

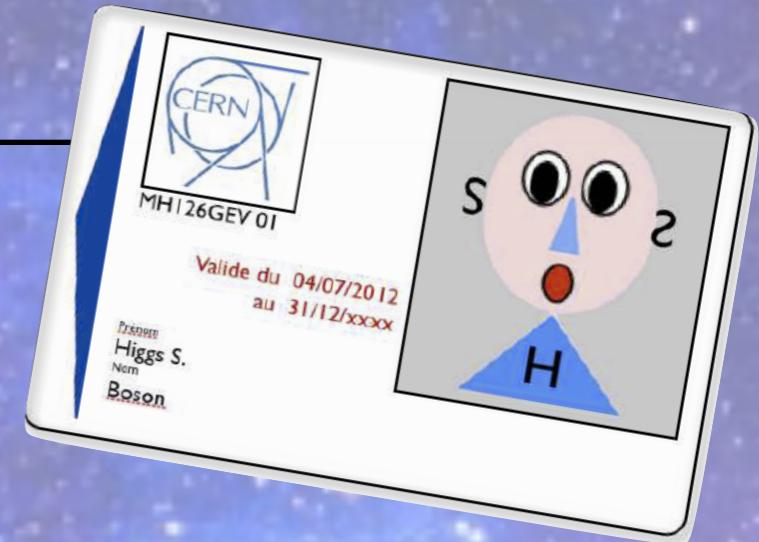
Higgs Theory or Cracking the Code of the Universe with the Higgs boson

M. Mühlleitner (KIT)
*30th Anniversary of the
Recontres du Vietnam
Windows on the Universe
ICISE, Quy Nhon, 6-12 Aug 2023*

Outline



- ♦ Introduction
- ♦ Potential Parameters
 - Higgs Masses
 - Higgs Self-Couplings
- ♦ More on Precision: BSM Decays
- ♦ Higgs Pair Production
 - Precision
 - Phenomenology
- ♦ HH and Baryogenesis
- ♦ Conclusions



Outline

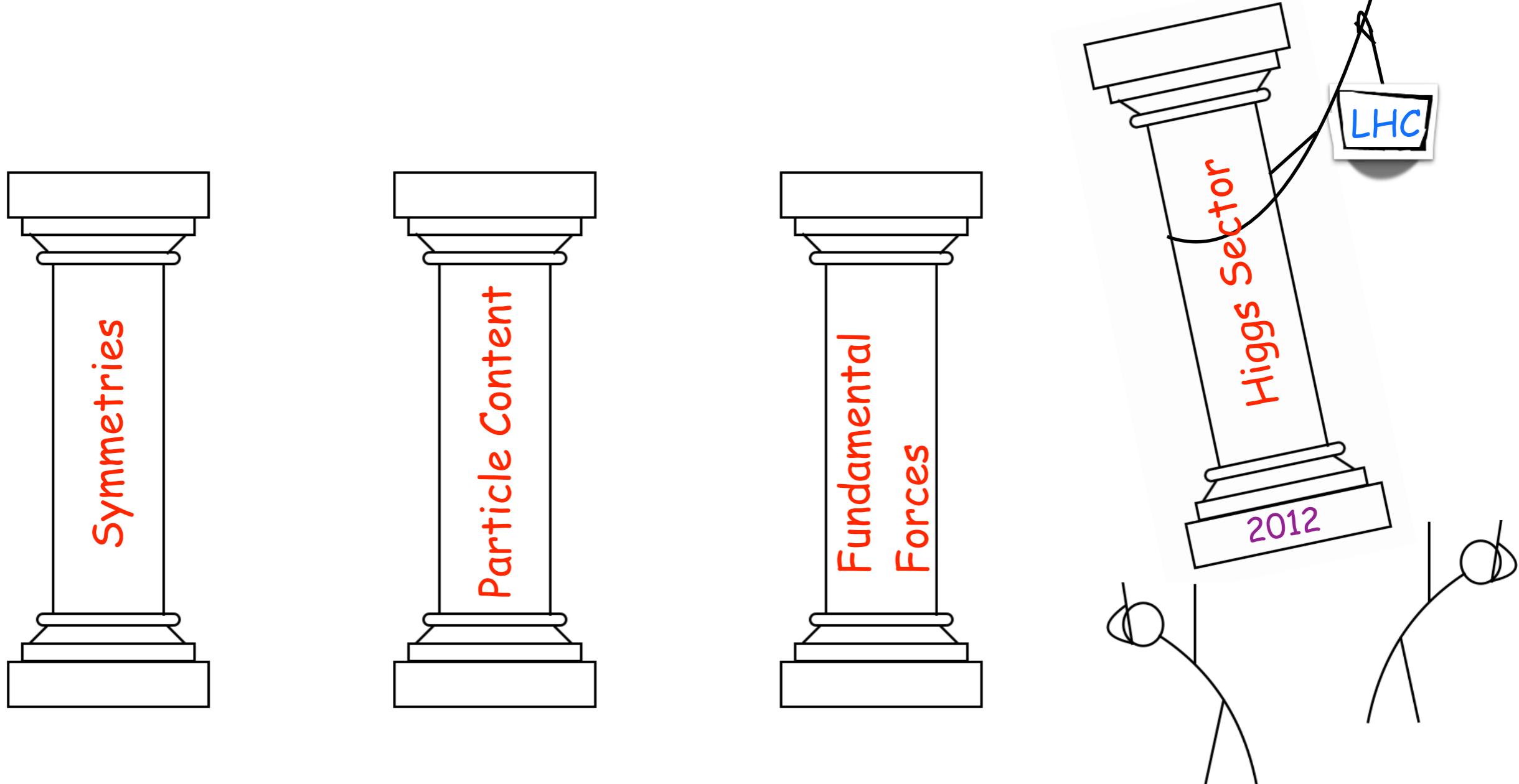
Disclaimer 1: Not covered
Higgs production cross
sections, Dark Matter

- 
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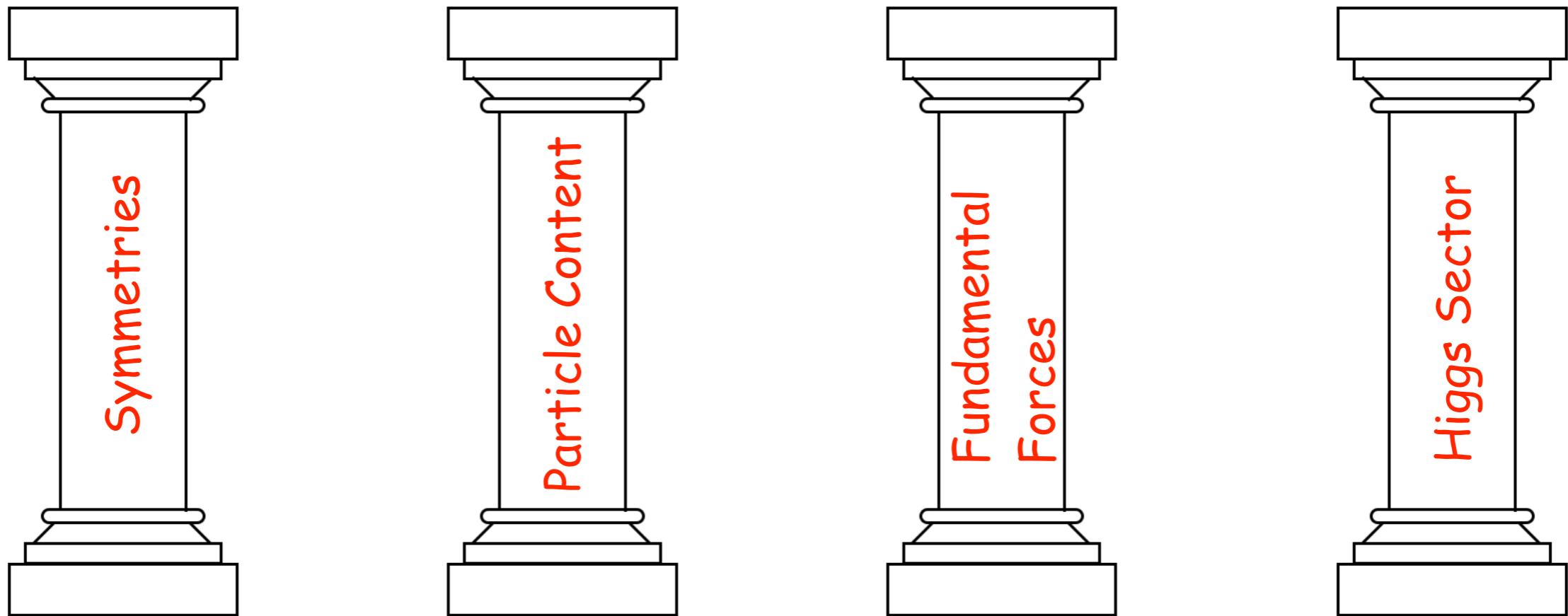


Disclaimer 2: Focus on
Beyond-Standard-Model
Theories & Phenomenology

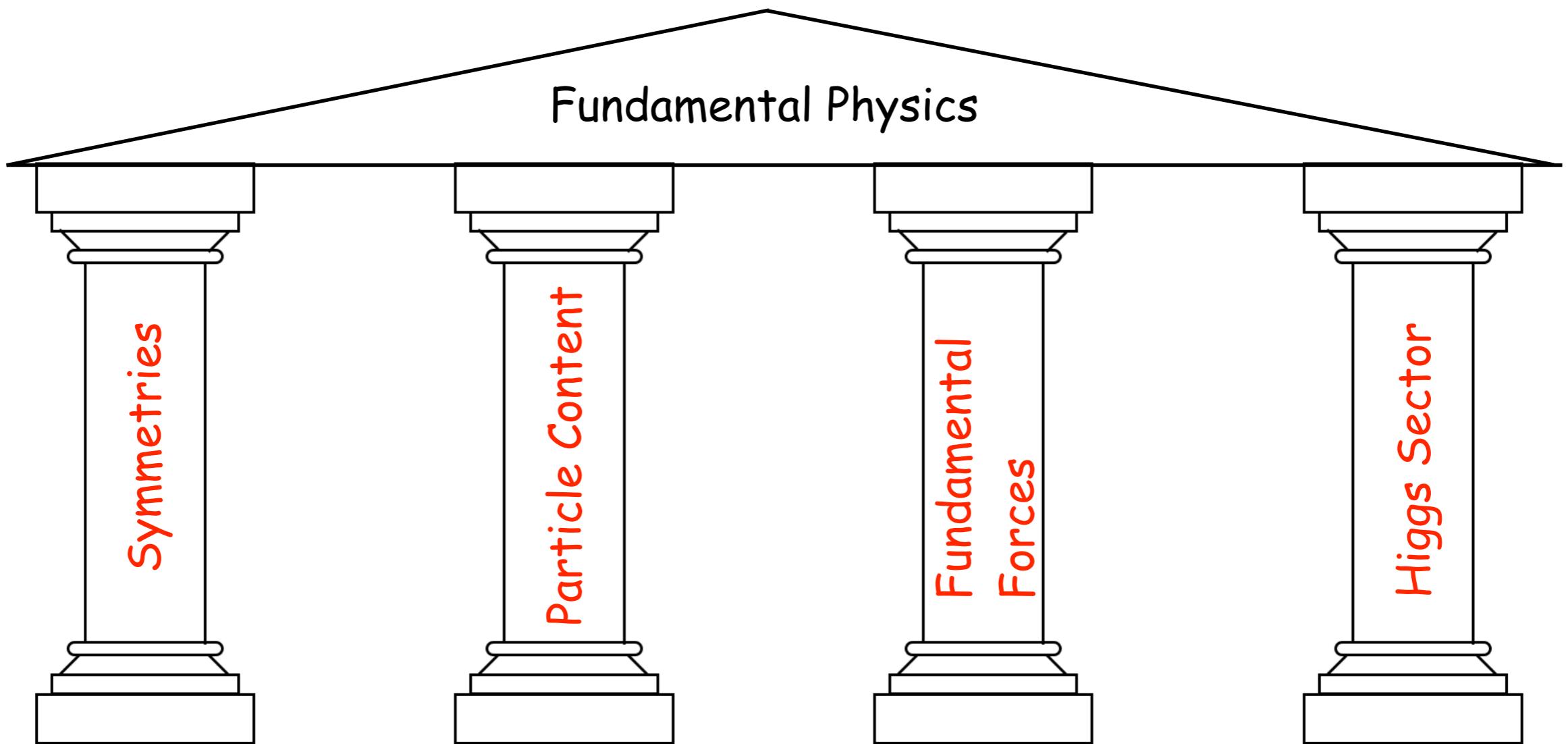
The Four Pillars of the Standard Model



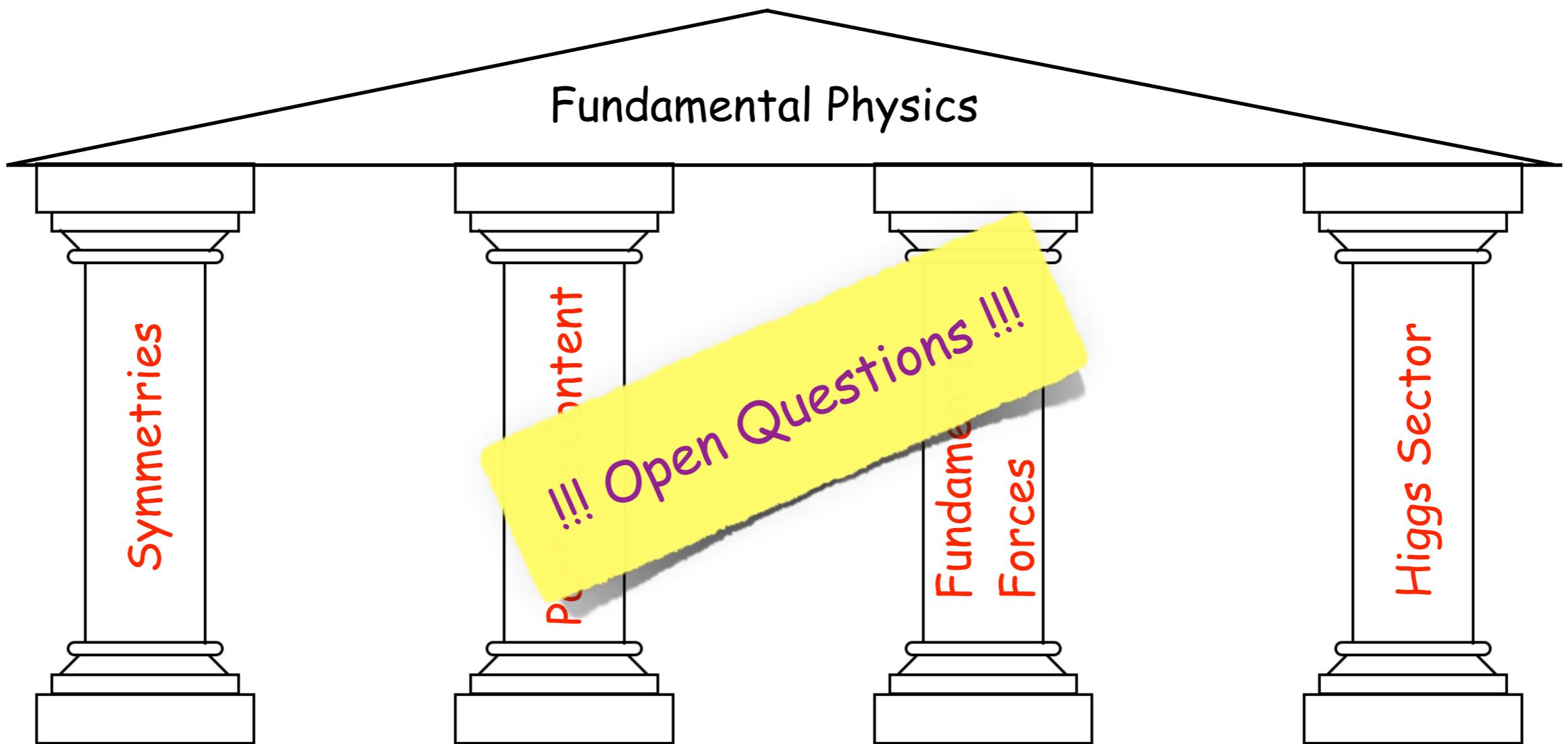
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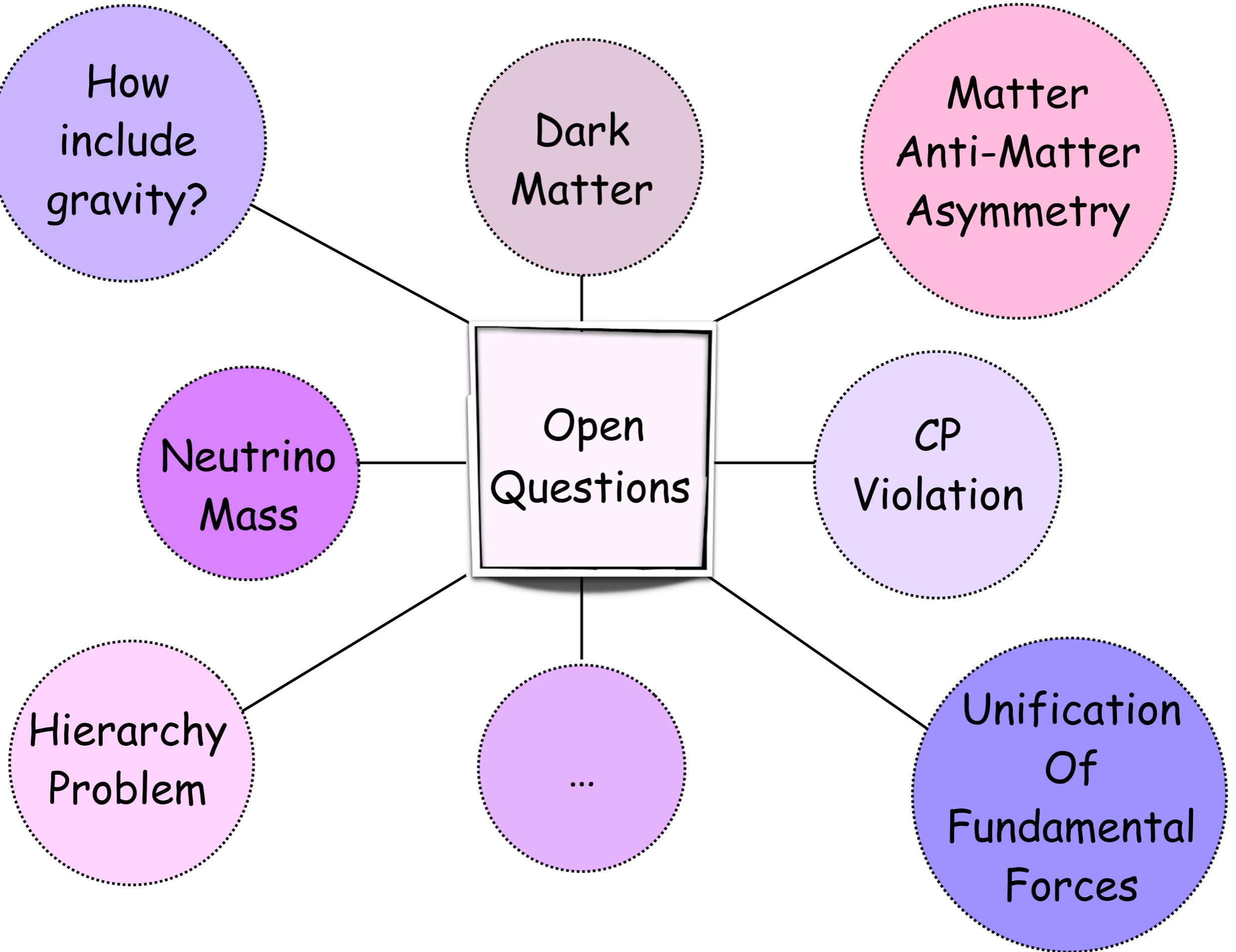


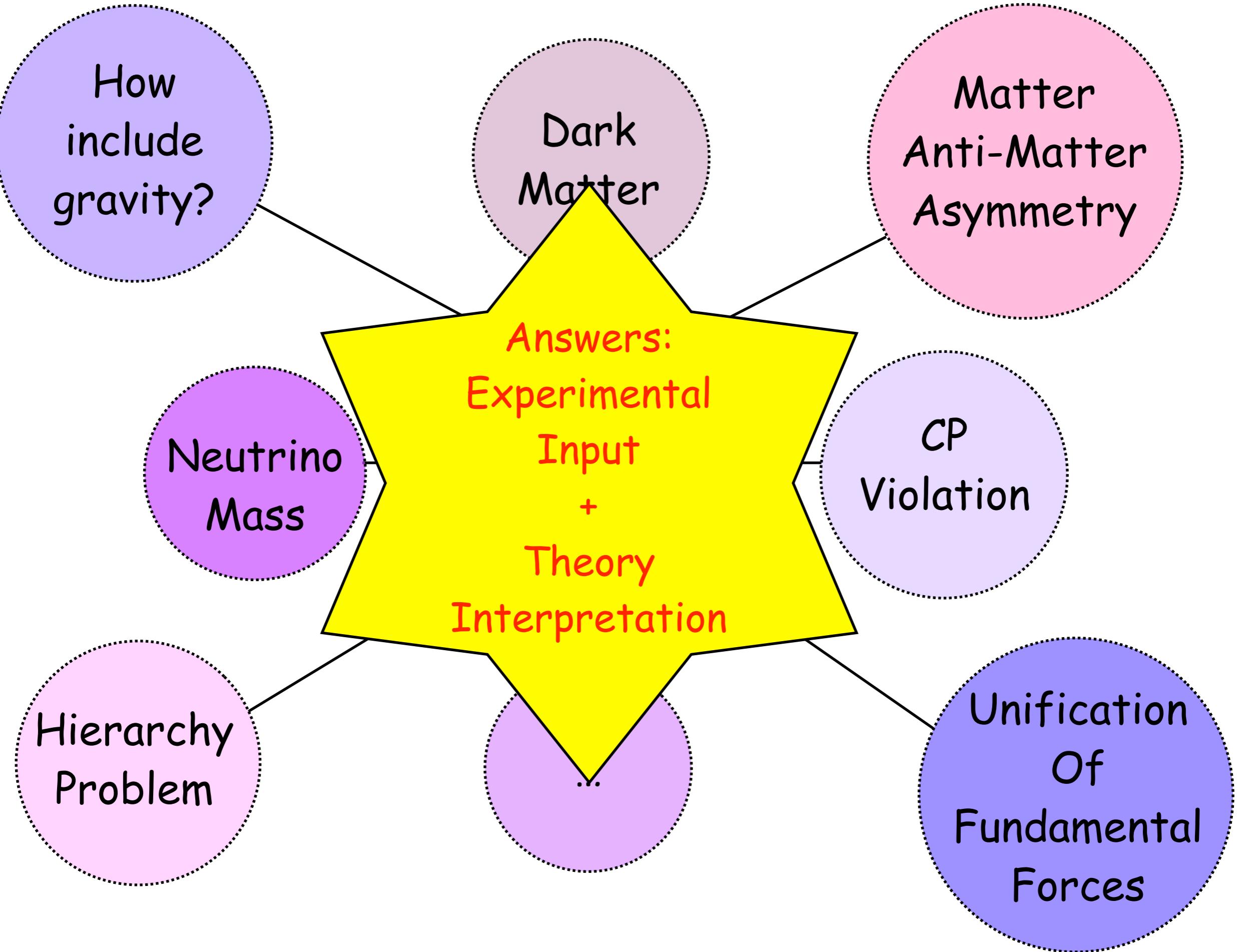
The Standard Model is Structurally Complete



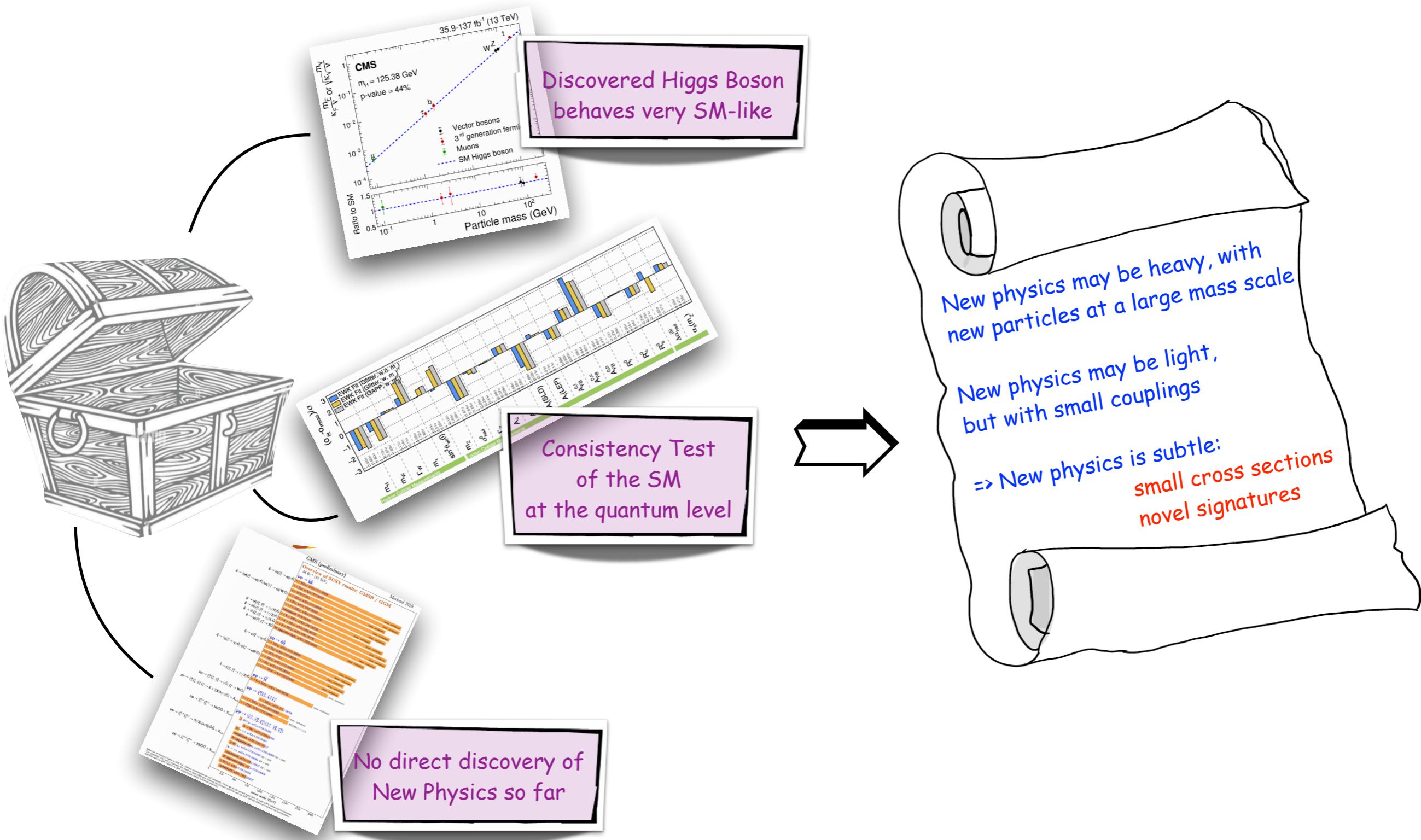
The Standard Model is Structurally Complete - But







Status

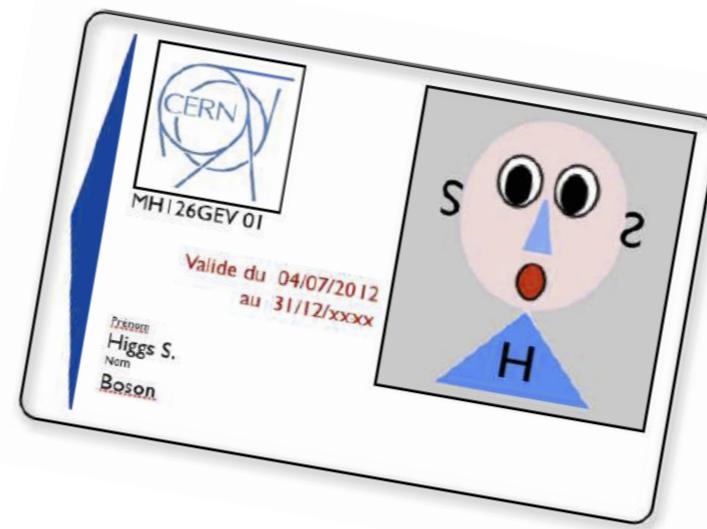


How to corner New Physics?

- ♦ **Experimental reality:** No Beyond the Standard Model Physics discovered so far!
Guido Altarelli, 16/1/12, KIT: „The situation is depressing, but not desperate.“

- ♦ We have the SM-like Higgs boson

What can we learn from Higgs physics?



- ♦ Corner new physics:

Combination of all available information from different sectors and experiments:
Higgs physics, Dark Matter searches, baryogenesis, astrophysics, cosmology, ...

Experiment: **Precision analyses** - new analysis techniques, ML, ...

Theory: **Precision predictions** for observables for SM, BSM (specific models, EFT)

Potential Parameters



The Role of the Higgs Boson Mass

♦ Present Accuracy: [ATLAS,CMS]

$$M_H = 125.09 \pm 0.21 \text{ (stat)} \pm 0.11 \text{ (syst)} \text{ GeV}$$

♦ Why precision?

- * Self-consistency test of SM at quantum level
(e.g.: Higgs loop corrections to W boson mass)
- * $M_H \leftrightarrow$ stability of the electroweak vacuum [Degrassi et al; Bednyakov et al]
- * Higgs mass uncertainty feeds back in uncertainty on Higgs observables
- * Test parameter relations in beyond-SM theories
⇒ indirect constraint of viable BSM parameter space!

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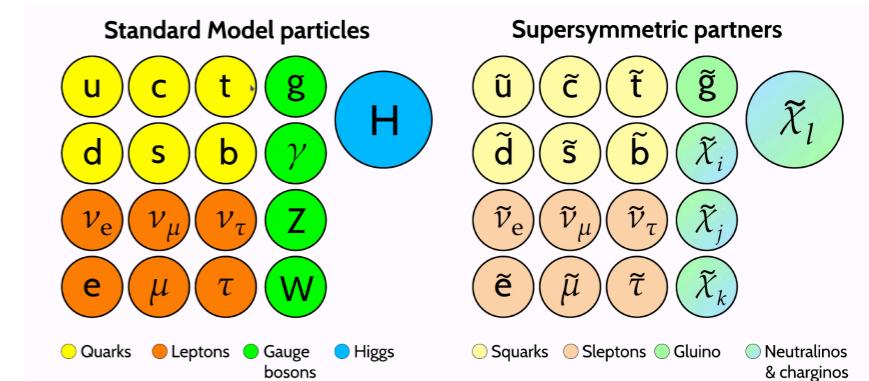
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⇒ indirect constraint of viable BSM parameter space!

Supersymmetry

♦ Supersymmetry:

- enlarged particle spectrum: each SM particle has SUSY partner
- enlarged Higgs sector: requires at least 2 complex Higgs doublets



♦ Minimal Supersymmetric extension (MSSM): 2 complex Higgs doublets

5 Higgs bosons: h, H, A, H^+, H^-

4 neutralinos: $\tilde{\chi}_i^0$ ($i = 1, \dots, 4$)

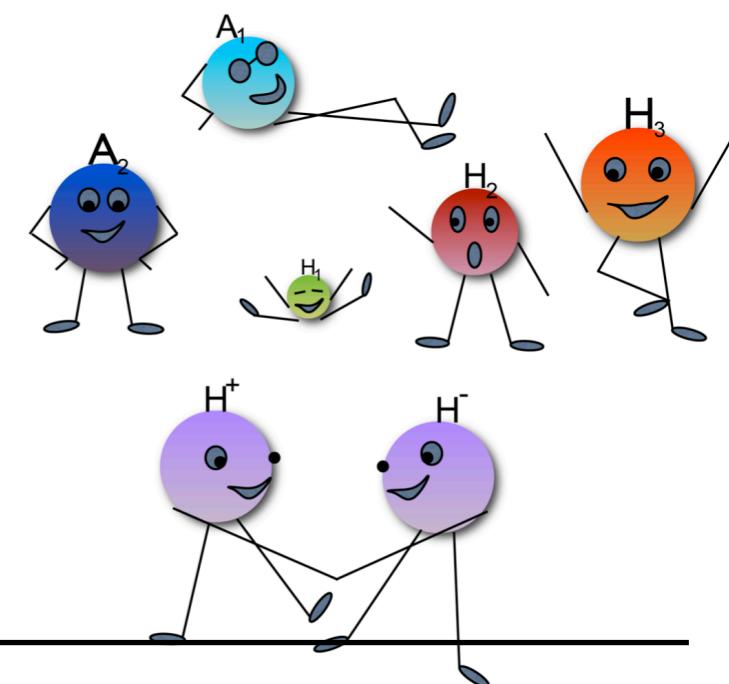
♦ Next-to-MSSM (NMSSM): 2 complex Higgs doublets plus complex singlet field

- enlarged Higgs and neutralino sector

7 Higgs bosons: $H_1, H_2, H_3, A_1, A_2, H^+, H^-$

5 neutralinos: $\tilde{\chi}_i^0$ ($i = 1, \dots, 5$)

- solves mu problem, interesting phenomenology



Higgs Mass in New Physics Extensions - Supersymmetry

Higgs boson mass:

- * SM: fundamental parameter, not predicted by the theory
- * Supersymmetry: calculable from input parameters;
quantum corrections Δm_H^2 are important!

$$\text{MSSM: } m_H^2 \approx M_Z^2 \cos^2 2\beta \quad + \Delta m_H^2 \leftarrow (85 \text{ GeV})^2 !$$

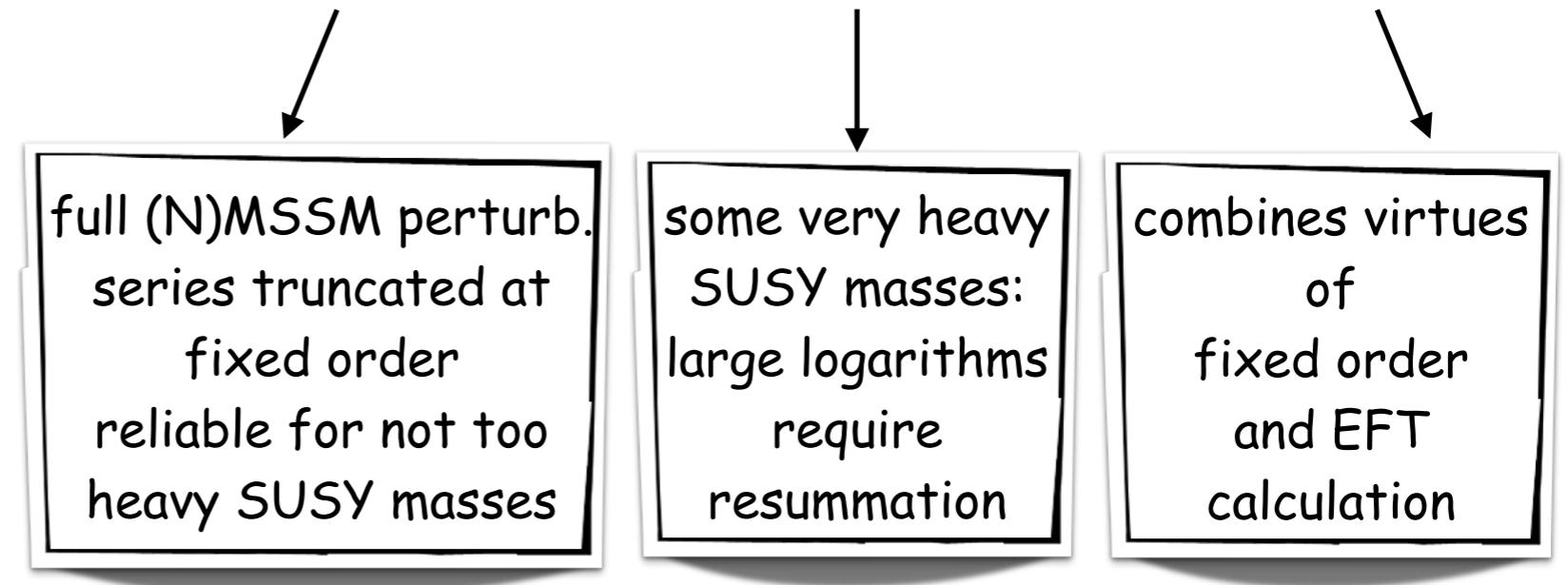
$$\text{NMSSM: } m_H^2 \approx M_Z^2 \cos^2 2\beta + \lambda^2 v^2 \sin^2 2\beta \quad + \Delta m_H^2 \leftarrow (55 \text{ GeV})^2$$

NMSSM:

- * less important loop corrections needed compared to the MSSM

Status Spectrum Calculations

❖ Methods for Higgs mass calculations: fixed-order (FO) - effective field theory (EFT) - hybrid



❖ Status MSSM spectrum calculations:

FO: up to 2-loop in on-shell (OS) and DR scheme, partial 3-loop in DR scheme

EFT: up to N^3LL

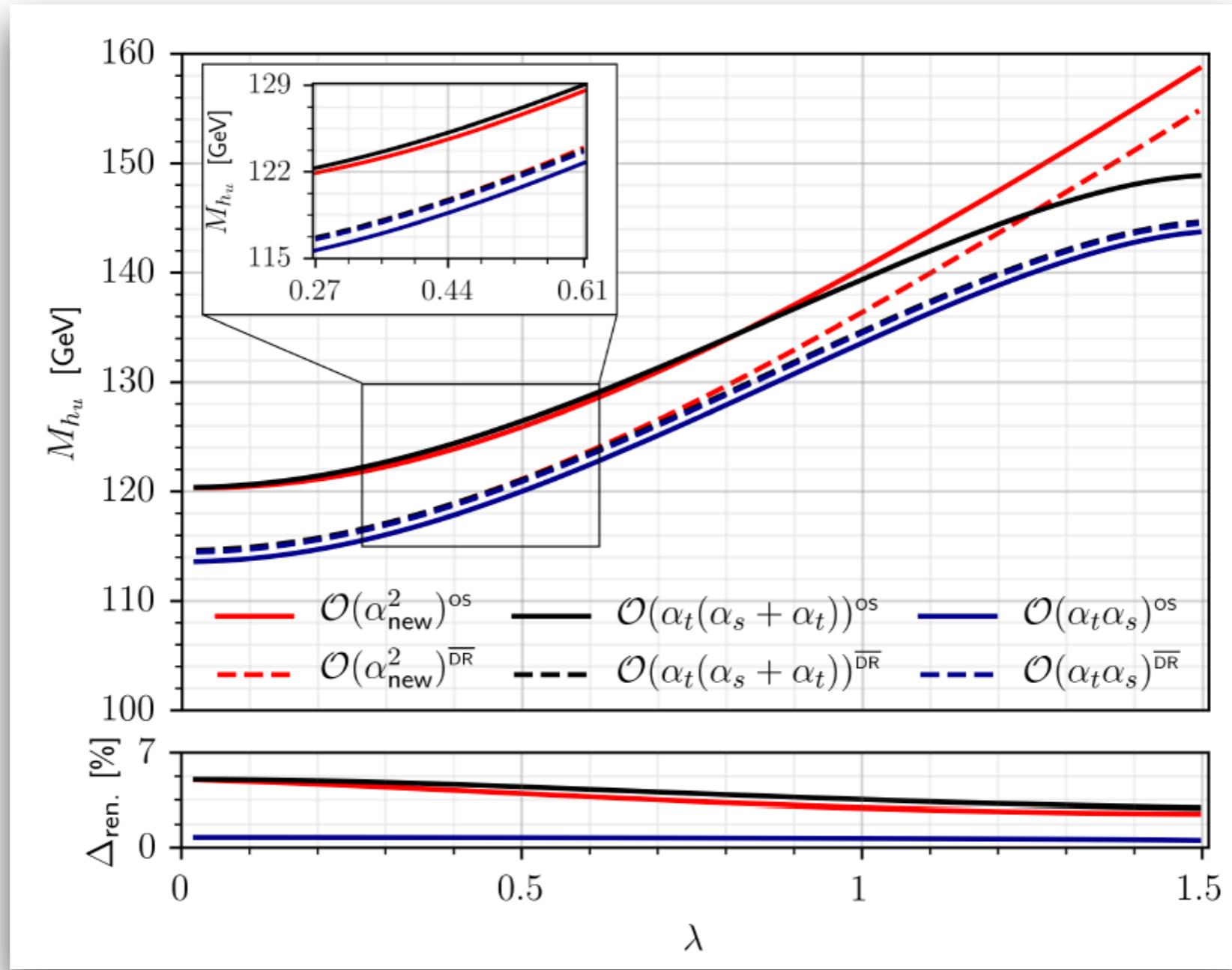
❖ Status NMSSM spectrum calculations:

up to 2-loop in mixed OS-DR scheme and in DR-scheme

$\mathcal{O}(\alpha_{\text{new}}^2) \approx \mathcal{O}((\alpha_\lambda + \alpha_\kappa + \alpha_t)^2)$ Mass Corrections in the CP-Violating NMSSM

Corrections to h_u -like Higgs (\triangleq SM-like Higgs)

[Dao, Gabelmann, MM, Rzehak, '21]



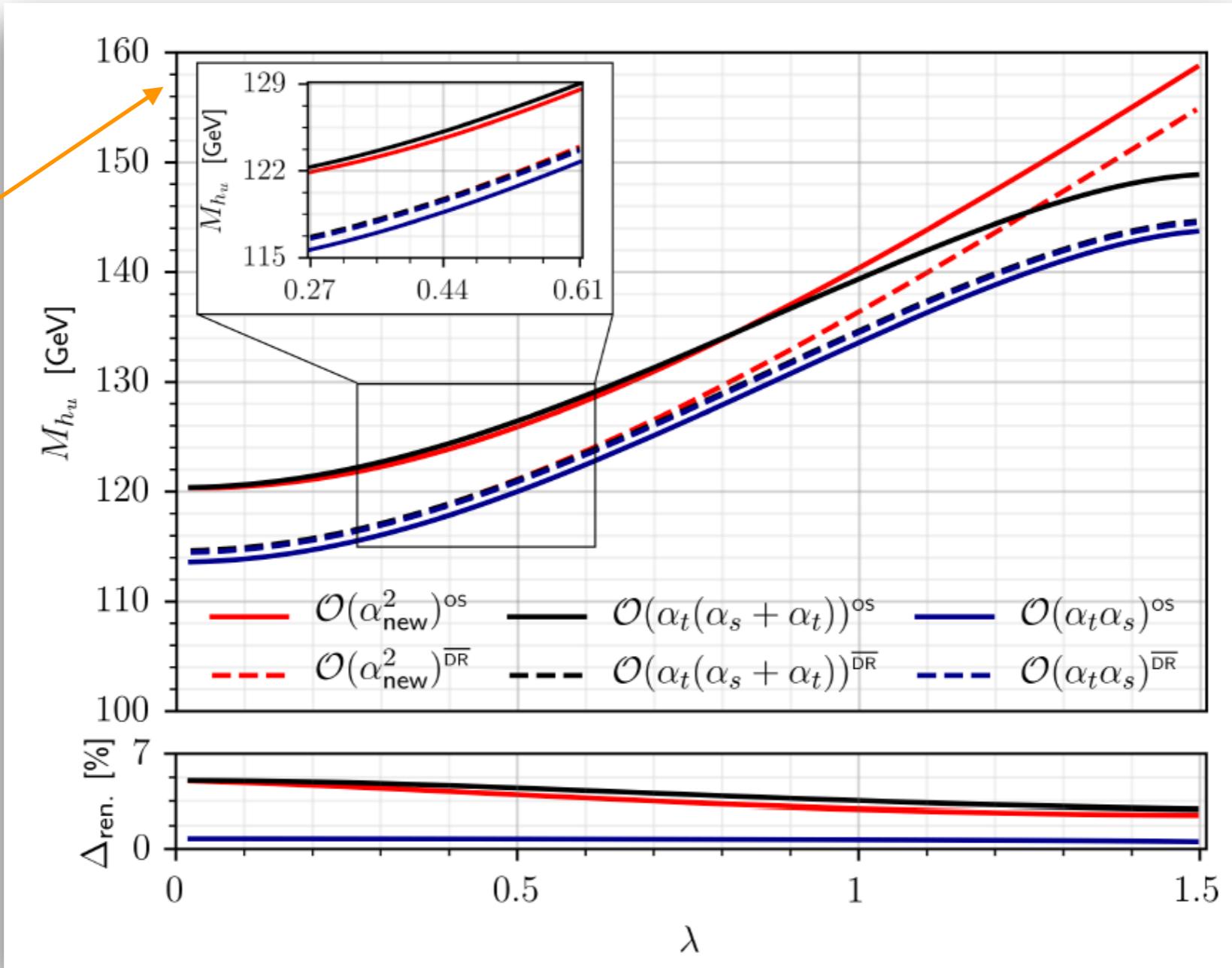
$$\Delta_{\text{ren.}} = \frac{|\lambda^{m_t(\overline{\text{DR}})} - \lambda^{m_t(\text{OS})}|}{\lambda^{m_t(\overline{\text{DR}})}} : \text{remaining theoretical error: } \mathcal{O}(\text{few}\%)$$

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Corrections to h_u -like Higgs (\triangleq SM-like Higgs)

[Dao, Gabelmann, MM, Rzehak, '21]

Zoomed:
compatible w/
HiggsSignals after
including the new
correction

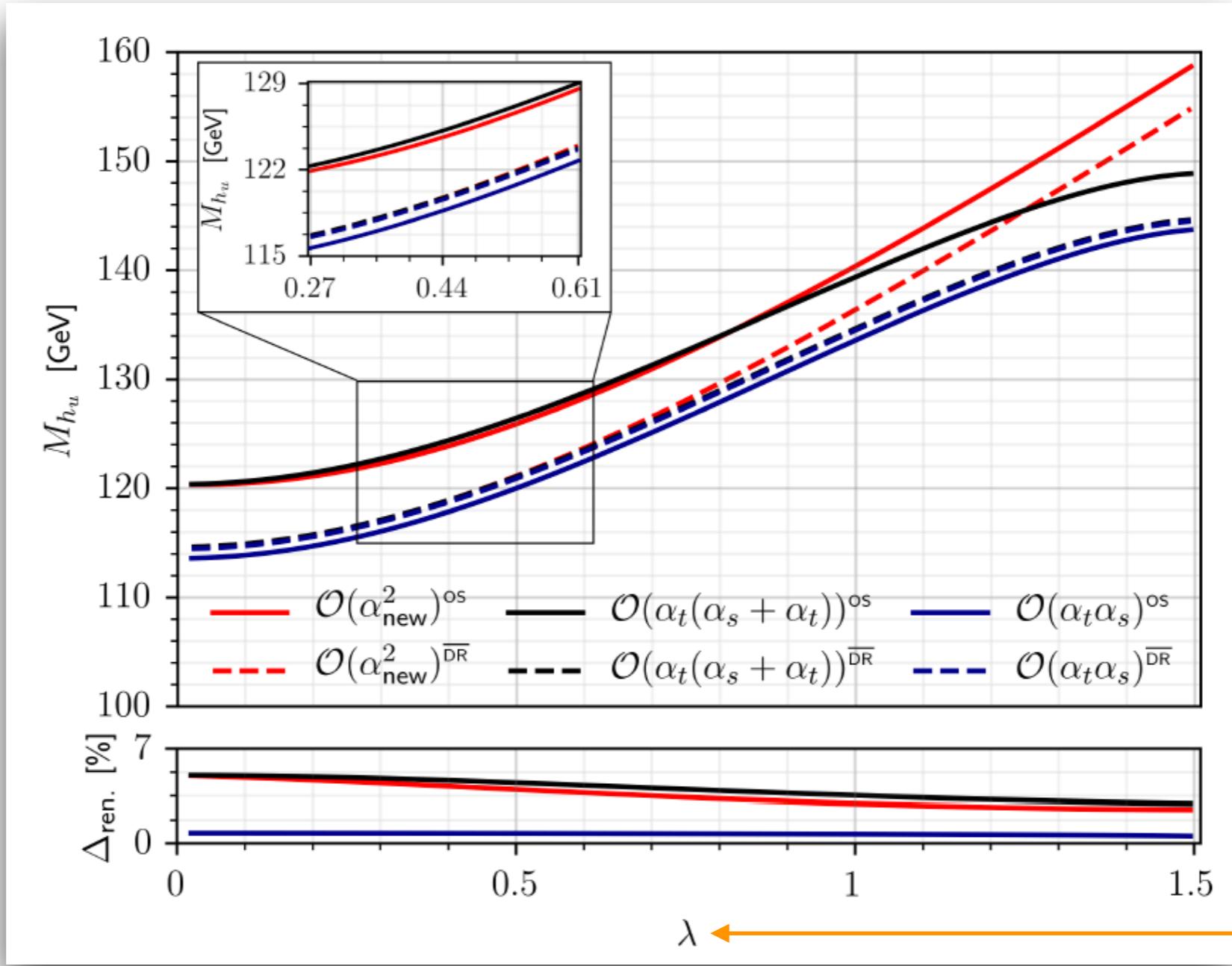


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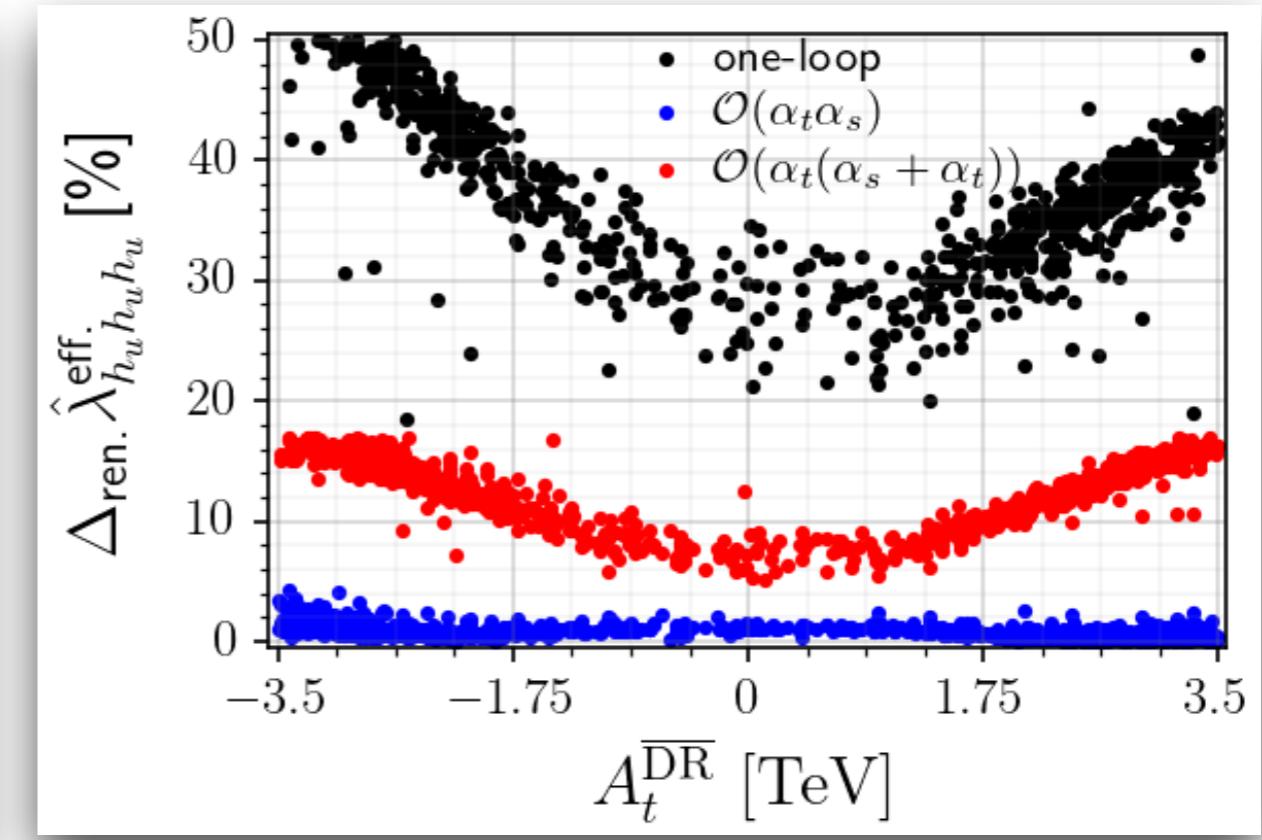
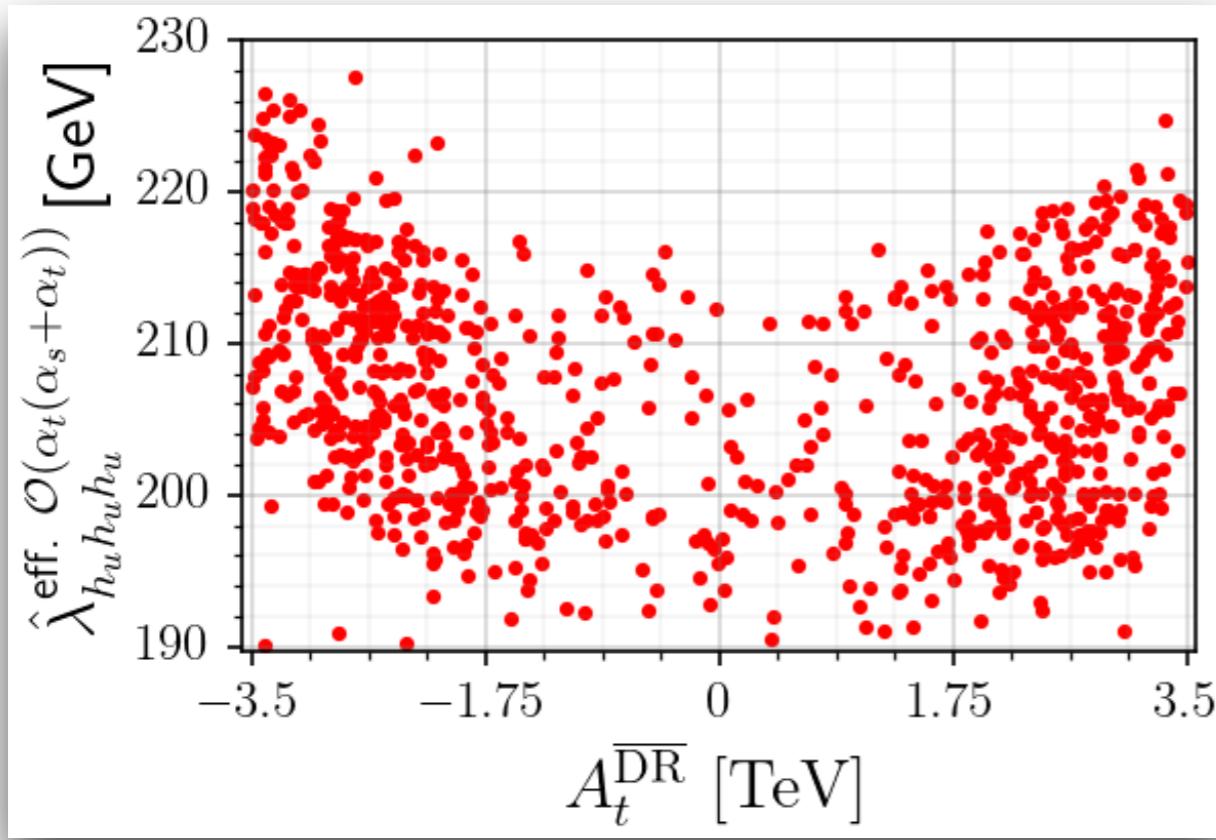
Loop Corrected Trilinear Higgs Self-Couplings at $\mathcal{O}(\alpha_t(\alpha_s + \alpha_t))$

- Masses $M_{ij} = (\partial^2 V_H / \Phi_i \Phi_j)|_{\Phi=0}$ and Higgs self-couplings $\lambda_{ijk} = (\partial^3 V_H / \Phi_i \Phi_j \Phi_k)|_{\Phi=0}$ related through Higgs potential V_H => catch up in precision w/ masses
- Very sensitive to physics beyond the SM (BSM)
important input for di-Higgs production
important input for Higgs-to-Higgs decays
important input for electroweak phase transitions
- Available in NMSSM:
full 1-loop [Dao,MM,Streicher,Walz,'13]
2-loop $\mathcal{O}(\alpha_t \alpha_s)$ [Dao,MM,Ziesche,'15]
2-loop $\mathcal{O}(\alpha_t(\alpha_t + \alpha_s))$ [Borschensky,Dao,Gabelmann,MM,Rzezhak,'22]

Loop Corrected Trilinear Higgs Self-Couplings at $\mathcal{O}(\alpha_t(\alpha_s + \alpha_t))$

Corrections to h_u -like Higgs (\triangleq SM-like Higgs)

[Borschensky, Dao, Gabelmann, MM, Rzehak '22]



$\hat{\lambda}_{abc}^{\text{eff}}$: renormalized loop-corrected Higgs self-coupling at vanishing external momentum

Theoretical uncertainty via renormalization scheme variation:

$$\Delta_{\text{ren}} = \frac{|\lambda^{m_t(\overline{\text{DR}})} - \lambda^{m_t(\text{OS})}|}{\lambda^{m_t(\overline{\text{DR}})}}$$

Results comply w/ SM value $\lambda_{HHH}^{\text{SM}} = \frac{3M_H^2}{v} = 191 \text{ GeV}$ within theoretical uncertainty



More on Precision:
BSM Decays

Status Standard Model Decays

[Taken from talk by M. Spira]

Partial Width	QCD	Electroweak	Total	on-shell Higgs
$H \rightarrow b\bar{b}/c\bar{c}$	~ 0.2%	~ 0.5%	~ 0.5%	NNNNLO / NLO
$H \rightarrow \tau^+\tau^-/\mu^+\mu^-$		~ 0.5%	~ 0.5%	NLO
$H \rightarrow gg$	~ 3%	~ 1%	~ 3%	NNNLO approx. / NLO
$H \rightarrow \gamma\gamma$	< 1%	< 1%	~ 1%	NLO / NLO
$H \rightarrow Z\gamma$	< 1%	~ 5%	~ 5%	(N)LO / LO
$H \rightarrow WW/ZZ \rightarrow 4f$	< 0.5%	~ 0.5%	~ 0.5%	(N)NLO

Impact of EW corrections on SM Higgs branching ratios $\Delta BR = \frac{BR^{QCD\&EW} - BR^{QCD}}{BR^{QCD}}$ [HDECAY]

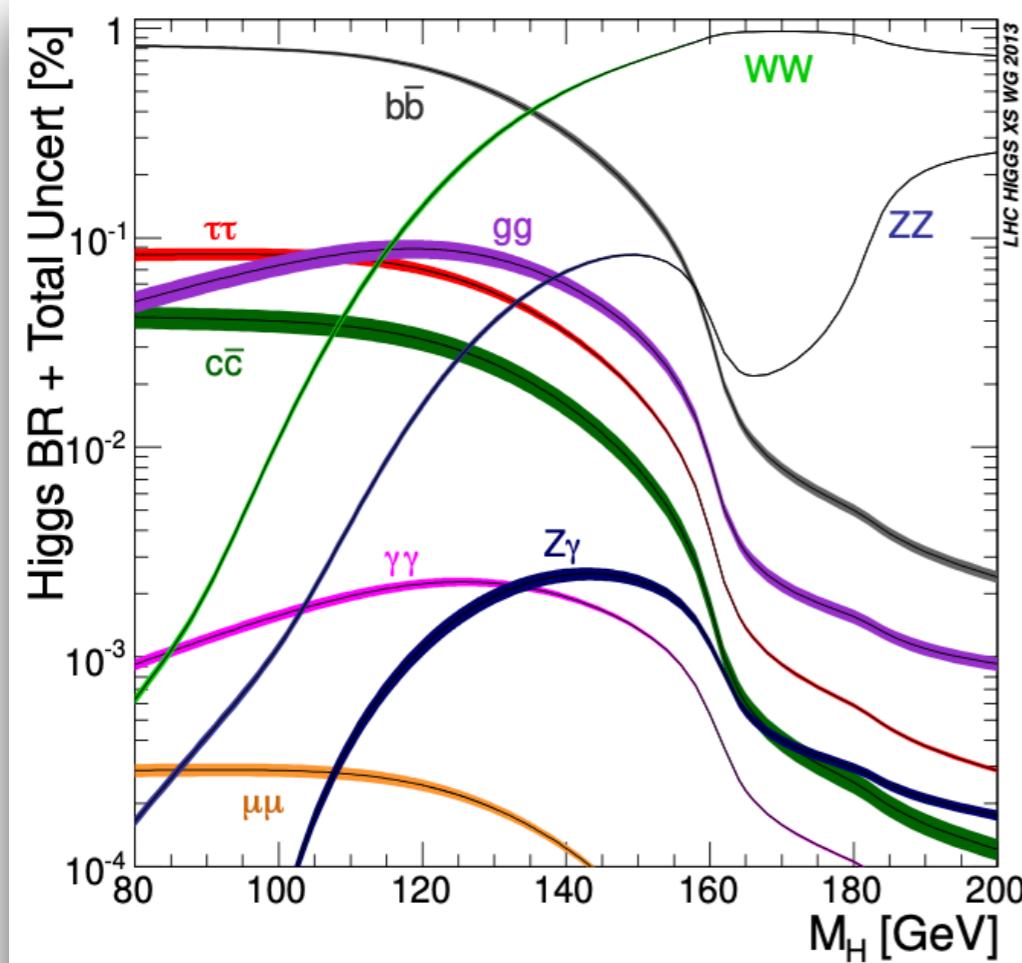
ΔBR	$b\bar{b}$	$\tau^+\tau^-$	$\mu^+\mu^-$	$s\bar{s}$	$c\bar{c}$	gg	$\gamma\gamma$	$Z\gamma$	W^+W^-	ZZ
	-1.76%	-1.59%	-3.52%	2.24%	-3.81%	4.34%	-2.29%	-0.71%	3.68%	1.61%

Standard Model Branching Ratios

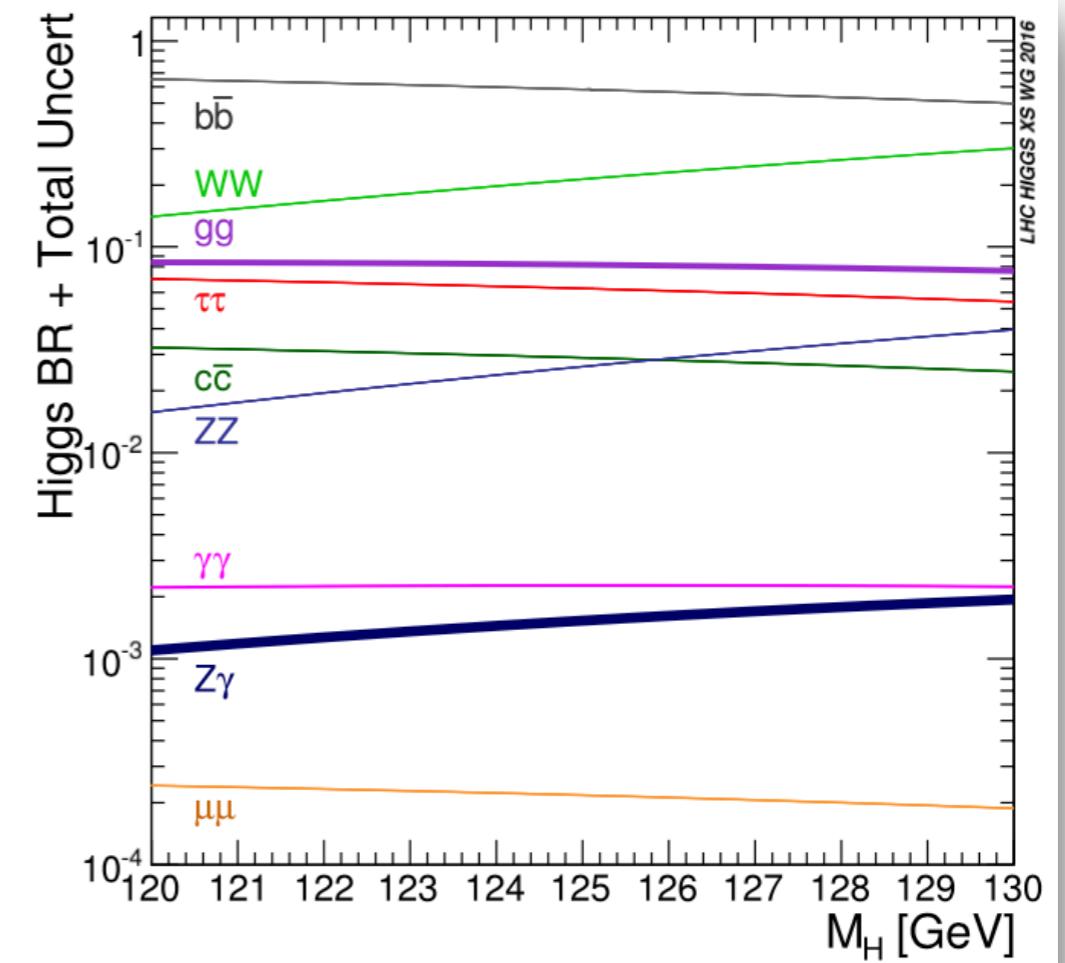
[HDECAY & Prophecy4f]

[Denner, Heinemeyer, Puljak, Rebuzzi, Spira]

YR3



YR4



- Total uncertainties: parametric & theory uncertainties added linearly
- Refinements of input parameters, full NLO EW corrs. to $H \rightarrow ff$, NLO quark-mass effects in $H \rightarrow gg$

Higher-Order Impact in Beyond-SM Theories (BSM)

Impact of EW corrections on SM Higgs branching ratios $\Delta BR = \frac{BR^{\text{QCD\&EW}} - BR^{\text{QCD}}}{BR^{\text{QCD}}}$ [HDECAY]

ΔBR	$b\bar{b}$	$\tau^+\tau^-$	$\mu^+\mu^-$	$s\bar{s}$	$c\bar{c}$	gg	$\gamma\gamma$	$Z\gamma$	W^+W^-	ZZ
	-1.76%	-1.59%	-3.52%	2.24%	-3.81%	4.34%	-2.29%	-0.71%	3.68%	1.61%

Example: Impact of EW corrections on branching ratios of SM-like 2HDM Higgs boson

Type	$\Delta BR_{h\bar{b}\bar{b}}^{S_1}$	$\Delta BR_{h\bar{b}\bar{b}}^{S_2}$	$\Delta BR_{h\bar{b}\bar{b}}^{S_3}$	$\Delta BR_{h\bar{b}\bar{b}}^{\text{OS2}}$	$\Delta BR_{h\bar{b}\bar{b}}^{\overline{\text{MS}}}$
I	$\lesssim 2.5\% (96\%)$	$\lesssim 5.0\% (98\%)$	$\lesssim 2.5\% (90\%)$	$\lesssim 2.5\% (94\%)$	$\lesssim 10.0\% (50\%)$
	$\lesssim 5.0\% (100\%)$	$\lesssim 7.5\% (99\%)$	$\lesssim 5.0\% (99\%)$	$\lesssim 5.0\% (99\%)$	$\gtrsim 100.0\% (12\%)$
II	$\lesssim 2.5\% (99\%)$	$\lesssim 2.5\% (54\%)$	$\lesssim 2.5\% (98\%)$	$\lesssim 2.5\% (81\%)$	$\lesssim 40.0\% (50\%)$
	$\lesssim 5.0\% (100\%)$	$\lesssim 7.5\% (96\%)$	$\lesssim 5.0\% (99\%)$	$\lesssim 5.0\% (99\%)$	$\gtrsim 100.0\% (36\%)$
LS	$\lesssim 2.5\% (96\%)$	$\lesssim 2.5\% (54\%)$	$\lesssim 2.5\% (75\%)$	$\lesssim 2.5\% (94\%)$	$\lesssim 17.5\% (50\%)$
	$\lesssim 5.0\% (99\%)$	$\lesssim 5.0\% (97\%)$	$\lesssim 5.0\% (99\%)$	$\lesssim 5.0\% (99\%)$	$\gtrsim 100.0\% (14\%)$
FL	$\lesssim 2.5\% (96\%)$	$\lesssim 2.5\% (54\%)$	$\lesssim 2.5\% (75\%)$	$\lesssim 2.5\% (94\%)$	$\lesssim 17.5\% (50\%)$
	$\lesssim 5.0\% (99\%)$	$\lesssim 5.0\% (97\%)$	$\lesssim 5.0\% (99\%)$	$\lesssim 5.0\% (99\%)$	$\gtrsim 100.0\% (12\%)$
Type	$\Delta BR_{h\gamma\gamma/hZZ}^{S_1}$	$\Delta BR_{h\gamma\gamma/hZZ}^{S_2}$	$\Delta BR_{h\gamma\gamma/hZZ}^{S_3}$	$\Delta BR_{h\gamma\gamma/hZZ}^{\text{OS2}}$	$\Delta BR_{h\gamma\gamma/hZZ}^{\overline{\text{MS}}}$
I	$\lesssim 5.0\% (97\%)$	$\lesssim 5.0\% (90\%)$	$\lesssim 5.0\% (90\%)$	$\lesssim 5.0\% (94\%)$	$\lesssim 20.0\% (50\%)$
	$\lesssim 7.5\% (99\%)$	$\lesssim 10.0\% (98\%)$	$\lesssim 7.5\% (99\%)$	$\lesssim 7.5\% (99\%)$	$\gtrsim 100.0\% (21\%)$
II	$\lesssim 5.0\% (99\%)$	$\lesssim 5.0\% (60\%)$	$\lesssim 2.5\% (96\%)$	$\lesssim 5.0\% (82\%)$	$\lesssim 62.0\% (50\%)$
	$\lesssim 7.5\% (99\%)$	$\lesssim 12.5\% (96\%)$	$\lesssim 5.0\% (99\%)$	$\lesssim 7.5\% (97\%)$	$\gtrsim 100.0\% (47\%)$
LS	$\lesssim 5.0\% (97\%)$	$\lesssim 5.0\% (75\%)$	$\lesssim 2.5\% (88\%)$	$\lesssim 5.0\% (95\%)$	$\lesssim 12.5\% (50\%)$
	$\lesssim 7.5\% (99\%)$	$\lesssim 10.0\% (99\%)$	$\lesssim 5.0\% (99\%)$	$\lesssim 7.5\% (99\%)$	$\gtrsim 100.0\% (13\%)$
FL	$\lesssim 5.0\% (97\%)$	$\lesssim 5.0\% (75\%)$	$\lesssim 2.5\% (88\%)$	$\lesssim 5.0\% (95\%)$	$\lesssim 15.0\% (50\%)$
	$\lesssim 7.5\% (99\%)$	$\lesssim 10.0\% (99\%)$	$\lesssim 5.0\% (99\%)$	$\lesssim 7.5\% (99\%)$	$\gtrsim 100.0\% (11\%)$
Type	$\Delta BR_{h\tau^+\tau^-}^{S_1}$	$\Delta BR_{h\tau^+\tau^-}^{S_2}$	$\Delta BR_{h\tau^+\tau^-}^{S_3}$	$\Delta BR_{h\tau^+\tau^-}^{\text{OS2}}$	$\Delta BR_{h\tau^+\tau^-}^{\overline{\text{MS}}}$
I	$\lesssim 2.5\% (98\%)$	$\lesssim 2.5\% (88\%)$	$\lesssim 2.5\% (97\%)$	$\lesssim 2.5\% (98\%)$	$\lesssim 7.5\% (50\%)$
	$\lesssim 5.0\% (99\%)$	$\lesssim 5.0\% (99\%)$	$\lesssim 5.0\% (99\%)$	$\lesssim 5.0\% (99\%)$	$\gtrsim 100.0\% (12\%)$

[Krause,MM,'19]

Higher-Order Impact in Beyond-SM Theories (BSM)

Impact of EW corrections on SM Higgs branching ratios $\Delta BR = \frac{BR^{\text{QCD&EW}} - BR^{\text{QCD}}}{BR^{\text{QCD}}}$ [HDECAY]

ΔBR	$b\bar{b}$	$\tau^+\tau^-$	$\mu^+\mu^-$	$s\bar{s}$	$c\bar{c}$	gg	$\gamma\gamma$	$Z\gamma$	W^+W^-	ZZ
	-1.76%	-1.59%	-3.52%	2.24%	-3.81%	4.34%	-2.29%	-0.71%	3.68%	1.61%

Example: Impact of EW corrections on branching ratios of non-SM-like 2HDM Higgs boson

Type	$\Delta BR_{H\tau^+\tau^-}^{S_1}$	$\Delta BR_{H\tau^+\tau^-}^{S_2}$	$\Delta BR_{H\tau^+\tau^-}^{S_3}$	$\Delta BR_{H\tau^+\tau^-}^{S_4}$	$\Delta BR_{H\tau^+\tau^-}^{\overline{\text{MS}}}$
I	$\lesssim 15.0\% (49\%)$	$\lesssim 15.0\% (51\%)$	$\lesssim 15.0\% (48\%)$	$\lesssim 15.0\% (55\%)$	$\lesssim 60.0\% (50\%)$
	$\lesssim 35.0\% (88\%)$	$\lesssim 35.0\% (88\%)$	$\lesssim 35.0\% (77\%)$	$\lesssim 35.0\% (88\%)$	$\gtrsim 100.0\% (40\%)$
II	$\lesssim 15.0\% (54\%)$	$\lesssim 20.0\% (53\%)$	$\lesssim 10.0\% (51\%)$	$\lesssim 25.0\% (47\%)$	$\lesssim 85.0\% (14\%)$
	$\lesssim 25.0\% (91\%)$	$\lesssim 30.0\% (90\%)$	$\lesssim 35.0\% (90\%)$	$\lesssim 40.0\% (86\%)$	$\gtrsim 100.0\% (84\%)$
LS	$\lesssim 15.0\% (54\%)$	$\lesssim 17.5\% (48\%)$	$\lesssim 7.5\% (46\%)$	$\lesssim 25.0\% (46\%)$	$\lesssim 77.5\% (15\%)$
	$\lesssim 27.5\% (90\%)$	$\lesssim 30.0\% (88\%)$	$\lesssim 30.0\% (88\%)$	$\lesssim 40.0\% (85\%)$	$\gtrsim 100.0\% (81\%)$
FL	$\lesssim 15.0\% (55\%)$	$\lesssim 17.5\% (48\%)$	$\lesssim 7.5\% (46\%)$	$\lesssim 25.0\% (46\%)$	$\lesssim 77.5\% (15\%)$
	$\lesssim 27.5\% (90\%)$	$\lesssim 30.0\% (88\%)$	$\lesssim 30.0\% (88\%)$	$\lesssim 40.0\% (85\%)$	$\gtrsim 100.0\% (81\%)$

[Krause,MM,'19]

Type	$\Delta BR_{HZA}^{S_1}$	$\Delta BR_{HZA}^{S_2}$	$\Delta BR_{HZA}^{S_3}$	$\Delta BR_{HZA}^{S_4}$	$\Delta BR_{HZA}^{\overline{\text{MS}}}$
I	$\lesssim 5.0\% (51\%)$	$\lesssim 5.0\% (51\%)$	$\lesssim 10.0\% (46\%)$	$\lesssim 10.0\% (53\%)$	$\lesssim 80.0\% (26\%)$
	$\lesssim 15.0\% (80\%)$	$\lesssim 15.0\% (80\%)$	$\lesssim 30.0\% (80\%)$	$\lesssim 22.5\% (83\%)$	$\gtrsim 100.0\% (52\%)$
II	$\lesssim 5.0\% (68\%)$	$\lesssim 5.0\% (69\%)$	$\lesssim 10.0\% (50\%)$	$\lesssim 7.5\% (73\%)$	$\lesssim 85.0\% (20\%)$
	$\lesssim 10.0\% (91\%)$	$\lesssim 12.5\% (94\%)$	$\lesssim 25.0\% (81\%)$	$\lesssim 10.0\% (90\%)$	$\gtrsim 100.0\% (56\%)$
LS	$\lesssim 5.0\% (65\%)$	$\lesssim 5.0\% (65\%)$	$\lesssim 10.0\% (48\%)$	$\lesssim 7.5\% (41\%)$	$\lesssim 85.0\% (29\%)$
	$\lesssim 10.0\% (86\%)$	$\lesssim 10.0\% (86\%)$	$\lesssim 27.5\% (80\%)$	$\lesssim 15.0\% (90\%)$	$\gtrsim 100.0\% (44\%)$
FL	$\lesssim 5.0\% (65\%)$	$\lesssim 5.0\% (63\%)$	$\lesssim 10.0\% (53\%)$	$\lesssim 7.5\% (51\%)$	$\lesssim 82.5\% (20\%)$
	$\lesssim 10.0\% (88\%)$	$\lesssim 10.0\% (88\%)$	$\lesssim 15.0\% (83\%)$	$\lesssim 10.0\% (84\%)$	$\gtrsim 100.0\% (30\%)$

Type	$\Delta BR_{HW^\pm H^\mp}^{S_1}$	$\Delta BR_{HW^\pm H^\mp}^{S_2}$	$\Delta BR_{HW^\pm H^\mp}^{S_3}$	$\Delta BR_{HW^\pm H^\mp}^{S_4}$	$\Delta BR_{HW^\pm H^\mp}^{\overline{\text{MS}}}$
I	$\lesssim 5.0\% (56\%)$	$\lesssim 5.0\% (55\%)$	$\lesssim 10.0\% (49\%)$	$\lesssim 10.0\% (57\%)$	$\lesssim 70.0\% (25\%)$

IV. Summary and Outlook (21/23)

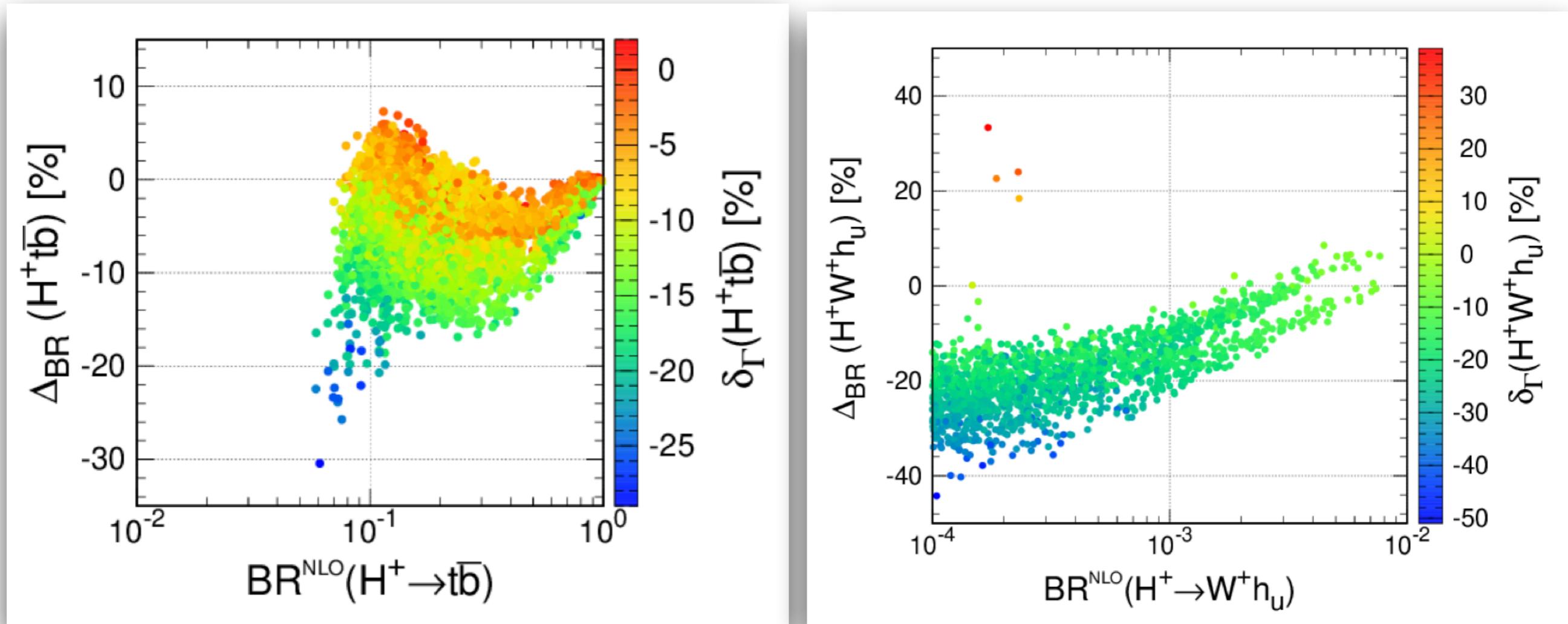
SUSY-EW & SUSY-QCD Corrected Charged Higgs Decays

Scan points compatible w/ Higgs data

[HiggsSignals,HiggsBounds]

[Dao,Fritz,Krause,MM,Patel,'19]

[Dao,MM,Patel,Sakurai,'21]



- Corrections to charged Higgs decays:
 Δ_{BR} : NLO impact on branching ratio, δ_T : NLO impact on partial width
- Implemented in NMSSMCALCEW [Dao,Baglio,MM,Patel,Sakurai]

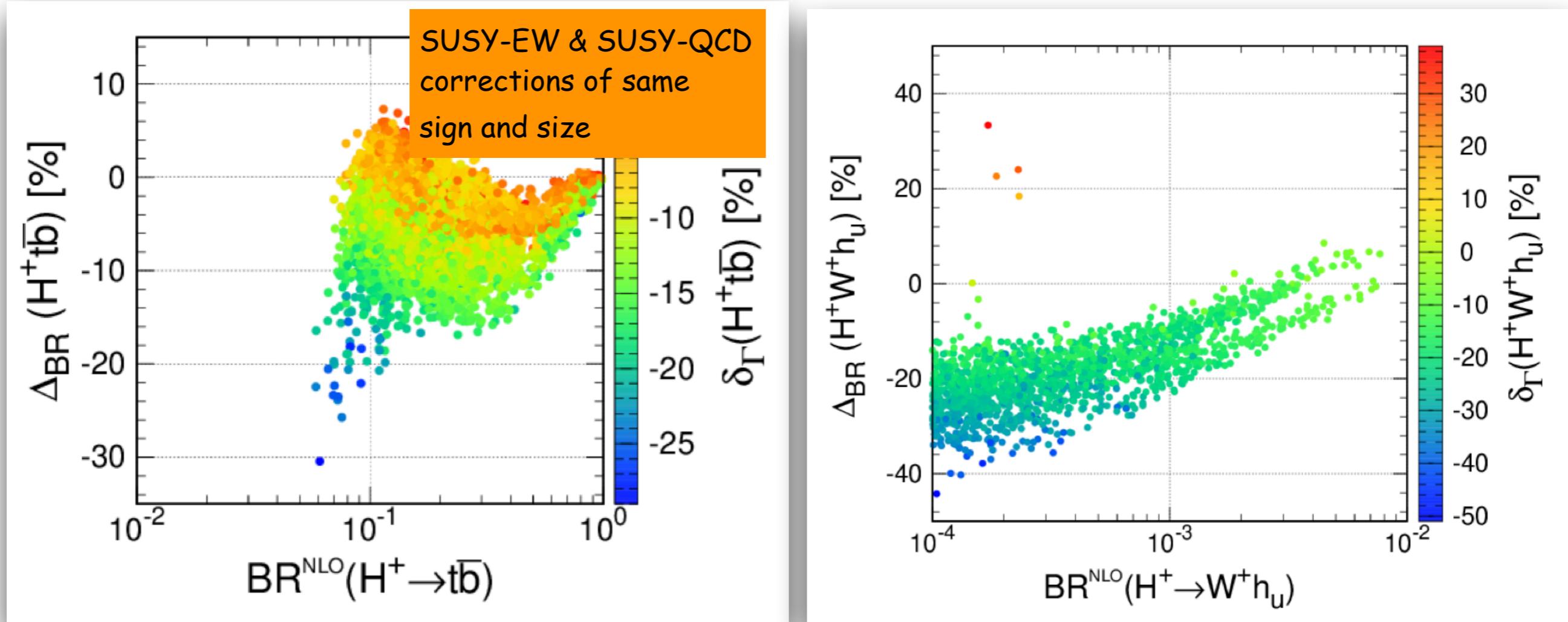
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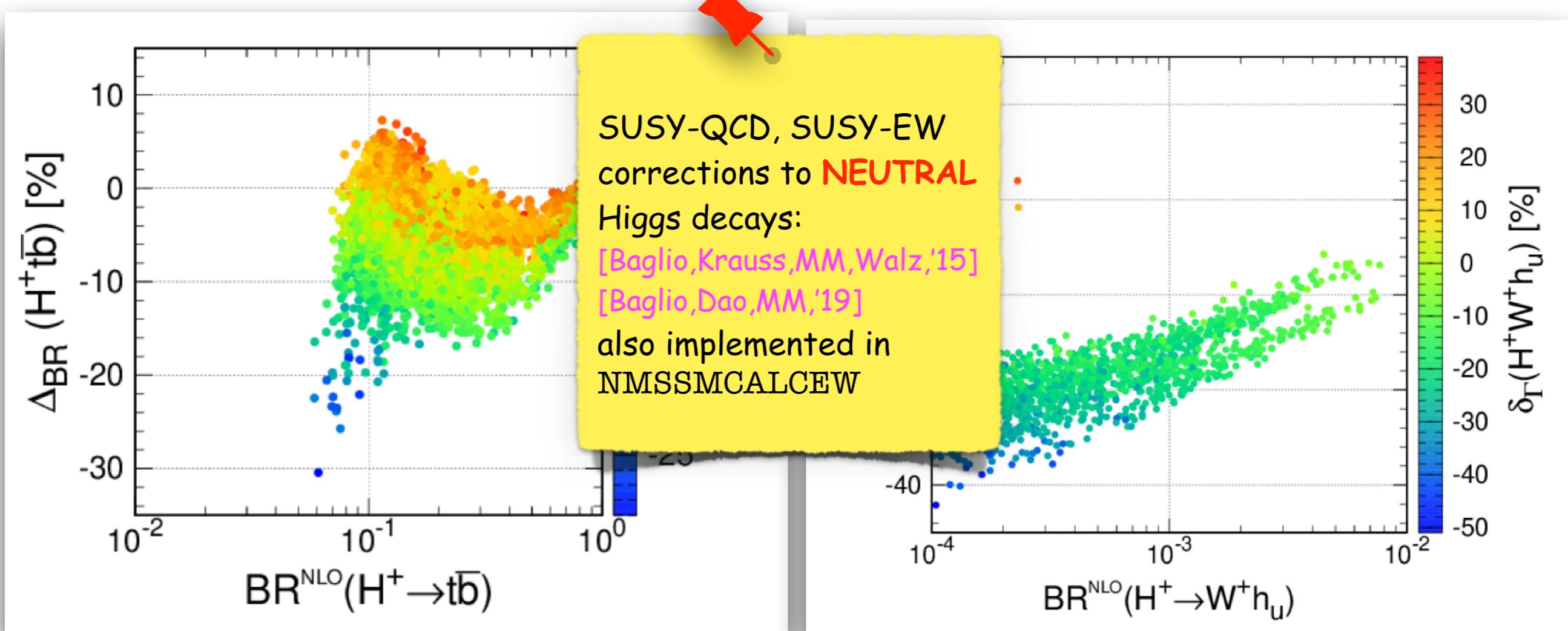
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- Corrections to charged Higgs decays:
 Δ_{BR} : NLO impact on branching ratio, δ_{Γ} : NLO impact on partial width
- Implemented in NMSSMCALCEW [Dao, Baglio, MM, Patel, Sakurai]

HH Production
Precision



Ultimate Test of the Higgs Mechanism

$$V(H) = \frac{1}{2} M_H^2 H^2 + \frac{M_H^2}{2v} H^3 + \frac{M_H^2}{8v^2} H^4$$

Higgs mass : $M_H = \sqrt{2\lambda} v$

trilinear Higg self-coupling : $\lambda_{HHH} = 3M_H^2/M_Z^2$

quadrilinear Higgs self-coupling : $\lambda_{HHHH} = 3M_H^2/M_Z^4$

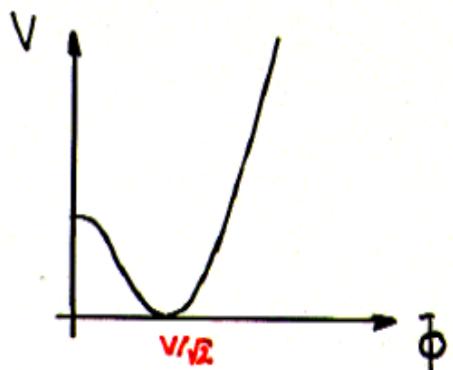
(units $\lambda_0 = 33.8 \text{ GeV}/\lambda_0^2$)



$$V(\Phi) = \lambda(\Phi^\dagger \Phi - \frac{v^2}{2})^2$$

$v = 246 \text{ GeV}$

$$\Phi = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v+H \end{pmatrix} \sim$$



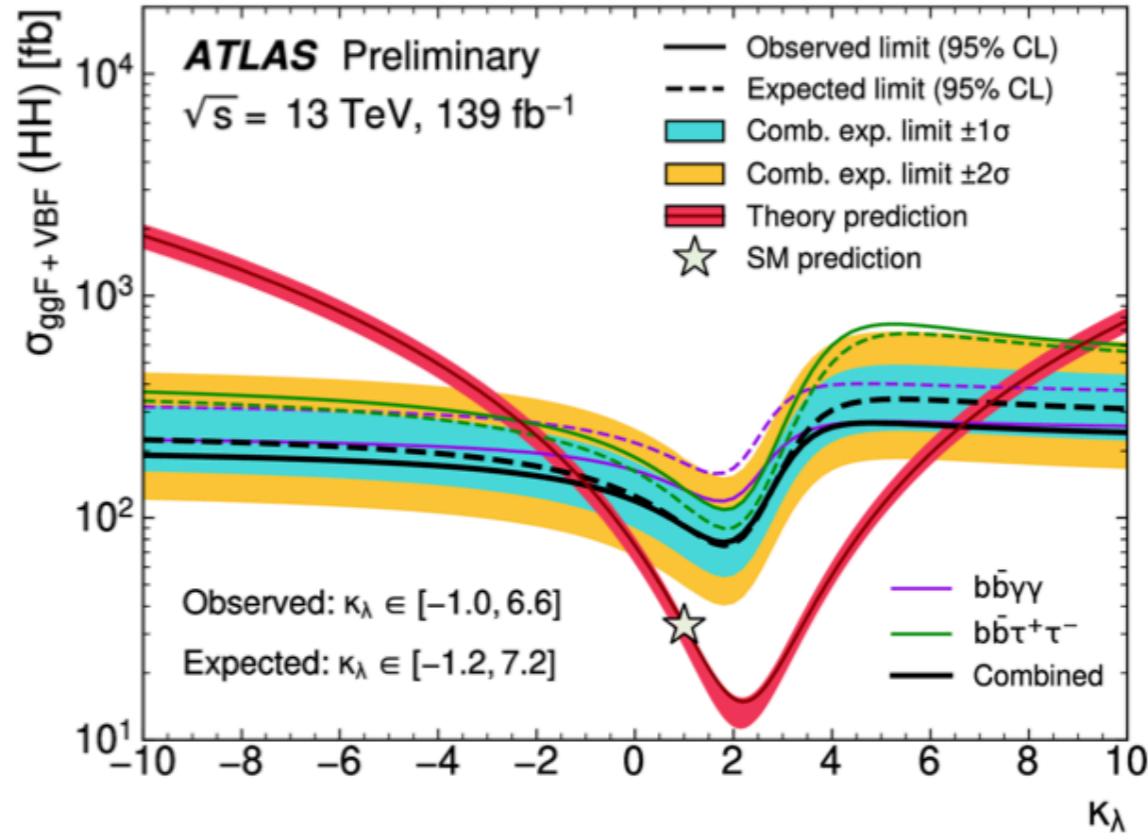
Slides from LCWS, Fermilab, 10/2000
[Djouadi, Kilian, MM, Zerwas, 03/99, 04/99]

(a) trilinear coupling : via Higgs pair production

(b) quadrilinear coupling : via triple Higgs production

measurement of the Higgs self-couplings
and
reconstruction of the Higgs potential } \Rightarrow establish the scalar
sector of the Higgs mechanism
experimentally

Experimental Results - Limits on Trilinear Higgs Self-Coupling



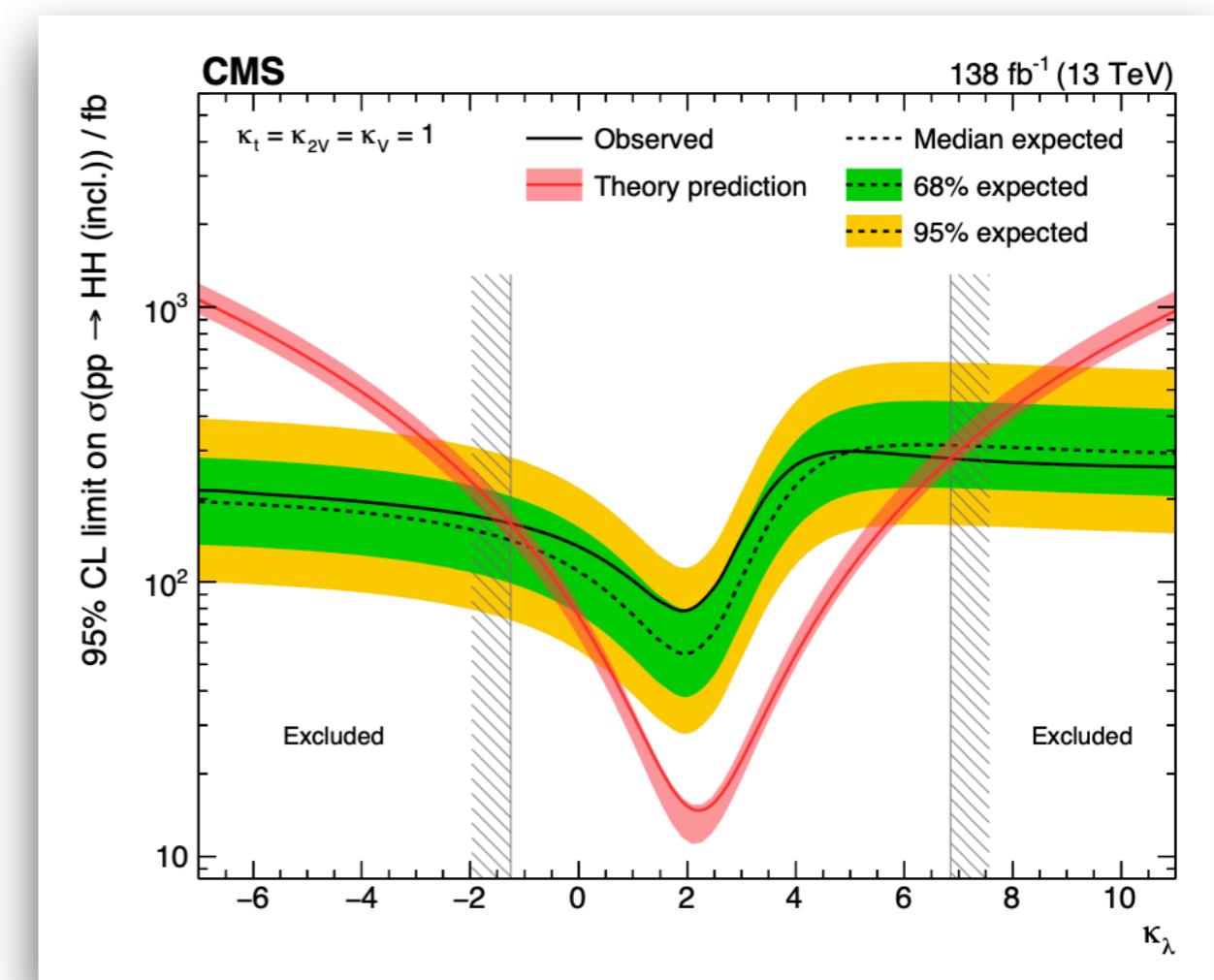
$$-1.24 \leq \kappa_\lambda \leq 6.49$$

[Rui Zhang, ATLAS, HH Workshop' 22]

Observed: $\kappa_\lambda \in [-1.0, 6.6]$

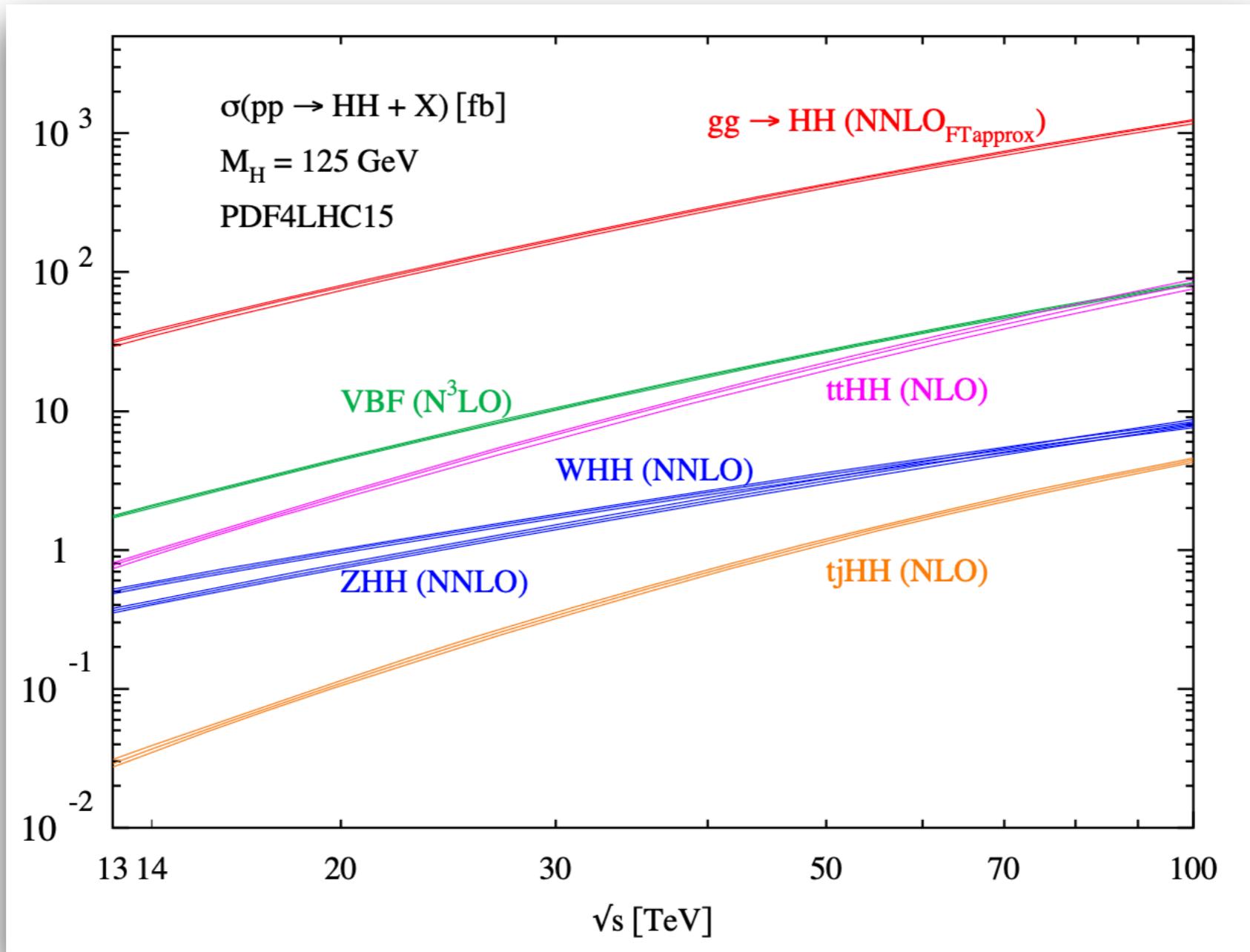
Expected: $\kappa_\lambda \in [-1.2, 7.2]$

[CMS, 2207.00043]



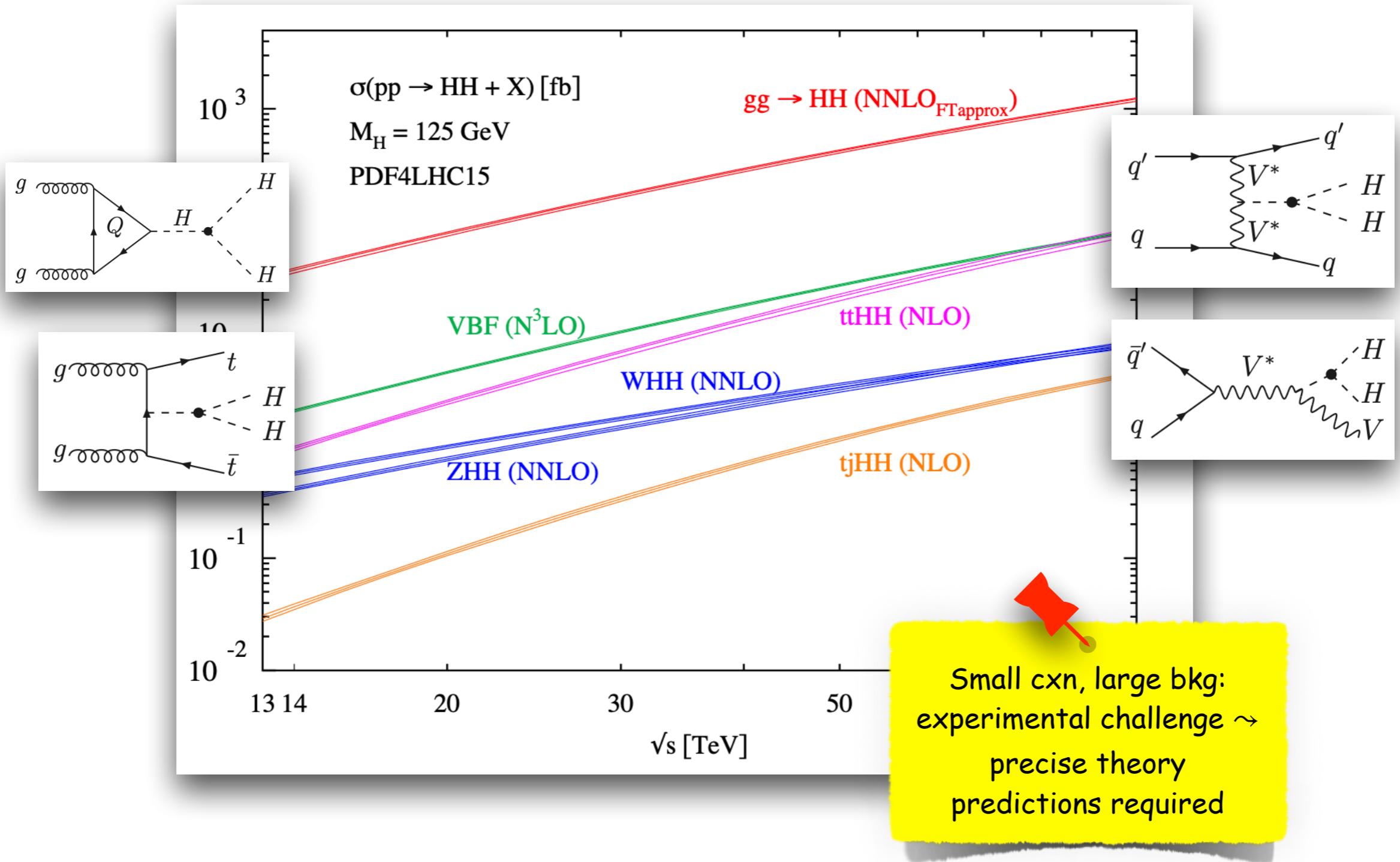
Double Higgs Production Processes

[HH, White paper]



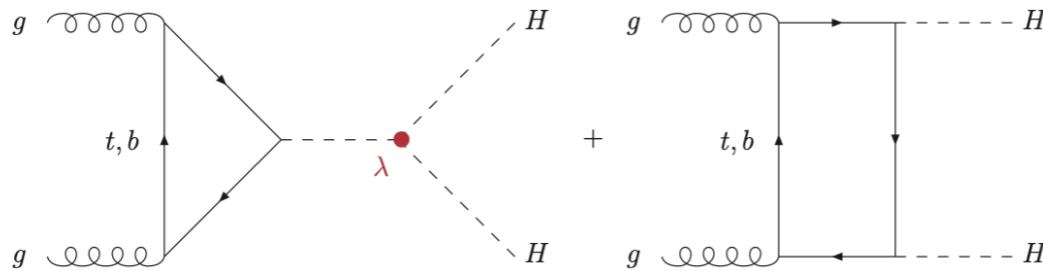
Double Higgs Production Processes

[HH, White paper]

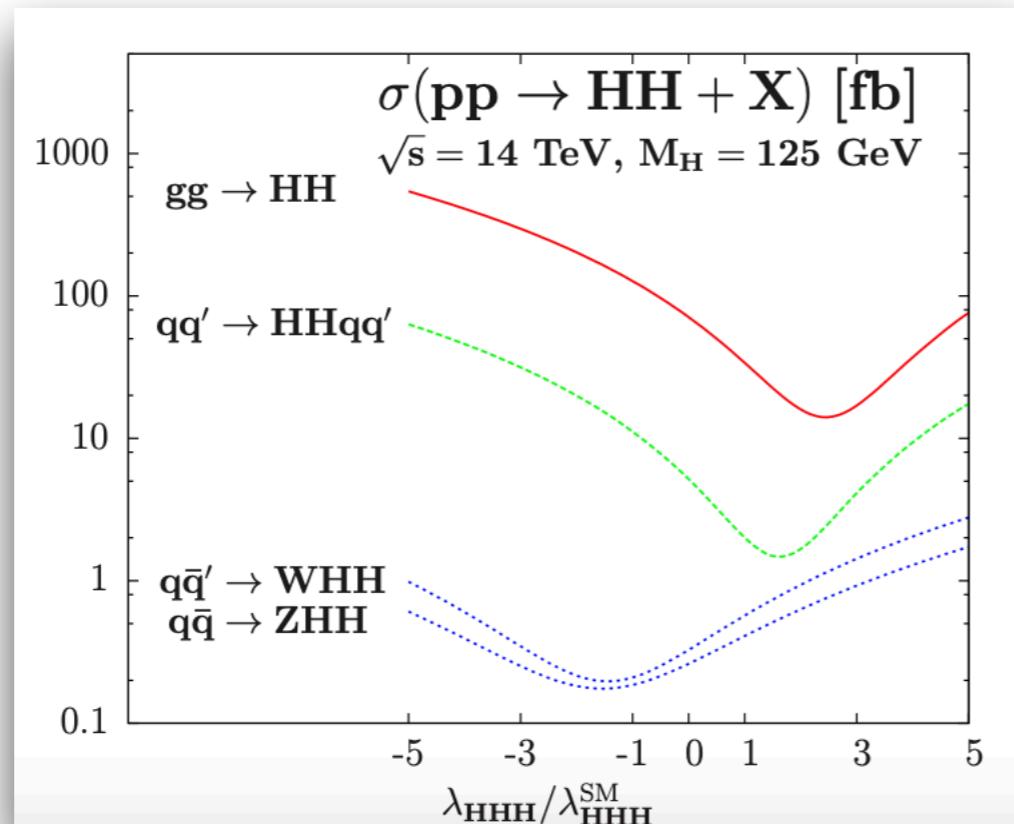


Higgs Pair Production through Gluon Fusion

- ♦ Loop mediated at leading order - SM: third generation dominant



- ♦ Threshold region sensitive to λ ; large M_{HH} : sensitive to c_{tt}/c_{bb} [e.g. boosted Higgs pairs]



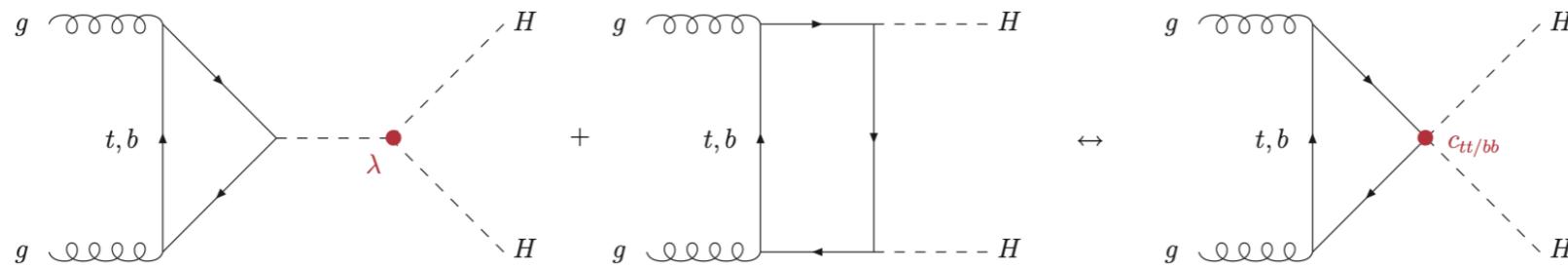
[Baglio,Djouadi,Gröber,MM,Quévillon,Spira]

$$gg \rightarrow HH : \frac{\Delta\sigma}{\sigma} \sim -\frac{\Delta\lambda}{\lambda}$$

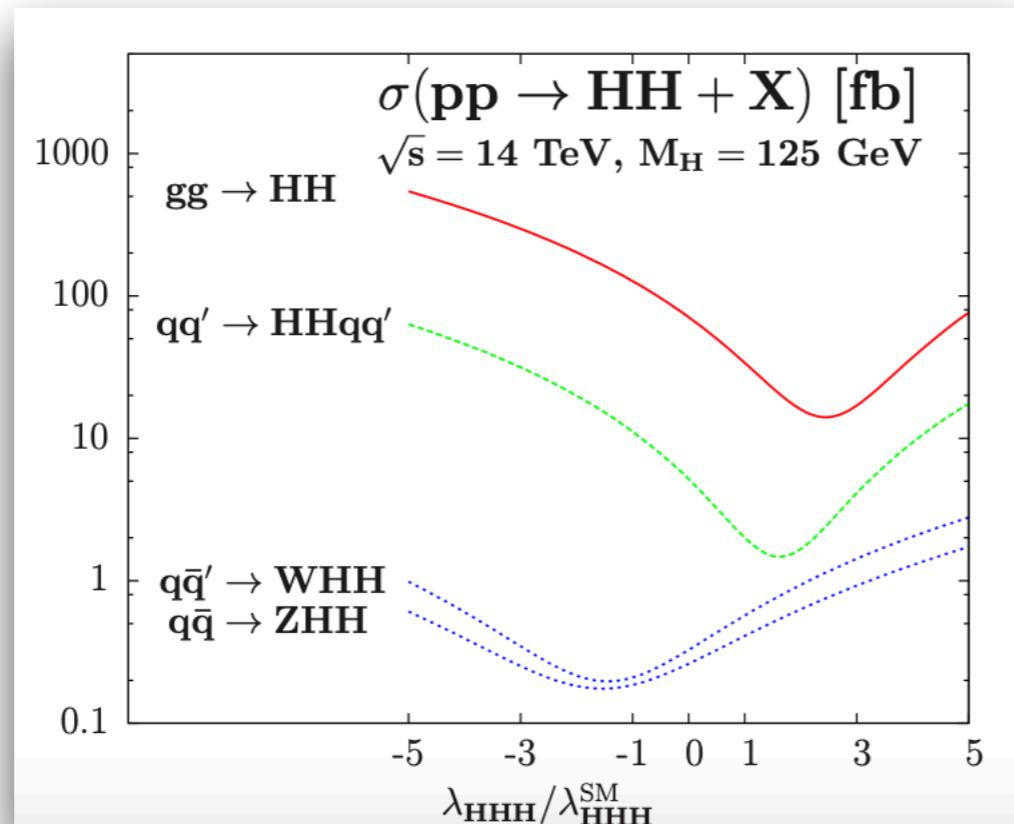
decreasing with M_{HH}

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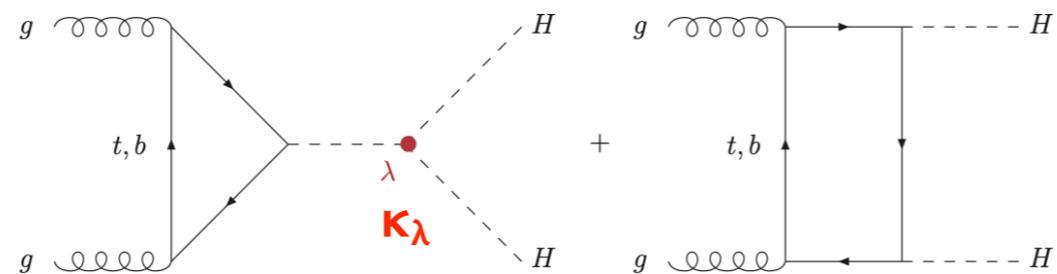
decreasing with M_{HH}

Higher-Order QCD Corrections to Higgs Pair Production

- ♦ 2-loop QCD corrections: $\lesssim 70\%$ [HTL, $\mu=M_{HH}/2$] [Dawson,Dittmaier,Spira]
- ♦ 2-loop QCD corrections: $\sigma = \sigma_0 + \sigma_1/m_t^2 + \dots + \sigma_4/m_t^8$
[refinement: full LO at differential level] [Grigo,Hoff,Melnikov,Steinhauser]
- ♦ Mass effects @ NLO in real corrections: $\sim -10\%$
[Frederix,Frixione,Hirschi,Maltoni,Mattelaer,Torrielli,Vryonidou,Zaro]
- ♦ NNLO QCD corrections: $\sim 20\%$ [HTL] [de Florian,Mazzitelli; Grigo,Melnikov,Steinhauser]
- ♦ N³LO QCD corrections: $\sim 5\%$ [HTL] [Chen,Li,Shao,Wang]
- ♦ NNLO Monte Carlo: inclusion of full top-mass effects @ NLO [partly at NNLO]
[Grazzini,Heinrich,Jones,Kallweit,Kerner,Lindert,Mazzitelli]
- ♦ NLO: matching to parton showers [Heinrich,Jones,Kerner,Luisoni,Vryonidou]
- ♦ New expansion/extrapolation methods:
 - (i) $1/m_t^2$ expansion + conformal mapping + Padé approximants [Gröber,Maier,Rauh]
 - (ii) p_T^2 expansion [Bonciani,Degassi,Giardino,Gröber]
- ♦ NLO: small mass expansion [$Q^2 \gg m_t^2$] [Davies,Mishima,Steinhauser,Wellmann]
- ♦ Combination of full NLO and small mass expansion [Davies,Heinrich,Jones,Kerner,Mishima,Steinhauser,Wellmann]

Higher-Order QCD, EW Corrections to Higgs Pair Production

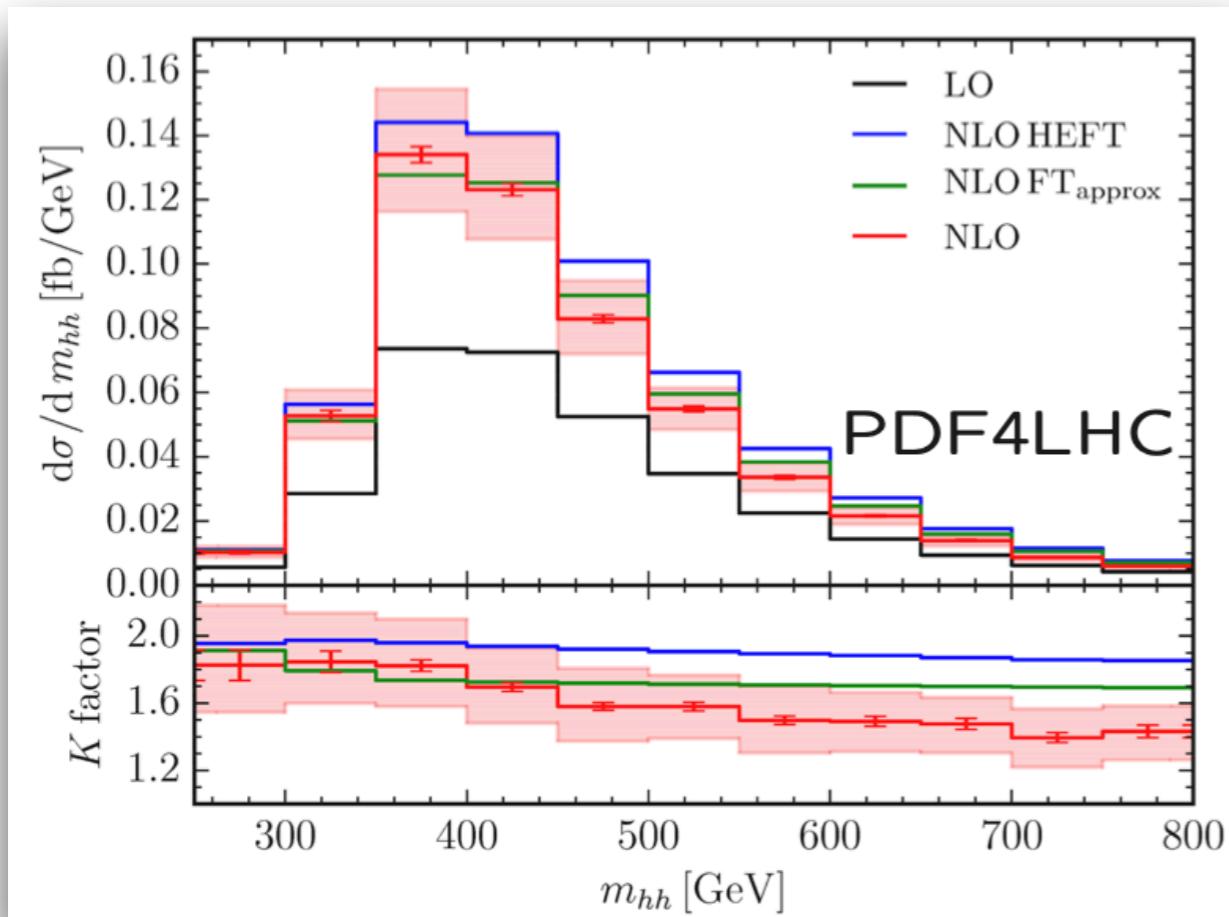
- Complete list, see e.g. twiki of LHC Higgs Working Subgroup HH and recent reviews
 - > recommendations for cross sections to be used given for
 - different c.m. energies
 - different coupling modifiers κ_λ
 - > uncertainties on di-Higgs cross sections



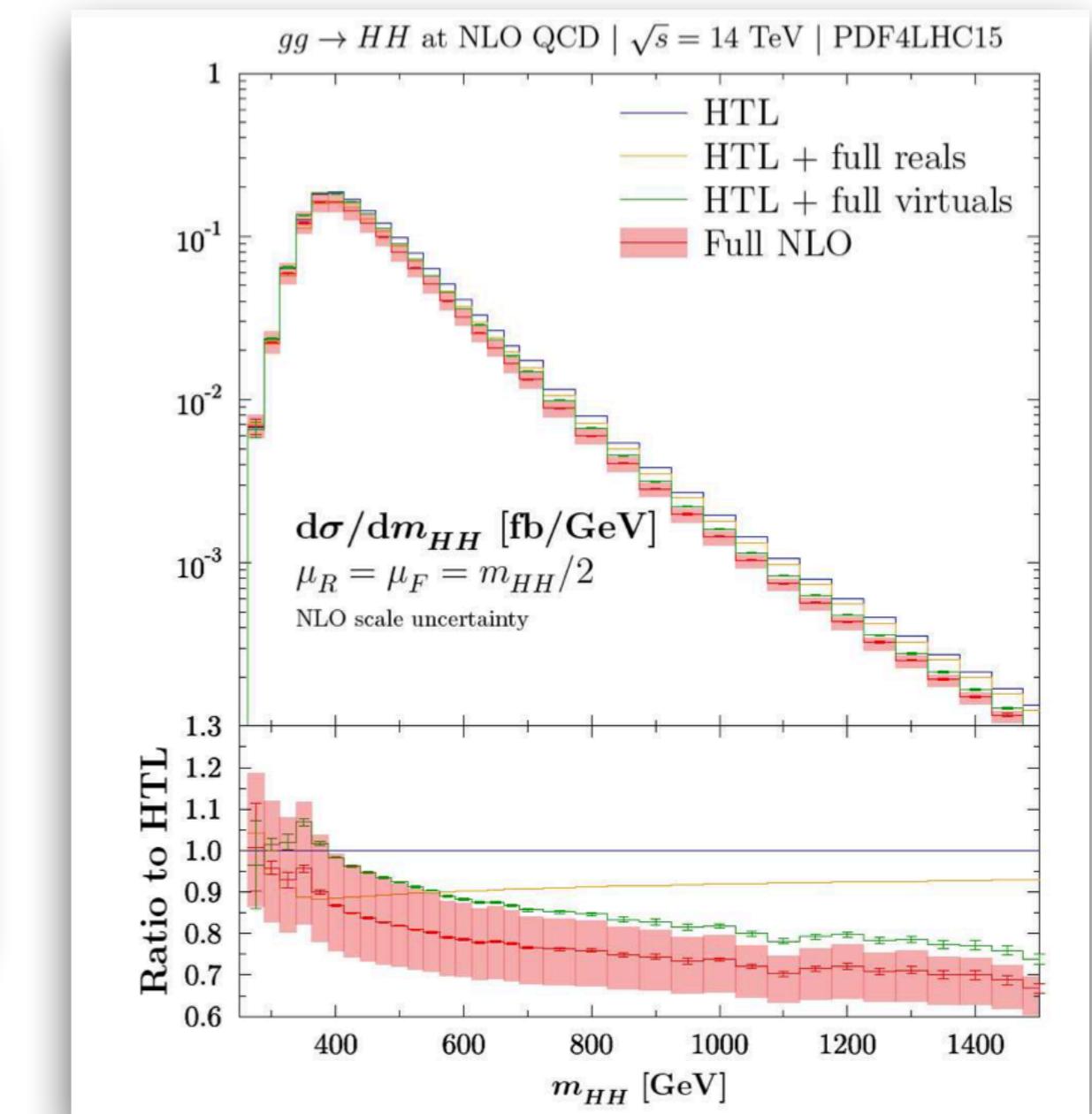
- First results on EW corrections:
 - ♦ top-Yukawa induced corrections: 0.2%, not absorbable in effective trilinear coupling [MM,Schlenk,Spira,'22]
 - ♦ top Yukawa corrections in the high-energy limit [Davies,Mishima,Schönwald,Steinhauser,Zhang,'22]

Full NLO QCD Calculation

[Borowka, Greiner, Heinrich, Jones, Kerner,
Schlenk, Schubert, Zirke]



[Baglio, Campanario, Glaus, MM, Ronca, Spira, Streicher]



$$\sigma_{NLO}^{HTL} = 38.75^{+18\%}_{-15\%} \text{ fb}$$

$$m_t = 173 \text{ GeV}$$

$$32.81(7)^{+13.5\%}_{-12.5\%} \text{ fb}$$

$$38.66^{+18\%}_{-15\%} \text{ fb}$$

$$172.5 \text{ GeV}$$

Uncertainties at NLO QCD

- ♦ Renormalization and factorization scale uncertainties at NLO:

$$\begin{aligned}\sqrt{s} = 13 \text{ TeV} : \quad \sigma_{tot} &= 27.73(7)^{+13.8\%}_{-12.8\%} \text{ fb} \\ \sqrt{s} = 14 \text{ TeV} : \quad \sigma_{tot} &= 32.81(7)^{+13.5\%}_{-12.5\%} \text{ fb} \\ \sqrt{s} = 27 \text{ TeV} : \quad \sigma_{tot} &= 127.0(2)^{+11.7\%}_{-10.7\%} \text{ fb} \\ \sqrt{s} = 100 \text{ TeV} : \quad \sigma_{tot} &= 1140(2)^{+10.7\%}_{-10.0\%} \text{ fb}\end{aligned}$$

- ♦ m_t scale/scheme uncertainties at NLO:

$$\begin{aligned}\sqrt{s} = 13 \text{ TeV} : \quad \sigma_{tot} &= 27.73(7)^{+4\%}_{-18\%} \text{ fb} \\ \sqrt{s} = 14 \text{ TeV} : \quad \sigma_{tot} &= 32.81(7)^{+4\%}_{-18\%} \text{ fb} \\ \sqrt{s} = 27 \text{ TeV} : \quad \sigma_{tot} &= 127.8(2)^{+4\%}_{-18\%} \text{ fb} \\ \sqrt{s} = 100 \text{ TeV} : \quad \sigma_{tot} &= 1140(2)^{+3\%}_{-18\%} \text{ fb}\end{aligned}$$

- ♦ Linear sum of uncertainties ~>

Final Uncertainties at $\text{FT}_{\text{approx}}$

- ♦ Final combined renormalization/factorization scale and m_t scale/scheme uncertainties at $\text{NNLO}_{\text{FTapprox}}^*$:

$$\sqrt{s} = 13 \text{ TeV} : \sigma_{tot} = 31.05^{+6\%}_{-23\%} \text{ fb}$$

$$\sqrt{s} = 14 \text{ TeV} : \sigma_{tot} = 36.69^{+6\%}_{-23\%} \text{ fb}$$

$$\sqrt{s} = 27 \text{ TeV} : \sigma_{tot} = 139.9^{+5\%}_{-22\%} \text{ fb}$$

$$\sqrt{s} = 100 \text{ TeV} : \sigma_{tot} = 1224^{+4\%}_{-21\%} \text{ fb}$$

* $\text{FT}_{\text{approx}}$: full NNLO QCD in the heavy-top-limit with full LO and NLO mass effects and full mass dependence in the one-loop double real corrections at NNLO QCD

Uncertainties for Different Higgs Self-Coupling Values

♦ Final combined uncertainties at NNLO_{FTapprox}:

$\kappa_\lambda = -10$:	$\sigma_{tot} = 1680^{+13\%}_{-14\%}$ fb
$\kappa_\lambda = -5$:	$\sigma_{tot} = 598.9^{+13\%}_{-15\%}$ fb
$\kappa_\lambda = -1$:	$\sigma_{tot} = 131.9^{+11\%}_{-16\%}$ fb
$\kappa_\lambda = 0$:	$\sigma_{tot} = 70.38^{+8\%}_{-18\%}$ fb
$\kappa_\lambda = 1$:	$\sigma_{tot} = 31.05^{+6\%}_{-23\%}$ fb
$\kappa_\lambda = 2$:	$\sigma_{tot} = 13.81^{+3\%}_{-28\%}$ fb
$\kappa_\lambda = 2.4$:	$\sigma_{tot} = 13.10^{+6\%}_{-27\%}$ fb
$\kappa_\lambda = 3$:	$\sigma_{tot} = 18.67^{+12\%}_{-22\%}$ fb
$\kappa_\lambda = 5$:	$\sigma_{tot} = 94.82^{+18\%}_{-13\%}$ fb
$\kappa_\lambda = 10$:	$\sigma_{tot} = 672.2^{+16\%}_{-13\%}$ fb

HH Production
Phenomenology

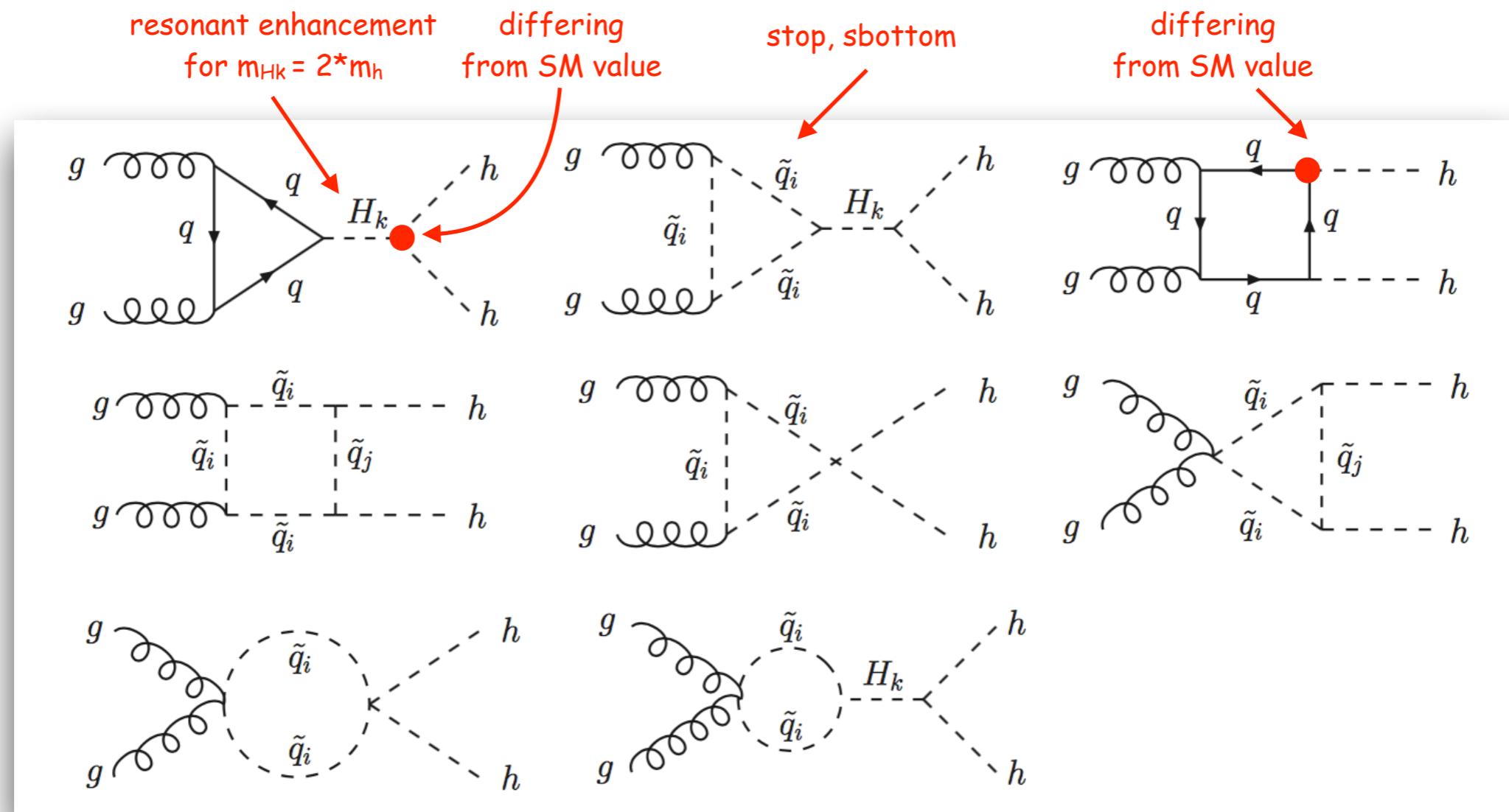


New Physics Effects in Higgs Pair Production

- Cross section: - different trilinear couplings - different Yukawa couplings
- novel particles in the loops - resonant enhancement - novel couplings

• Example NMSSM:

[taken from Dao,MM,Streicher,Walz,'13]





2 Higgs doublets

h, H, A, H^+, H^-

SFOEWPT, DM,
plus charged Higgs

CP-violating

H_1, H_2, H_3, H^+, H^-

plus *CP* violation
baryogenesis

Singlet extension

H_1, H_2, H_3, H^+, H^-

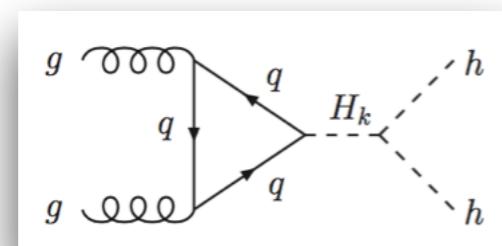
rich pheno, DM

Supersymmetry

$H_1, H_2, H_3, A, H^+, H^-$

a lot (DM, CPviol.,
Hierarchy, ...)

Resonant Enhancement



Higgs-to-Higgs Cascade decays

♦ Following results based on:

Abouabid, Arhrib, Azevedo, El Falaki, Ferreira, MMM, Santos, „Benchmarking Di-Higgs Production in Extended Higgs Sectors”, JHEP 09 (2022) 011

Parameter Point Samples

- ♦ Scans in parameter spaces of the models w/ ScannerS:

take into account all relevant theoretical and experimental constraints

+ limits from di-Higgs searches

4b: [ATLAS-CONF-Note-2021-030, ATLAS,1804.06174], WW $\gamma\gamma$: [ATLAS,1807.08567]

bb $\gamma\gamma$: [ATLAS,1807.04873]; bbWW: [ATLAS,1811.04671, bbZZ: [CMS,2006.06391]

bb $\tau\tau$: [ATLAS,1808.00336;ATLAS-CONF-Note-2021-035;ATLAS,2007.14811], 4W: [ATLAS,1811.11028]

- ♦ Computation of Higgs pair production cxn:

HPAIR [Spira] for C2HDM [Gröber,MM,Spira,'17], NMSSM [Dao,MM,Streicher,Walz,'13],
2HDM [MM], N2HDM [MM]: Born-improved HTL cxn; K-factors 1.4-2.1

- ♦ Scatter plots:

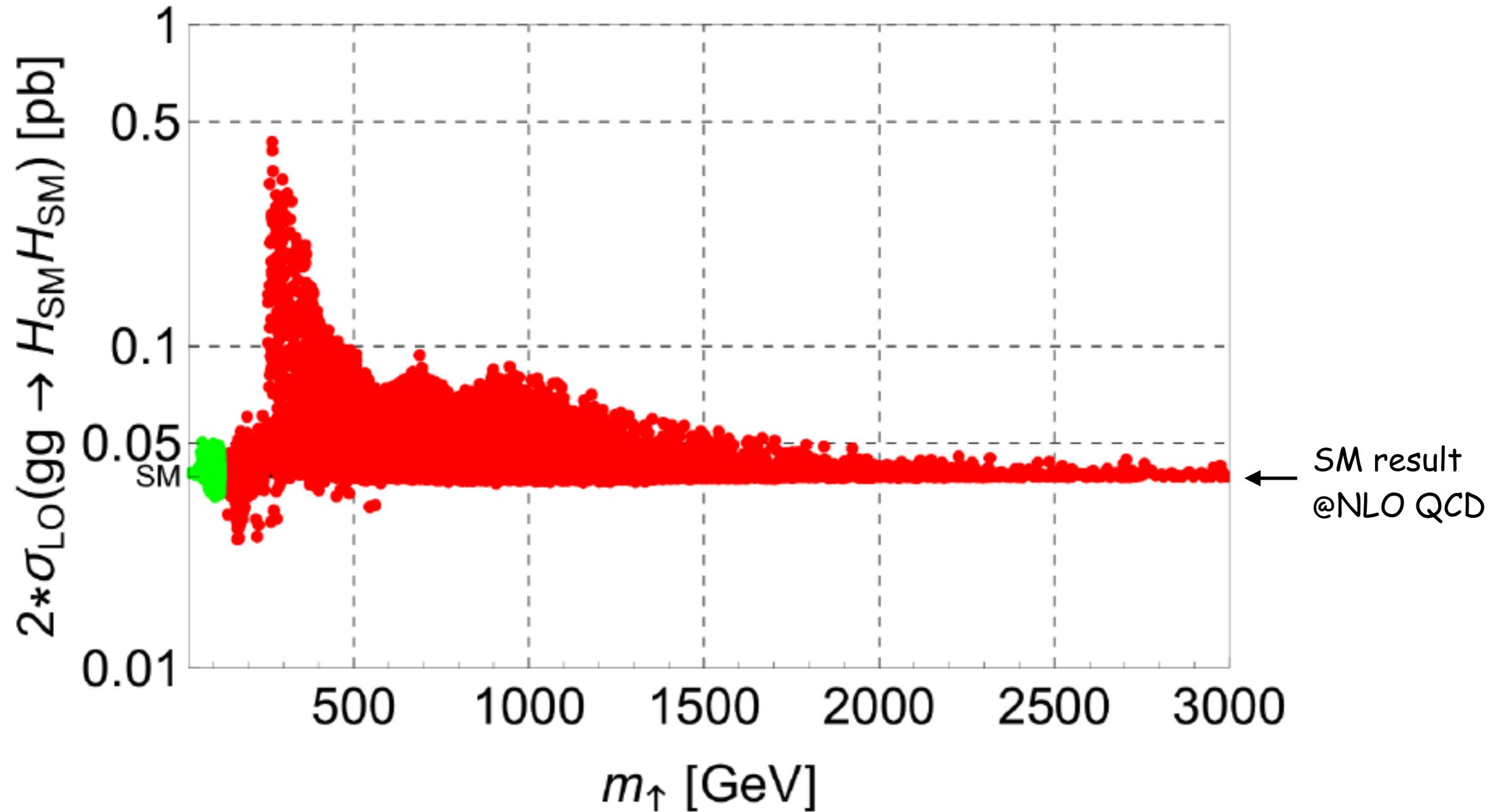
LO cxn times factor 2 (to approx. account for NLO QCD), benchmark points include
NLO QCD calculated w/ HPAIR

2-Higgs Doublet Model: SM-like Higgs Pair Production

[Abouabid,Arhrib,Azevedo,El Falaki,Ferreira,MM,Santos,'21]

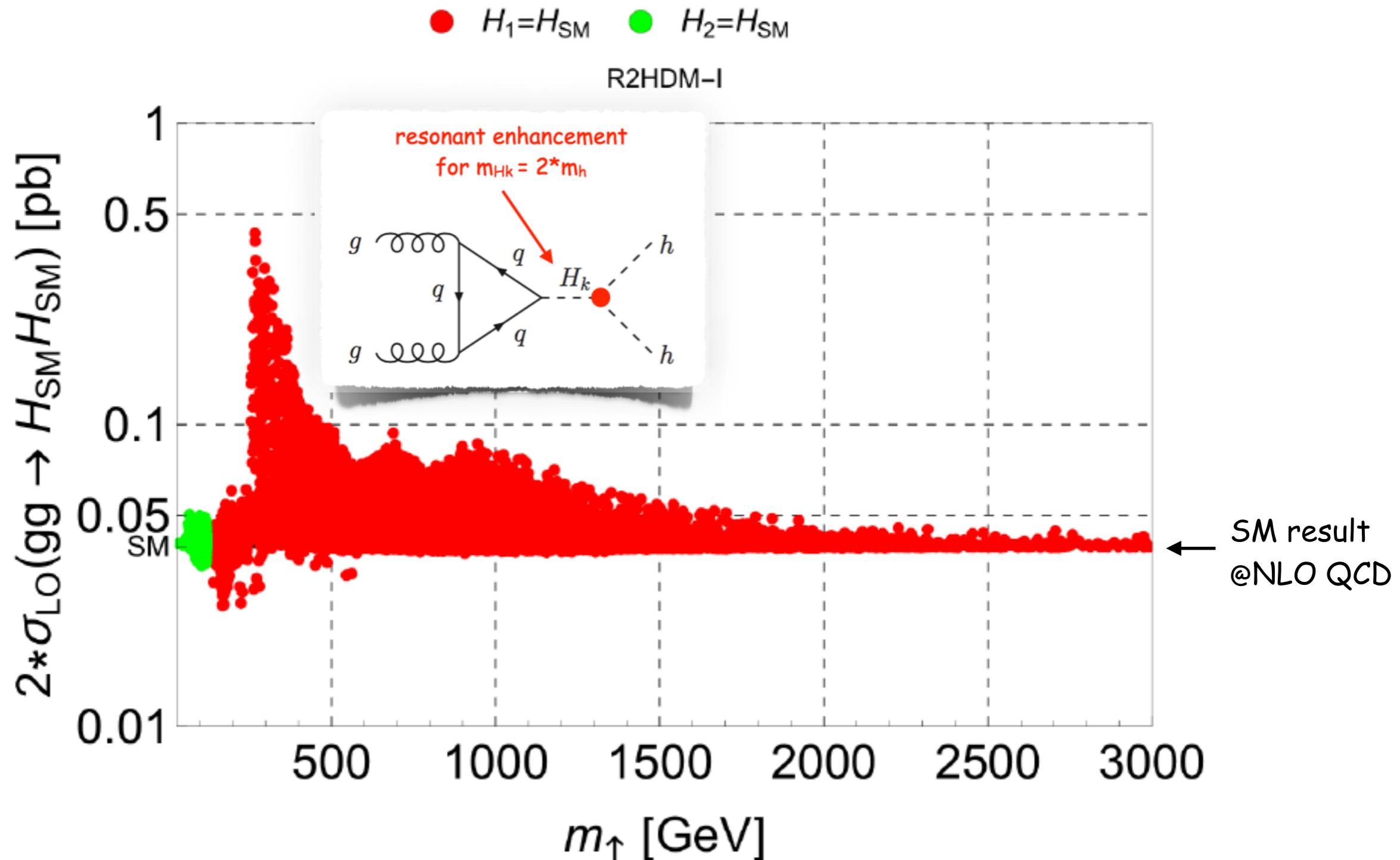
● $H_1=H_{\text{SM}}$ ● $H_2=H_{\text{SM}}$

R2HDM-I



2-Higgs Doublet Model: SM-like Higgs Pair Production

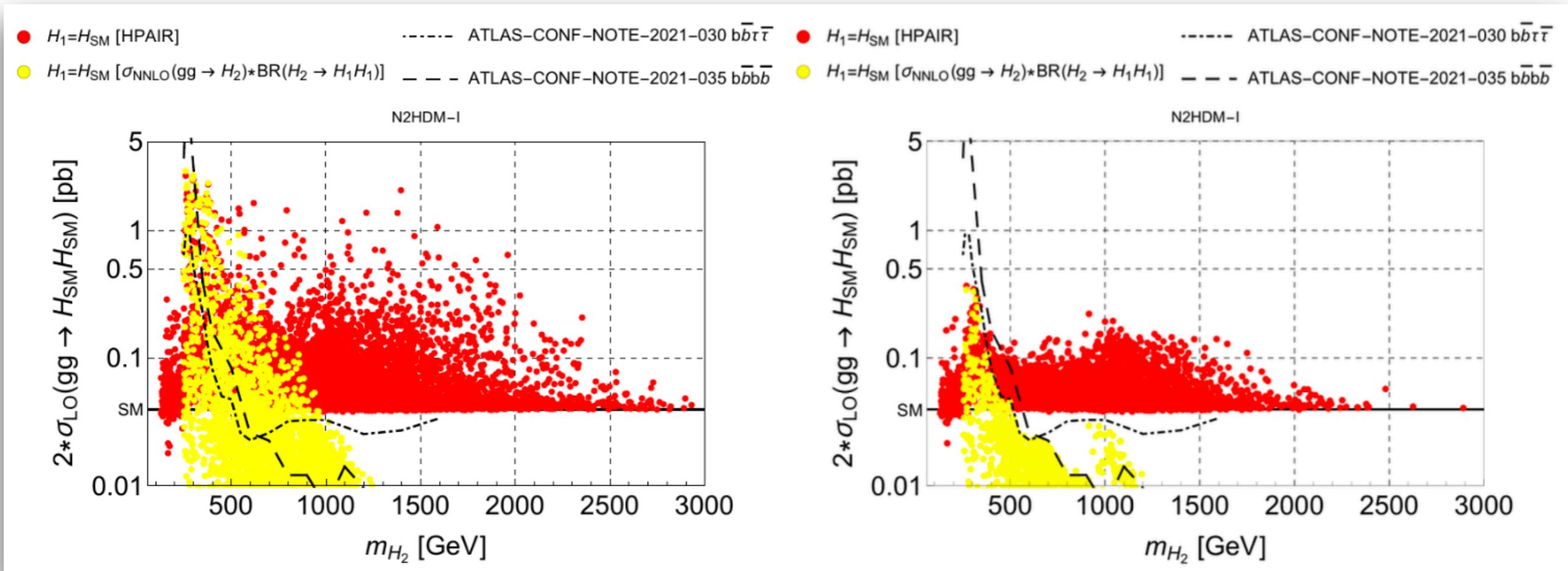
[Abouabid,Arhrib,Azevedo,El Falaki,Ferreira,MM,Santos,'21]



Impact of Constraints - Example N2HDM Type I H_{SM} H_{SM} Production

[Abouabid, Arhrib, Azevedo, El Falaki, Ferreira, MM, Santos, '21]

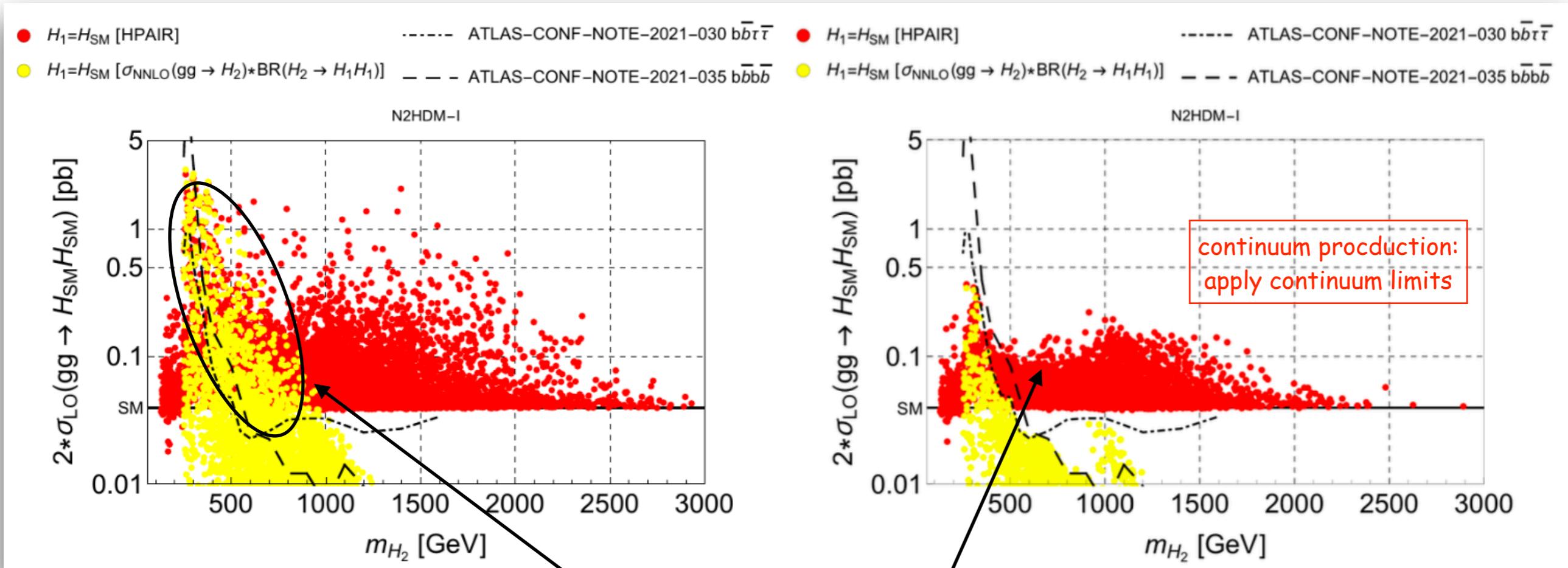
Yellow - Resonant Prod: $\sigma_{NNLO}(H_2) * BR(H_2 \rightarrow H_{SM} H_{SM})$ Red - Continuum Prod: $2 * \sigma_{LO}(H_{SM} H_{SM})$



Impact of Constraints - Example N2HDM Type I H_{SM} H_{SM} Production

[Abouabid, Arhrib, Azevedo, El Falaki, Ferreira, MM, Santos, '21]

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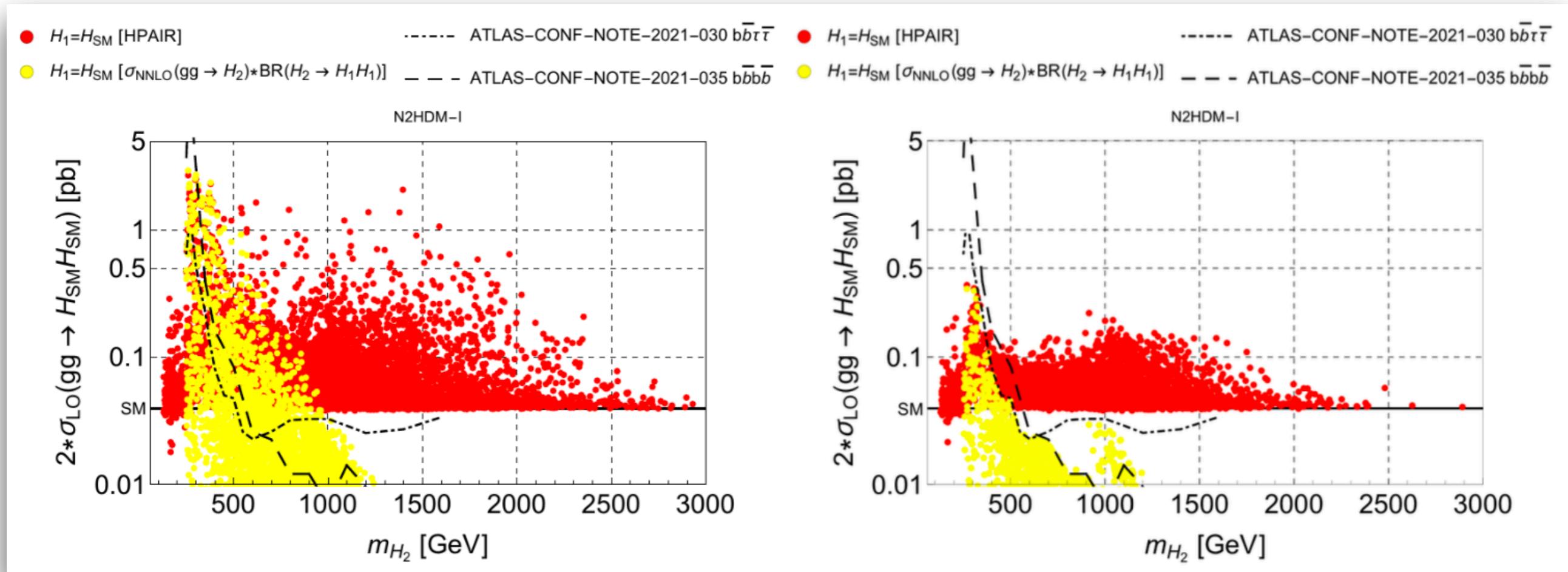


resonant constraint
on single Higgs times
branching ratio

Impact of Constraints - Example N2HDM Type I H_{SM} H_{SM} Production

[Abouabid, Arhrib, Azevedo, El Falaki, Ferreira, MM, Santos, '21]

Yellow - Resonant Prod: $\sigma_{\text{NNLO}}(H_2) * \text{BR}(H_2 \rightarrow H_{\text{SM}} H_{\text{SM}})$ Red - Continuum Prod: $2 * \sigma_{\text{LO}}(H_{\text{SM}} H_{\text{SM}})$



- Factor 2 roughly accounts for NLO QCD corrections
(benchmark points w/ HPAIR at NLO QCD in heavy-top-limit)
- Resonant searches start constraining BSM models

Single Higgs versus Di-Higgs Cascade Decays

- ♦ Singlet extended N2HDM, NMSSM: non-SM Higgs is singlet-like and/or more down- than up-type like => suppressed direct production rate
- ♦ Sample parameter point N2HDM T1:

m_{H_1} [GeV]	m_{H_2} [GeV]	m_{H_3} [GeV]	m_A [GeV]	m_{H^\pm} [GeV]	$\tan \beta$
125.09	281.54	441.25	386.98	421.81	1.990
α_1	α_2	α_3	v_s [GeV]	$\text{Re}(m_{12}^2)$ [GeV 2]	
1.153	0.159	0.989	9639	29769	

Final state:

$$6b: \quad \sigma_{H_1 H_2}^{\text{NLO}} \times \text{BR}(H_2 \rightarrow H_1 H_1) \times \text{BR}(H_1 \rightarrow b\bar{b})^3 = 509 \cdot 0.37 \cdot 0.60^3 \text{ fb} = 40 \text{ fb}$$

$$4b: \quad \sigma^{\text{NNLO}}(H_2) \times \text{BR}(H_2 \rightarrow H_1 H_1) \times \text{BR}(H_1 \rightarrow b\bar{b})^2 = 161 \cdot 0.37 \cdot 0.60^2 \text{ fb} = 21 \text{ fb}$$

H₂ has tiny couplings to b-quarks => better chances to be discovered in di-Higgs than single Higgs channels

$H\bar{H}$ & Baryogenesis



Quảng trường Big Bang (Big Bang Square)

Quảng trường được lấy cảm hứng từ vụ nổ Big Bang - sự khởi đầu vũ trụ và sự

Điểm nhấn:
Tháp Big Bang (Bigbang Tower) tượng trưng cho khía cạnh vũ trụ và Big Bang.
Nhà khán giả ngoài trời (Amphitheater) làm giảm ồn ào và
ngăn chặn bụi bẩn làm vui khỏe và hứa hẹn không khí tươi mới



Electroweak Baryogenesis

- **Electroweak Baryogenesis (EWBG):** generation of the observed baryon-antibaryon asymmetry in the electroweak phase transition (EWPT) [Riemer-Sorensen, Jenssen '17]

$$5.8 \cdot 10^{-10} < \frac{n_B - n_{\bar{B}}}{n_\gamma} < 6.6 \cdot 10^{-10}$$

- **Sakharov Conditions:** [Sakharov '67]

- * (i) B number violation (sphaleron processes)
- * (ii) C and CP violation
- * (iii) Departure from thermal equilibrium

- **Additional constraint:** EW phase transition must be strong first order PT [Quiros '94; Moore '99]

$$\xi_c \equiv \frac{\langle \Phi_c \rangle}{T_c} \geq 1$$

$\langle \Phi_c \rangle$ and T_c field configuration and temperature at phase transition

- ♦ 2HDM type II struggles to reach SFOEWPT (compared to type I)

[see e.g. Basler,Krause,MM,Wittbrodt,Wlotzka,'16]

- ♦ For 2HDM type II points with $\xi_c < 1$:

What extra dynamics is required to achieve SFOEWPT?

- ♦ Our model: CP -conserving 2HDM with softly broken discrete Z_2 symmetry

$$V_{\text{tree}}(\Phi_1, \Phi_2) = m_{11}^2(\Phi_1^\dagger \Phi_1) + m_{22}^2(\Phi_2^\dagger \Phi_2) - \textcolor{blue}{m_{12}^2}(\Phi_1^\dagger \Phi_2 + \Phi_2^\dagger \Phi_1) + \lambda_1(\Phi_1^\dagger \Phi_1)^2 + \lambda_2(\Phi_2^\dagger \Phi_2)^2 \\ + \lambda_3(\Phi_1^\dagger \Phi_1)(\Phi_2^\dagger \Phi_2) + \lambda_4(\Phi_1^\dagger \Phi_2)(\Phi_2^\dagger \Phi_1) + \frac{1}{2}\lambda_5[(\Phi_1^\dagger \Phi_2)^2 + (\Phi_2^\dagger \Phi_1)^2]$$

- ♦ Extended by (purely scalar) dim-6 EFT contributions to the Higgs potential [Anisha et al.,'19]

$$\mathcal{L}_{\text{EFT}} = \mathcal{L}_{\text{2HDM}} + \sum_i \frac{C_6^i}{\Lambda^2} O_6^i \quad \Rightarrow \quad V_{\text{dim-6}} = - \sum_i \frac{C_6^i}{\Lambda^2} O_6^i$$

- ♦ Higgs pair production: a tool for fingerprinting an SFOEWPT?

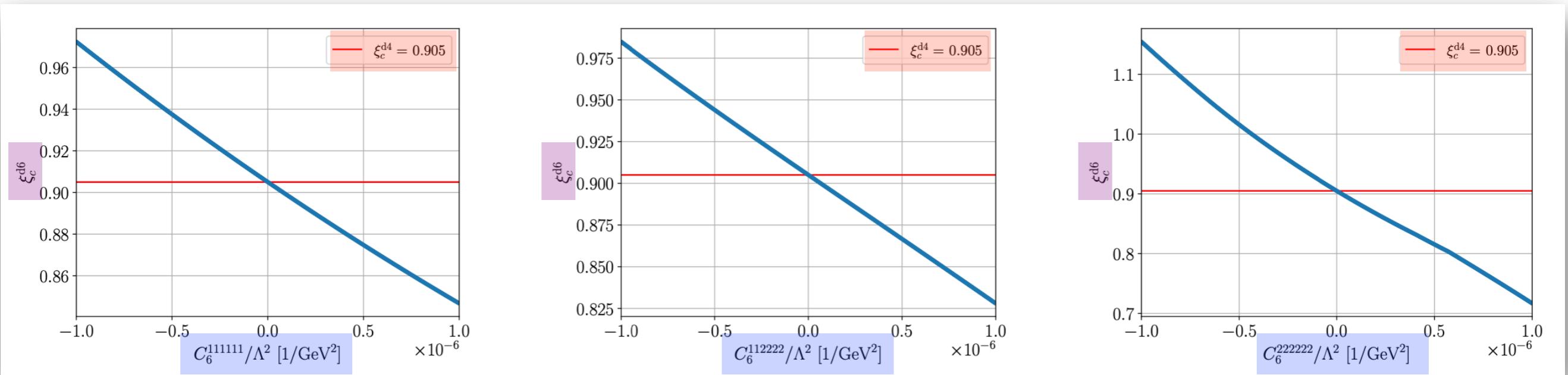
O_6^{111111}	$(\Phi_1^\dagger \Phi_1)^3$	O_6^{222222}	$(\Phi_2^\dagger \Phi_2)^3$
O_6^{111122}	$(\Phi_1^\dagger \Phi_1)^2 (\Phi_2^\dagger \Phi_2)$	O_6^{112222}	$(\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2)^2$
O_6^{122111}	$(\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) (\Phi_1^\dagger \Phi_1)$	O_6^{122122}	$(\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2)$
O_6^{121211}	$(\Phi_1^\dagger \Phi_2)^2 (\Phi_1^\dagger \Phi_1) + \text{h.c.}$	O_6^{121222}	$(\Phi_1^\dagger \Phi_2)^2 (\Phi_2^\dagger \Phi_2) + \text{h.c.}$

- absorb dim-6 contributions (to scalar masses) in shifts $\lambda_i \rightarrow \lambda_i + \delta\lambda_i, m_{12}^2 \rightarrow m_{12}^2 + \delta m_{12}^2$
- ⇒ scalar mass spectrum same as for dim-4 @ LO
- ⇒ shift EFT effects into **Higgs self-couplings & multi-Higgs final states**

- Computation of ξ_c with BSMPT [Basler,Biermann,Mühlleitner,Müller]:
Loop-corrected effective potential at finite temperature including daisy resummation of bosonic masses; „OS“ renormalization

Effect of Dim-6 Operators

[Anisha,Biermann,Englert,MM,'22]



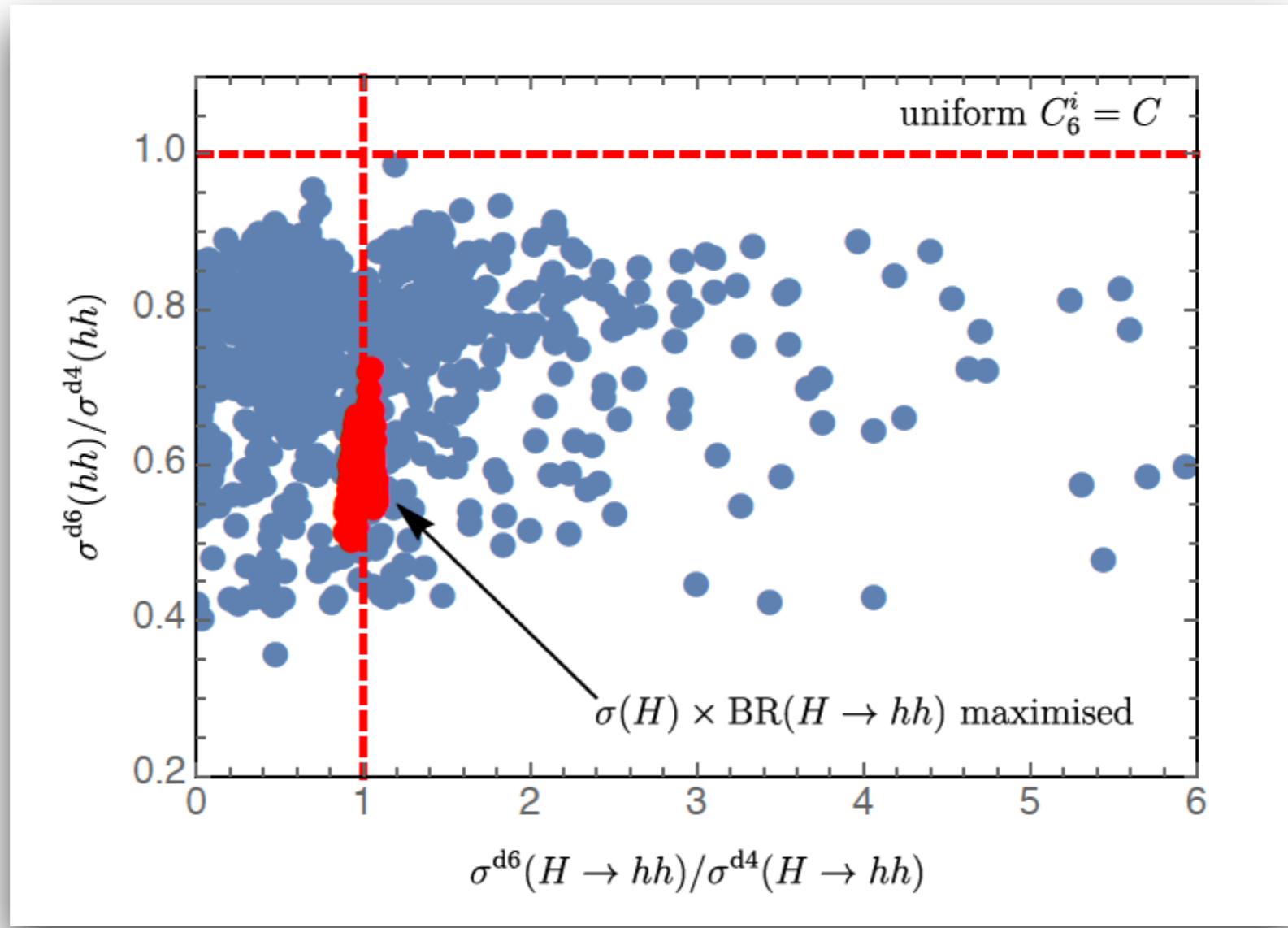
impact of individual Wilson coefficients on ξ_c^{d6} for $\xi_c^{d4} \approx 0.9$:

- linear response $\sim C_6^{i,j}$ \rightarrow perturbativity ok
- SFOEWPT achievable in agreement with experimental constraints

interference effects in heavy Higgs production in $t\bar{t}$ final state are width dependent
→ sensitive to EFT modifications: overall effect is small after taking the Higgs data constraints into account => hh production important tool for fingerprinting SFOEWPT

Correlation of ξ_c^{d4} , continuum and resonant hh production

[Anisha,Biermann,Englert,MM,'22]



- Points with $\xi_c^{d6} \approx 1$ for $\xi_c^{d4} \geq 0.3$ (red Higgs-philic points: $\xi_c^{d4} > 0.15$)
- Higgs-philic points: resonance contribution modified by ~5-10%, continuum production modified by ~50%

Conclusions



- ♦ Flaws of SM call for new physics; no direct signs of new physics => Higgs boson
- ♦ Combine results of all available observables, precision important
- ♦ Both QCD&EW corrections are important; corrections can be more important in BSM models
- ♦ Precision in HH
 - slowly catching up w/ H production
 - NLO QCD mass effects important: -15% (inclusive), -30-40% (distribution at large M_{HH})
 - uncertainties from top mass scale and scheme choice are significant
- ♦ HH in extended Higgs sectors
 - large cross sections due to resonant enhancement possible
 - resonant searches start testing BSM models in HH
 - interesting effects in singlet models: di-Higgs can beat single Higgs
- ♦ Electroweak baryogenesis requires strong first order EWPT
 - extension of 2HDM by scalar dim-6 operators can lead to SFOEWPT
 - can be probed through combination of resonant-non-resonant di-Higgs production

Higgs boson can give many insights in BSM physics
Interesting times ahead!

*Thank you for
your attention!*

