

BSM from SM precision

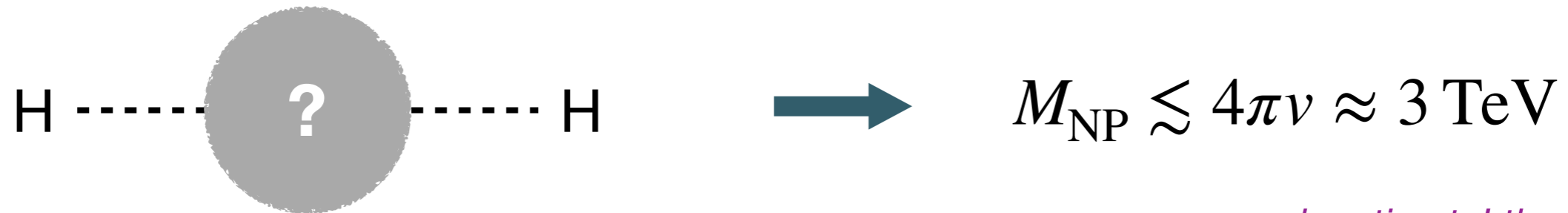
Dario Buttazzo



Why colliders?

Goal: explore physics at least up to $M \approx 10 \text{ TeV}$

- ◆ What causes EWSB? i.e. does the SM hold up to few TeV?



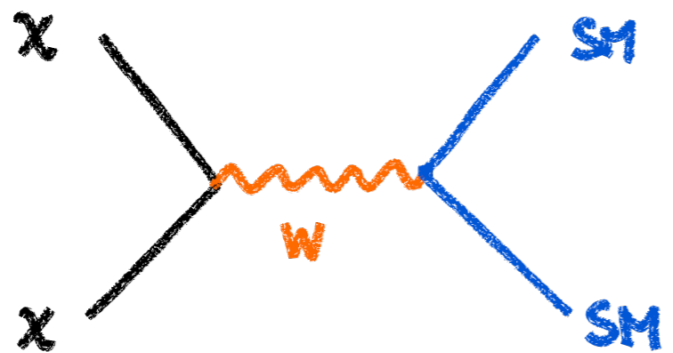
rough estimate! there can easily be some $O(1)$ factor

... and how is it related to the flavor problem?

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- ◆ What causes EWSB? i.e. does the SM hold up to few TeV?
- ◆ What is dark matter? Is it a WIMP?



$$M_{\text{DM}} \approx 1 - 15 \text{ TeV}$$

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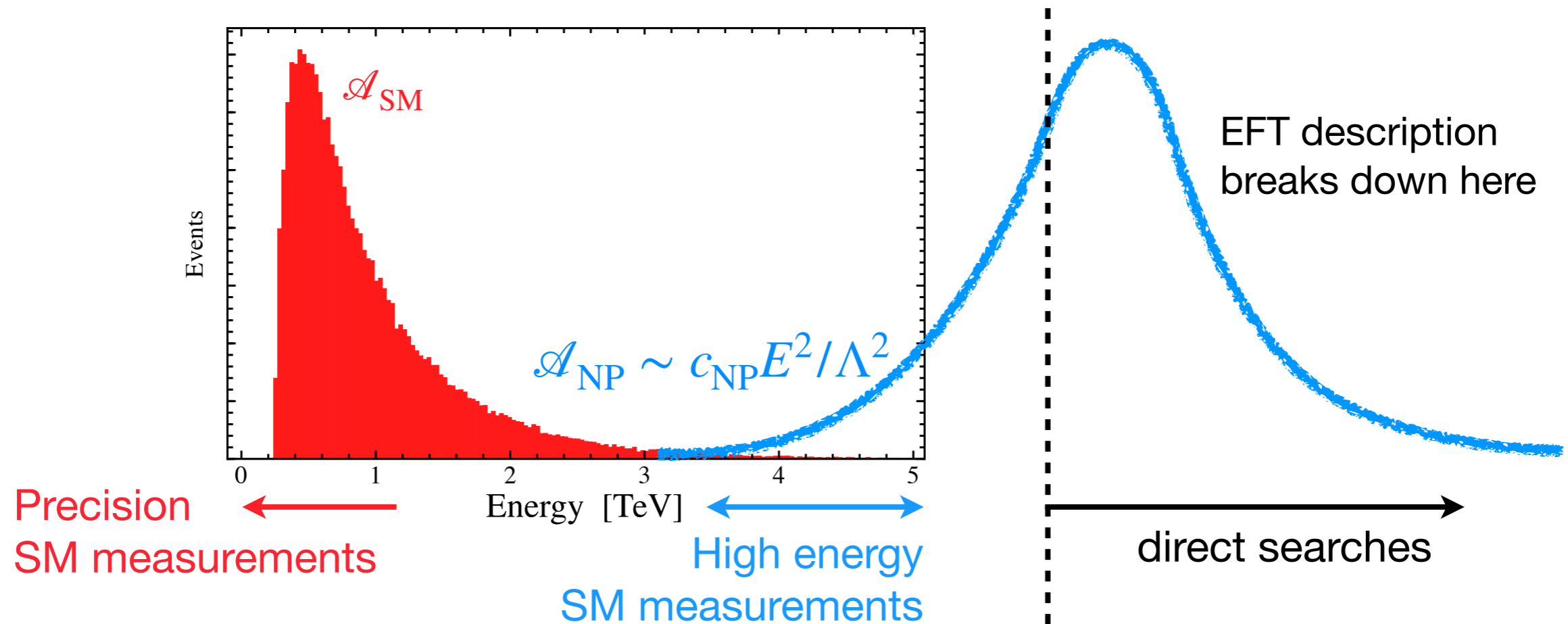
Goal: explore physics at least up to $M \approx 10 \text{ TeV}$

- ◆ What causes EWSB? i.e. does the SM hold up to few TeV?
- ◆ What is dark matter? Is it a WIMP?
- ◆ Electroweak radiation: new phenomena *in the SM*

Restoration of EW symmetry and radiation of “massless” EW bosons



Two paths to precision

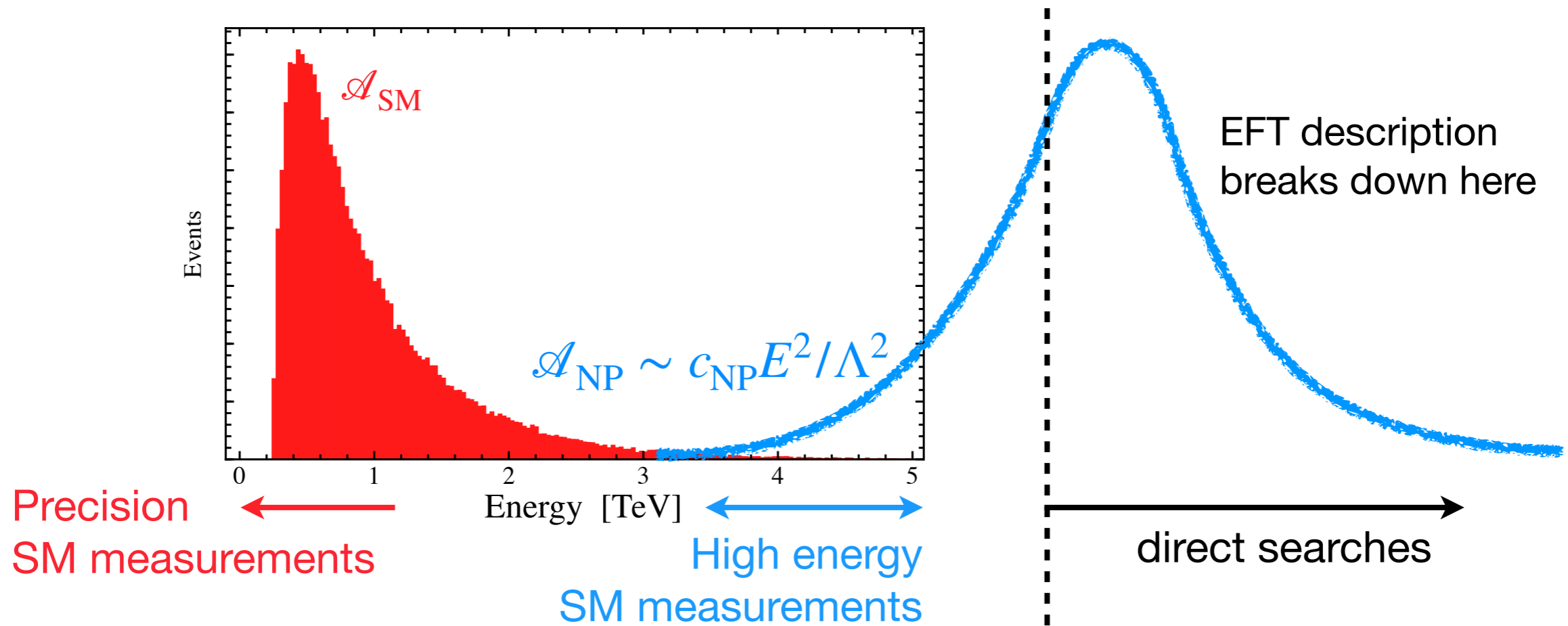


- ◆ The “multipole expansion” of particle physics: EFT

$$\mathcal{L} = \mathcal{L}_{SM}^{d=4} + \frac{1}{\Lambda^2} \sum_i c_i \mathcal{O}_i^{d=6} + \frac{1}{\Lambda^4} \sum_i c_i \mathcal{O}_i^{d=8} + \dots$$

- ▶ Universal: particle content + Lorentz symmetry + SM internal symmetries
- ▶ UV model encoded in values of Wilson coefficients c_i

Two paths to precision



Two ways to improve precision on coefficients (test higher scales Λ)

♦ **High rate:**

More events = Better precision

♦ **High energy:**

New physics effects grow $\sim E^2$

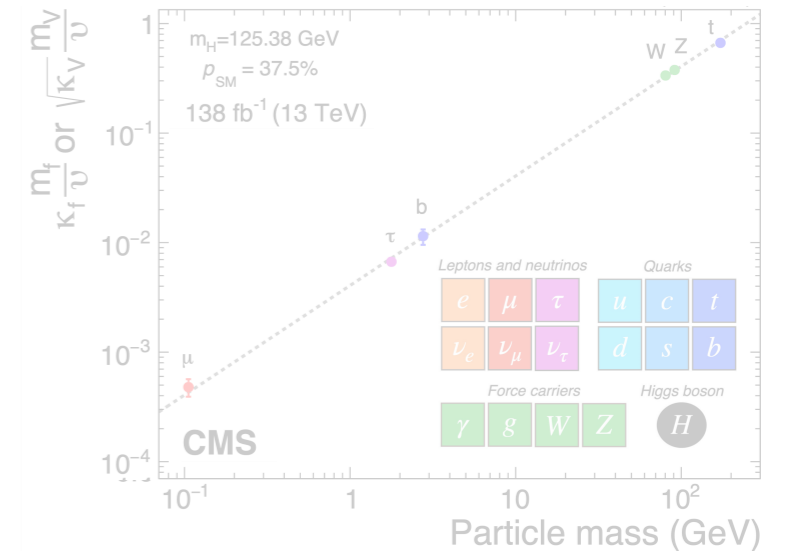
Hard scattering $\sigma_{SM} \sim 1/s$

Where do we stand?

◆ The SM works well at the TeV scale: $\longrightarrow M_{\text{NP}} \gtrsim \text{few TeV directly}$

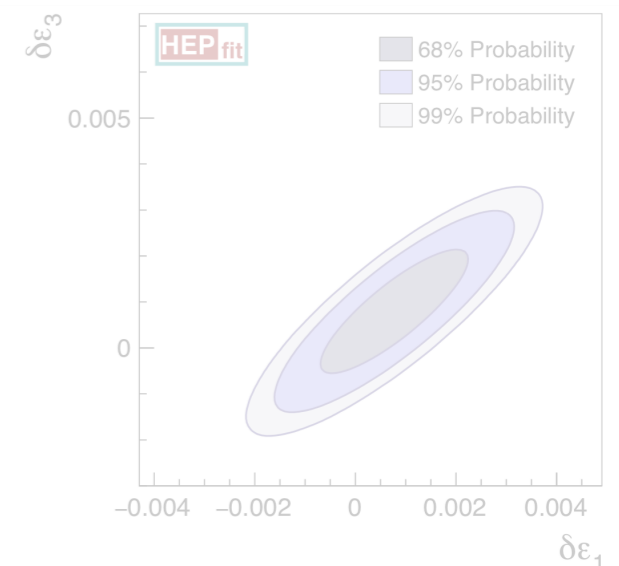
◆ The Higgs boson is SM-like:

$$\delta\kappa \sim \frac{v^2}{M_{\text{NP}}^2} g_\star^2 \lesssim 5\% \quad \longrightarrow \quad M_{\text{NP}} \gtrsim g_\star \text{ TeV}$$



◆ The EW sector is SM-like:

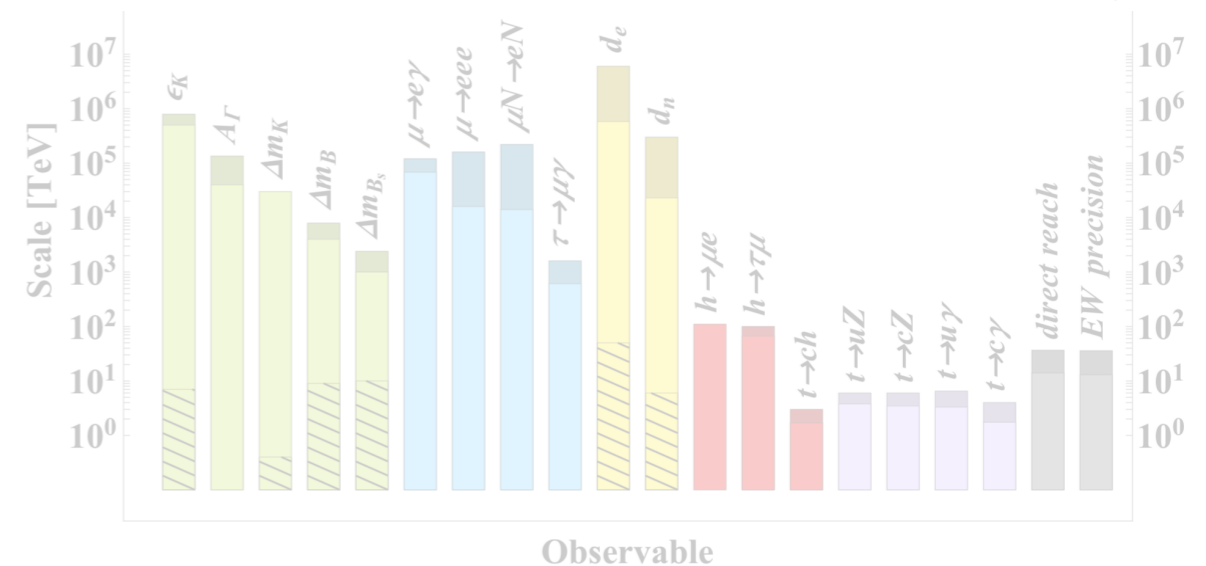
$$\delta\varepsilon \sim \frac{m_W^2}{M_{\text{NP}}^2} \lesssim \text{few} \times 10^{-3} \quad \longrightarrow \quad M_{\text{NP}} \gtrsim 2 \text{ TeV}$$



◆ The CKM picture of flavor and CP works well; lepton flavor is conserved

$$\frac{\delta\mathcal{O}_{ij}}{\mathcal{O}_{ij}^{\text{SM}}} \sim \frac{v^2}{M_{\text{NP}}^2} \frac{4\pi}{\alpha} \frac{c_{ij}}{\xi_{ij}} \lesssim 10\% \quad \text{flavor suppression of the SM}$$

$$\longrightarrow \quad M_{\text{NP}} \gtrsim 3 \text{ TeV} \left(\frac{c_{ij}}{\xi_{ij}} \right)^{1/2}$$

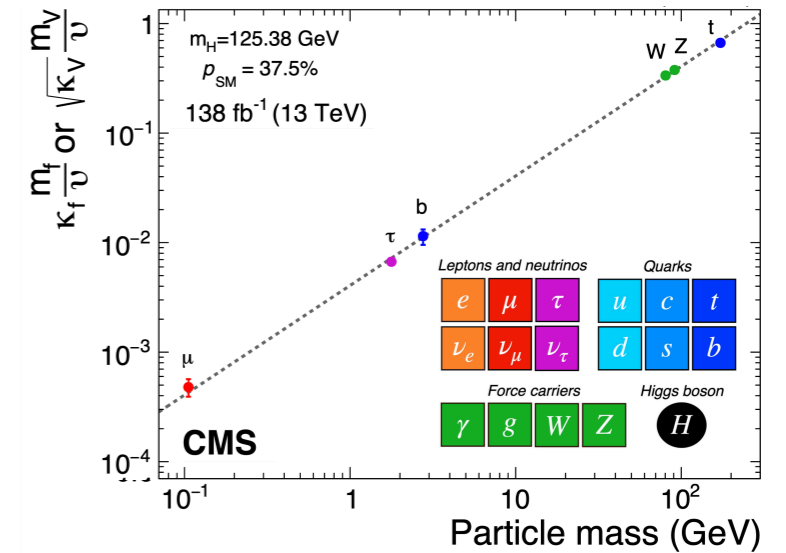


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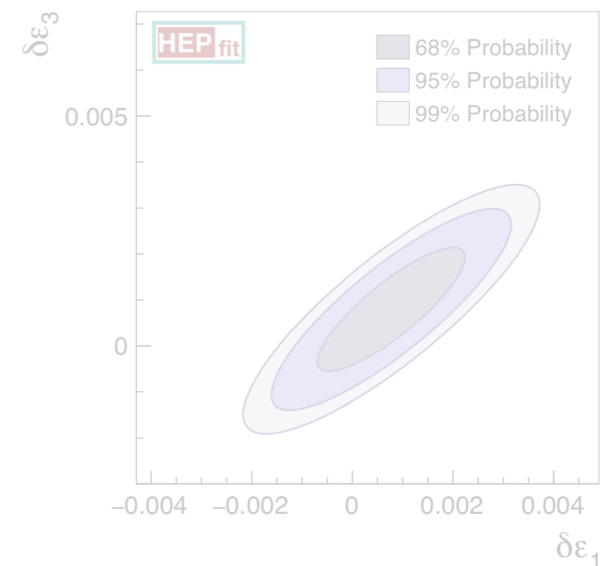
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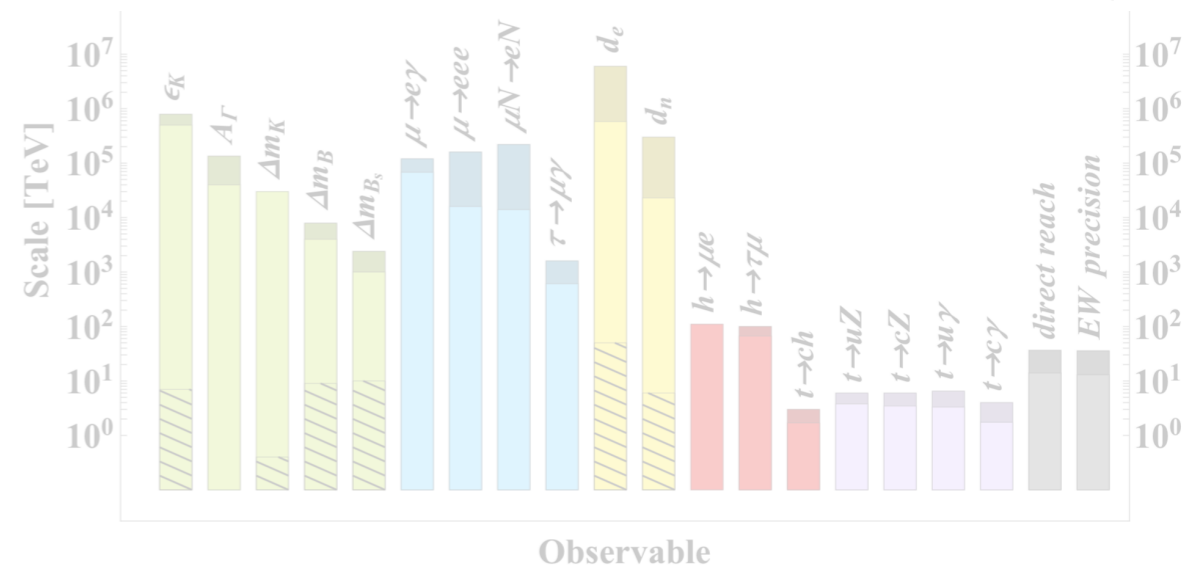
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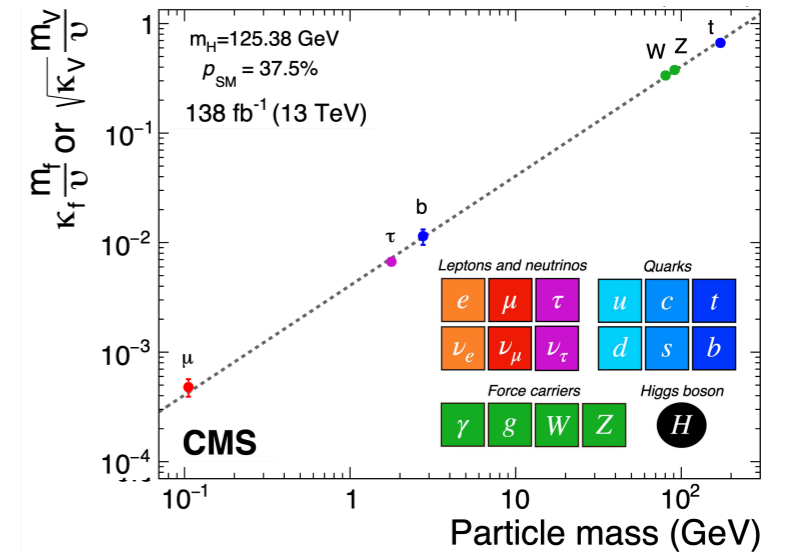


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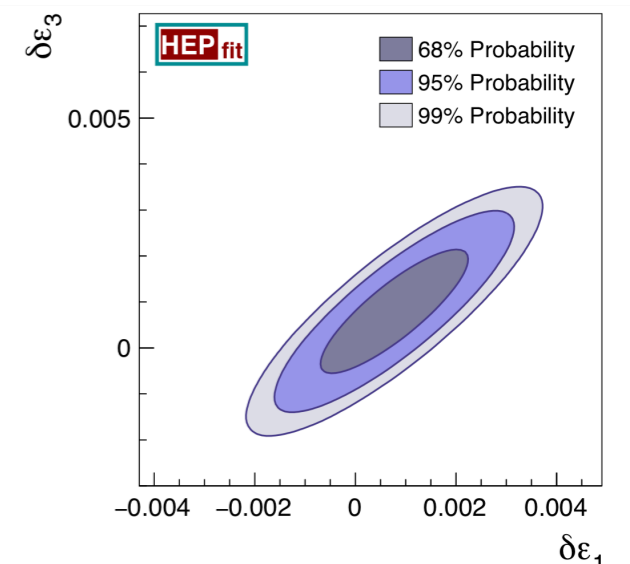
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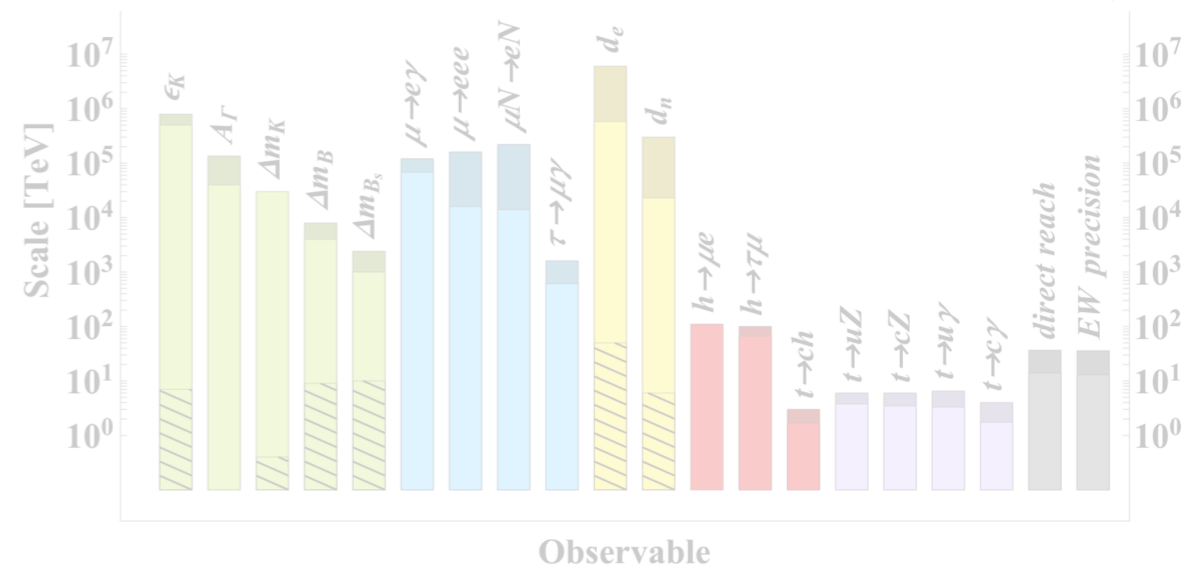
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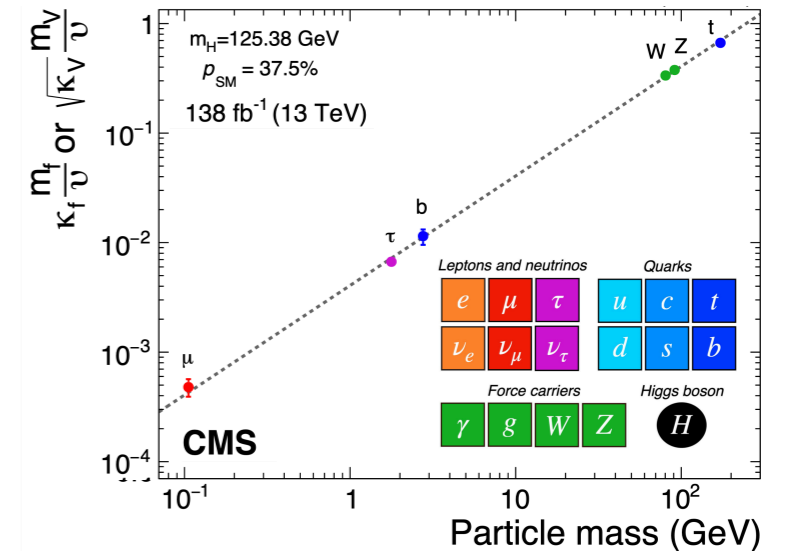


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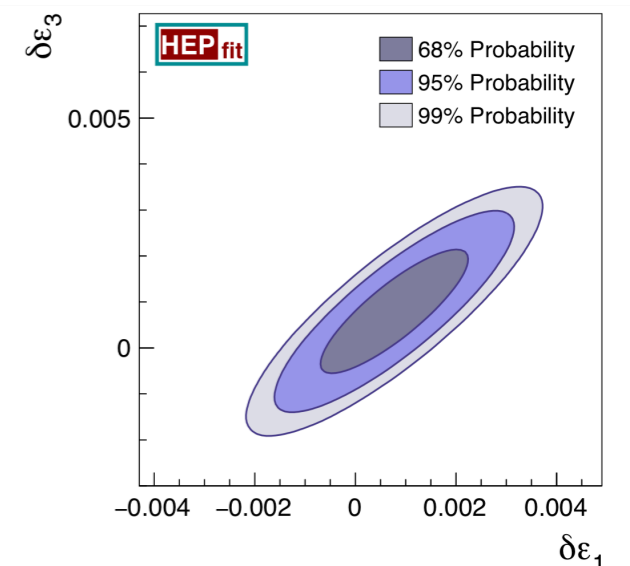
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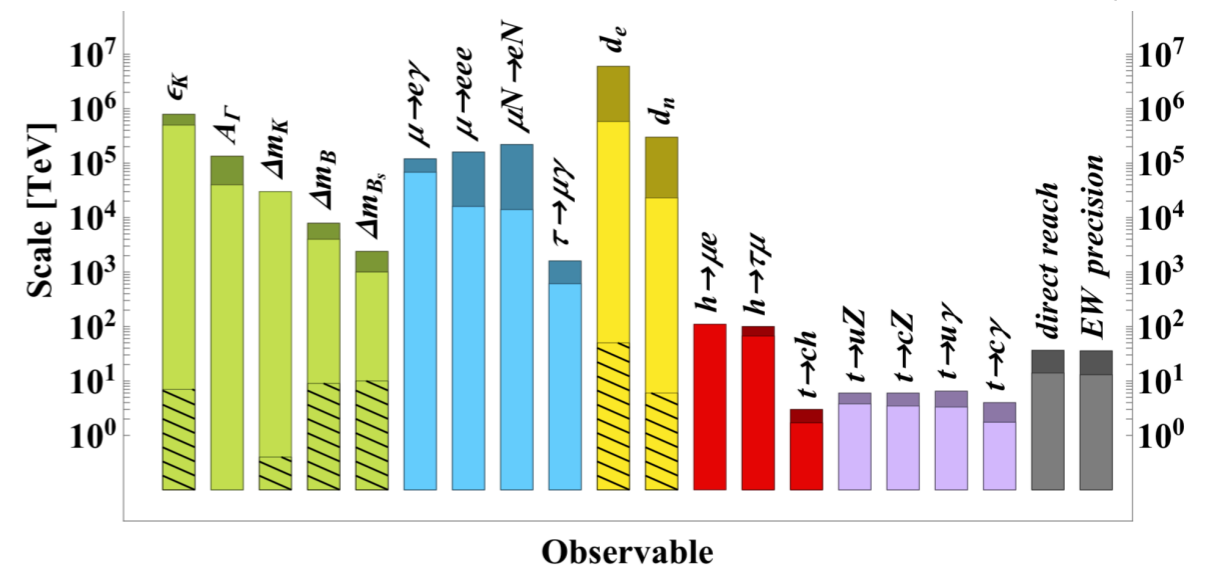
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The flavor puzzle

- SM Yukawa couplings have an extremely hierarchical pattern

$$\begin{array}{l}
 m_u \sim \begin{pmatrix} \cdot & \cdot & \text{large red circle} \end{pmatrix} \\
 m_d \sim \begin{pmatrix} \cdot & \cdot & \text{small green circle} \end{pmatrix}
 \end{array}
 \quad
 V_{\text{CKM}} \sim \begin{pmatrix} \text{large purple circle} & \text{small purple circle} & \text{tiny purple circle} \\ \text{small purple circle} & \text{large purple circle} & \text{tiny purple circle} \\ \text{tiny purple circle} & \text{tiny purple circle} & \text{large purple circle} \end{pmatrix}
 \quad
 m_\ell \sim \begin{pmatrix} \cdot & \cdot & \text{small blue circle} \end{pmatrix}$$

➡ What's the origin of this flavor structure? Why are there 3 families?

- Most likely NP in the Higgs sector couples to SM fermions in similar way...

$$Y_u \approx \begin{pmatrix} \text{small} & \text{dashed box with tiny red dot} \\ \text{dashed line} & \text{large red circle} \end{pmatrix}
 \quad
 \begin{array}{c} \text{fermion} \\ \text{fermion} \end{array} \text{---} \text{NP} \text{---}$$

$$\lambda_q \approx \begin{pmatrix} \text{small} & \text{dashed box with tiny red dot} \\ \text{dashed box with tiny red dot} & \text{large red circle} \end{pmatrix}
 \quad
 \begin{array}{c} \text{fermion} \\ \text{fermion} \end{array} \text{---} \text{NP} \text{---} \begin{array}{c} \text{fermion} \\ \text{fermion} \end{array}$$

- Symmetries: e.g. MFV or U(2) models

[Barbieri et al. 2011](#); [Isidori et al. 2017](#); ...

- Dynamics: different NP scales for different families, related to Higgs

[Panico, Pomarol 2016](#); [Bordone et al. 2017](#), etc...

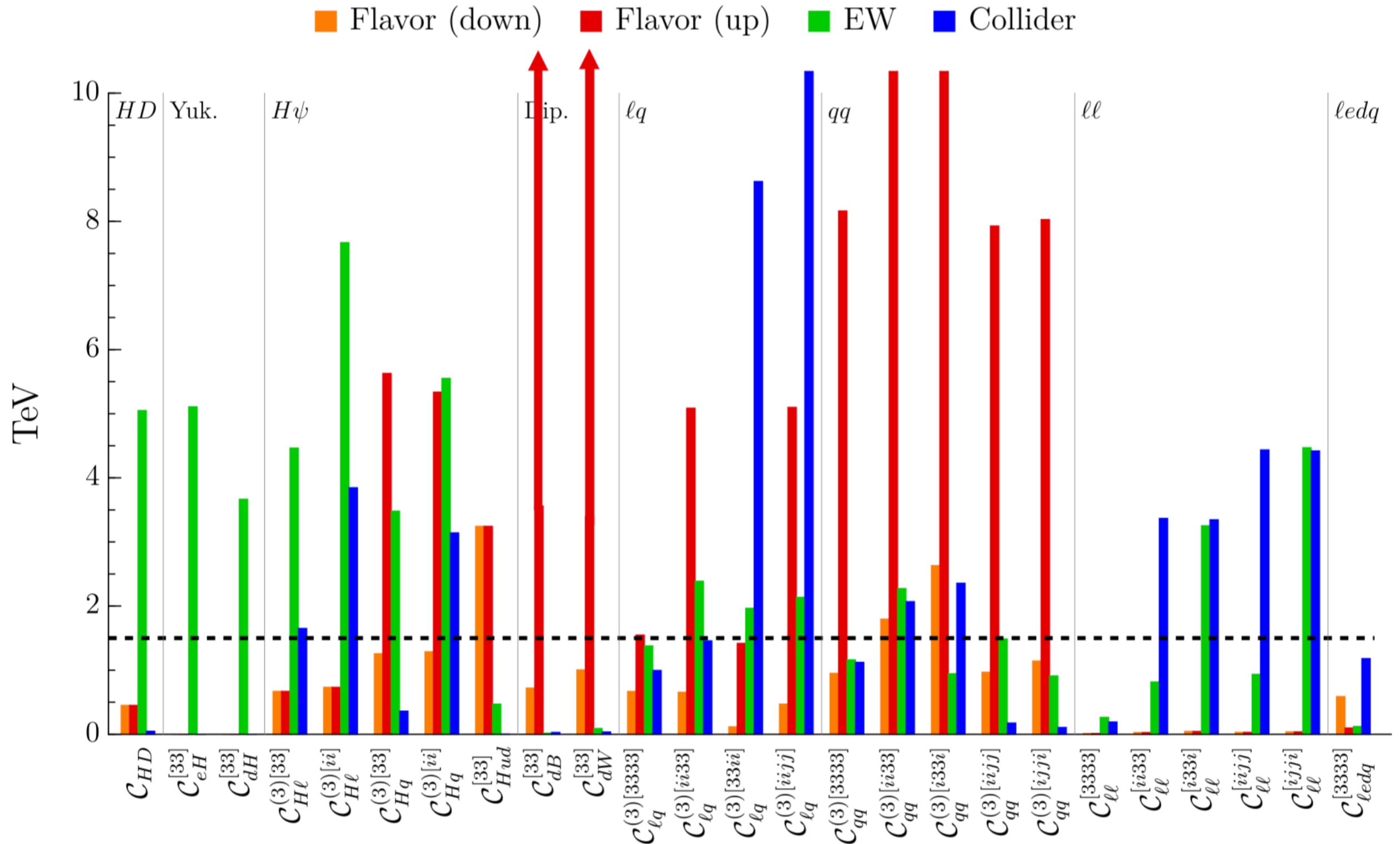


$$M_{\text{NP}} \lesssim 3 \text{ TeV}$$

with O(1) couplings

Where do we stand?

- ◆ SMEFT with CKM-like suppression ($U(2)^3$ flavor symmetry):



Where do we stand?

◆ SMEFT with CKM-like suppression ($U(2)^3$ flavor symmetry):

◆ + mild suppression of light gen. interactions

$$\varepsilon_{\text{loop}} = \frac{g_i}{16\pi^2}$$

$$\varepsilon_Q = 0.16$$

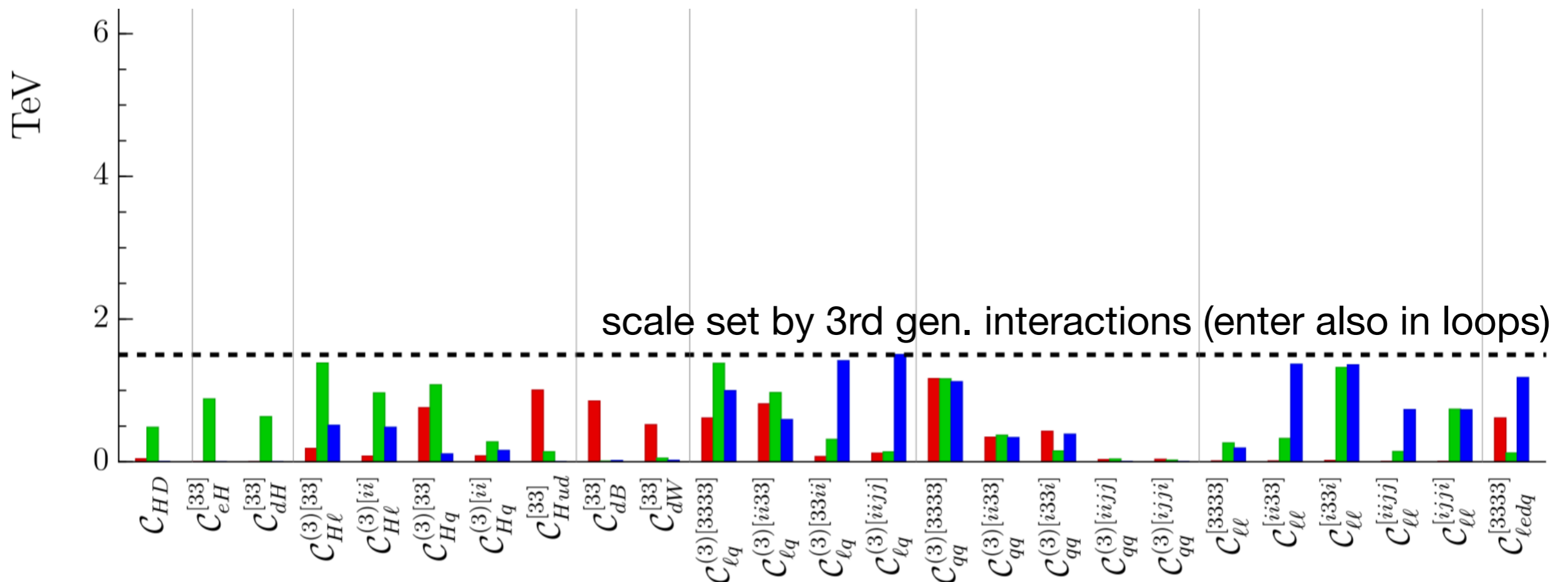
$$\varepsilon_L = 0.40$$

$$\varepsilon_H = 0.31$$

$$\varepsilon_F = 0.15$$

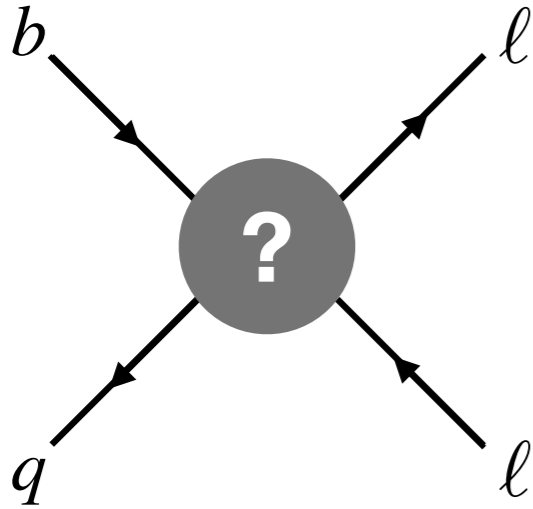
◆ + some flavor alignment

■ Flavor ■ EW ■ Collider



Third-generation flavor processes

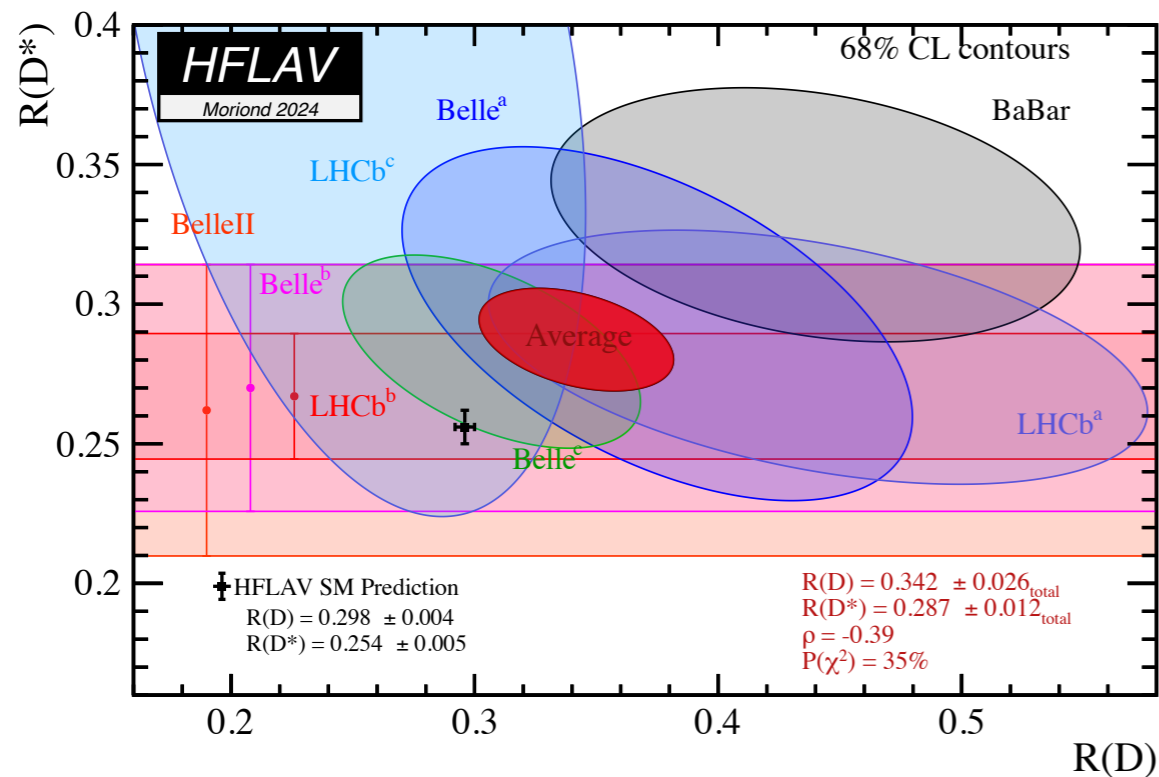
- ◆ Semi-leptonic charged-current decays $b \rightarrow c\tau\nu$



- ◆ Example: left-handed current, EW triplet
(scalar/tensor currents also possible, more constrained)

Third-family operator after CKM rotation $q_L^3 = \begin{pmatrix} V_{i3}u_L^i \\ b_L \end{pmatrix}$

$$(\bar{q}_L^3 \gamma_\mu \sigma^a q_L^3)(\bar{\ell}_L^3 \gamma^\mu \sigma^a \ell_L^3) = V_{cb}(\bar{b}_L \gamma_\mu c_L)(\bar{\nu}_\tau \gamma^\mu \tau_L) + \dots$$

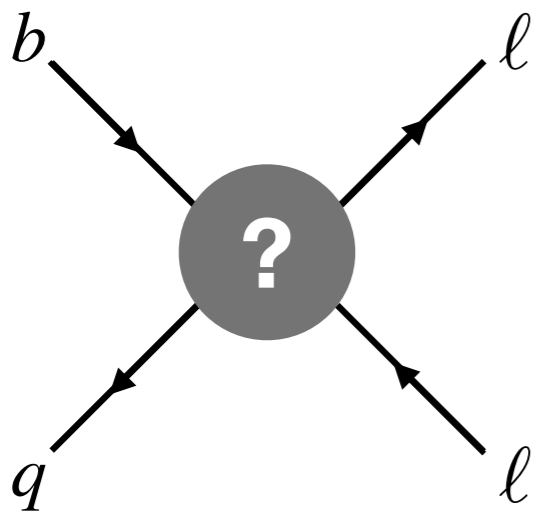


Today: effect $\sim 10\%$ of SM

$$M_{\text{NP}} = \Lambda \times g_\star \gtrsim 1.2 \text{ TeV} \times g_\star$$

Third-generation flavor processes

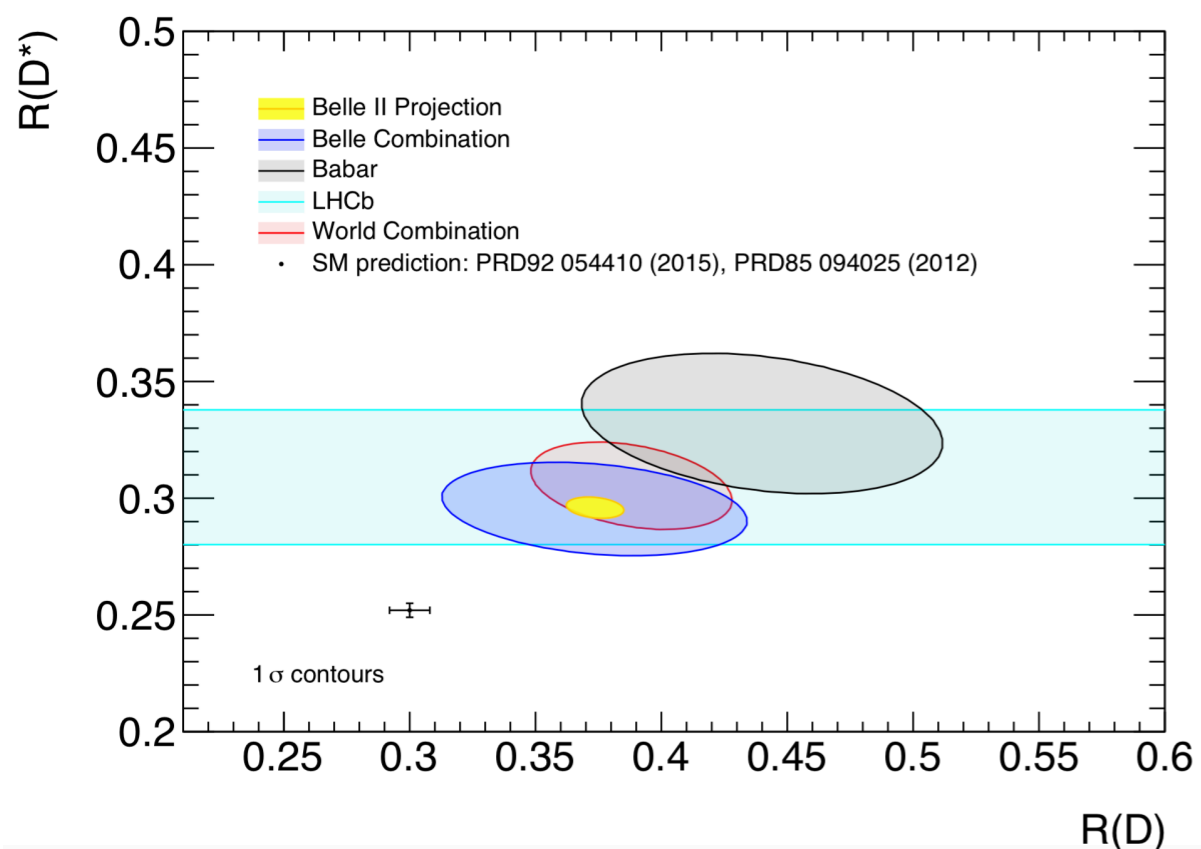
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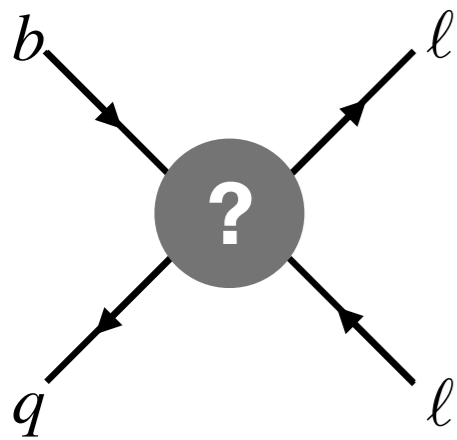


Belle II prospects: ~ 1% of SM

$$M_{\text{NP}} = \Lambda \times g_\star \gtrsim 4 \text{ TeV} \times g_\star$$

👉 talk by F. Forti on Wednesday

Correlations: neutral currents

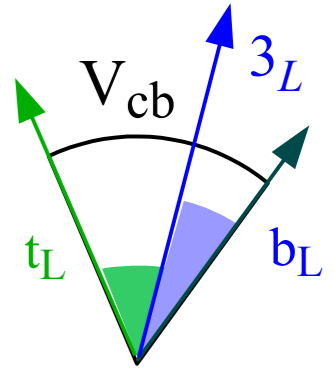


- Flavor misalignment generates FCNC:

$$(\bar{q}_L^3 \gamma_\mu \sigma^a q_L^3)(\bar{\ell}_L^3 \gamma^\mu \sigma^a \ell_L^3) = V_{cb}(1-\theta)(\bar{b}_L \gamma_\mu c_L)(\bar{\nu}_\tau \gamma^\mu \tau_L)$$

$$+ V_{ts} \theta \left[(\bar{b}_L \gamma_\mu s_L)(\bar{\tau}_L \gamma^\mu \tau_L) - (\bar{b}_L \gamma_\mu s_L)(\bar{\nu}_\tau \gamma^\mu \nu_\tau) \right] + \dots$$

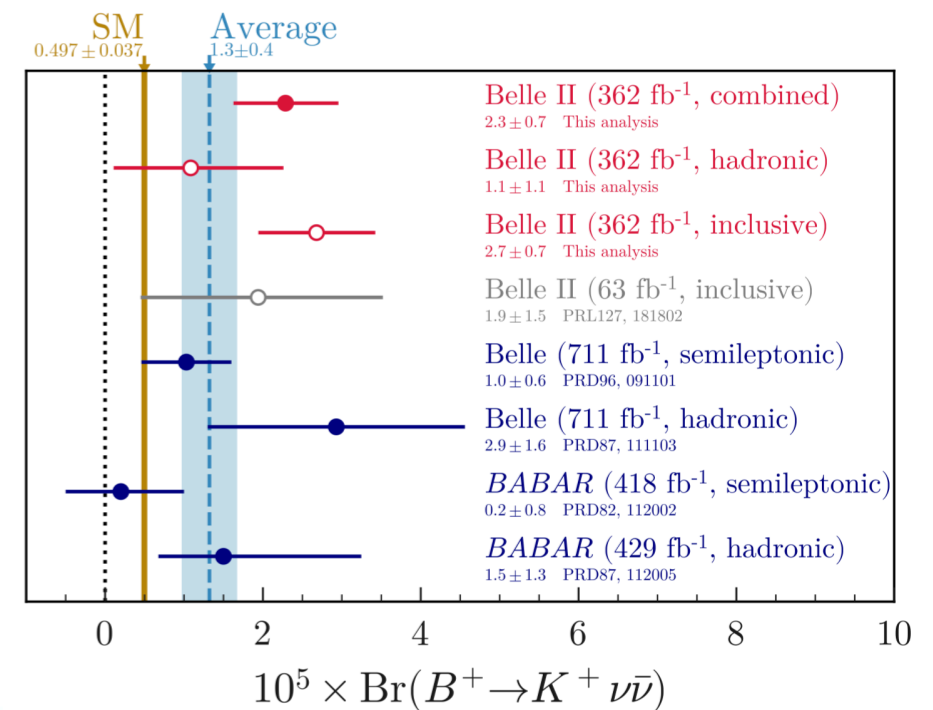
related by $SU(2)_L$



related by $SU(2)_L$
+ flavor

- $b \rightarrow s\nu\nu$ will be measured precisely by Belle II

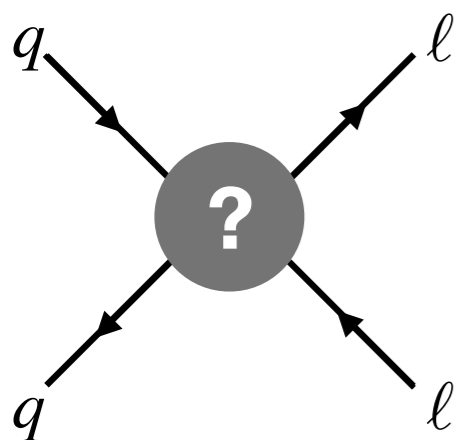
Observables	Belle II 50 ab^{-1}
$\text{Br}(B^+ \rightarrow K^+ \nu \bar{\nu})$	11%
$\text{Br}(B^0 \rightarrow K^{*0} \nu \bar{\nu})$	9.6%
$\text{Br}(B^+ \rightarrow K^{*+} \nu \bar{\nu})$	9.3%



- $b \rightarrow s\tau\tau$ possible at FCC-ee!

Decay mode/Experiment	Belle II (50/ab)	LHCb Upgr. (50/fb)	FCC-ee
$\mathcal{B}(B^0 \rightarrow K^*(892)\tau^+\tau^-)$	~ 10	—	~ 1000
$B_s \rightarrow \mu^+\mu^-$	n/a	~ 500	~ 800
$\mathcal{B}(B_s \rightarrow \tau^+\tau^-)$			
$B^+ \rightarrow \tau^+\nu$	7%	—	2%
$B_c^+ \rightarrow \tau^+\nu$	n/a	—	5%

Correlations: second generation



- Flavor misalignment generates FCNC...

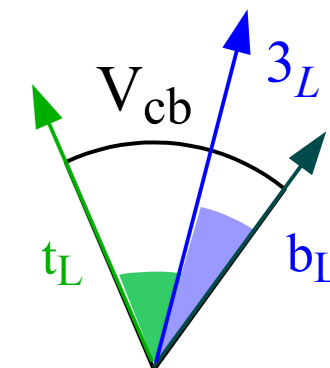
$$(\bar{q}_L^3 \gamma_\mu \sigma^a q_L^3)(\bar{\ell}_L^3 \gamma^\mu \sigma^a \ell_L^3) = V_{cb}(1-\theta)(\bar{b}_L \gamma_\mu c_L)(\bar{\nu}_\tau \gamma^\mu \tau_L)$$

$$+ V_{ts}^* \theta \left[(\bar{b}_L \gamma_\mu s_L)(\bar{\tau}_L \gamma^\mu \tau_L) - (\bar{b}_L \gamma_\mu s_L)(\bar{\nu}_\tau \gamma^\mu \nu_\tau) \right] + \dots$$

related by $SU(2)_L$

$$+ V_{ts}^* V_{td} \theta^2 (\bar{s}_L \gamma_\mu d_L)(\bar{\nu}_\tau \gamma_\mu \nu_\tau) + V_{cb} V_{ub}^* (1-\theta)^2 (\bar{c}_L \gamma_\mu u_L)(\bar{\nu}_\tau \gamma_\mu \nu_\tau)$$

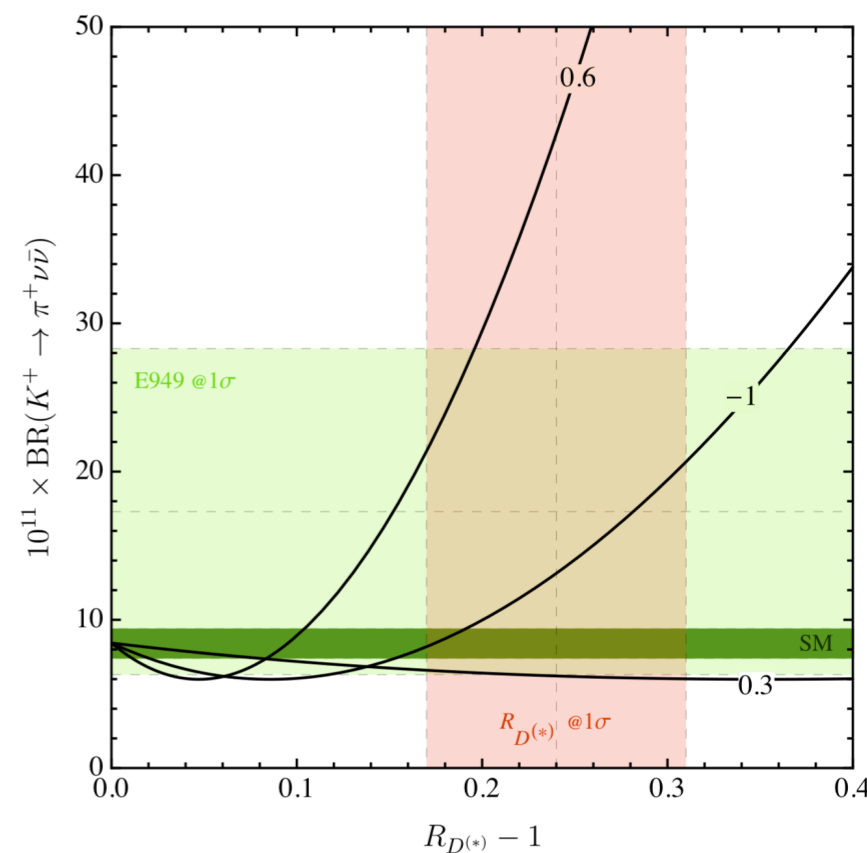
related by $SU(2)_L + \text{flavor}$



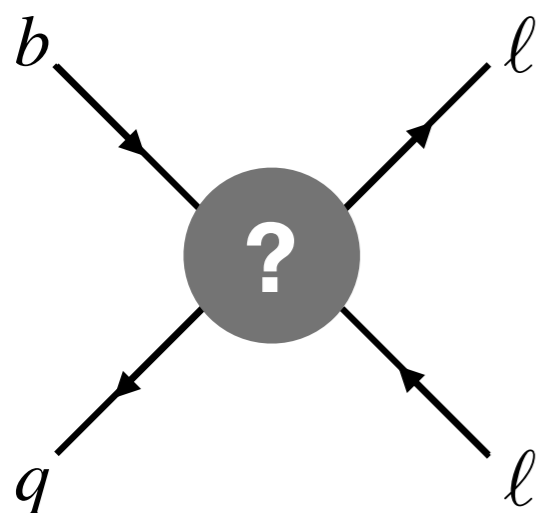
... and couplings to light quarks

- Kaon sector: $s \rightarrow d\nu\nu$ from NA62 and KOTO
- Charm sector: various clean $c \rightarrow u\nu\nu$ decays measurable!

Bause, Gisbert, Golz, Hiller 2010.02225, 2007.05001



High- p_T searches at LHC



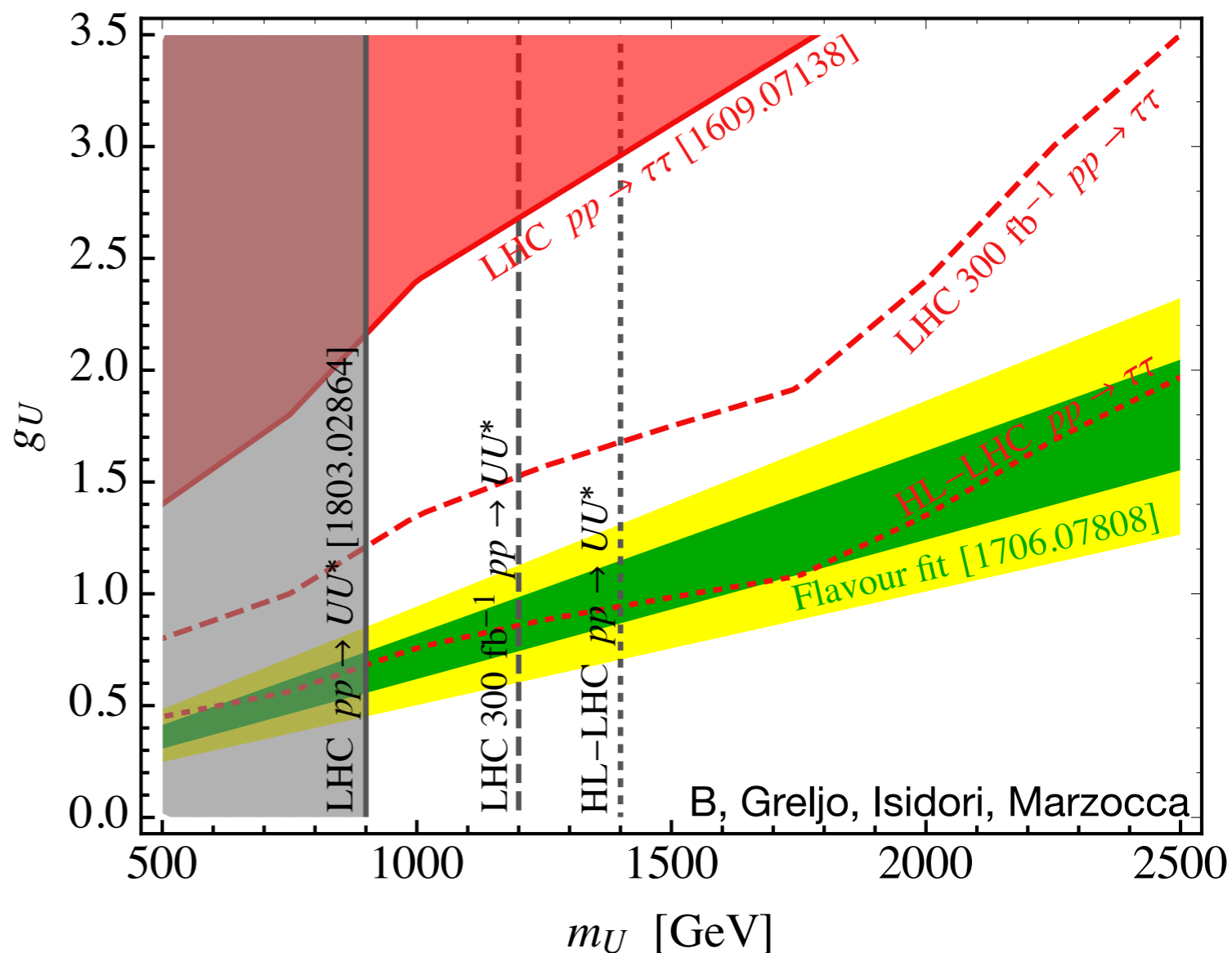
- ◆ The same operators can be probed with high- p_T processes at LHC, e.g. $bb \rightarrow \tau\tau$, $bc \rightarrow \tau\nu$

Faroughy, Greljo, Kamenik 2016

Greljo, Camalich, Ruiz 2018

- ◆ Strong suppression at high invariant masses due to proton PDF
- ◆ Flavor suppression

HL-LHC will not probe the full parameter space testable by rare decays



B, Greljo, Isidori, Marzocca

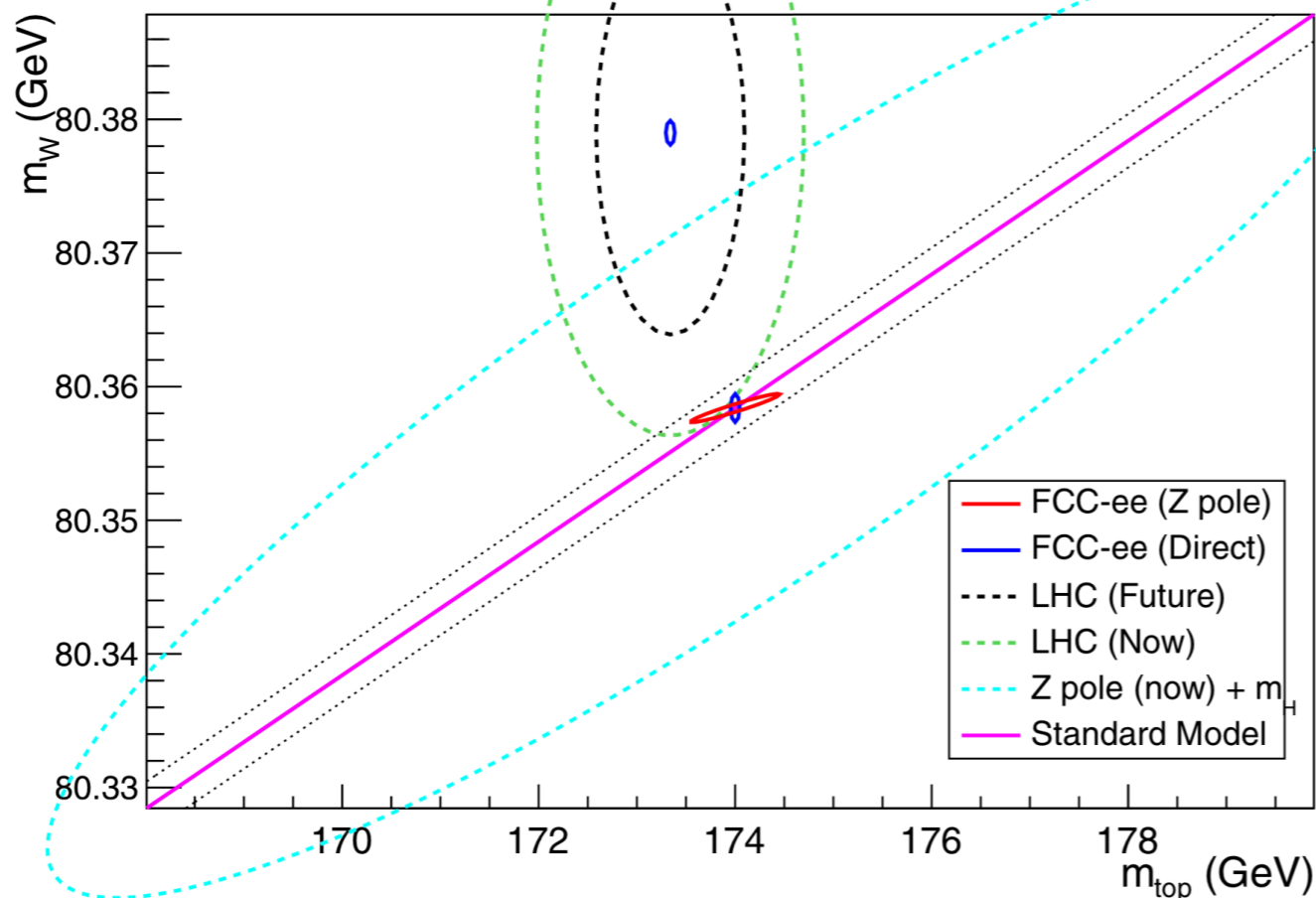
EW precision

- ◆ Higgs & EWSB physics \longleftrightarrow EW precision measurements

$$\mathcal{O}_T = (H^\dagger D^\mu H)^2 \quad \Delta\rho$$

$$\mathcal{O}_W = (H^\dagger \sigma^a D^\mu H) D^\nu W_{\mu\nu}^a \quad \sin^2 \theta_{\text{eff}}$$

$$\mathcal{O}_B = (H^\dagger D^\mu H) \partial^\nu B_{\mu\nu}$$



- ◆ FCC-ee: 6×10^{12} Z bosons
ultimate precision at the Z pole,
limited by syst. and th. errors

$$\Delta \hat{S} \sim \frac{m_W^2}{M_{\text{NP}}^2} \lesssim \text{few} \times 10^{-5}$$

$$\longrightarrow M_{\text{NP}} \gtrsim 12 \text{ TeV}$$

	Current	HL-LHC	ILC ₂₅₀ (& ILC ₉₁)		CEPC	FCC-ee	CLIC ₃₈₀ (& CLIC ₉₁)	
<i>S</i>	0.13	0.053	0.012	0.009	0.0068	0.0038	0.032	0.011
<i>T</i>	0.08	0.041	0.014	0.013	0.0072	0.0022	0.023	0.012

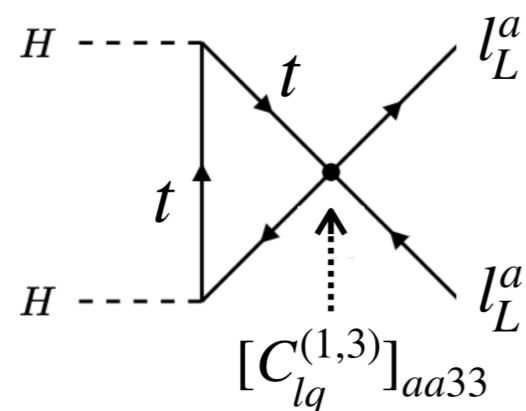
EW precision

Why 10^{12} Z bosons?

- Lepton asymmetries are small: $N_{\text{events}} = N_Z \times \text{BR}(Z \rightarrow \ell^+ \ell^-) \times A_\ell \sim 3 \times 10^{-4} N_Z$
 $\implies N_Z \approx 10^{12}$ for 10^{-4} precision.

- In general, several more operators enter the EW fit

4-fermion interactions affect EW observables through one loop RGE



2311.00020, 1704.04504

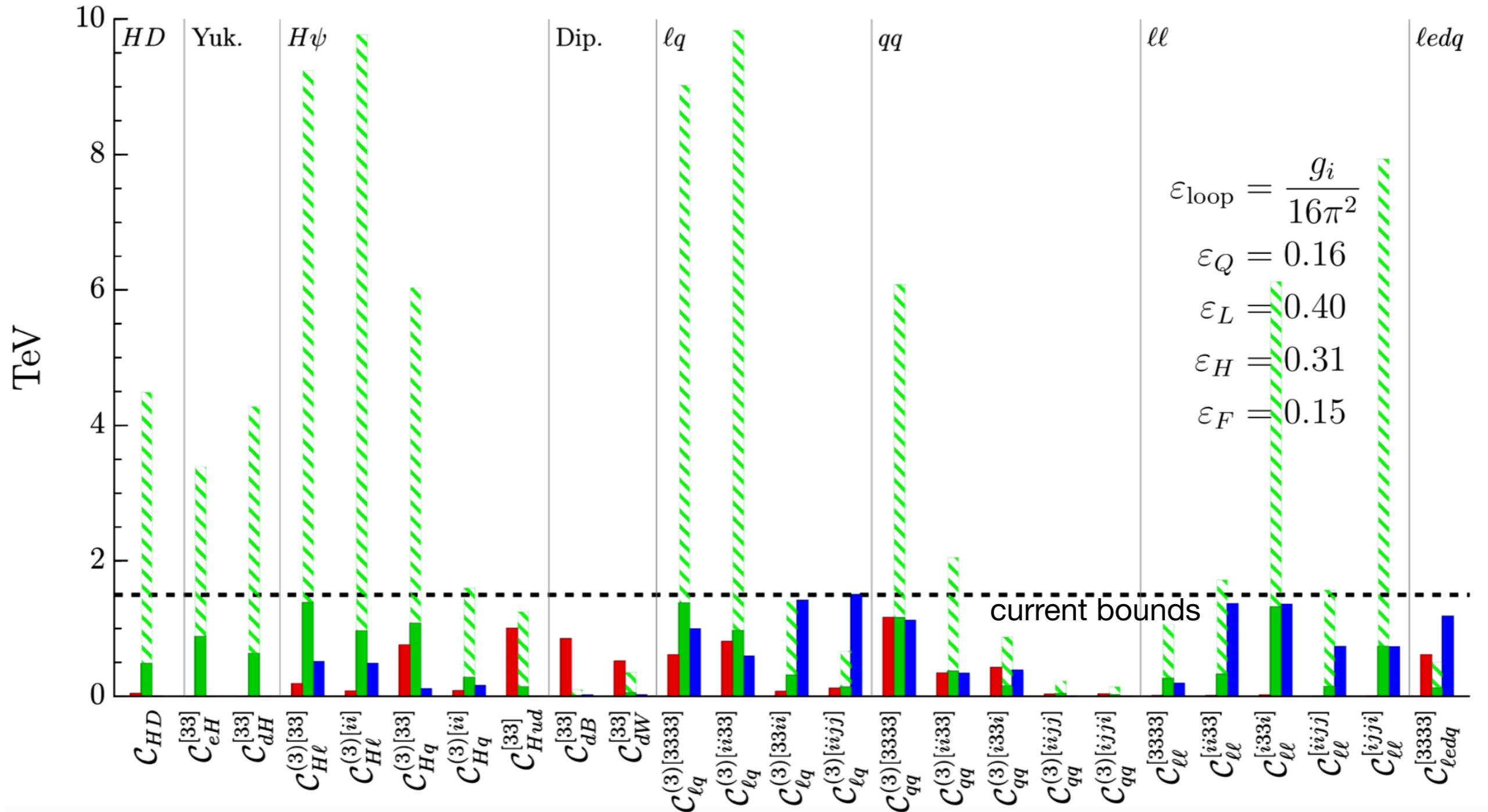
$\dots \longrightarrow [C_{Hl}^{(1,3)}]_{aa}$
 rates and asymmetries
 in $Z \rightarrow \ell\ell$

$b \rightarrow c\ell\nu$ decays,
 LH current

EW precision

- ◆ $U(2)^3$ flavor symmetry + suppression of light gen. + some flavor alignment

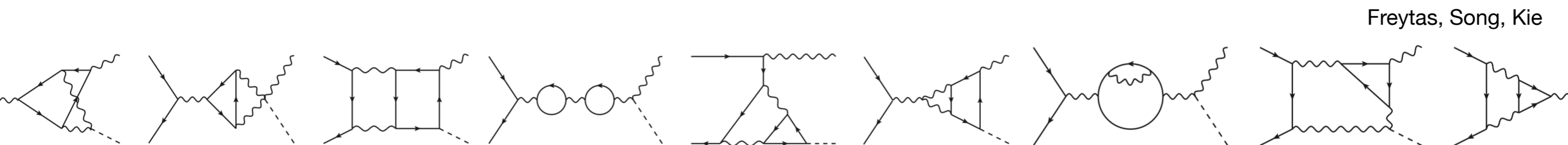
■ Flavor ■ EW ■ Collider



Challenges

- ◆ Precision measurements need to be matched with SM theory predictions of comparable precision
- ◆ Already now, huge rates of b, c hadrons at LHC not always reflected in improvement of physics reach, due to QCD (e.g. hadronic channels, V_{cb} puzzle in semi-leptonic decays, K and D mixing, ...)

$\Delta\hat{S} \lesssim 10^{-5} \longrightarrow$ NNLO EW corrections required

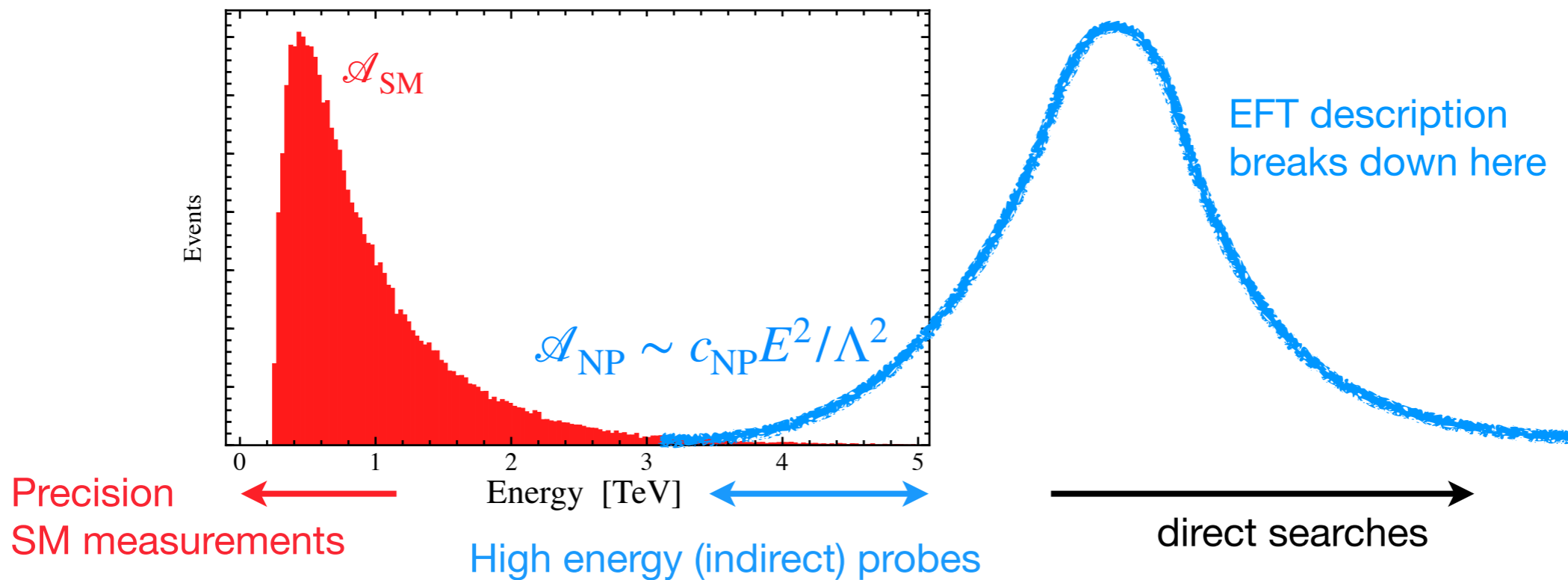


- ◆ High rate measurements eventually limited by systematics

We'll need to measure physics at higher energy to improve!

EW precision at high-energy

- NP effects are more important at high energies $\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda^2} \sum C_i \mathcal{O}_i$



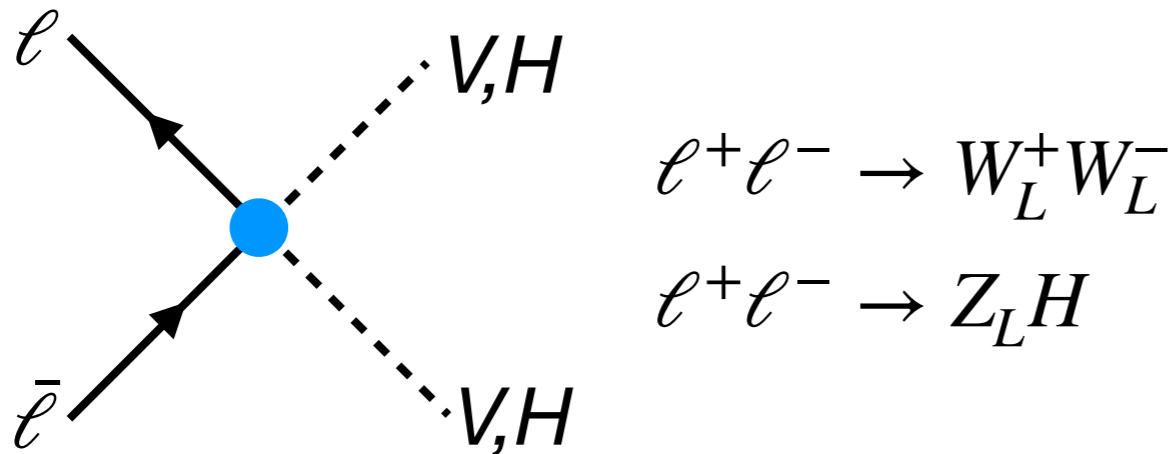
$$\frac{\Delta\sigma(E)}{\sigma_{\text{SM}}(E)} \propto \frac{E^2}{\Lambda_{\text{BSM}}^2} \approx \begin{cases} 10^{-6}, & E \sim 100 \text{ GeV} \\ 10^{-2}, & E \sim 10 \text{ TeV} \end{cases}$$

... taken to the extreme at a μ -collider with 10's of TeV!

- ➡ “Towards a muon collider” Accettura et al. 2303.08533
- ➡ talk by Karri on Thursday

Example: high-energy di-bosons

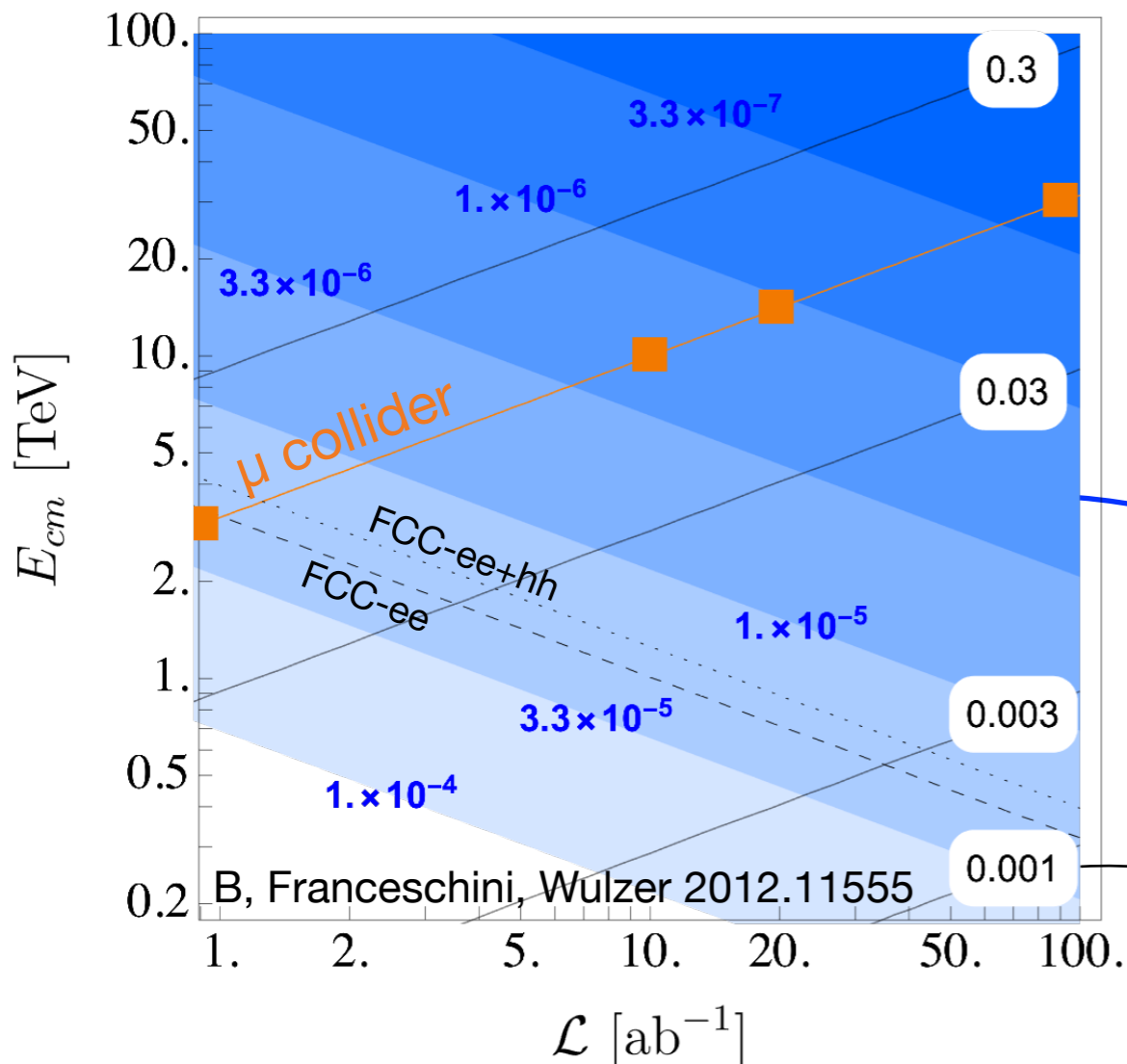
- Longitudinal $2 \rightarrow 2$ scattering amplitudes at high energy:



Determined by the same two operators that affect also EWPT (in flavor-universal theories):

$$\mathcal{O}_W = (H^\dagger \sigma^a D^\mu H) D^\nu W_{\mu\nu}^a$$

$$\mathcal{O}_B = (H^\dagger D^\mu H) \partial^\nu B_{\mu\nu}$$



related with Z-pole observables

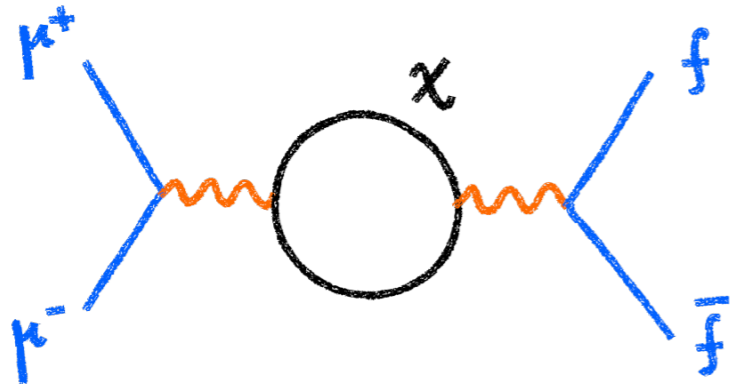
$$\hat{S} = m_W^2 (C_W + C_B)$$

LEP: 10^{-3} , FCC: few 10^{-5} **MuC: 10^{-6}**

precision of measurement

EW-charged matter

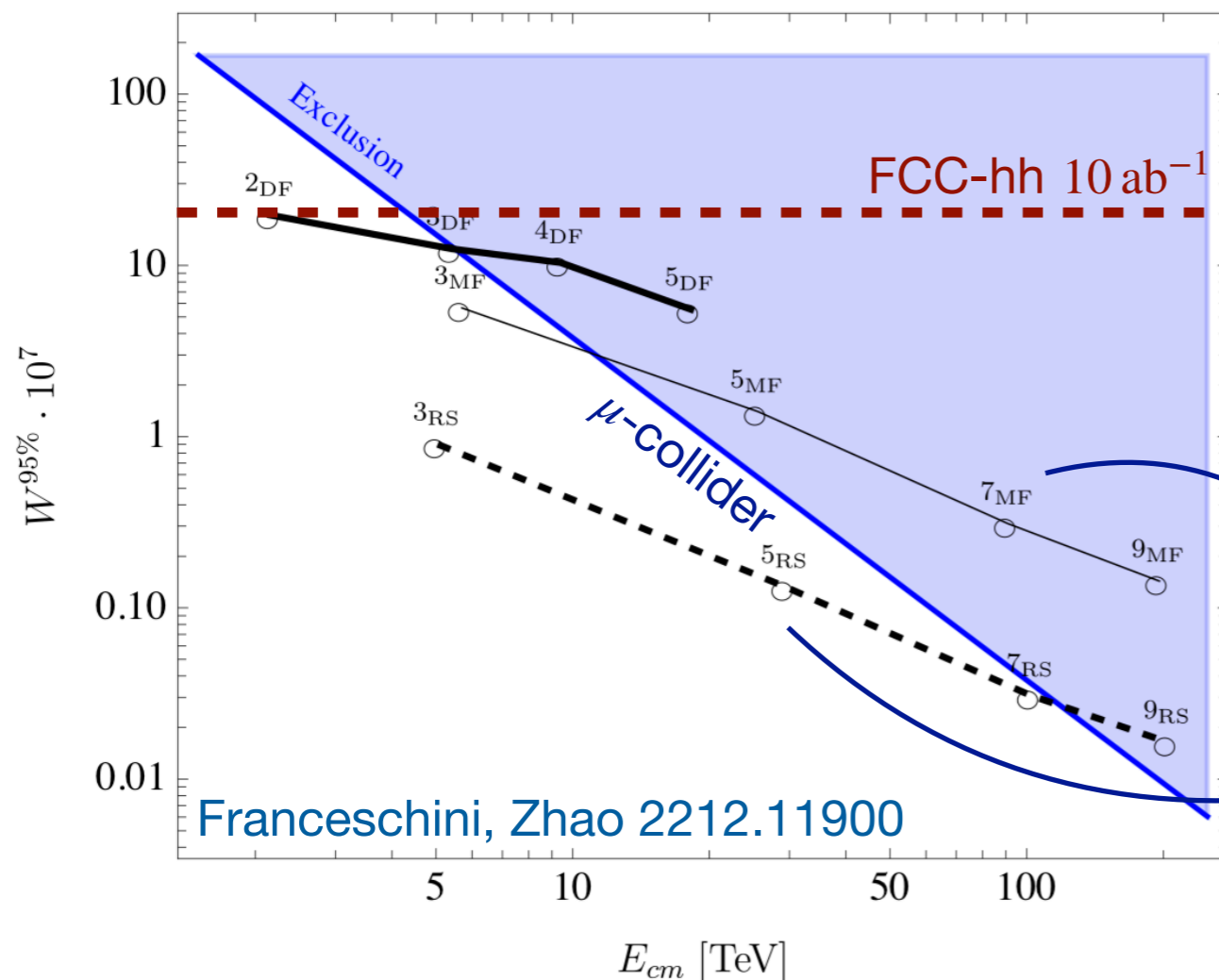
- ♦ All EW multiplets contribute to high-energy $2 \rightarrow 2$ fermion scattering: effects that grow with energy, can be tested at μ collider



can be WIMP dark matter if $M \sim \text{few TeV}$

Cirelli, Fornengo, Strumia hep-ph/0512090

Bottaro, B, Costa, Franceschini, Panci, Redigolo, Vittorio 2107.09688, 2205.04486



$$\hat{W} \approx 10^{-7} \times \left(\frac{1 \text{ TeV}}{M_{\text{DM}}} \right)^2 n^3 \propto 1/n^2$$

$$\hat{Y} \approx 10^{-7} \times \left(\frac{1 \text{ TeV}}{M_{\text{DM}}} \right)^2 Y^2 n \propto 1/n^4$$

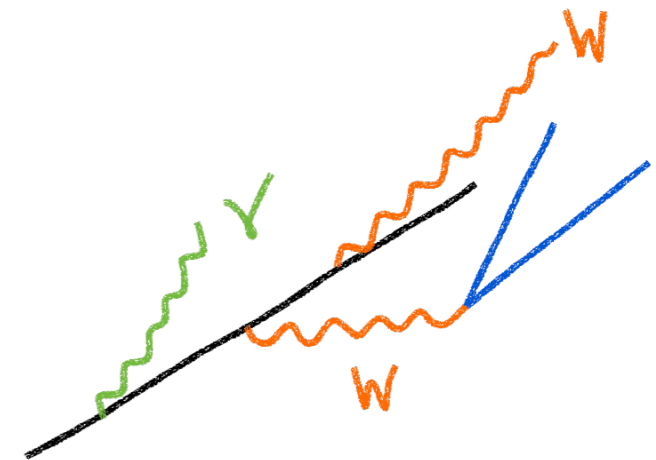
right of blue line: can be tested indirectly

left of blue line: can be tested directly

EW radiation

EW radiation becomes important at multi-TeV energies!

Especially relevant for muon collider, but also FCC-hh...

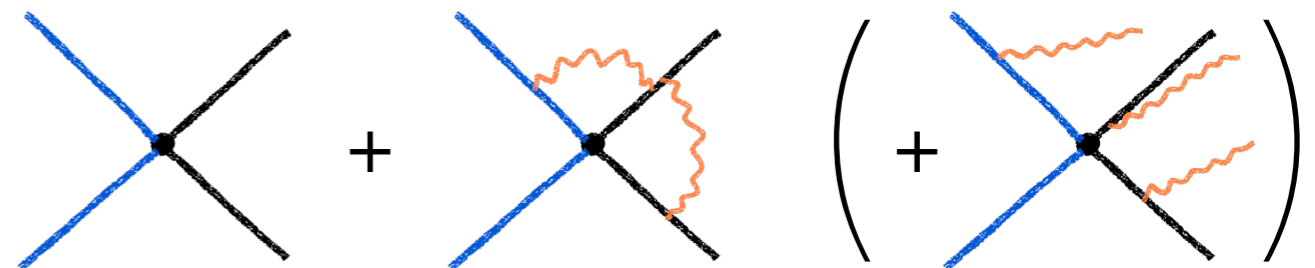


- ◆ $m_{W,Z} \ll E$: γ , W , Z are all similar!
- ◆ Multiple gauge boson emission is not suppressed

$$\text{Sudakov factor } \frac{\alpha}{4\pi} \log^2\left(\frac{E^2}{m_W^2}\right) \times \text{Casimir} \approx 1 \text{ for } E \sim 10 \text{ TeV}$$

- ➔ Which cross-section? Exclusive, (semi-)inclusive, depending on amount of radiation included

see [Chen, Glioti, Rattazzi, Ricci, Wulzer 2202.10509](#)

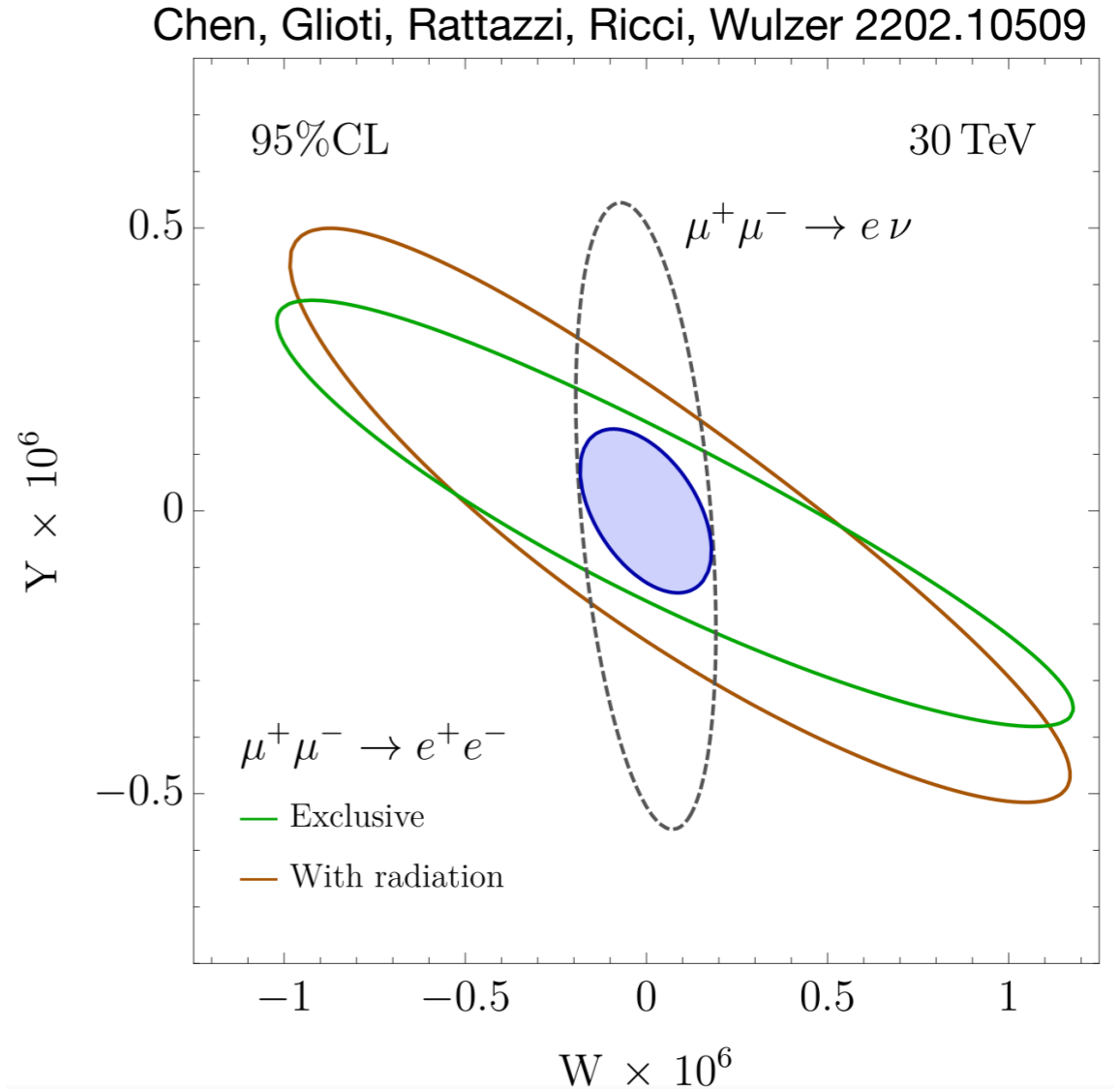
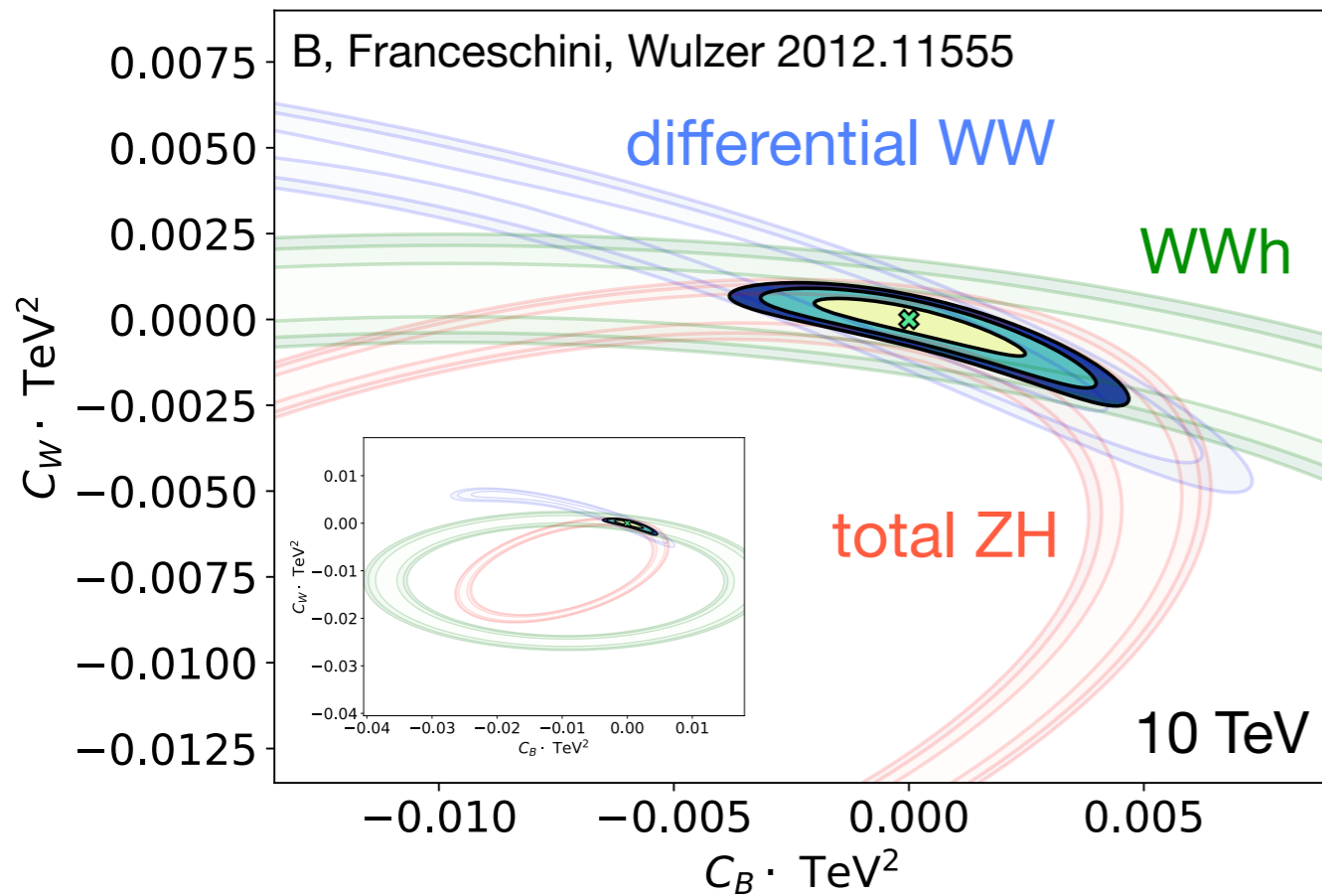


- ➔ Initial state is EW-charged:

(Precise) resummation of double logs needed. Goal: % or ‰ precision

- ➔ Could one define EW jets? Neutrino “jet tagging”?

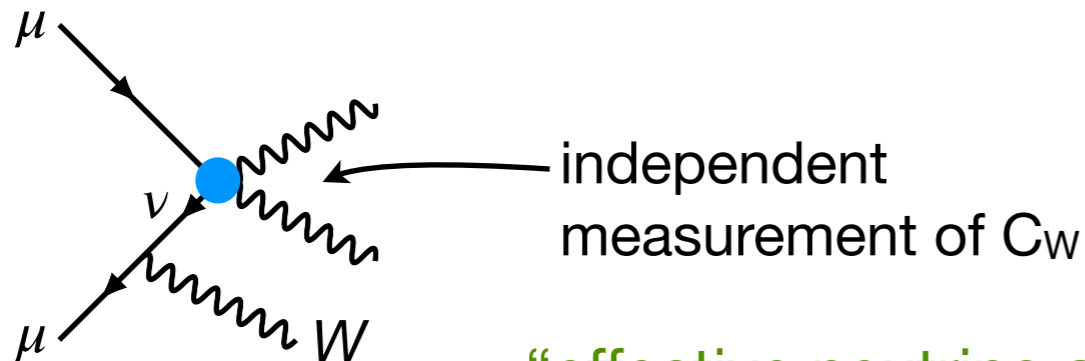
EW radiation



Gauge boson radiation important:

soft W emission allows to access

charged processes $\ell \nu \rightarrow W^\pm Z, W^\pm H$



“effective neutrino approximation”

- ◆ contains new physical information!
- ◆ need to properly define inclusive observables, resummation of logs, ...

Higgs factories

- ◆ All proposed future colliders will be able to produce millions of Higgses
→ study single Higgs couplings with below percent precision!

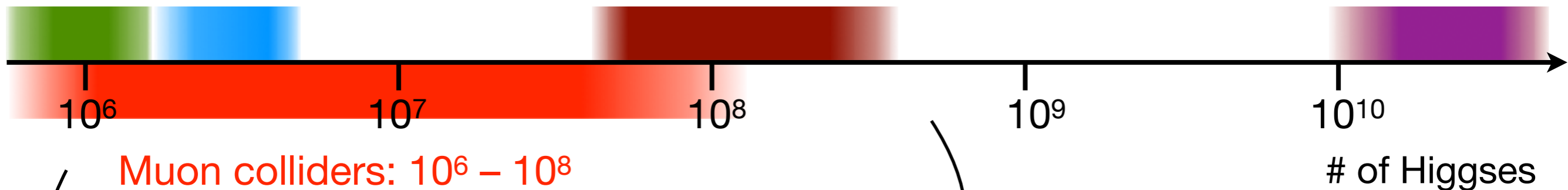
(as a comparison: 1.7×10^7 Z bosons @ LEP)

Low energy
 e^+e^- factories
(FCC-ee, CEPC,
ILC, CLIC380)

TeV-scale
 e^+e^- factories
(CLIC, ILC1000)

LHC: few $\times 10^7$
HL-LHC: few $\times 10^8$

FCC-hh:
few $\times 10^{10}$



Muon colliders: $10^6 - 10^8$

clean environment:
can measure “large” Higgs
BR w/ almost 10^{-3} precision

large QCD backgrounds:
only rare modes (BR $< 10^{-3}$)
easily accessible

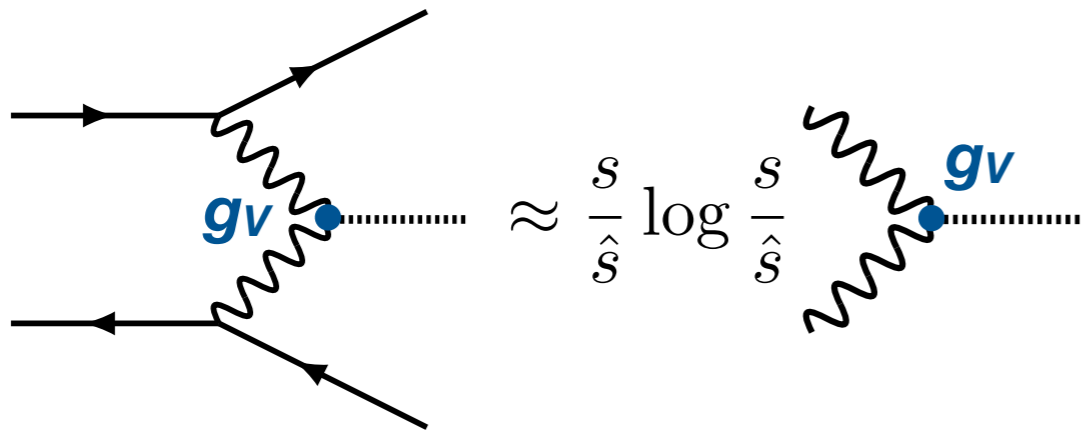
Higgs factories

- ◆ **Low-energy e+e- factories:** $e^+e^- \rightarrow Zh$ @ 240 GeV



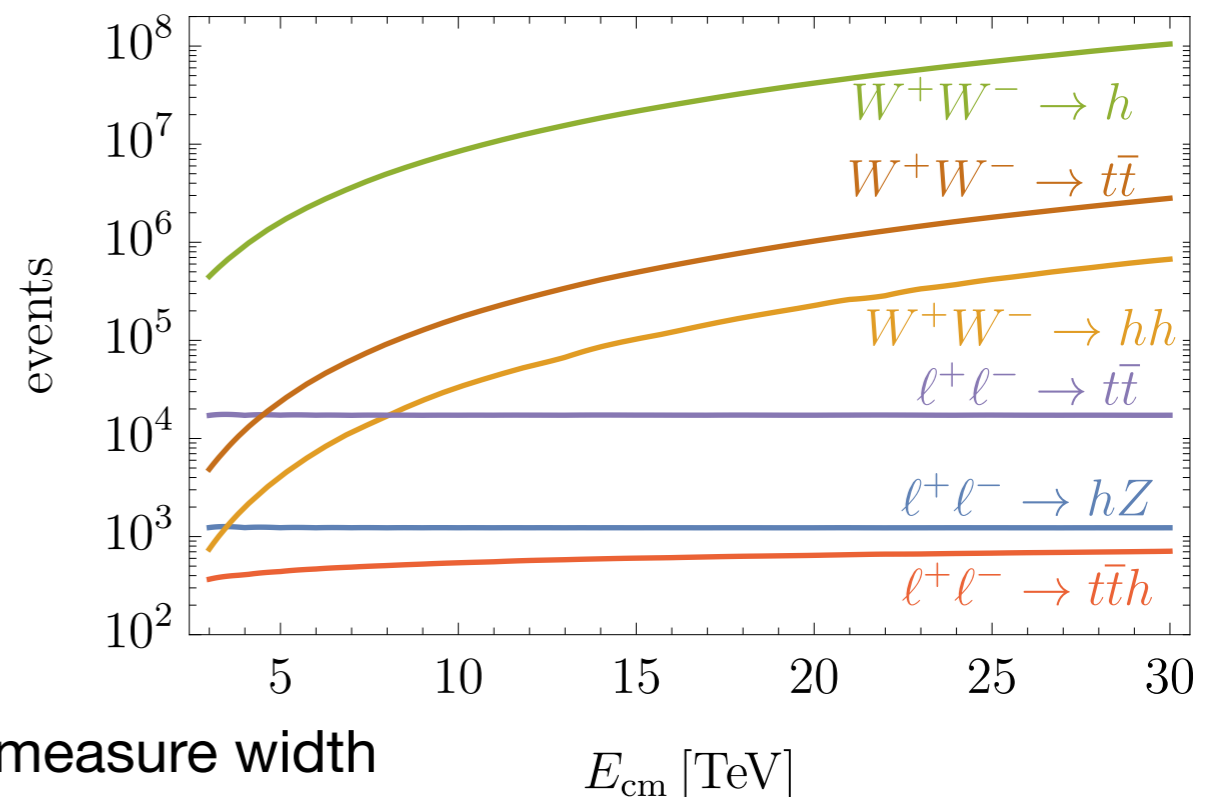
- ◆ measure the recoil (missing mass) of h against Z
- ◆ *direct* measurement of $g_V \rightarrow$ other couplings + width

- ◆ **A high-energy lepton collider** is a “vector boson collider”



- ◆ potentially huge single H production (10^7 - 10^8 at 10-30 TeV)
- ◆ hard neutrinos from W-fusion not seen
- ZZ fusion (forward lepton tagging) could still measure width

For “soft” SM final state $\hat{s} \sim m_{EW}^2$
cross-section is enhanced



Higgs factories

$\kappa-0$ fit	HL-LHC	LHeC	HE-LHC		ILC			CLIC			CEPC	FCC-ee		FCC-ee/ eh/hh	$\mu^+\mu^-$ 10000
			S2	S2'	250	500	1000	380	1500	3000		240	365		
κ_W [%]	1.7	0.75	1.4	0.98	1.8	0.29	0.24	0.86	0.16	0.11	1.3	1.3	0.43	0.14	0.1
κ_Z [%]	1.5	1.2	1.3	0.9	0.29	0.23	0.22	0.5	0.26	0.23	0.14	0.20	0.17	0.12	0.4
κ_g [%]	2.3	3.6	1.9	1.2	2.3	0.97	0.66	2.5	1.3	0.9	1.5	1.7	1.0	0.49	0.7
κ_γ [%]	1.9	7.6	1.6	1.2	6.7	3.4	1.9	98*	5.0	2.2	3.7	4.7	3.9	0.29	0.8
$\kappa_{Z\gamma}$ [%]	10.	—	5.7	3.8	99*	86*	85*	120*	15	6.9	8.2	81*	75*	0.69	7.2
κ_c [%]	—	4.1	—	—	2.5	1.3	0.9	4.3	1.8	1.4	2.2	1.8	1.3	0.95	2.3
κ_t [%]	3.3	—	2.8	1.7	—	6.9	1.6	—	—	2.7	—	—	—	1.0	3.1
κ_b [%]	3.6	2.1	3.2	2.3	1.8	0.58	0.48	1.9	0.46	0.37	1.2	1.3	0.67	0.43	0.4
κ_μ [%]	4.6	—	2.5	1.7	15	9.4	6.2	320*	13	5.8	8.9	10	8.9	0.41	3.4
κ_τ [%]	1.9	3.3	1.5	1.1	1.9	0.70	0.57	3.0	1.3	0.88	1.3	1.4	0.73	0.44	0.6

dominant channels:
~ few %

rare modes:
high rate helps!

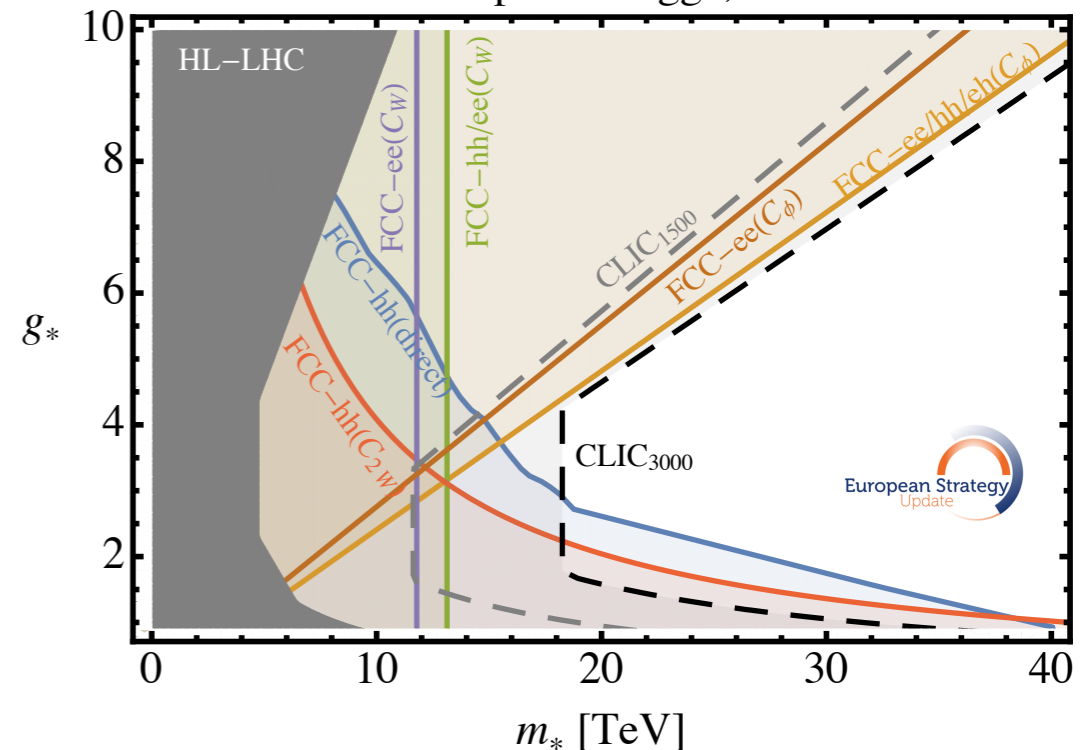
2103.14043

What NP scales will we test with the Higgs?

$$\delta\kappa \sim \frac{v^2}{M_{\text{NP}}^2} g_\star^2 \lesssim \mathbf{0.2\%}$$

→ $M_{\text{NP}} \gtrsim g_\star \mathbf{6 \text{ TeV}}$

Composite Higgs, 2σ

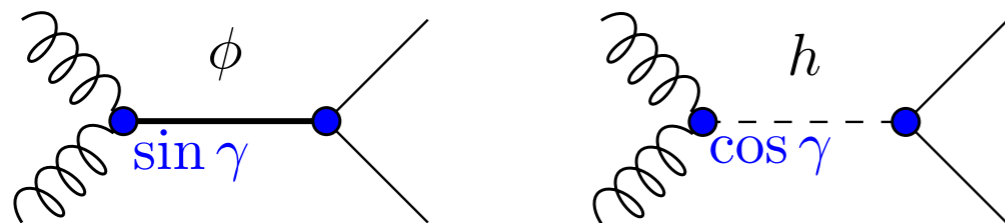


Direct vs indirect

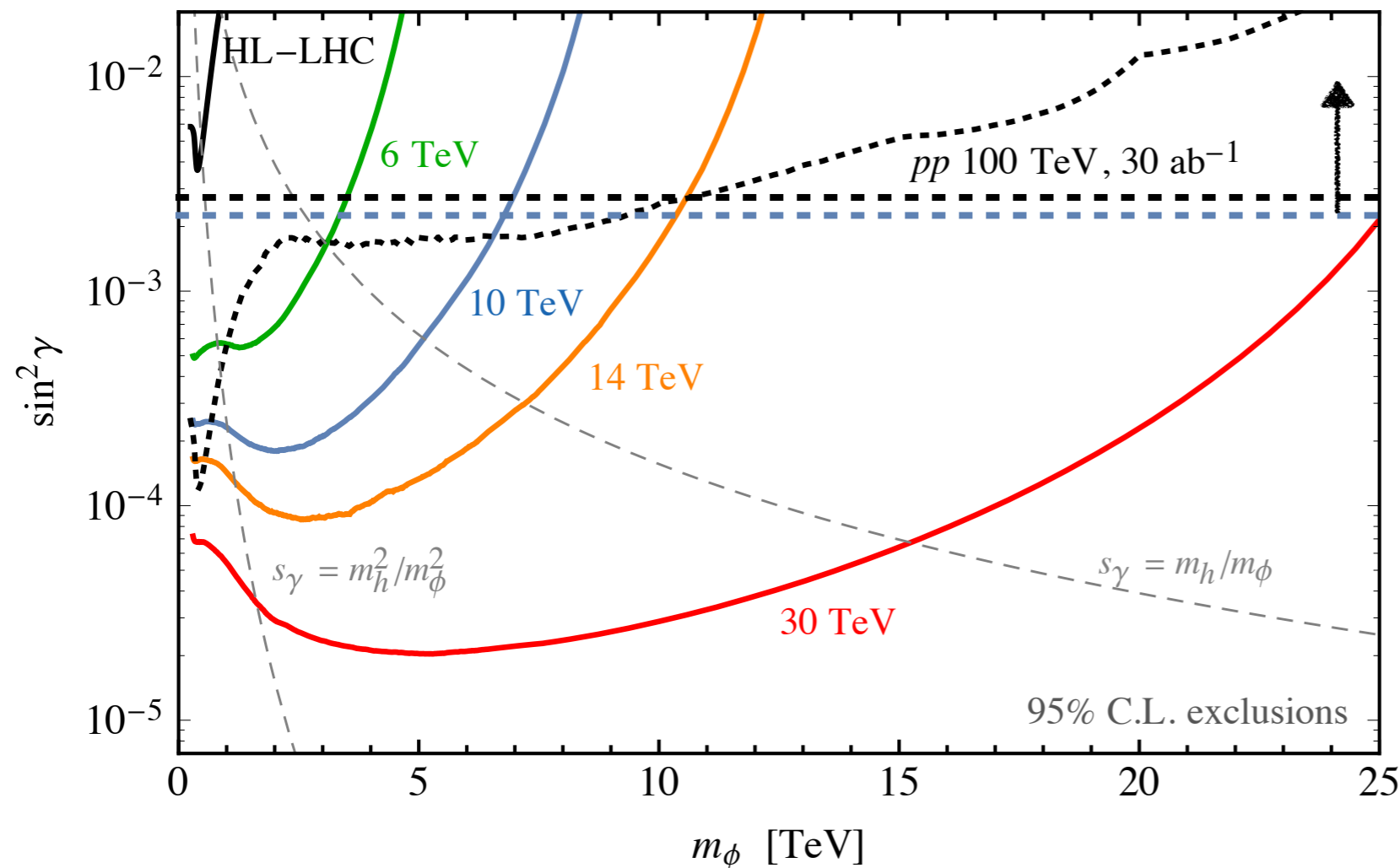
Compare single Higgs couplings measurements with reach of direct searches

- ▶ **Example: singlet scalar** $\mathcal{L}_{\text{int}} \sim \phi |H|^2$

ϕ is like a heavy Higgs with narrow width + hh decay



one single parameter controls resonance production, decay, & Higgs coupling modifications

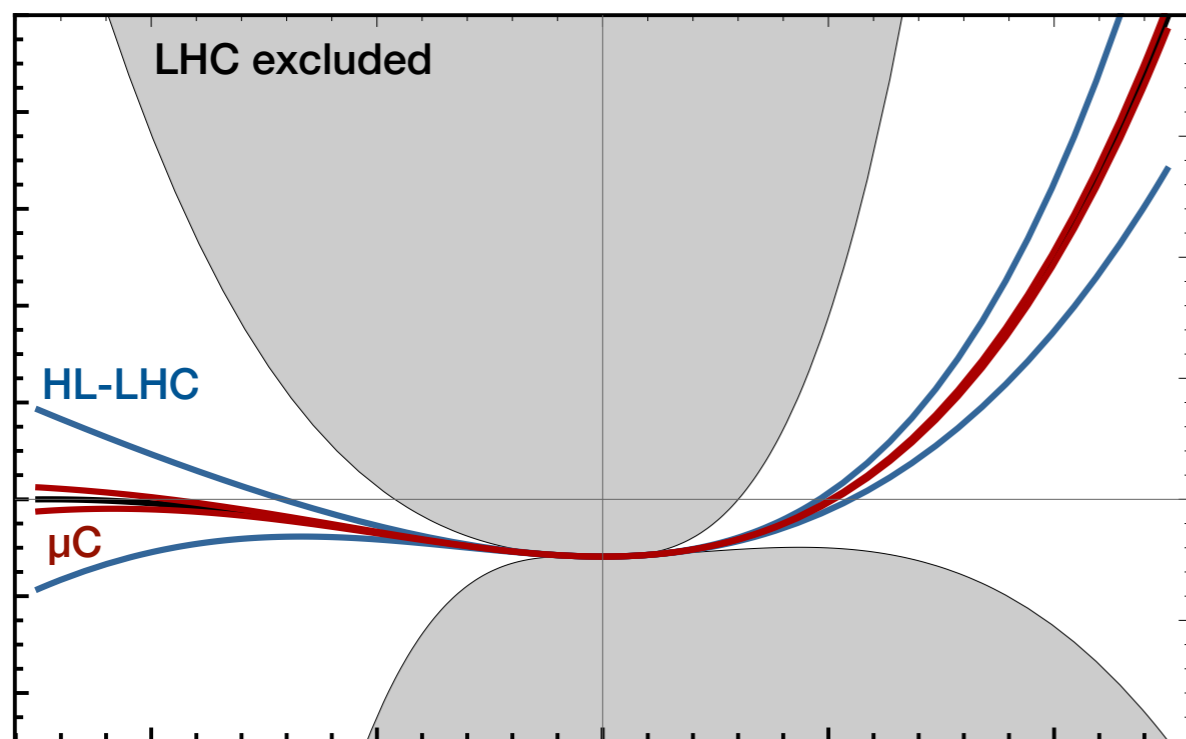


can be probed by single higgs

B, Redigolo, Sala, Tesi 1807.04743

Double Higgs production

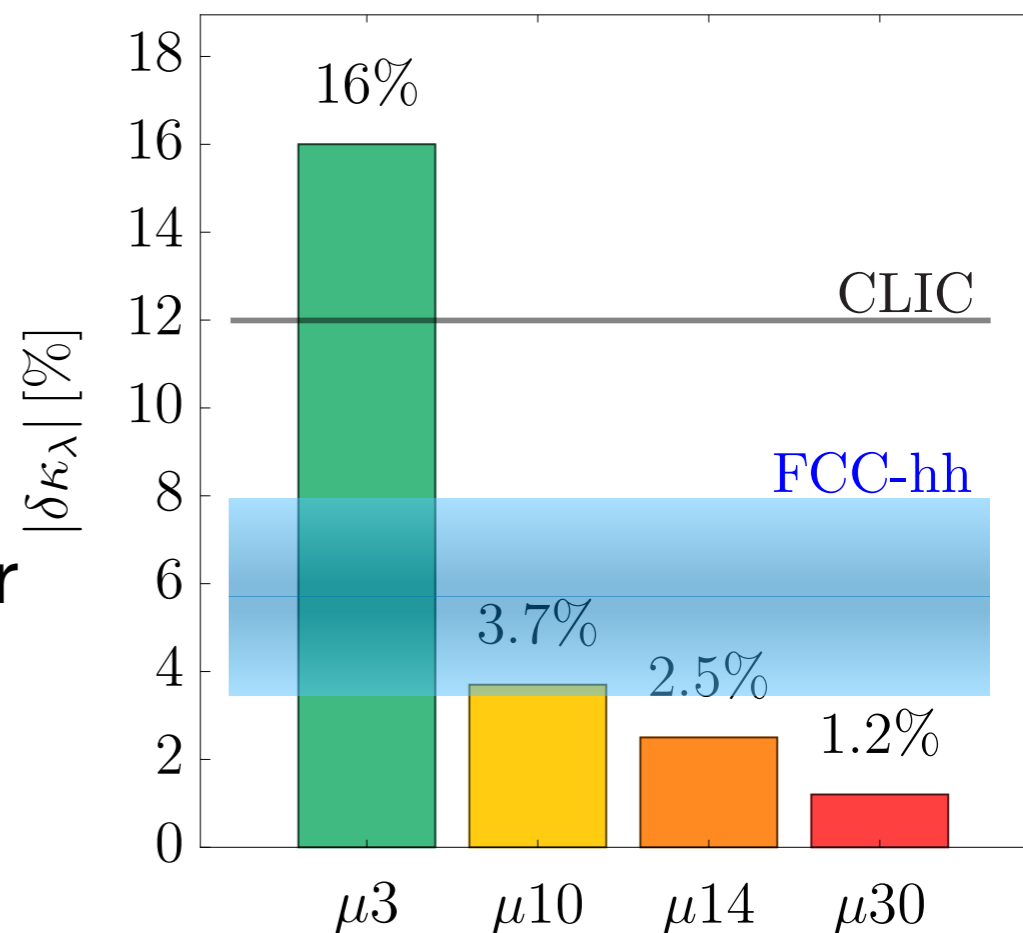
- Measurement of trilinear coupling: access to the Higgs potential



credits: Craig, Petrossian-Byrne

- very poorly known today!
- HL-LHC will only reach 50% precision on SM value

- Precise determination *only* possible at high-energy machines: need high rate!
100 TeV FCC-hh or multi-TeV Muon collider

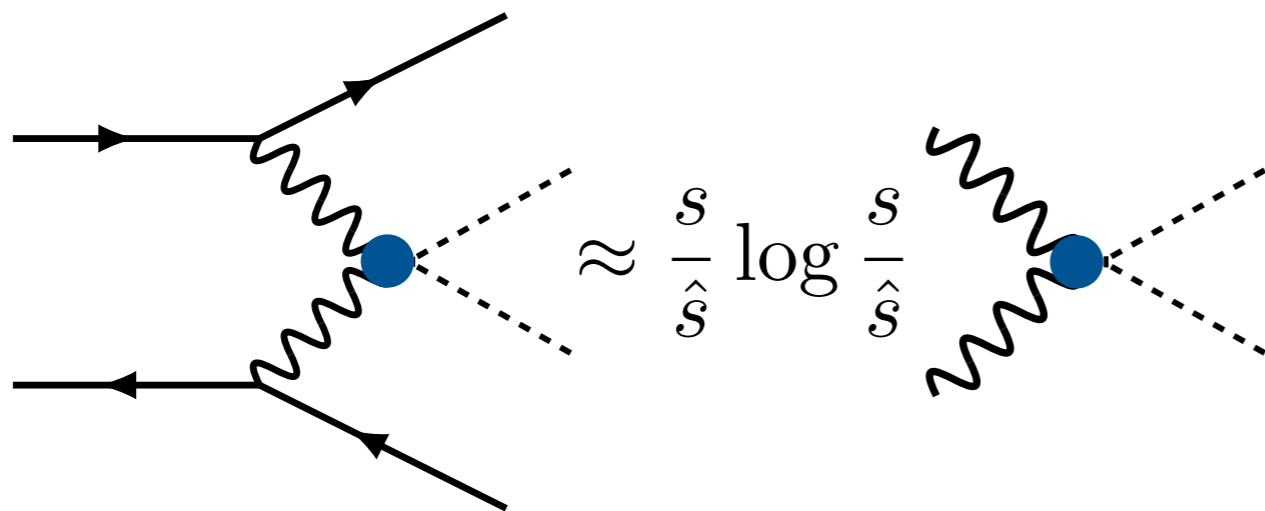


Mangano et al. 2004.03505
B, Franceschini, Wulzer 2012.11555
Costantini et al. 2005.10289

Han et al. 2008.12204
CLIC 1901.05897

High rate probes

- High rate: more events = better precision



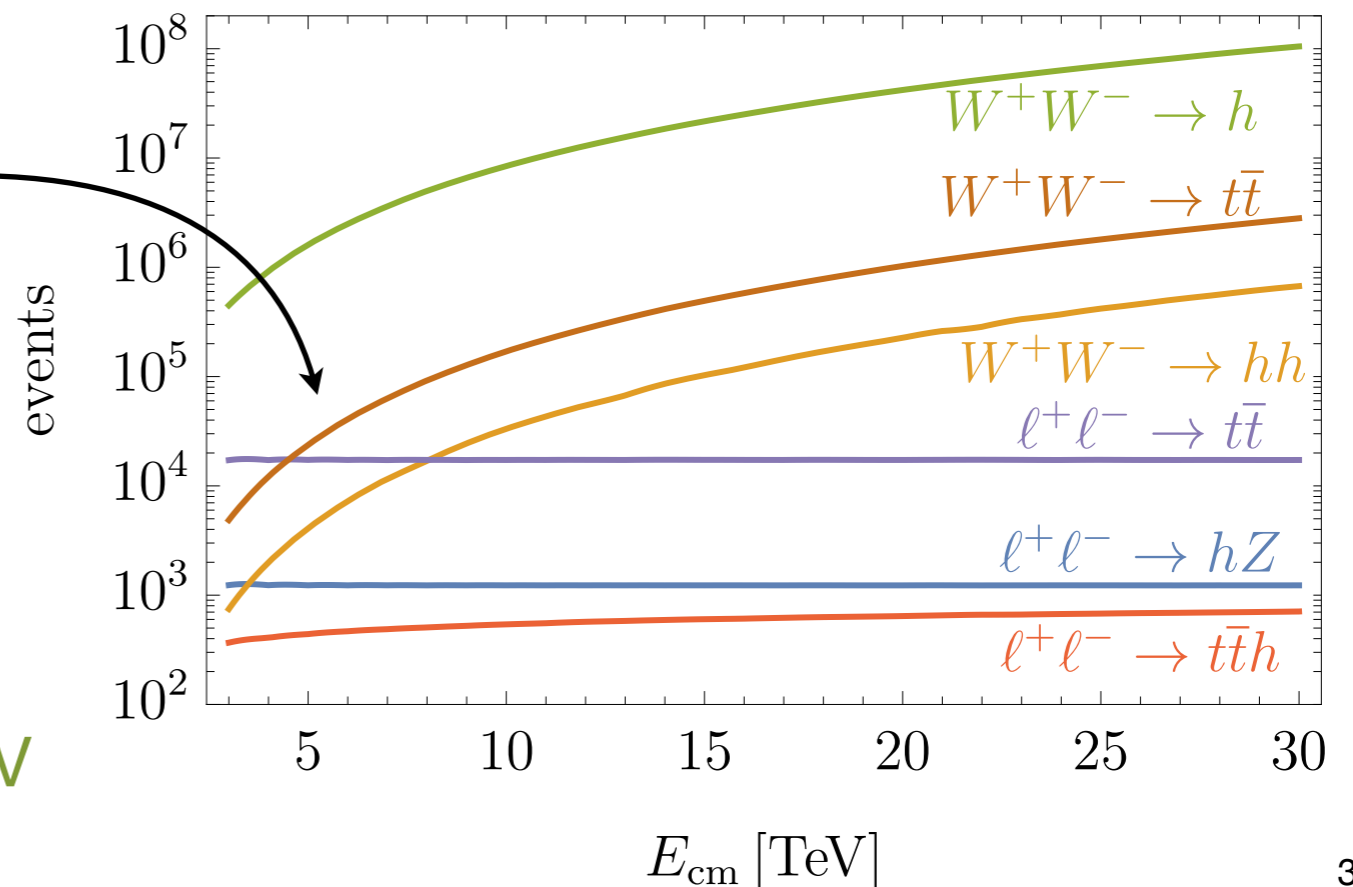
A High Energy Lepton Collider is a “vector boson collider”

For “soft” SM final state $\hat{s} \sim m_{EW}^2$ cross-section is enhanced

Dawson 1985

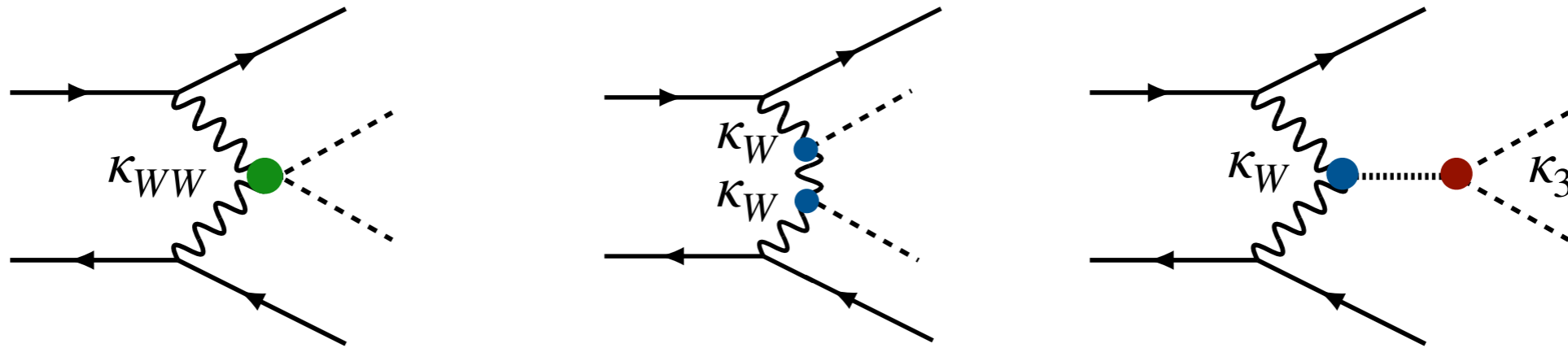
Above few TeV the VBF cross-section dominates over the hard $2 \rightarrow 2$

- Huge single Higgs rate in vector-boson-fusion: 10^7 - 10^8 Higgs bosons at 10-30 TeV



Double Higgs production

- ◆ Depends on h^3 coupling κ_3 but also on W-boson couplings κ_W, κ_{WW} :



large degeneracy in total cross-section:
coefficients not determined
from hh production alone

Double Higgs production

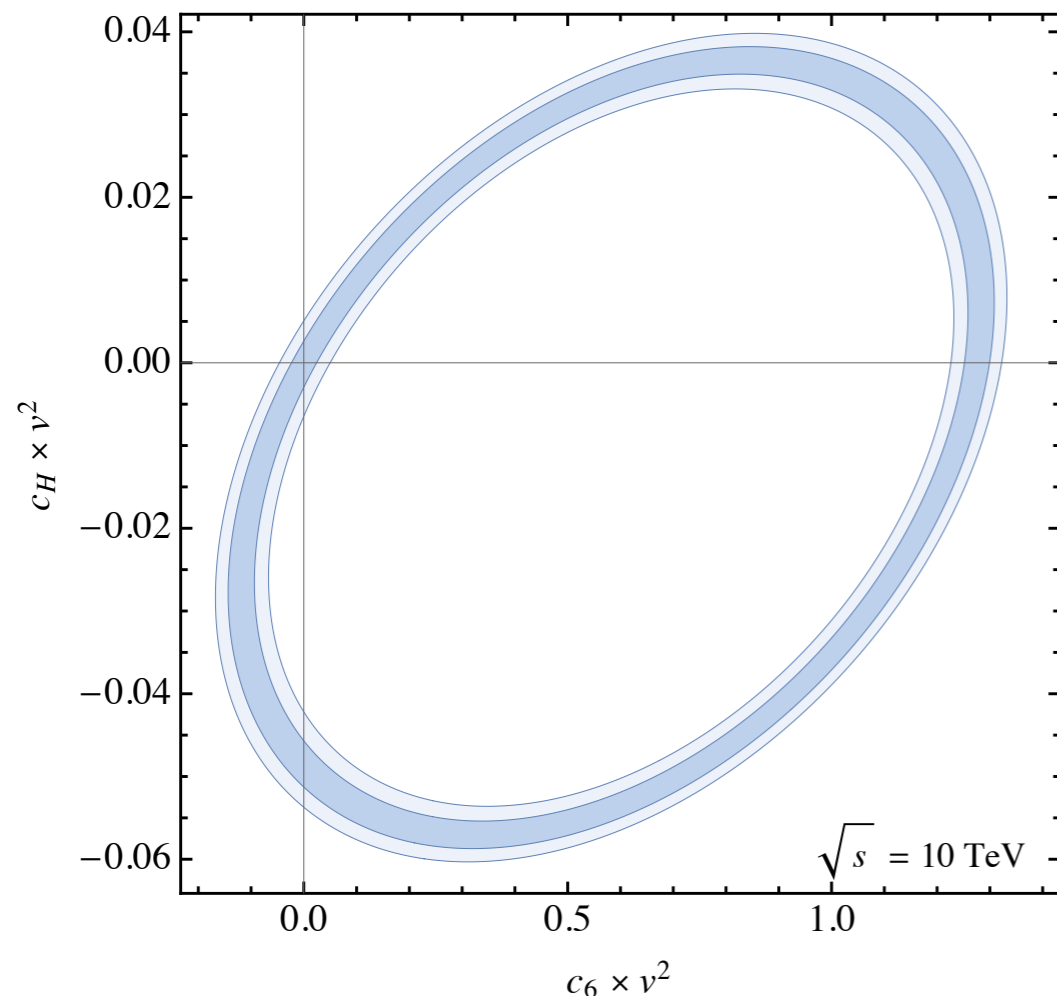
- ◆ Depends on h^3 coupling κ_3 but also on W-boson couplings κ_W, κ_{WW} :

- ◆ Two dim. 6 operators: $\mathcal{O}_6 = -\lambda|H|^6$ $\mathcal{O}_H = \frac{1}{2} (\partial_\mu |H|^2)^2$

$$\kappa_3 = 1 + v^2 \left(C_6 - \frac{3}{2} C_H \right)$$

$$\kappa_W = 1 - v^2 C_H / 2$$

$$\kappa_{WW} = 1 - 2v^2 C_H$$



large degeneracy in total cross-section:
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Double Higgs production

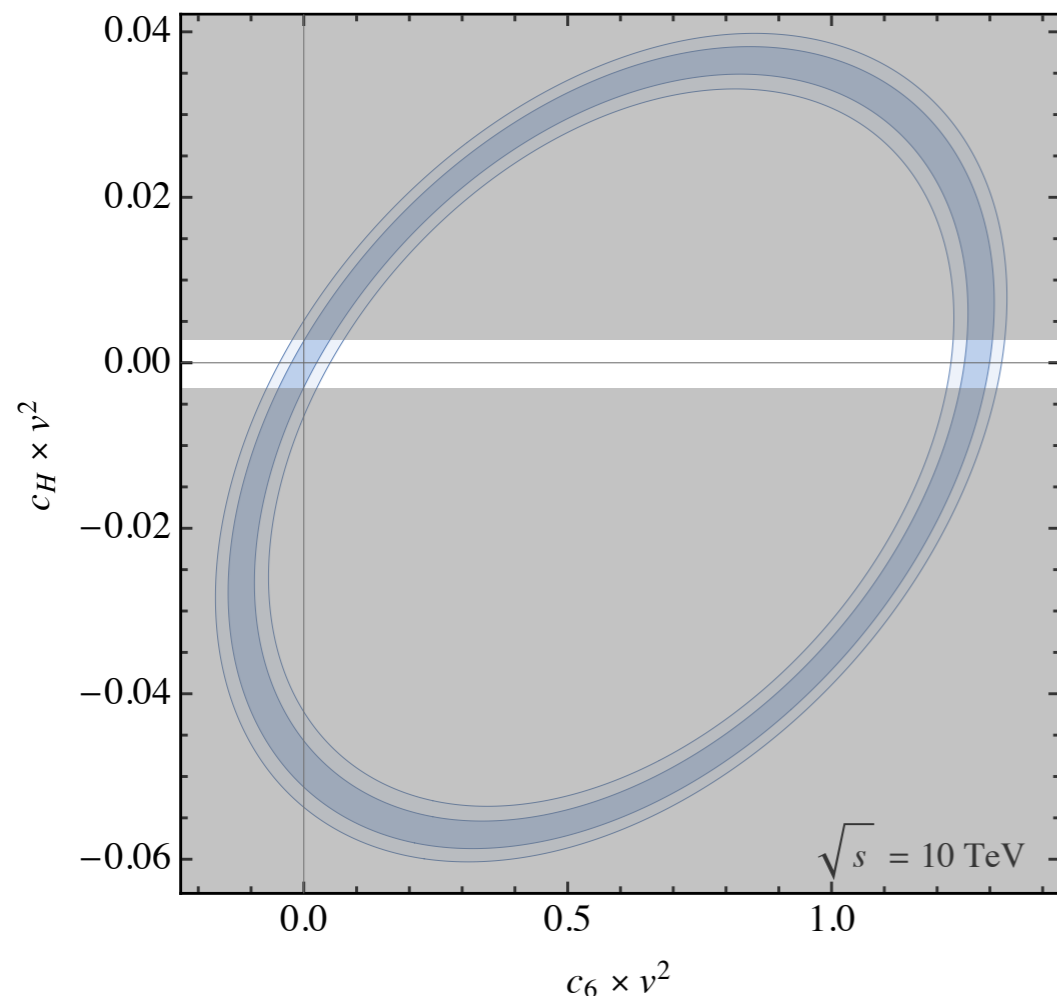
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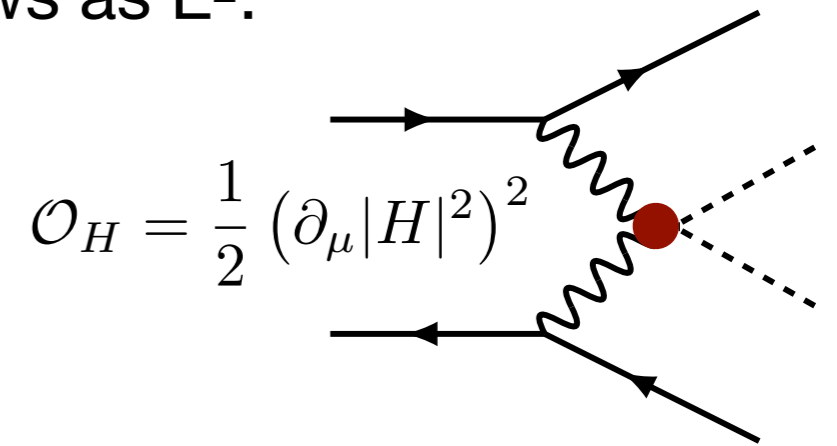
\mathcal{O}_H can also be constrained from
single Higgs couplings:

$$\Delta\kappa_{V,f} = v^2 C_H / 2 \lesssim \text{few} \times 10^{-3}$$

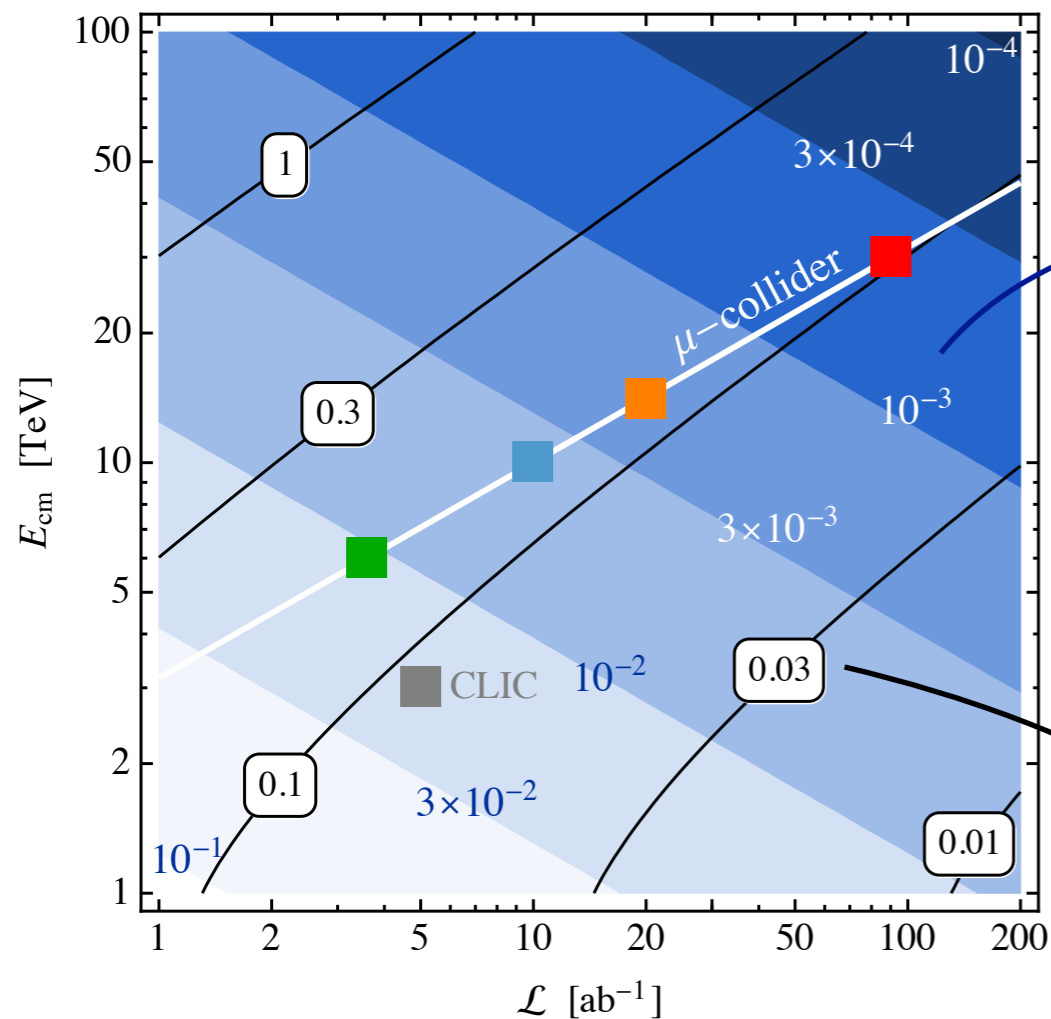
Double Higgs at high mass

- NP contribution from \mathcal{O}_H (equivalently κ_W, κ_{WW}) grows as E^2 :
high mass tail gives a *direct* measurement of C_H

High-energy $WW \rightarrow hh$ more sensitive than Higgs pole physics at energies $\gtrsim 10$ TeV

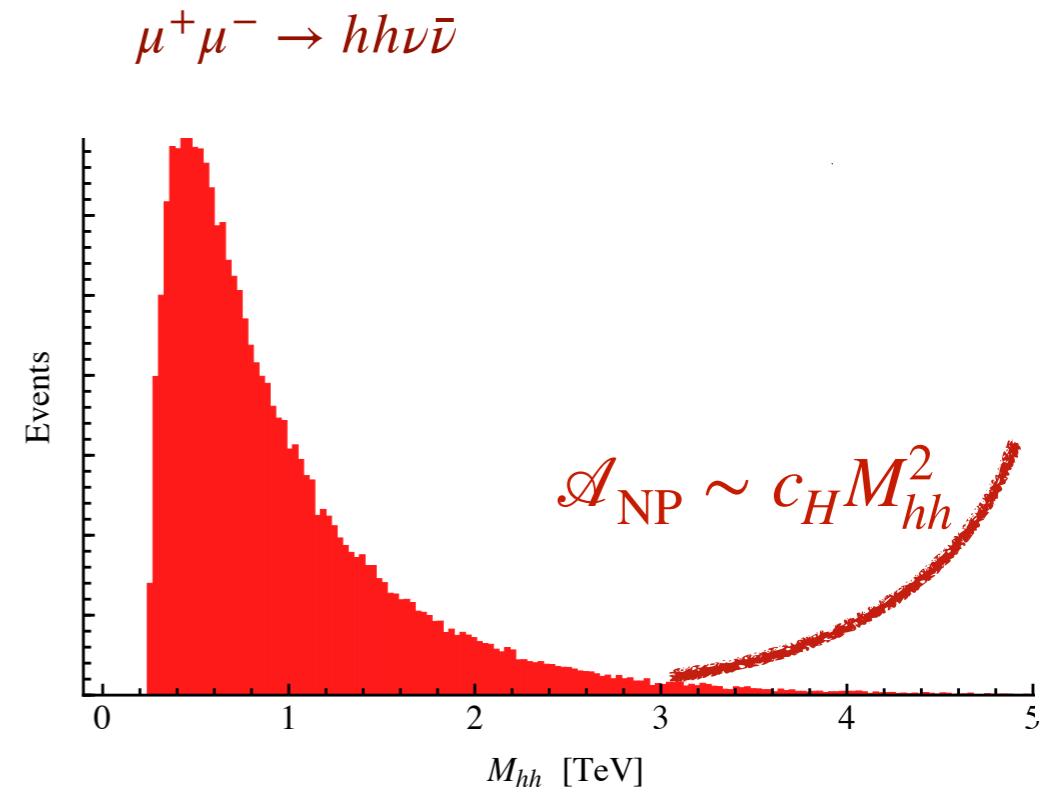


$$\mathcal{O}_H = \frac{1}{2} (\partial_\mu |H|^2)^2$$



$$\xi \equiv C_H V^2$$

S/B low-precision measurement



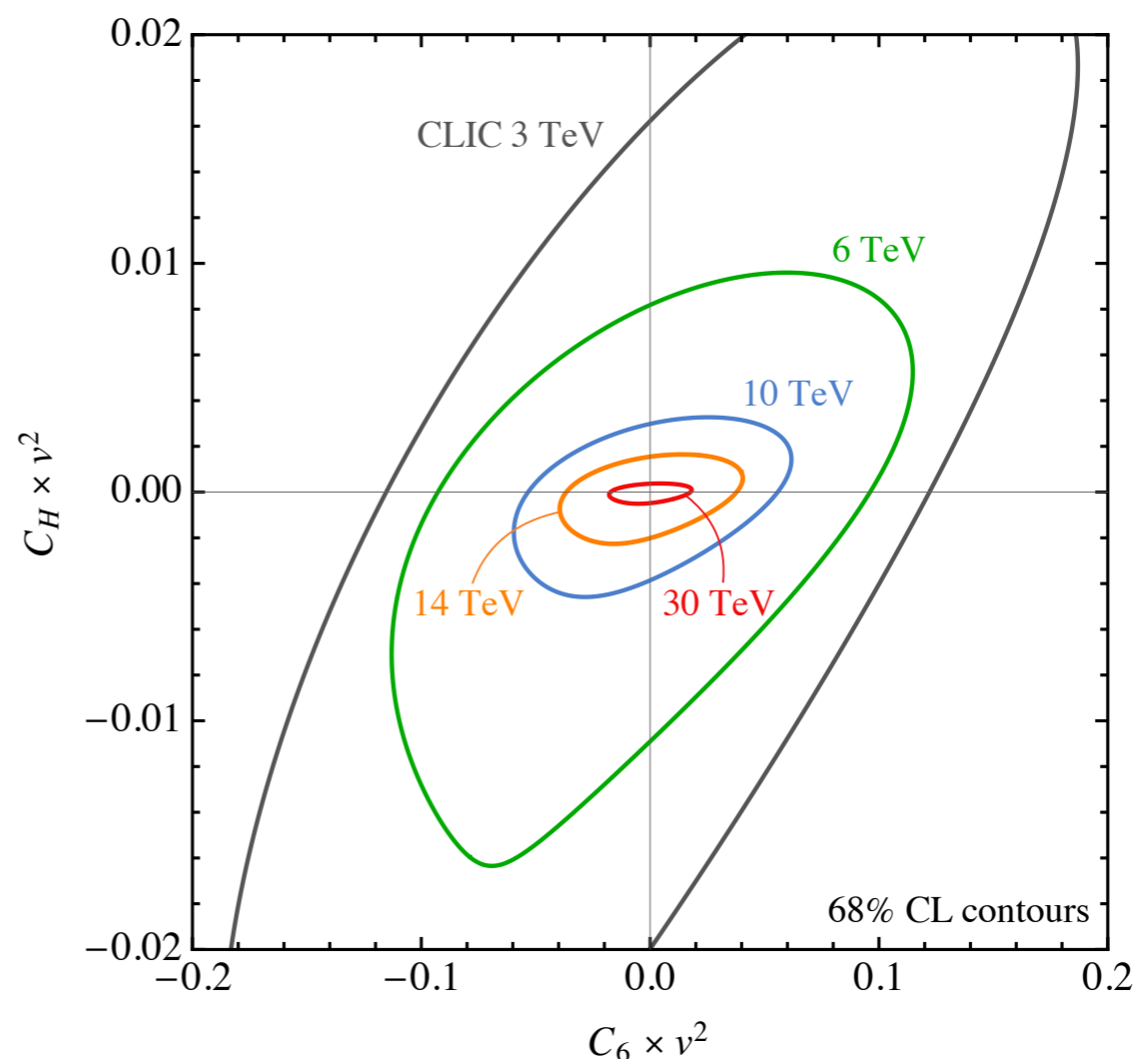
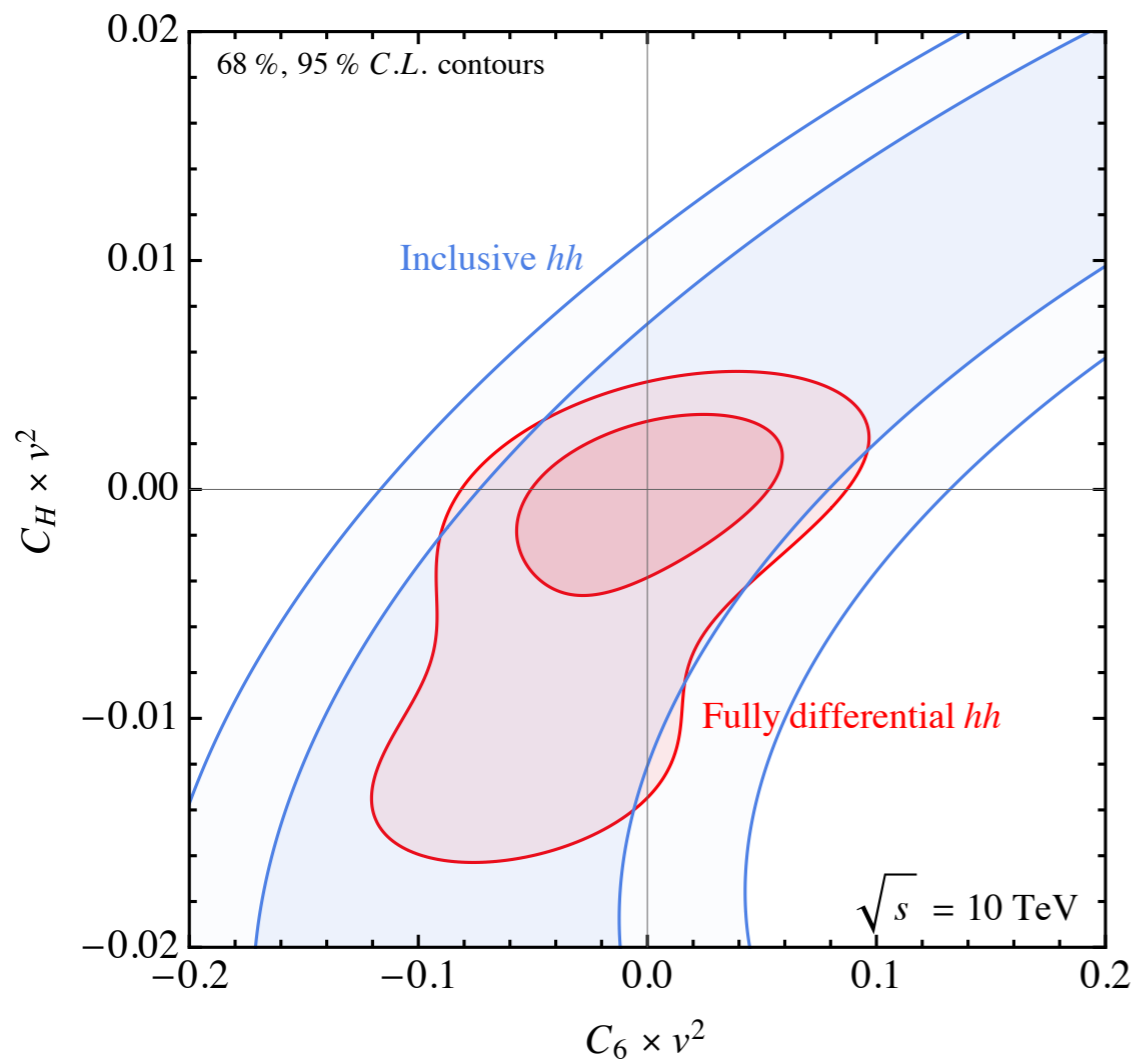
(see also Contino et al. 1309.7038)

Double Higgs at high mass

- ◆ SM Effective Theory: $\mathcal{L}_{\text{EFT}} = \mathcal{L}_{\text{SM}} + \sum_i C_i \mathcal{O}_i^{(6)} + \dots$
- ◆ Trilinear coupling is affected by two operators: $\kappa_3 = 1 + v^2 \left(C_6 - \frac{3}{2} C_H \right)$

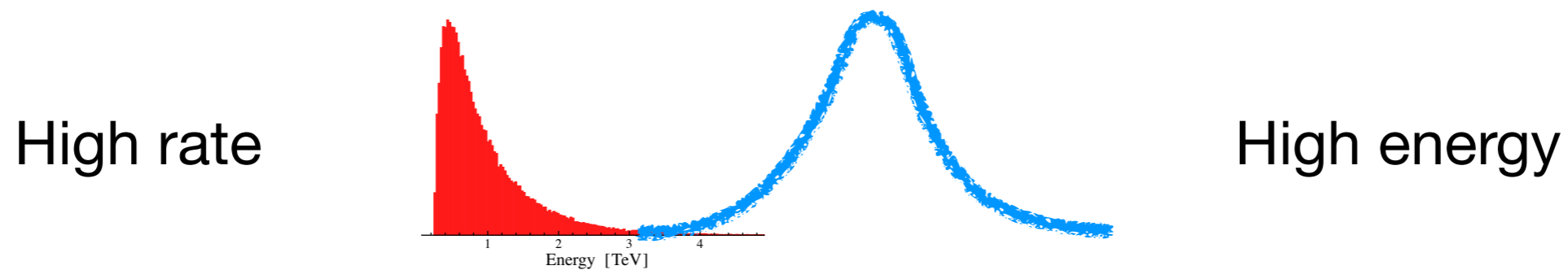
$$\mathcal{O}_6 = -\lambda |H|^6 \quad \mathcal{O}_H = \frac{1}{2} (\partial_\mu |H|^2)^2$$

Differential analysis in p_T and M_{hh} :



Summary

- ✦ Long-term goal of particle physics: **explore the 10+ TeV scale.**
- ✦ Precision SM measurements might be the quickest way...
- ✦ Two complementary paths to precision:



Flavor: rare decays w/ 3rd family, neutrino modes

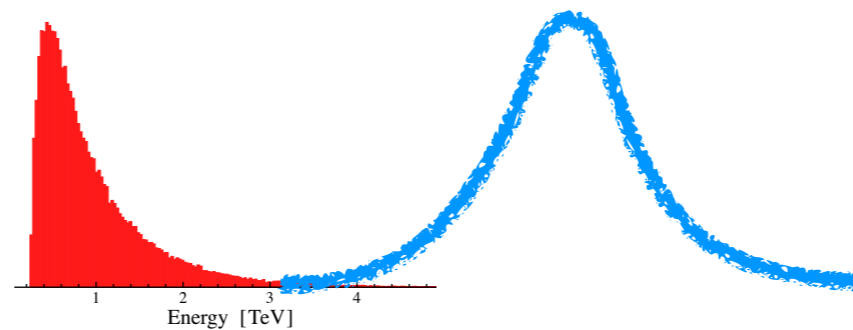
Electroweak: Z-pole precision, high-energy probes, radiation

Higgs: couplings, self-interaction, high-pT probes

Summary

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High rate



High energy

Flavor: rare decays w/ 3rd family, neutrino modes

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Xin cảm ơn!