

Muon g-2 in the SM: status and prospects

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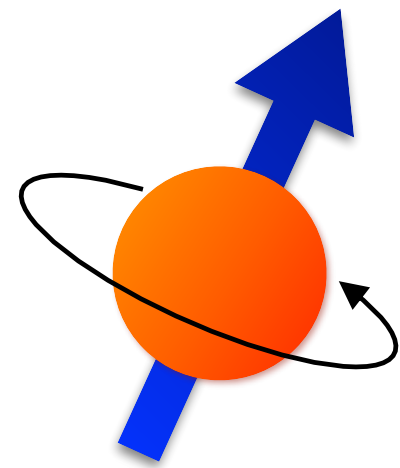


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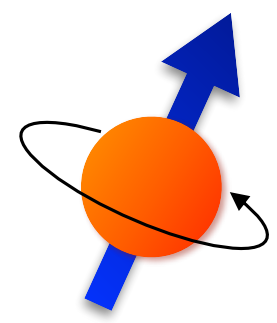
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Outline



- Introduction
- Muon $g-2$ Theory Initiative
- Hadronic corrections in comparison
- HVP
 - puzzles
- HLbL
- Summary and Outlook
- Appendix

- “The anomalous magnetic moment of the muon in the SM”:
1st White Paper published in 2020 (132 authors, 82 institutions) [T. Aoyama et al, [arXiv:2006.04822](https://arxiv.org/abs/2006.04822), Phys. Repts. 887 (2020) 1-166.]
- “Prospects for precise predictions of a_μ in the SM”: 2022 Snowmass Summer Study, [arXiv:2203.15810](https://arxiv.org/abs/2203.15810)
- Summary statement on the status of Muon $g-2$ Theory in the SM: <https://muon-gm2-theory.illinois.edu>



Anomalous magnetic moment

The magnetic moment of charged leptons (e, μ, τ): $\vec{\mu} = g \frac{e}{2m} \vec{S}$

Dirac (leading order): $g = 2$

$$= (-ie) \bar{u}(p') \gamma^\mu u(p)$$

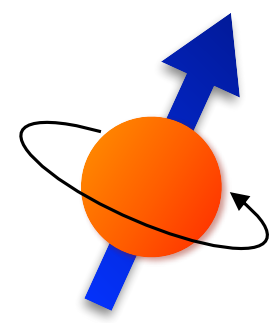
Quantum effects (loops):

$$= (-ie) \bar{u}(p') \left[\gamma^\mu F_1(q^2) + \frac{i\sigma^{\mu\nu} q_\nu}{2m} F_2(q^2) \right] u(p)$$

Note: $F_1(0) = 1$ and $g = 2 + 2 F_2(0)$

Anomalous magnetic moment:

$$a \equiv \frac{g - 2}{2} = F_2(0)$$



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Quantum effects (loops):

$$g = 2 \left(1 + \frac{\alpha}{2\pi} \right)$$

All SM particles contribute

$$= (-ie) \bar{u}(p') \left[\gamma^\mu F_1(q^2) + \frac{i\sigma^{\mu\nu} q_\nu}{2m} F_2(q^2) \right] u(p)$$

Note: $F_1(0) = 1$ and $g = 2 + 2 F_2(0)$

Anomalous magnetic moment: $a \equiv \frac{g - 2}{2} = F_2(0) = \frac{\alpha}{2\pi} + O(\alpha^2) + \dots = 0.00116\dots$

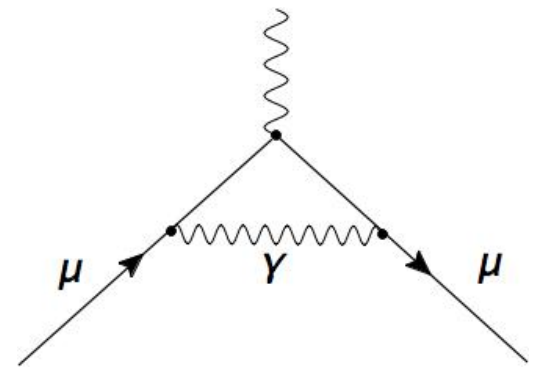
Muon g-2: SM contributions

$$a_{\mu} = a_{\mu}(\text{QED}) + a_{\mu}(\text{EW}) + a_{\mu}(\text{hadronic})$$

Muon $g-2$: SM contributions

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QED

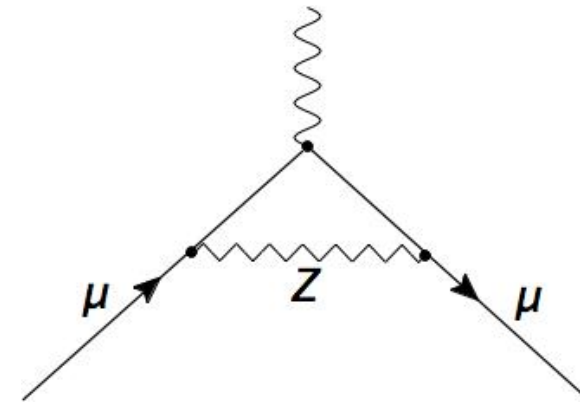


+... (5 loops)

$$116\,584\,718.9(1) \times 10^{-11}$$

0.001 ppm

EW

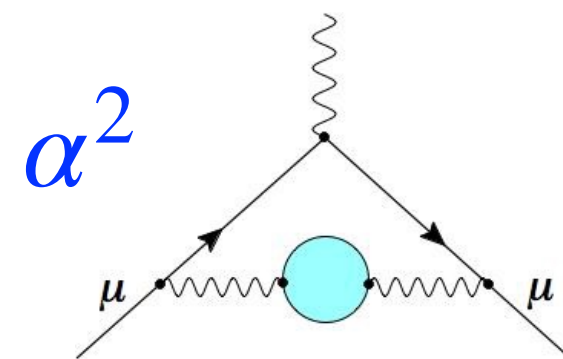


+... (2 loops)

$$153.6(1.0) \times 10^{-11}$$

0.01 ppm

HVP



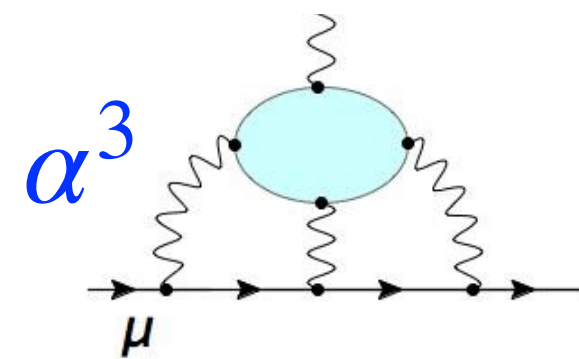
+... (NNLO)

$$6845(40) \times 10^{-11}$$

[0.6%]

0.34 ppm

HLbL



+... (NLO)

$$92(18) \times 10^{-11}$$



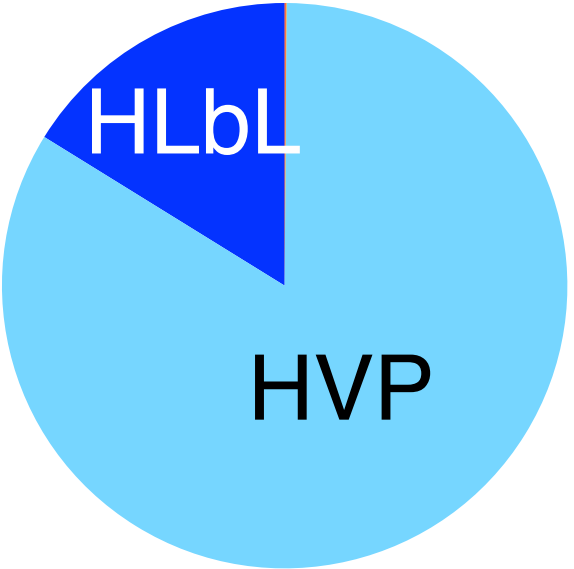
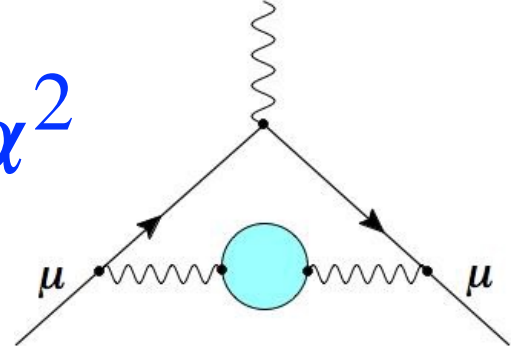
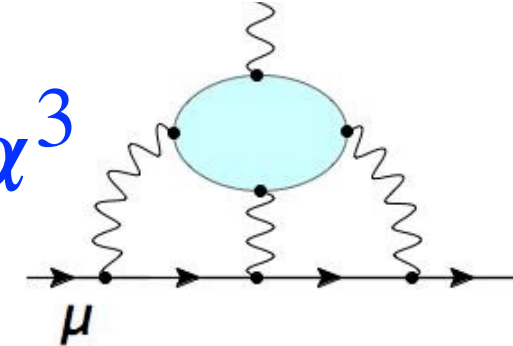
[20%]

0.15 ppm

Hadronic corrections

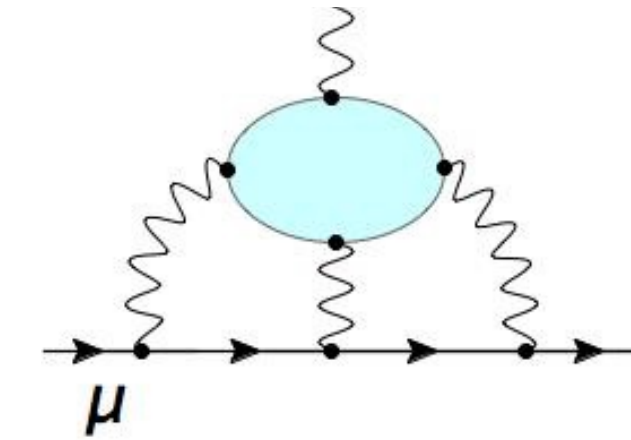
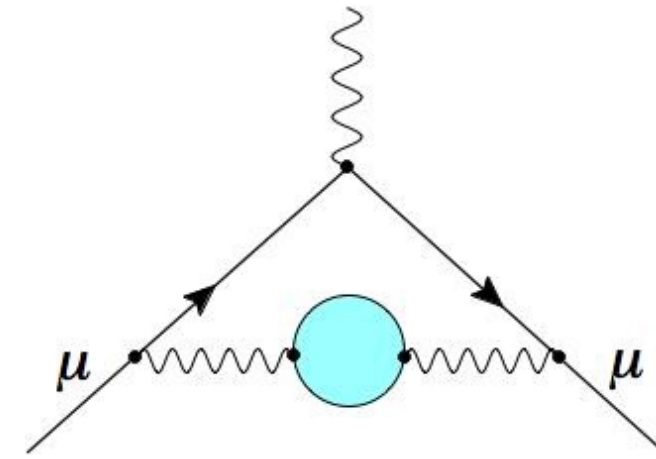
Muon g-2: SM contributions

$$a_\mu = a_\mu(\text{QED}) + a_\mu(\text{EW}) + a_\mu(\text{hadronic})$$

contribution	error ²		
 		$116\,584\,718.9(1) \times 10^{-11}$	0.001 ppm
		$153.6(1.0) \times 10^{-11}$	0.01 ppm
HVP  α^2	+... (NNLO)	$6845(40) \times 10^{-11}$ [0.6%]	0.34 ppm
HLbL  α^3	+... (NLO)	$92(18) \times 10^{-11}$ [20%]	0.15 ppm

Hadronic corrections

Muon g-2: hadronic corrections



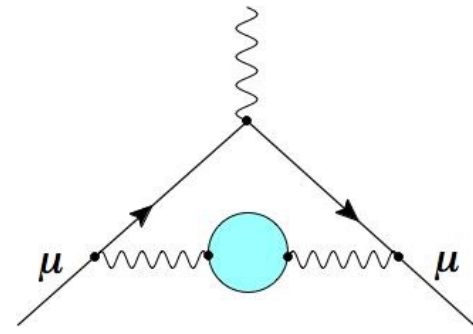
- ★ Hadronic contributions are obtained by integrating over all possible virtual photon momenta, integral is weighted towards low q^2 .
- ★ Cannot use perturbation theory to reliably compute the hadronic bubbles
- ★ Two-point & four-point functions:

$$\text{HVP: } \langle 0 | T \{ j_\mu j_\nu \} | 0 \rangle$$

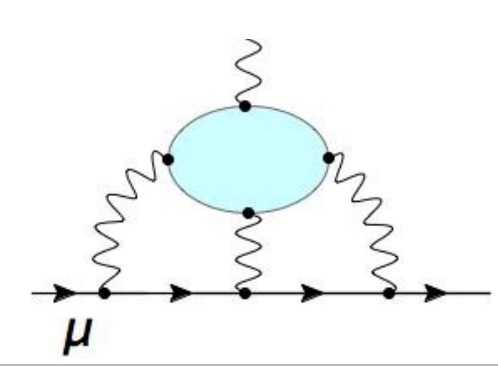
$$\text{HLbL: } \langle 0 | T \{ j_\mu j_\nu j_\rho j_\sigma \} | 0 \rangle$$

Two independent approaches

1. Dispersive, data-driven
2. Lattice QCD



Hadronic Corrections



Two independent approaches:

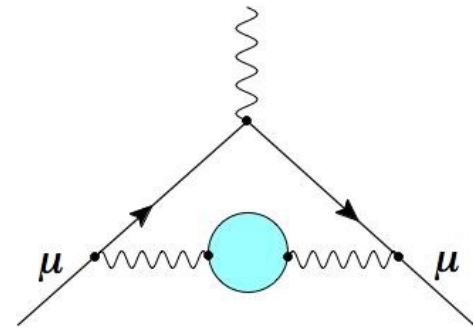
• For HVP: use dispersion relations to rewrite integral in terms of hadronic cross section:

$$\text{Im} \left[\text{wavy} \cdot \text{loop} \cdot \text{wavy} \right] \sim \left| \text{wavy} \cdot \text{hadrons} \right|^2 \implies \text{e}^+ \text{e}^- \text{ annihilation} \rightarrow \text{wavy} \cdot \text{hadrons}$$

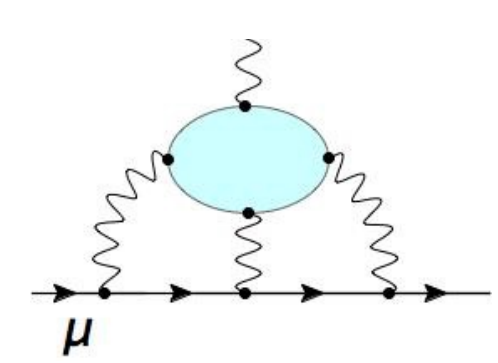
The diagram shows the imaginary part of a muon loop diagram with photon insertions is proportional to the squared magnitude of a diagram where a photon from an e^+e^- annihilation vertex couples to a hadronic vacuum polarization insertion.

Many experiments (over 20+ years) have measured the e^+e^- cross sections for the different channels over the needed energy range with increasing precision.

For HLbL: **new dispersive approach**



Hadronic Corrections



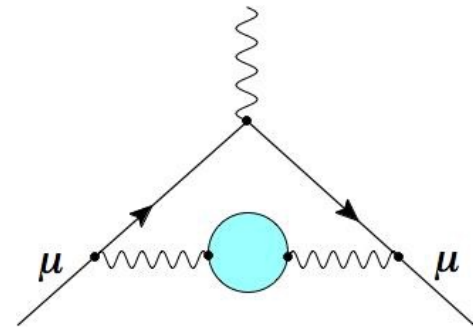
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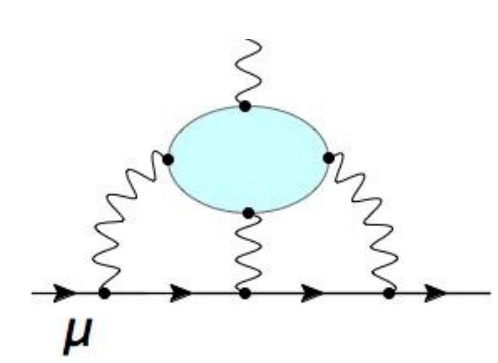
$$\text{Im}[\text{wavy line} \cdot \text{blue circle} \cdot \text{wavy line}] \sim |\text{wavy line} \cdot \text{hadrons}|^2 \implies a_{\mu}^{\text{HVP,LO}} = \left(\frac{\alpha}{\pi}\right)^2 \int dq^2 \omega(q^2) \hat{\Pi}(q^2) = \frac{m_{\mu}^2}{12\pi^3} \int ds \frac{\hat{K}(s)}{s} \sigma_{\text{exp}}(s)$$

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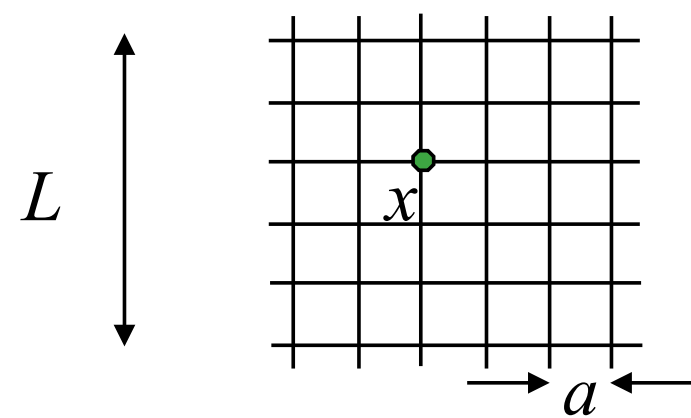
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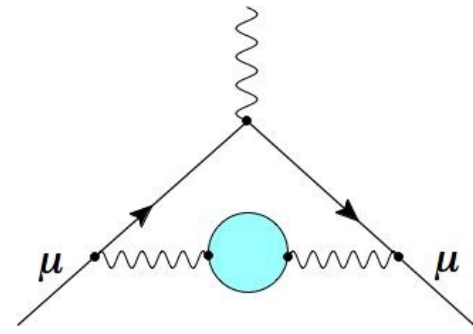
• Direct calculation using Euclidean Lattice QCD



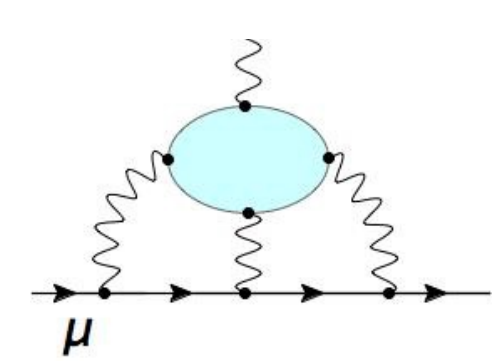
Approximations:
 discrete space-time (spacing a)
 finite spatial volume (L), and time extent (T)
 ...

- *ab-initio* method to quantify QCD effects
- already used for simple hadronic quantities with high precision
- requires large-scale computational resources
- **allows for entirely SM theory based evaluations**

Integrals are evaluated numerically using Monte Carlo methods.



Hadronic Corrections



Two independent approaches:

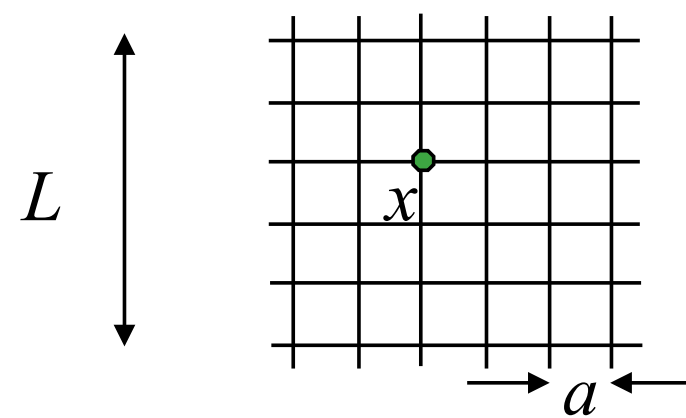
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$$a_\mu^{\text{HVP,LO}} = 4\alpha^2 \int_0^\infty dt C(t) \tilde{w}(t)$$

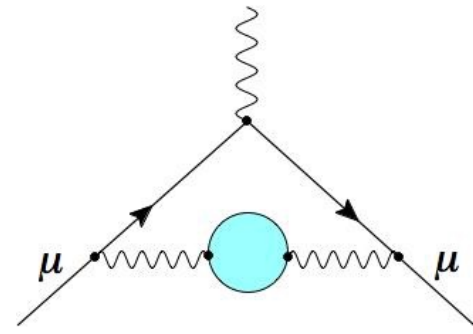
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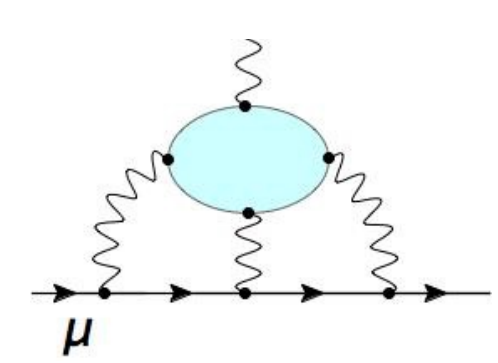
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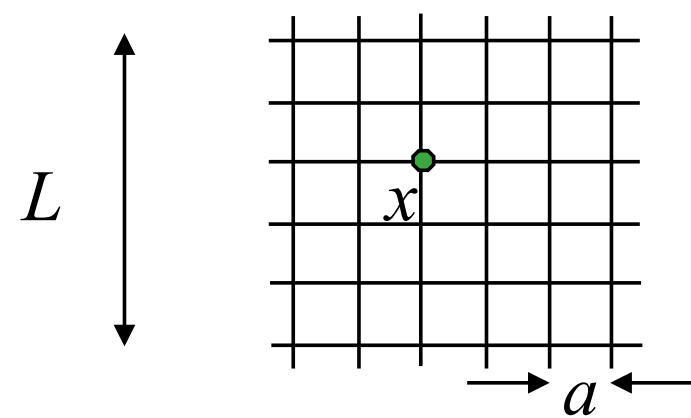
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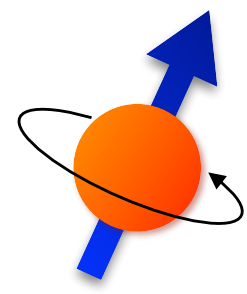
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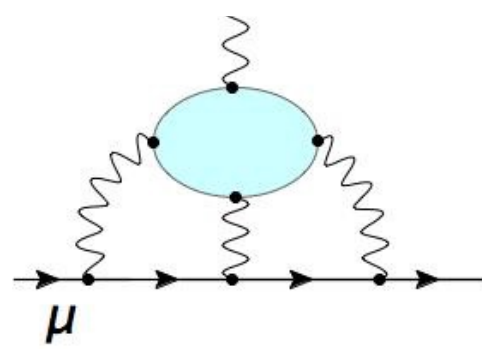
Muon $g-2$ Theory Initiative

Steering Committee

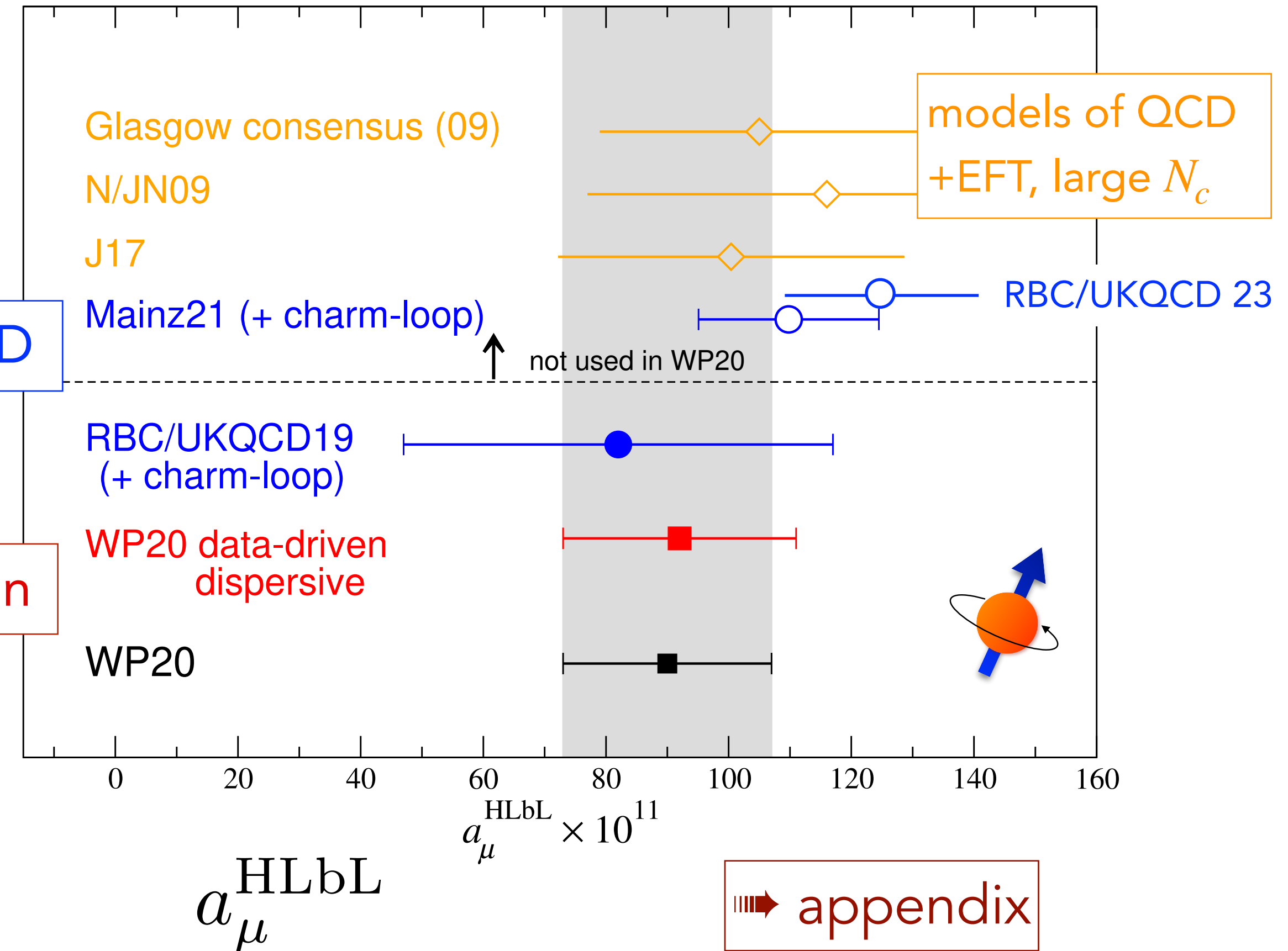
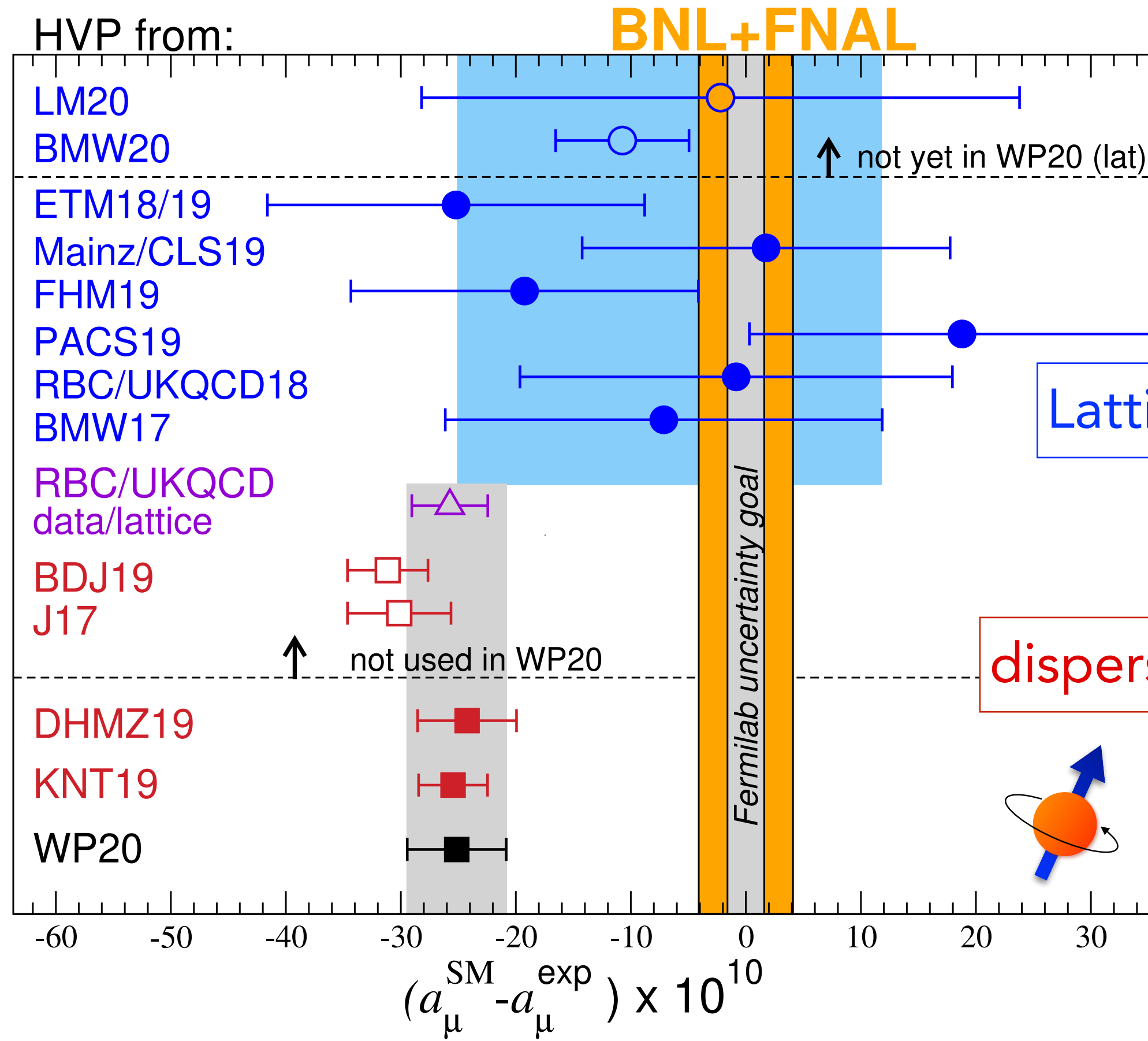
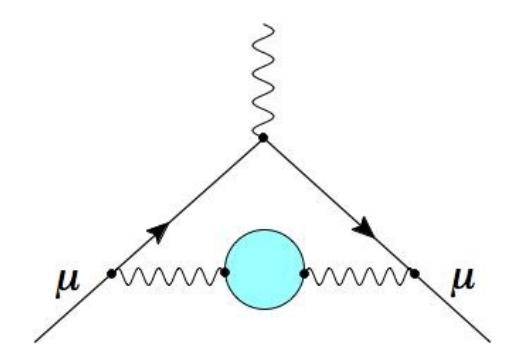
- Gilberto Colangelo (Bern)
- Michel Davier (Orsay) co-chair
- Aida El-Khadra (UIUC & Fermilab) chair
- Martin Hoferichter (Bern)
- Christoph Lehner (Regensburg University) co-chair
- Laurent Lellouch (Marseille)
- Tsutomu Mibe (KEK)
J-PARC Muon $g-2$ /EDM experiment
- Lee Roberts (Boston)
Fermilab Muon $g-2$ experiment
- Thomas Teubner (Liverpool)
- Hartmut Wittig (Mainz)

- Maximize the impact of the Fermilab and J-PARC experiments
 - quantify and reduce the theoretical uncertainties on the hadronic corrections
- summarize the theory status and assess reliability of uncertainty estimates
- organize workshops to bring the different communities together:
 - [First plenary workshop @ Fermilab: 3-6 June 2017](#)
 - [HVP workshop @ KEK: 12-14 February 2018](#)
 - [HLbL workshop @ U Connecticut: 12-14 March 2018](#)
 - [Second plenary workshop @ HIM \(Mainz\): 18-22 June 2018](#)
 - [Third plenary workshop @ INT \(Seattle\): 9-13 September 2019](#)
 - [Lattice HVP at high precision workshop \(virtual\): 16-20 November 2020](#)
 - [Fourth plenary workshop @ KEK \(virtual\): 28 June - 02 July 2021](#)
 - [Fifth plenary workshop @ Higgs Centre \(Edinburgh\): 5-9 September 2022](#)
 - [Sixth plenary workshop @ University of Bern: 4-8 September 2023](#)
 - Seventh plenary workshop @ KEK (Japan): June 2024
 - Eight plenary workshop: 2025 in the US — seeking proposals

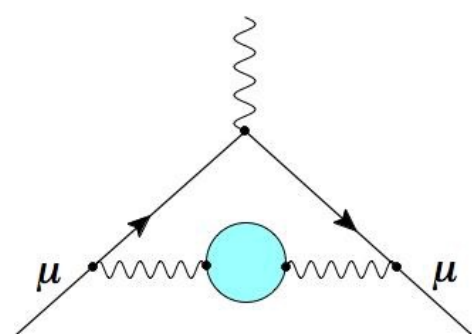
<https://muon-gm2-theory.illinois.edu>



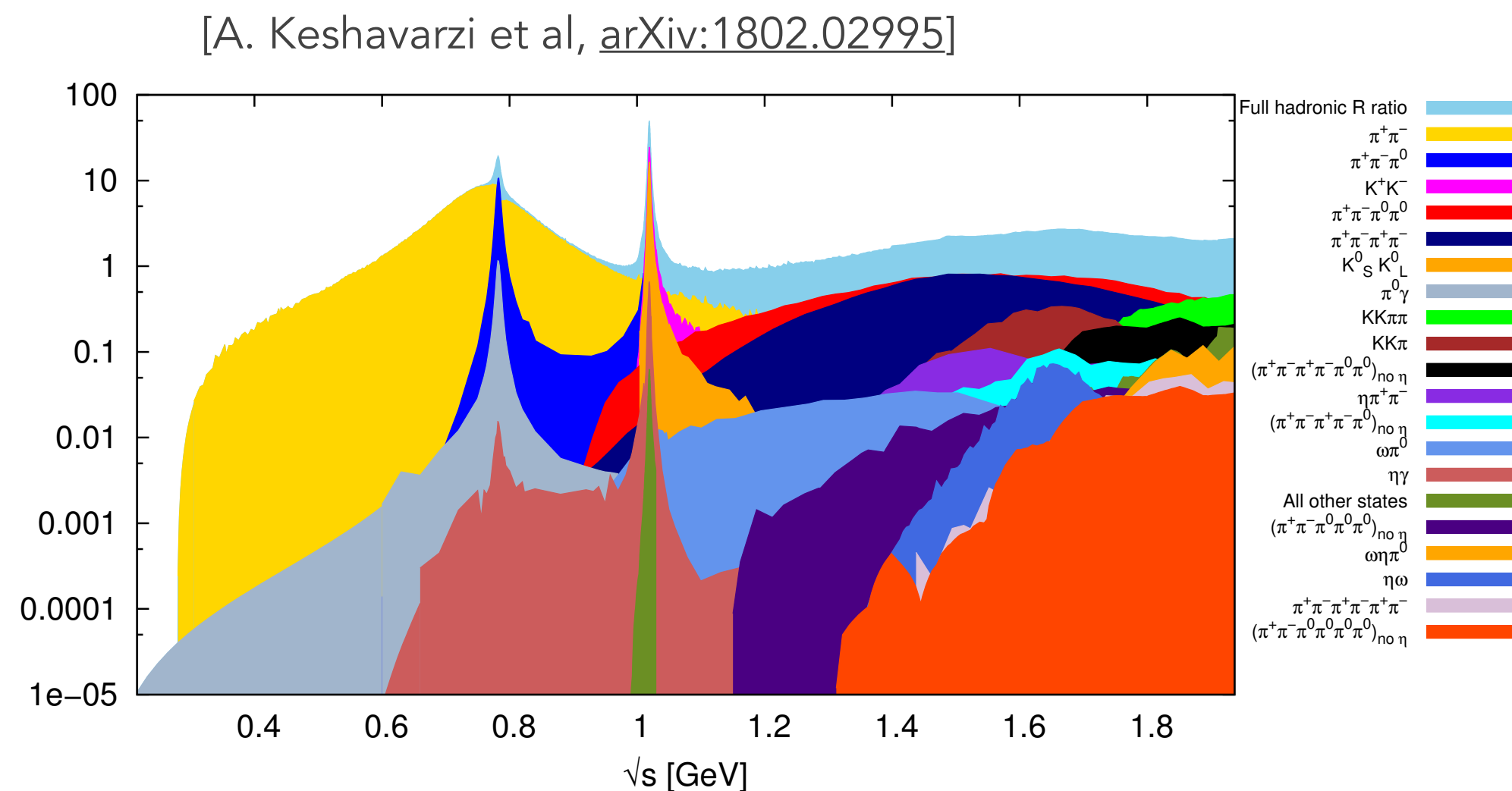
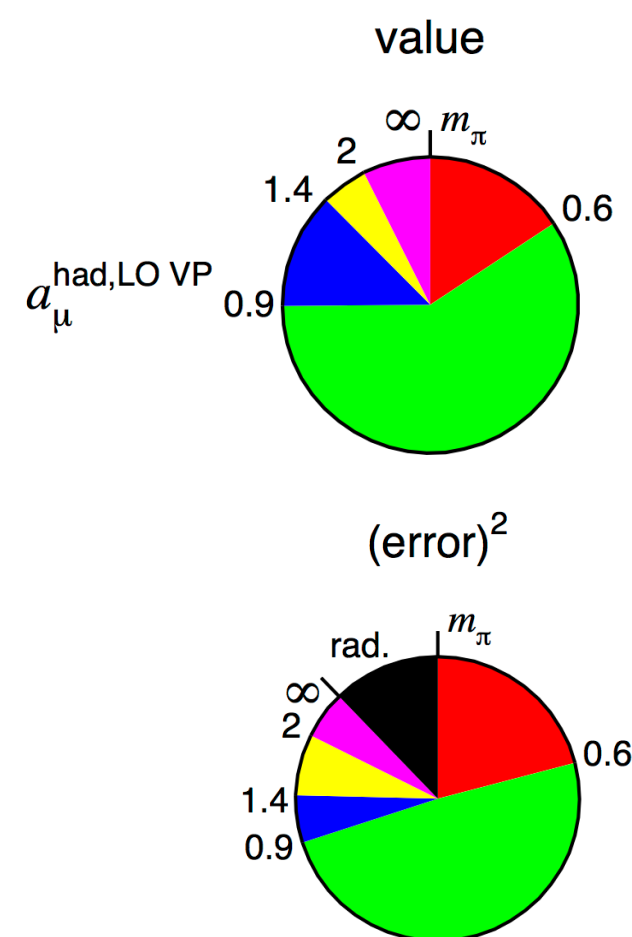
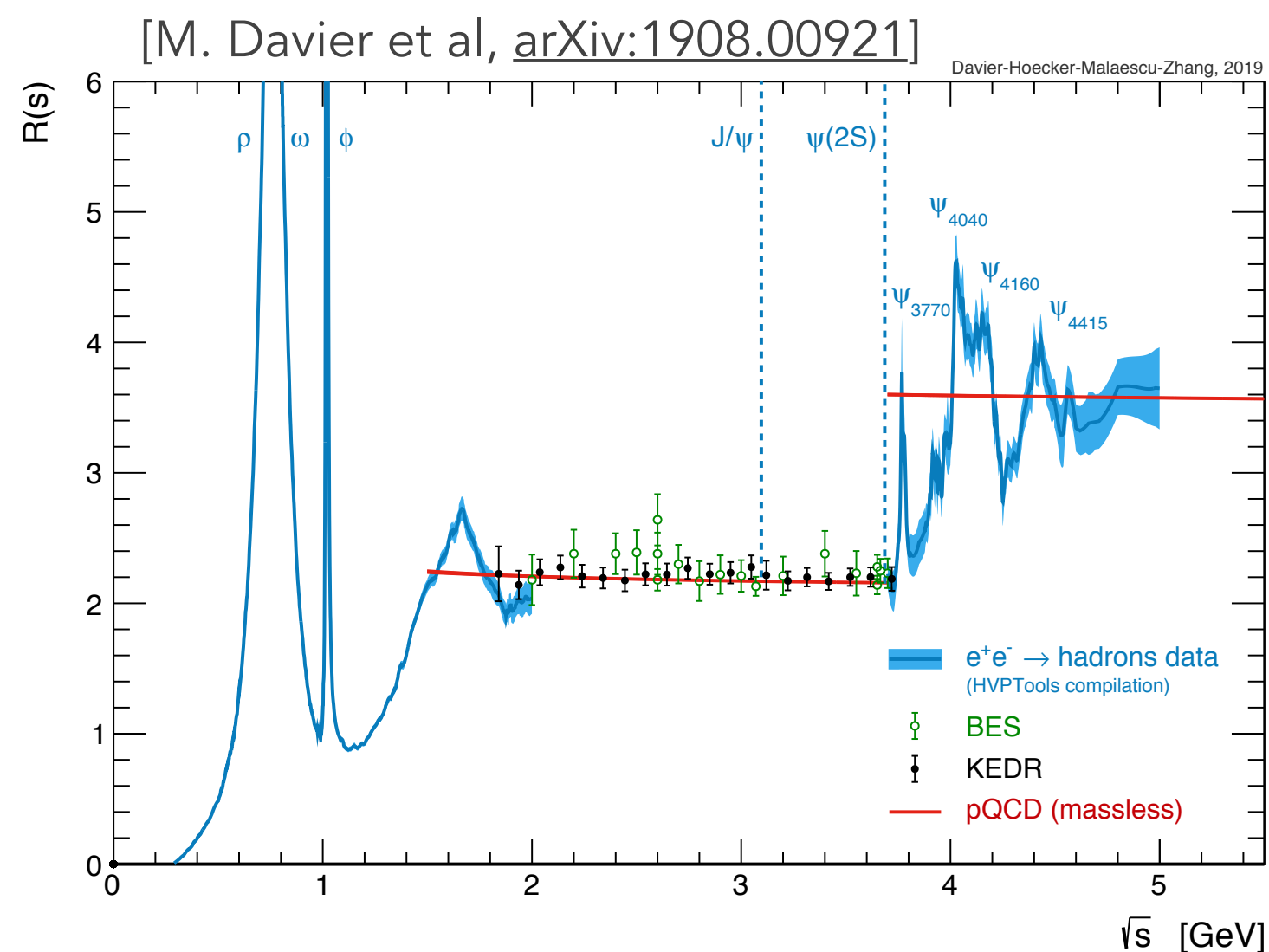
Hadronic Corrections: Comparisons



$$a_\mu^{\text{SM}} = a_\mu^{\text{HVP}} + [a_\mu^{\text{QED}} + a_\mu^{\text{Weak}} + a_\mu^{\text{HLbL}}]$$



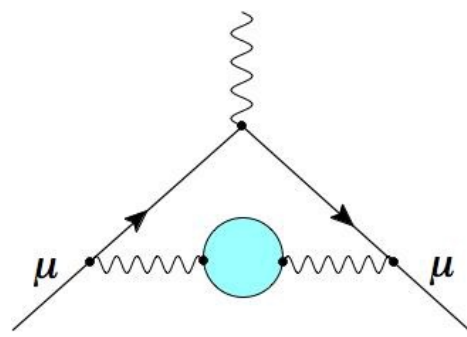
HVP: data-driven



- $\sigma_{\text{had}}(s)$ defined to include real & virtual photons
- direct integration method:** no modelling of $\sigma_{\text{had}}(s)$, summing up contributions from all hadronic channels
- total hadronic cross section $\sigma_{\text{had}}(s)$ from > 100 data sets in more than 35 channels summed up to $\sqrt{s} \sim 2 \text{ GeV}$**
- $\sqrt{s} > 2 \text{ GeV}$: inclusive data + pQCD + narrow resonances
- two independent compilations (DHMZ, KNT) using the direct integration method**

Tensions between BaBar and KLOE data sets:

- Cross checks using analyticity and unitarity relating pion form factor to $\pi\pi$ scattering
- Combinations of data sets affected by tensions
 - conservative merging procedure



HVP: data-driven

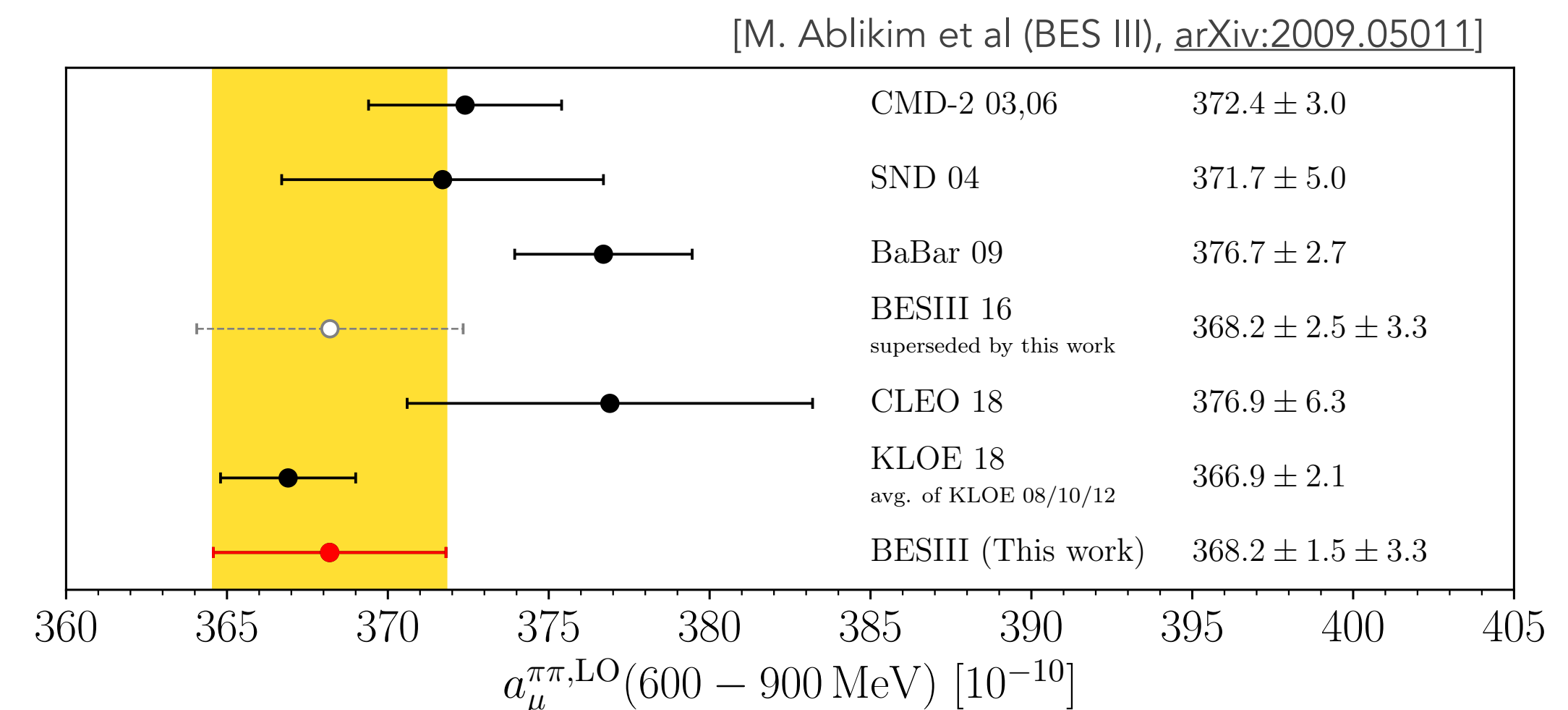
2020 White Paper [T. Aoyama et al, [arXiv:2006.04822](https://arxiv.org/abs/2006.04822), Phys. Repts. 887 (2020) 1-166.]

Conservative merging procedure to obtain a realistic assessment of the underlying uncertainties:

- account for tensions between data sets
- account for differences in methodologies for compilation of experimental inputs and treatment of correlations between systematic errors
- include results using constraints from unitarity & analyticity in $\pi\pi$ and $\pi\pi\pi$ channels
[Colangelo et al, 2018; Anantharayan et al, 2018; Davier et al, 2019; Hoferichter et al, 2019]
- Full NLO radiative corrections [Campanario et al, 2019]

$$a_{\mu}^{\text{HVP,LO}} = 693.1 (2.8)_{\text{exp}} (0.7)_{\text{DV+pQCD}} (2.8)_{\text{BaBar-KLOE}} \times 10^{-10}$$

$$= 693.1 (4.0) \times 10^{-10}$$



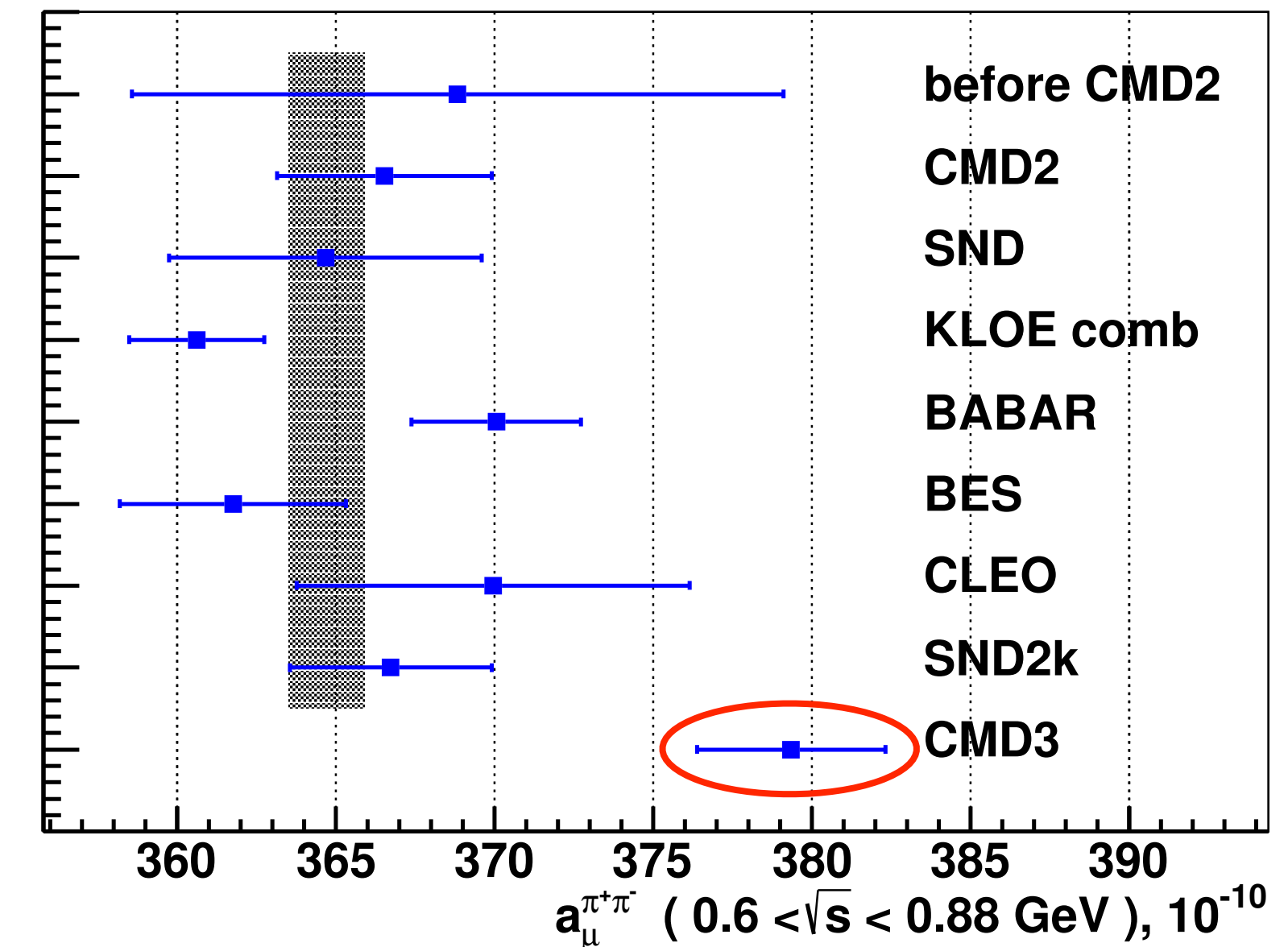
HVP: data-driven

T. Teubner @ Zurich workshop

New results for $\sigma_{\text{had}}(s)$:

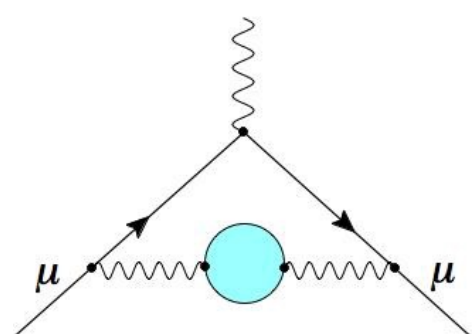
- **$\pi+\pi-\pi^0$** , BESIII (2019), arXiv:1912.11208
- **$\pi+\pi^-$** [covariance matrix erratum], BESIII (2020), Phys.Lett.B 812 (2021)
- **$K+K-\pi^0$** , SND (2020), Eur.Phys.J.C 80 (2020) 12, 1139
- **$e\pi^0\gamma$** (res. only), SND (2020), Eur.Phys.J.C 80 (2020) 11, 1008
- **$\pi+\pi^-$** , SND (2020), JHEP 01 (2021) 113
- **$e\tau\omega \rightarrow \pi^0\gamma$** , SND (2020), Eur.Phys.J.C 80 (2020) 11, 1008
- **$\pi+\pi-\pi^0$** , SND (2020), Eur.Phys.J.C 80 (2020) 10, 993
- **$\pi+\pi-\pi^0$** , BaBar (2021), Phys.Rev.D 104 (2021) 11, 112003
- **$\pi+\pi-2\pi^0\omega$** , BaBar (2021), Phys. Rev. D 103, 092001
- **$e\tau e\gamma$** , SND (2021), Eur.Phys.J.C 82 (2022) 2, 168
- **$e\tau\omega$** , BaBar (2021), Phys.Rev.D 104 (2021) 11, 112004
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- **$2\pi+2\pi-3\pi^0$** , BaBar (2021), Phys. Rev. D 103, 092001
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- **$\pi+\pi-\pi+\pi-\eta$** , BaBar (2021), Phys. Rev. D 103, 092001
- **inclusive**, BESIII (2021), Phys.Rev.Lett. 128 (2022) 6, 062004
- ...

New: from CMD-3 [F. Ignatov et al, [arXiv:2302.08834](https://arxiv.org/abs/2302.08834)]



A new puzzle!

- discrepancies between experiments now $\gtrsim (3 - 5) \sigma$ need to be understood/resolved
- [\(virtual\) scientific seminar + discussion panel on CMD-3 measurement](#)
March 27 (8:00 –11:00 am US CDT)
Discussions are continuing....
- [6th Muon g-2 Theory Initiative workshop](#) (4-8 Sep 2023, Bern)



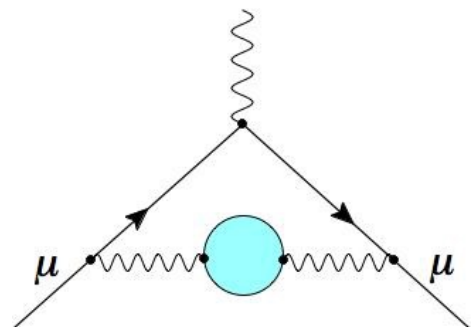
HVP: data-driven

Ongoing work on experimental inputs:

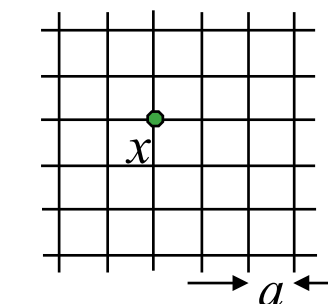
- **BaBar**: new analysis of large data set in $\pi\pi$ channel, also $\pi\pi\pi$, other channels
- **KLOE**: new analysis of large data set in $\pi\pi$ channel, other channels
- **SND**: new results for $\pi\pi$ channel, other channels in progress
- **BESIII**: new results in 2021 for $\pi\pi$ channel, continued analysis also for $\pi\pi\pi$, other channels
- **Belle II**: [arXiv:2207.06307](https://arxiv.org/abs/2207.06307) (Snowmass WP)
Better ultimate statistics than BaBar or KLOE; similar or better systematics for low-energy cross sections

Ongoing work on theoretical aspects:

- **better treatment of structure dependent radiative corrections (NLO) in $\pi\pi$ and $\pi\pi\pi$ channels**
so far: FsQED (scalar QED + pion form factor)
tests of radiative corrections using exp. measurement of charge asymmetry [Ignatov + Lee, arXiv:2204.12235]
new dispersive treatment [Colangelo et al, arXiv:2207.03495]
- **Developing NNLO Monte Carlo generators** (STRONG 2020 workshop <https://agenda.infn.it/event/28089/>)
- **including τ decay data**: requires nonperturbative evaluation of IB correction [M. Bruno et al, arXiv:1811.00508]



Lattice HVP: Introduction



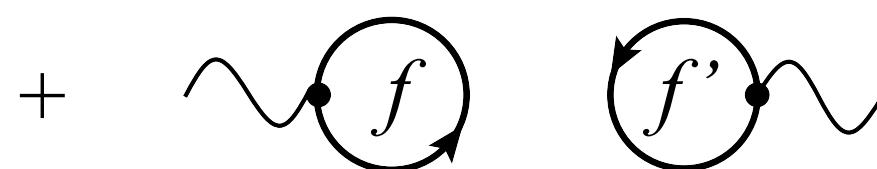
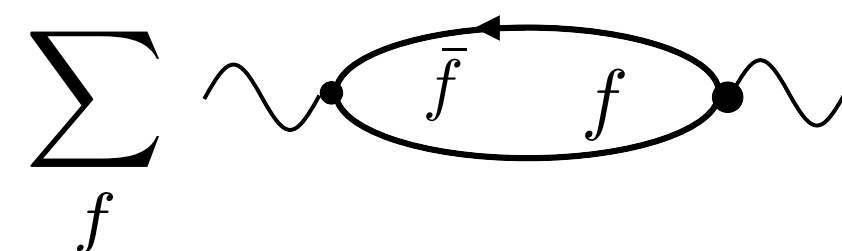
Calculate a_μ^{HVP} in Lattice QCD:

$$a_\mu^{\text{HVP,LO}} = \sum_f a_{\mu,f}^{\text{HVP,LO}} + a_{\mu,\text{disc}}^{\text{HVP,LO}}$$

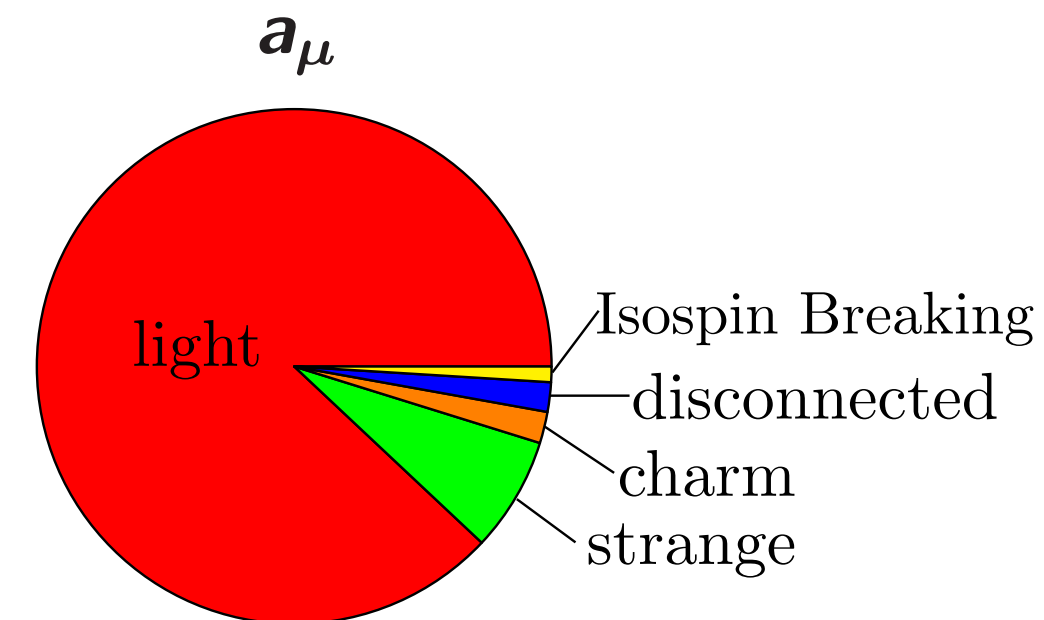
- Separate into connected for each quark flavor + disconnected contributions (gluon and sea-quark background not shown in diagrams)

Note: almost always $m_u = m_d$

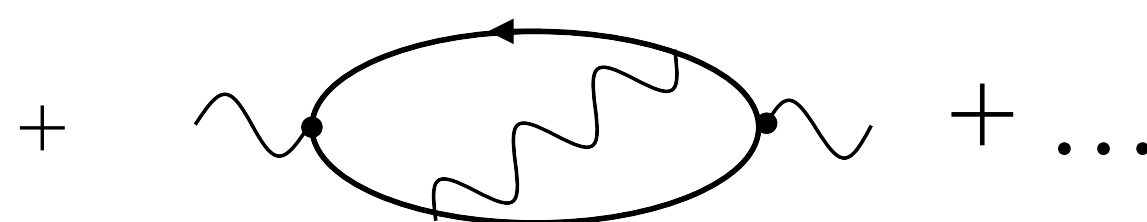
$f = ud, s, c, b$



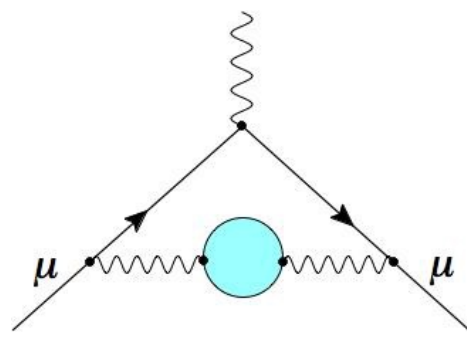
- light-quark connected contribution: $a_\mu^{\text{HVP,LO}}(ud) \sim 90\%$ of total
- s, c, b -quark contributions $a_\mu^{\text{HVP,LO}}(s, c, b) \sim 8\%, 2\%, 0.05\%$ of total
- disconnected contribution: $a_{\mu,\text{disc}}^{\text{HVP,LO}} \sim 2\%$ of total
- Isospinbreaking (QED + $m_u \neq m_d$) corrections: $\delta a_\mu^{\text{HVP,LO}} \sim 1\%$ of total



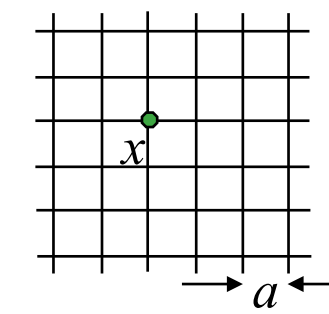
- need to add QED and strong isospin breaking ($\sim m_u - m_d$) corrections:



$$a_\mu^{\text{HVP,LO}} = a_\mu^{\text{HVP,LO}}(ud) + a_\mu^{\text{HVP,LO}}(s) + a_\mu^{\text{HVP,LO}}(c) + a_{\mu,\text{disc}}^{\text{HVP,LO}} + \delta a_\mu^{\text{HVP,LO}}$$



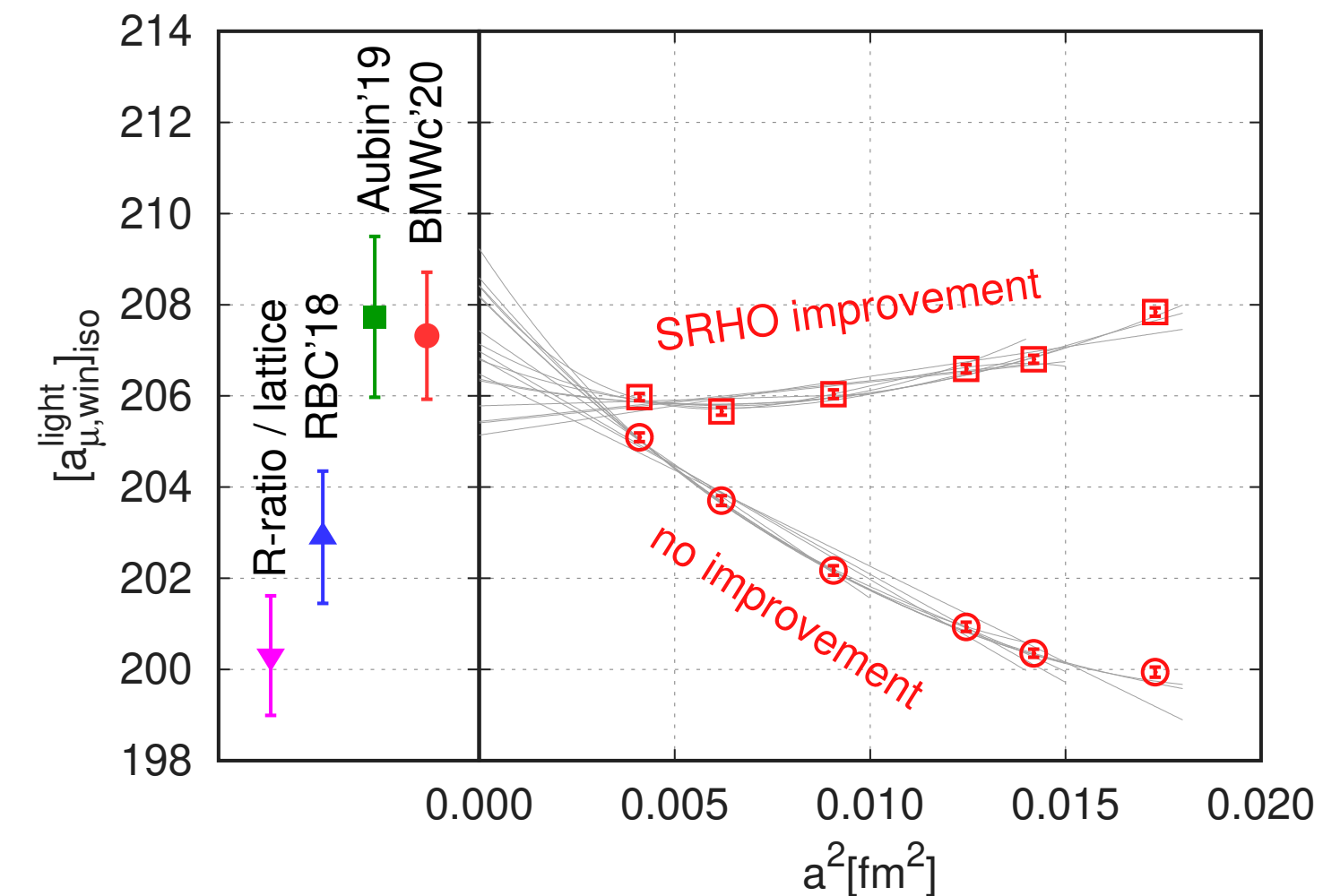
Lattice HVP: results



$$a_{\mu}^{\text{HVP,LO}} = 4\alpha^2 \int_0^{\infty} dt C(t) \tilde{w}(t)$$

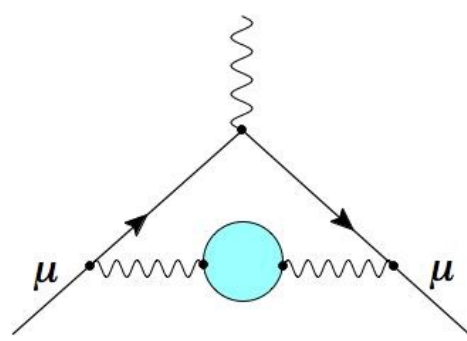
In 2020 WP:

- Lattice HVP average at 2.6 % total uncertainty: $a_{\mu}^{\text{HVP,LO}} = 711.6 (18.4) \times 10^{10}$
- BMW 20 [Sz. Borsanyi et al, arXiv:2002.12347, 2021 Nature] first LQCD calculation with sub-percent (0.8 %) error in tension with data-driven HVP (2.1σ)
- Further tensions for intermediate window:
 - 3.7σ tension with data-driven evaluation
 - 2.2σ tension with RBC/UKQCD18

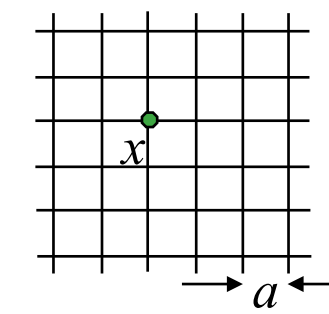


Staggered fermions:

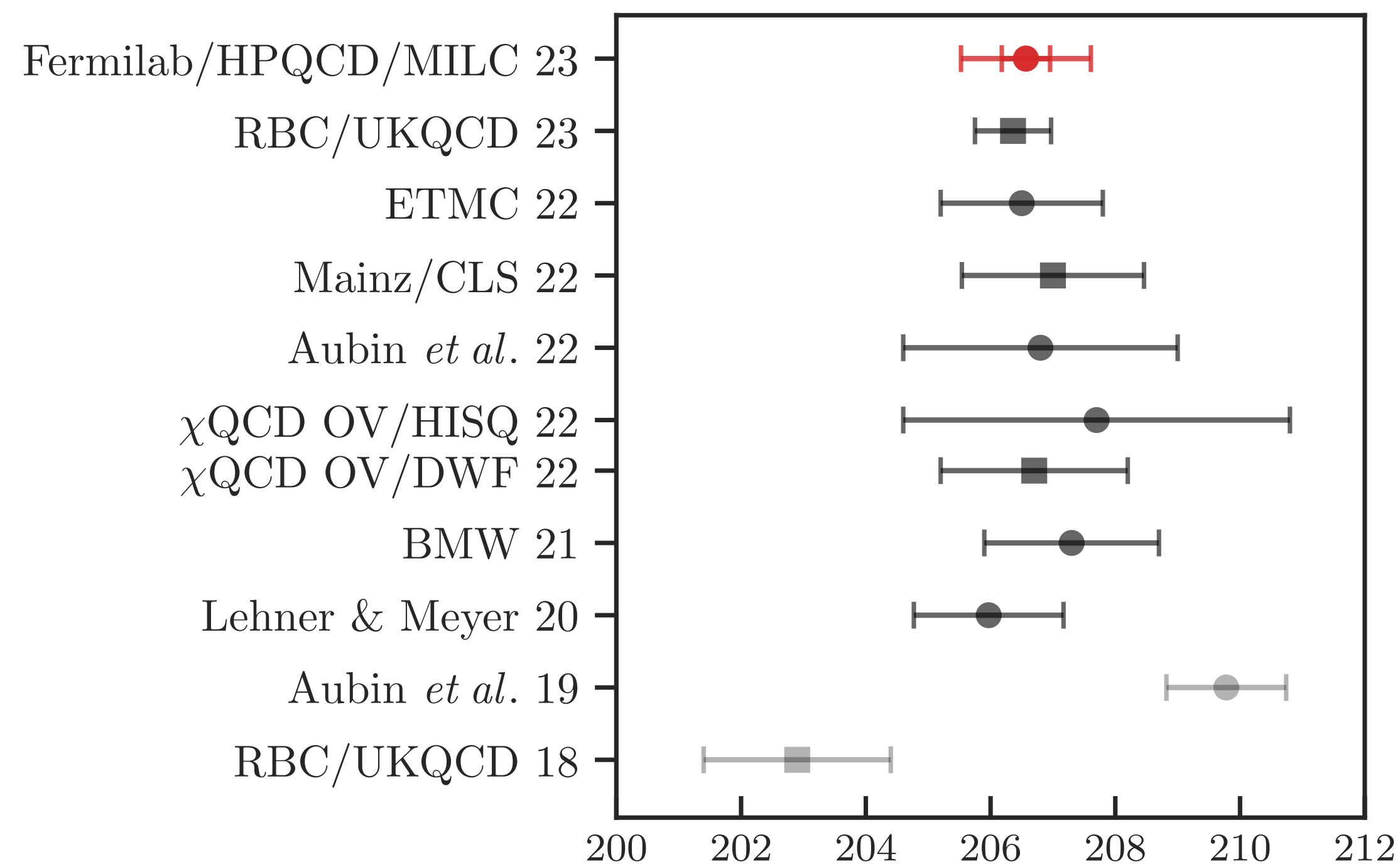
- taste-breaking effects (which yield taste splittings) are significant (sometimes dominant) source of discretization errors
- possible to use EFT schemes (ChPT, Chiral Model, MLLGS) to correct for taste-splitting effects before taking continuum extrapolation: continuum limit should not be affected



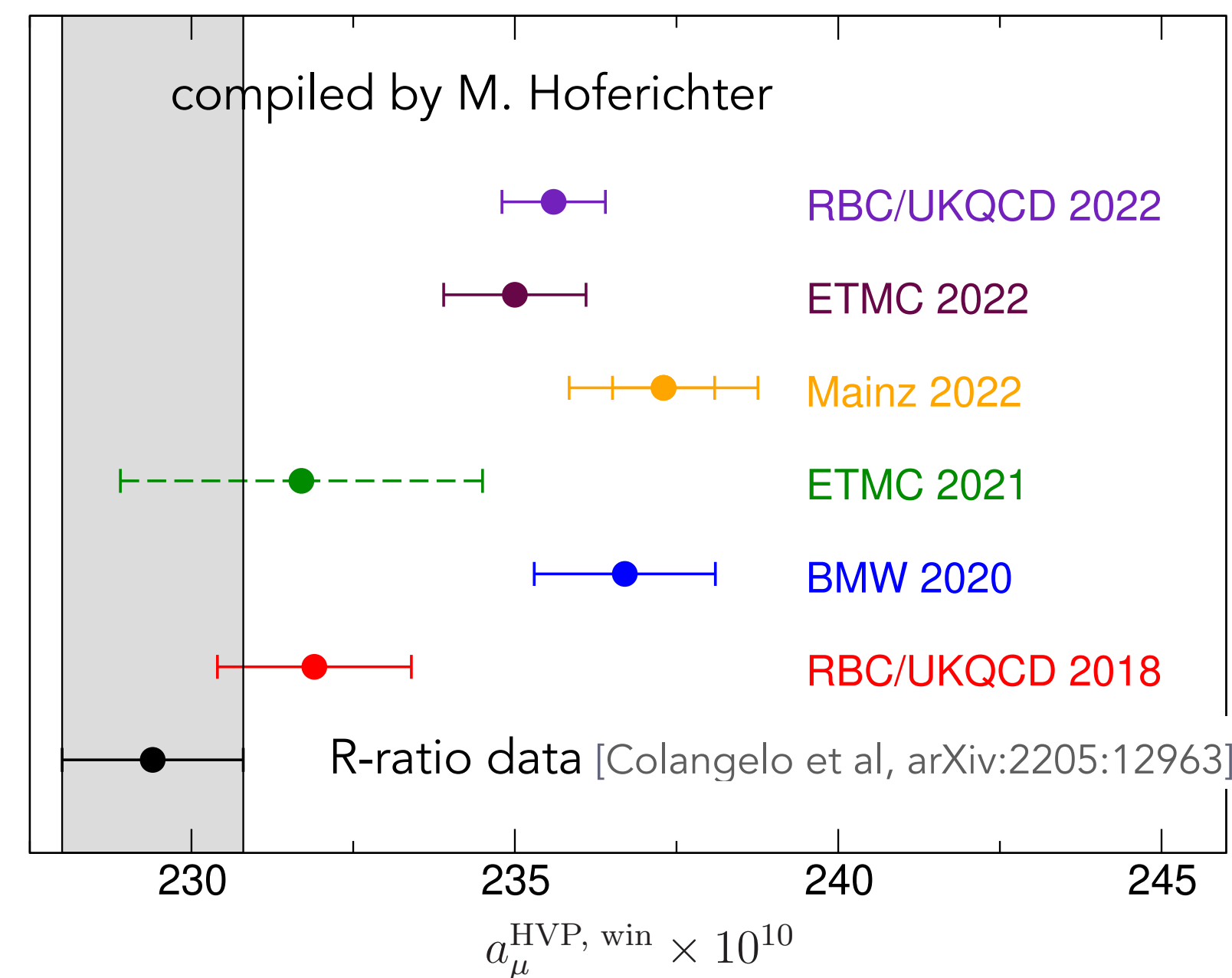
Lattice HVP: results



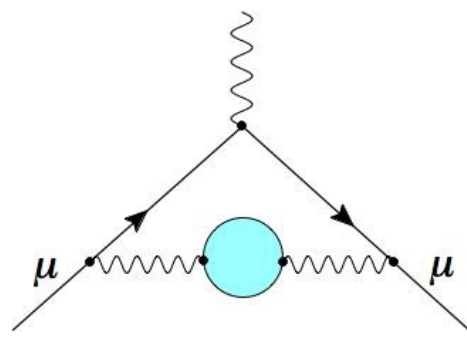
- new results in 2022/2023 for intermediate window, a_μ^W from six different lattice groups.
- blind analyses: Fermilab/HPQCD/MILC + RBC/UKQCD
- lattice-only comparison of light-quark connected contribution to intermediate window:



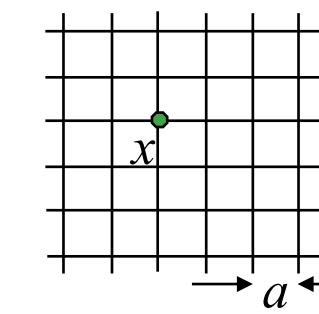
- LQCD results including all contributions



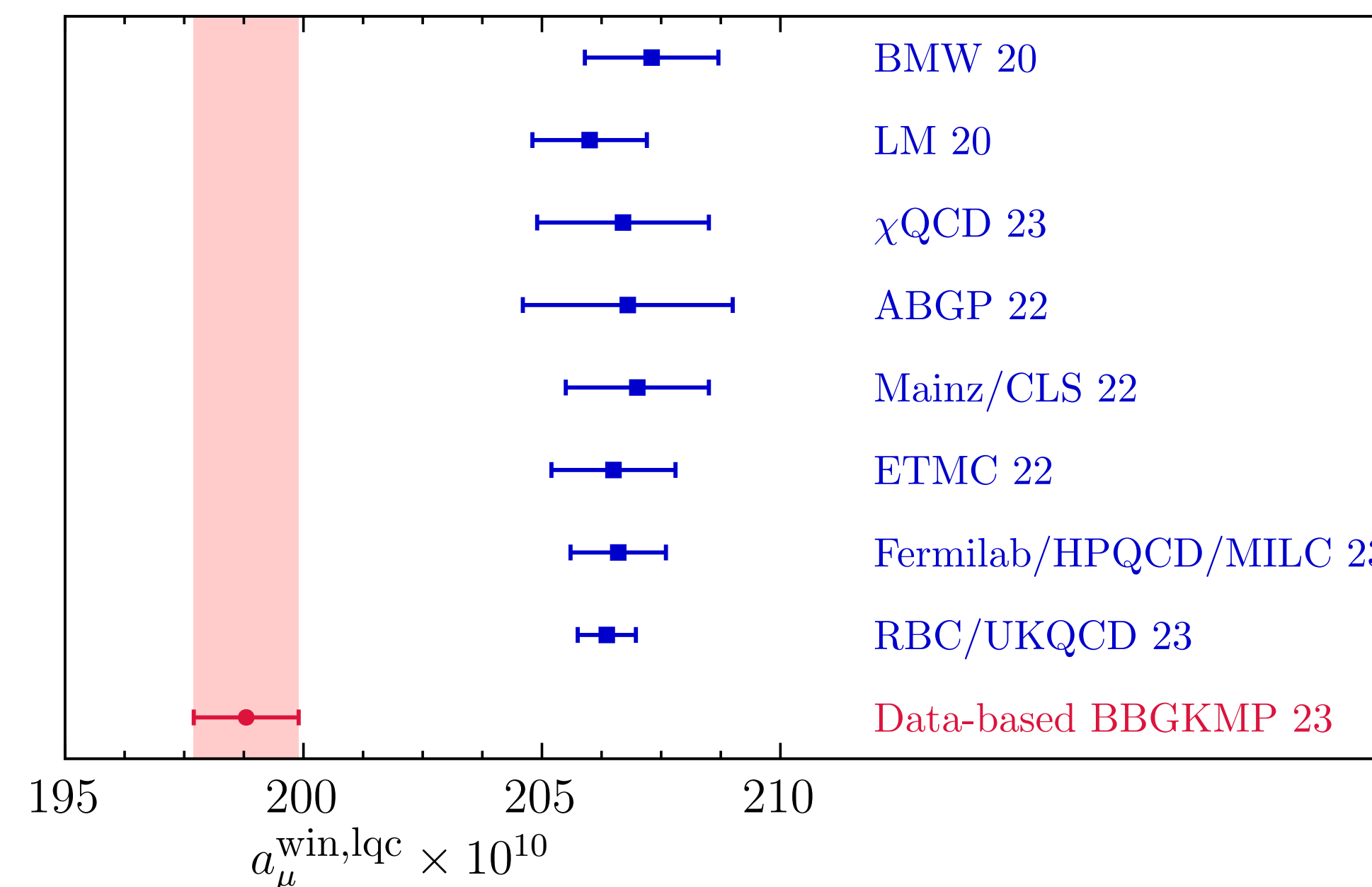
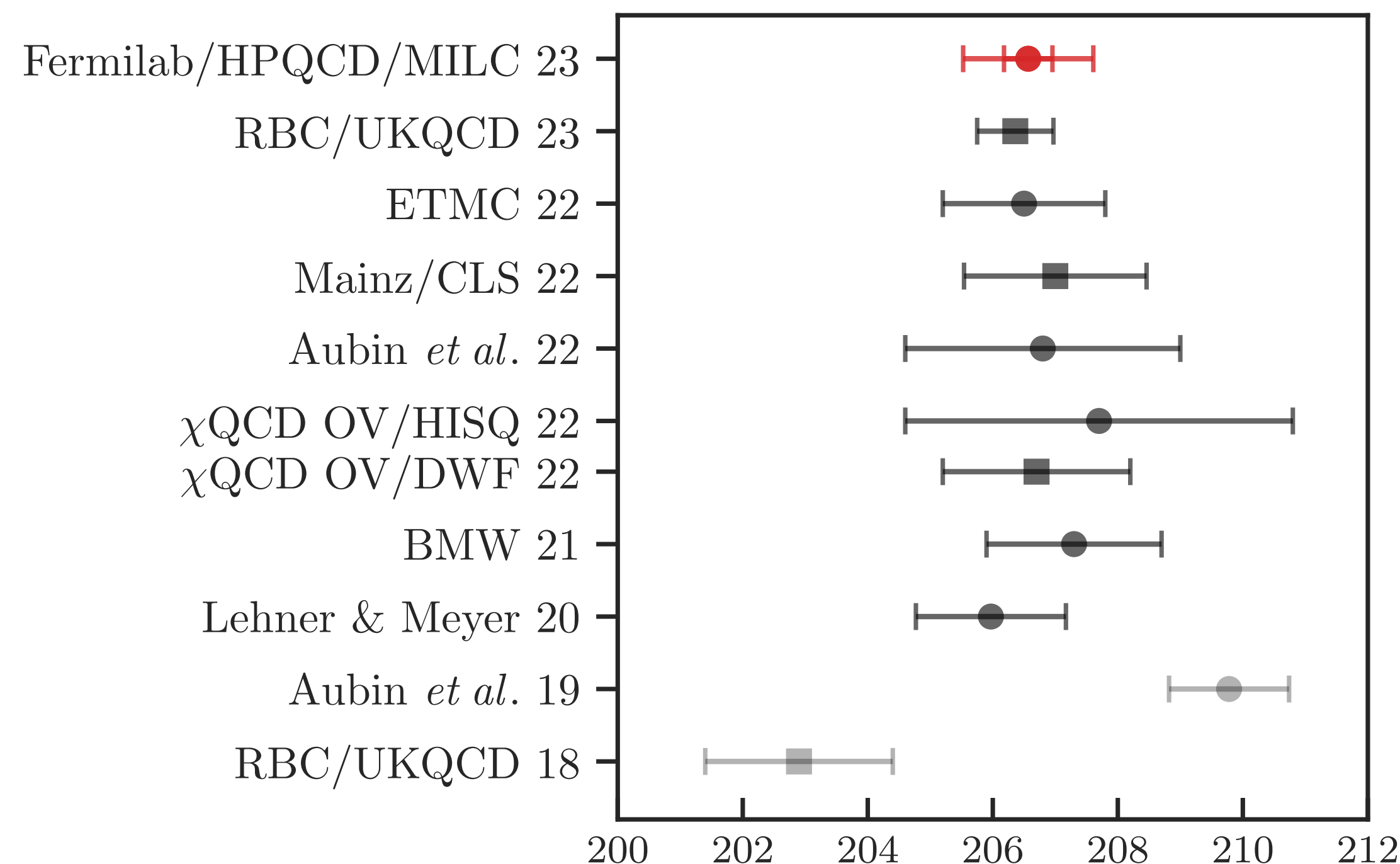
$\sim (3.5 - 4)\sigma$ tensions between LQCD and (pre-2023) data-driven evaluations



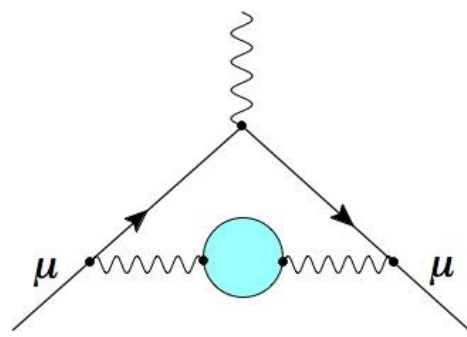
Lattice HVP: results



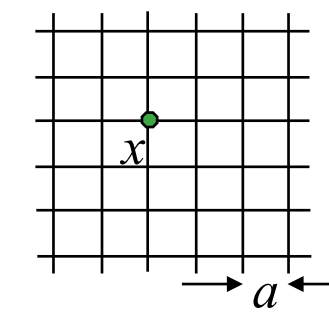
- new results in 2022/2023 for intermediate window, a_μ^W from six different lattice groups.
- blind analyses: Fermilab/HPQCD/MILC + RBC/UKQCD
- lattice-only comparison of light-quark connected contribution
- dispersive evaluation of light-quark connected contribution [benno, et al, arXiv:2306.



primary source of tension



Lattice HVP: outlook



Ongoing work:

Evaluations of short-distance windows [ETMC, RBC/UKQCD]

Proposals for computing more windows:

- Use linear combinations of finer windows to locate the tension (if it persists) in \sqrt{s} [Colangelo et al, arXiv:12963]
- Use larger windows, excluding the long-distance region $t \gtrsim 2 \text{ fm}$ to maximize the significance of any tension [Davies et al, arXiv:2207.04765]

For total HVP:

- independent lattice results at sub-percent precision: coming soon!
- Including $\pi\pi$ states for refined long-distance computation (Mainz, RBC/UKQCD, FNAL/MILC)
- include smaller lattice spacings to test continuum extrapolations (needs adequate computational resources)

g-2 sessions @ Lattice 2023 conference

Summary

- ★ consistent results from independent, precise LQCD calculations for light-quark connected contribution to intermediate window a_μ^W ($\sim 1/3$ of $a_\mu^{\text{HVP,LO}}$) \Rightarrow 3 – 4 σ tension with data-driven results?
- ★ still need independent LQCD results for long-distance contribution, total HVP: coming soon
 - \Rightarrow develop method average for lattice HVP results, assess tensions (if any) with data-driven average
- ★ Programs and plans in place to improve by 2025:
 - 📍 data-driven HVP: if differences are resolved/understood, $\sim 0.3\%$
new measurements from BaBar, KLOE, SND, Belle II,.... will shed light on current discrepancies (blind analyses are paramount!)
improved treatment of structure dependent radiative corrections (NLO) in $\pi\pi$ and $\pi\pi\pi$ channels
 - 📍 lattice HVP: if no tensions between independent lattice results, $\sim 0.5\%$
 - 📍 dispersive HLbL and lattice HLbL: no puzzles, steady progress, $\sim 10\%$
- ★ IF tensions/differences between data-driven HVP and lattice HVP are resolved, SM prediction will likely match precision goal of the Fermilab experiment.
- ★ IF NOT, will need detailed comparisons, explore connections between HVP, $\sigma(e^+e^-)$, $\Delta\alpha$, global EW fits.
- ★ BSM implications \Rightarrow appendix
 - \Rightarrow continued coordination by Theory Initiative: workshops, WPs, ...

Near-term Timeline

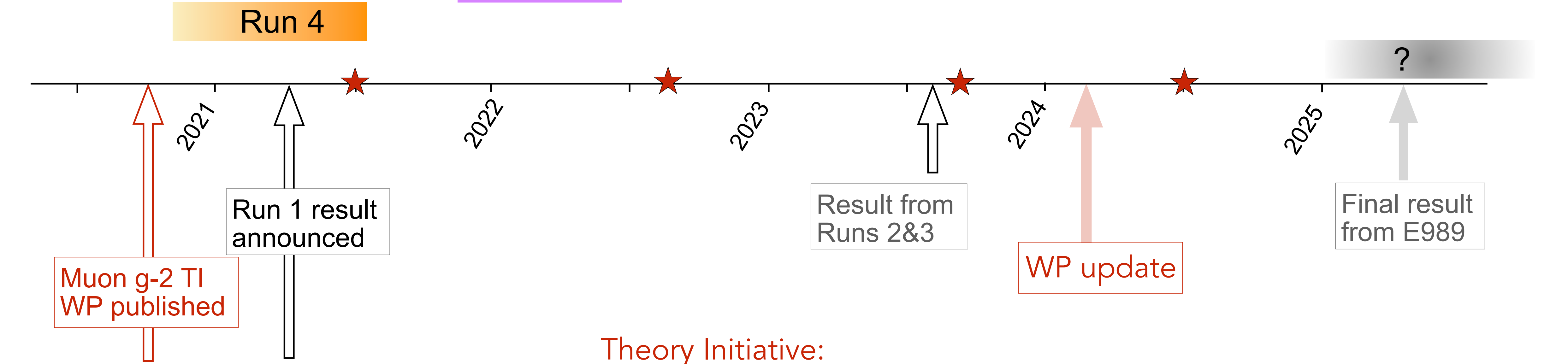
FNAL E989

J-PARC E34

Run 4

Run 5

Run 6

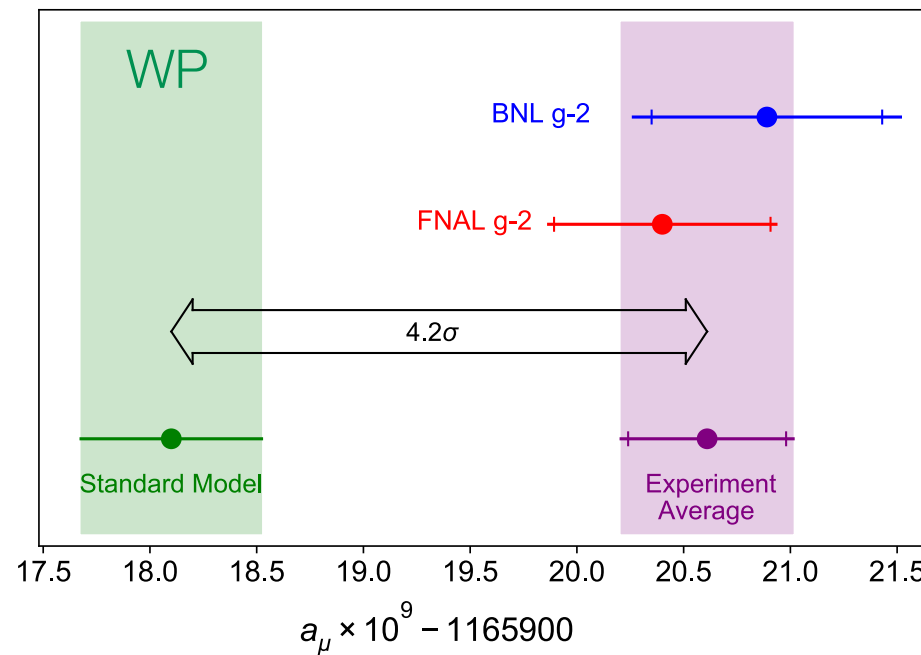


Theory Initiative:

- ★ ongoing activities: develop method average for Lattice HVP
- ★ CMD-3 seminar (virtual): **27 March 2023** at 8:00am US CDT
- ★ WP update with all available results ~ early 2024

- ★ TI workshops:
 - Jun 2021 @ KEK (virtual)
 - Sep 2023 @ Bern

- Sep 2022 @ Higgscentre
- Summer 2024 @ KEK



Outlook

★ Experimental program beyond 2025:

- 📍 J-PARC: Muon $g-2$ /EDM
- 📍 Fermilab: future muon campus experiments?
- 📍 Belle II, BESIII, Novosibirsk,...
- 📍 Chiral Belle (?)

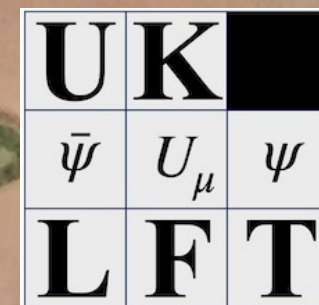
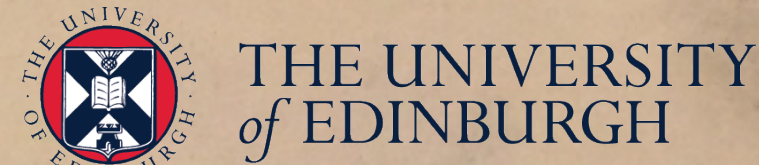
★ Data-driven/dispersive program beyond 2025:

- 📍 development of NNLO MC generators
- 📍 for HLbL, improved experimental/lattice inputs together with further development of dispersive approach

★ MUonE will provide a space-like measurement of HVP

★ Lattice QCD beyond 2025:

- 📍 access to future computational resources (coming Exascale) will enable improvements of all errors (statistical and systematic)
- 📍 concurrent development of better methods and algorithms (gauge-field sampling, noise reduction) will accelerate progress
- 📍 **beyond $g-2$** : a rich program relevant for all areas of HEP



Cảm ơn!

