

# Supermassive primordial black holes from QCD axion bubbles

Based on JCAP10(2023)049, JCAP05(2024)092.



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To build the model of primordial origin of SMBH which is consistent with observations

# Backgrounds

# Supermassive Black Hole (SMBH)

- SMBH= $\mathcal{O}(10^6) M_{\odot}$  black holes, which are frequently observed at the center of galaxy.

- Quite large SMBHs (e.g.  $10^{7-9} M_{\odot}$ ) are observed at high red shift (e.g.  $z \sim 7 - 10$ )

—————→ non-standard BH growth: super-Eddington accretion

or

non-standard BH origin: PBH

# Primordial Black Hole (PBH)

- Hypothetical black hole which is formed from overdense region in the early universe.
- Lots of motivations: DM, GW source, SMBH seed, etc.
- Formation condition: Their density contrast exceeds some threshold. [B. J. Carr(1975), Harada et. al.(2022)]

$$\delta = \frac{\rho - \rho_{BG}}{\rho_{BG}} > \mathcal{O}(1)$$

energy density :  $\rho$

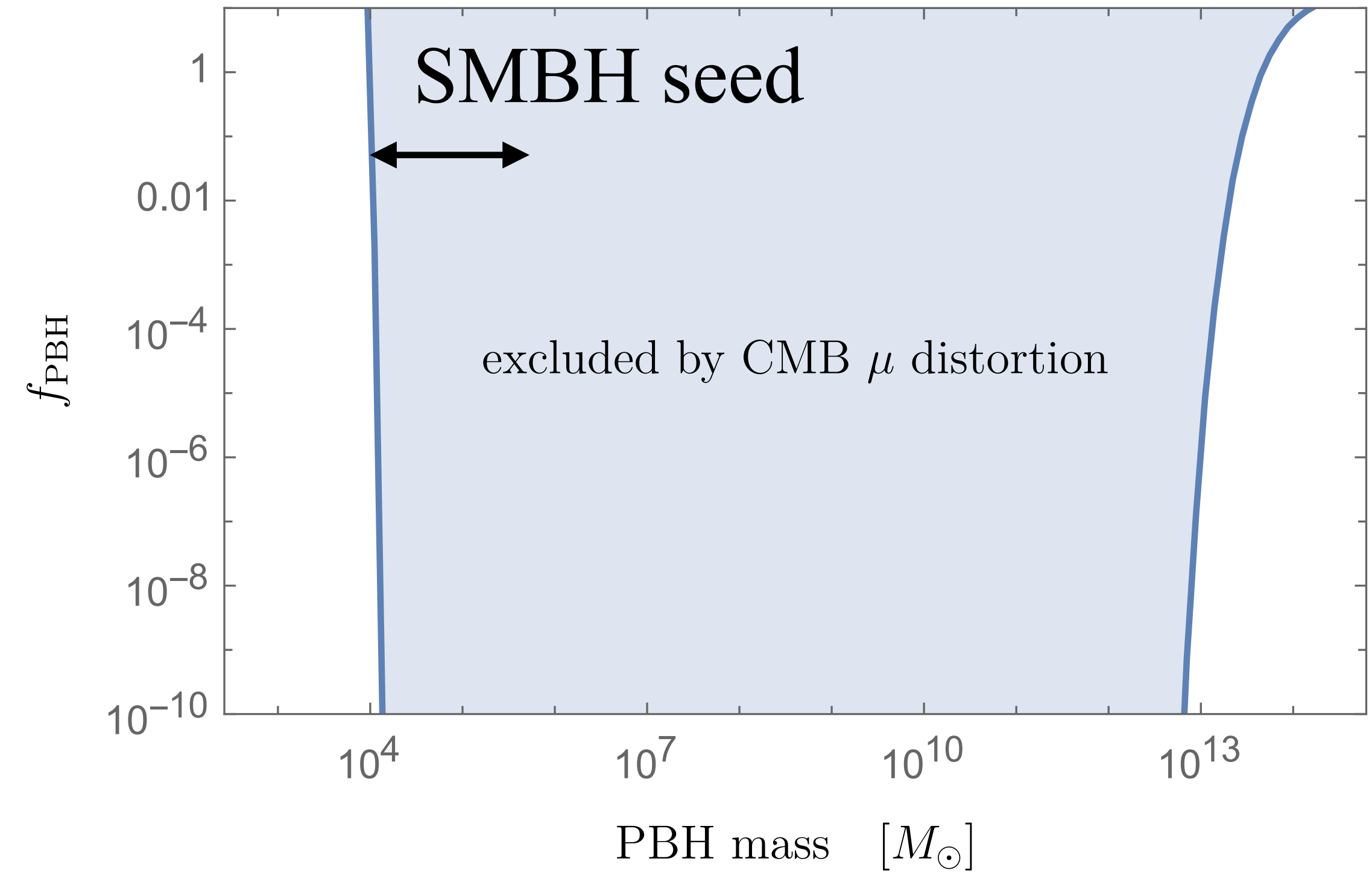
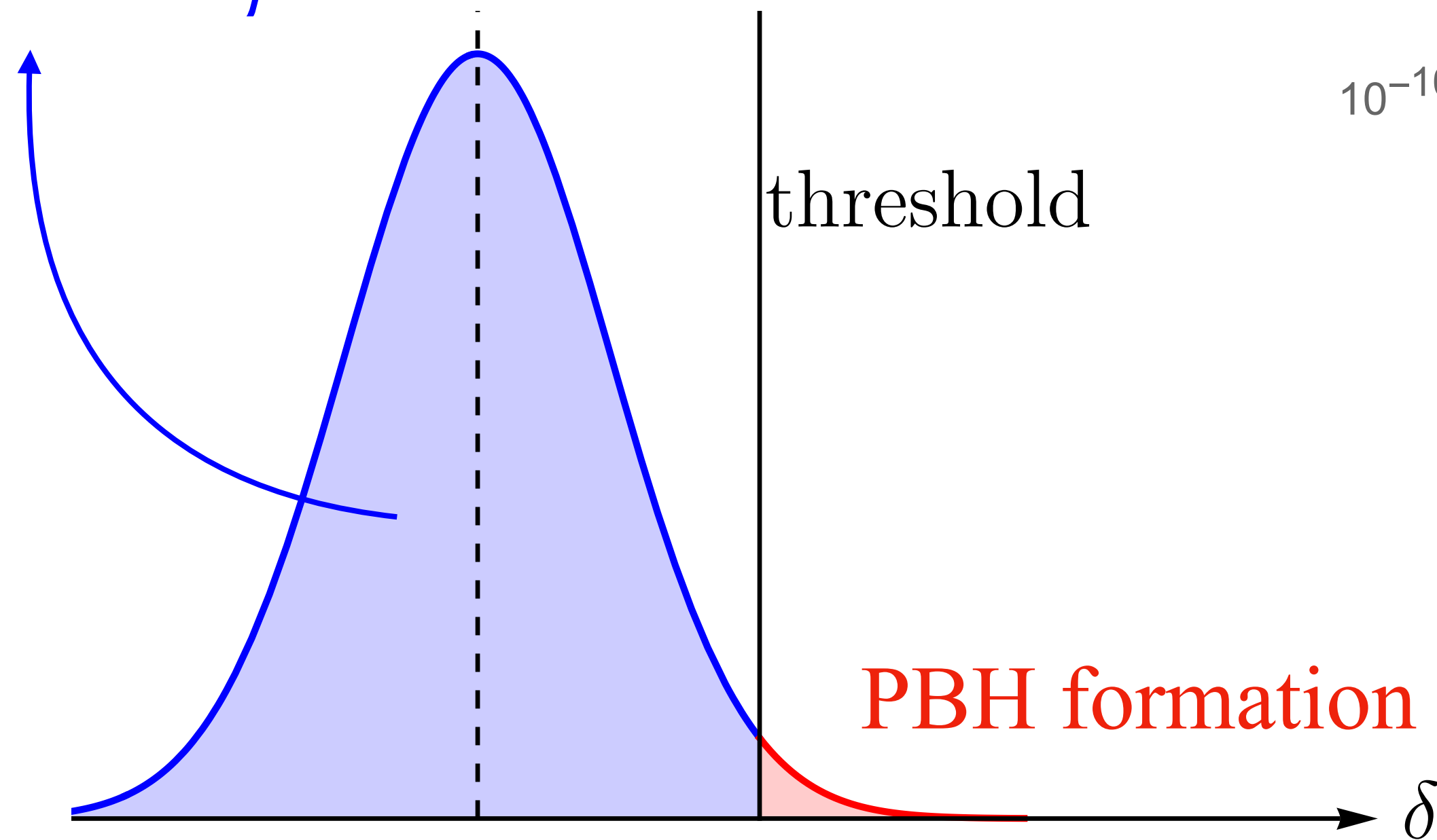
BG energy density :  $\rho_{BG}$

# Constraints on PBH

- Simplest model: PBH formation from inflationary density fluctuations

→ Gaussian density perturbation

also contribute to  $\mu$ -distortion

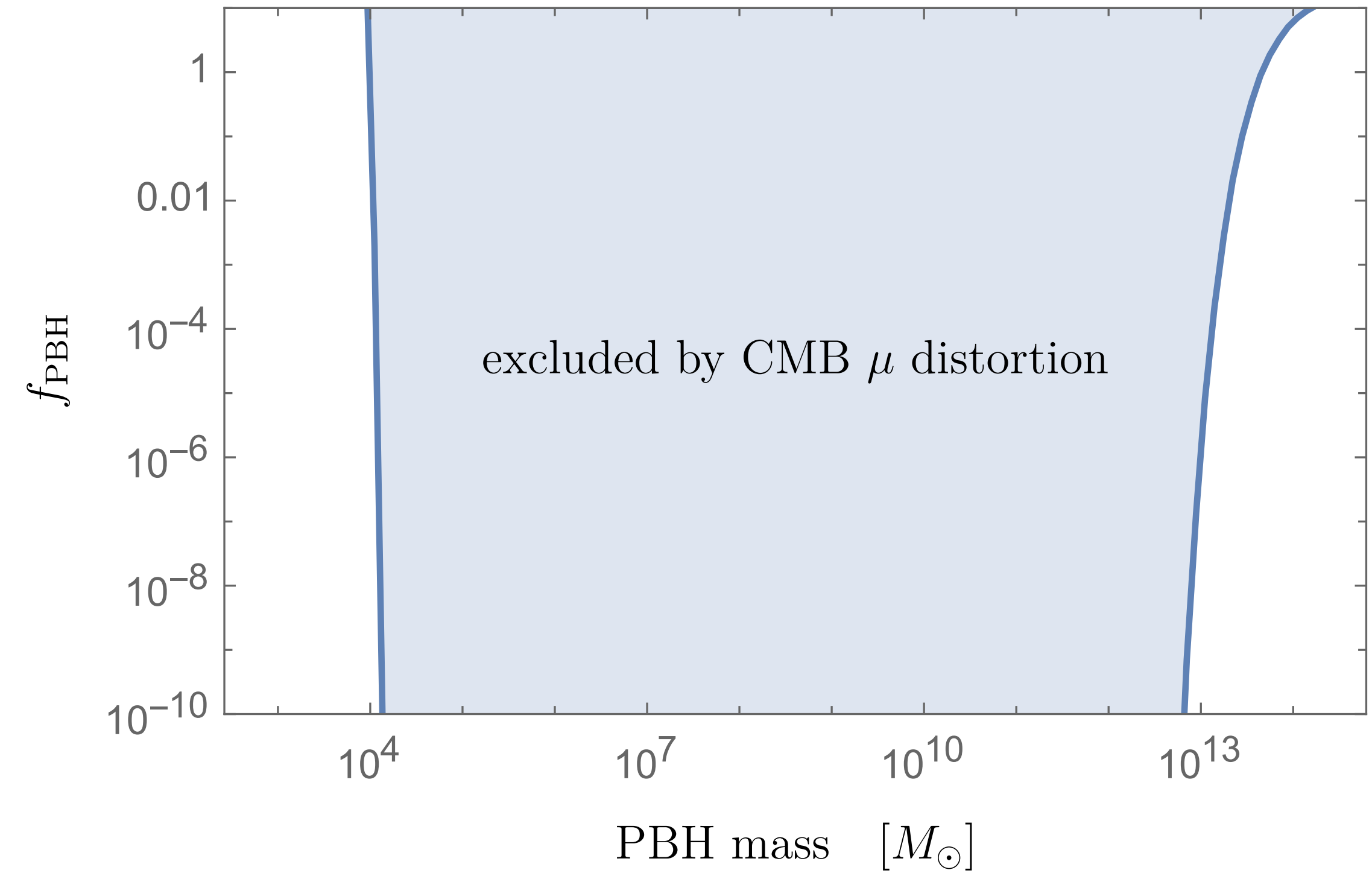
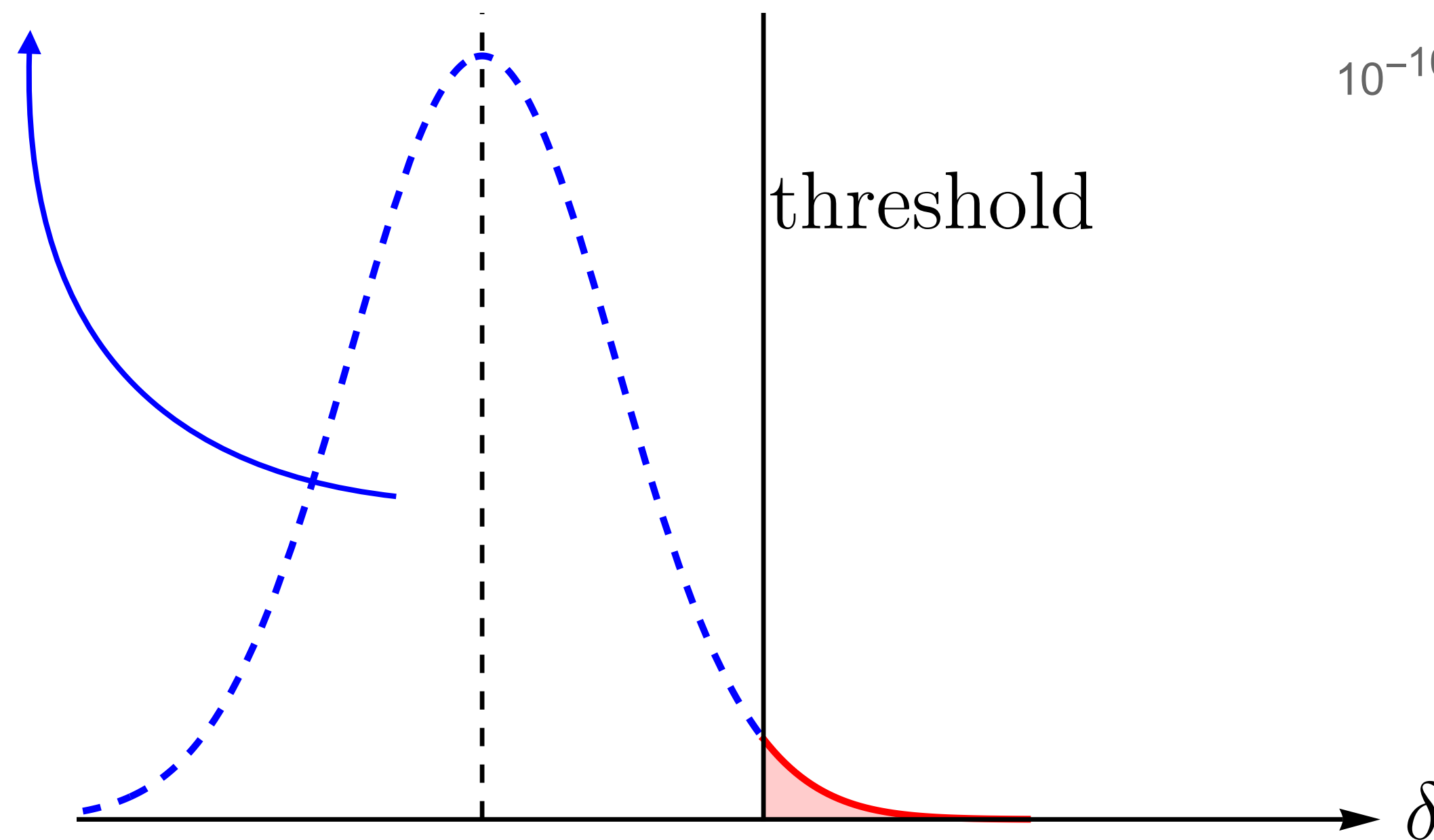


extracted from Carr et. al.(2020)

# Constraints on PBH

- PBH formation to explain SMBH seeds  
    → non-Gaussian density perturbation

no contribution to  $\mu$ -distortion



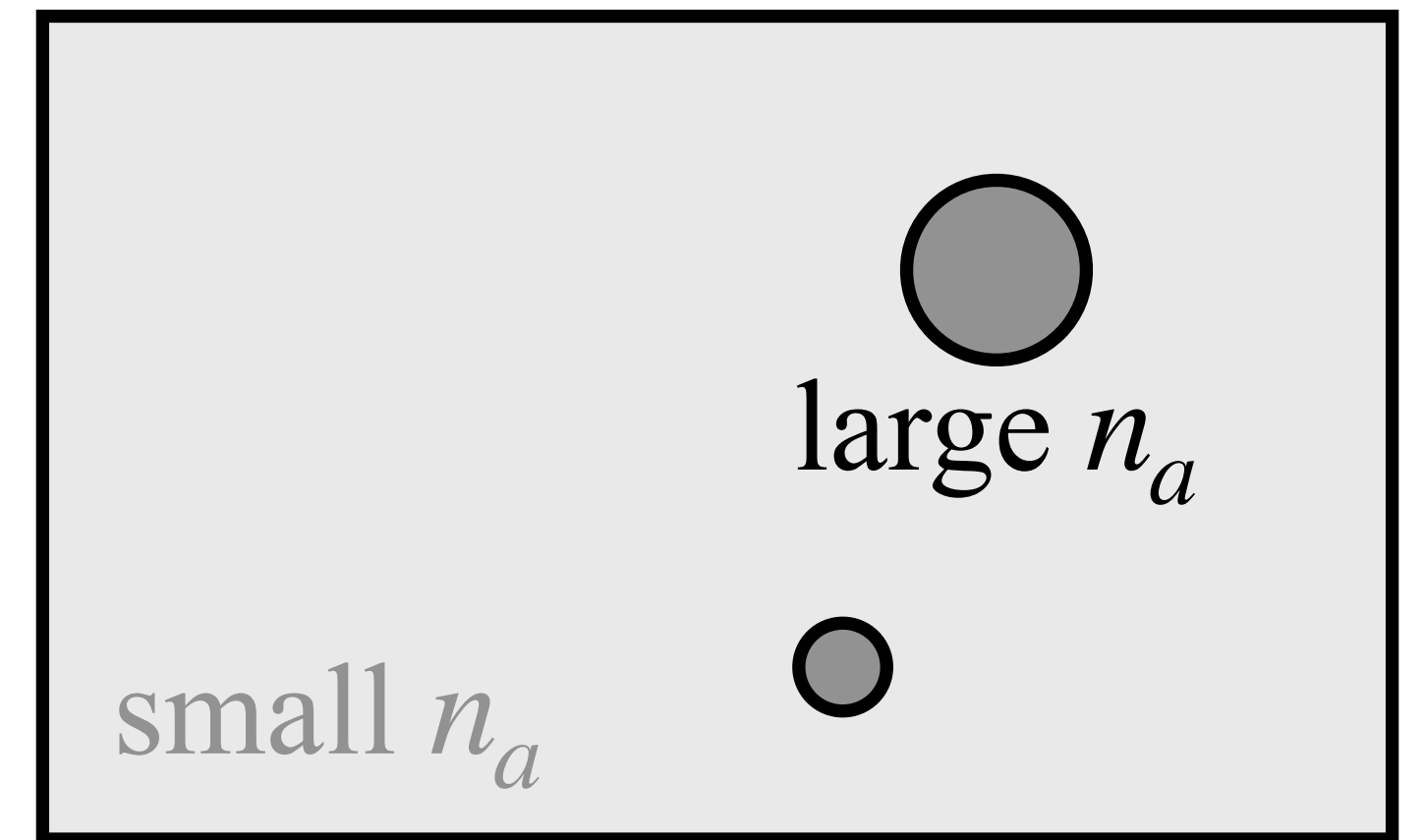
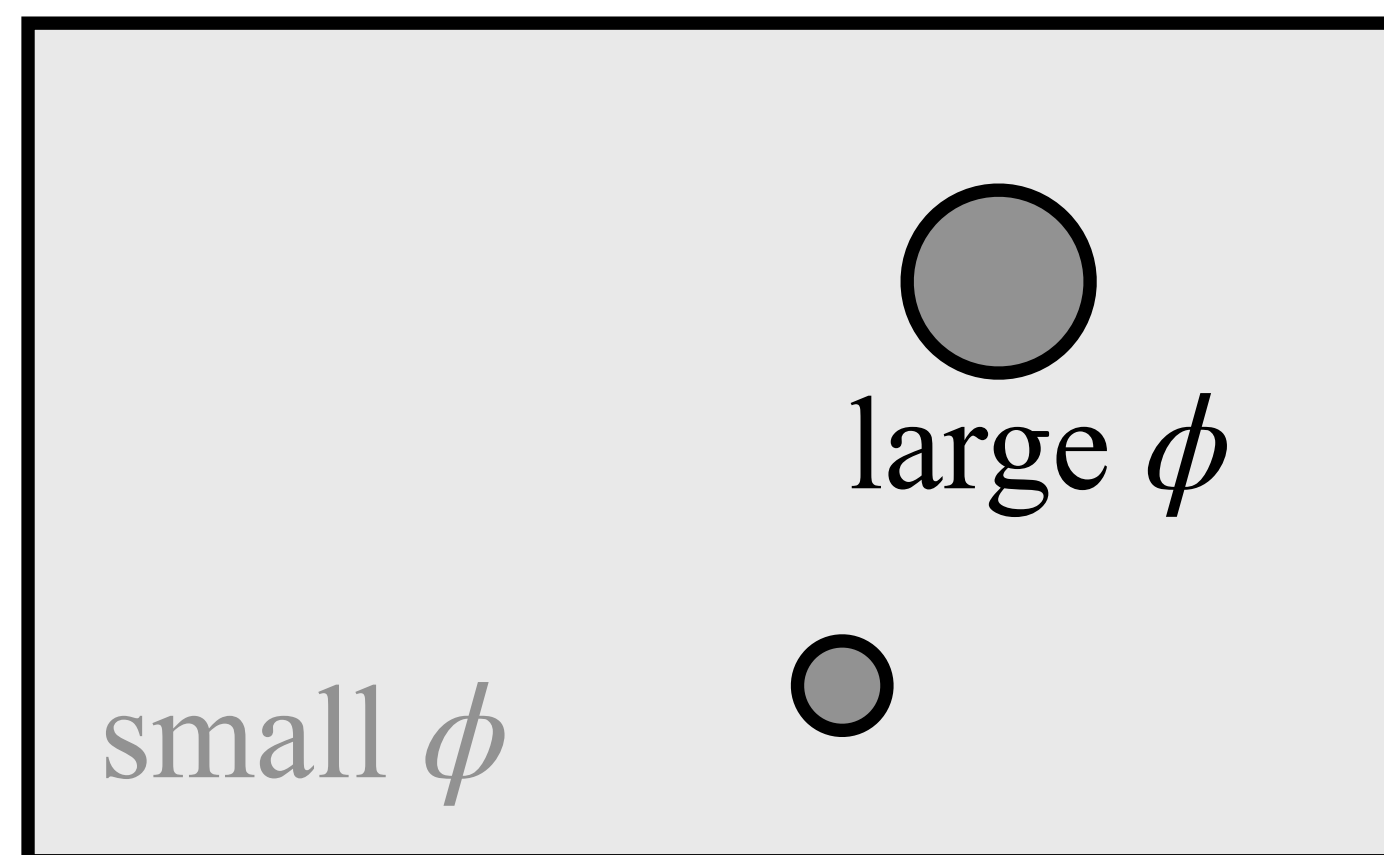
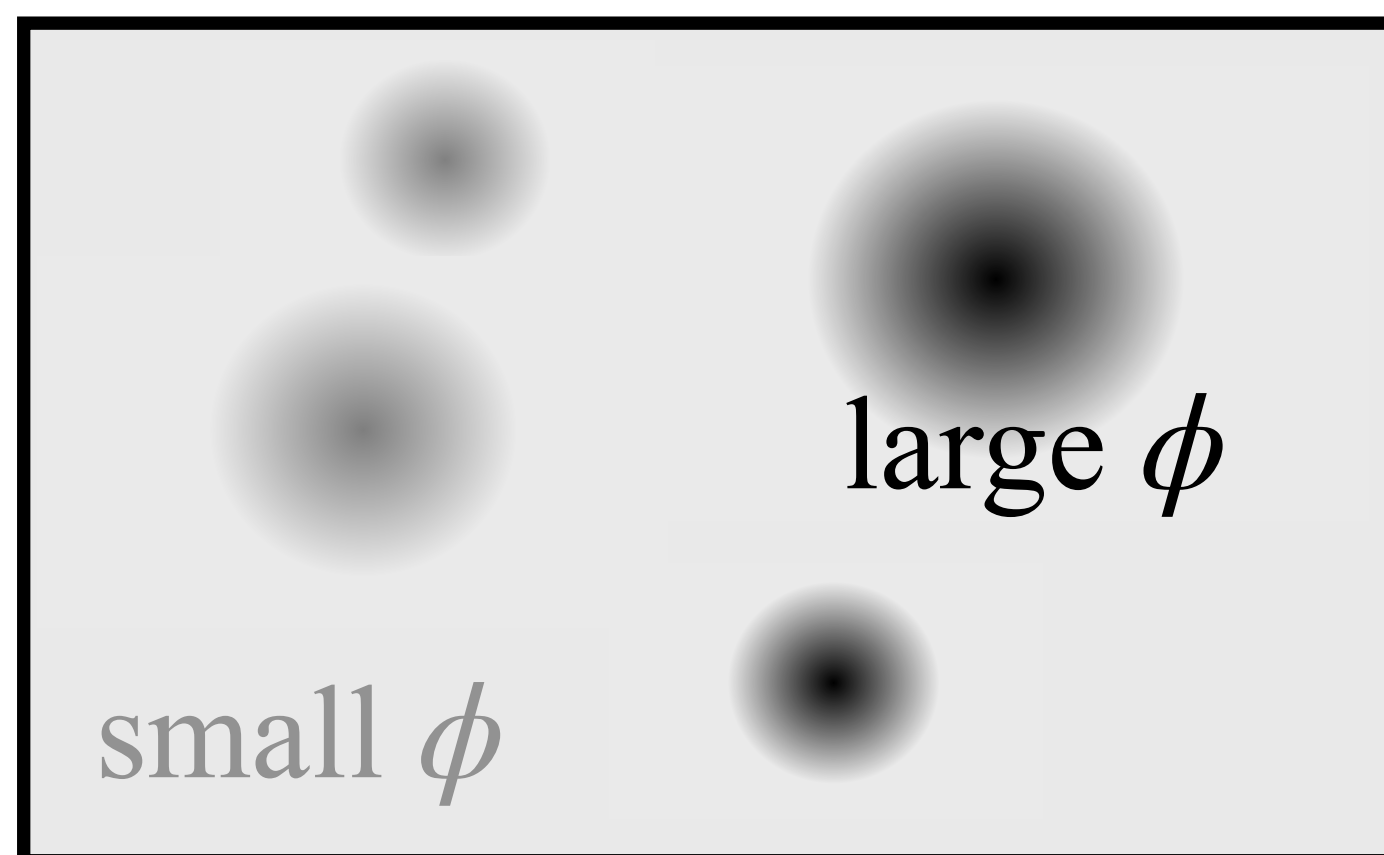
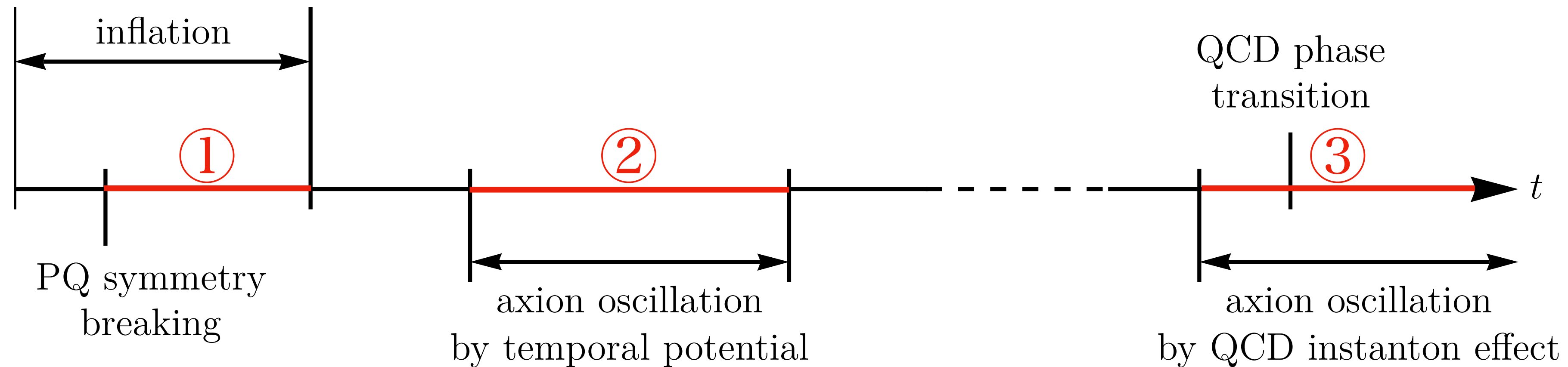
extracted from Carr et. Al.(2020)

# Overview of the Model



# PBH Formation from QCD Axion Bubbles

Previous study[N. Kitajima & F. Takahashi(2020)]



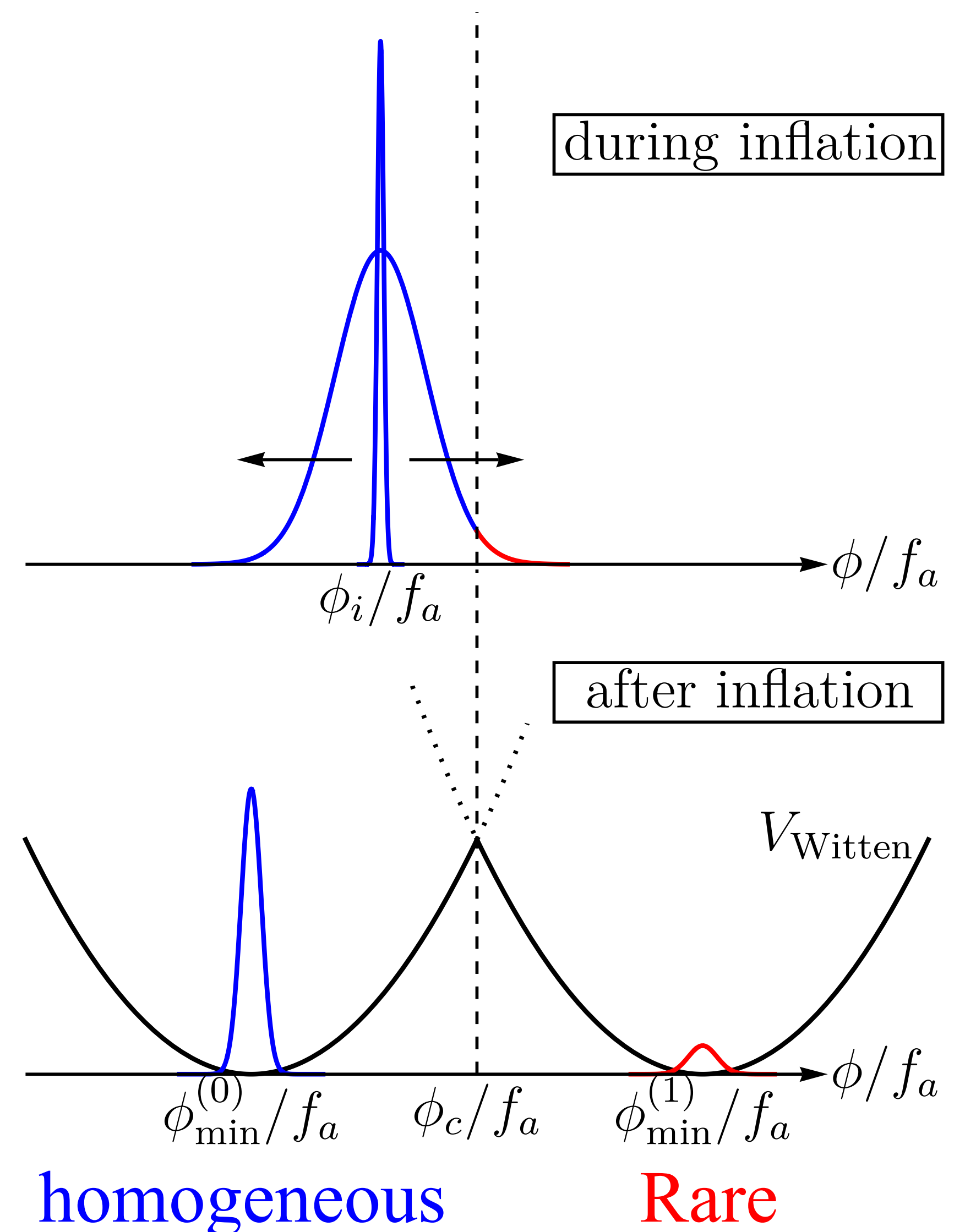
# PBH Formation from QCD Axion Bubbles

Previous study[N. Kitajima & F. Takahashi(2020)]

① During inflation, axion field acquires quantum fluctuations as a spectator field.

② Axion acquires a temporal potential and starts oscillation.

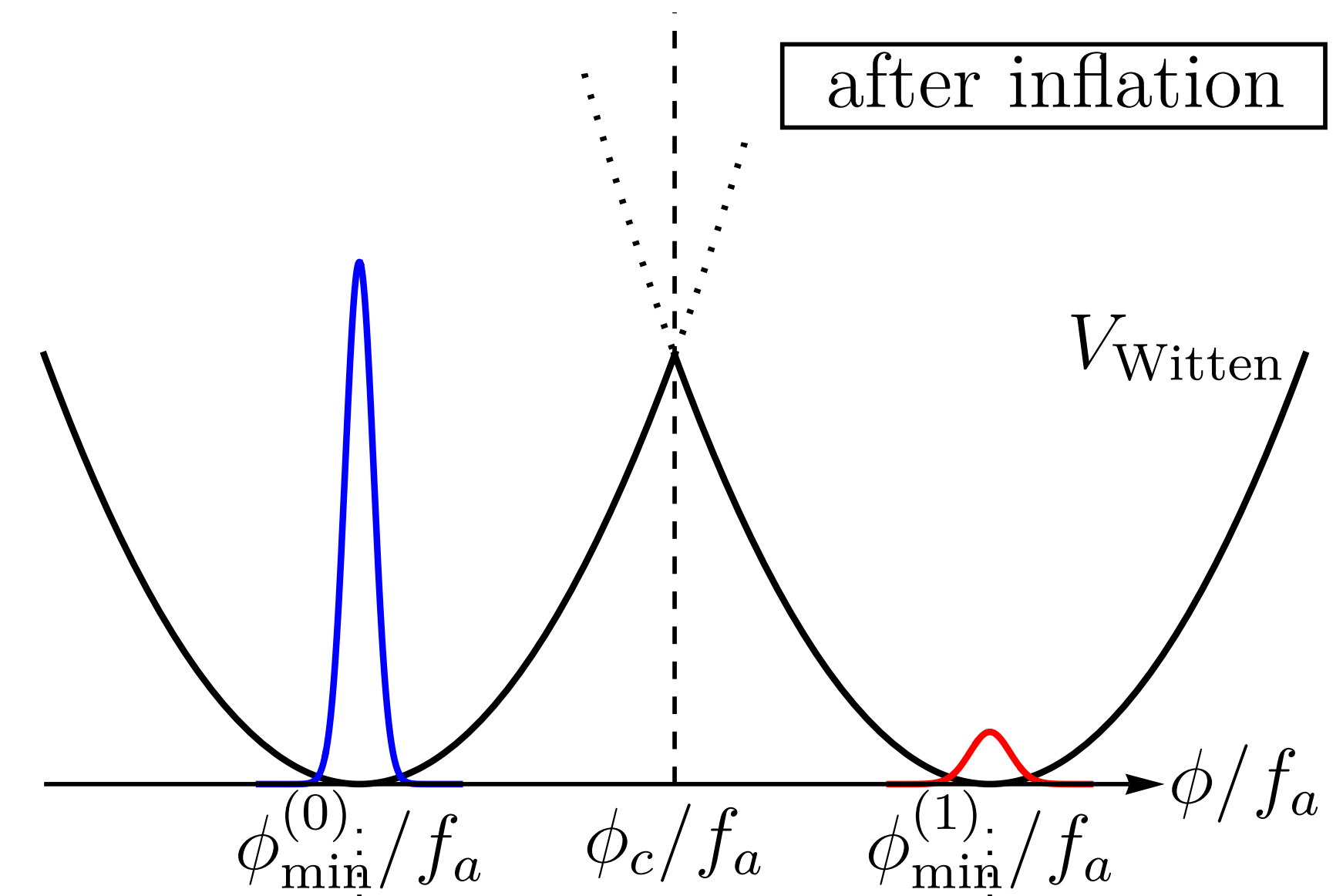
→ field value settles down to the minima



# PBH Formation from QCD Axion Bubbles

- ③ Around the QCD phase transition, axion acquires its mass thanks to the non-perturbative QCD effect.

$$V_{\text{QCD}}(\phi) = m_a^2(T) f_a^2 \left( 1 - \cos \frac{\phi}{f_a} \right)$$



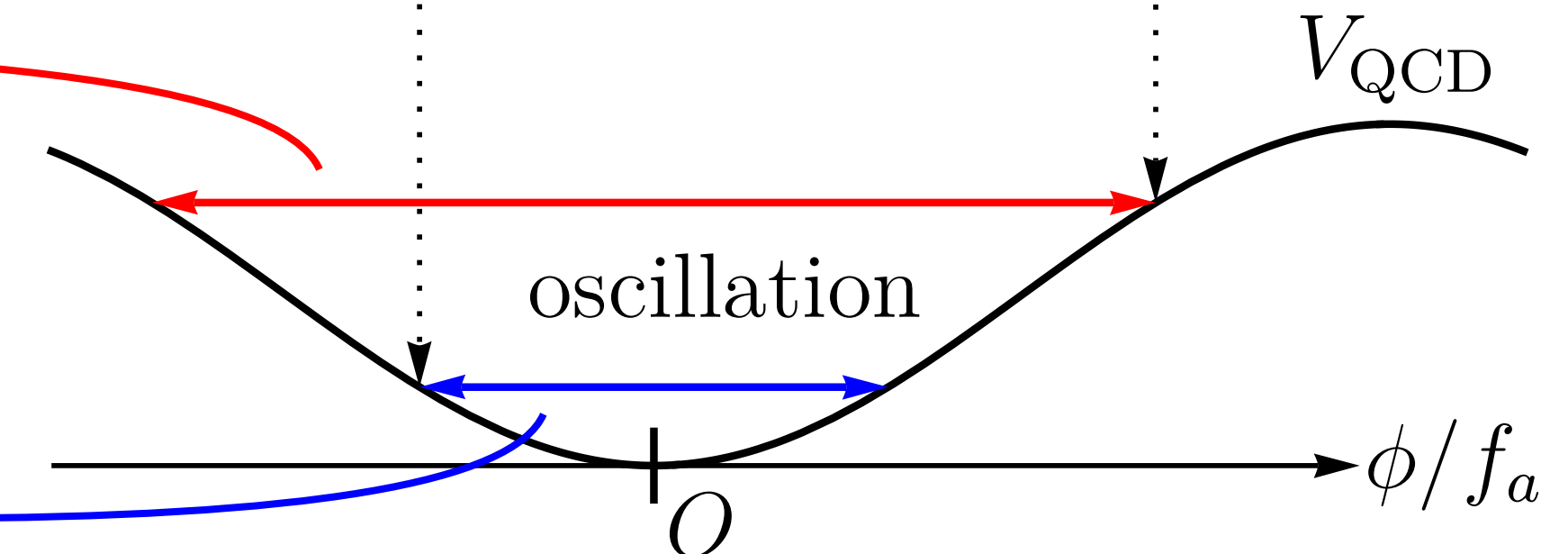
around QCD scale

rare & overdense

→ axion bubble

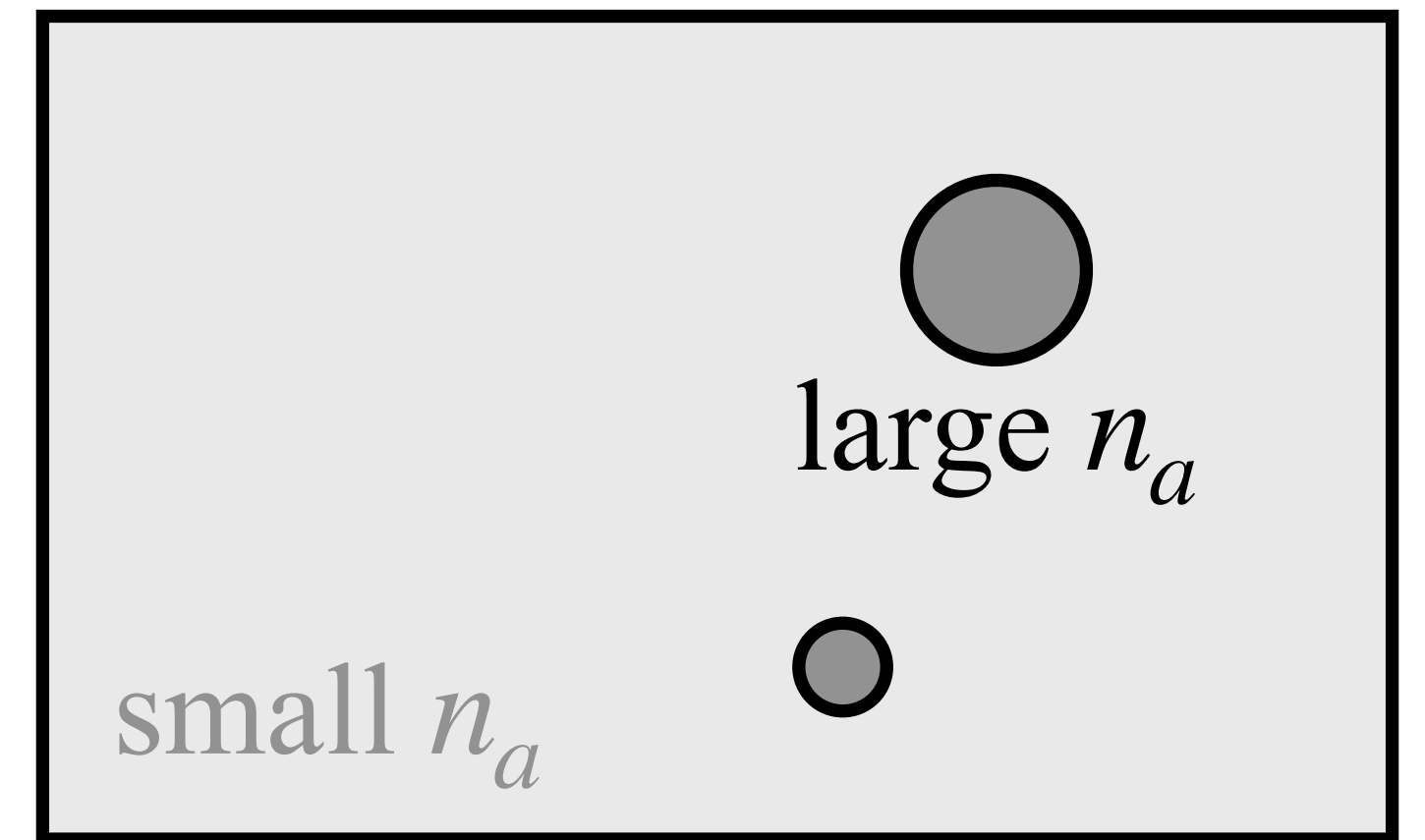
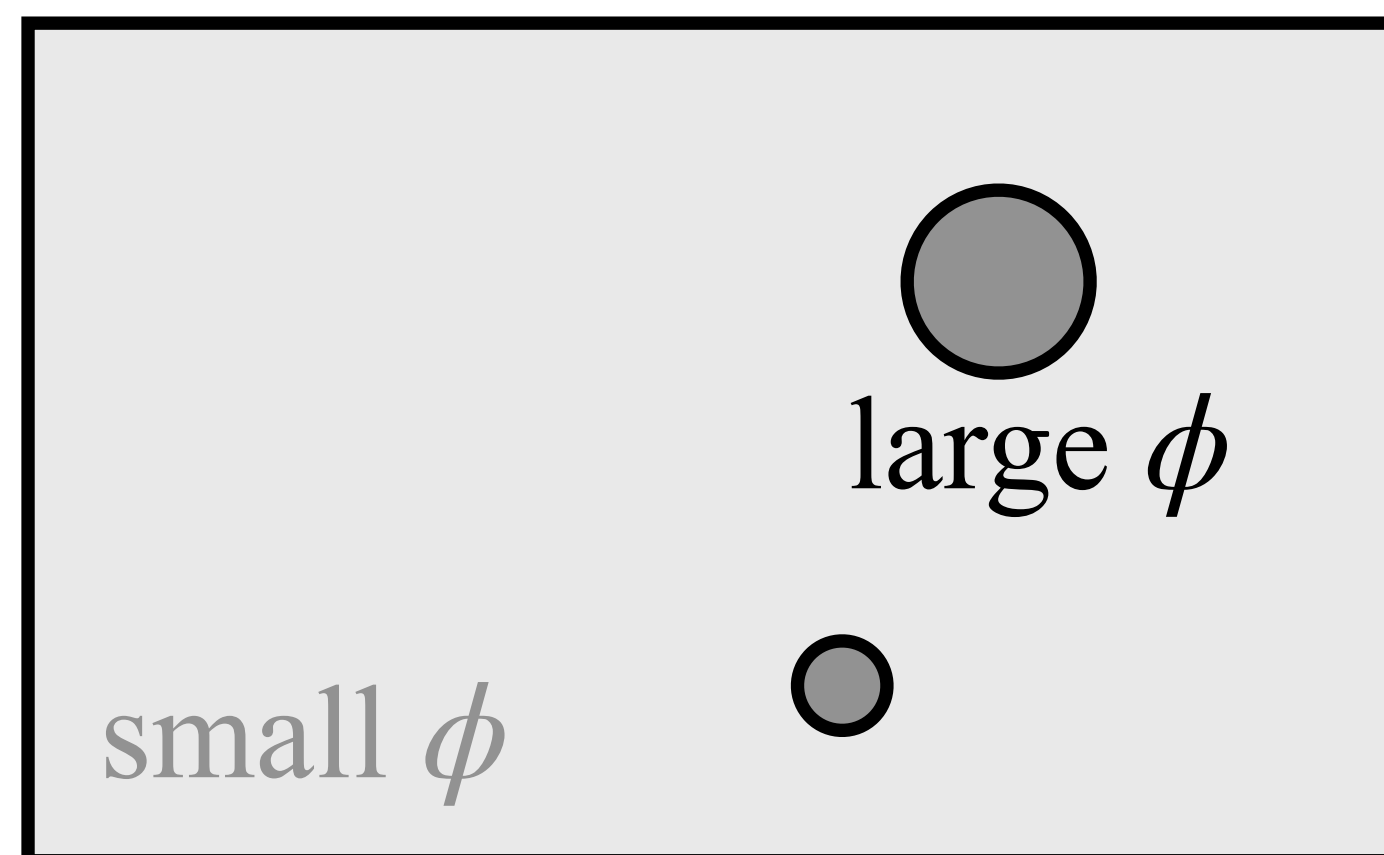
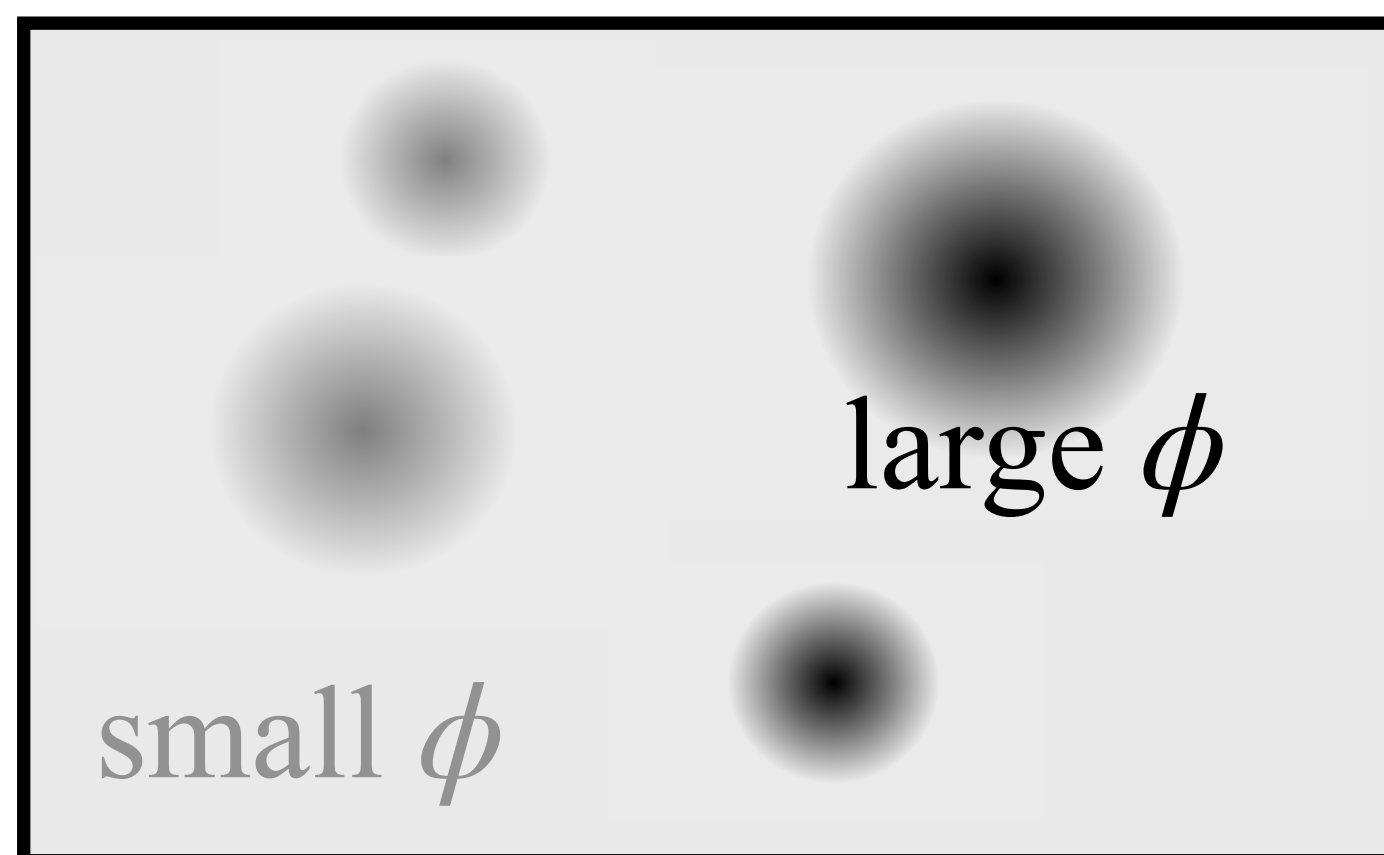
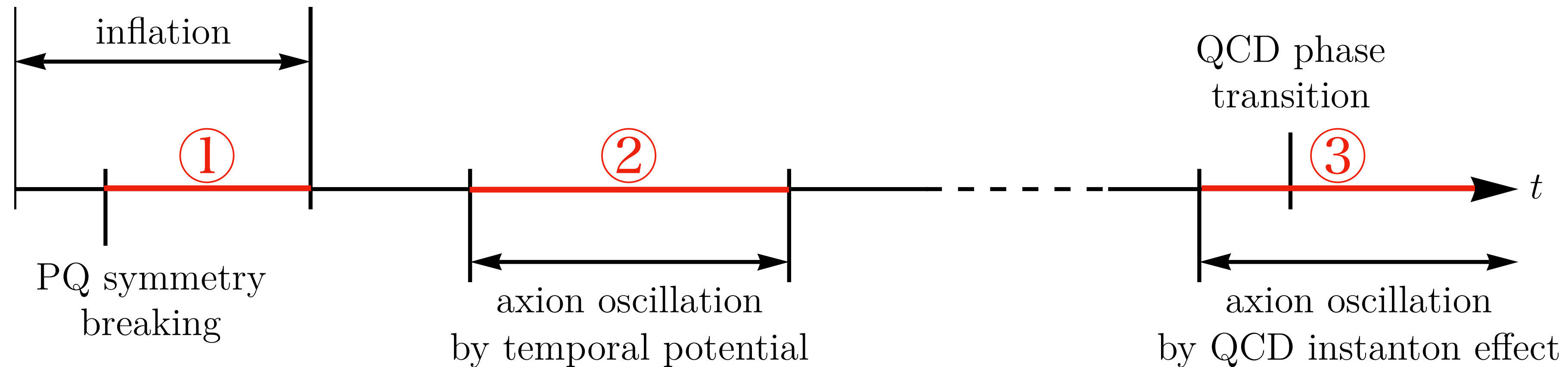
homogeneous & background

→ dark matter



# PBH Formation from QCD Axion Bubbles

Previous study[N. Kitajima & F. Takahashi(2020)]



# Details of the model

# Dark Matter(DM) Abundance

Previous study[N. Kitajima & F. Takahashi(2020)]

- Axion oscillation starts

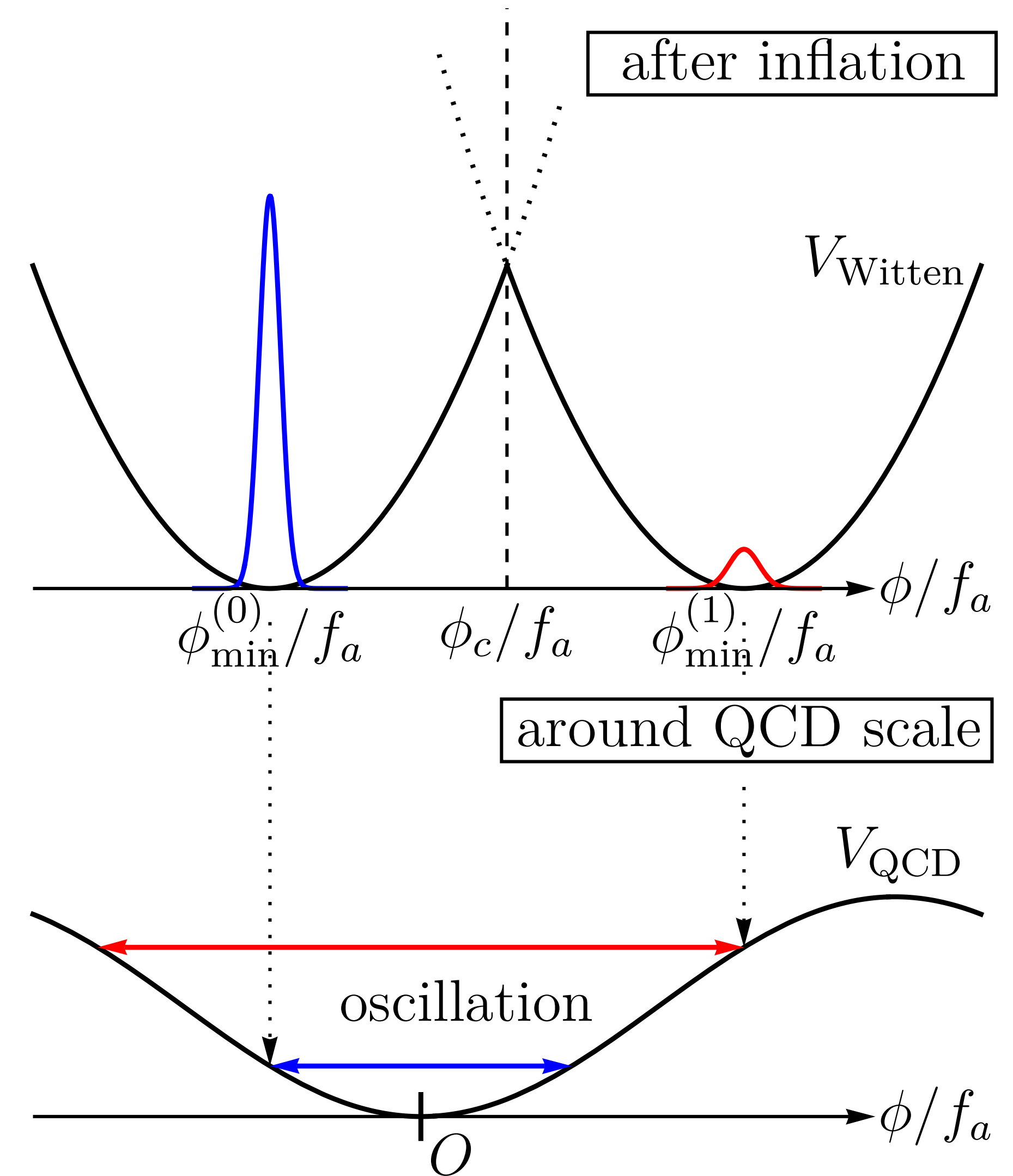
$$m_a(T_{\text{osc}}) = 3H(T_{\text{osc}})$$

- Axion number density.

$$n_a(T_{\text{osc}}) \simeq \frac{1}{2}m_a(T_{\text{osc}}) \phi_{\text{osc}}^2$$

- To account for the all DM abundance, we set

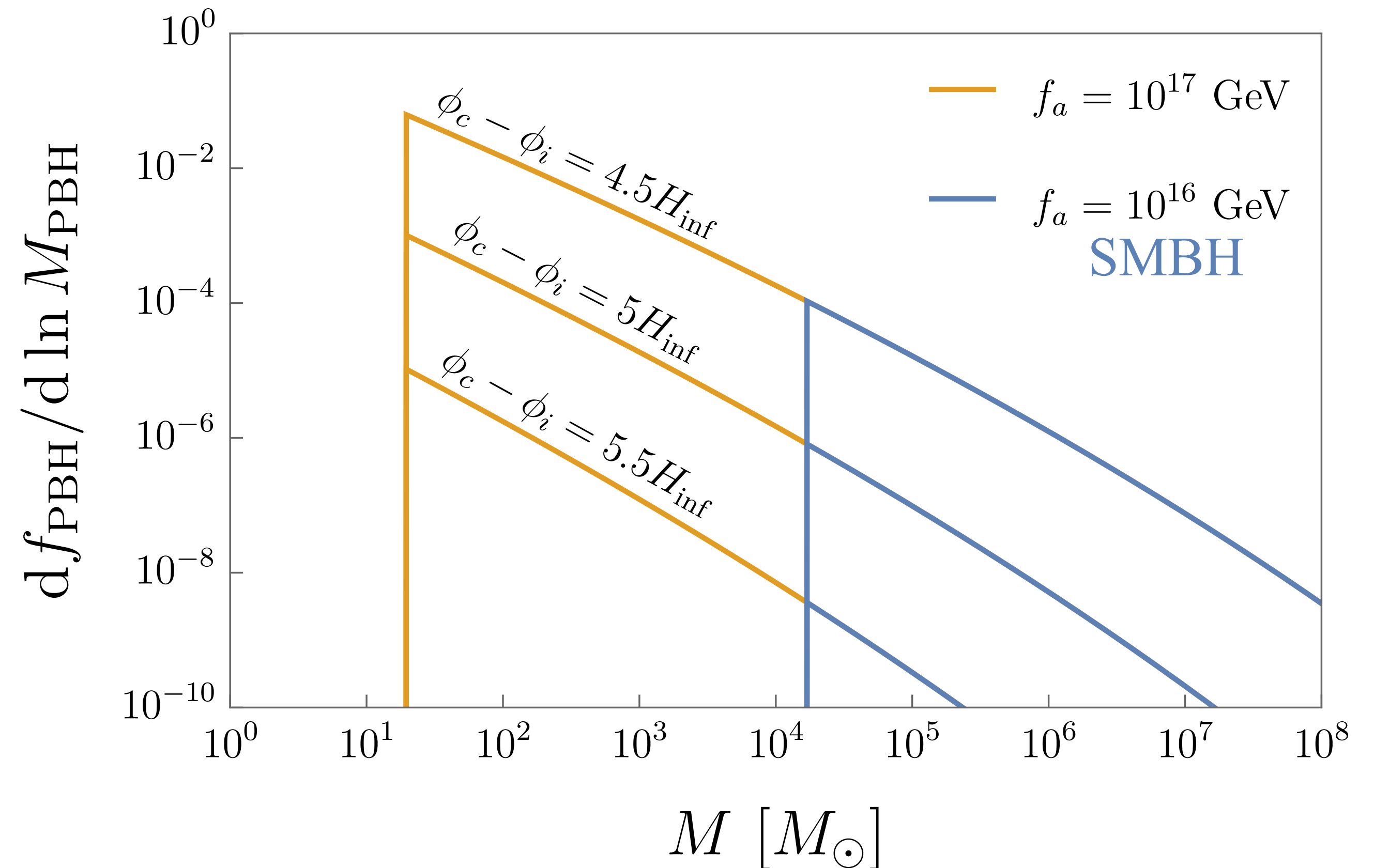
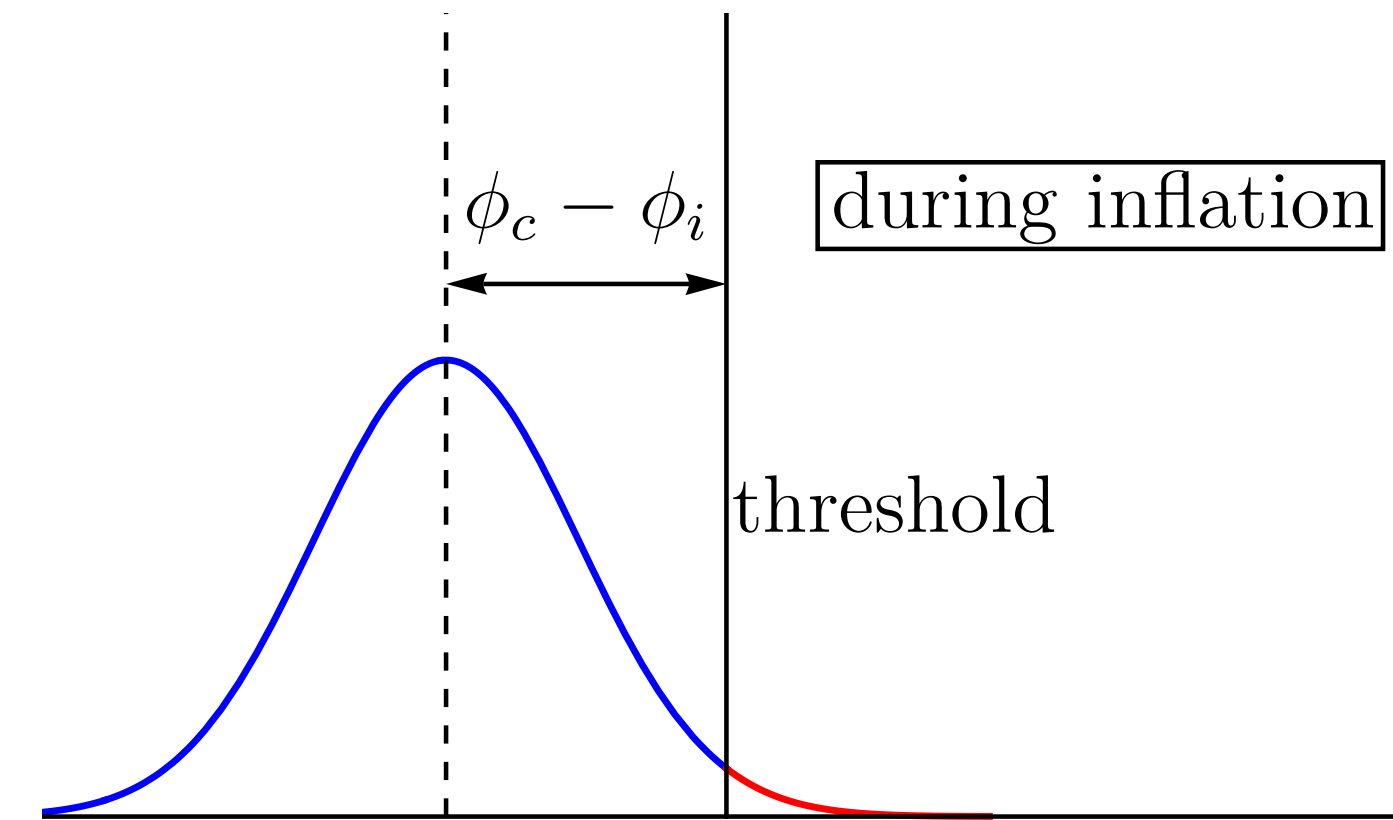
$$\frac{\phi_{\text{min}}^{(0)}}{f_a} = 4.3 \times 10^{-3} \left( \frac{g_{\text{osc}}}{60} \right)^{0.21} \left( \frac{f_a}{10^{16}\text{GeV}} \right)^{-0.58}$$



# Abundance of PBHs

Previous study [N. Kitajima & F. Takahashi (2020)]

- Axion decay constant  $f_a$   
 → PBH mass range
- PBH model for SMBH seed  
 ↔  $f_a = 10^{16}$  GeV
- Mass spectrum with a peak  
 → monochromatic mass approximation

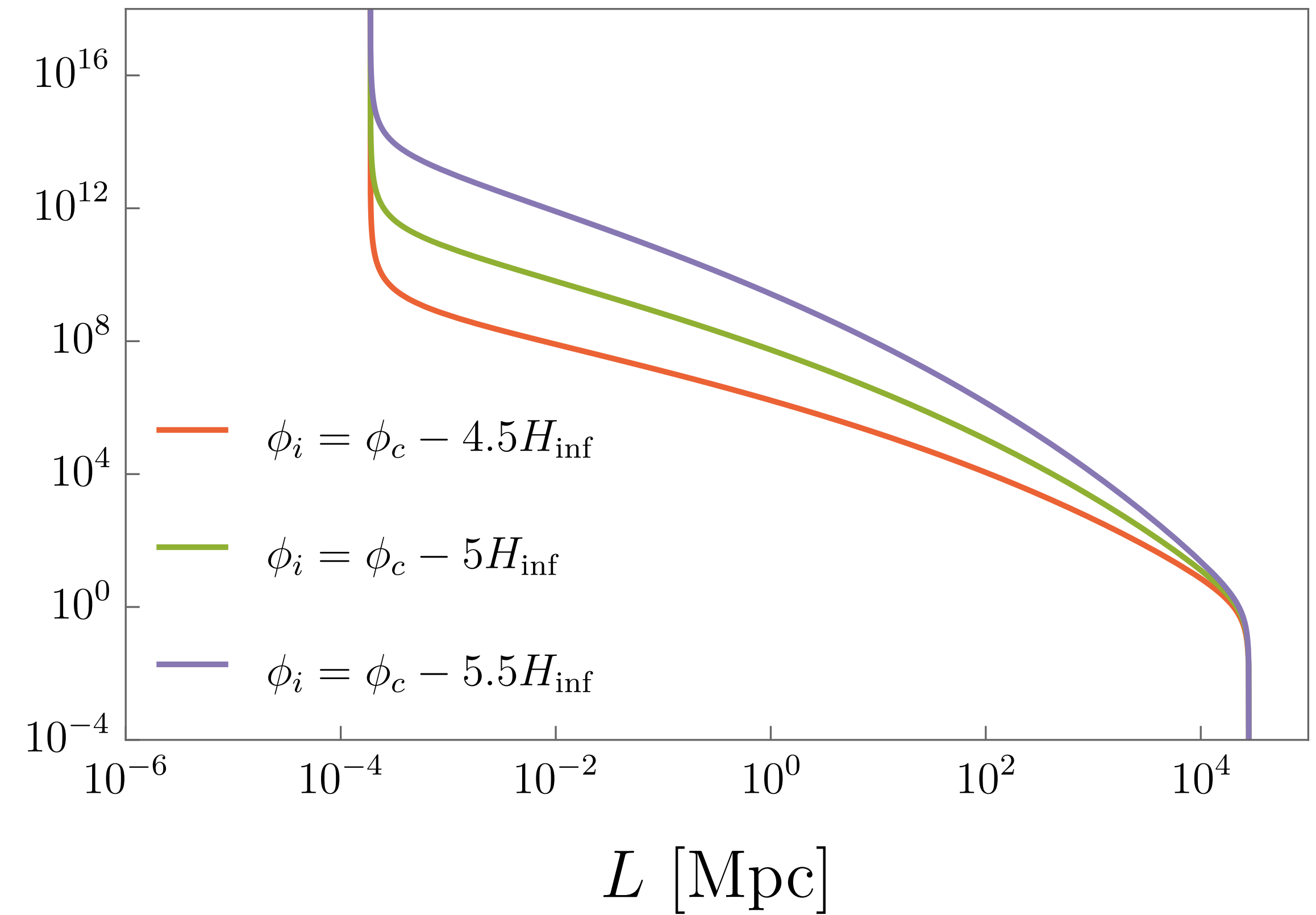
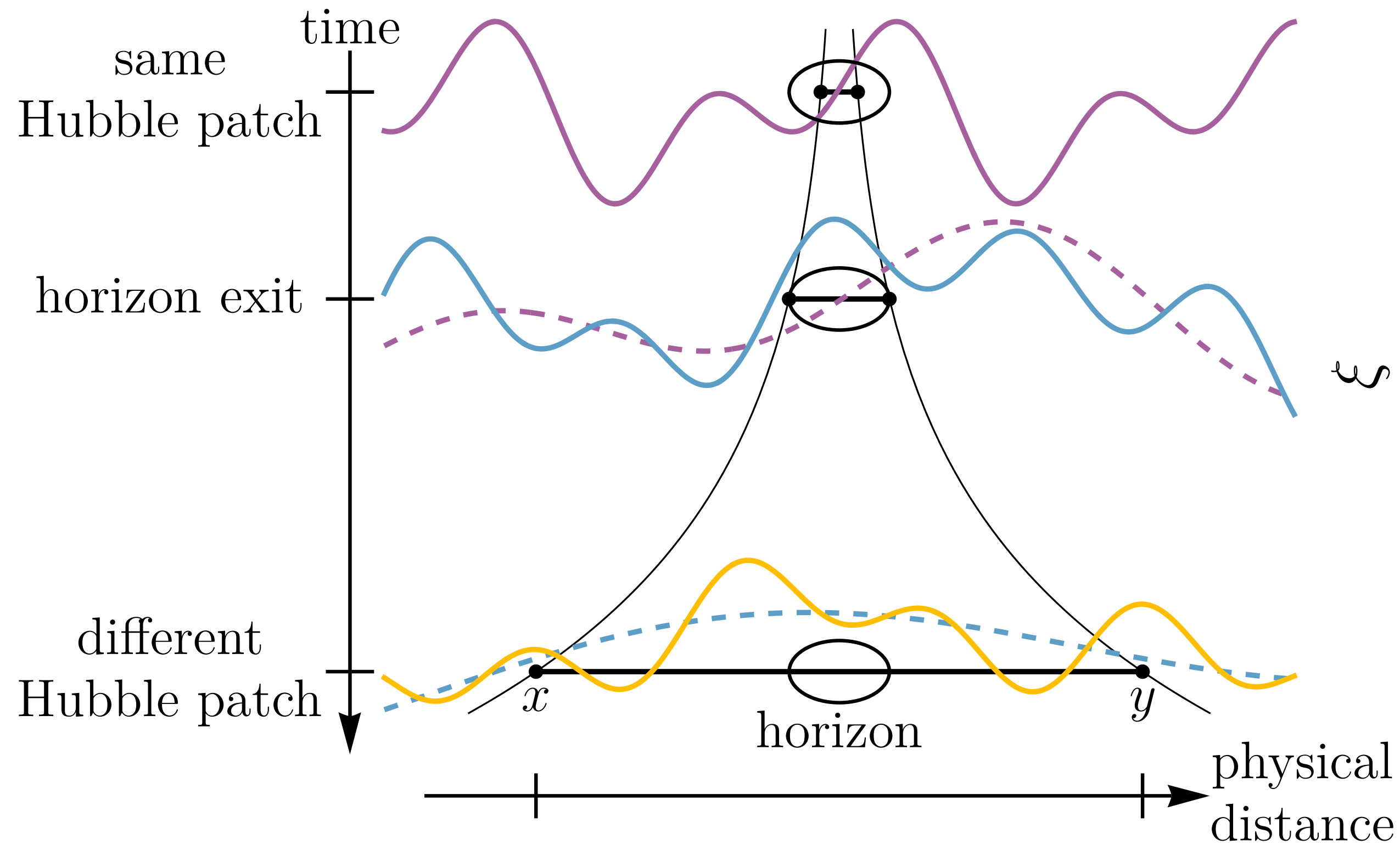




# Two-point Correlations of PBHs

Our work[JCAP10(2023)049]

$$\xi(\mathbf{x}) = \sum_{i \neq j} \frac{M_i M_j}{\rho_{\text{PBH}}^2} \langle \delta^{(3)}(\mathbf{x} - \mathbf{x}_i) \delta^{(3)}(-\mathbf{x}_j) \rangle - 1$$

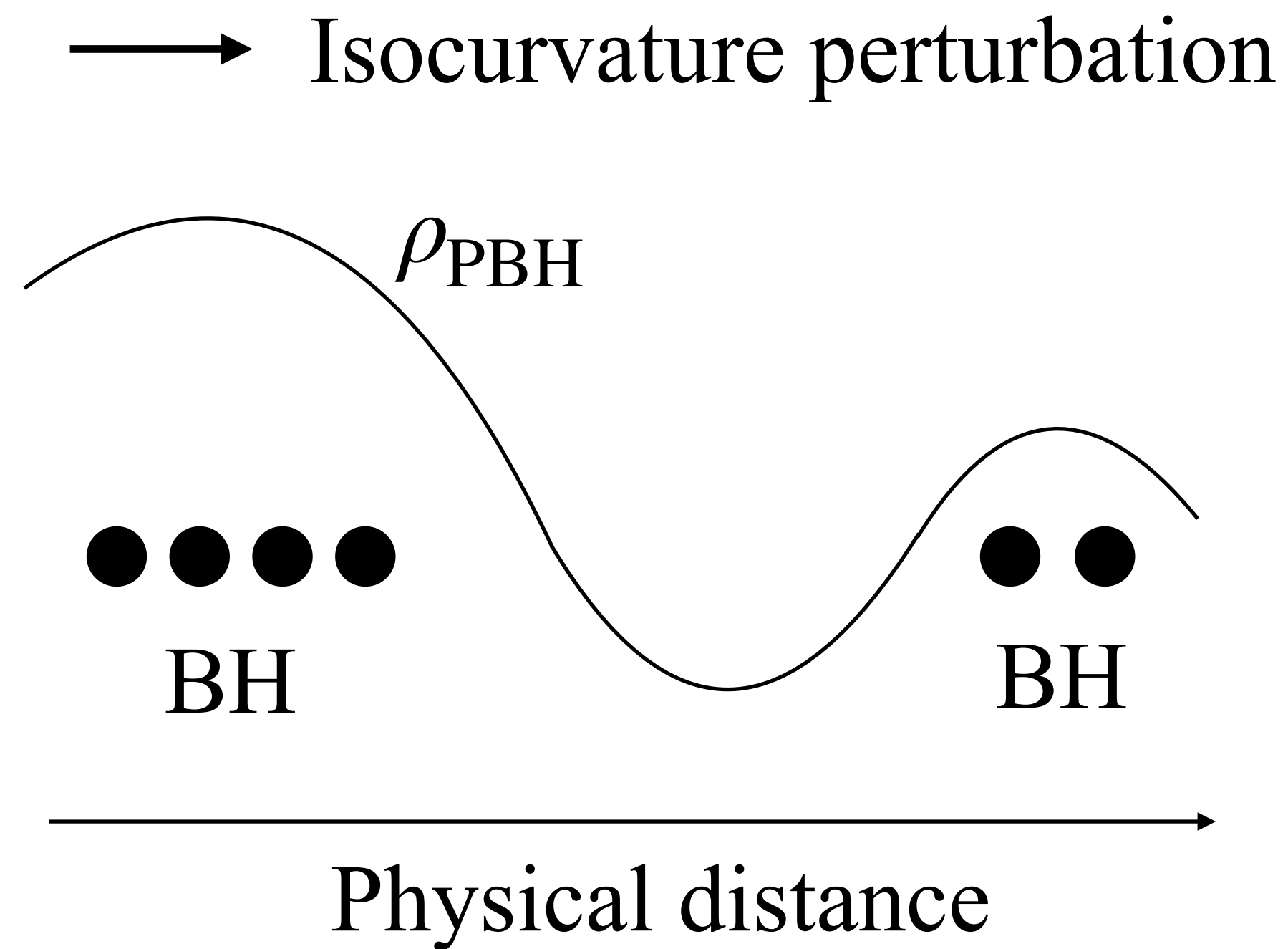




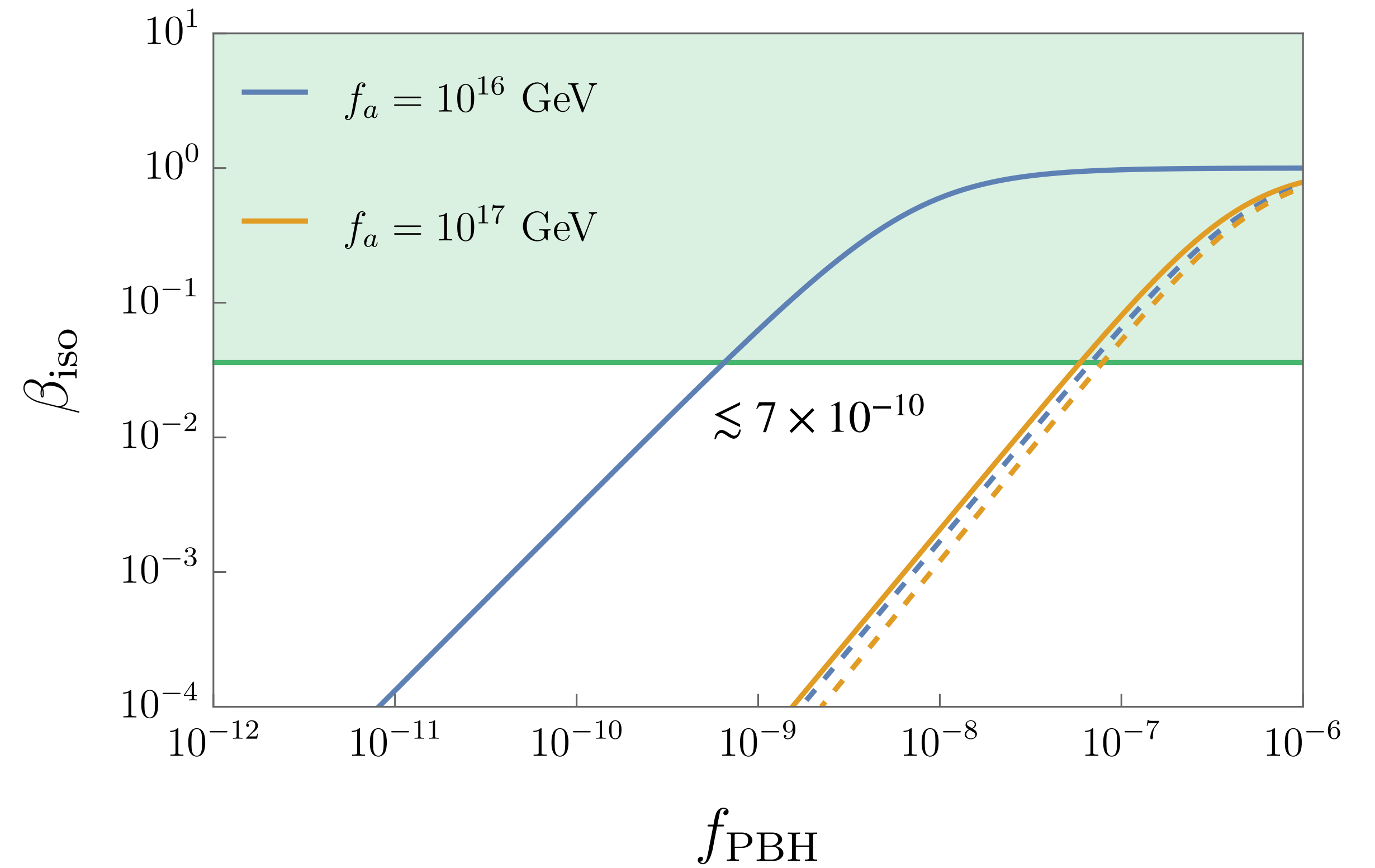
# Isocurvature Perturbations

Our work[JCAP10(2023)049]

- PBH clustering



- CMB constraint on isocurvature perturbation



$$f_{\text{SMBH}}^{(\text{obs})} \sim 3 \times 10^{-9} \text{ [C. J. Willott et. al.(2010)]}$$

# Angular Correlation Functions of SMBH

Previous study[T. Shinohara et.al. (2023)]

- New observational constraint: Angular correlation function of SMBH.

- The angular correlation function

$$w(x) = \langle \Delta_{\text{PBH}}(0,0)\Delta_{\text{PBH}}(\theta, \varphi) \rangle$$

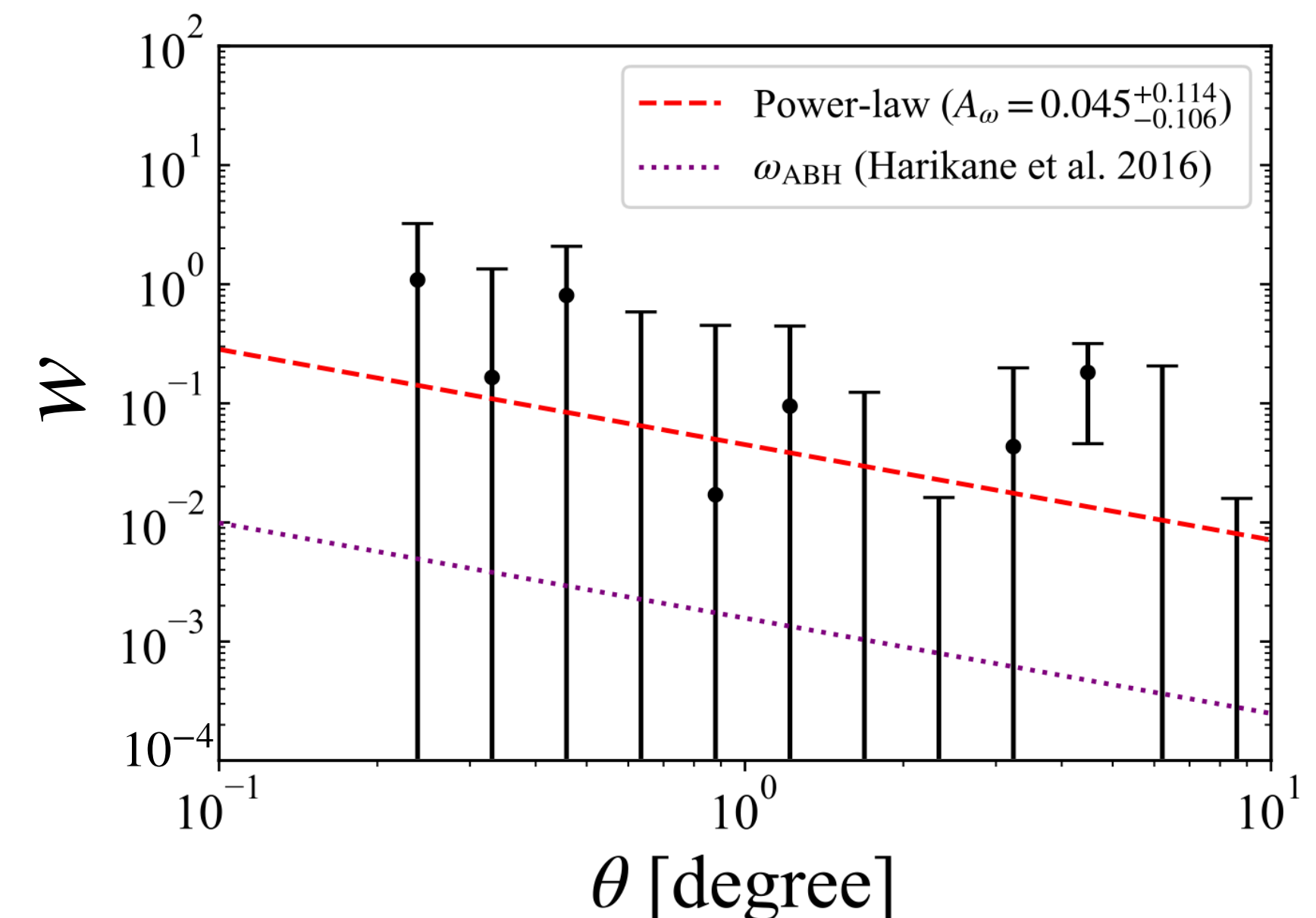
where

$\Delta_{\text{PBH}}$  = fluctuation of 2D number density

$$\mathbf{x} = (r, \theta, \varphi)$$

- Much larger angular correlation than the observational upper limit.

$$w(0.24^\circ) \sim 10^{6-7} \gg w_{\text{upper}}^{(\text{obs})}(0.24) = 5.37$$



Cite: Shinohara et.al. (2023)

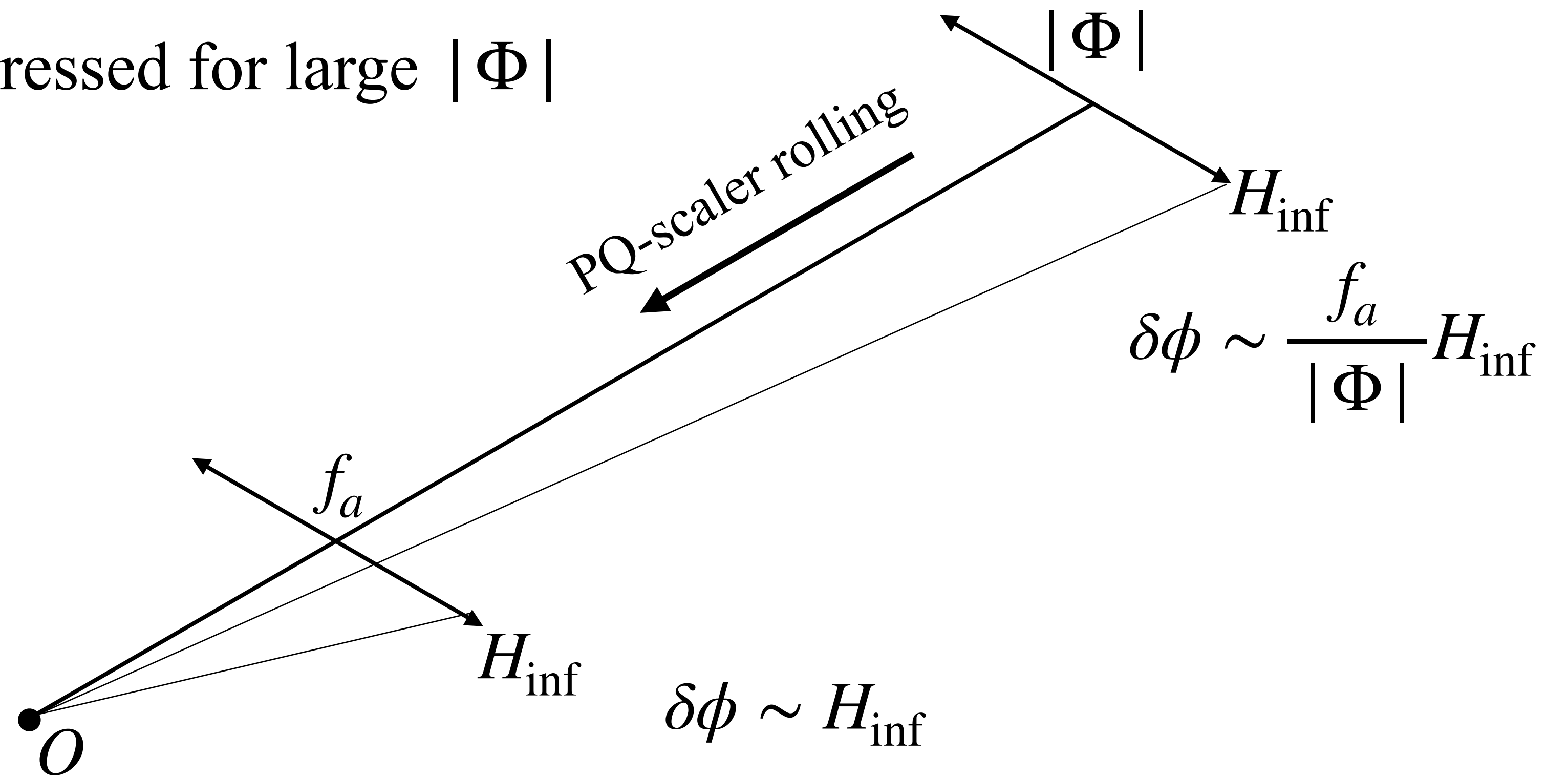
# Suppression of Isocurvature Perturbation

Our work[JCAP05(2024)092]

- Idea: PQ-scalar rolling in the early stage of inflation

$$\Phi = |\Phi| e^{i\frac{\phi}{f_a}}$$

- Axion fluctuation is suppressed for large  $|\Phi|$



# Modified Model

Our work[JCAP05(2024)092]

- Assumption:

PQ-scalar potential at  $|\Phi| \gtrsim f_a$

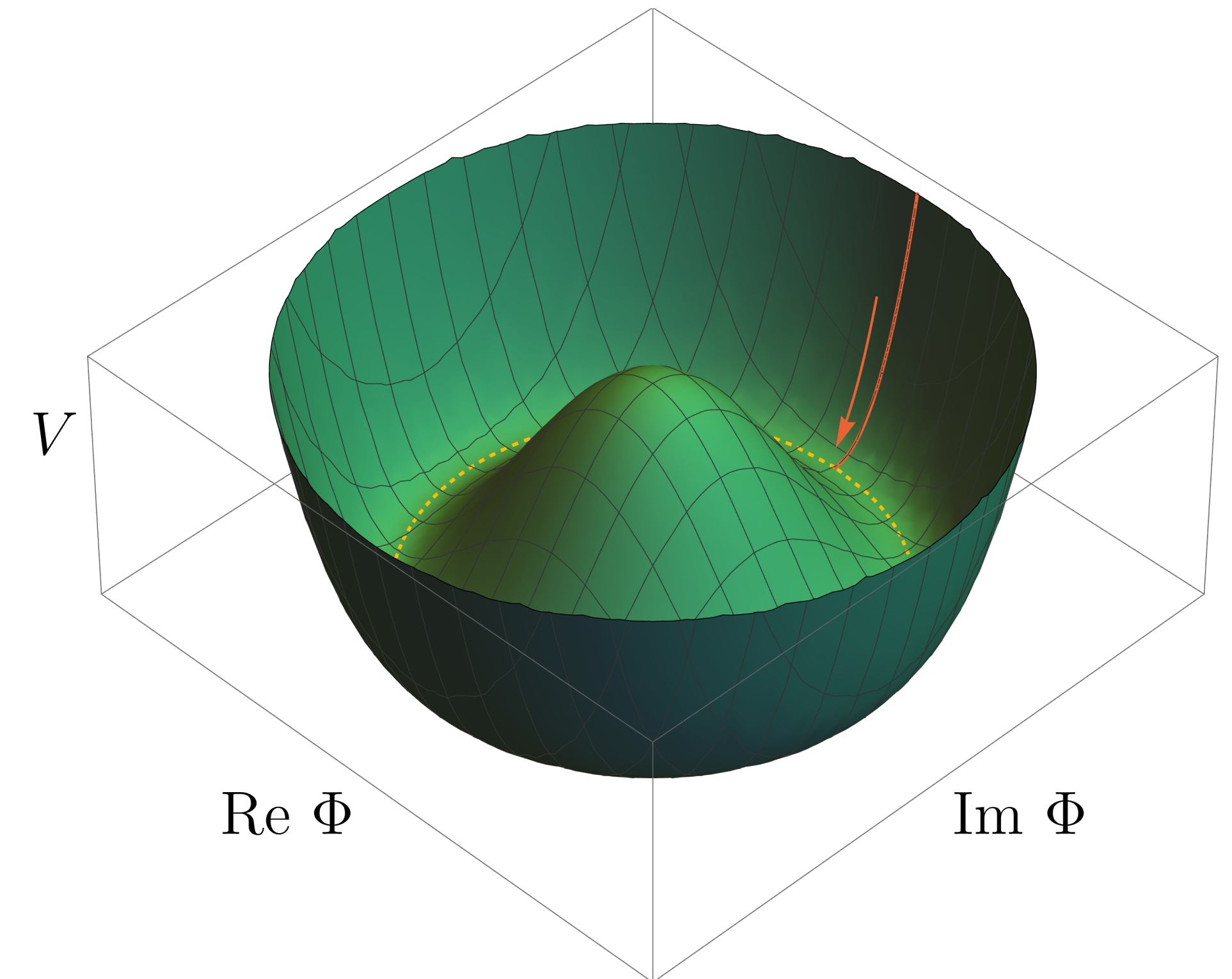
$\simeq$  the Hubble-induced mass term

$$V(|\Phi|) \simeq \frac{1}{2} c_I H_{\text{inf}}^2 |\Phi|^2, \quad c_I = \mathcal{O}(1)$$

EOM  $\longrightarrow$   $|\Phi| = |\Phi_*| e^{-\lambda H_{\text{inf}}(t-t_*)},$

$$\lambda = \frac{3}{2} \left( 1 \pm \sqrt{1 - \frac{4}{9} c_I} \right),$$

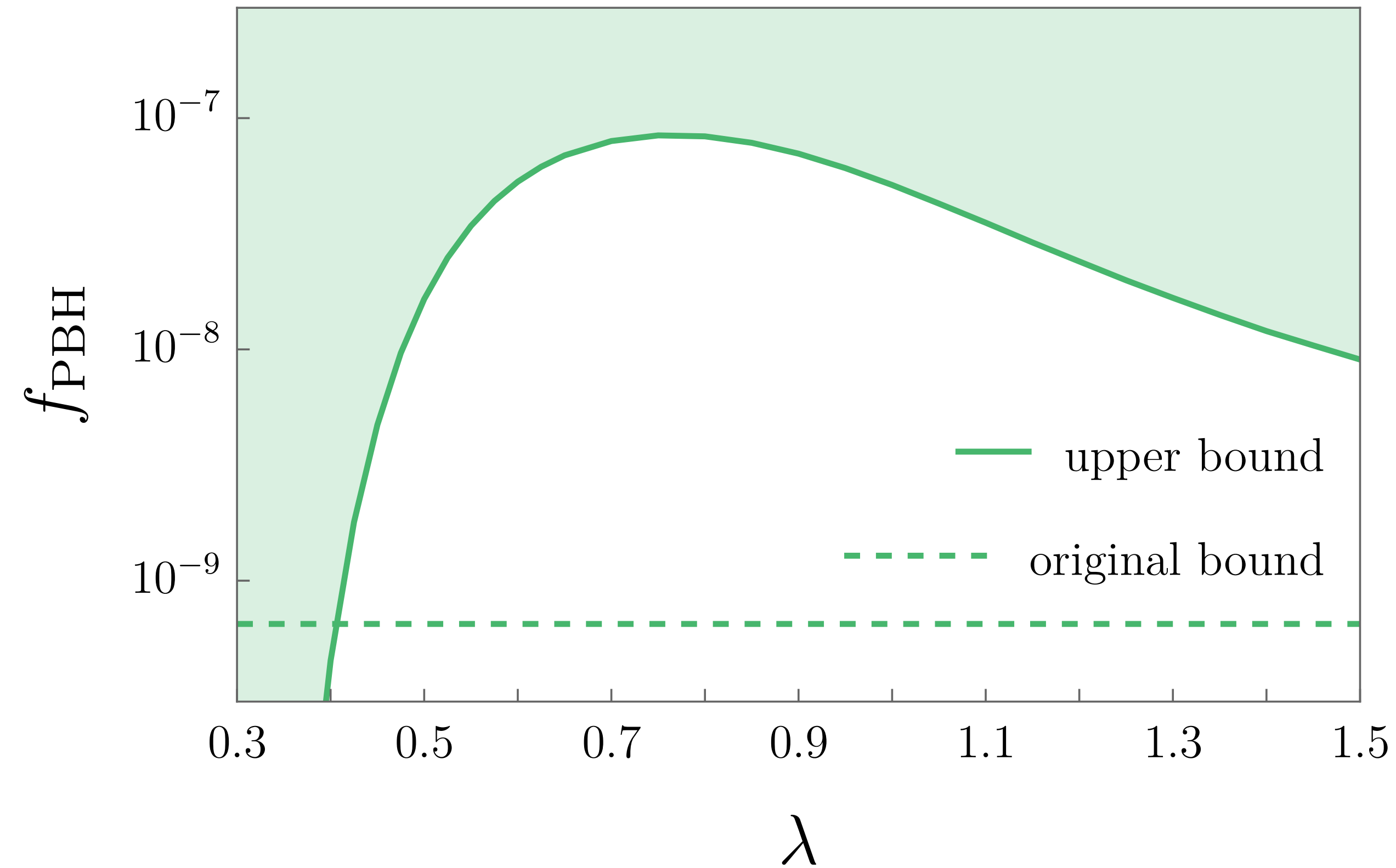
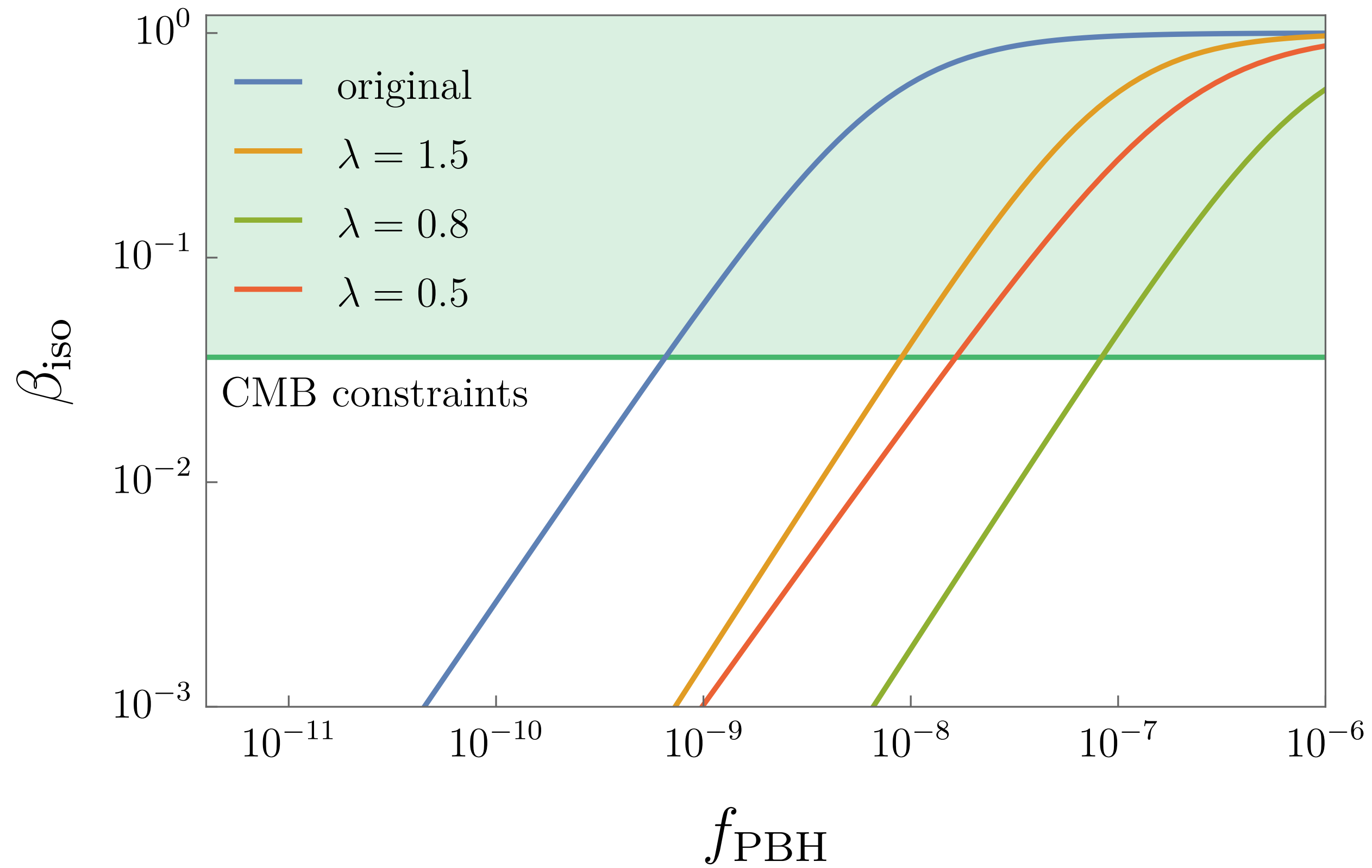
PQ scalar:  $\Phi$ , axion field:  $\phi = f_a \arg \Phi$



※ This is just an image.

# Suppression of Isocurvature Perturbation

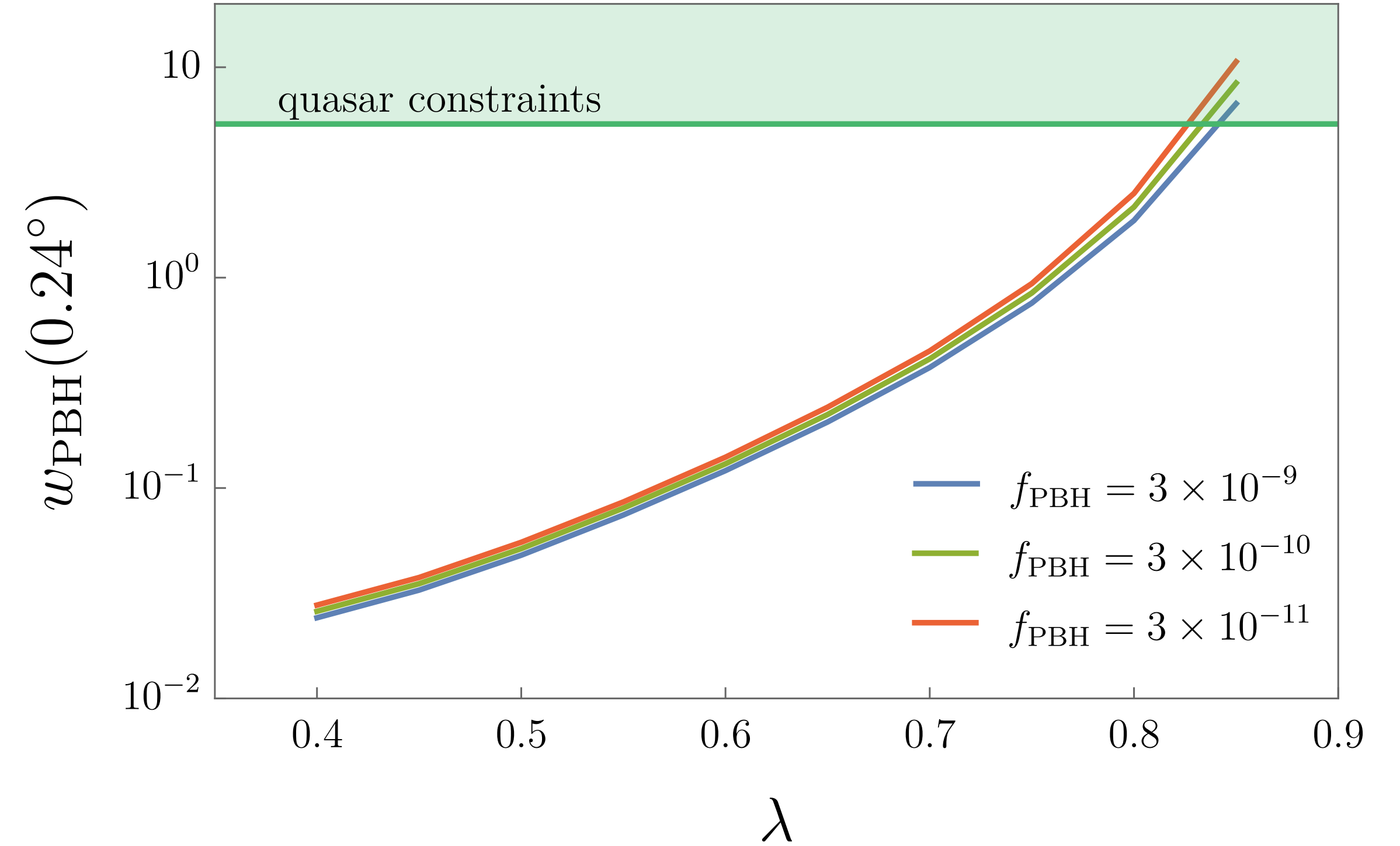
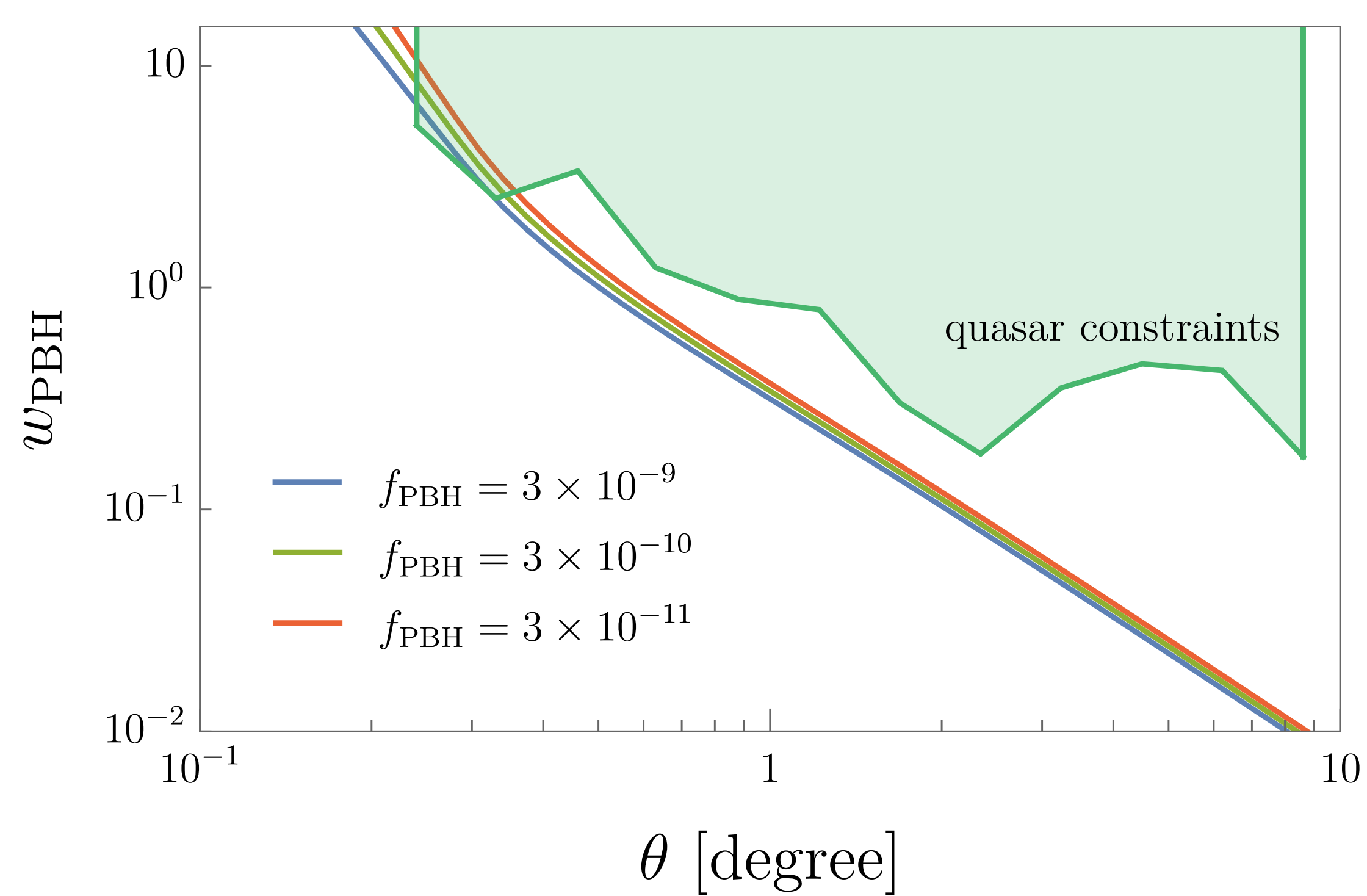
Our work[JCAP05(2024)092]



The observational constraint is  $0.45 \lesssim \lambda$ .

# Angular Correlation Function of PBH

Our work[JCAP05(2024)092]



The observational constraint is  $\lambda \lesssim 0.8$ .



# Summary

- PBH model with large inflationary density fluctuation is strongly constrained by CMB  $\mu$ -distortion, in the mass region of SMBH seeds.
- To avoid the constraint, PBH formation from axion bubbles is proposed but its spatial distribution has strong observational constraints.
- Our modified model can explain primordial origin of SMBH without any violation of the observational constraints.

Thank you for your attention.