 67 pulsars from the 15-year pulsar-timing data set collected by the North American Nanohertz Observatory for Gravitational Waves. The correlations follow the Hellings–Downs pattern expected for a stochastic gravitational-wave background. The presence of such a gravitational-wave background with a power-law–spectrum is favored over a model with only independent pulsar noises with a Bayes factor in excess of 10^{14} , and this same model is favored over an uncorrelated common power-law–spectrum model with Bayes factors of 200–1000, depending on spectral modeling choices. We have built a statistical background distribution for these latter Bayes factors using a method that removes inter-pulsar correlations from our data set, finding $p = 10^{-3}$ (approx. 3σ) for the observed Bayes factors in the null no-correlation scenario. A frequentist test statistic built directly as a weighted sum of inter-pulsar correlations yields $p = 5 \times 10^{-5}$ – 1.9×10^{-4} (approx. 3.5 – 4σ). Assuming a fiducial $f^{-2/3}$ characteristic-strain spectrum, as appropriate for an ensemble of binary supermassive black-hole inspirals, the strain amplitude is $2.4^{+0.7}_{-0.6} \times 10^{-15}$ (median + 90% credible interval) at a reference frequency of 1 yr^{-1} . The inferred gravitational-wave background amplitude and spectrum are consistent with astrophysical expectations for a signal from a population of supermassive black-hole binaries, although more exotic cosmological and astrophysical sources cannot be excluded. The observation of Hellings–Downs correlations points to the gravitational-wave origin of this signal.

EVIDENCE FOR GWB

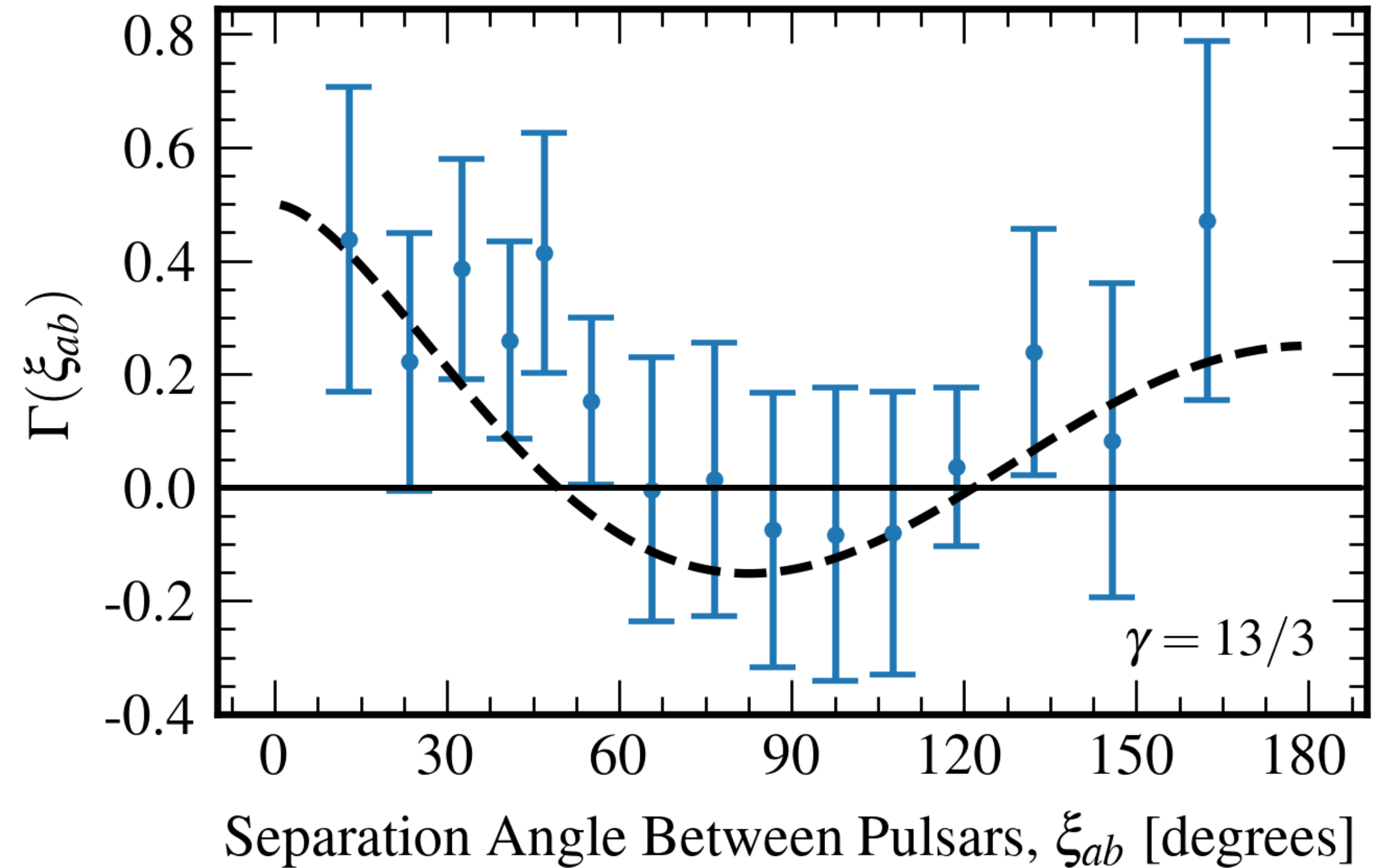
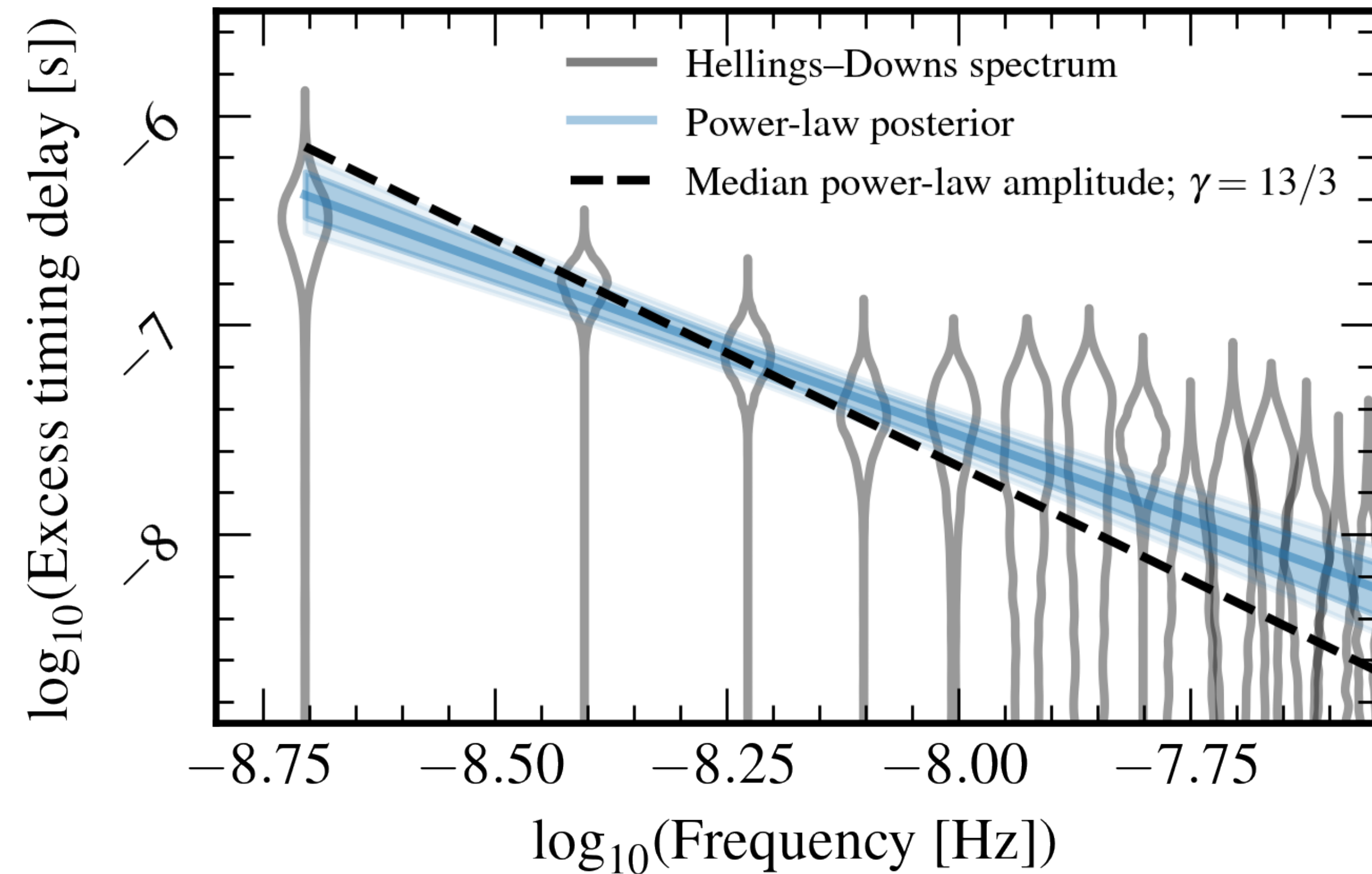
$$\langle \delta t_a(t_i) \delta t_b(t_j) \rangle \propto \Gamma_{ab} \int df H(f) e^{2\pi i f(t_i - t_j)}$$



we find evidence for Hellings & Downs correlation with a p -value of $5 \times 10^{-5} - 1.9 \times 10^{-4}$ (approx. $3.5 - 4\sigma$)

EVIDENCE FOR GWB

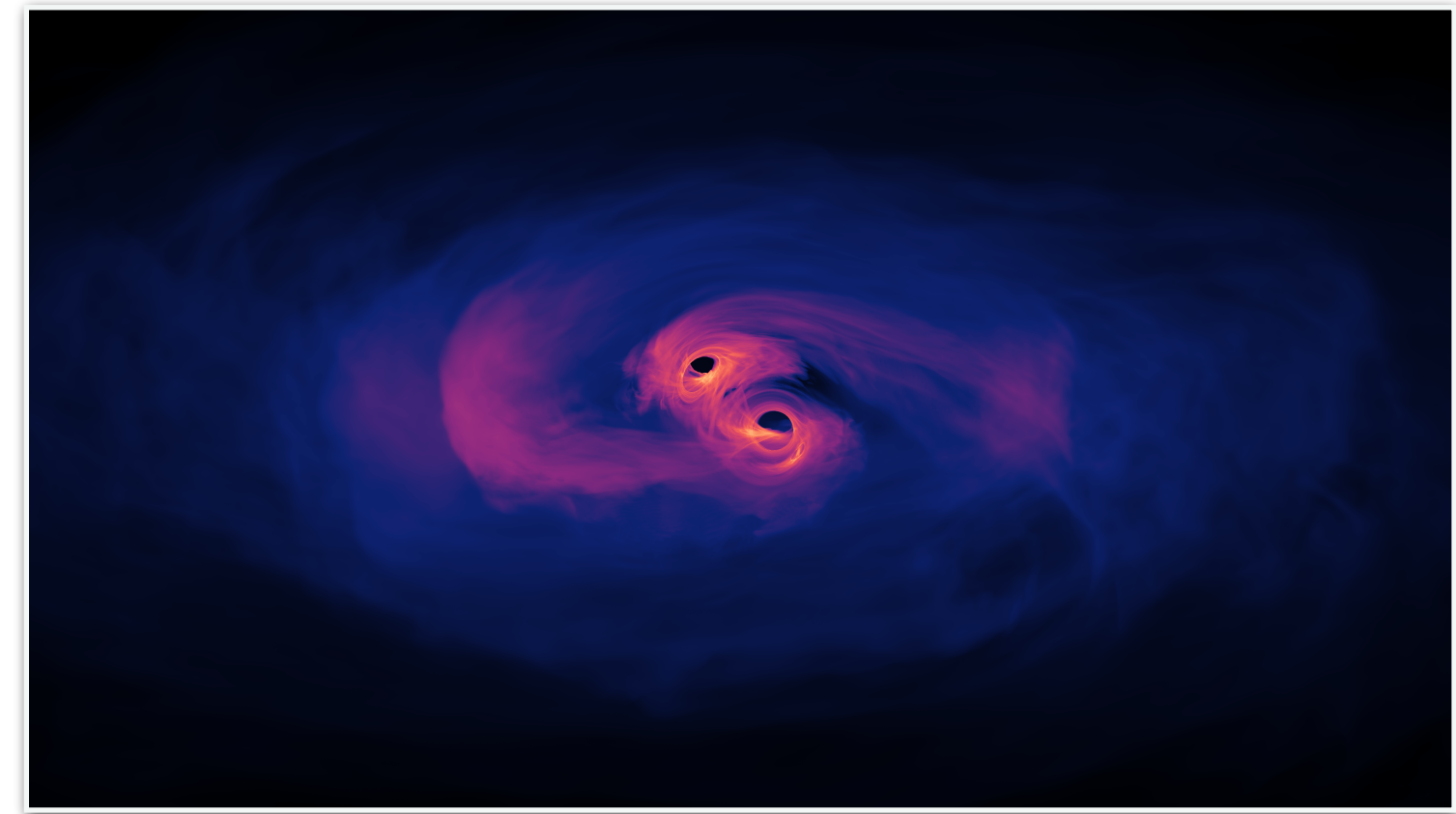
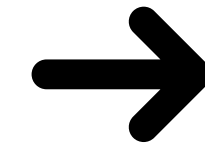
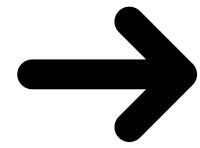
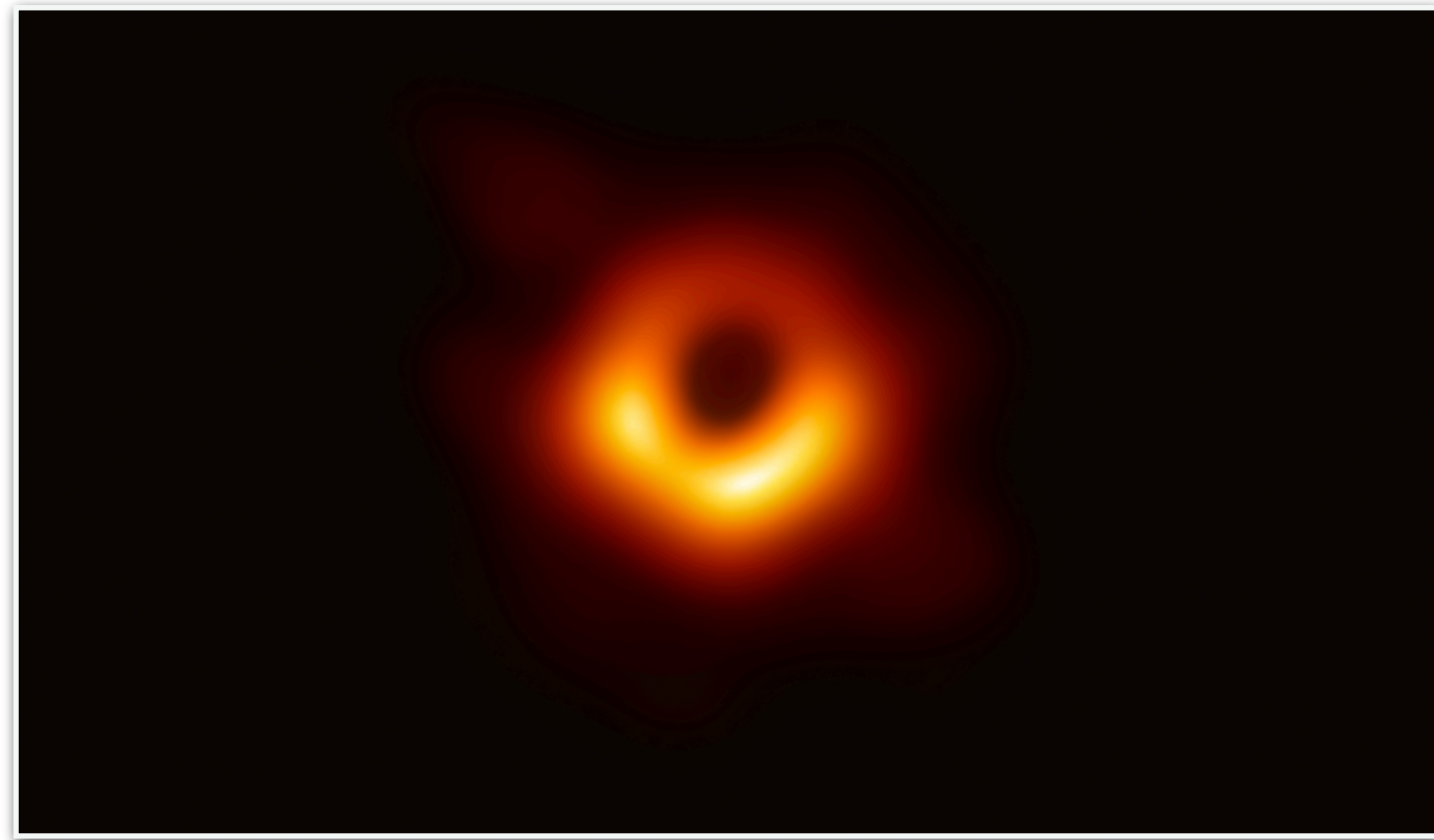
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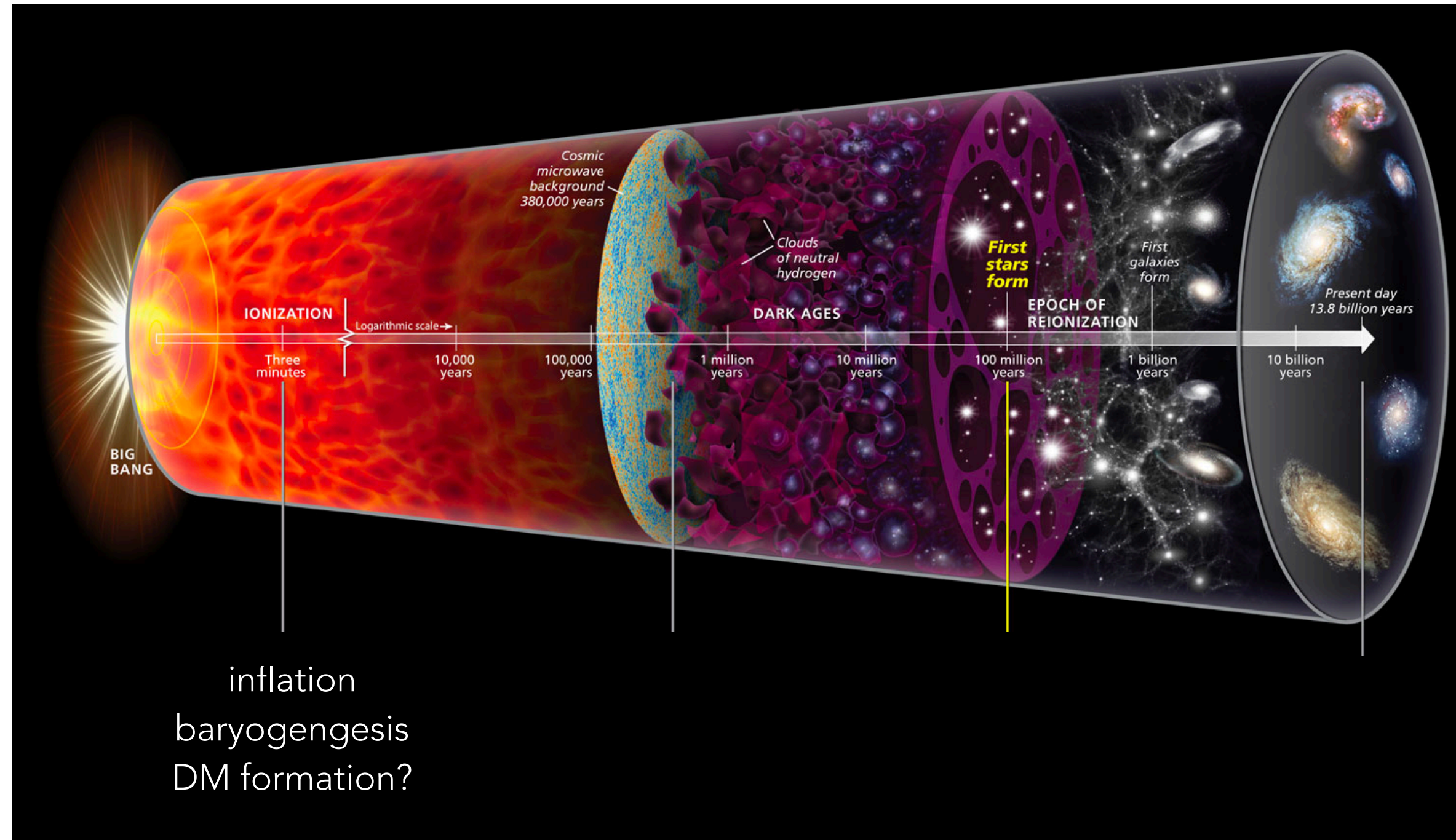
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what is the source?

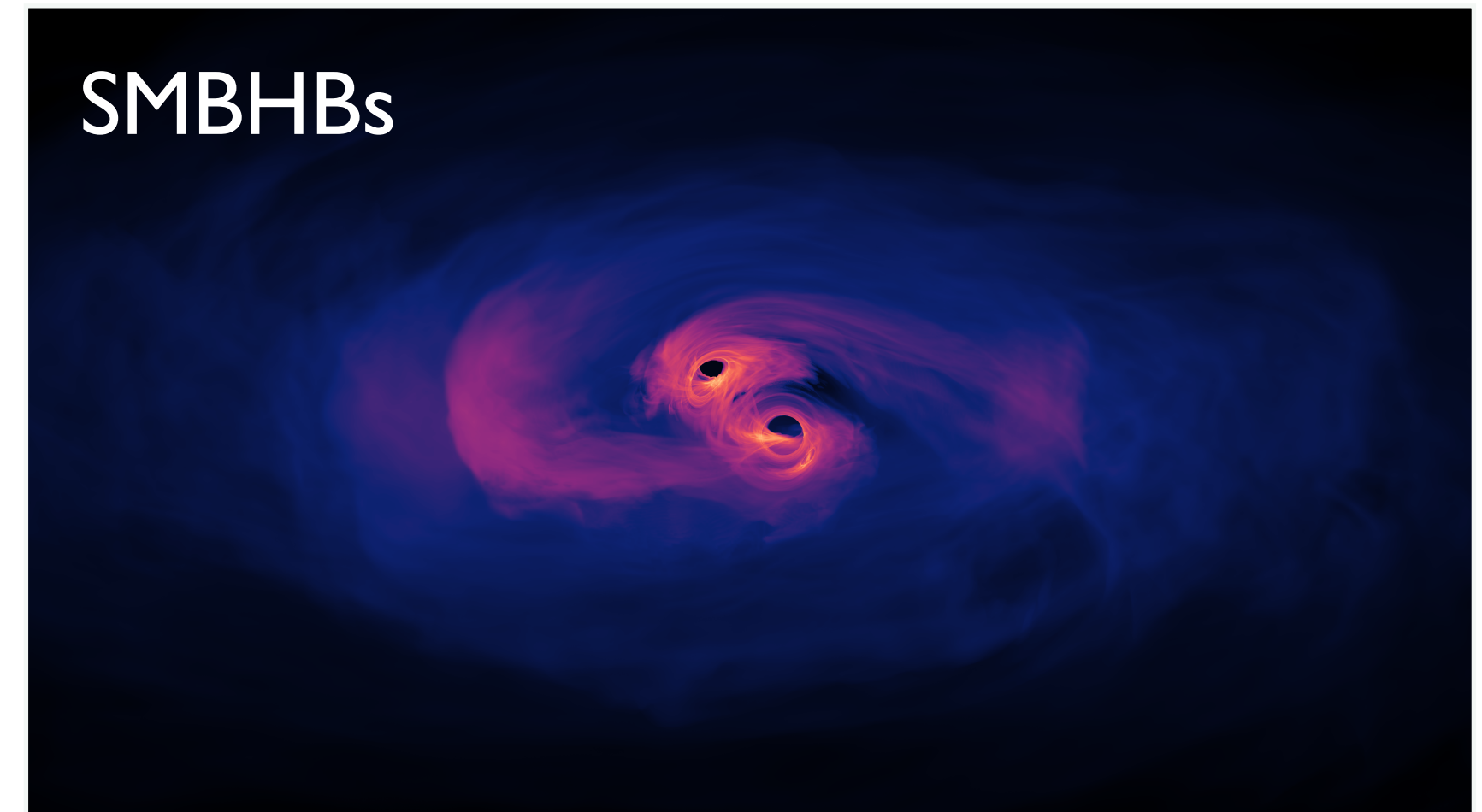
ASTRO OR COSMO?



ASTRO OR COSMO?



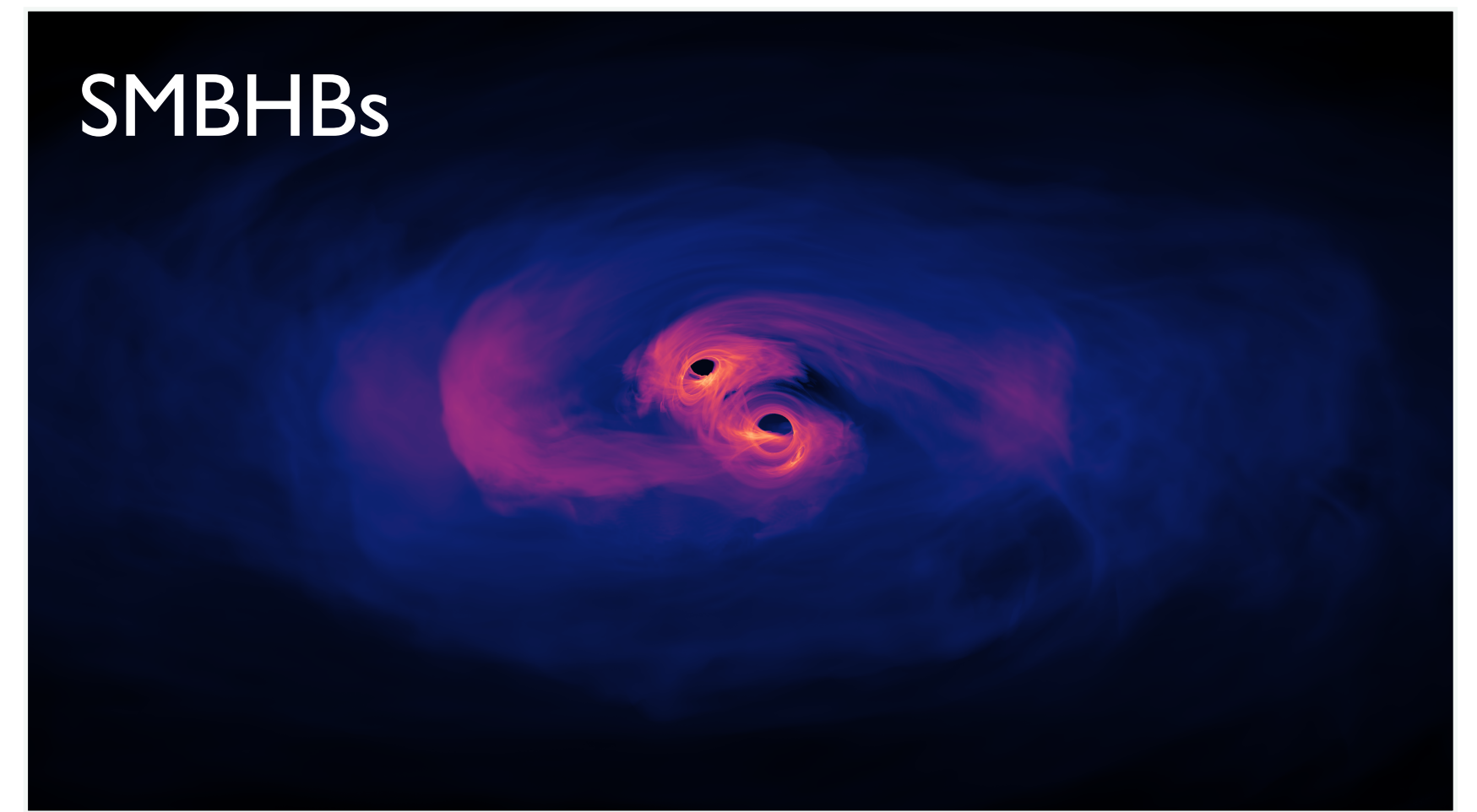
VS



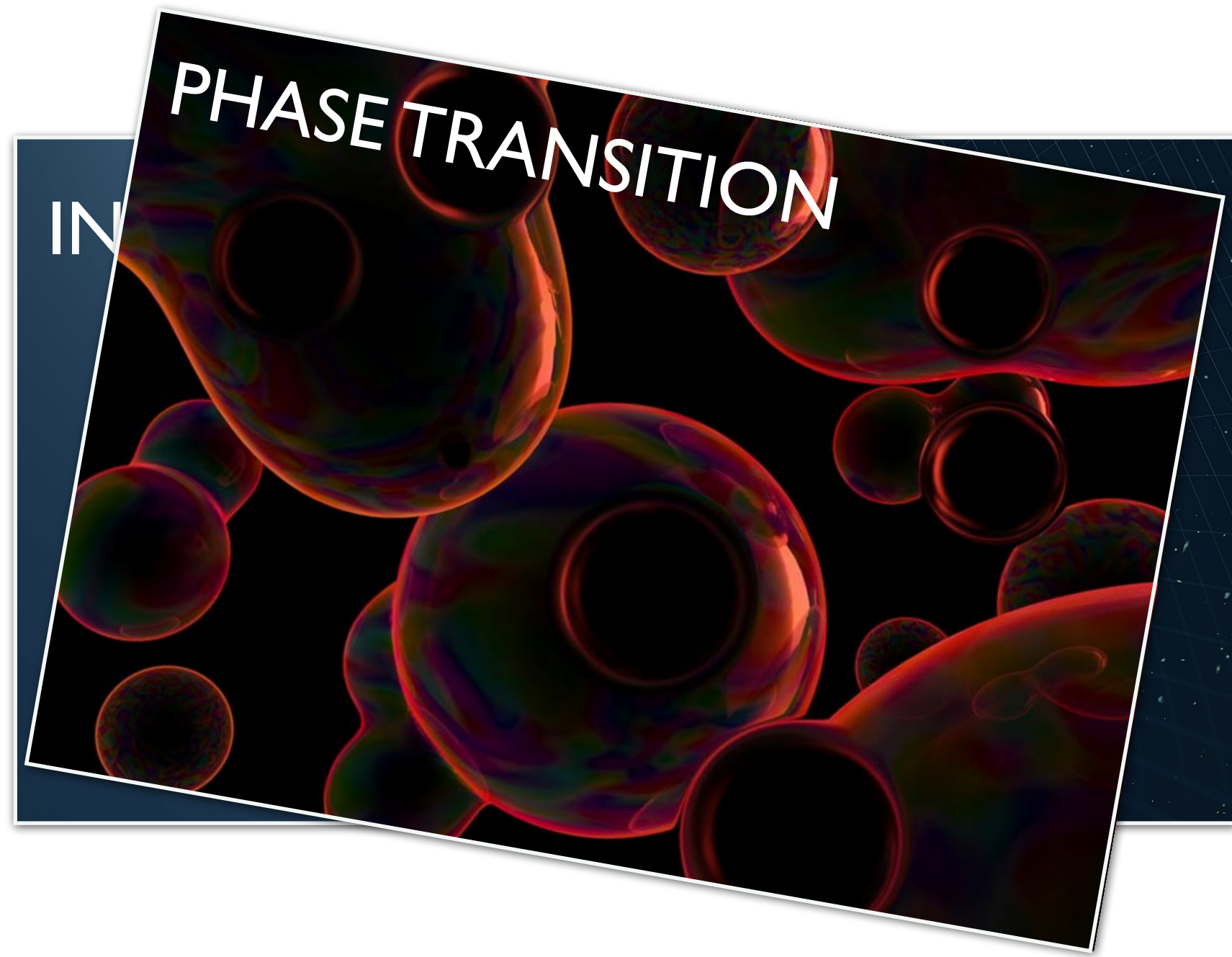
ASTRO OR COSMO?



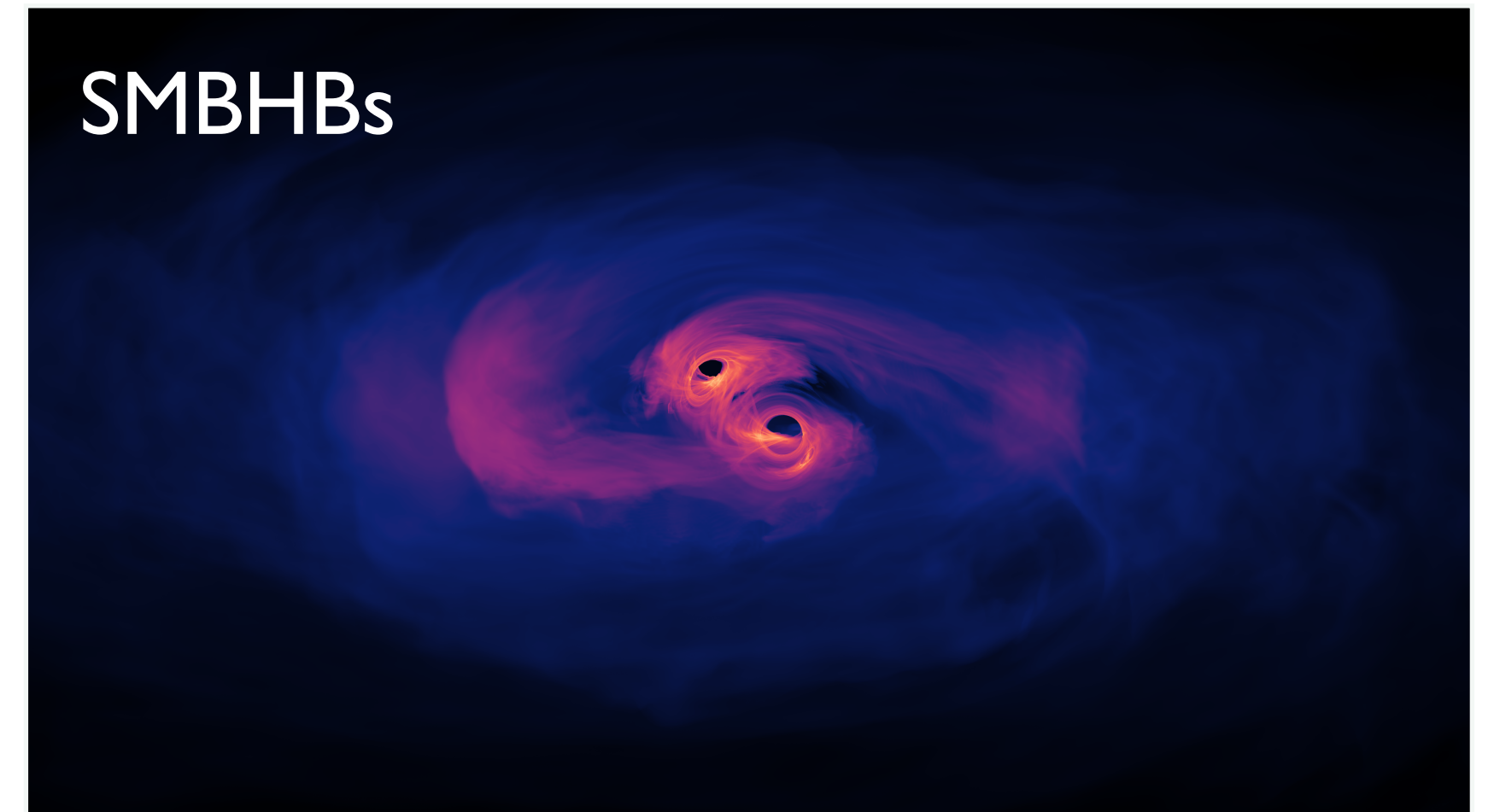
VS



ASTRO OR COSMO?



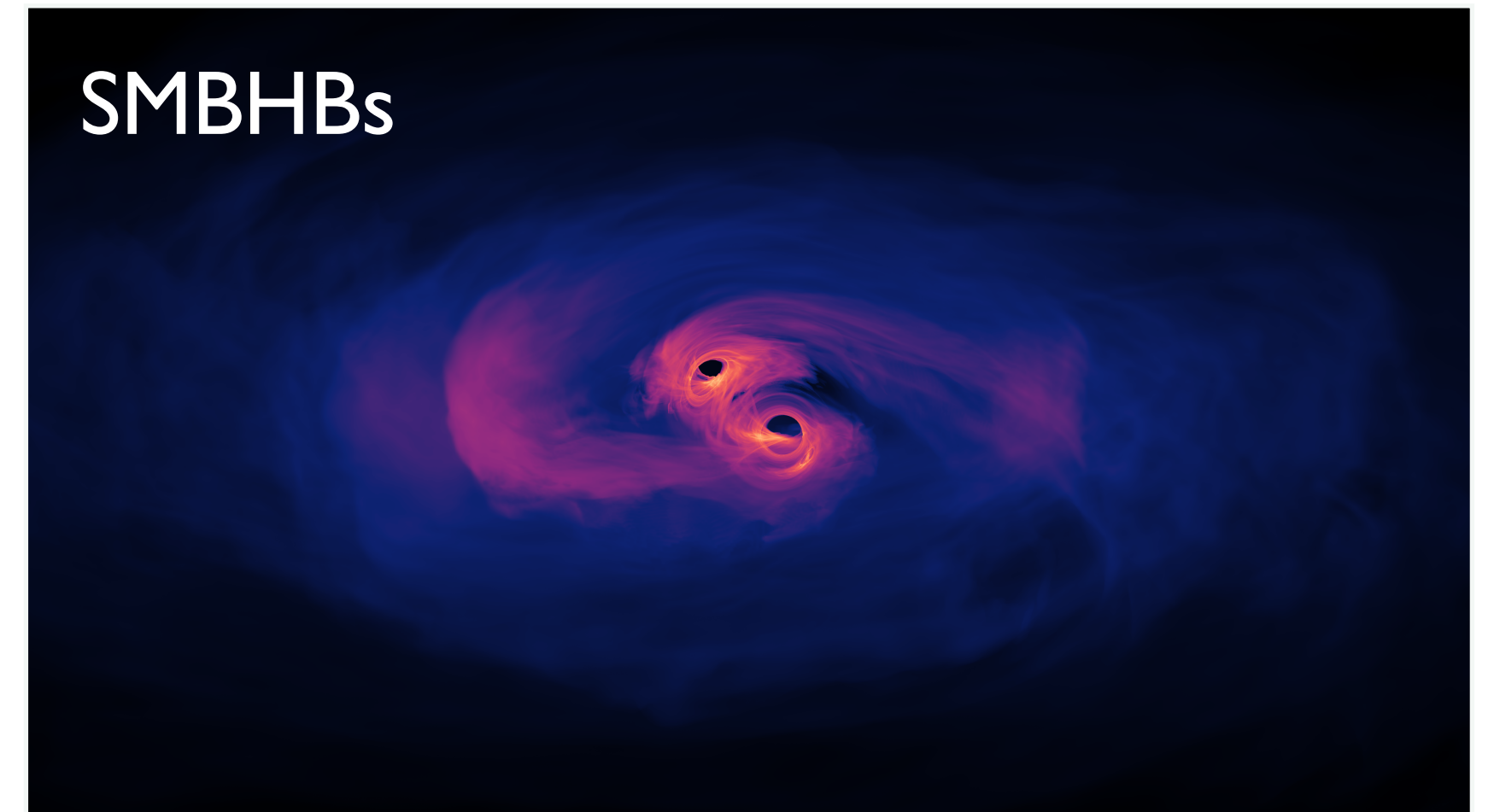
VS



ASTRO OR COSMO?



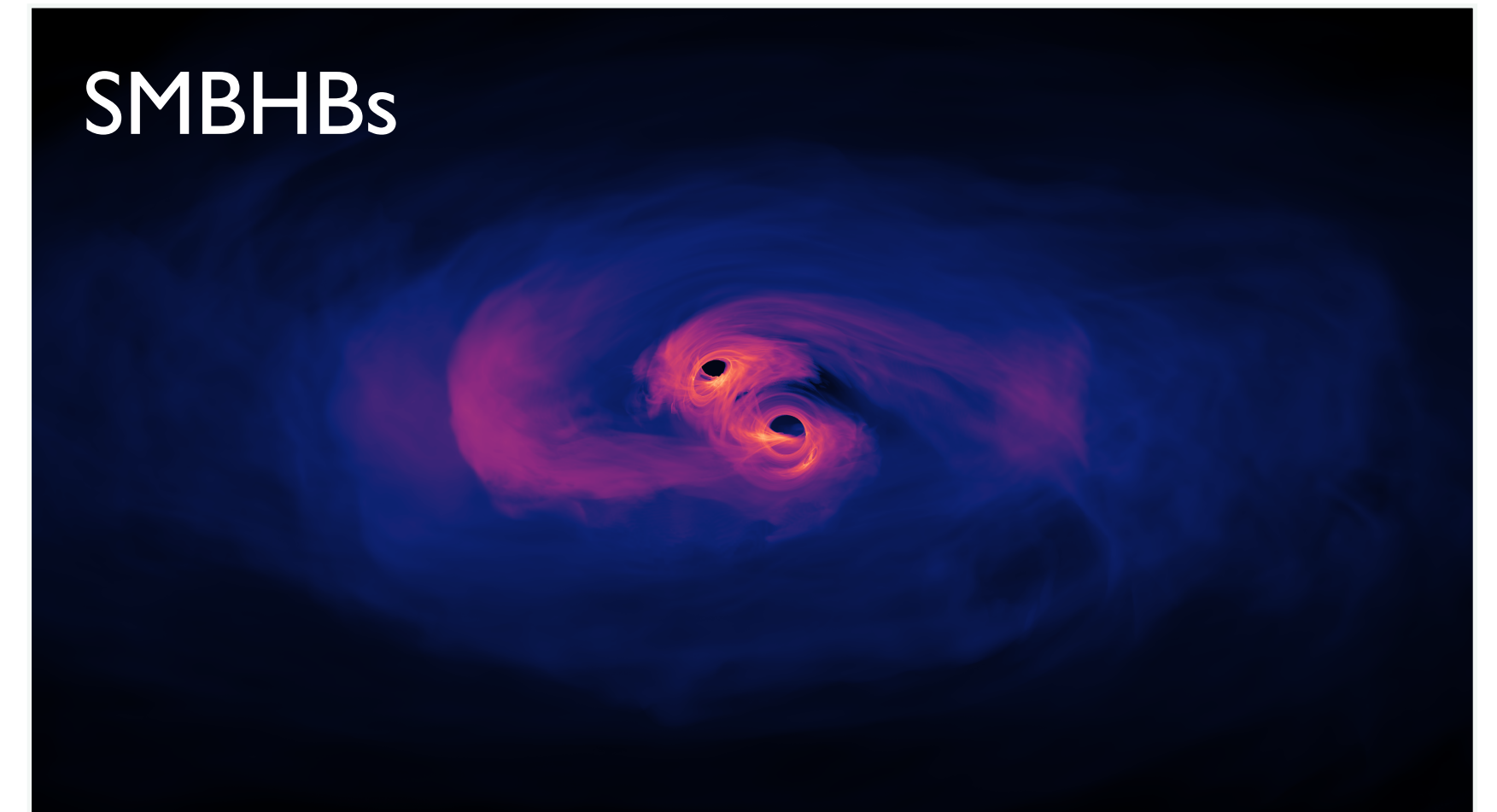
VS



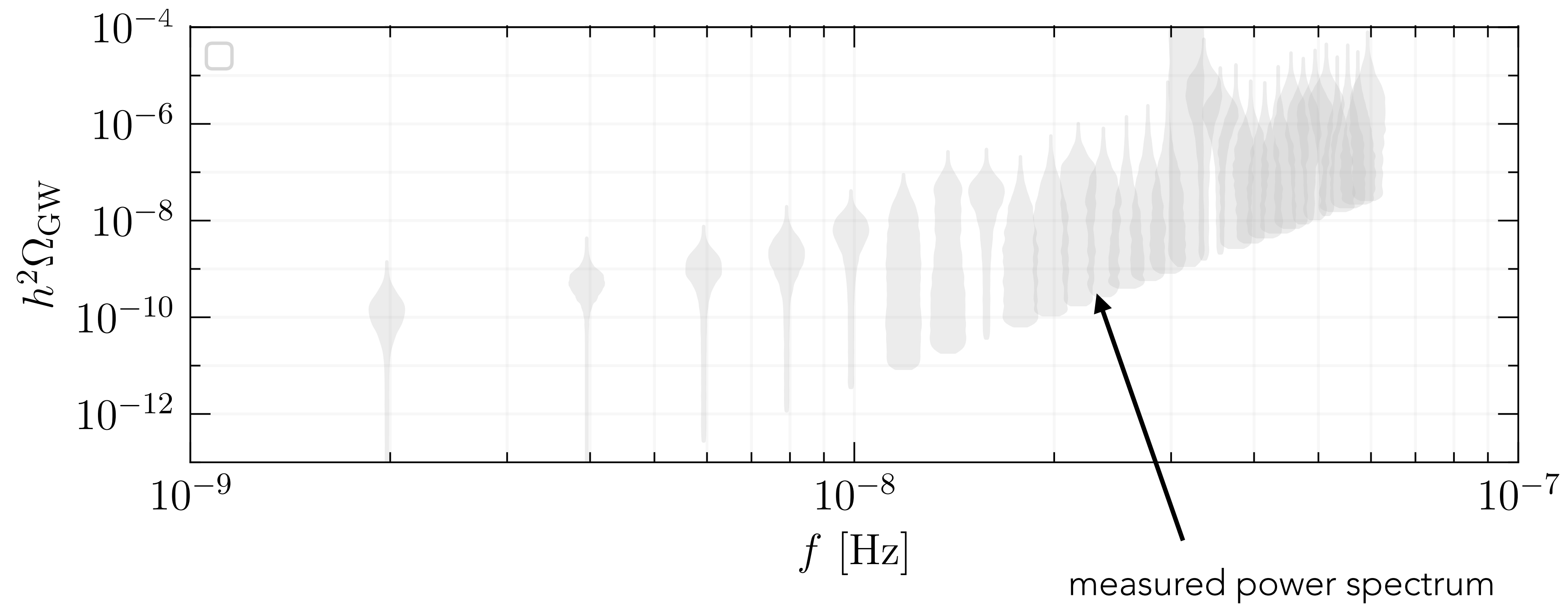
ASTRO OR COSMO?



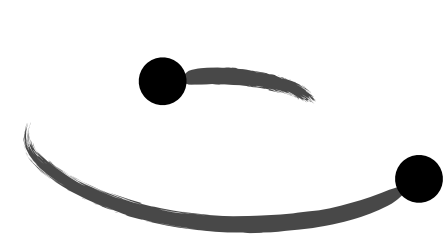
VS



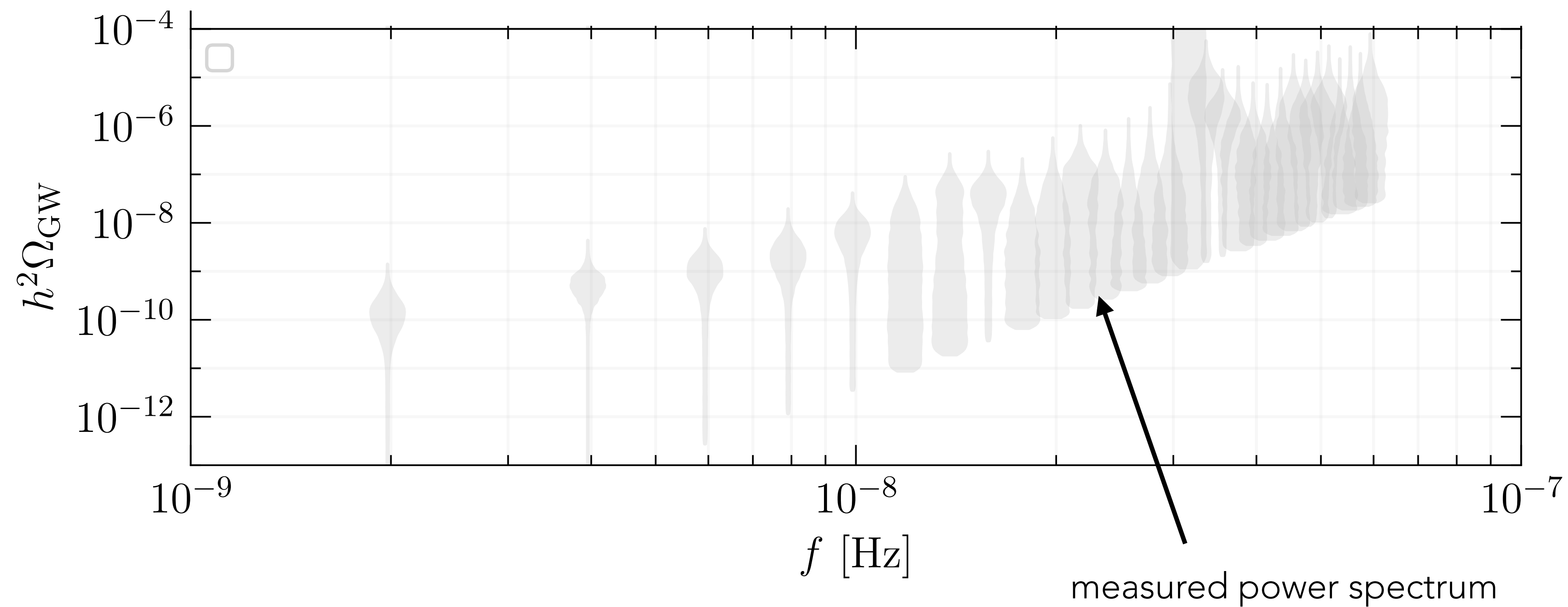
SPECTRAL DISCRIMINATION



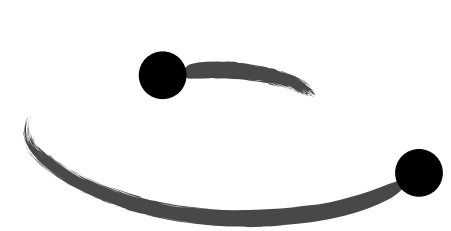
SPECTRAL DISCRIMINATION



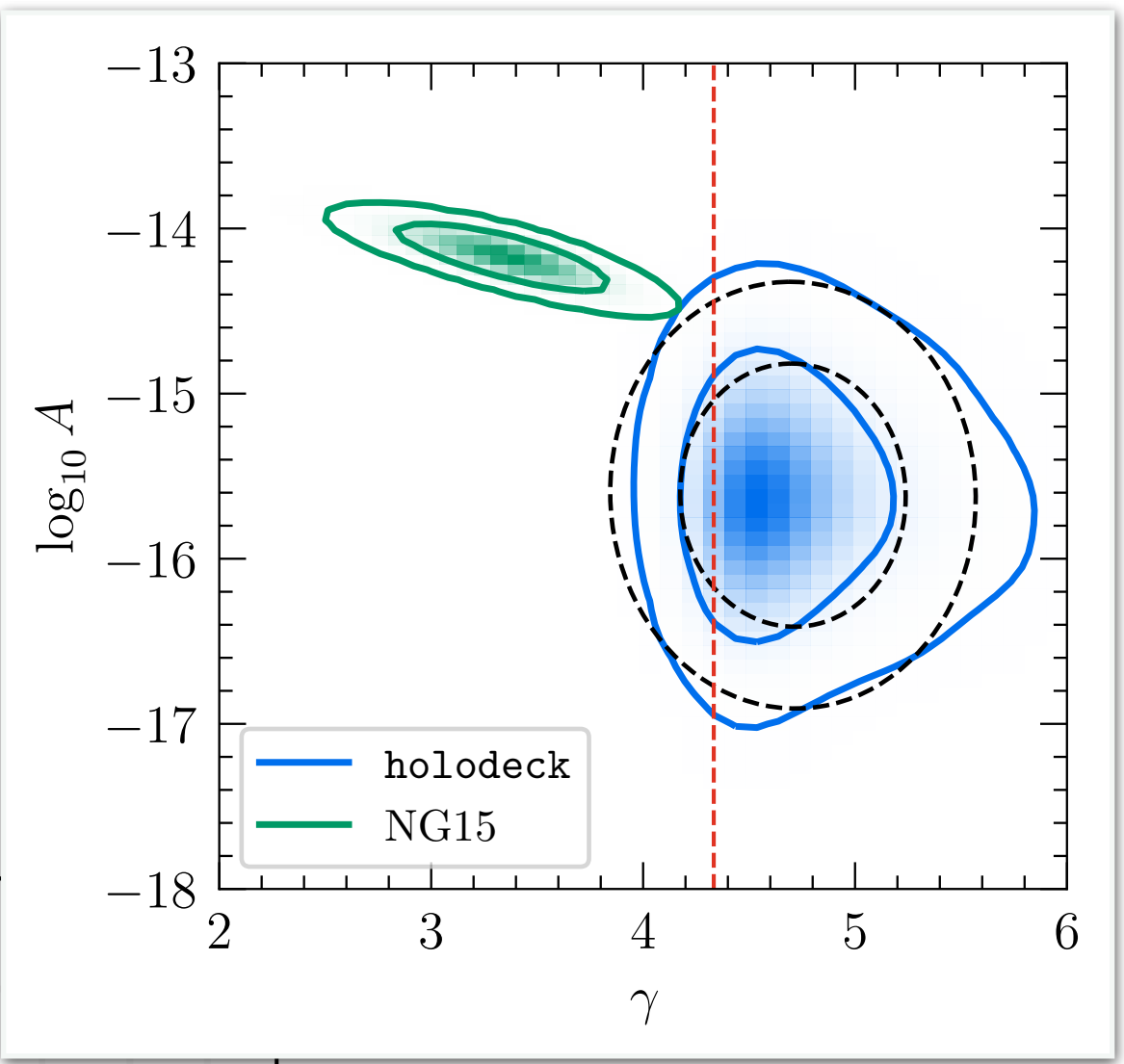
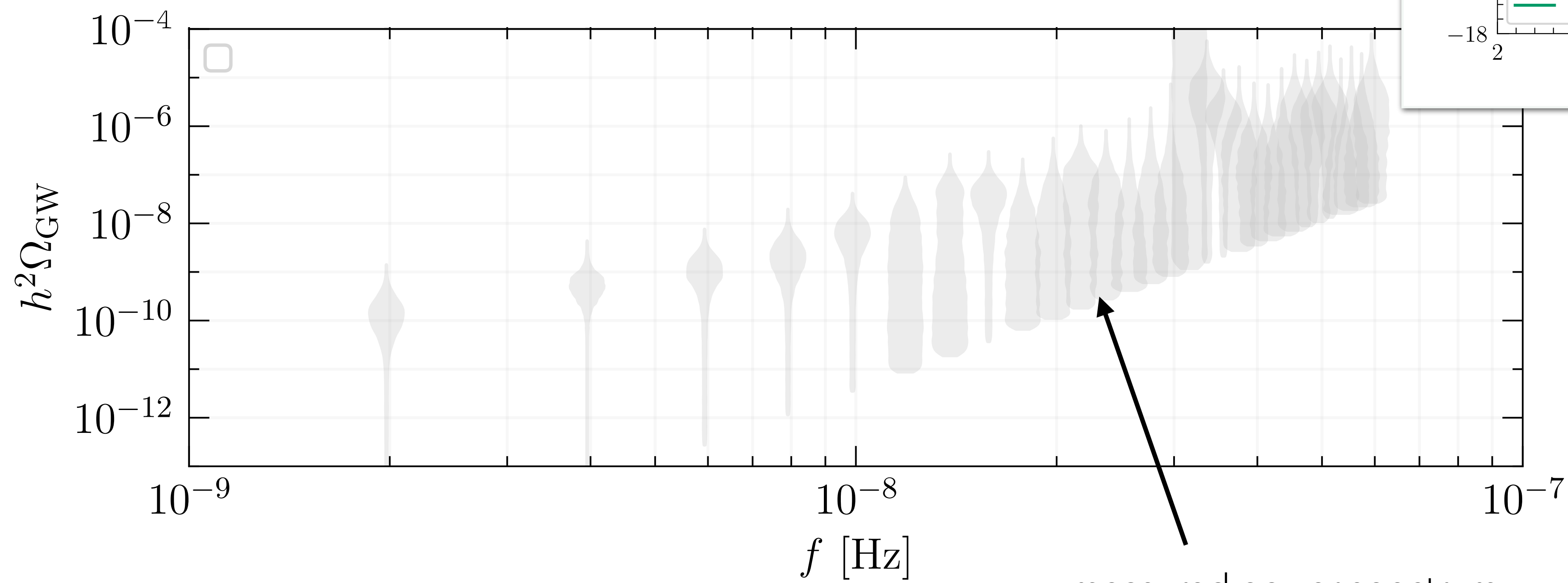
$$h^2\Omega_{\text{GW}} \propto \frac{A^2}{H_0^2} \left(\frac{f}{\text{yr}^{-1}} \right)^{5-\gamma} \text{yr}^{-2}$$



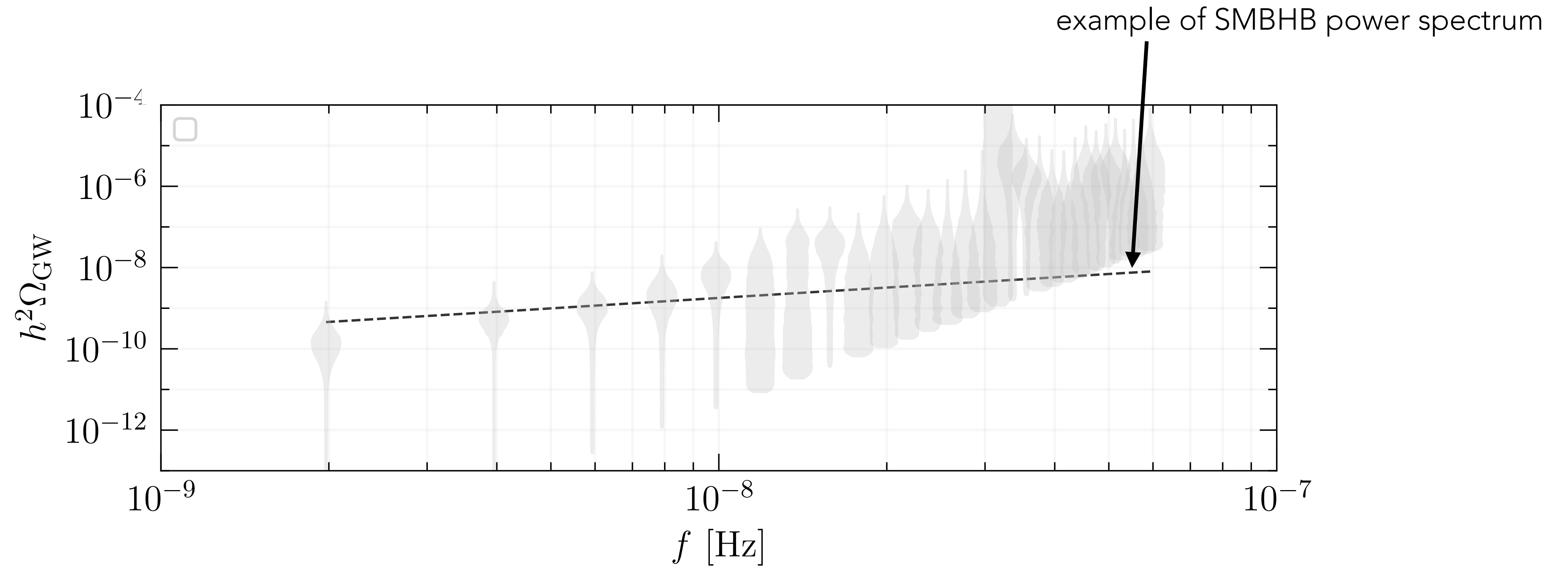
SPECTRAL DISCRIMINATION



$$h^2\Omega_{\text{GW}} \propto \frac{A^2}{H_0^2} \left(\frac{f}{\text{yr}^{-1}} \right)^{5-\gamma} \text{yr}^{-2}$$

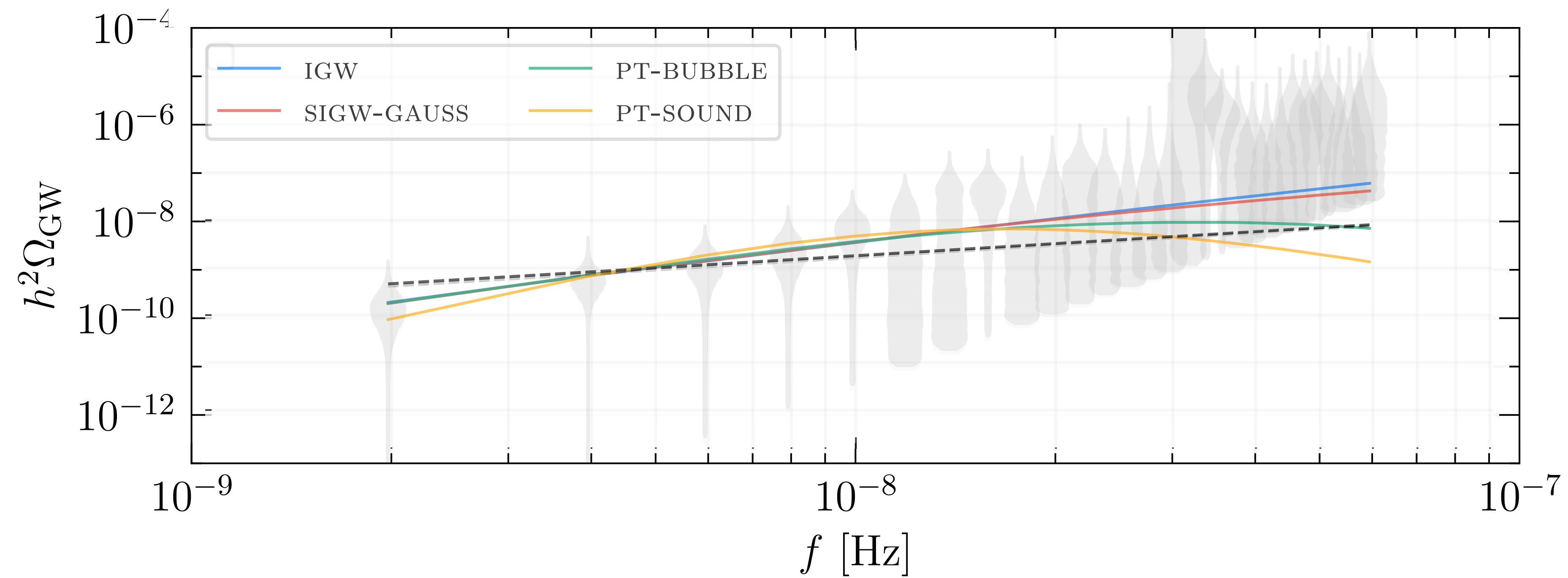


SPECTRAL DISCRIMINATION



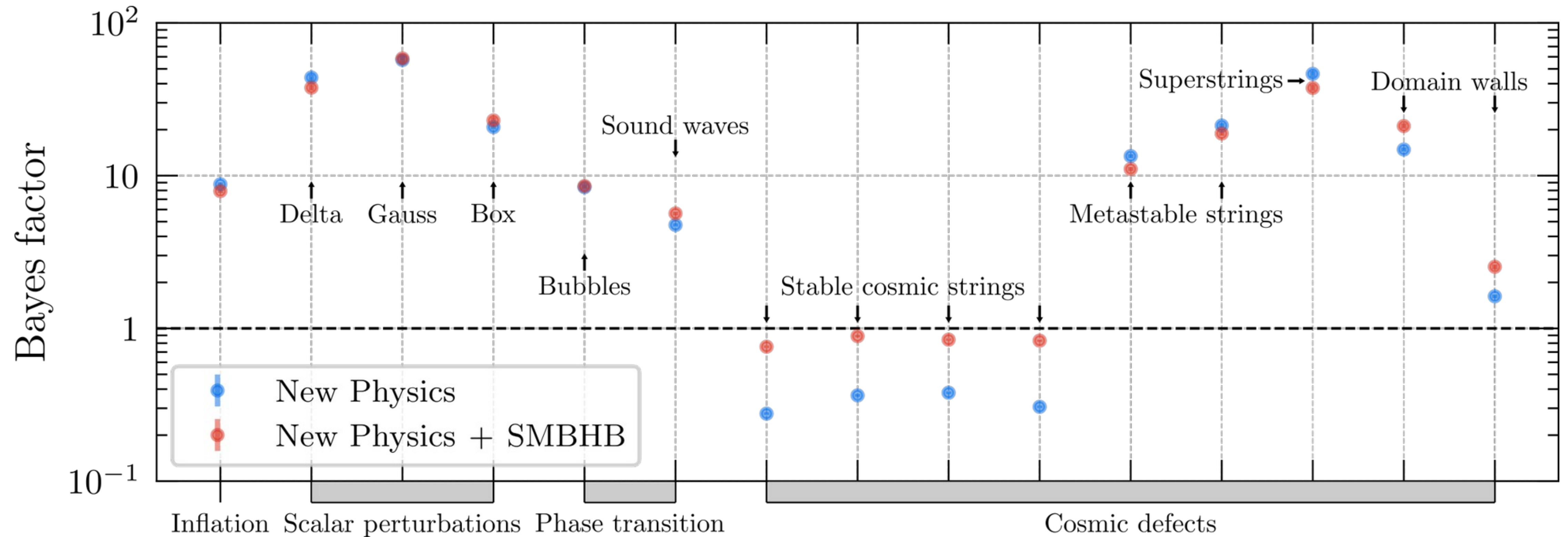
SPECTRAL DISCRIMINATION

$$h^2\Omega_{\text{GW}}(f; \Theta)$$



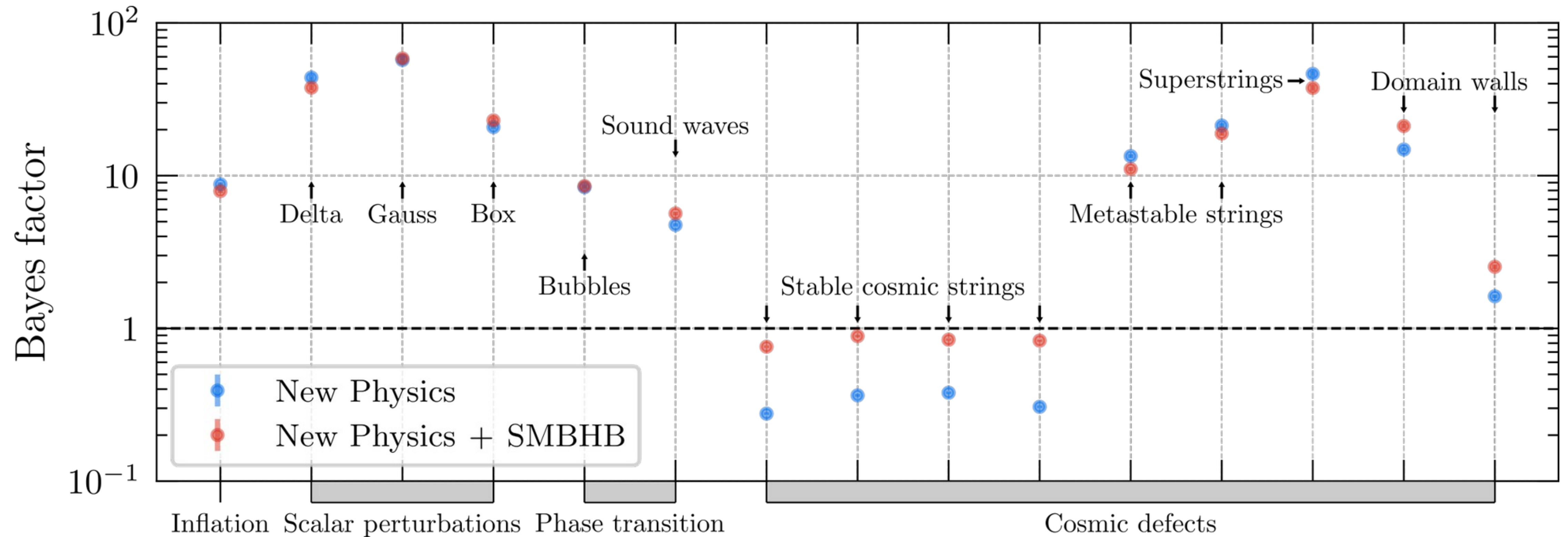
SPECTRAL DISCRIMINATION

many cosmological models seem to be preferred over SMBHB...



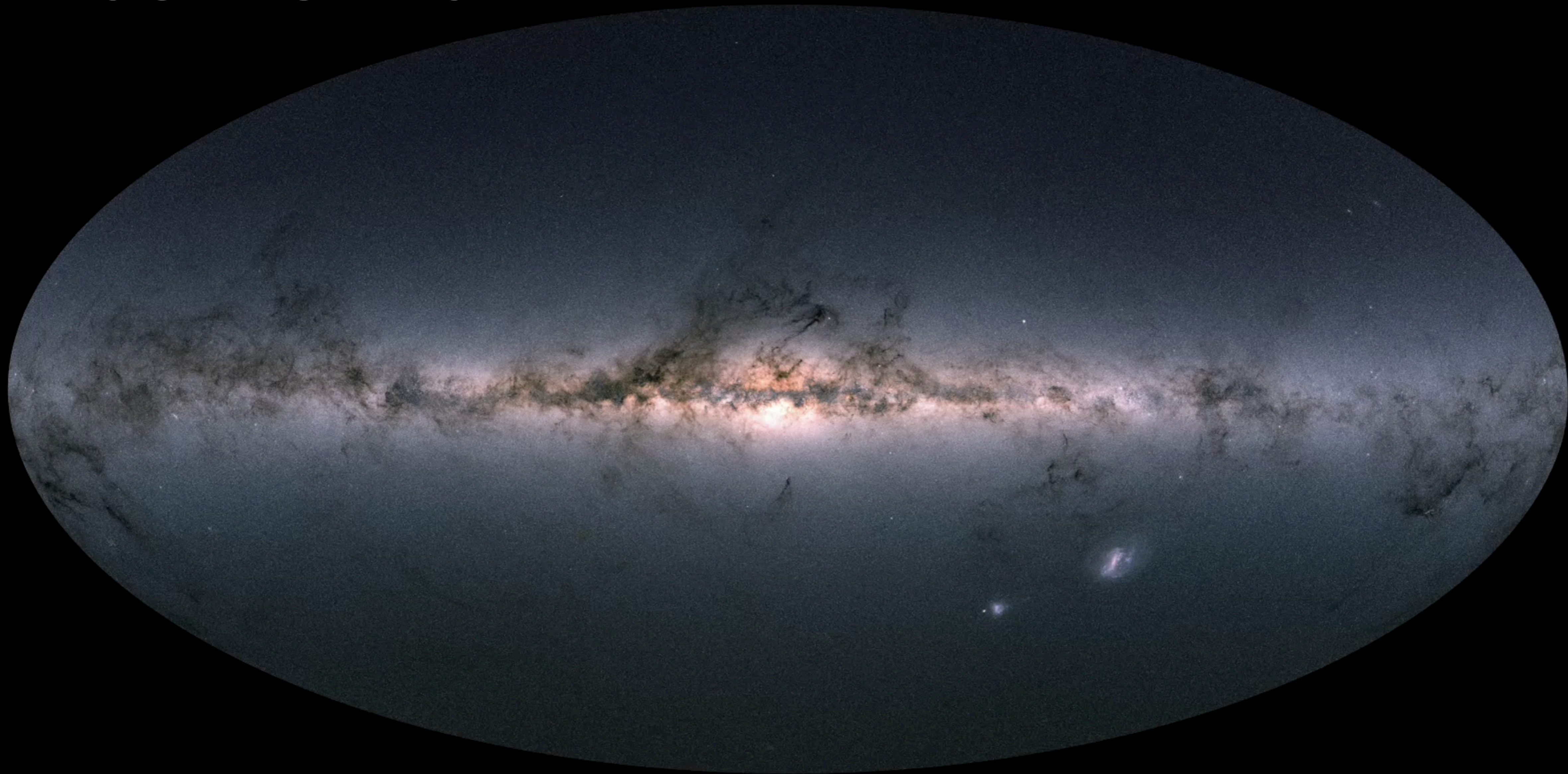
SPECTRAL DISCRIMINATION

many cosmological models seem to be preferred over SMBHB...
...however, systematic uncertainties are still too large to make a definitive claim



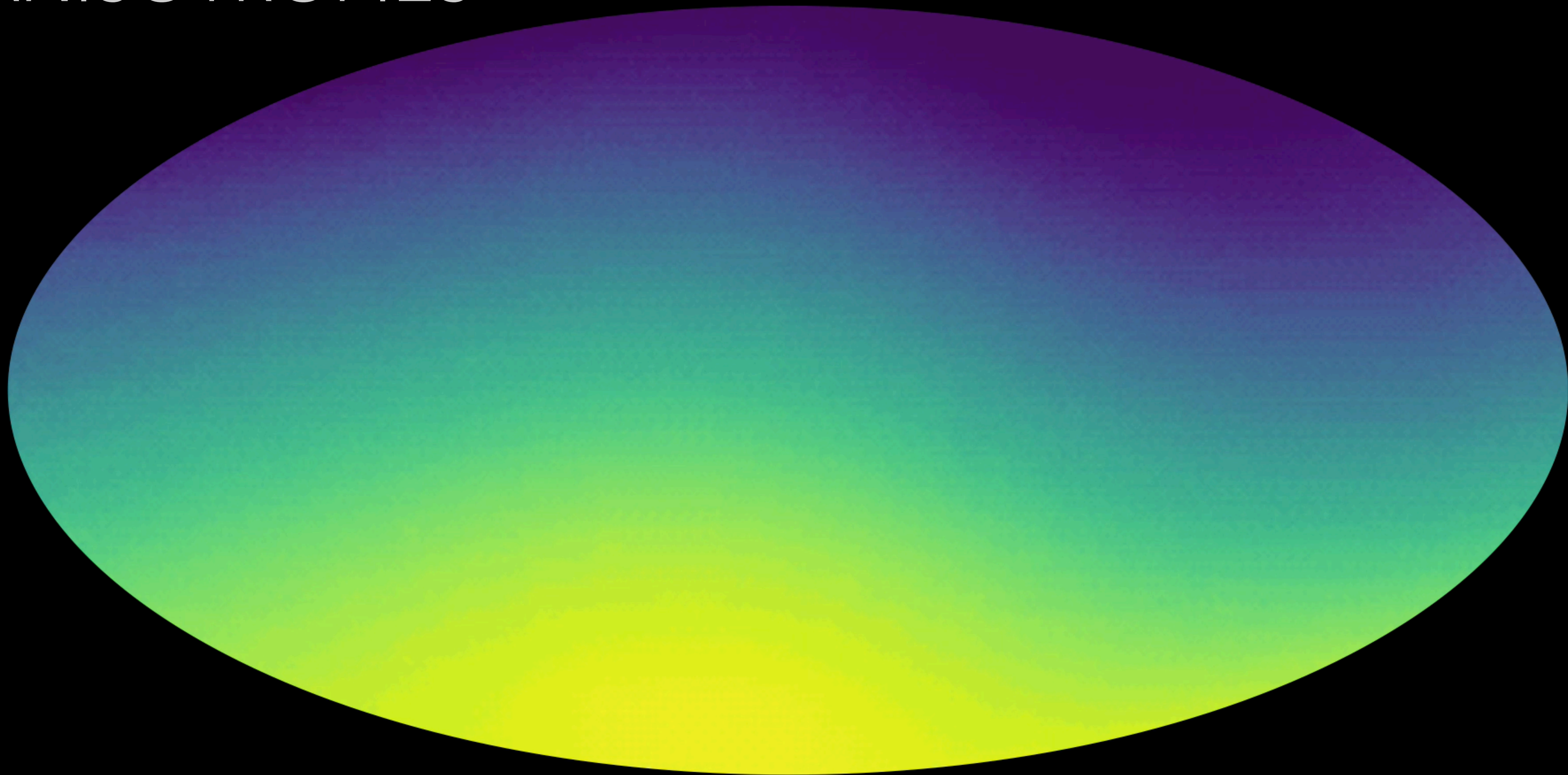
what now?

ANISOTROPIES



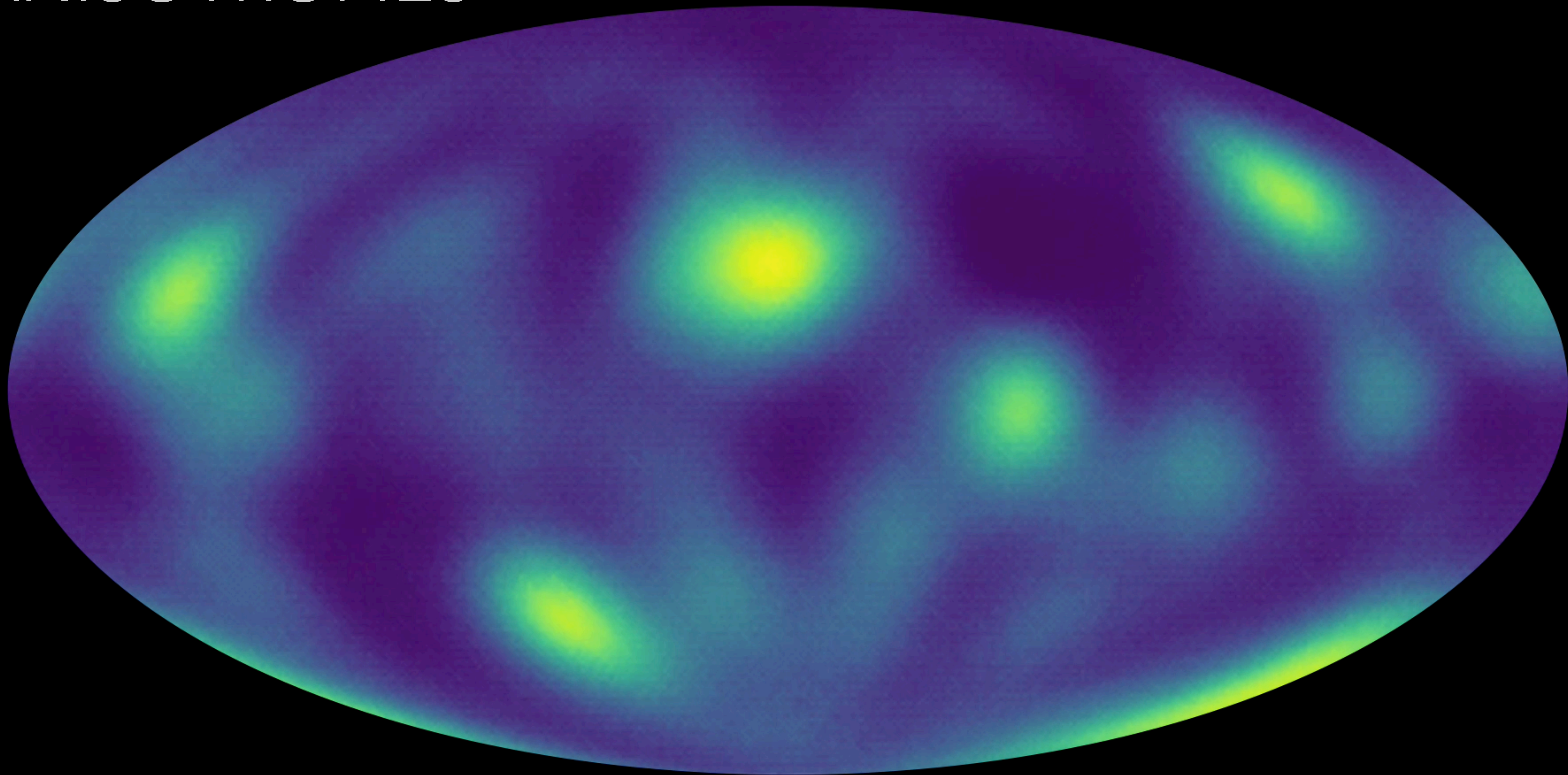
Credit: ESA/Gaia/DPAC

ANISOTROPIES

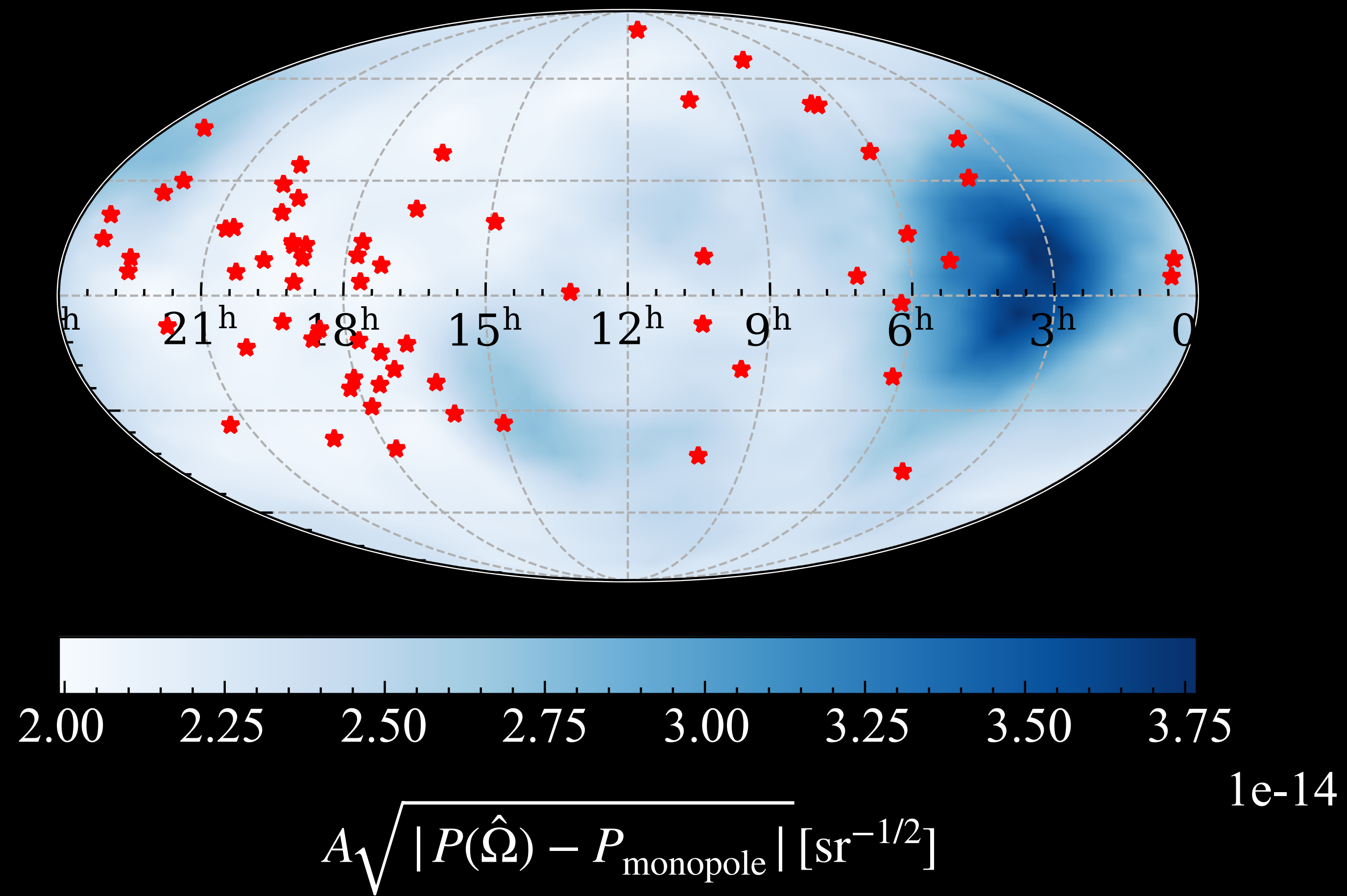


Simulated Data

ANISOTROPIES



Simulated Data



no statistically significant deviation from isotropy

THE PATH FORWARD

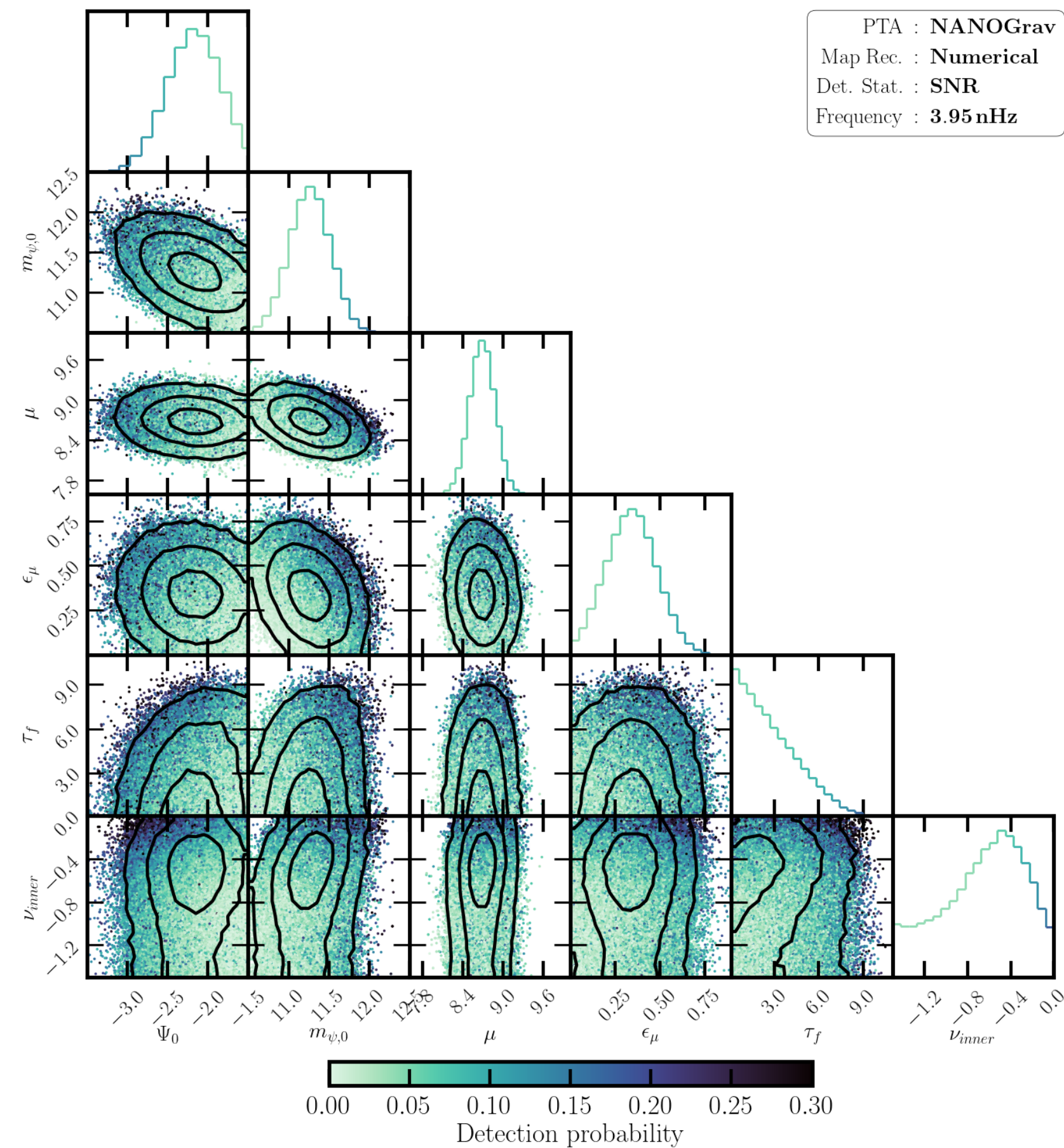
what do these null detections teach us?

└─ is there a tension between these null detections and the SMBHB interpretation of the GWB?

THE PATH FORWARD

what do these null detections teach us?

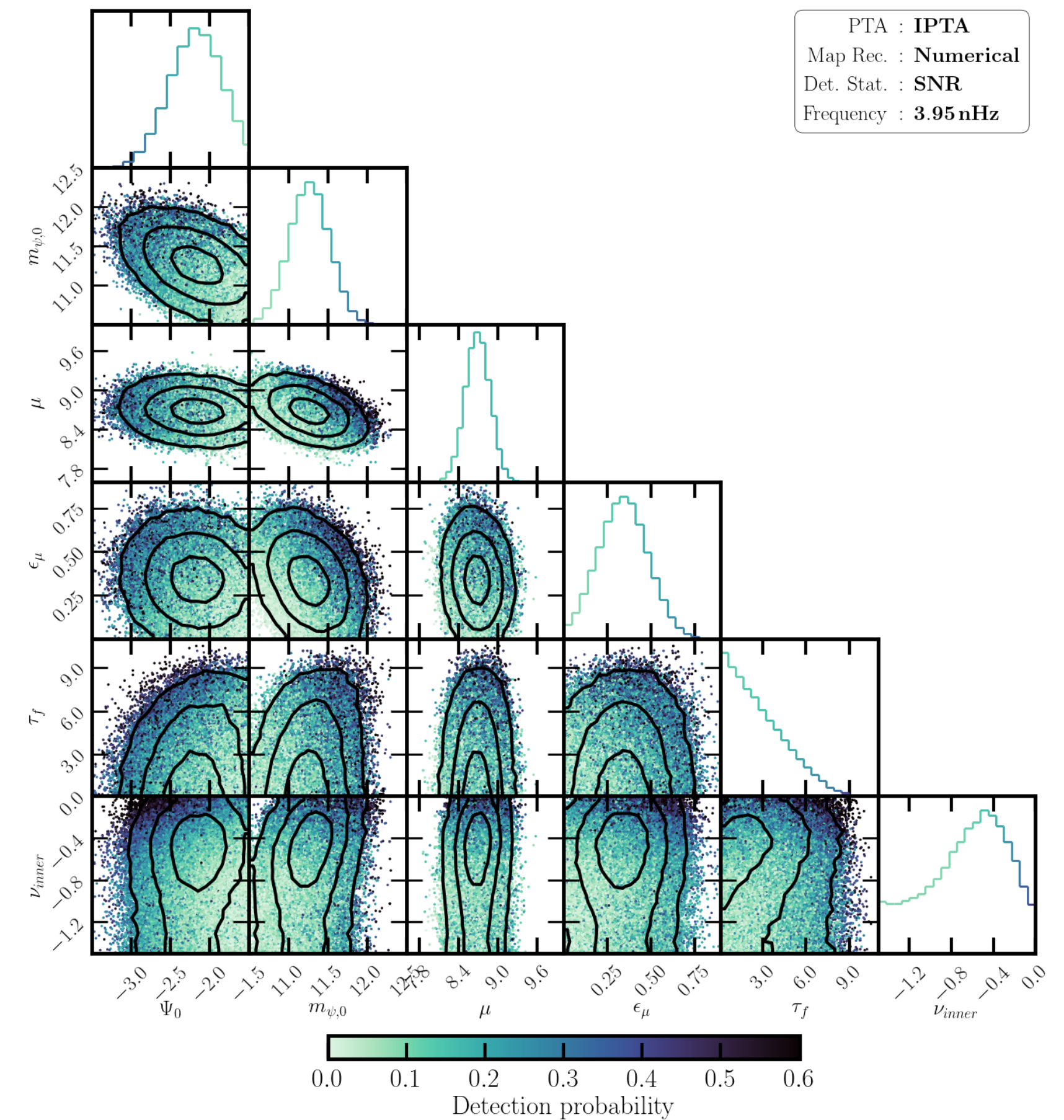
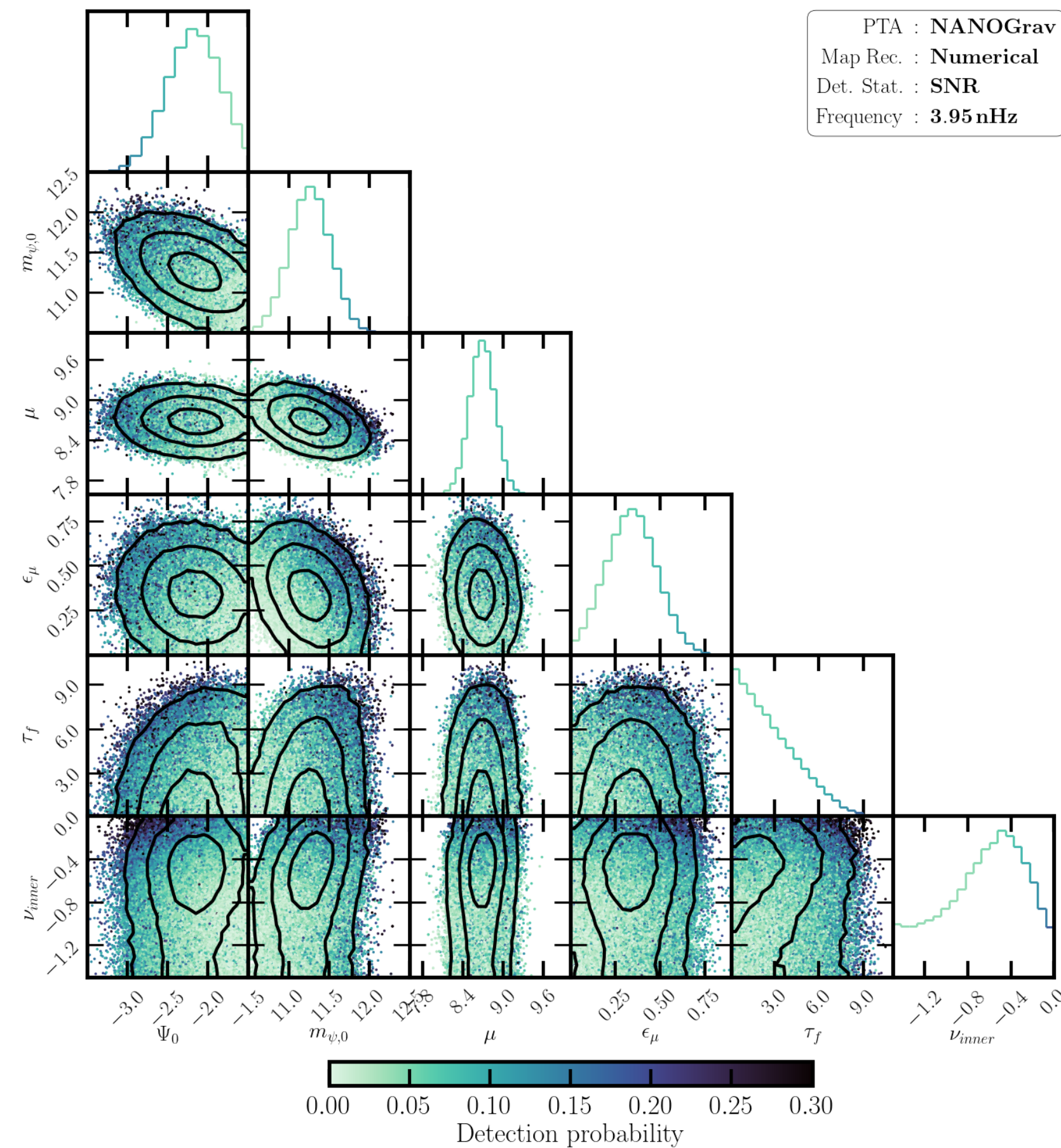
└→ is there a tension between these null detections and the SMBHB interpretation of the GWB? **No**
Lemke, **AM**, Gersbach, "*Detecting Gravitational Wave Anisotropies from Supermassive Black Hole Binaries*", PRD 111, 6 (2025)



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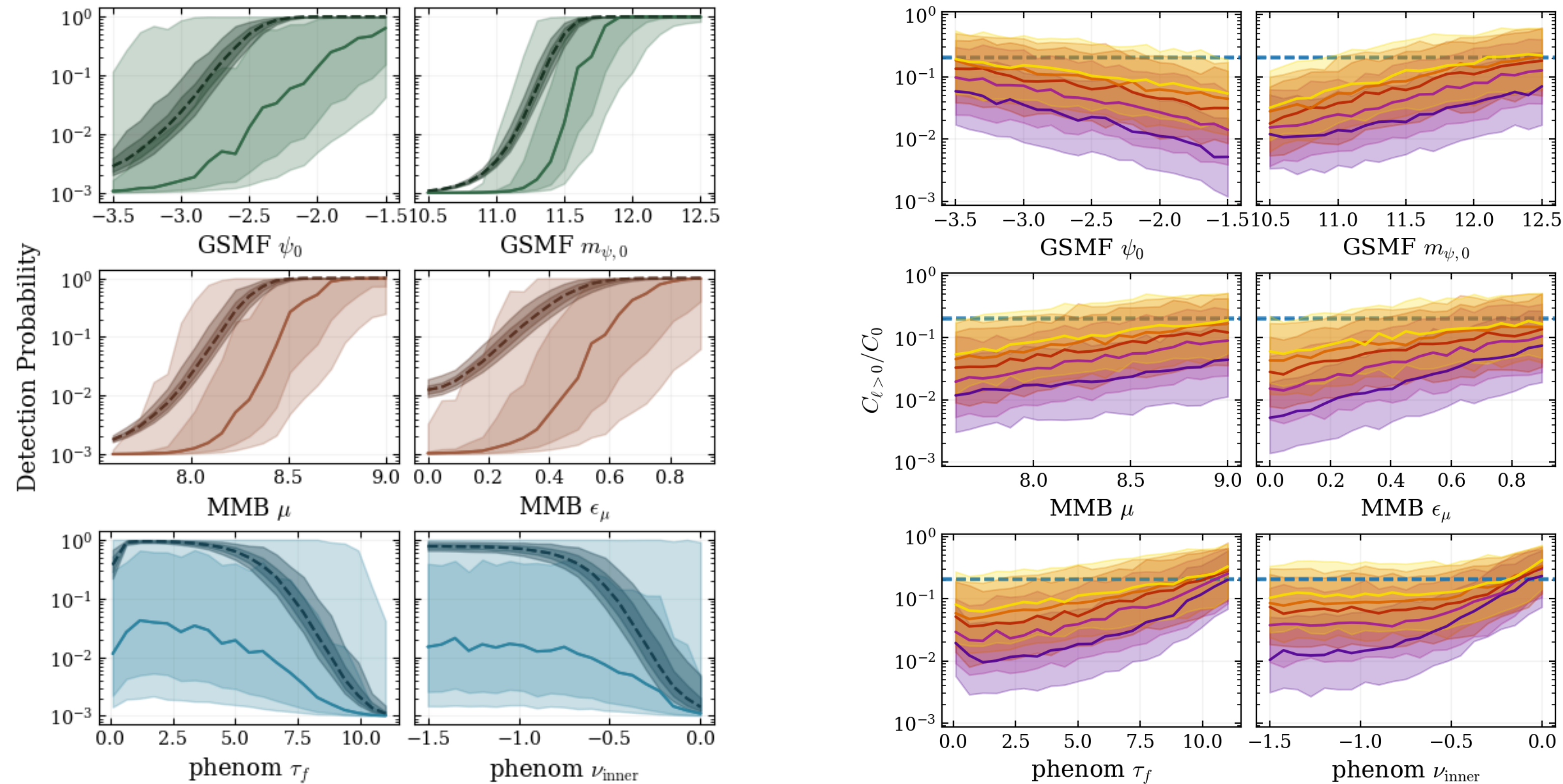
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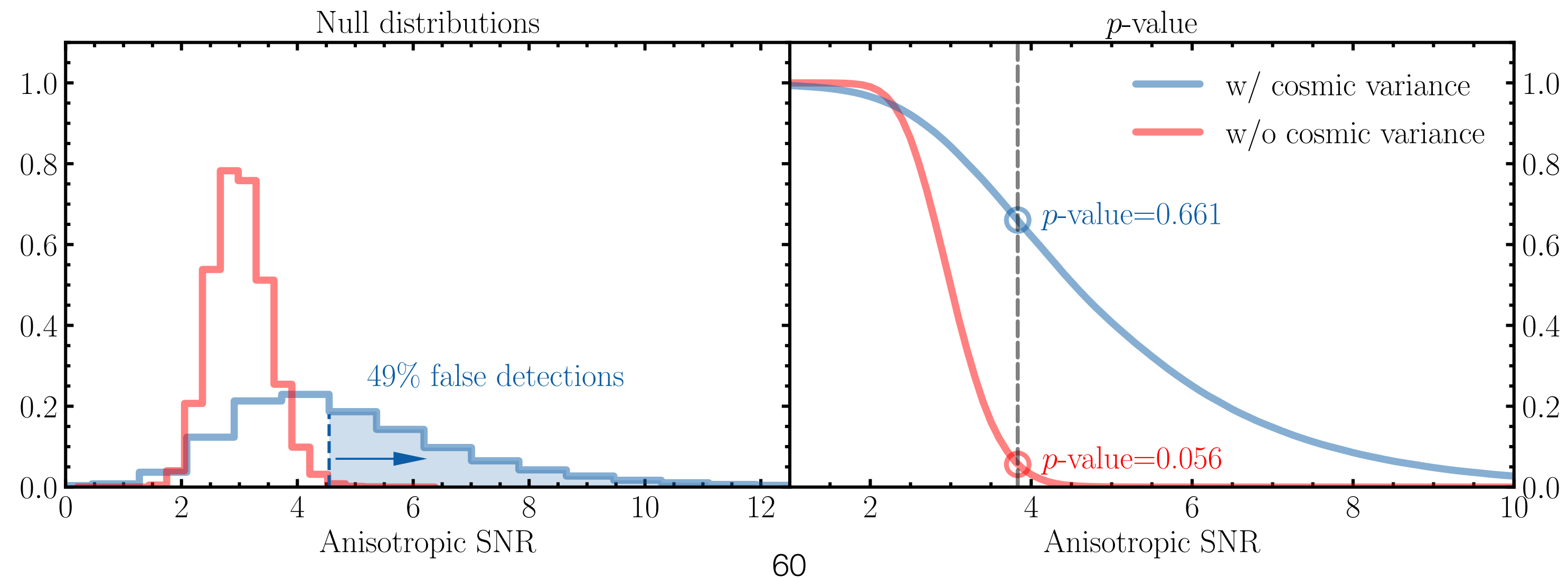
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new data is coming

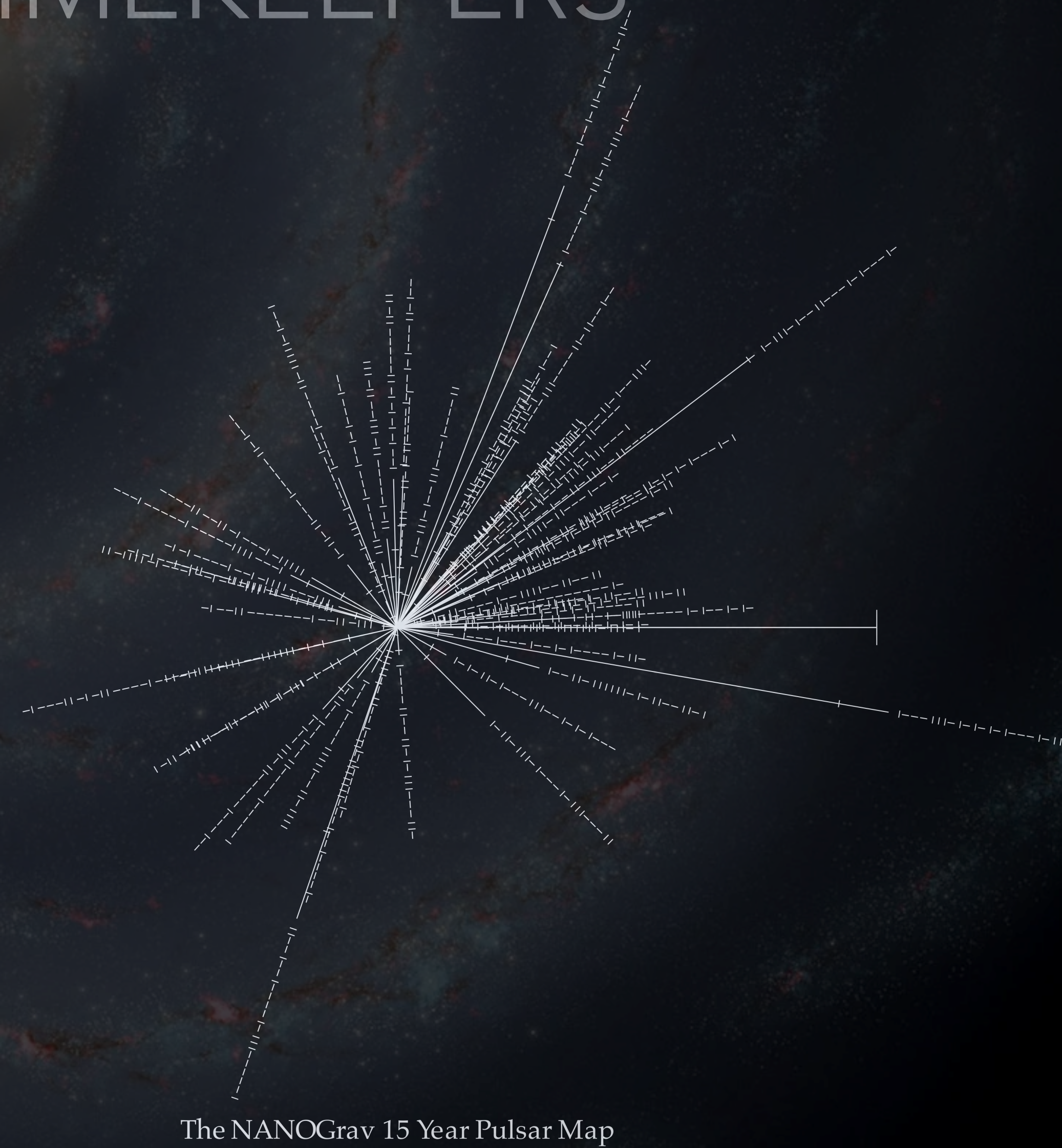
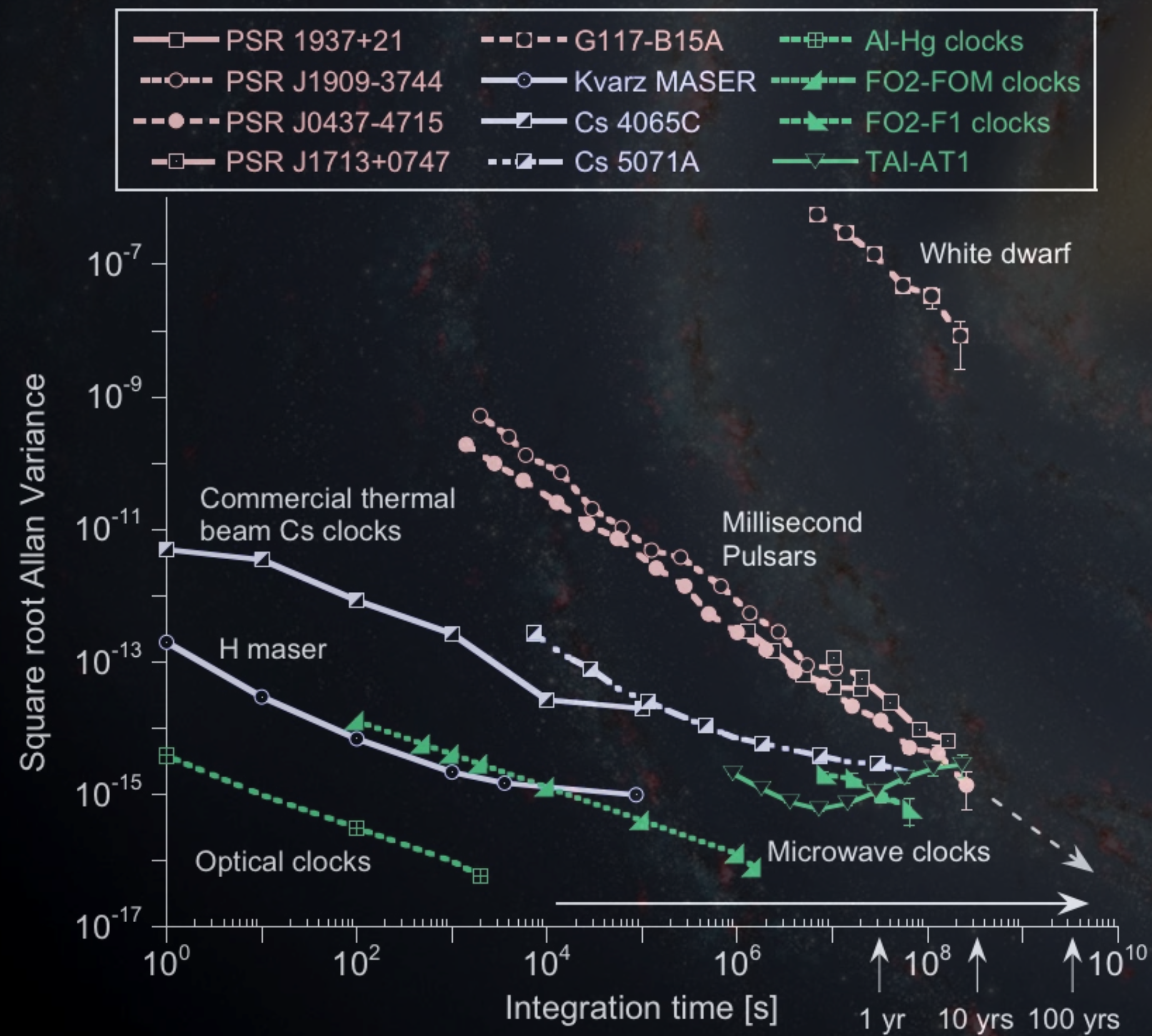
→ NANOGrav 20-year data set. **Already analyzing preliminary data set.**

→ IPTA DR3. **Data combination near completion.**

PTAs are not just a GW detector

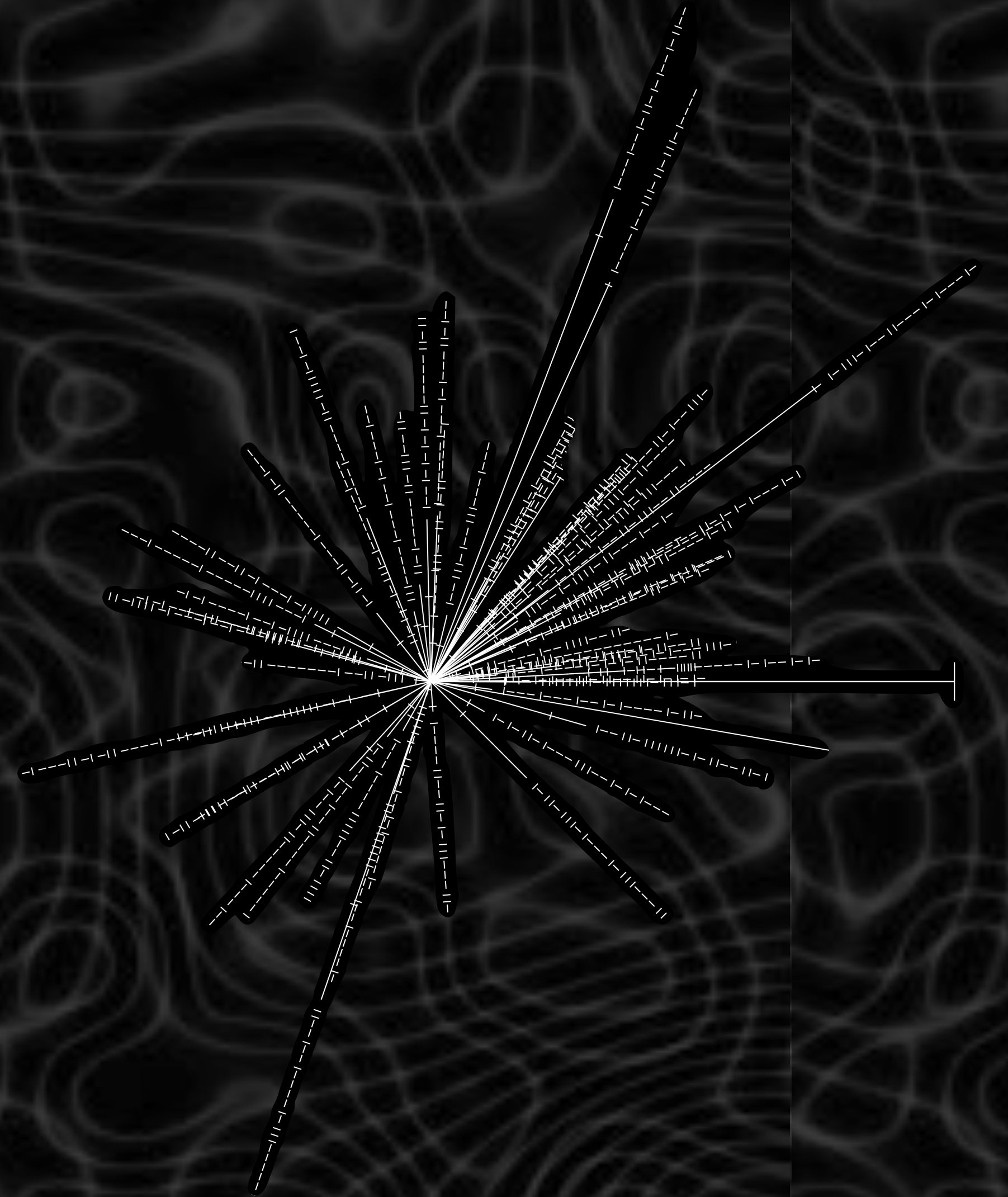
A GALACTIC NETWORK OF TIMEKEEPERS

Hartnett and Luiten [1004.0115]



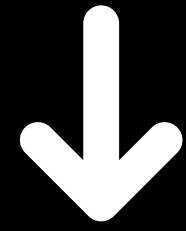
TESTS OF DM PROPERTIES

$$\phi(\vec{x}, t) = \frac{\sqrt{2\rho_\phi}}{m_\phi} \hat{\phi}(\vec{x}) \cos(m_\phi t + \gamma(\vec{x}))$$

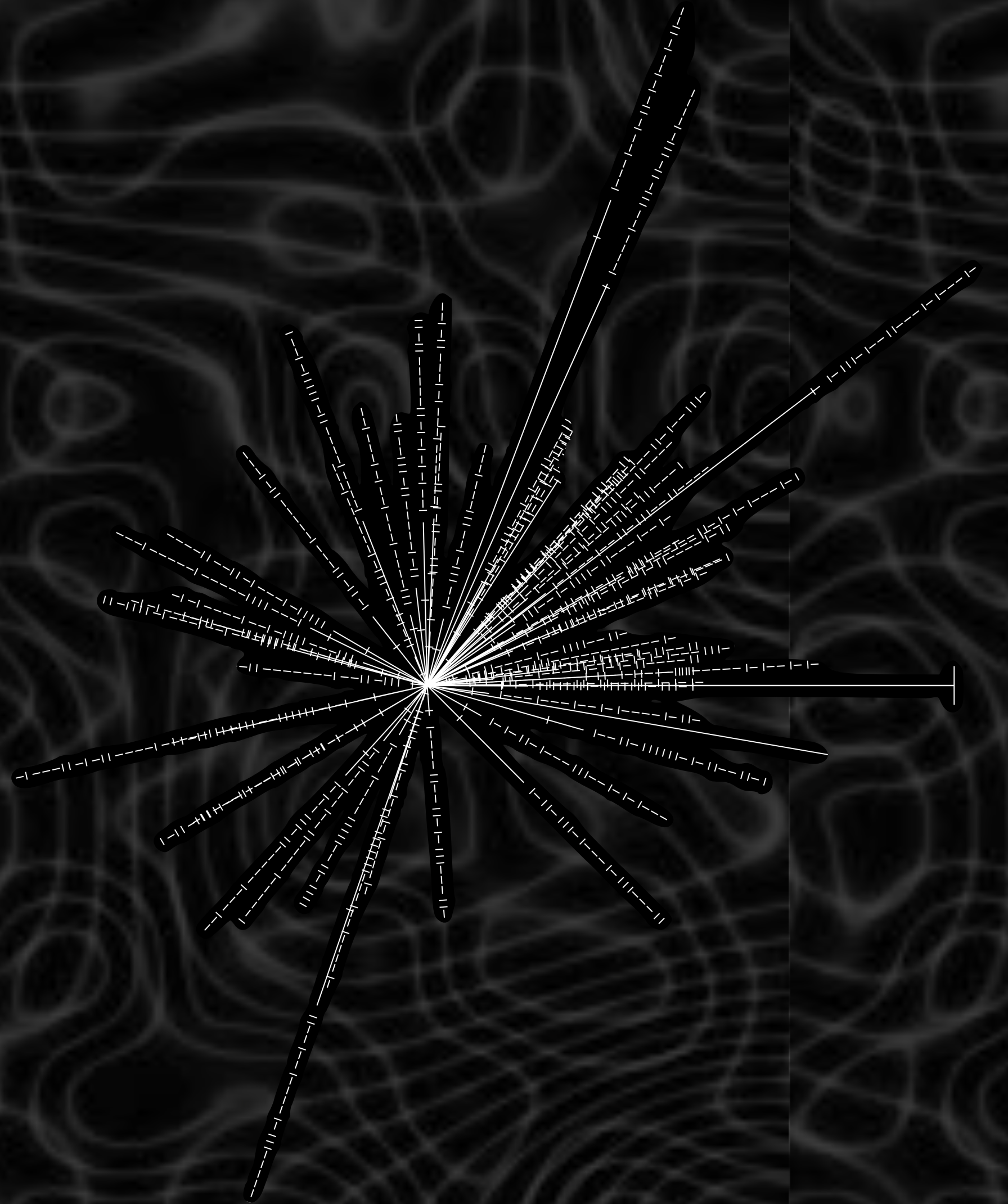


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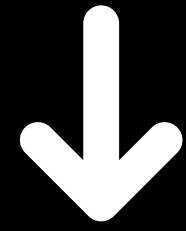


$$ds^2 = \left[1 + 2\Phi(t, \vec{x})\right] dt^2 - \left[1 - 2\Psi(t, \vec{x})\right] dx^2$$

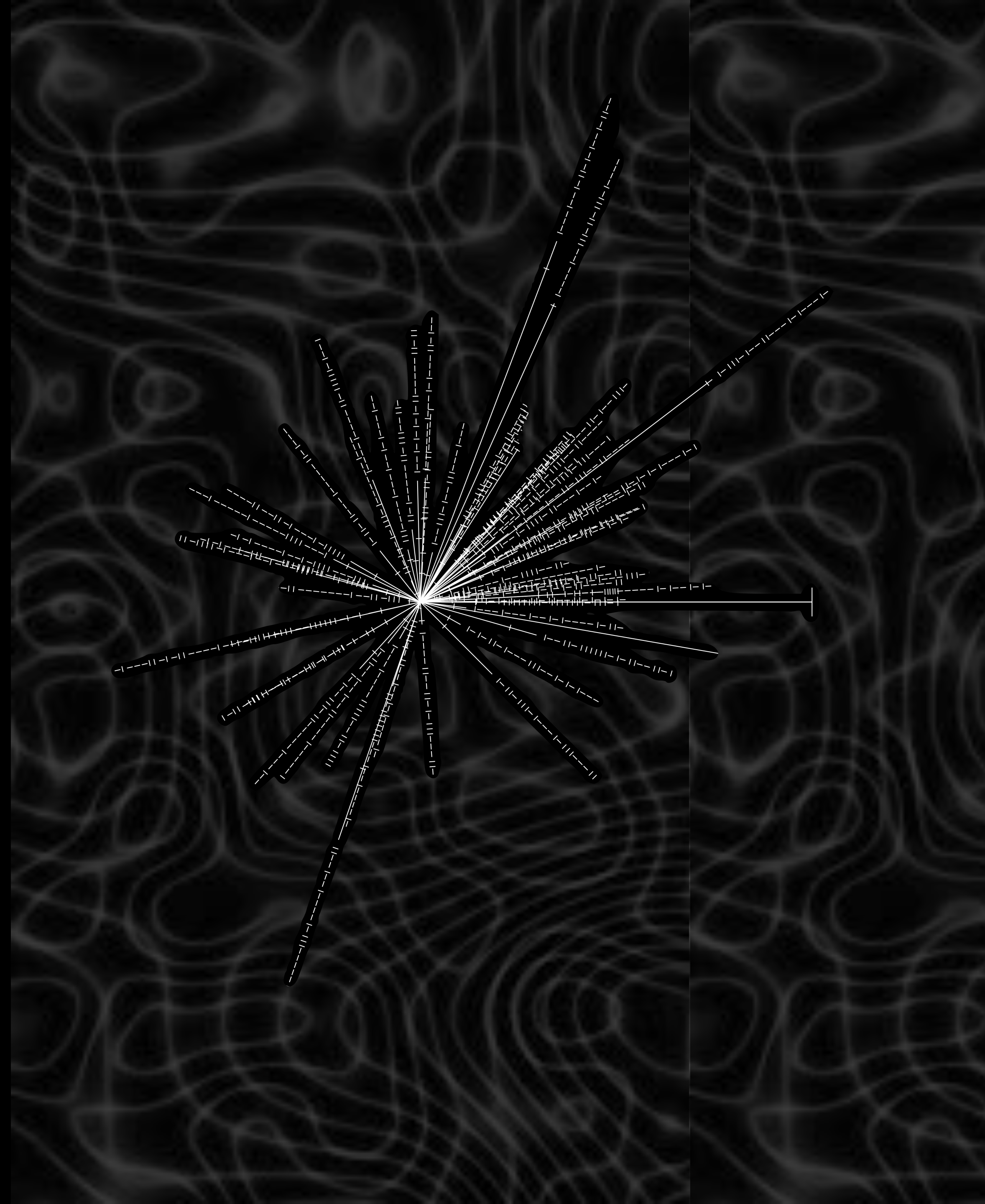
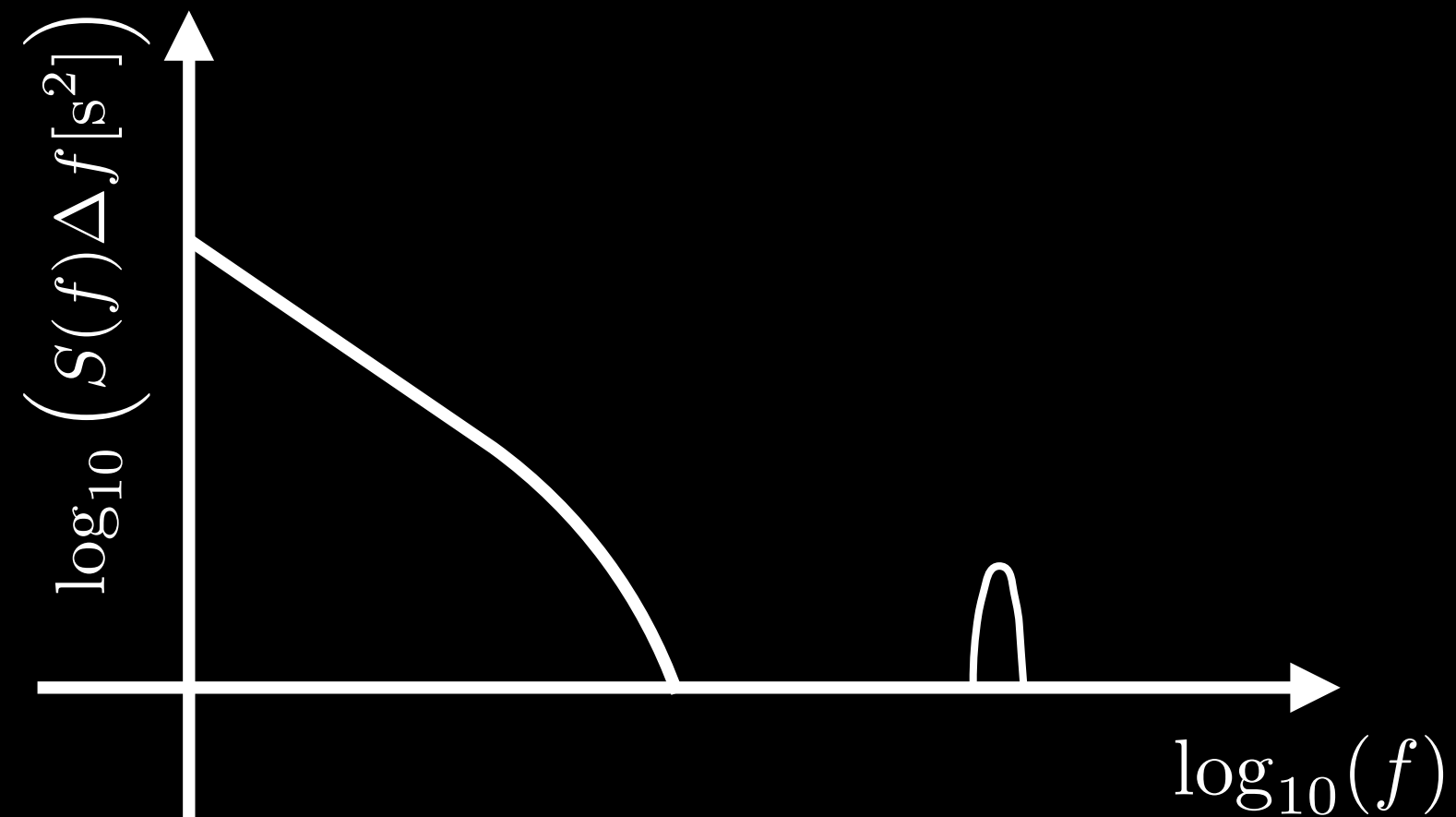
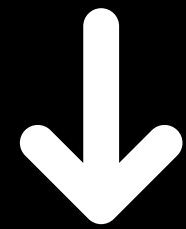


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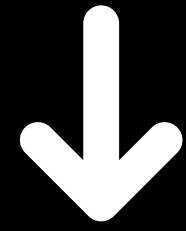


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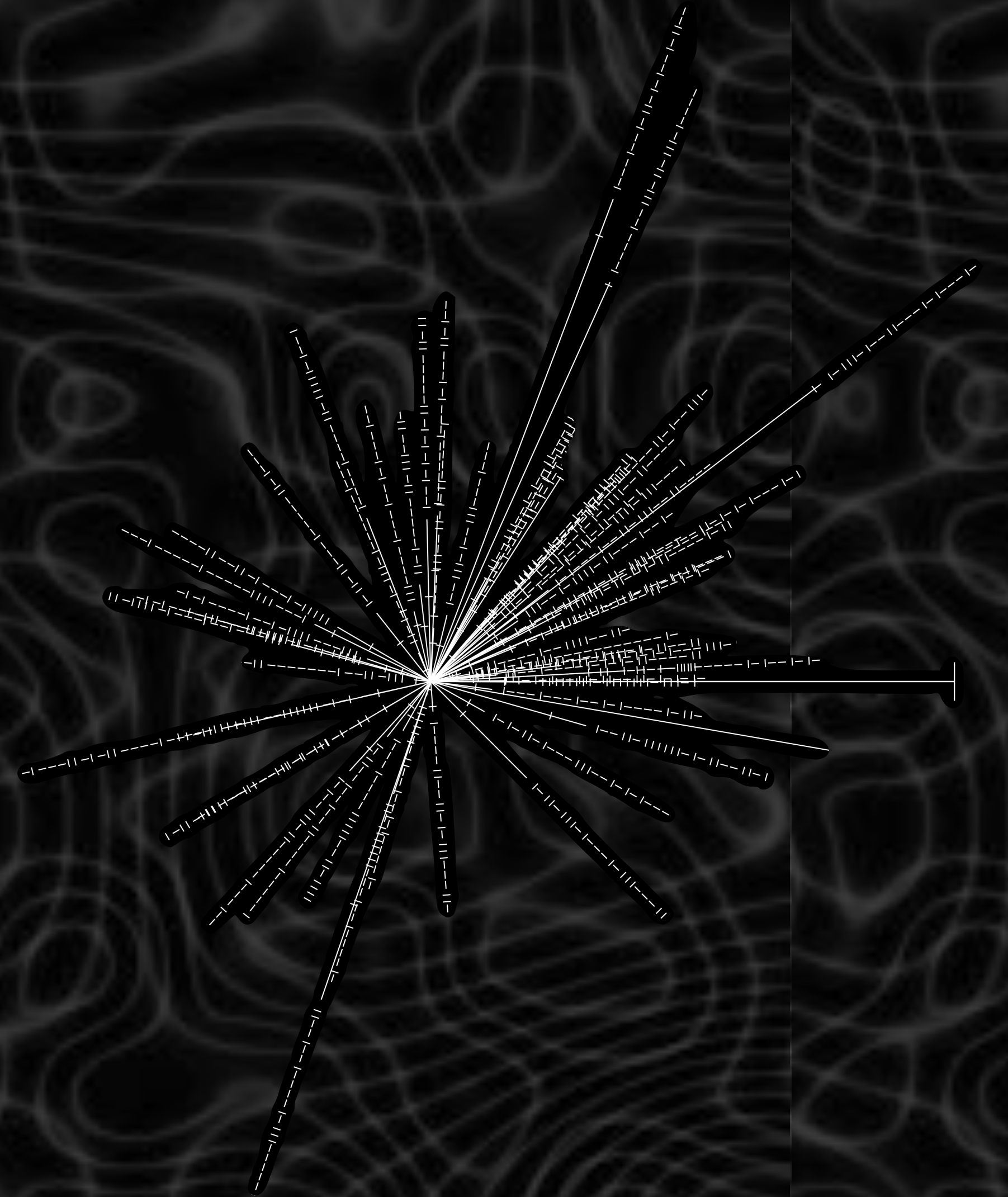
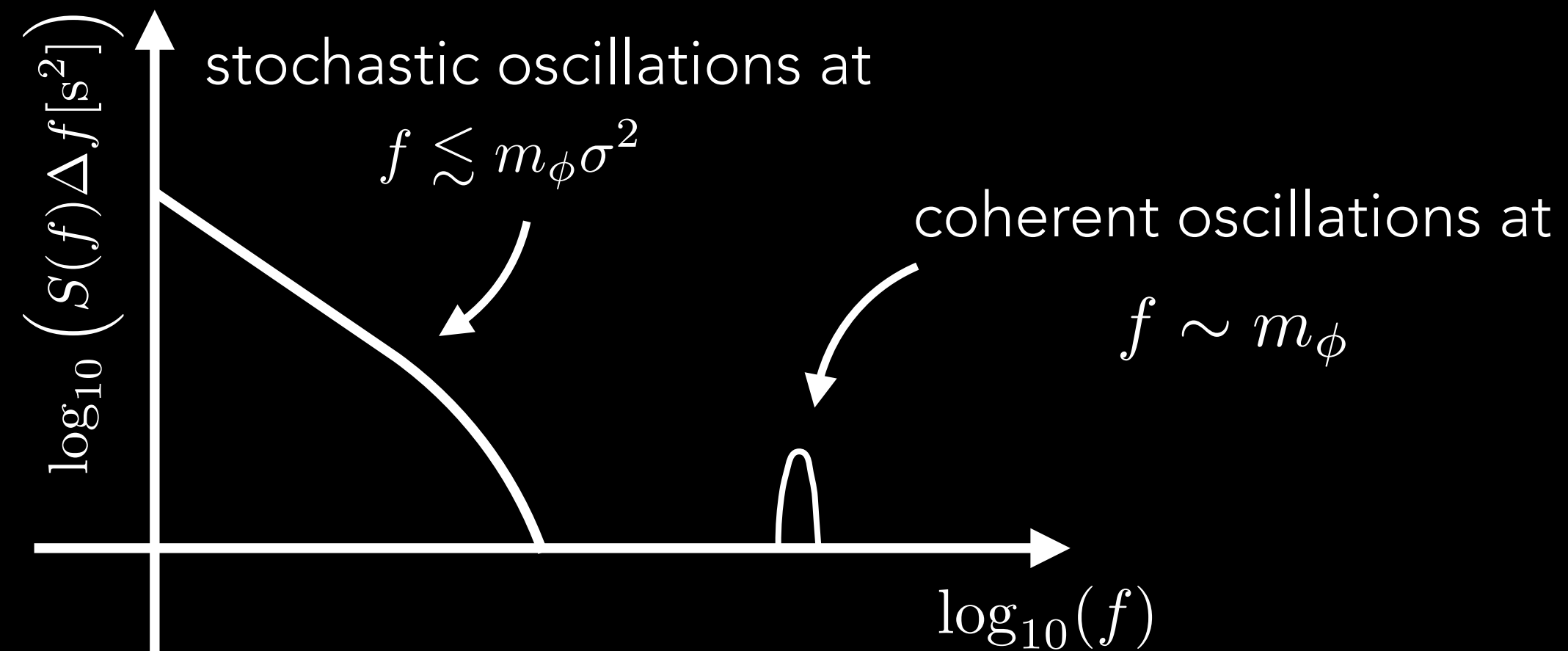
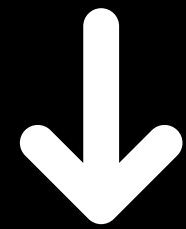


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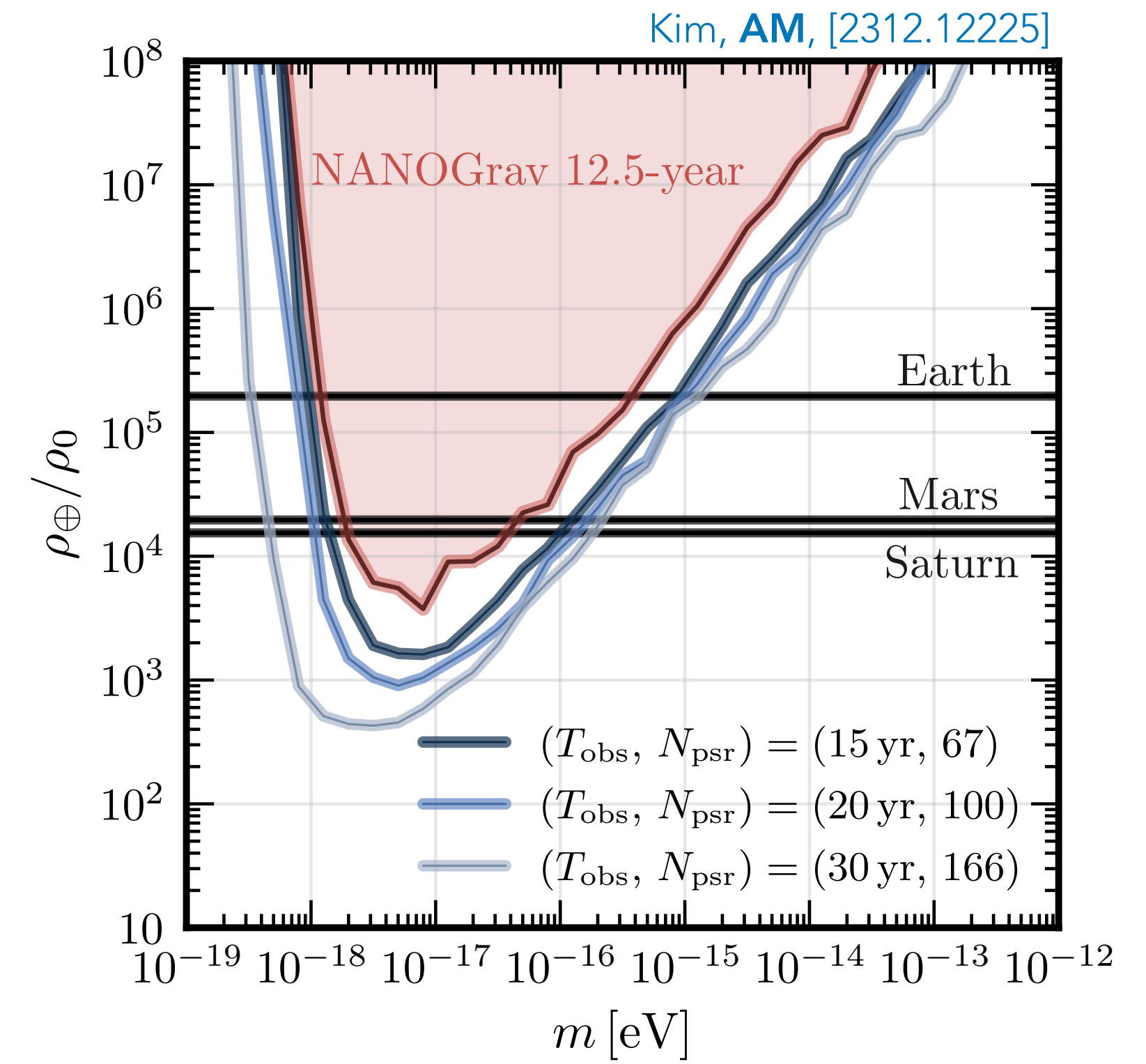
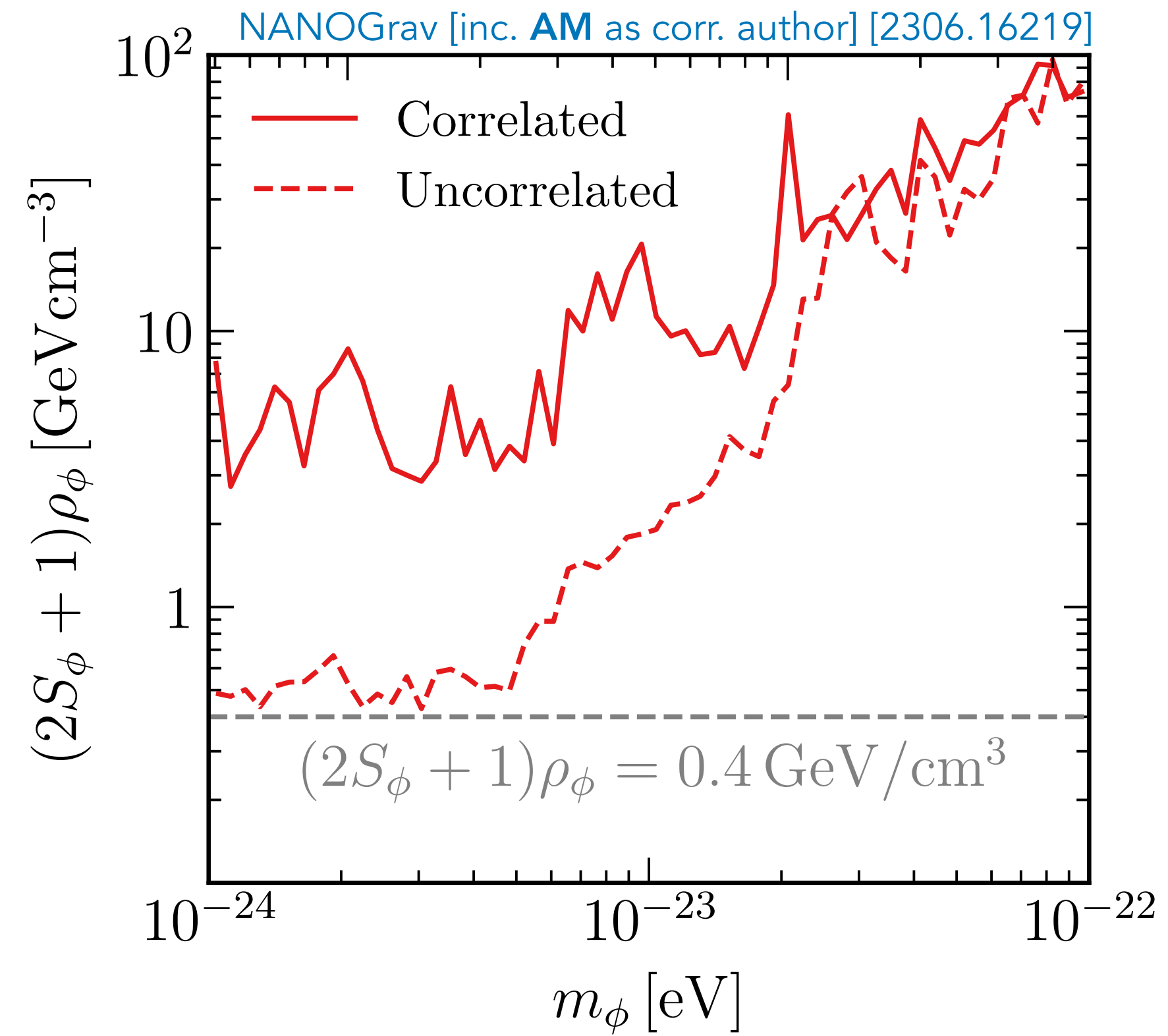
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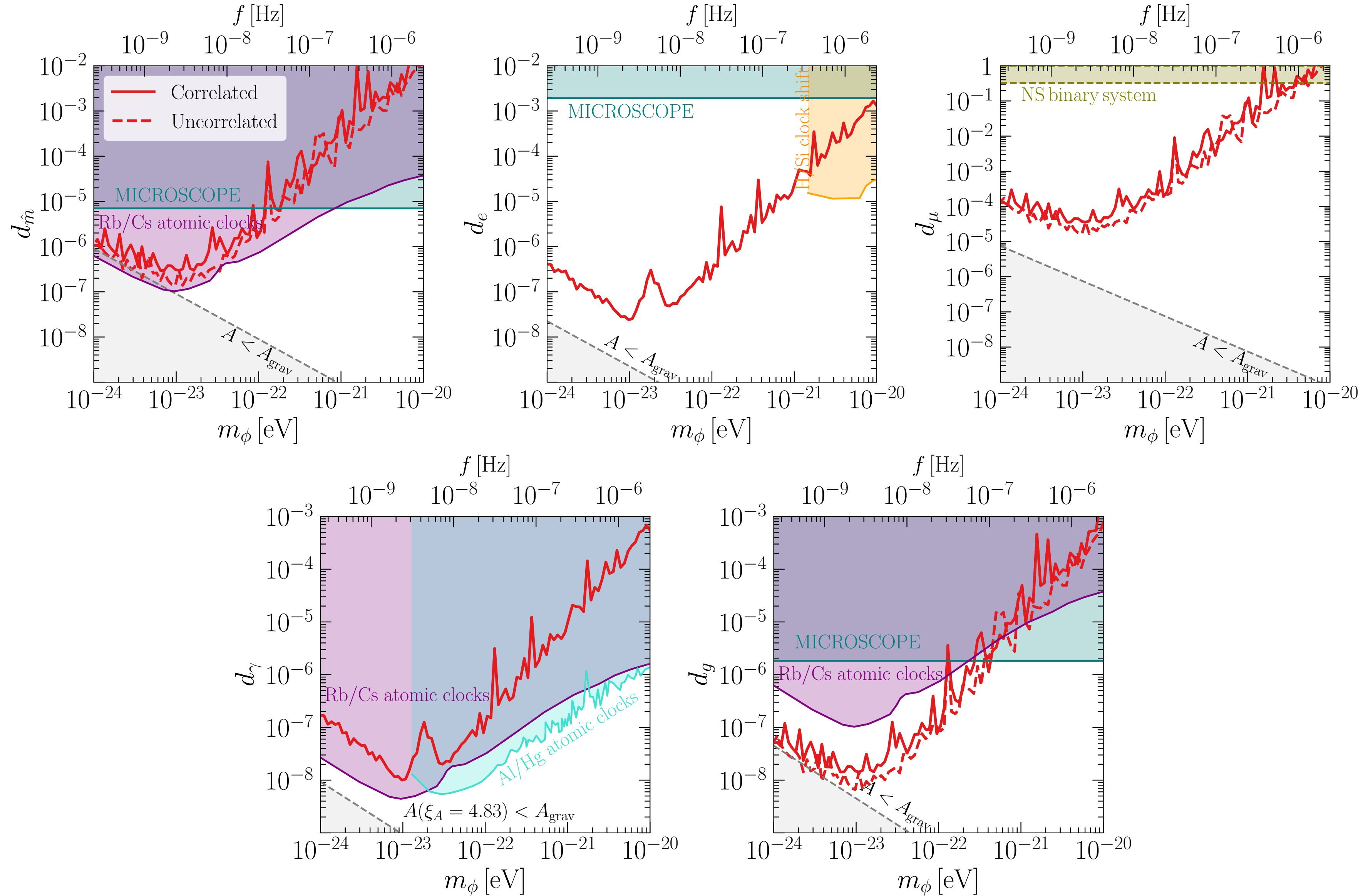
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TESTS OF DARK MATTER PROPERTIES



CLOCK SHIFTS



Kaplan, **AM**, Trickle, *"Constraining fundamental constant variations from ultralight dark matter with pulsar timing arrays"*, PRD 106 (2022)

NANOGrav [inc. **AM** as corresponding author], *"The NANOGrav 15yr Data Set: Search for Signals from New Physics"*, ApJL 951, L11 (2023).

ULDM AND MUCH MORE

testing dark matter distribution within the Milky Way

- searches for dark matter substructures in the Milky Way
NANOGrav [inc. **AM** as corresponding author], *"The NANOGrav 15yr Data Set: Search for Signals from New Physics"*, ApJL 951, L11(2023).
Lee, **AM**, Trickle, Zurek, *"Probing Small-Scale Power Spectra with Pulsar Timing Arrays"*, JHEP 06 (2021)
- searches for ULDM particles in the $10^{-16} - 10^{-14}$ eV mass range
Kim, **AM**, *"Stochastic ultralight dark matter fluctuations in pulsar timing arrays"*, PRD 109 (2024)
Kim, Gan, **AM**, *"Probing Quadratically Coupled ULDM with PTAs"*, in preparation
- ALPs searches using pulsar polarization data
Xue, **AM**, Trickle, Verma *"Pulsar Polarization Array Limits on Ultralight Axion-like Dark Matter from the NANOGrav collaboration"*, in preparation

tests of dark matter density profiles

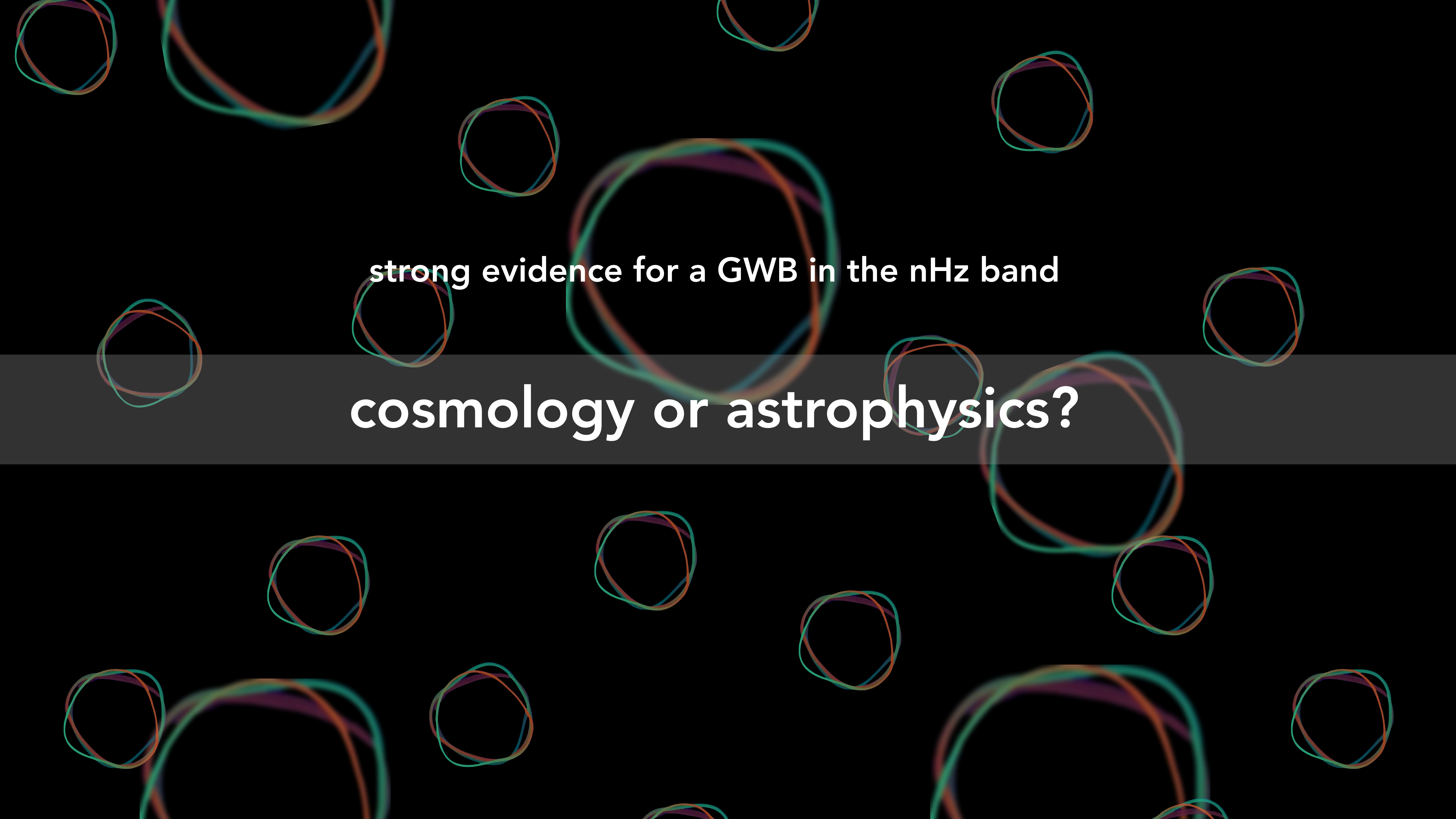
- dark matter effects on SMBHB orbital evolution
NANOGrav [inc. **AM**], *"Galaxy Tomography with the Gravitational Wave Background from Supermassive Black Hole Binaries"*, [arXiv:2411.05906]

tests of GR

- constraints on the graviton mass
Cordes, **AM**, Schmitz, Schröder, Wassner *"On the overlap reduction function of pulsar timing array searches for gravitational waves in modified gravity"*, Class. Quant. Grav. 42 (2025)
- searches for additional GW polarizations
NANOGrav [inc. **AM**], *"The NANOGrav 15 yr Data Set: Search for Transverse Polarization Modes in the Gravitational-wave Background"*,

The background of the slide is black, featuring numerous overlapping circles in shades of teal, orange, and purple. These circles vary in size and are scattered across the entire frame, creating a complex, abstract pattern. A horizontal grey band is positioned across the middle of the image, containing the main text.

strong evidence for a GWB in the nHz band



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cosmology or astrophysics?



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CW and anisotropies will help us discriminating

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PTAs can help us test a wide range of NP models