

Precision Electroweak Physics in the SM and Beyond

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- Introduction
- m_t , M_W and the fit to EWPO in the SM
- m_t , M_W and the fit to EWPO beyond the SM:
 - Oblique NP
 - SMEFT
- Summary and outlook

INTRODUCTION

- $SU(2)_L \times U(1)_Y$ gauge symmetry hidden at low energies, but restored in the UV
 - tree-level relations among weak couplings and masses corrected by finite and calculable loop corrections
 - precision measurements of masses and couplings
 - test the quantum structure of the SM
 - probe NP through its virtual effects

SYMMETRIES OF THE SM HIGGS SECTOR

In the SM, one Higgs doublet φ w. potential

$$V(\varphi) = -\frac{\mu^2}{2} |\varphi|^2 + \frac{\lambda}{4} |\varphi|^4 = -\frac{\mu^2}{2} \text{Tr}(\Phi^\dagger \Phi) + \frac{\lambda}{4} \text{Tr}(\Phi^\dagger \Phi)^2$$

with $\Phi \equiv \frac{1}{\sqrt{2}} \begin{pmatrix} \varphi_0^* & \varphi_+ \\ -\varphi_+^* & \varphi_0 \end{pmatrix}$, invariant under $\Phi \rightarrow U_L \Phi U_R^\dagger$

where $SU(2)_L$ coincides with gauge $SU(2)$, while Y with the third component of $SU(2)_R$. The charge-conserving

$\langle \Phi \rangle \equiv \frac{1}{2} \begin{pmatrix} v & 0 \\ 0 & v \end{pmatrix}$ leaves the diagonal $SU(2)_V$ unbroken,

ensuring $M_{W_1} = M_{W_2} = M_{W_3}$ and $\rho \equiv \frac{M_W^2}{M_Z^2 \cos^2 \theta_W} = 1$

SYMMETRIES OF THE SM HIGGS SECTOR

- Promoting right-handed quarks to $SU(2)_R$ doublets, one can write Yukawa couplings in the form

$$\bar{Q}_L \Phi \begin{pmatrix} Y_u & 0 \\ 0 & Y_d \end{pmatrix} Q_R$$

which would be $SU(2)_R$ -invariant for $Y_u=Y_d$.

Therefore, the tree-level prediction $\rho=1$ gets loop corrections proportional to $G_F m_t^2$.

EXPERIMENTAL INPUTS

- SM input parameters:
 - $G_F, \alpha, M_Z, M_H, m_t, \alpha_s(M_Z), \Delta\alpha_{\text{had}}^{(5)}$
- For $\Delta\alpha_{\text{had}}^{(5)}$ we use lattice QCD in the Euclidean + perturbative running
- For m_t , "standard" average completely dominated by recent CMS l+jets measurement: $m_t=171.77\pm 0.37 \text{ GeV}$. However, there is a 3.5σ tension with the TeVatron average $m_t=174.34\pm 0.64 \text{ GeV}$, so consider also "conservative" average with error inflated to 1 GeV . Notice: PDG recipe would give a "ultra-conservative" 1.7 GeV error.

M_W : New Exp. Average

- Also for M_W , "standard" average completely dominated by recent CDF measurement.
- Updating the ATLAS measurement, and taking QED and PDF uncertainties fully correlated between TeVatron and LHC experiments, we obtain $M_W=80409.3\pm 7.9$ MeV (previous average was $M_W=80413.3\pm 8.0$ MeV.) Assuming no correlation moves the central value by half σ to $M_W=80406.4\pm 7.3$ MeV; I will not present results for this choice.
- Also in this case there are tensions between LHC, TeVatron and LEP measurements, so consider also "conservative" average with error inflated à la PDG to 18 MeV

M_W : SM vs EXPERIMENT

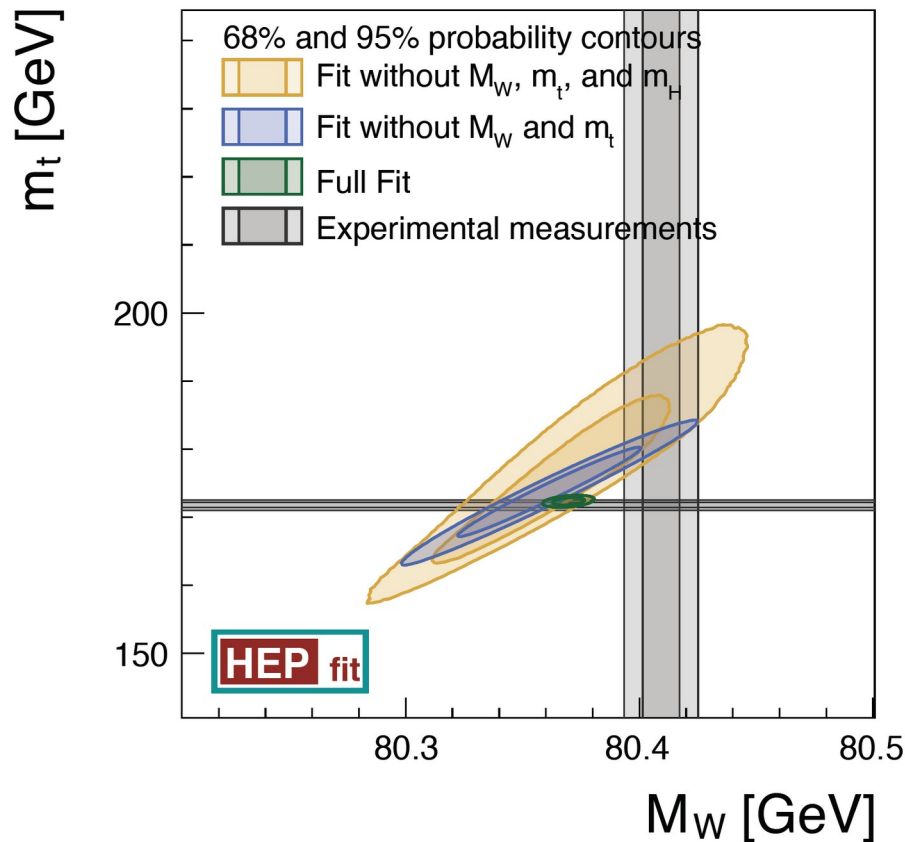
| Model | Pred. M_W [GeV] <i>standard average</i> | Pull | Pred. M_W [GeV] <i>conservative average</i> | Pull |
|-------|----------------------------------------------|--------------|--------------------------------------------------|--------------|
| SM | 80.3499 ± 0.0056 | 6.1σ | 80.3505 ± 0.0077 | 3.0σ |

- The SM prediction is obtained omitting the experimental information on M_W . Before the CDF update, the tension was 1.8σ . Current theory error on M_W in the SM is 4 MeV.

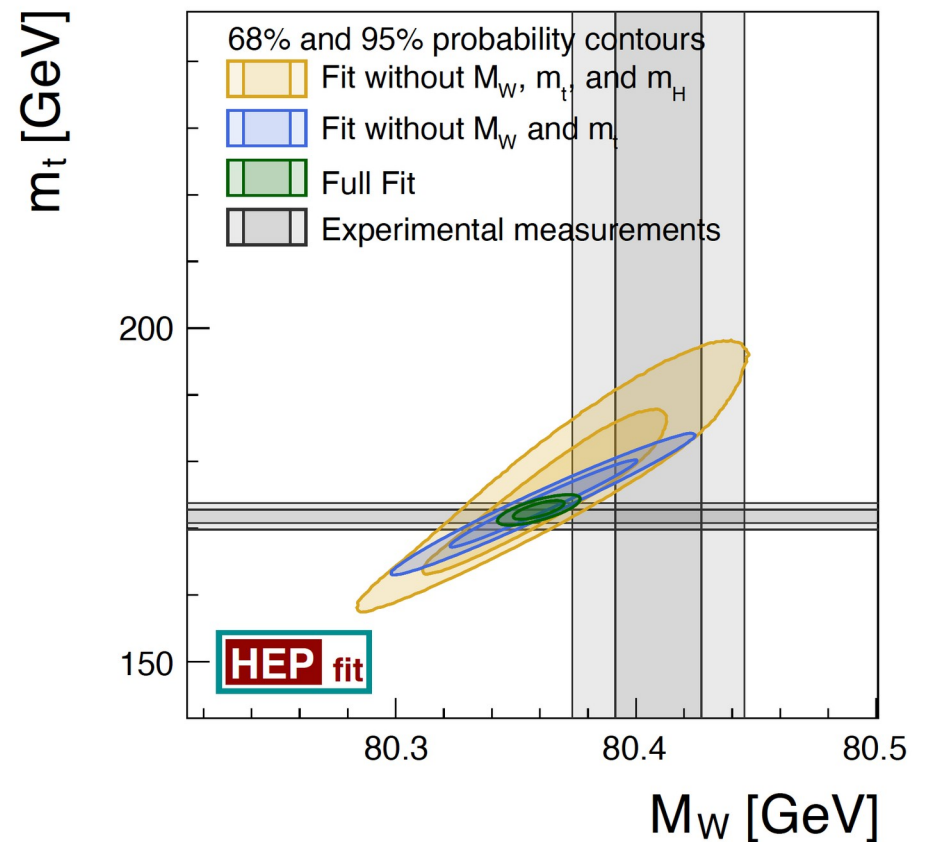
Awramik et al, '03

INTERPLAY OF M_W WITH OTHER OBSERVABLES

standard

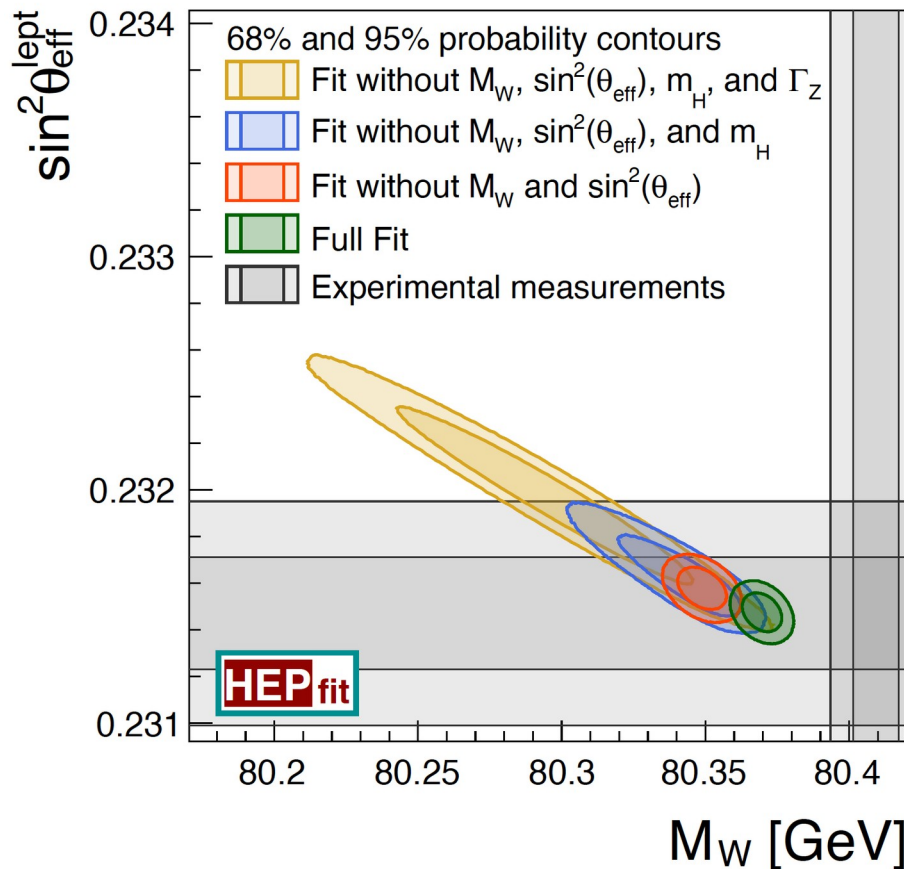


conservative

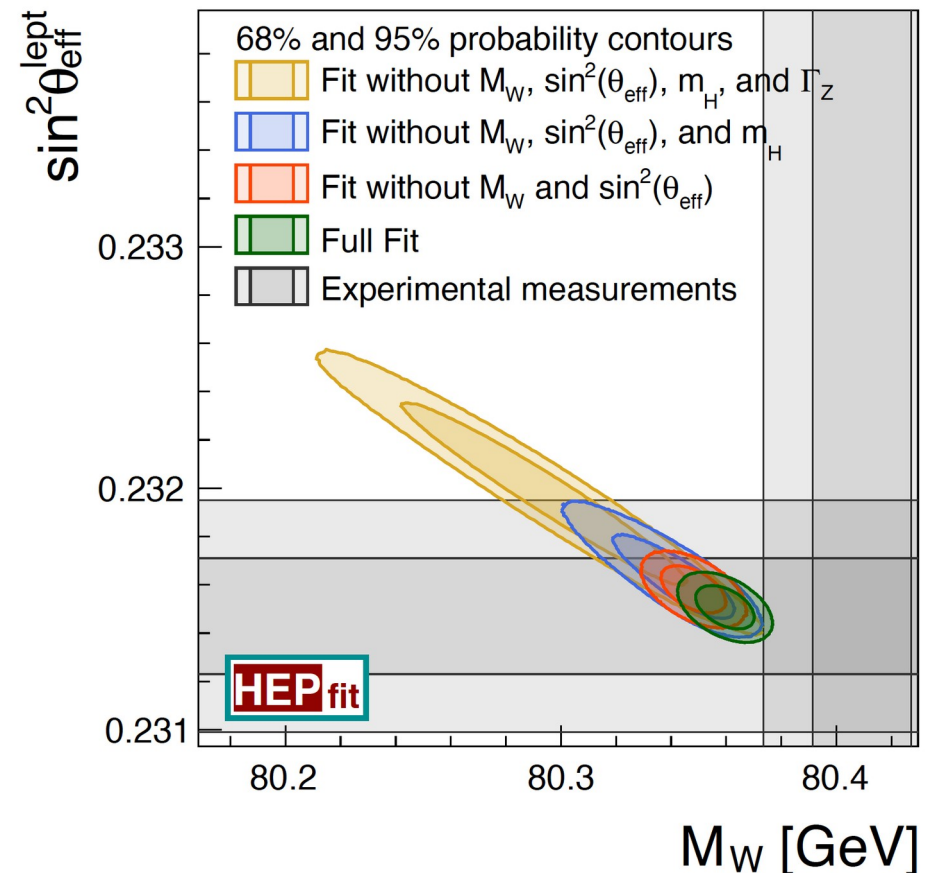


INTERPLAY OF M_W WITH OTHER OBSERVABLES

standard



conservative



Terminology

- **Full Fit/Posterior:** use all available information on both SM parameters and EWPOs. Gives our current best knowledge, assuming the validity of the SM
- **Prediction/Indirect:** remove experimental information on one EWPO (**prediction**) or on one SM parameter (**indirect determination**). Allows to compute pulls and local compatibility, using the output predictive pdf for the observable/parameter removed from the fit.

Terminology

- **Full Prediction:** use only exp info on SM parameters. Using the output pdf (including correlations) for EWPOs and the exp results allows to compute global p-value.
- **Full Indirect:** use only exp info on EWPO. Useful to identify tensions in data that cannot be relaxed in the SM irrespective of the values of SM parameters.

| | Measurement | Posterior | Indirect/Prediction | Pull | Full Indirect | Pull | Full Prediction | Pull |
|------------------------------------------------------------------------|-----------------------|-------------------------------------------------|-------------------------------------------------|------|-------------------------------------------------|------|-------------------------------------------------|------|
| $\alpha_s(M_Z)$ | 0.1177 ± 0.0010 | 0.11763 ± 0.00095 [0.11577, 0.11946] | 0.1170 ± 0.0028 [0.1116, 0.1225] | 0.2 | 0.1217 ± 0.0047 [0.1126, 0.1310] | -0.8 | 0.1177 ± 0.0010 [0.1157, 0.1197] | 0.0 |
| $\delta\alpha_{\text{had}}^5$ | 0.02766 ± 0.00010 | 0.027541 ± 0.000096 [0.027352, 0.027730] | 0.02624 ± 0.00033 [0.02559, 0.02689] | 4.1 | 0.02793 ± 0.00068 [0.02661, 0.02926] | -0.4 | 0.02766 ± 0.00010 [0.02746, 0.02786] | 0.0 |
| M_Z [GeV] | 91.1875 ± 0.0021 | 91.1910 ± 0.0020 [91.1870, 91.1949] | 91.2287 ± 0.0068 [91.2154, 91.2421] | -5.8 | 91.210 ± 0.039 [91.134, 91.287] | -0.6 | 91.1875 ± 0.0021 [91.1834, 91.1916] | 0.0 |
| m_t [GeV] | 171.79 ± 0.38 | 172.34 ± 0.37 [171.61, 173.06] | 180.9 ± 1.5 [178.0, 183.8] | -5.9 | 186.7 ± 9.5 [168.0, 205.1] | -1.6 | 171.80 ± 0.38 [171.05, 172.54] | 0.0 |
| m_H [GeV] | 125.21 ± 0.12 | 125.21 ± 0.12 [124.97, 125.44] | 94.0 ± 5.0 [83.3, 104.3] | 4.1 | 241.2 ± 121.3 [100.8, 626.8] | -0.8 | 125.21 ± 0.12 [124.97, 125.45] | 0.0 |
| M_W [GeV] | 80.4093 ± 0.0079 | 80.3696 ± 0.0045 [80.3608, 80.3786] | 80.3499 ± 0.0056 [80.3390, 80.3609] | 6.1 | 80.4089 ± 0.0078 [80.3934, 80.4241] | 0.0 | 80.3496 ± 0.0057 [80.3386, 80.3608] | 6.1 |
| Γ_W [GeV] | 2.085 ± 0.042 | 2.08896 ± 0.00052 [2.08793, 2.08999] | 2.08896 ± 0.00052 [2.08793, 2.08998] | -0.1 | 2.0940 ± 0.0023 [2.0896, 2.0984] | -0.2 | 2.08744 ± 0.00059 [2.08627, 2.08859] | 0.0 |
| $\sin^2 \theta_{\text{eff}}^{\text{lept}}(Q_{\text{FB}}^{\text{had}})$ | 0.2324 ± 0.0012 | 0.231474 ± 0.000055 [0.231366, 0.231583] | 0.231473 ± 0.000055 [0.231364, 0.231581] | 0.8 | 0.23146 ± 0.00014 [0.23119, 0.23173] | 0.8 | 0.231558 ± 0.000062 [0.231436, 0.231679] | 0.7 |
| $P_\tau^{\text{pol}} = \mathcal{A}_\ell$ | 0.1465 ± 0.0033 | 0.14739 ± 0.00044 [0.14654, 0.14825] | 0.14741 ± 0.00044 [0.14655, 0.14827] | -0.3 | 0.1475 ± 0.0011 [0.1454, 0.1496] | -0.3 | 0.14675 ± 0.00049 [0.14580, 0.14770] | -0.1 |
| Γ_Z [GeV] | 2.4955 ± 0.0023 | 2.49454 ± 0.00064 [2.49328, 2.49580] | 2.49434 ± 0.00068 [2.49300, 2.49567] | 0.5 | 2.4953 ± 0.0020 [2.4912, 2.4993] | 0.1 | 2.49397 ± 0.00068 [2.49262, 2.49531] | 0.6 |
| σ_h^0 [nb] | 41.480 ± 0.033 | 41.4892 ± 0.0077 [41.4742, 41.5042] | 41.4914 ± 0.0080 [41.4758, 41.5072] | -0.3 | 41.462 ± 0.030 [41.403, 41.522] | 0.4 | 41.4923 ± 0.0080 [41.4766, 41.5081] | -0.4 |
| R_ℓ^0 | 20.767 ± 0.025 | 20.7487 ± 0.0080 [20.7329, 20.7645] | 20.7451 ± 0.0086 [20.7281, 20.7621] | 0.8 | 20.760 ± 0.022 [20.717, 20.802] | 0.2 | 20.7468 ± 0.0087 [20.7298, 20.7637] | 0.7 |
| $A_{\text{FB}}^{0,\ell}$ | 0.0171 ± 0.0010 | 0.016293 ± 0.000096 [0.016106, 0.016482] | 0.016284 ± 0.000096 [0.016097, 0.016476] | 0.8 | 0.01631 ± 0.00024 [0.01585, 0.01679] | 0.8 | 0.01615 ± 0.00011 [0.01594, 0.01636] | 1.0 |
| \mathcal{A}_ℓ (SLD) | 0.1513 ± 0.0021 | 0.14739 ± 0.00044 [0.14654, 0.14825] | 0.14742 ± 0.00045 [0.14654, 0.14832] | 1.8 | 0.1475 ± 0.0011 [0.1454, 0.1496] | 1.6 | 0.14675 ± 0.00049 [0.14580, 0.14770] | 2.1 |
| R_b^0 | 0.21629 ± 0.00066 | 0.215894 ± 0.000100 [0.215697, 0.216090] | 0.21589 ± 0.00010 [0.21569, 0.21609] | 0.6 | 0.21543 ± 0.00036 [0.21472, 0.21614] | 1.1 | 0.21591 ± 0.00010 [0.21571, 0.21611] | 0.6 |
| R_c^0 | 0.1721 ± 0.0030 | 0.172198 ± 0.000054 [0.172093, 0.172302] | 0.172199 ± 0.000054 [0.172094, 0.172304] | -0.1 | 0.17240 ± 0.00018 [0.17205, 0.17277] | -0.1 | 0.172189 ± 0.000054 [0.172084, 0.172295] | -0.1 |
| $A_{\text{FB}}^{0,b}$ | 0.0996 ± 0.0016 | 0.10334 ± 0.00031 [0.10273, 0.10393] | 0.10335 ± 0.00032 [0.10273, 0.10398] | -2.3 | 0.10338 ± 0.00077 [0.10189, 0.10489] | -2.1 | 0.10288 ± 0.00034 [0.10220, 0.10354] | -2.0 |
| $A_{\text{FB}}^{0,c}$ | 0.0707 ± 0.0035 | 0.07384 ± 0.00023 [0.07339, 0.07428] | 0.07385 ± 0.00024 [0.07339, 0.07432] | -0.9 | 0.07391 ± 0.00059 [0.07275, 0.07507] | -0.9 | 0.07348 ± 0.00025 [0.07298, 0.07398] | -0.8 |
| \mathcal{A}_b | 0.923 ± 0.020 | 0.934768 ± 0.000040 [0.934690, 0.934845] | 0.934769 ± 0.000040 [0.934691, 0.934846] | -0.6 | 0.93460 ± 0.00016 [0.93428, 0.93492] | -0.6 | 0.934721 ± 0.000041 [0.934642, 0.934801] | -0.6 |
| \mathcal{A}_c | 0.670 ± 0.027 | 0.66795 ± 0.00021 [0.66753, 0.66837] | 0.66795 ± 0.00022 [0.66753, 0.66838] | 0.1 | 0.66817 ± 0.00054 [0.66711, 0.66921] | 0.1 | 0.66766 ± 0.00022 [0.66722, 0.66810] | 0.1 |
| \mathcal{A}_s | 0.895 ± 0.091 | 0.935675 ± 0.000039 [0.935597, 0.935752] | 0.935674 ± 0.000040 [0.935597, 0.935752] | -0.4 | 0.935714 ± 0.000099 [0.935523, 0.935907] | -0.5 | 0.935621 ± 0.000041 [0.935541, 0.935702] | -0.5 |
| $\text{BR}_{W\ell\bar{\nu}_\ell}$ | 0.10860 ± 0.00090 | 0.108388 ± 0.000022 [0.108345, 0.108431] | 0.108388 ± 0.000022 [0.108344, 0.108431] | 0.2 | 0.10829 ± 0.00011 [0.10807, 0.10850] | 0.3 | 0.108386 ± 0.000023 [0.108340, 0.108432] | 0.2 |
| $\sin^2 \theta_{\text{eff}}^{\text{ll}}(\text{HC})$ | 0.23143 ± 0.00025 | 0.231474 ± 0.000055 [0.231366, 0.231583] | 0.231477 ± 0.000056 [0.231366, 0.231588] | -0.2 | 0.23146 ± 0.00014 [0.23119, 0.23173] | -0.1 | 0.231558 ± 0.000062 [0.231436, 0.231679] | -0.5 |
| R_{uc} | 0.1660 ± 0.0090 | 0.172220 ± 0.000031 [0.172158, 0.172282] | 0.172220 ± 0.000031 [0.172158, 0.172281] | -0.7 | 0.17242 ± 0.00018 [0.17208, 0.17278] | -0.7 | 0.172212 ± 0.000032 [0.172149, 0.172275] | -0.7 |

| | Measurement | Posterior | Indirect/Prediction | Pull | Full Indirect | Pull | Full Prediction | Pull |
|------------------------------------------------------------------------|-----------------------|-------------------------------------------------|-------------------------------------------------|------------|-------------------------------------------------|------|-------------------------------------------------|------------|
| $\alpha_s(M_Z)$ | 0.1177 ± 0.0010 | 0.11791 ± 0.00094 [0.11606, 0.11976] | 0.1197 ± 0.0028 [0.1142, 0.1253] | -0.7 | 0.1218 ± 0.0047 [0.1126, 0.1310] | -0.8 | 0.1177 ± 0.0010 [0.1157, 0.1197] | 0.0 |
| $\delta\alpha_{\text{had}}^5$ | 0.02766 ± 0.00010 | 0.027624 ± 0.000097 [0.027432, 0.027814] | 0.02703 ± 0.00040 [0.02624, 0.02781] | 1.5 | 0.02792 ± 0.00071 [0.02653, 0.02932] | -0.4 | 0.02766 ± 0.00010 [0.02747, 0.02786] | -0.1 |
| M_Z [GeV] | 91.1875 ± 0.0021 | 91.1883 ± 0.0021 [91.1843, 91.1924] | 91.218 ± 0.011 [91.196, 91.240] | -2.7 | 91.209 ± 0.039 [91.134, 91.287] | -0.5 | 91.1875 ± 0.0021 [91.1834, 91.1916] | -0.1 |
| m_t [GeV] | 171.8 ± 1.0 | 172.75 ± 0.93 [170.92, 174.59] | 179.1 ± 2.5 [174.0, 184.0] | -2.6 | 186.5 ± 10.1 [166.7, 205.8] | -1.4 | 171.8 ± 1.0 [169.8, 173.8] | 0.0 |
| m_H [GeV] | 125.21 ± 0.12 | 125.21 ± 0.12 [124.97, 125.44] | 105.0 ± 11.3 [87.7, 134.1] | 1.5 | 238.4 ± 121.3 [98.1, 629.5] | -0.8 | 125.21 ± 0.12 [124.97, 125.45] | 0.1 |
| M_W [GeV] | 80.409 ± 0.018 | 80.3595 ± 0.0070 [80.3456, 80.3733] | 80.3505 ± 0.0077 [80.3355, 80.3656] | 3.0 | 80.407 ± 0.017 [80.373, 80.441] | 0.1 | 80.3497 ± 0.0079 [80.3342, 80.3653] | 3.1 |
| Γ_W [GeV] | 2.085 ± 0.042 | 2.08831 ± 0.00067 [2.08700, 2.08963] | 2.08830 ± 0.00067 [2.08700, 2.08961] | -0.1 | 2.0939 ± 0.0026 [2.0888, 2.0989] | -0.2 | 2.08743 ± 0.00073 [2.08601, 2.08889] | 0.0 |
| $\sin^2 \theta_{\text{eff}}^{\text{lept}}(Q_{\text{FB}}^{\text{had}})$ | 0.2324 ± 0.0012 | 0.231507 ± 0.000060 [0.231389, 0.231623] | 0.231505 ± 0.000059 [0.231388, 0.231622] | 0.7 | 0.23146 ± 0.00014 [0.23119, 0.23173] | 0.8 | 0.231558 ± 0.000068 [0.231426, 0.231691] | 0.7 |
| $P_{\tau}^{\text{pol}} = \mathcal{A}_{\ell}$ | 0.1465 ± 0.0033 | 0.14713 ± 0.00047 [0.14622, 0.14806] | 0.14716 ± 0.00047 [0.14622, 0.14808] | -0.2 | 0.1475 ± 0.0011 [0.1454, 0.1496] | -0.3 | 0.14674 ± 0.00053 [0.14570, 0.14779] | -0.1 |
| Γ_Z [GeV] | 2.4955 ± 0.0023 | 2.49444 ± 0.00067 [2.49313, 2.49574] | 2.49423 ± 0.00071 [2.49285, 2.49562] | 0.5 | 2.4952 ± 0.0021 [2.4911, 2.4993] | 0.1 | 2.49396 ± 0.00072 [2.49257, 2.49538] | 0.6 |
| σ_h^0 [nb] | 41.480 ± 0.033 | 41.4907 ± 0.0076 [41.4756, 41.5057] | 41.4928 ± 0.0080 [41.4771, 41.5086] | -0.4 | 41.462 ± 0.030 [41.403, 41.522] | 0.4 | 41.4924 ± 0.0080 [41.4767, 41.5083] | -0.4 |
| R_{ℓ}^0 | 20.767 ± 0.025 | 20.7495 ± 0.0080 [20.7337, 20.7652] | 20.7460 ± 0.0087 [20.7291, 20.7630] | 0.8 | 20.760 ± 0.022 [20.717, 20.803] | 0.2 | 20.7470 ± 0.0087 [20.7297, 20.7638] | 0.8 |
| $A_{\text{FB}}^{0,\ell}$ | 0.0171 ± 0.0010 | 0.01624 ± 0.00010 [0.01604, 0.01644] | 0.01623 ± 0.00010 [0.01602, 0.01643] | 0.9 | 0.01631 ± 0.00024 [0.01585, 0.01679] | 0.8 | 0.01615 ± 0.00012 [0.01592, 0.01638] | 1.0 |
| \mathcal{A}_{ℓ} (SLD) | 0.1513 ± 0.0021 | 0.14713 ± 0.00047 [0.14622, 0.14806] | 0.14715 ± 0.00049 [0.14619, 0.14811] | 1.9 | 0.1475 ± 0.0011 [0.1454, 0.1496] | 1.6 | 0.14674 ± 0.00053 [0.14570, 0.14779] | 2.1 |
| R_b^0 | 0.21629 ± 0.00066 | 0.21588 ± 0.00010 [0.21567, 0.21608] | 0.21587 ± 0.00011 [0.21566, 0.21608] | 0.6 | 0.21545 ± 0.00038 [0.21470, 0.21617] | 1.1 | 0.21591 ± 0.00011 [0.21570, 0.21611] | 0.6 |
| R_c^0 | 0.1721 ± 0.0030 | 0.172206 ± 0.000054 [0.172100, 0.172313] | 0.172206 ± 0.000054 [0.172099, 0.172312] | 0.0 | 0.17239 ± 0.00019 [0.17204, 0.17277] | -0.1 | 0.172190 ± 0.000055 [0.172082, 0.172297] | -0.1 |
| $A_{\text{FB}}^{0,b}$ | 0.0996 ± 0.0016 | 0.10315 ± 0.00033 [0.10250, 0.10380] | 0.10316 ± 0.00034 [0.10248, 0.10384] | -2.2 | 0.10338 ± 0.00076 [0.10187, 0.10488] | -2.1 | 0.10287 ± 0.00037 [0.10214, 0.10361] | -2.0 |
| $A_{\text{FB}}^{0,c}$ | 0.0707 ± 0.0035 | 0.07370 ± 0.00025 [0.07321, 0.07418] | 0.07370 ± 0.00026 [0.07319, 0.07421] | -0.9 | 0.07391 ± 0.00059 [0.07275, 0.07507] | -0.9 | 0.07348 ± 0.00028 [0.07293, 0.07403] | -0.8 |
| \mathcal{A}_b | 0.923 ± 0.020 | 0.934739 ± 0.000040 [0.934661, 0.934819] | 0.934740 ± 0.000040 [0.934661, 0.934820] | -0.6 | 0.93461 ± 0.00017 [0.93427, 0.93494] | -0.6 | 0.934721 ± 0.000041 [0.934640, 0.934802] | -0.6 |
| \mathcal{A}_c | 0.670 ± 0.027 | 0.66783 ± 0.00023 [0.66737, 0.66828] | 0.66783 ± 0.00023 [0.66737, 0.66829] | 0.1 | 0.66815 ± 0.00054 [0.66711, 0.66922] | 0.1 | 0.66766 ± 0.00024 [0.66718, 0.66814] | 0.1 |
| \mathcal{A}_s | 0.895 ± 0.091 | 0.935652 ± 0.000043 [0.935568, 0.935736] | 0.935653 ± 0.000043 [0.935568, 0.935736] | -0.4 | 0.935713 ± 0.000099 [0.935518, 0.935906] | -0.5 | 0.935622 ± 0.000045 [0.935533, 0.935709] | -0.5 |
| $\text{BR}_{W \ell \bar{\nu}_{\ell}}$ | 0.10860 ± 0.00090 | 0.108381 ± 0.000022 [0.108338, 0.108424] | 0.108381 ± 0.000022 [0.108338, 0.108424] | 0.2 | 0.10829 ± 0.00011 [0.10808, 0.10851] | 0.3 | 0.108386 ± 0.000023 [0.108340, 0.108432] | 0.2 |
| $\sin^2 \theta_{\text{eff}}^l$ (HC) | 0.23143 ± 0.00025 | 0.231507 ± 0.000060 [0.231389, 0.231623] | 0.231511 ± 0.000061 [0.231392, 0.231632] | -0.3 | 0.23146 ± 0.00014 [0.23119, 0.23173] | -0.1 | 0.231558 ± 0.000068 [0.231426, 0.231691] | -0.5 |
| R_{uc} | 0.1660 ± 0.0090 | 0.172227 ± 0.000033 [0.172163, 0.172292] | 0.172227 ± 0.000033 [0.172164, 0.172292] | -0.7 | 0.17242 ± 0.00018 [0.17207, 0.17278] | -0.7 | 0.172211 ± 0.000034 [0.172145, 0.172277] | -0.7 |

LOCAL vs GLOBAL SIGNIFICANCE

- Considering the whole set of EWPO, what is the global agreement with the SM?
- Compute global p-value of the “full prediction”, taking into account experimental and theoretical correlations:
 - $p=1.2 \cdot 10^{-4}$, i.e. 3.9σ (standard scenario)
 - $p=0.27$, i.e. 1.1σ (conservative scenario)

M_W BEYOND THE SM

- Add heavy NP that decouples, leaving its virtual footprints:
 - dominantly in gauge Boson propagators: “oblique” NP
 - in the complete set of gauge-invariant dimension six operators (SMEFT)
- For explicit models (Z' , composite Higgs, etc.) see e.g. Strumia '22

OBLIQUE NP

- Assume NP dominant contribution is in gauge Boson propagators:

$$S = -16\pi\Pi_{30}^{\text{NP}'}(0) = 16\pi [\Pi_{33}^{\text{NP}'}(0) - \Pi_{3Q}^{\text{NP}'}(0)],$$

$$T = \frac{4\pi}{s_W^2 c_W^2 M_Z^2} [\Pi_{11}^{\text{NP}}(0) - \Pi_{33}^{\text{NP}}(0)],$$

$$U = 16\pi [\Pi_{11}^{\text{NP}'}(0) - \Pi_{33}^{\text{NP}'}(0)]$$

- EWPO are modified as follows:

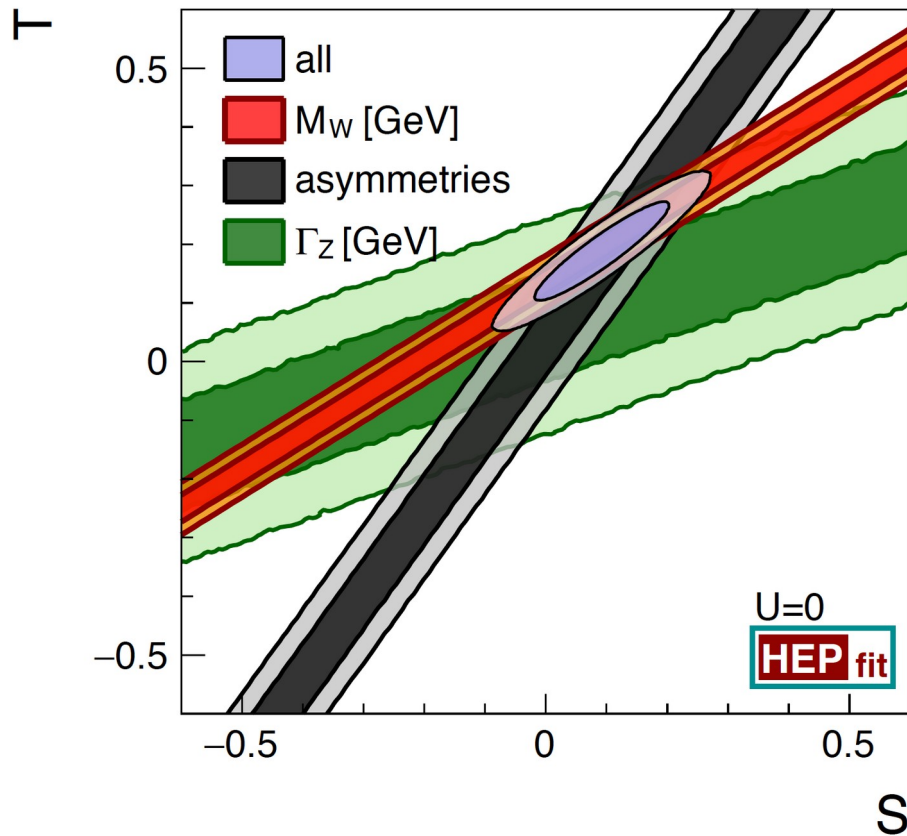
$$- \delta\Gamma_Z \propto -10(3 - 8s_W^2) S + (63 - 126s_W^2 - 40s_W^4) T$$

$$- \delta M_W, \delta\Gamma_W \propto S - 2c_W^2 T - \frac{(c_W^2 - s_W^2) U}{2s_W^2}$$

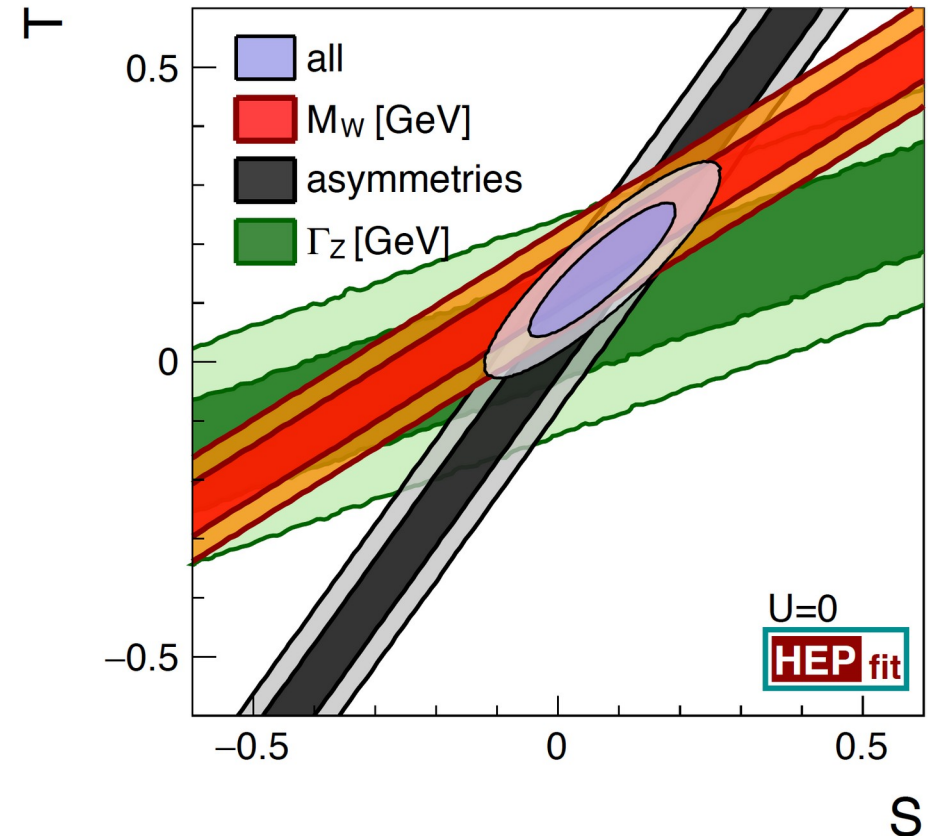
$$- \text{all other observables: } S - 4c_W^2 s_W^2 T$$

OBLIQUE NP: $U=0$

standard



conservative



OBLIQUE NP: RESULTS

- Compare models using the Information Criterion:

$$IC \equiv -2\overline{\log \mathcal{L}} + 4\sigma_{\log \mathcal{L}}^2$$

| | Result | Correlation | | Result | Correlation | | |
|----------|--------------------------------------------------|-------------|------|---------------------------------------------------|-------------|-------|------|
| | (IC _{ST} /IC _{SM} = 24.5/73.9) | | | (IC _{STU} /IC _{SM} = 25.3/73.9) | | | |
| <i>S</i> | 0.092 ± 0.073 | 1.00 | | 0.004 ± 0.096 | 1.00 | | |
| <i>T</i> | 0.188 ± 0.056 | 0.93 | 1.00 | 0.04 ± 0.12 | 0.91 | 1.00 | |
| <i>U</i> | — | — | — | 0.122 ± 0.087 | -0.65 | -0.88 | 1.00 |

- No significant gain in IC for U≠0

| Model | Pred. M_W [GeV] | Pull | Pred. M_W [GeV] | Pull |
|-------|-------------------------|--------------|-----------------------------|--------------|
| | <i>standard average</i> | | <i>conservative average</i> | |
| SM | 80.3499 ± 0.0056 | 6.1 σ | 80.3505 ± 0.0077 | 3.0 σ |
| ST | 80.366 ± 0.029 | 1.4 σ | 80.367 ± 0.029 | 1.2 σ |
| STU | 80.32 ± 0.54 | 0.2 σ | 80.32 ± 0.54 | 0.2 σ |

THE SMEFT

- Most general gauge-invariant Lagrangian built with SM fields up to dimension d (here $d=6$)
- Some relevant operators in the "Warsaw basis":

$$\begin{aligned}\mathcal{O}_{\phi WB} &= (\phi^\dagger \sigma_i \phi) W_{\mu\nu}^i B^{\mu\nu}, \quad \rightarrow \mathbf{S} \\ \mathcal{O}_{\phi D} &= (\phi^\dagger D^\mu \phi)^* (\phi^\dagger D_\mu \phi), \quad \rightarrow \mathbf{T} \\ \mathcal{O}_{ll} &= (\bar{l}_L \gamma^\mu l_L)(\bar{l}_L \gamma^\mu l_L)\end{aligned}$$

$$\begin{aligned}\mathcal{O}_{\phi l}^{(1)} &= (\phi^\dagger i \overleftrightarrow{D}_\mu \phi)(\bar{l}_L \gamma^\mu l_L), \\ \mathcal{O}_{\phi l}^{(3)} &= (\phi^\dagger i \overleftrightarrow{D}_\mu^i \phi)(\bar{l}_L \sigma_i \gamma^\mu l_L), \\ \mathcal{O}_{\phi e} &= (\phi^\dagger i \overleftrightarrow{D}_\mu \phi)(\bar{e}_R \gamma^\mu e_R), \\ \mathcal{O}_{\phi q}^{(1)} &= (\phi^\dagger i \overleftrightarrow{D}_\mu \phi)(\bar{q}_L \gamma^\mu q_L), \\ \mathcal{O}_{\phi q}^{(3)} &= (\phi^\dagger i \overleftrightarrow{D}_\mu^i \phi)(\bar{q}_L \sigma_i \gamma^\mu q_L), \\ \mathcal{O}_{\phi u} &= (\phi^\dagger i \overleftrightarrow{D}_\mu \phi)(\bar{u}_R \gamma^\mu u_R), \\ \mathcal{O}_{\phi d} &= (\phi^\dagger i \overleftrightarrow{D}_\mu \phi)(\bar{d}_R \gamma^\mu d_R),\end{aligned}$$

M_W IN THE SMEFT

- Eight independent combinations of dim. 6 operators contribute to EWPO. In the

Warsaw basis:

$$\hat{C}_{\varphi f}^{(1)} = C_{\varphi f}^{(1)} - \frac{Y_f}{2} C_{\varphi D}, \quad f = l, q, e, u, d, \quad (6)$$

$$\hat{C}_{\varphi f}^{(3)} = C_{\varphi f}^{(3)} + \frac{c_w^2}{4s_w^2} C_{\varphi D} + \frac{c_w}{s_w} C_{\varphi WB}, \quad f = l, q, \quad (7)$$

$$\hat{C}_{ll} = \frac{1}{2}((C_{ll})_{1221} + (C_{ll})_{2112}) = (C_{ll})_{1221}, \quad (8)$$

- Again, one independent combination enters only M_W and Γ_w , namely: $\hat{C}_{\varphi l}^{(3)} - \hat{C}_{ll}/2$; very loose prediction for M_W from Γ_w

| Model | Pred. M_W [GeV] | Pull | Pred. M_W [GeV] | Pull |
|-------|-------------------------|---------------|-----------------------------|---------------|
| | <i>standard average</i> | | <i>conservative average</i> | |
| SMEFT | 80.66 ± 1.68 | -0.1σ | 80.66 ± 1.68 | -0.1σ |

SMEFT: FIT RESULTS

| | (IC _{SMEFT} /IC _{SM} = 31.8/73.9) | | | | | | | | |
|-----------------------------|-----------------------------------------------------|-------|-------|-------|-------|-------|-------|-------|------|
| $\hat{C}_{\varphi l}^{(1)}$ | -0.007 ± 0.011 | 1.00 | | | | | | | |
| $\hat{C}_{\varphi l}^{(3)}$ | -0.039 ± 0.015 | -0.68 | 1.00 | | | | | | |
| $\hat{C}_{\varphi e}$ | -0.015 ± 0.009 | 0.48 | 0.04 | 1.00 | | | | | |
| $\hat{C}_{\varphi q}^{(1)}$ | -0.018 ± 0.044 | -0.02 | -0.06 | -0.13 | 1.00 | | | | |
| $\hat{C}_{\varphi q}^{(3)}$ | -0.111 ± 0.043 | -0.03 | 0.04 | -0.16 | -0.37 | 1.00 | | | |
| $\hat{C}_{\varphi u}$ | 0.08 ± 0.15 | 0.06 | -0.04 | 0.04 | 0.61 | -0.77 | 1.00 | | |
| $\hat{C}_{\varphi d}$ | -0.63 ± 0.25 | -0.13 | -0.05 | -0.30 | 0.40 | 0.59 | -0.05 | 1.00 | |
| \hat{C}_{ll} | -0.021 ± 0.028 | -0.80 | 0.95 | -0.10 | -0.06 | -0.01 | -0.04 | -0.05 | 1.00 |

standard averages

- Cirigliano et al. noted that a combination of these operators also contributes to first-row CKM unitarity violation. This effect can be compensated by $C^{(3)}_{lq}$ which does not enter EWPO. However, $C^{(3)}_{lq}$ can be constrained by LHC e.g. in $pp \rightarrow ll$.

EWPO BEYOND THE SM

| | Measurement | ST | STU | SMEFT |
|-------------------------------------------------------------------------|-----------------------|-------------------------|-------------------------|-----------------------|
| M_W [GeV] | 80.4093 ± 0.0079 | 80.4065 ± 0.0075 | 80.4090 ± 0.0080 | 80.4090 ± 0.0080 |
| Γ_W [GeV] | 2.085 ± 0.042 | 2.09190 ± 0.00070 | 2.09215 ± 0.00075 | 2.0779 ± 0.0070 |
| $\sin^2 \theta_{\text{eff}}^{\text{lept}} (Q_{\text{FB}}^{\text{had}})$ | 0.2324 ± 0.0012 | 0.23143 ± 0.00014 | 0.23147 ± 0.00014 | |
| $P_{\tau}^{\text{pol}} = \mathcal{A}_{\ell}$ | 0.1465 ± 0.0033 | 0.1478 ± 0.0011 | 0.1474 ± 0.0011 | 0.1488 ± 0.0015 |
| Γ_Z [GeV] | 2.4955 ± 0.0023 | 2.4979 ± 0.0011 | 2.4951 ± 0.0022 | 2.4955 ± 0.0023 |
| σ_h^0 [nb] | 41.480 ± 0.033 | 41.4910 ± 0.0080 | 41.4905 ± 0.0075 | 41.482 ± 0.033 |
| R_{ℓ}^0 | 20.767 ± 0.025 | 20.7505 ± 0.0085 | 20.7510 ± 0.0080 | 20.769 ± 0.025 |
| $A_{\text{FB}}^{0,\ell}$ | 0.0171 ± 0.0010 | 0.01638 ± 0.00023 | 0.01631 ± 0.00024 | 0.01660 ± 0.00032 |
| \mathcal{A}_{ℓ} (SLD) | 0.1513 ± 0.0021 | 0.1478 ± 0.0011 | 0.1474 ± 0.0011 | 0.1488 ± 0.0015 |
| R_b^0 | 0.21629 ± 0.00066 | 0.21591 ± 0.00011 | 0.21591 ± 0.00011 | 0.21632 ± 0.00066 |
| R_c^0 | 0.1721 ± 0.0030 | 0.172195 ± 0.000055 | 0.172200 ± 0.000050 | 0.17159 ± 0.00099 |
| $A_{\text{FB}}^{0,b}$ | 0.0996 ± 0.0016 | 0.10361 ± 0.00076 | 0.10337 ± 0.00078 | 0.1009 ± 0.0014 |
| $A_{\text{FB}}^{0,c}$ | 0.0707 ± 0.0035 | 0.07405 ± 0.00058 | 0.07387 ± 0.00060 | 0.0734 ± 0.0023 |
| \mathcal{A}_b | 0.923 ± 0.020 | 0.934810 ± 0.000100 | 0.93478 ± 0.00010 | 0.903 ± 0.013 |
| \mathcal{A}_c | 0.670 ± 0.027 | 0.66813 ± 0.00053 | 0.66797 ± 0.00054 | 0.658 ± 0.020 |
| \mathcal{A}_s | 0.895 ± 0.091 | 0.935705 ± 0.000095 | 0.935680 ± 0.000100 | 0.905 ± 0.013 |
| $\text{BR}_{Wl\bar{\nu}_{\ell}}$ | 0.10860 ± 0.00090 | 0.108385 ± 0.000025 | 0.108380 ± 0.000020 | 0.10900 ± 0.00039 |
| $\sin^2 \theta_{\text{eff}}^{\text{ll}} (\text{HC})$ | 0.23143 ± 0.00025 | 0.23143 ± 0.00014 | 0.23147 ± 0.00014 | |
| R_{uc} | 0.1660 ± 0.0090 | 0.172220 ± 0.000030 | 0.172220 ± 0.000030 | 0.17162 ± 0.00099 |

Conclusions

- Remarkable experimental progress in m_t and M_W , but tensions among measurements present in both cases: outcome of M_W and m_t averaging group badly needed!
- Taken at face value, M_W implies a local (global) discrepancy at the 6.1σ (3.9σ) level, calling for NP
- Oblique/decoupling NP can accommodate the tension for scales close to the EW scale if loop-mediated, or at the TeV scale if tree-level/strongly interacting.
- If a more conservative averaging procedure is followed, the tension becomes much milder and the implications on NP much softer.
- **More measurements of M_W (and m_t) crucial!**