



Current status and prospects of CPT tests with neutrino oscillation experiments

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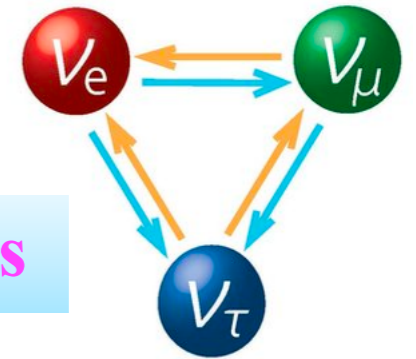
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1. Introduction

Testing CPT invariance with neutrino oscillation experiments

Neutrino oscillation: ν changes its flavor when traveling in spacetime



Flavor eigenstates

$$|\nu_\alpha\rangle = \sum_{i=1}^3 U_{\alpha i}^* |\nu_i\rangle \quad (\alpha = e, \mu, \tau)$$

Mass eigenstates

3 x 3 PMNS unitary matrix: 3 mixing angles ($\theta_{12}, \theta_{13}, \theta_{23}$), 1 CP-violating phase δ_{CP}

Oscillation probability

$$P(\nu_\alpha \rightarrow \nu_\beta) = |\langle \nu_\beta | \nu_\alpha \rangle|^2 = \left| \sum_i U_{\alpha i}^* U_{\beta i} e^{-i \frac{m_i^2 L}{2E}} \right|^2$$

ν mass
 $\propto \rho$ in matter
 ν energy
 $\theta_{12}, \theta_{13}, \theta_{23}, \delta_{CP}$
 distance traveled

- Under CPT transformation: $(\nu_\alpha \rightarrow \nu_\beta) \xrightarrow{CPT} (\bar{\nu}_\beta \rightarrow \bar{\nu}_\alpha)$

1. Introduction

Testing CPT invariance with neutrino oscillation experiments

- CPT asymmetry: $\mathcal{A}_{CPT} = P(\nu_\alpha \rightarrow \nu_\beta) - P(\bar{\nu}_\beta \rightarrow \bar{\nu}_\alpha)$
- Accelerator-based experiments (T2K, NOvA, Hyper-K, DUNE) study 4 channels: $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ and $\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu$
- Accelerator-based experiments **do not test** CPT symmetry via **appearance channels** since they don't focus on $\bar{\nu}_e \rightarrow \bar{\nu}_\mu$ channel
- Accelerator-based experiments **can test CPT** by their own **disappearance channels**

$$P(\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu) \approx 1 - \sin^2 2\theta_{23} \sin^2 \left(\frac{\Delta m_{31}^2 L}{4E} \right)$$

$$\mathcal{A}_{\mu\mu}^{CPT}(\sin^2 \theta_{23})$$

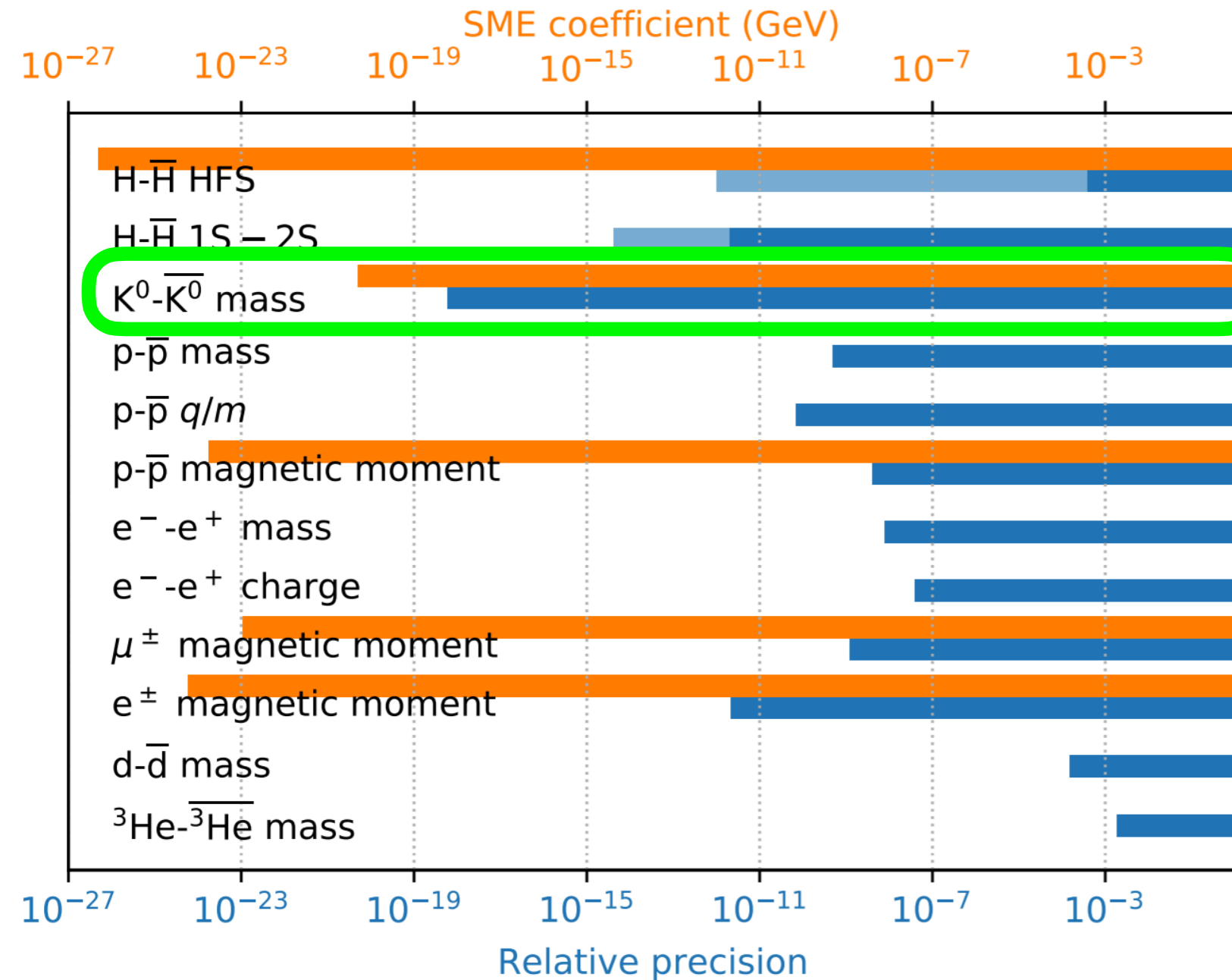
$$\mathcal{A}_{\mu\mu}^{CPT}(\Delta m_{31}^2)$$

$$\propto \delta_{\nu\bar{\nu}}(\sin^2 \theta_{23}) = \sin^2 \theta_{23} - \sin^2 \bar{\theta}_{23}$$

$$\propto \delta_{\nu\bar{\nu}}(\Delta m_{31}^2) = \Delta m_{31}^2 - \Delta \bar{m}_{31}^2$$

2. Current status of CPT tests

Current bounds on the direct CPT tests [arXiv:2111.04056 hep-ex]



- Current best constraint in terms of relative mass difference is given by $K^0 - \bar{K}^0$ system:

$$\left| \frac{m(K^0) - m(\bar{K}^0)}{m_K} \right| < 6 \times 10^{-19}$$

- This value looks very stringent. However, when converted to mass squared difference, it becomes much weaker

$$m^2(K^0) - m^2(\bar{K}^0) < 0.3 \text{ eV}^2$$

2. Current status of CPT tests

The most up-to-date bounds on CPTV at 3σ C.L. with ν experiments [[arXiv:2305.06384v1](#)]

$$|\delta(\sin^2\theta_{12})| < 0.187$$

$$|\delta(\sin^2\theta_{13})| < 0.029$$

$$|\delta(\sin^2\theta_{23})| < 0.19$$

$$|\delta(\Delta m_{21}^2)| < 3.7 \times 10^{-5} \text{ eV}^2$$

$$|\delta(\Delta m_{31}^2)| < 2.5 \times 10^{-4} \text{ eV}^2$$

$$(|\delta(X)| = |X - \bar{X}|)$$

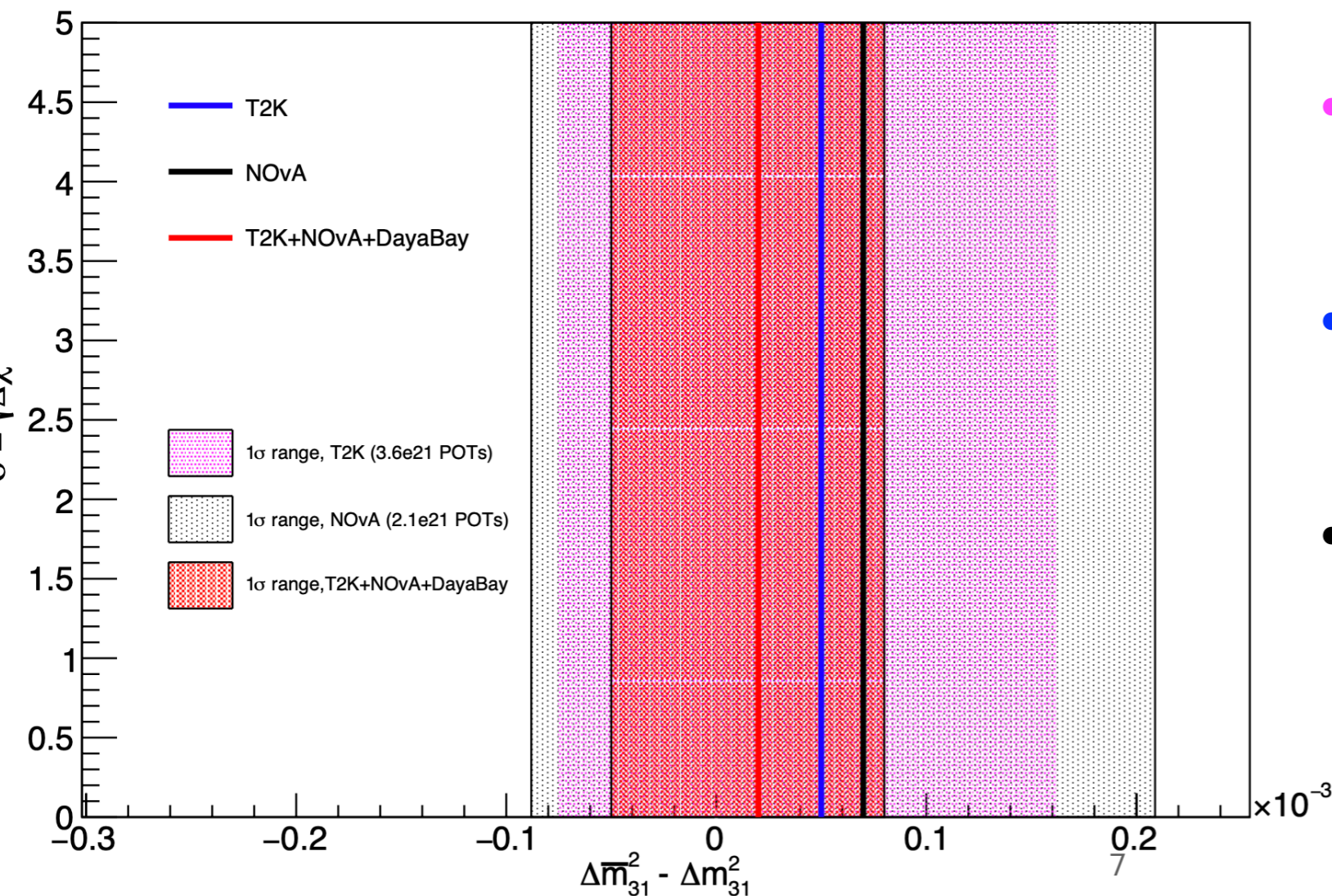
$$|m^2(K^0) - m^2(\bar{K}^0)| < 0.3 \text{ eV}^2$$

- In terms of mass squared difference, neutrino oscillation provides few orders better constraint on CPTV than neutral Kaon system

2. Current status of CPT tests

Current measurements of T2K, NOvA, and DayaBay experiments

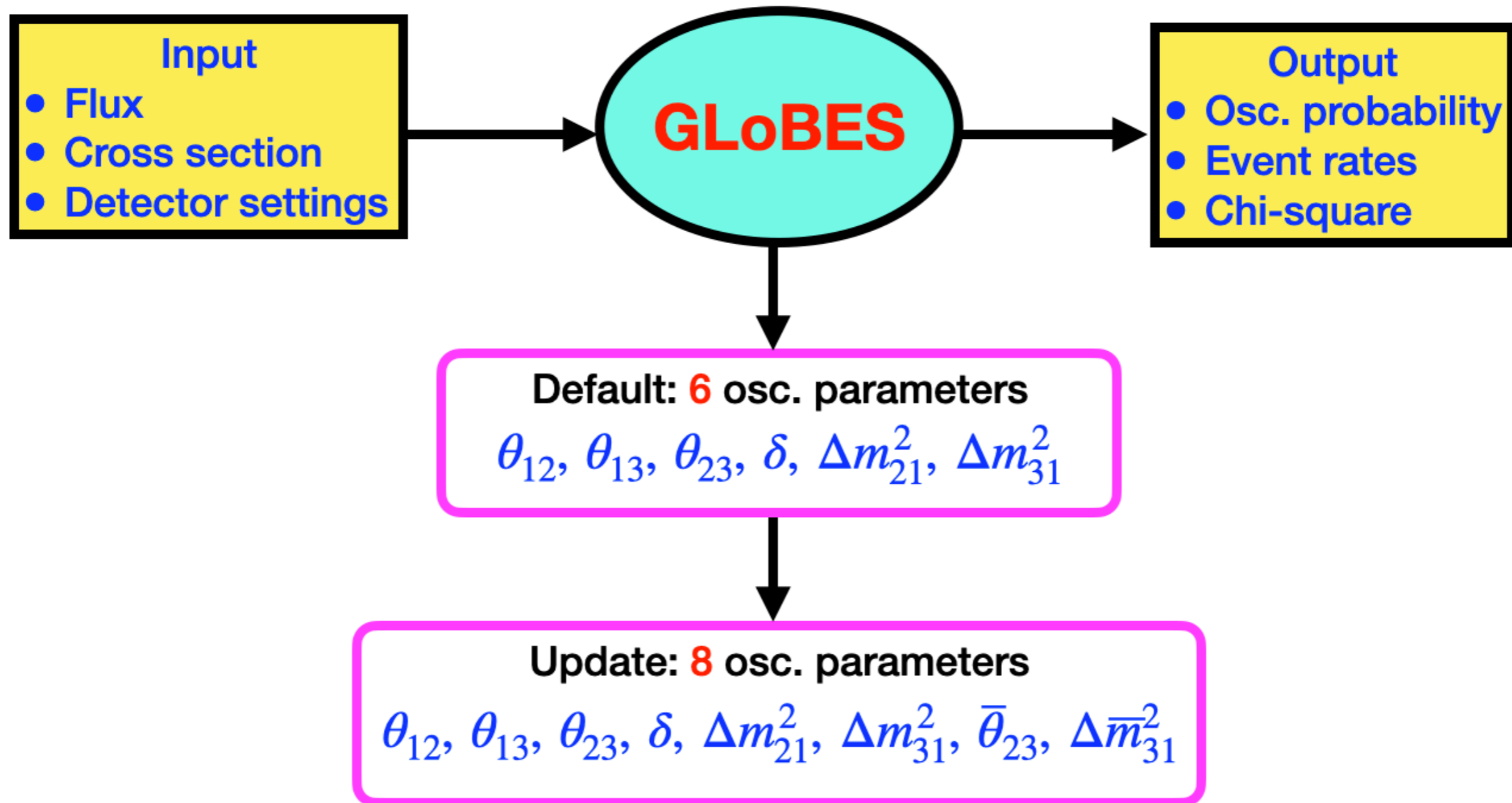
NO is assumed	T2K (3.6e21 POTs) <i>P.R.D 108 (2023) 7, 072011</i>	NOvA (2.1e21 POTs) <i>Mendez PhD thesis (2019)</i>	DayaBay (3158 days) <i>P.R.L 130, 161802 (2023)</i>	Combined
$\Delta m_{31}^2 / 10^{-3} eV^2$	$2.55^{+0.05}_{-0.06}$	$2.56^{+0.07}_{-0.09}$		$2.55^{+0.04}_{-0.05}$
$\Delta \bar{m}_{31}^2 / 10^{-3} eV^2$	$2.60^{+0.10}_{-0.11}$	$2.63^{+0.12}_{-0.13}$	$2.54^{+0.06}_{-0.06}$	$2.57^{+0.05}_{-0.05}$
$\delta(\Delta m_{31}^2) / 10^{-3} eV^2$	$0.05^{+0.11}_{-0.12}$	$0.07^{+0.14}_{-0.16}$		$0.02^{+0.06}_{-0.07}$



- Current T2K and NOvA data are consistent with CPT conservation hypothesis
- Combined data of T2K, NOvA, and Daya Bay is consistent with CPT conservation hypothesis
- Combine with DayaBay data significant improves the precision on $\Delta \bar{m}_{31}^2$

3. Prospects of CPT tests with neutrino oscillation experiments

- **GLOBES**: The General Long Baseline Experiment Simulator



- Use disappearance channels only
- In this report, we only focus on parameter $\delta(\Delta m_{31}^2)$

3. Prospects of CPT tests with neutrino oscillation experiments

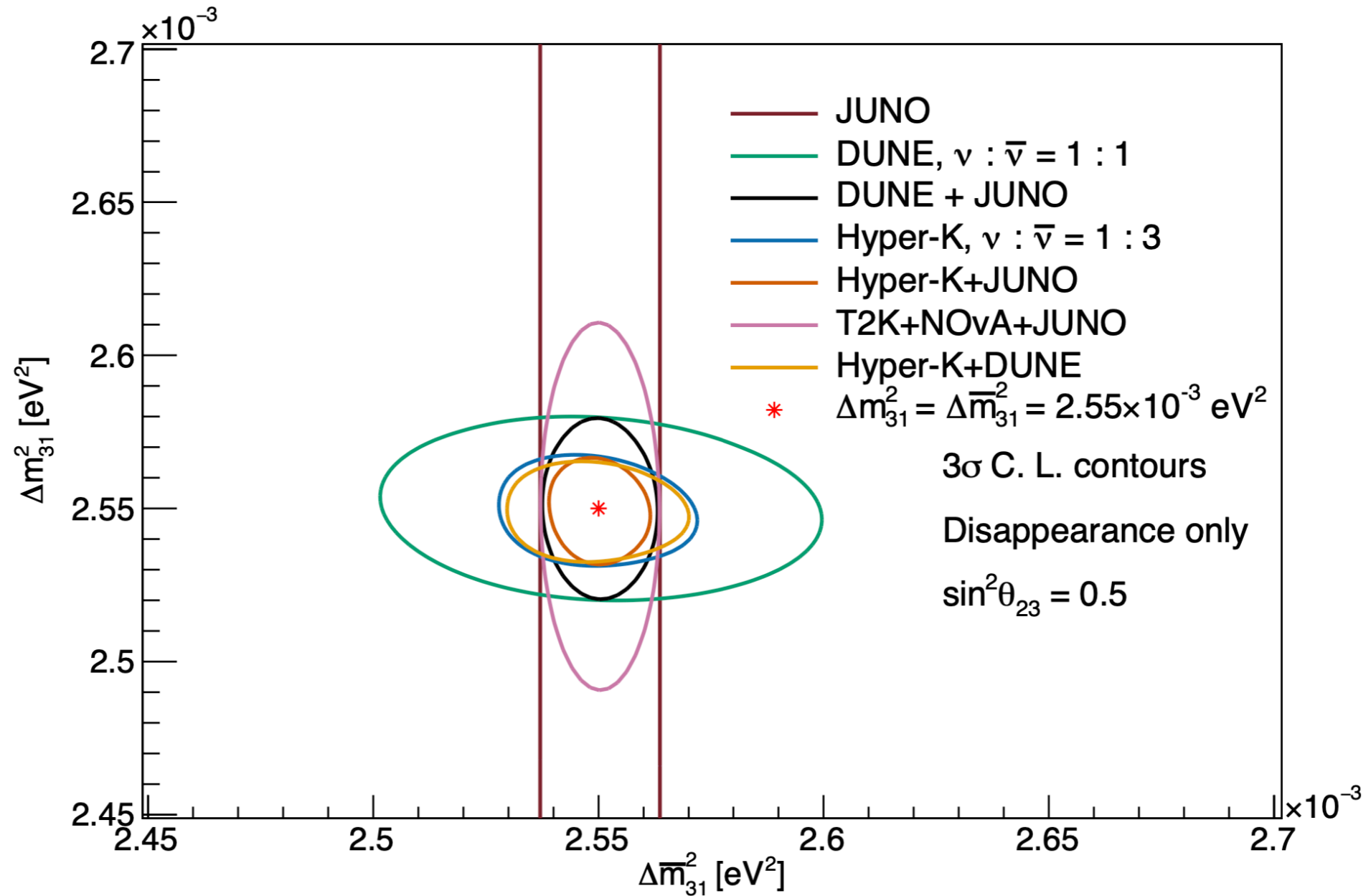
- GLOBES setup for T2K, NOvA, JUNO, Hyper-K, and DUNE

	T2K	NOvA	JUNO	Hyper-K	DUNE
Baseline (km)	295	810	52,5	295	1285
Matter density <i>g/cm³</i>	2,6	2,8	2,6	2,6	2,85
Detector mass (kt)	22,5	14	20	187	40
Exposure	$10 \times 10^{21} POT$	$7.2 \times 10^{21} POT$	6 years	10 years	10 years nominal
Power	0.77 MW	0.74 MW	26.6 GWth	1.3 MW	1.2 MW

- The exposures of T2K and NOvA are expected at the end of their runs

3. Prospects of CPT tests with neutrino oscillation experiments

- Assume CPT is conserved, 2D contours at 3σ C. L. bound on CPTV are made

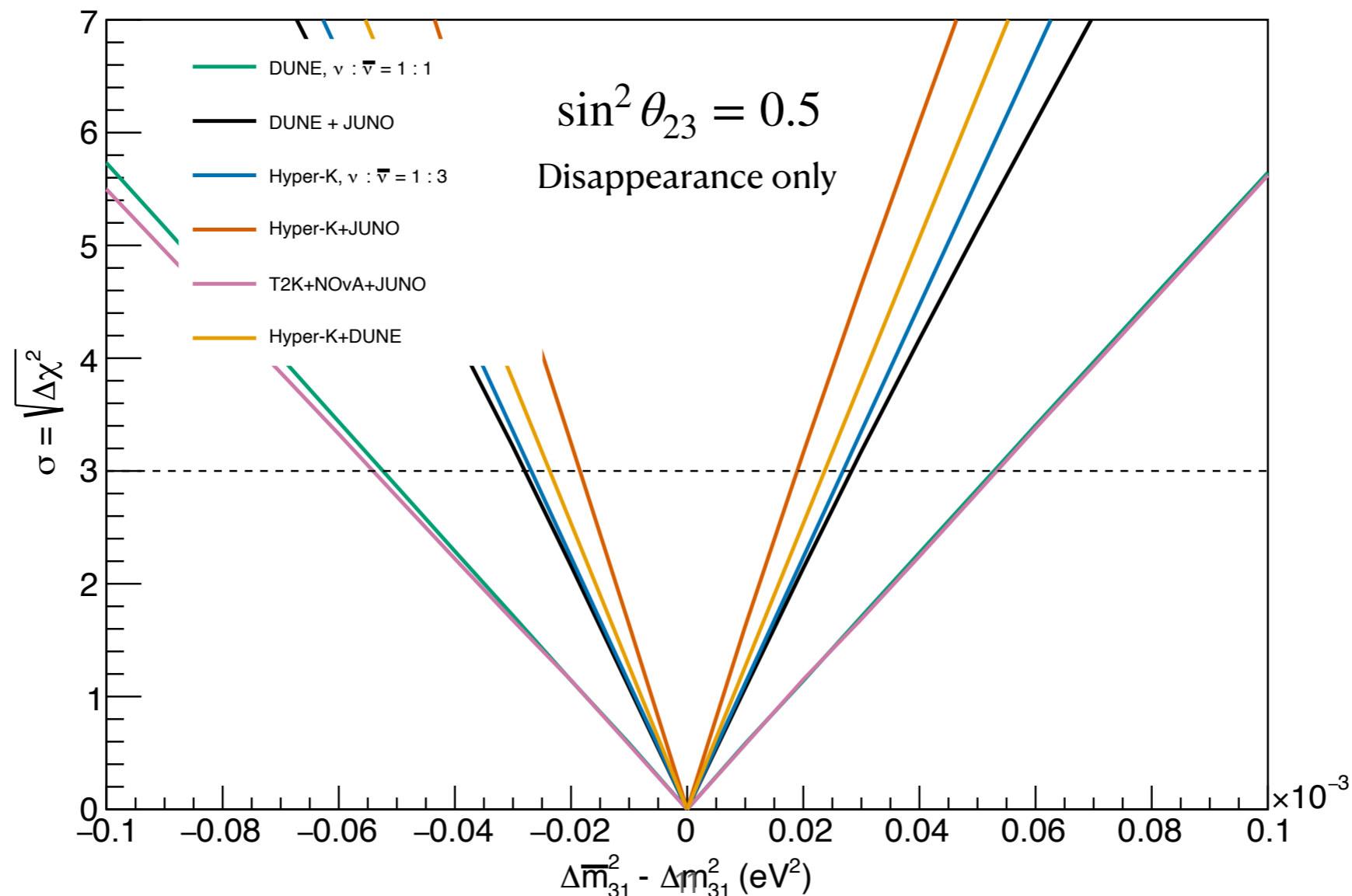


- JUNO will have better than 0.5% precision on $\Delta \bar{m}_{31}^2 \Rightarrow$ it can help to improve constraint on CPTV when combined data of other experiments with JUNO

3. Prospects of CPT tests with neutrino oscillation experiments

The bounds on CPTV with $\delta(\Delta m_{31}^2)$ at 3σ C.L. from different experimental configurations

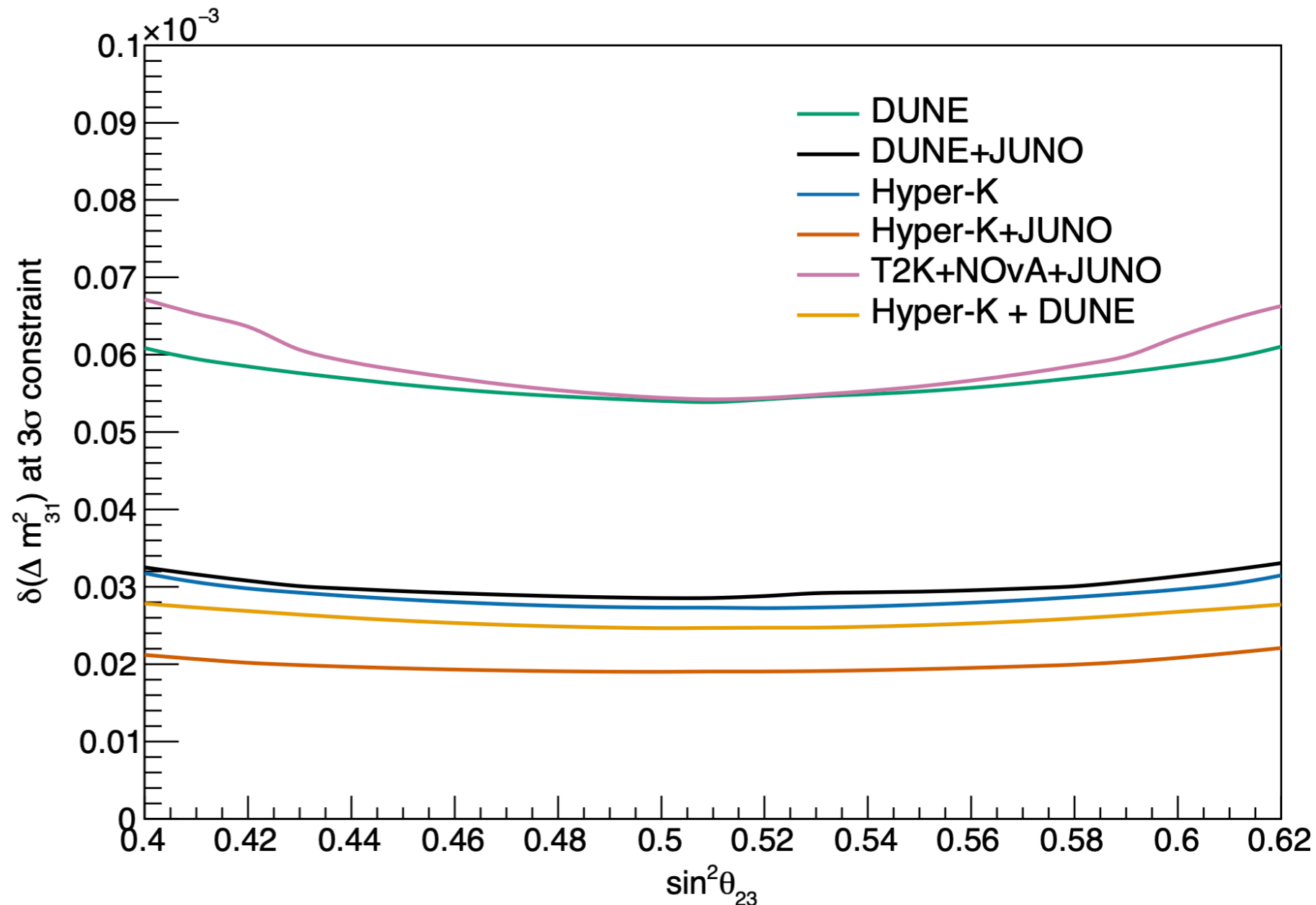
$\sin^2\theta_{23}$	Hyper-K +JUNO	Hyper-K $\nu : \bar{\nu} = 1 : 3$	DUNE + JUNO	DUNE $\nu : \bar{\nu} = 1 : 1$	T2K+NOvA+ JUNO
0,45	1.94E-05	2.76E-05	2.93E-05	5.54E-05	5.75E-05
0,50	1.89E-05	2.64E-05	2.83E-05	5.28E-05	5.33E-05
0,60	2.05E-05	2.91E-05	3.09E-05	5.83E-05	6.15E-05



3. Prospects of CPT tests with neutrino oscillation experiments

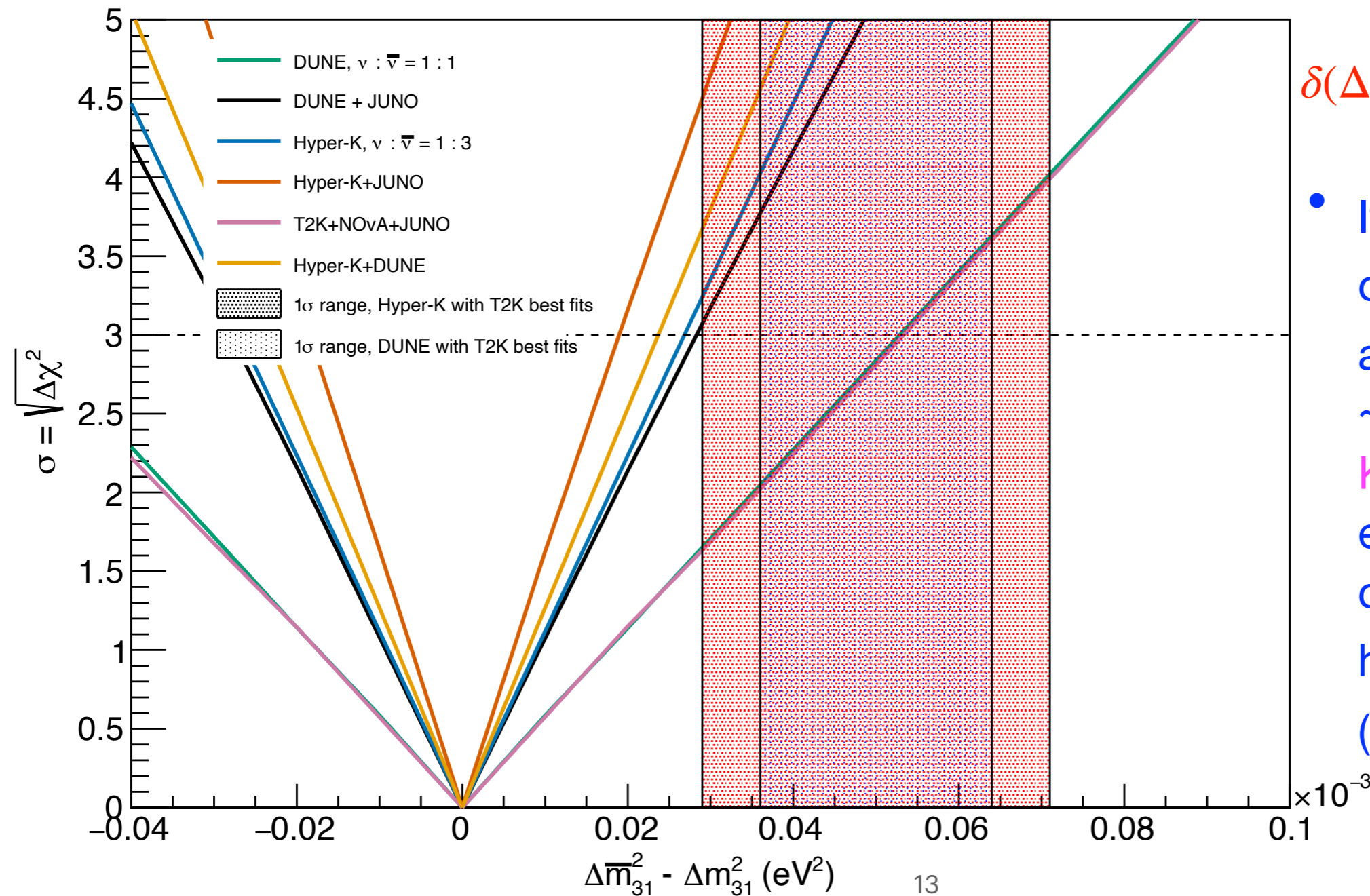
- Assume CPT is conserved, we calculate the bound on CPTV with $\delta(\Delta m_{31}^2)$ at 3σ C.L. within 3σ range of $\sin^2 \theta_{23}$ [0.40 - 0.62]

- Hyper-K will provide the **best constraint** on the CPTV in terms of Δm_{31}^2 among **single detector** experiments
- Hyper-K + JUNO** will give **best constraint** on the CPTV among the considered experimental configurations



3. Prospects of CPT tests with neutrino oscillation experiments

1 sigma uncertainty	HyperK (TDR) <i>arXiv:1805.04163v2</i>	DUNE <i>FPJIC (2020) 80:978</i>
$\Delta m_{31}^2 \text{ eV}^2$	1.5×10^{-5}	1.0×10^{-5}
$\Delta \bar{m}_{31}^2 \text{ eV}^2$	1.5×10^{-5}	1.0×10^{-5}
$\delta(\Delta m_{31}^2) \text{ eV}^2$	2.1×10^{-5}	1.4×10^{-5}

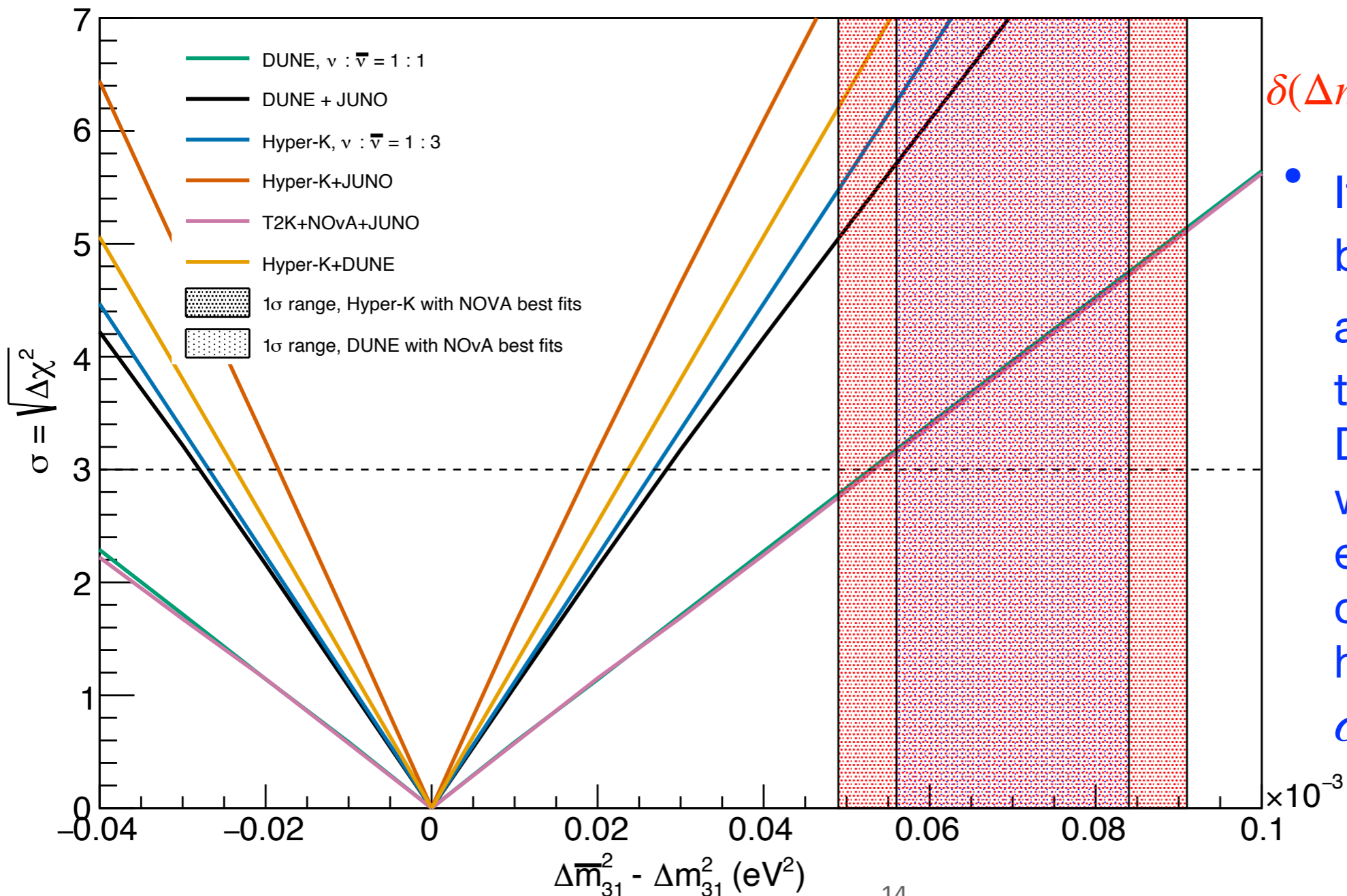


$$\delta(\Delta m_{31}^2)_{\text{T2K}} = 5 \times 10^{-5} \text{ eV}^2$$

- If current T2K best fits on Δm_{31}^2 and $\Delta \bar{m}_{31}^2$ are still true until ~2037, DUNE (Hyper-K) will be able to exclude CPT conservation hypothesis at $\sim 2.0\sigma$ ($\sim 3.2\sigma$) C. L.

3. Prospects of CPT tests with neutrino oscillation experiments

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$\delta(\Delta m_{31}^2) \text{ eV}^2$	2.1×10^{-5}	1.4×10^{-5}

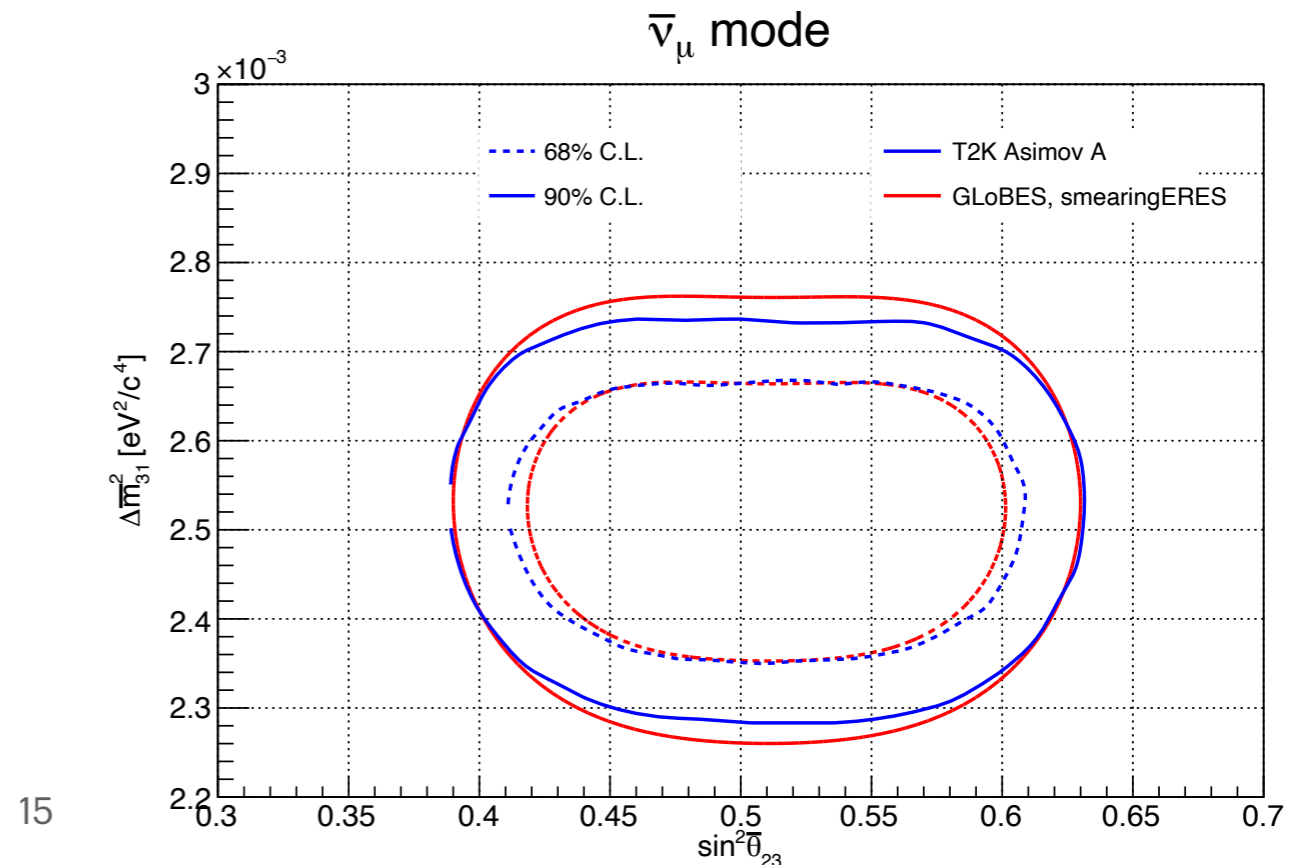
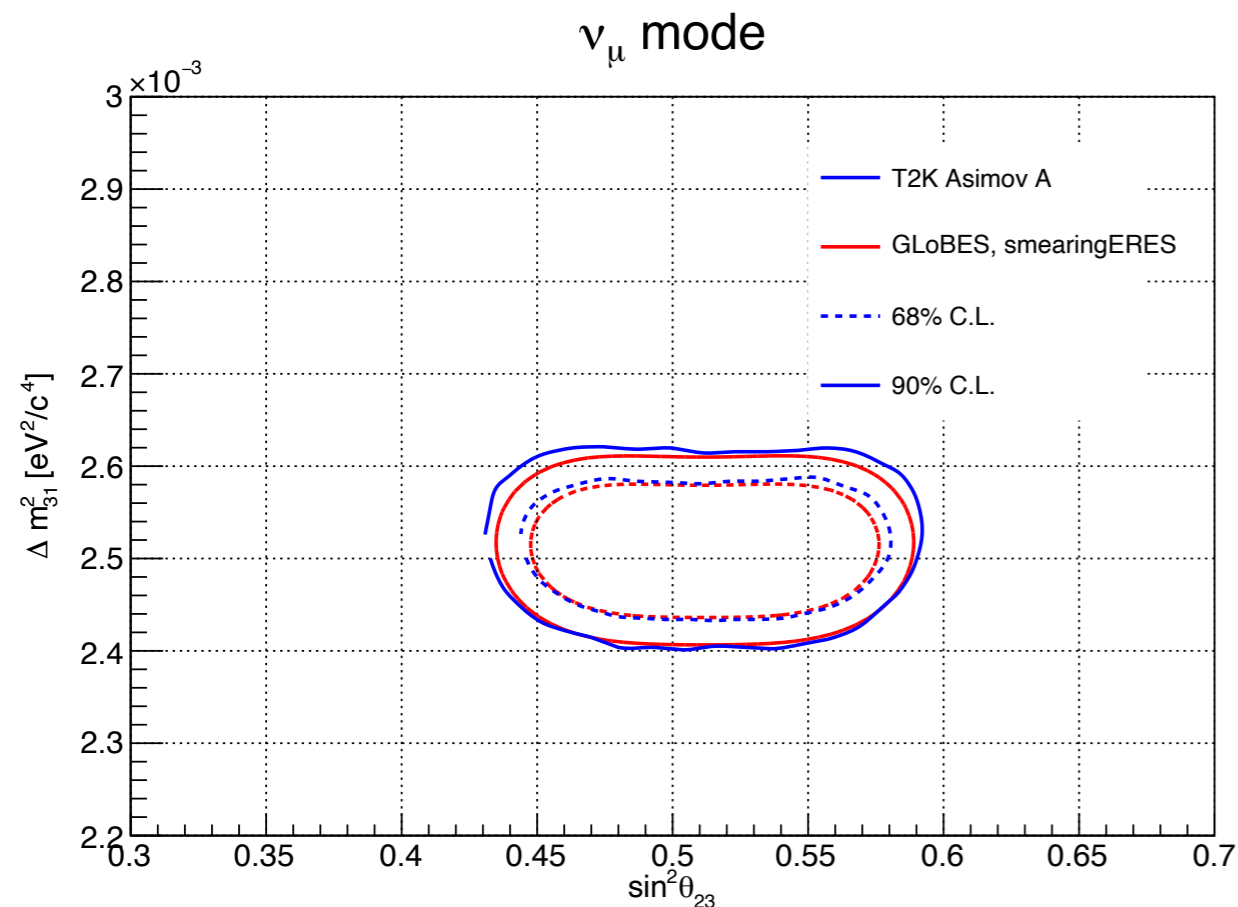


$$\delta(\Delta m_{31}^2)_{\text{NOvA}} = 7 \times 10^{-5} \text{ eV}^2$$

- If current NOvA best fits on Δm_{31}^2 and $\Delta \bar{m}_{31}^2$ are still true until ~2037, DUNE (Hyper-K) will be able to exclude CPT conservation hypothesis at $\sim 3.2 \sigma$ ($\sim 5.5 \sigma$) C. L.

3. Prospects of CPT tests with neutrino oscillation experiments

- We are developing a framework for global data fit using GLoBES
 - Update GLoBES to include interested oscillation parameters for anti-neutrino
 - Validate the experiments with real setups and their released data
 - Combine the data for the experiments
- We have tried to validate the T2K
 - Thinking of how to evaluate the difference between the two as an uncertainty in the data fit result



4. Conclusion

- Current T2K, NOvA and combined T2K+NOvA+DayaBay data are consistent with CPT conservation
- Hyper-K will provide the best constraint on CPTV in terms of $\delta(\Delta m_{31}^2)$ among the single detector experiments
- Hyper-K + JUNO has best constraint to the CPTV among the considered configurations
- **HyperK** can exclude CPT conservation at (5.5σ) 3.2σ *C.L.* if the current best fits of **(NOvA)** **T2K** on Δm_{31}^2 and $\Delta \bar{m}_{31}^2$ are still true until ~2037
- **DUNE** can exclude CPT conservation at (3.2σ) 2.0σ *C.L.* if the current best fits of **(NOvA)** **T2K** on Δm_{31}^2 and $\Delta \bar{m}_{31}^2$ are still true until ~2037
- A framework for global data fit on CPTV constraint has being developed



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