

# A substandard Candle: The low- $\nu$ Method

Rencontres du Vietnam: Neutrino  
2022/07/22

Luke Pickering for the NUISANCE Collaboration



# Motivation: Measuring the Neutrino Flux

$$N_{\text{near}}(E_{\text{obs}}) = \int dE_{\nu} \Phi_{\text{near}}(E_{\nu}) \cdot \sigma(E_{\nu}) \cdot D_{\text{near}}$$

$$N_{\text{far}}(E_{\text{obs}}) = \int dE_{\nu} \Phi_{\text{far}}(E_{\nu}) \cdot P_{\text{osc}}(E_{\nu}) \cdot \sigma(E_{\nu}) \cdot D_{\text{far}}$$

Can access

Want to know

Extract oscillation probability from observed rate.

- Observed rate is convolution of flux, cross-section, and oscillations
- Current uncertainty on flux (~5-10%) and cross-section (~10%)
- Use near detector to constrain rate+shape = flux  $\otimes$  cross-section
- Use constrained model to predict observation for a oscillation hypothesis to test

# Motivation: Measuring the Neutrino Flux

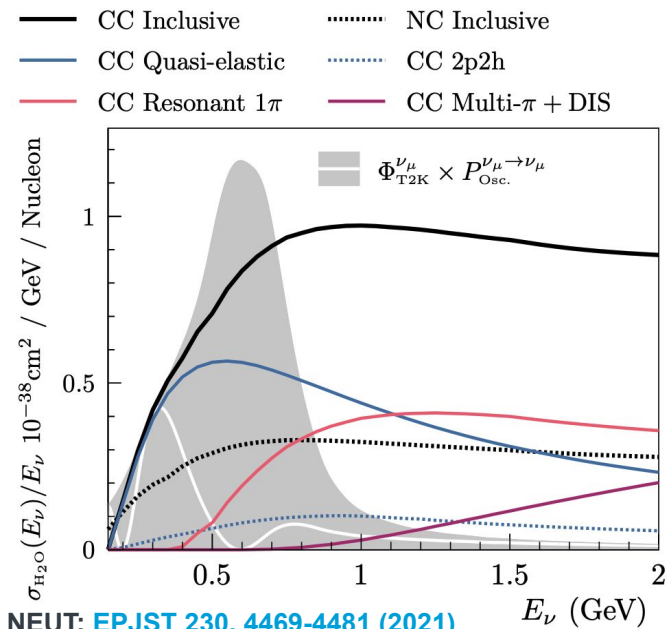
$$N_{\text{near}}(E_{\text{obs}}) = \int dE_{\nu} \Phi_{\text{near}}(E_{\nu}) \cdot \sigma(E_{\nu}) \cdot D_{\text{near}}$$

Ideally would use near detector to constrain flux and cross-section separately

*in situ* measurements are difficult:

- Wide band beam
- Cross-sections changing rapidly
- Detector effects cause significant smearing

Have to get creative...



NEUT: [EPJST 230, 4469-4481 \(2021\)](#)

# Getting Creative

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$$N_{\text{near}}(E_{\text{obs}}) = \int dE_{\nu} \Phi_{\text{near}}(E_{\nu}) \cdot \sigma(E_{\nu}) \cdot \mathbf{D}_{\text{near}}$$

General approach: Isolate events with a well-known cross-section and well understood detector effects

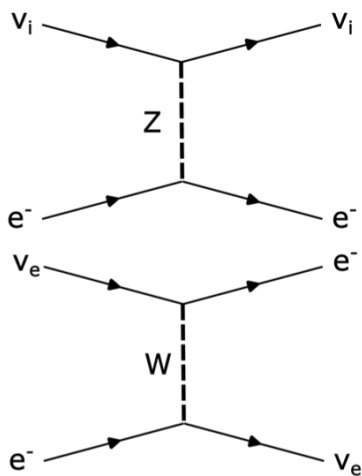
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Neutrino–electron elastic scattering:

- Simple interaction with no nuclear effects
- Rate is OOM lower than neutrino–nucleon scattering
- Future beams will produce sizeable sample
- Good for flux normalization



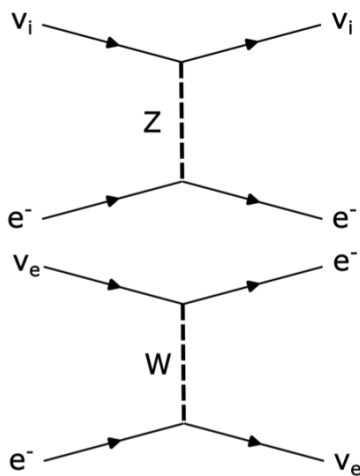
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Can try to isolate neutrino–nucleon events with a well-known cross-section:

- Select very-elastic events
- → Cross-section saturates at some  $E_{\nu}$
- → Almost all energy to visible final-state charged lepton
- Minimal energy lost to nuclear response/hadron production

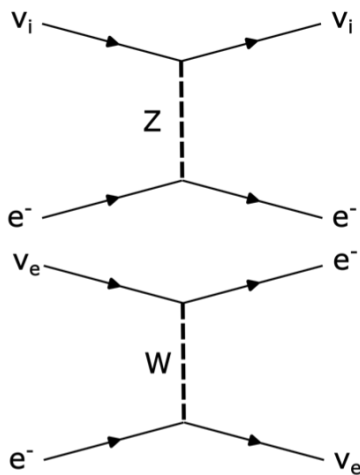
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## Neutrino reactions in the low- $y$ region

R. Belusevic

*Department of Physics, University College, University of London, London WC1E 6BT, United Kingdom*

D. Rein

*III. Physikalisches Institut, Rheinisch-Westfälische Technische Hochschule Aachen, D-5100 Aachen, Federal Republic of Germany*

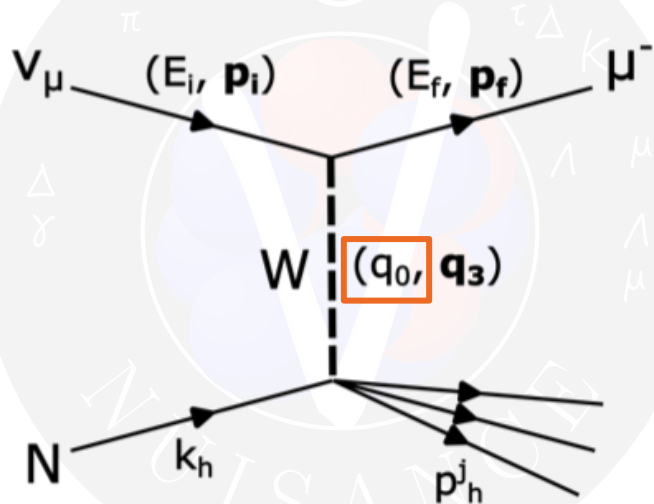
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The physics of nonscaling components in the region of low energy transfer (low- $y$  region) is described. The following neutrino-induced processes were considered: resonance production, quasi-elastic scattering, and coherent meson production off nuclei or nuclear fragments. It is shown that the total exclusive cross section in a certain kinematical domain is energy independent at high energies (above 20 GeV). This fact can, in principle, be used for relative normalization of the neutrino flux.

[Phys. Rev. D \*\*38\*\*, 2753 \(1988\)](#)

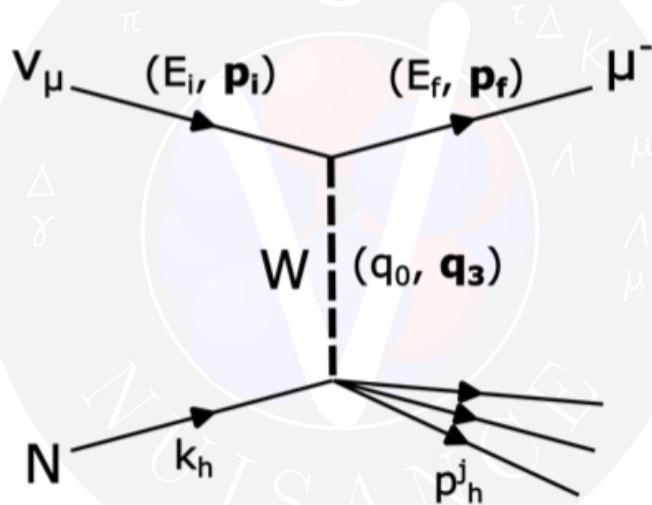


# A Problem in Terminology



- Originally the "low- $y$ " region
    - Low inelasticity  $\rightarrow$  High elasticity
  - "low- $\nu$ " coined in terms of DIS formalism
  - $\nu$  is ambiguous in neutrino-scattering physics
  - Has also been called "fixed  $\nu_0$ " method
  - Electron-scattering folks often use  $\omega = E_i - E_f$
- 
- I will try to use  $q_0$  as in the 0<sup>th</sup> component of the 4-momentum transfer  $q$ -vector.

# The "low- $\nu$ " Method

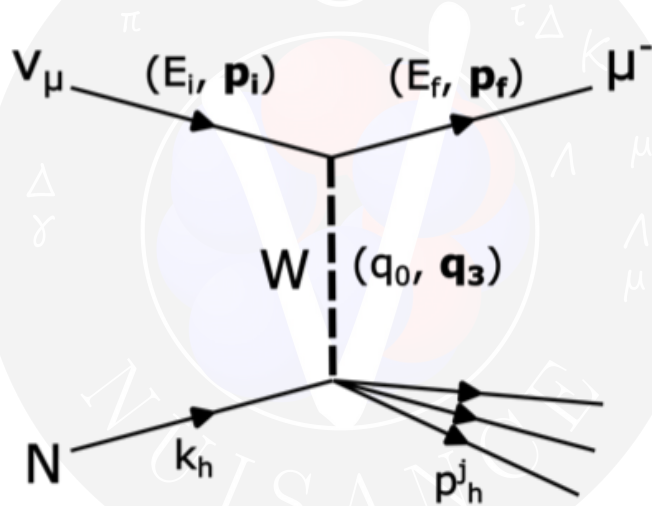


$+(-)$  for (anti)neutrino

$$\frac{d\sigma}{dq_0} = \frac{G_F^2 M}{\pi} \int_0^1 \left( F_2 - \frac{q_0}{E_\nu} [F_2^{(+)} x F_3] + \frac{q_0}{2E_\nu^2} \left[ \frac{Mx(1-R_L)}{1+R_L} F_2 \right] + \frac{q_0^2}{2E_\nu^2} \left[ \frac{F_2}{1+R_L} {}^{(+)} x F_3 \right] \right) dx, \quad (1)$$

- Write down inclusive DIS cross-section in terms of nucleon structure functions
- Notice that if  $\frac{q_0}{E_\nu} \ll 1$  any neutrino energy dependence disappears

# The "low- $\nu$ " Method

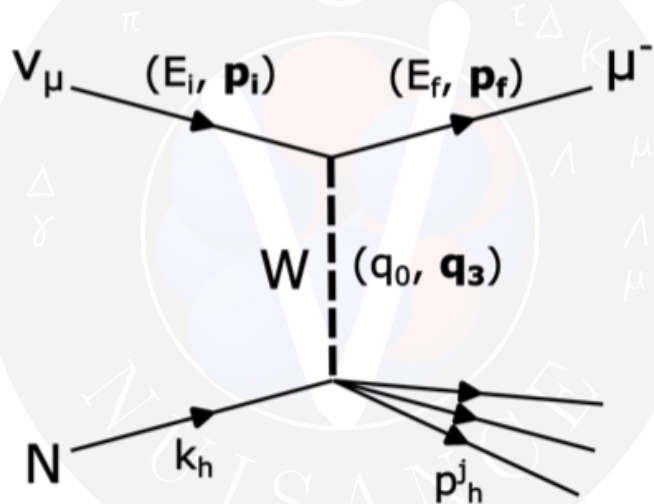


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# The "low- $\nu$ " Method



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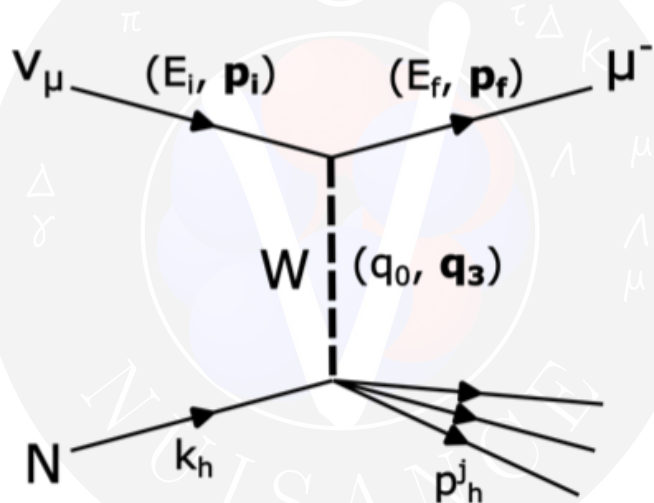
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$$N_{\text{near}}(E_{\text{obs}}) = \int dE_\nu \Phi_{\text{near}}(E_\nu) \cdot \sigma(E_\nu) \cdot D_{\text{near}}$$

constant

- Write down inclusive DIS cross-section in terms of nucleon structure functions
- Notice that if  $\frac{q_0}{E_\nu} \ll 1$  any neutrino energy dependence disappears
- A flat cross-section can be used to access the shape of the flux from the event rate!

# The Implicit Assumptions

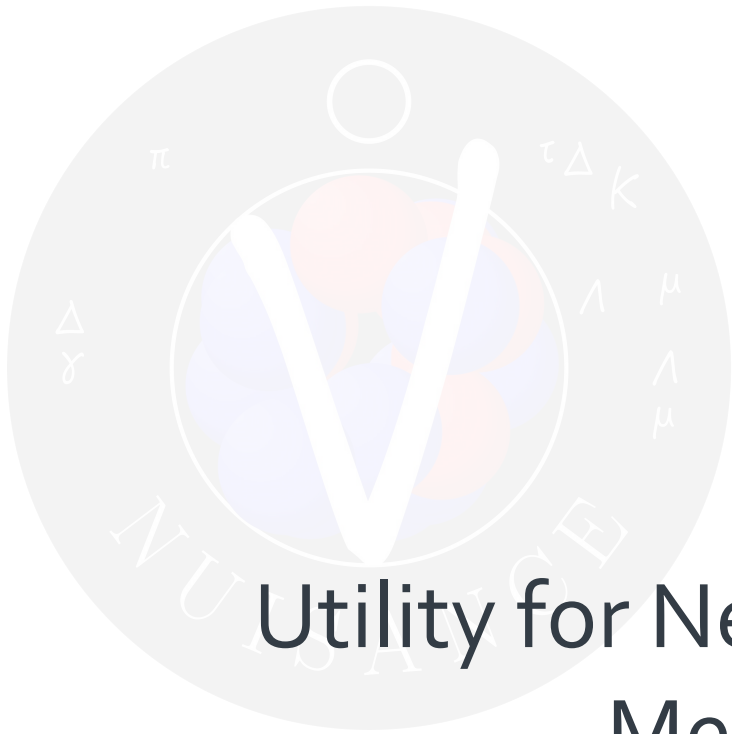


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The "low- $\nu$ " method works well if:

1. Eq. (1) describes the cross-section well in the region of interest
2. A sample with 'low enough'  $q_0$  can be unambiguously experimentally selected
3. The neutrino energy for events in the sample can be accurately reconstructed.



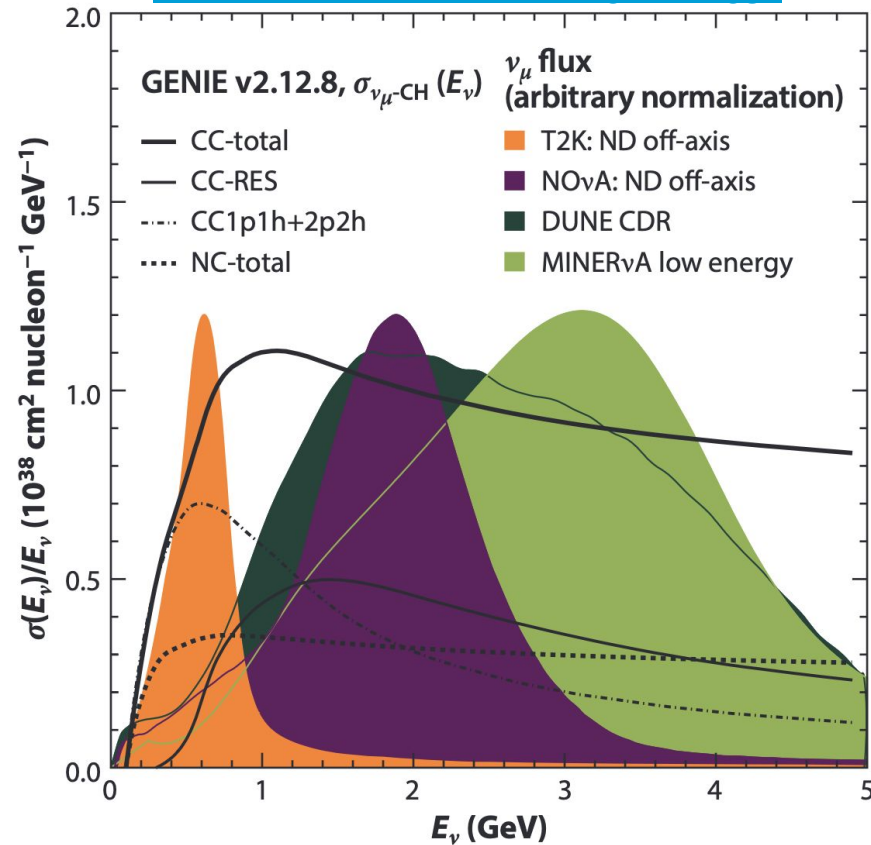
# Utility for Near-future Oscillation Measurements

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# Experimental Fluxes

Relevant neutrino energy range:  $< 5\text{GeV}$

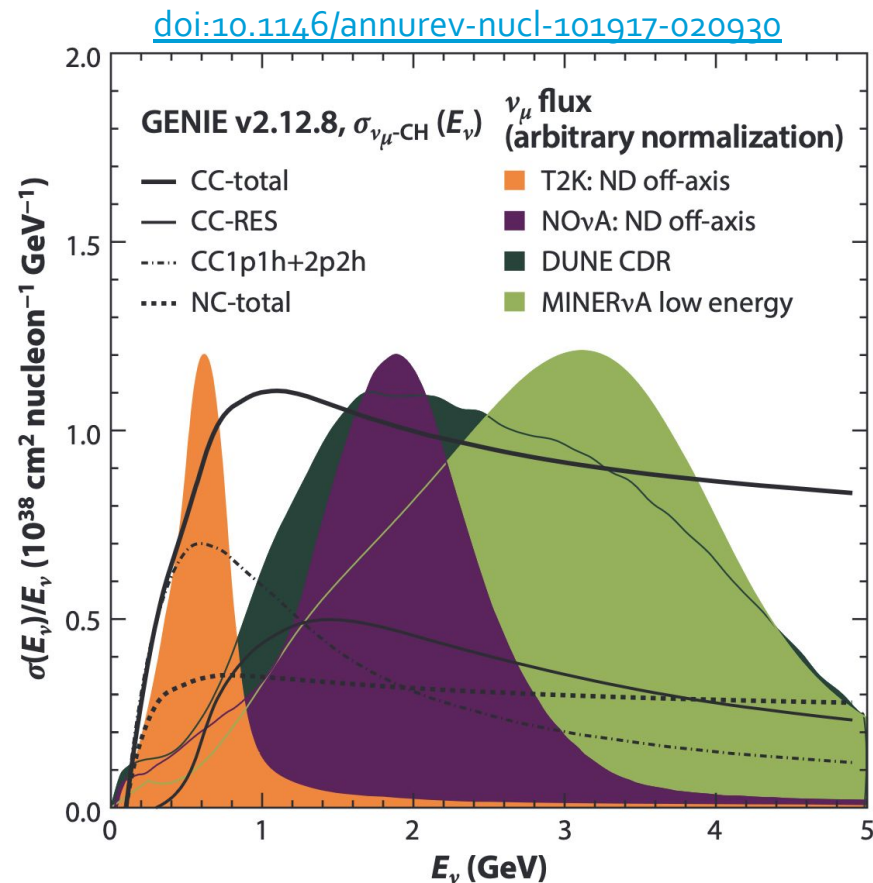
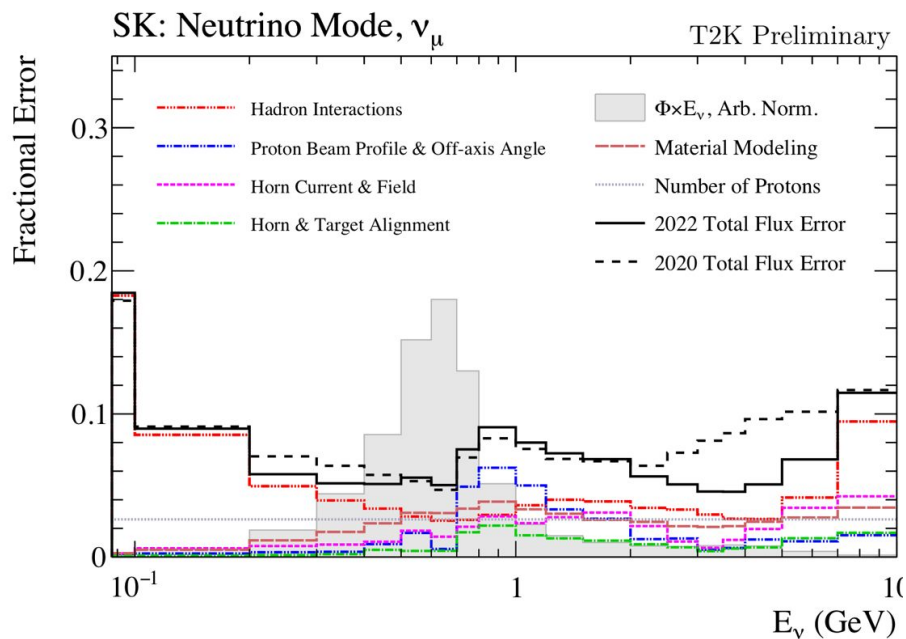
[doi:10.1146/annurev-nucl-101917-020930](https://doi.org/10.1146/annurev-nucl-101917-020930)



# Experimental Fluxes

Relevant neutrino energy range:  $< 5\text{GeV}$

Current flux uncertainty:  $\sim 5\%$  in the peak





## Neutrino reactions in the low- $y$ region

R. Belusevic

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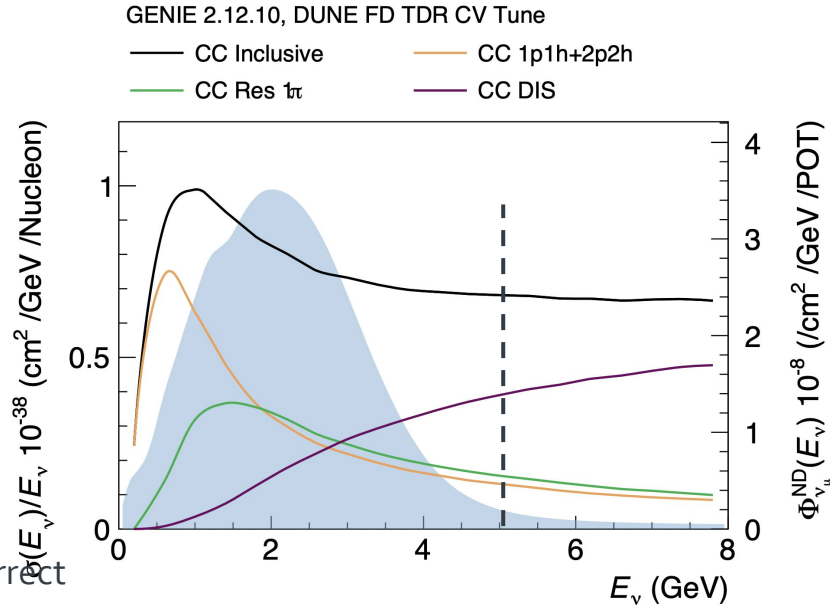
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[Phys. Rev. D \*\*38\*\*, 2753 \(1988\)](#)

# The Implicit Assumptions

- By 5 GeV the charged-current cross-section is \*mostly\* DIS.
- But we need  $q_0/E\nu \ll 1$ 
  - **DIS** formalism, but a selection of very-not **DIS** events...
- At what  $(q_0, E\nu)$  does Eq. (1) break down?
  - Recent implementations ask the interaction model to correct for any non-constant behavior [\[EPJC 72, 1973 \(2012\)\]](#)



The "low- $\nu$ " method works well if:

1. **Eq. (1) describes the cross-section well in the region of interest**
2. A sample with 'low enough'  $q_0$  can be unambiguously experimentally selected
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# Model Motivations

Need to investigate how well such a correction can be known with current simulation.

Use a spread of reasonable model predictions:

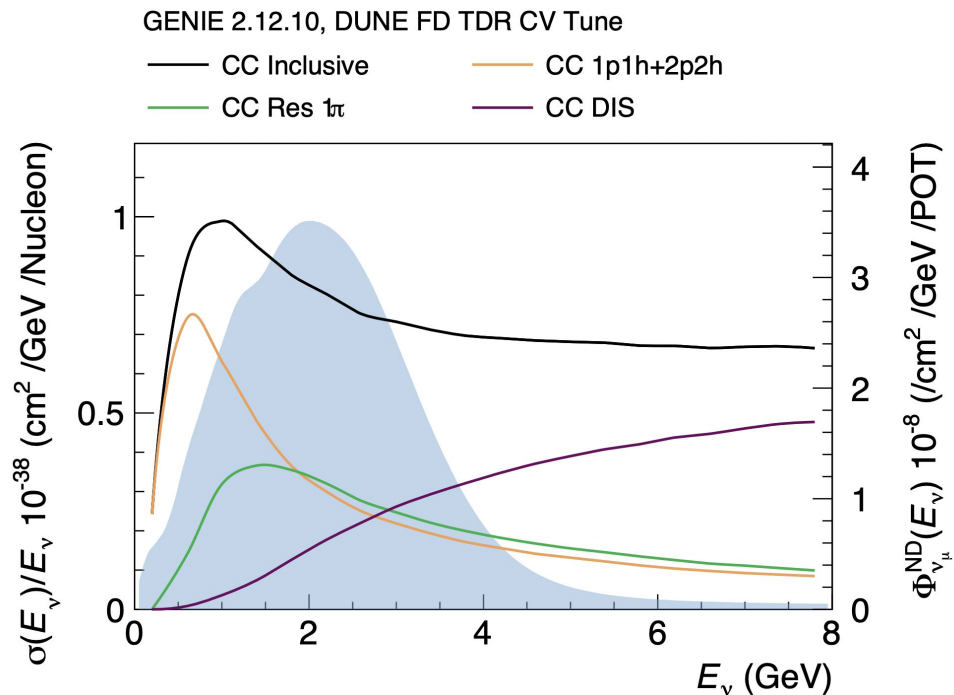
- $\Delta$  Not a replacement for well motivated theoretical uncertainties...
- $\gamma$  But they don't exist, so we have to make do with *semi*-sensible choices
- **GENIE:**
  - Version 2 – Used by MINERvA in their Low- $\nu$  constraint [[Phys. Rev. D 94, 112007](#)]
  - Version 3 – Currently used by NOvA, MicroBooNE for their analyses
- **NEUT:** Used by T2K
- **NuWro:** Performs well in comparisons to world cross-section data
- **GiBUU:** Sophisticated hadron-transport and quite different neutrino–nucleon model choices, also performs well in world data comparisons
- **SUSAv2 and CRPA:** State-of-the-art nuclear response modelling for pionless events

# A View From The DUNE

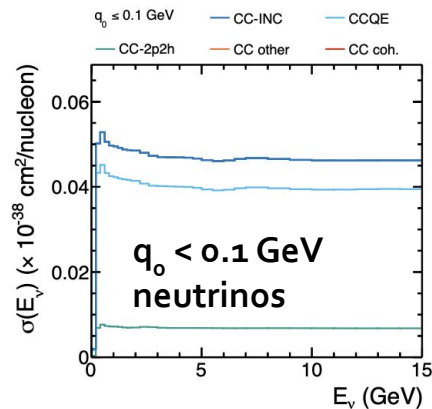
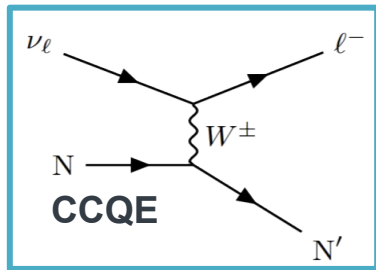
## Study Configuration:

- Ar<sub>40</sub> target
- Neutrinos and anti-neutrinos
- Spread of *reasonable* model choices

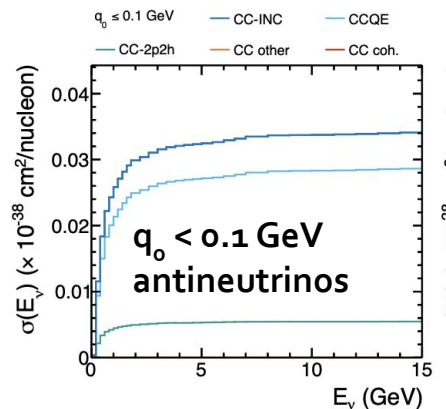
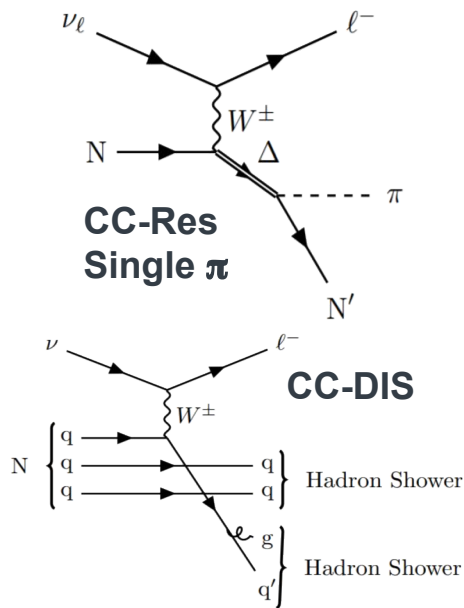
How well-understood is a perfect 'low- $q_0$ ' sample of events for a DUNE-like target?



# GENIE<sub>3</sub>: Total Cross Section

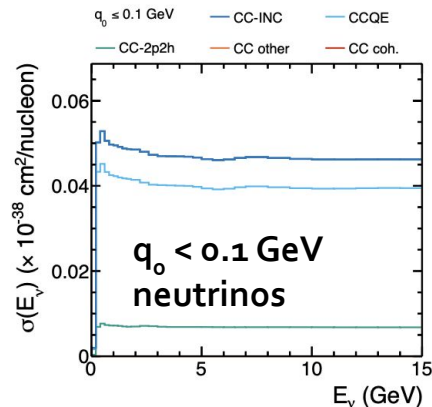
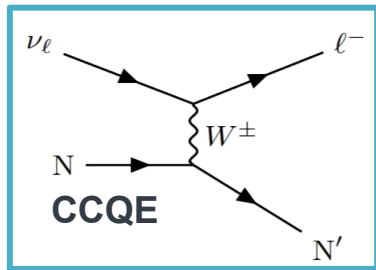
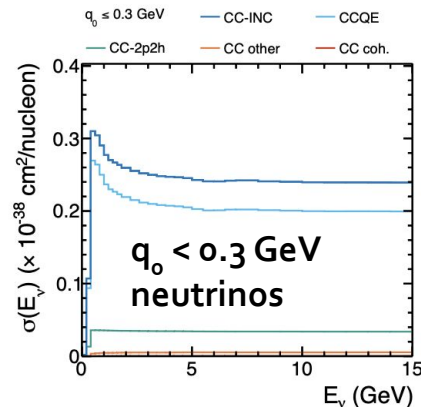
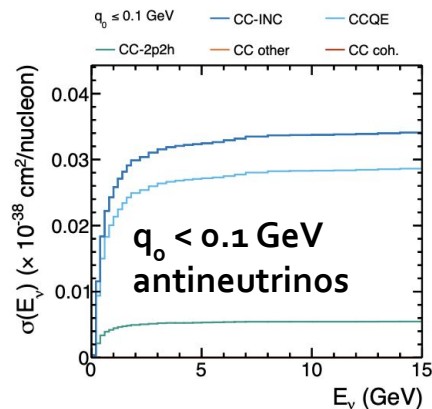
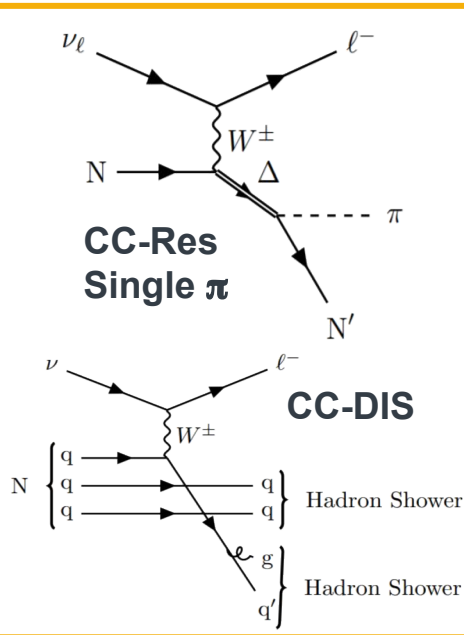
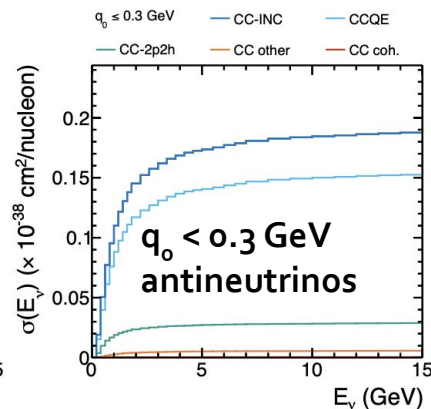


(a)  $\nu_\mu$ - $^{40}\text{Ar}$ ,  $q_0 \leq 0.1 \text{ GeV}$

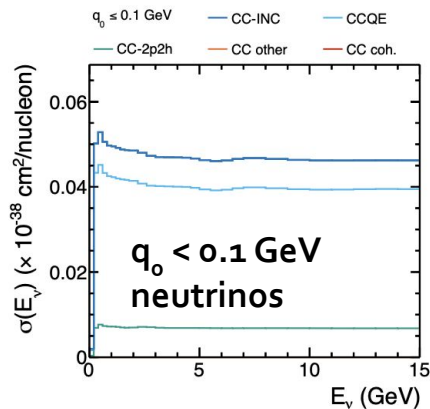
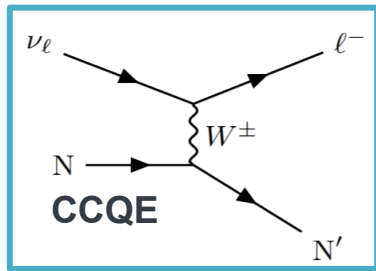
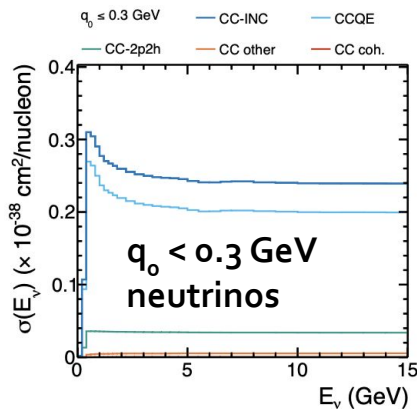
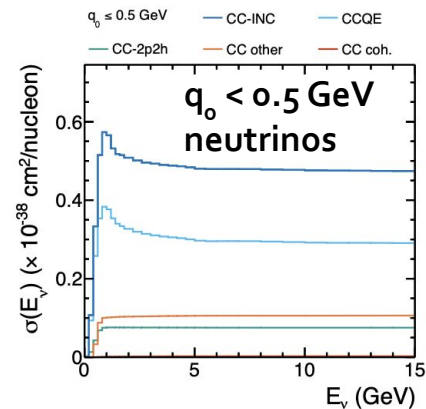
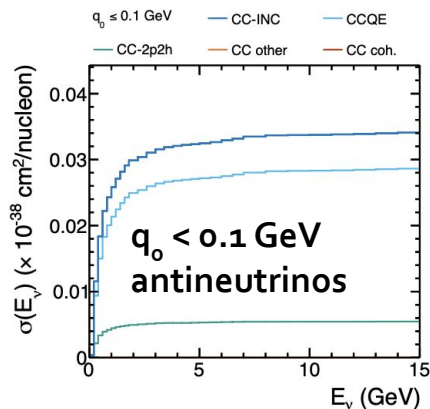
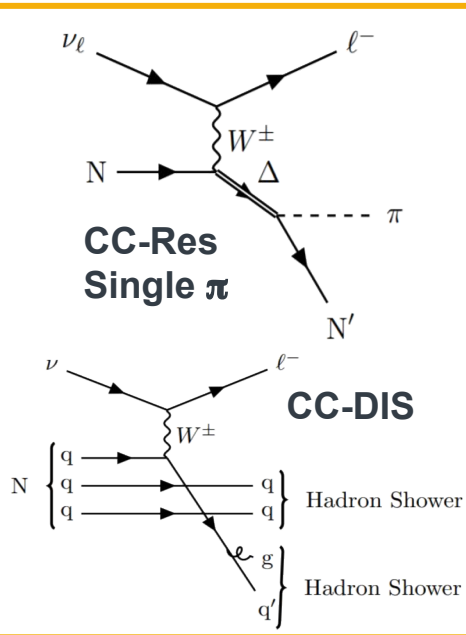
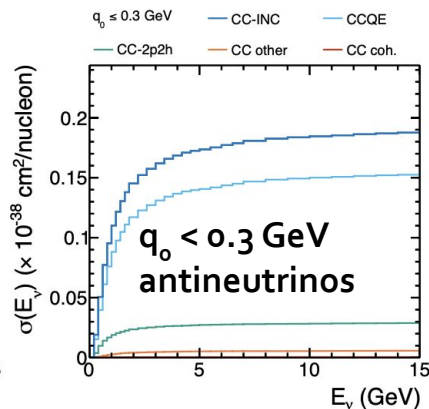
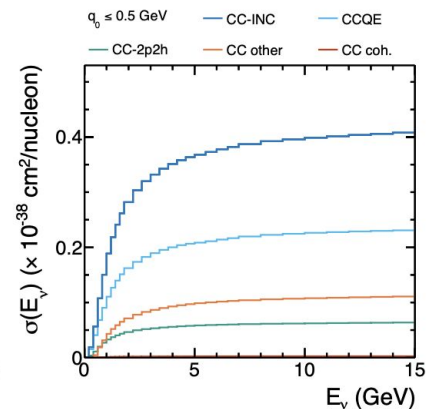


(d)  $\bar{\nu}_\mu$ - $^{40}\text{Ar}$ ,  $q_0 \leq 0.1 \text{ GeV}$

# GENIE<sub>3</sub>: Total Cross Section

(a)  $\nu_\mu-^{40}\text{Ar}$ ,  $q_0 \leq 0.1 \text{ GeV}$ (b)  $\nu_\mu-^{40}\text{Ar}$ ,  $q_0 \leq 0.3 \text{ GeV}$ (d)  $\bar{\nu}_\mu-^{40}\text{Ar}$ ,  $q_0 \leq 0.1 \text{ GeV}$ (e)  $\bar{\nu}_\mu-^{40}\text{Ar}$ ,  $q_0 \leq 0.3 \text{ GeV}$

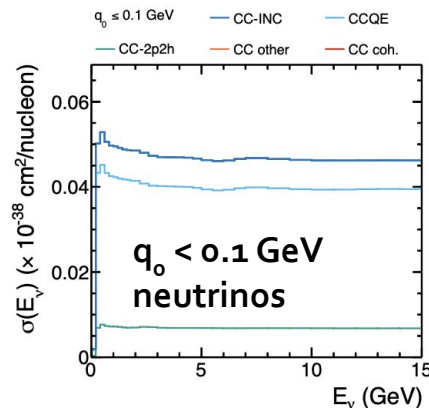
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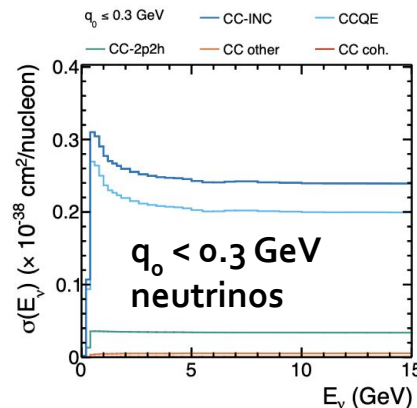
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## Observations:

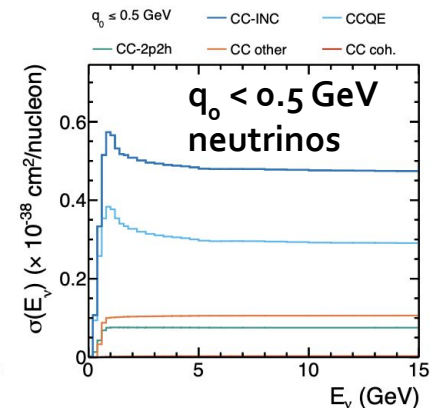
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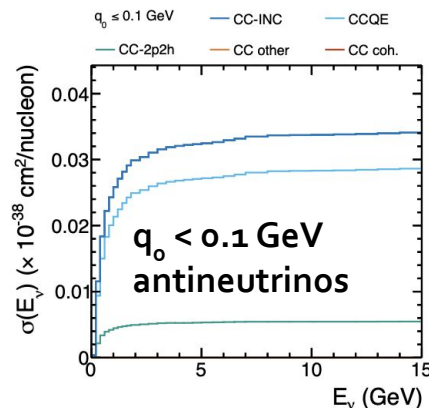
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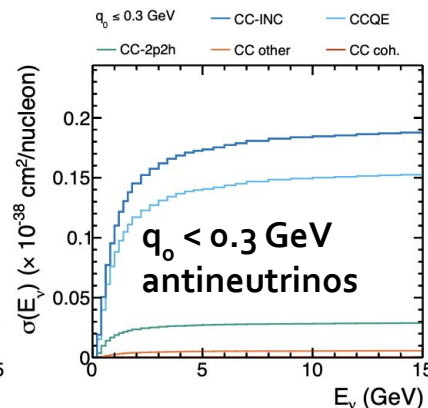
(b)  $\nu_\mu$ -<sup>40</sup>Ar,  $q_0 \leq 0.3$  GeV



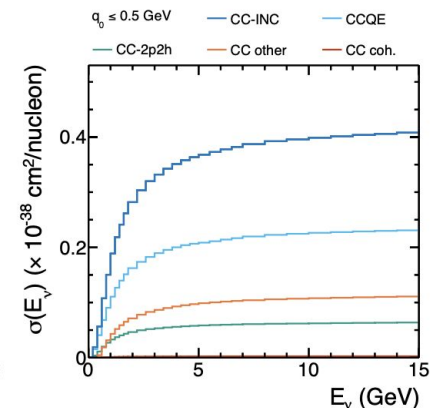
(c)  $\nu_\mu$ -<sup>40</sup>Ar,  $q_0 \leq 0.5$  GeV



(d)  $\bar{\nu}_\mu$ -<sup>40</sup>Ar,  $q_0 \leq 0.1$  GeV



(e)  $\bar{\nu}_\mu$ -<sup>40</sup>Ar,  $q_0 \leq 0.3$  GeV

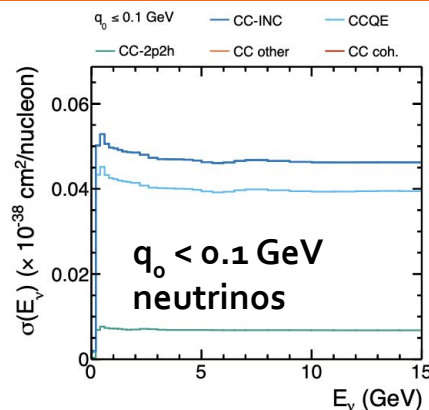
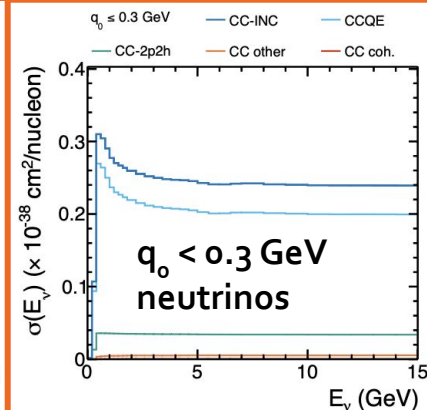
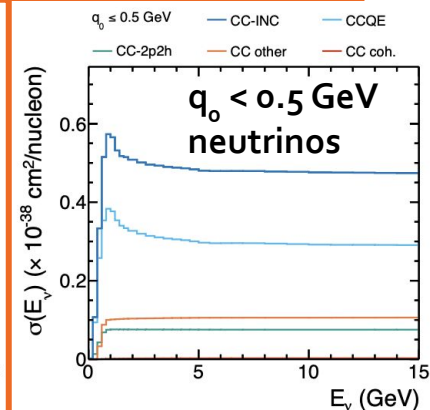
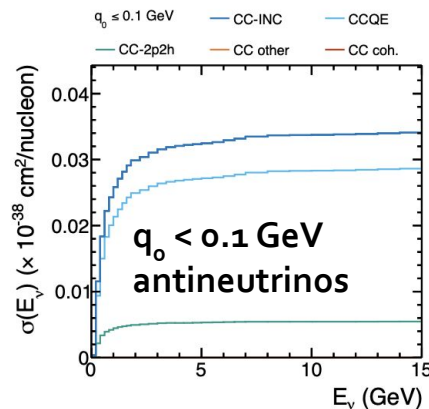
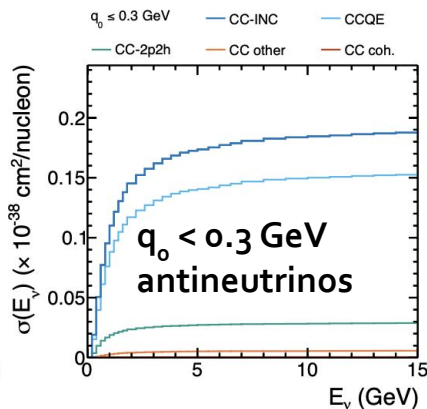
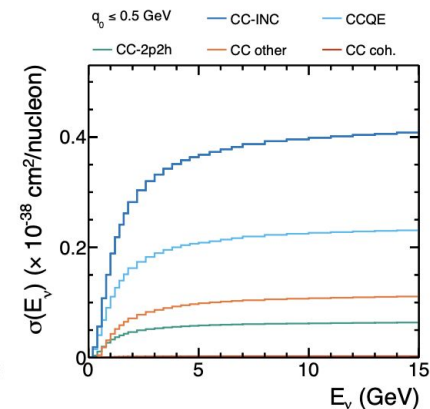


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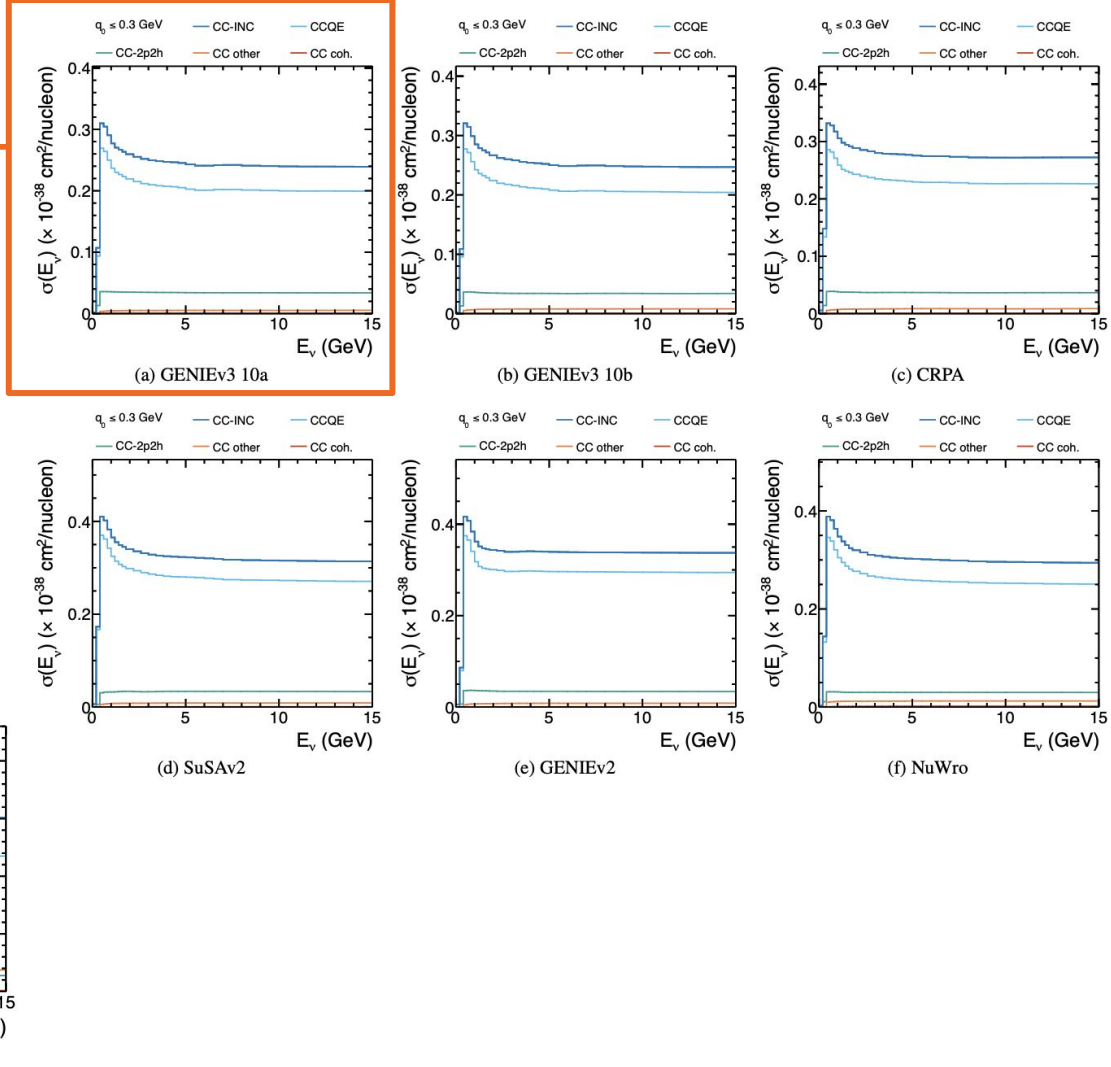
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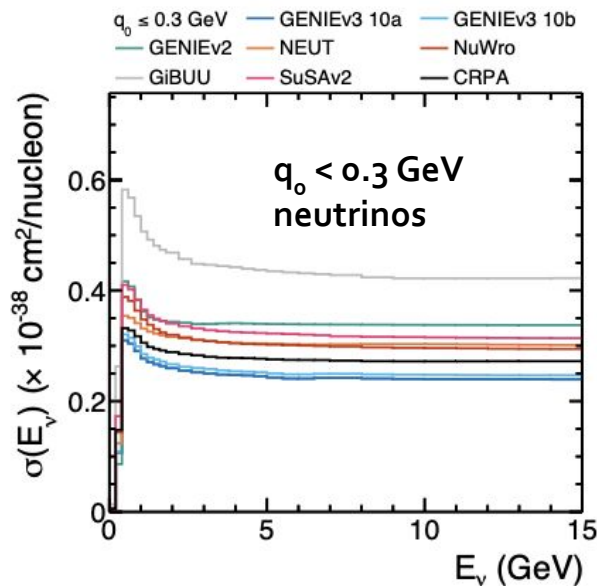
# Alternate Predictions

- General trends between predictions are similar by eye.
- GiBUU has very different 2p2h strength due to a model choice made for strength of correlated NN pairs.

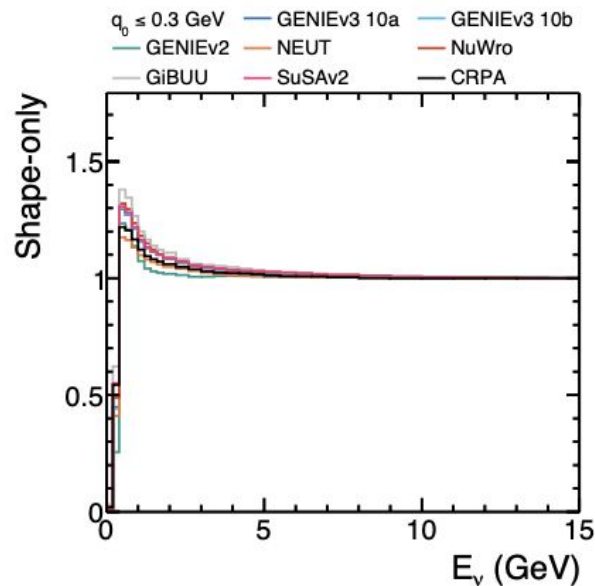


# Comparing the Predictions

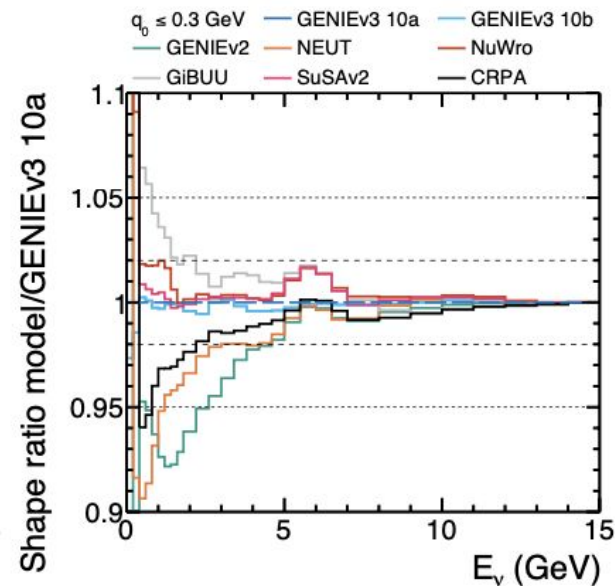
- Want to evaluate uncertainty on the relative constantness of the low- $q_0$  cross-section
  - Take GENIEv3 10a as the reference model and examine variation of predicted low- $q_0$  shapes
- For illustration have chosen  $q_0 < 0.3$  GeV



(a) Model comparison



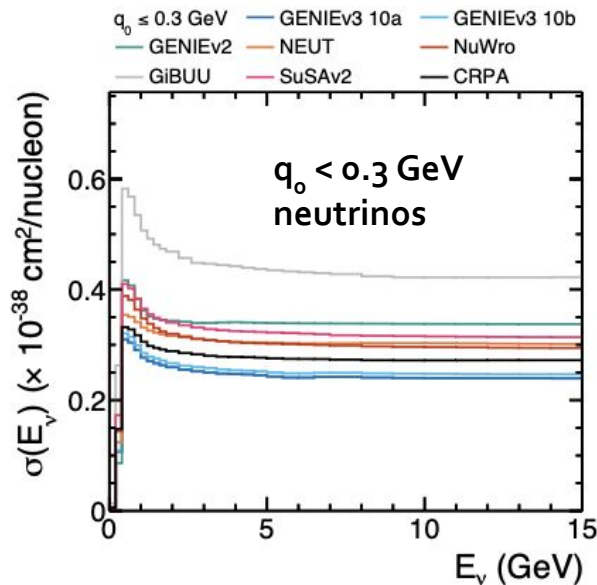
(b) Shape-only



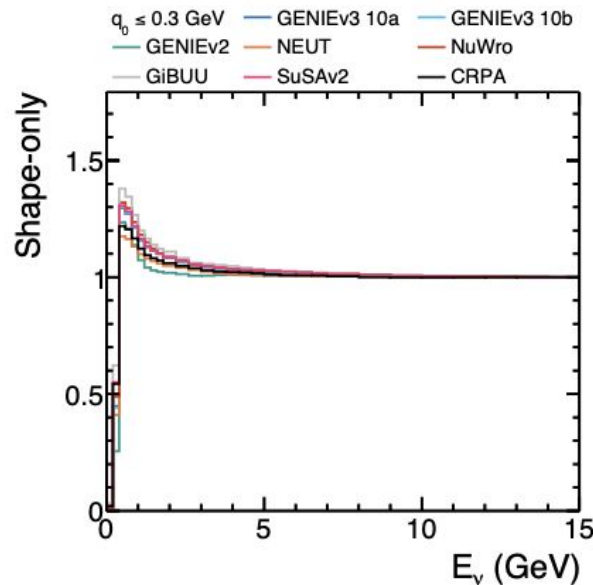
(c) Shape-only ratio

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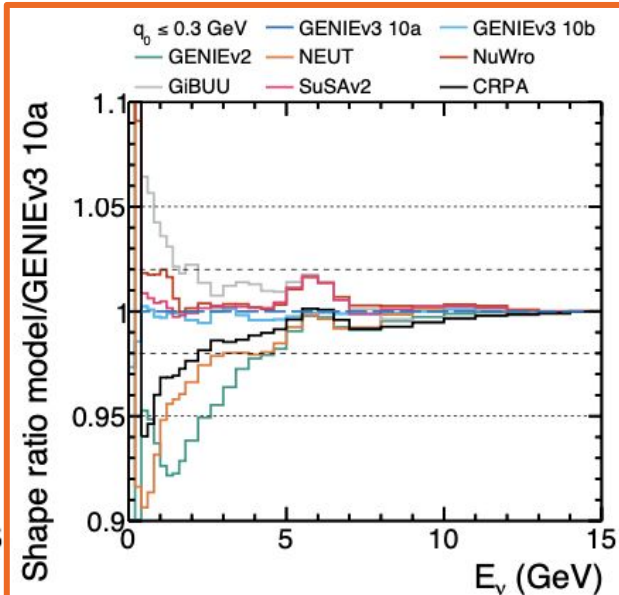
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(a) Model comparison



(b) Shape-only

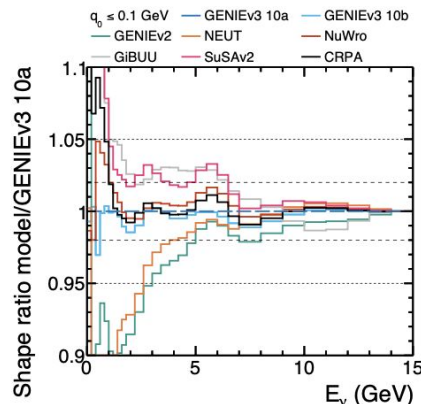


(c) Shape-only ratio

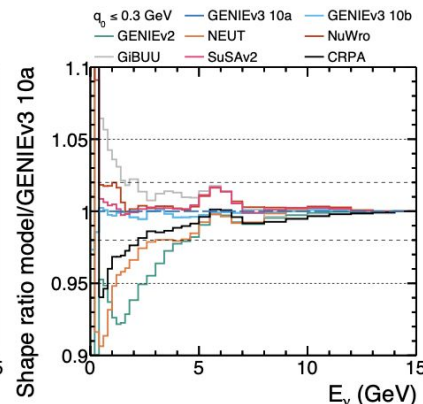
# Model Spread

Important LBL oscillation region 0.5–5 GeV:

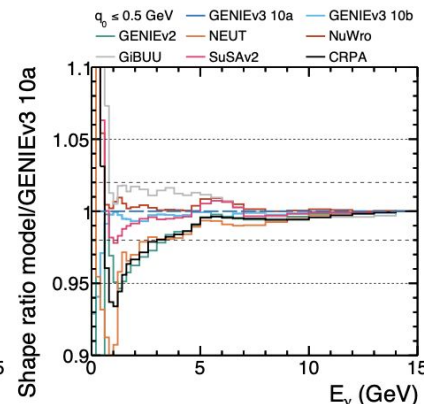
- Spread of 2–5% seen for neutrinos
- A bit larger for antineutrinos



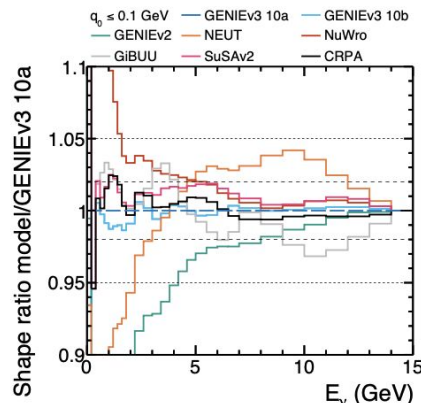
(a)  $\nu_{\mu}^{-40}\text{Ar}$ ,  $q_0 \leq 0.1$  GeV



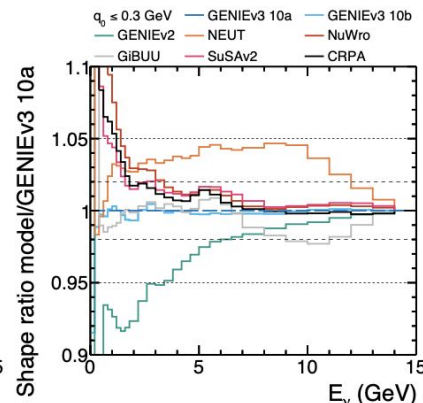
(b)  $\nu_{\mu}^{-40}\text{Ar}$ ,  $q_0 \leq 0.3$  GeV



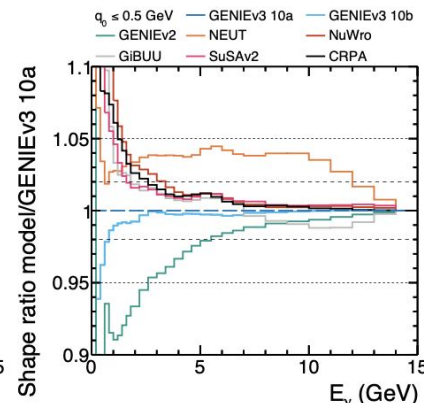
(c)  $\nu_{\mu}^{-40}\text{Ar}$ ,  $q_0 \leq 0.5$  GeV



(d)  $\bar{\nu}_{\mu}^{-40}\text{Ar}$ ,  $q_0 \leq 0.1$  GeV



(e)  $\bar{\nu}_{\mu}^{-40}\text{Ar}$ ,  $q_0 \leq 0.3$  GeV



(f)  $\bar{\nu}_{\mu}^{-40}\text{Ar}$ ,  $q_0 \leq 0.5$  GeV



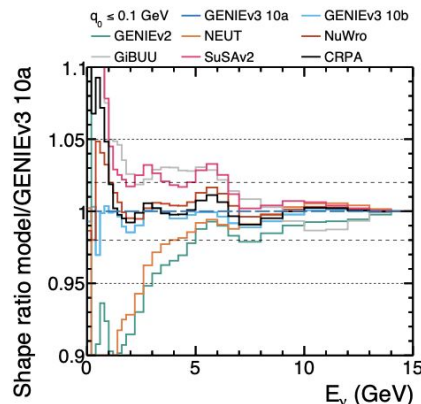
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Important LBL oscillation region 0.5–5 GeV:

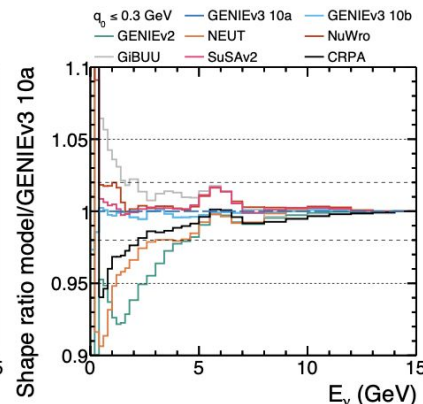
- Spread of 2–5% seen for neutrinos
- A bit larger for antineutrinos

Counterintuitively the spread reduces for higher  $q_0$  cuts:

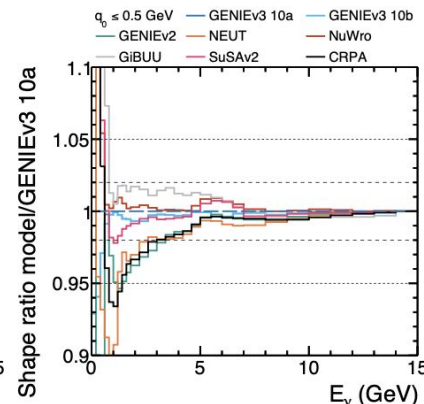
- Opposite behavior than predicted by Eq. (1)
- Likely due to nuclear effects that do not fit well into Eq. (1)
- Pion-production and DIS models are more similar between generators



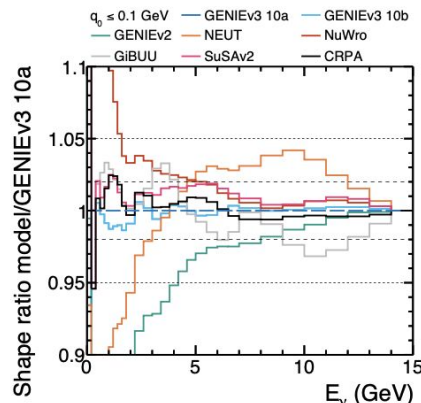
(a)  $\nu_{\mu}^{-40}\text{Ar}$ ,  $q_0 \leq 0.1$  GeV



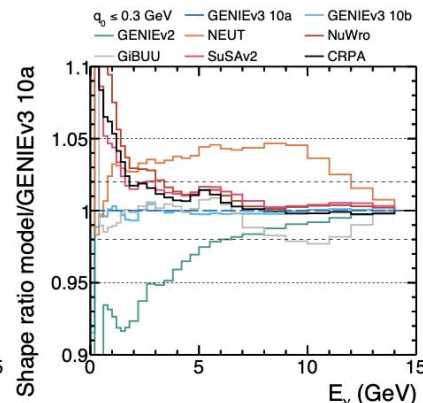
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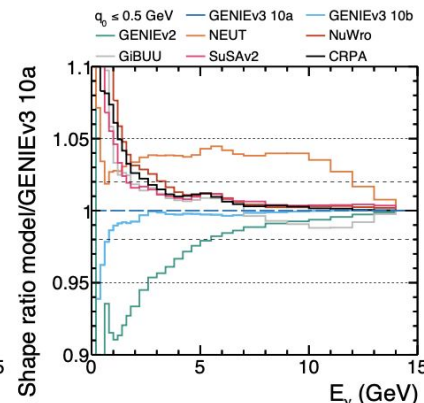
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(d)  $\bar{\nu}_{\mu}^{-40}\text{Ar}$ ,  $q_0 \leq 0.1$  GeV

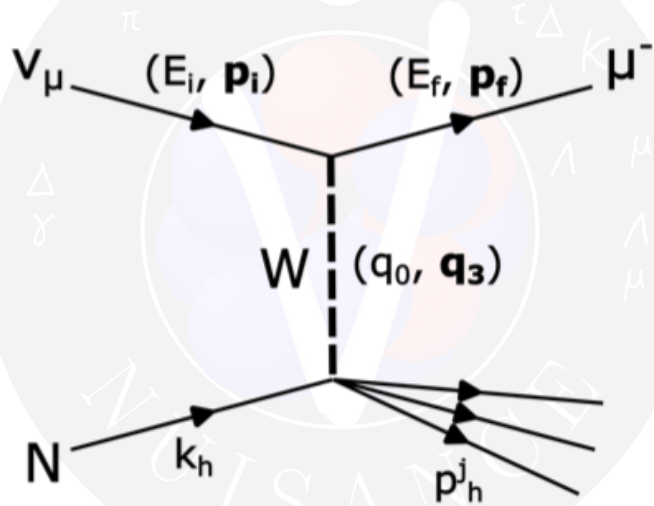


(e)  $\bar{\nu}_{\mu}^{-40}\text{Ar}$ ,  $q_0 \leq 0.3$  GeV



(f)  $\bar{\nu}_{\mu}^{-40}\text{Ar}$ ,  $q_0 \leq 0.5$  GeV

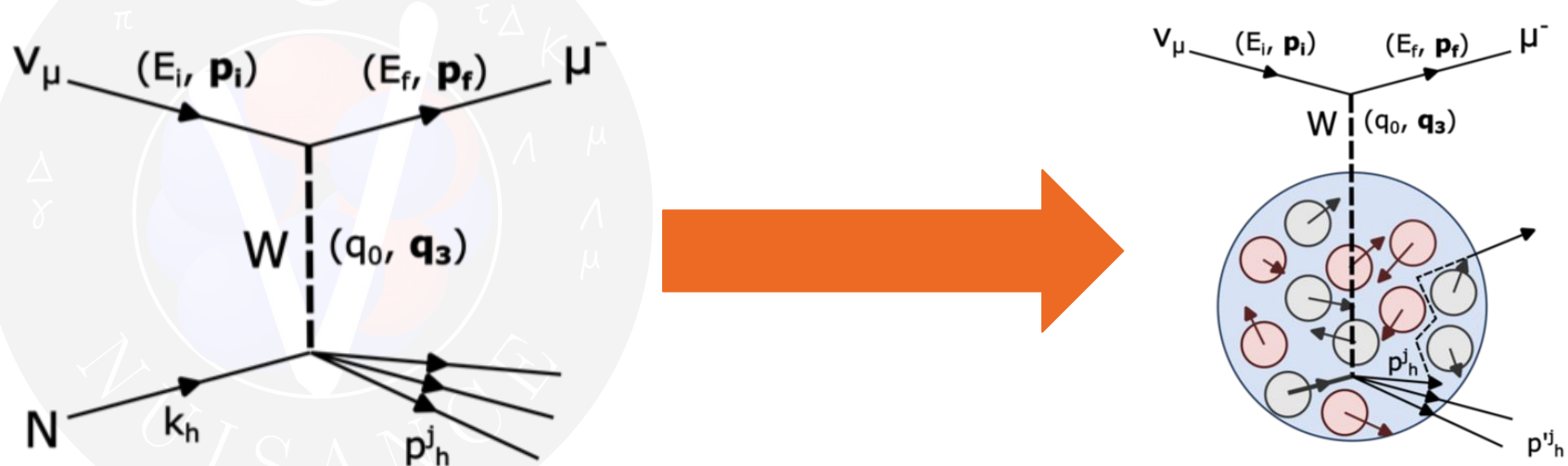
# The Implicit Assumptions



The "low- $\nu$ " method works well if:

1. Eq. (1) describes the cross-section well in the region of interest
2. A sample with 'low enough'  $q_0$  can be unambiguously experimentally selected
3. The neutrino energy for events in the sample can be accurately reconstructed.

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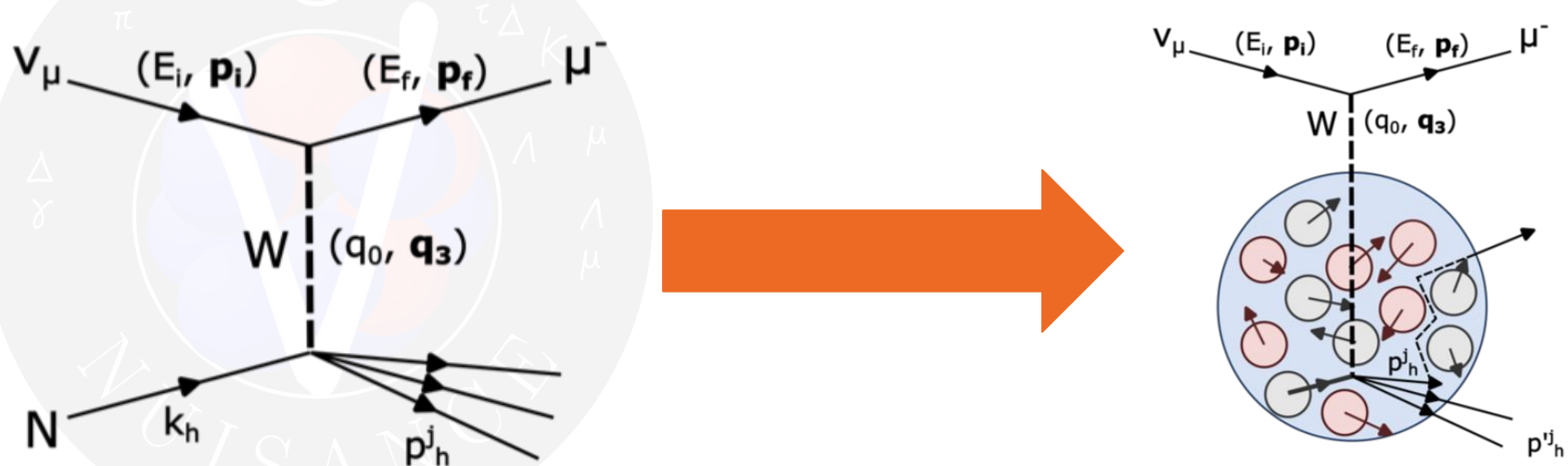


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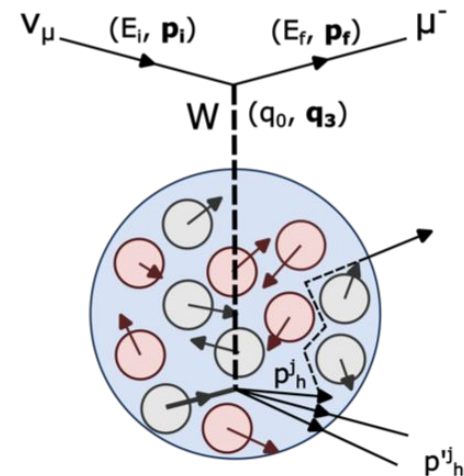


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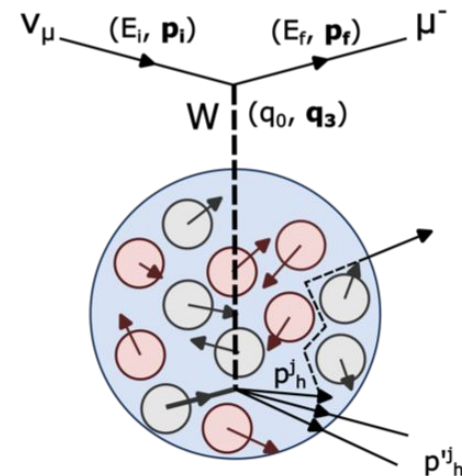
# Selecting a Low- $q_0$ Sample

- Cannot access true  $q_0$  because we cannot know incoming neutrino energy
  - Reconstruct from the hadronic side



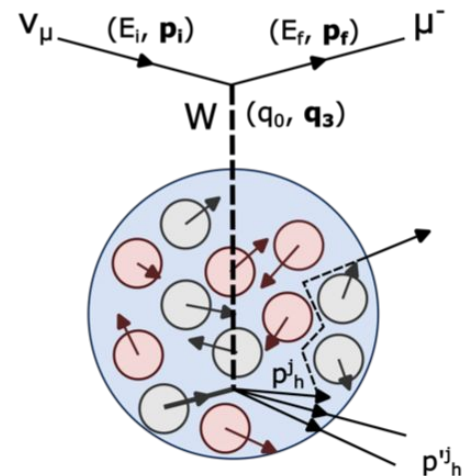
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- Define three  $q_0$  proxy variables
  - Perfect detector, measures all hadrons
  - Optimistic detector, can't see neutrons but tags every pion
  - Pessimistic detector, misses all neutrons and charged-pion masses



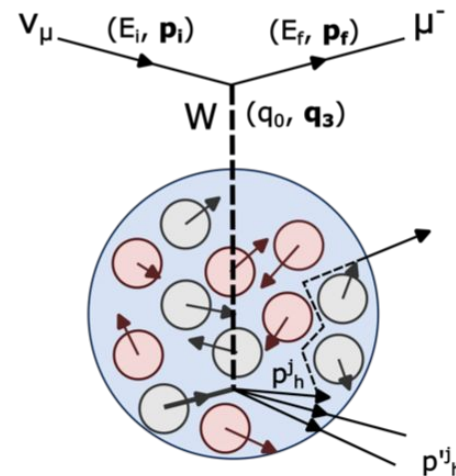
$$E_{\text{had}}^{\text{true}} = \left( \sum_{i=n,p} E_{\text{kin}}^i \right) + \left( \sum_{i=\pi^\pm, \pi^0, \gamma} E_{\text{total}}^i \right)$$

$$E_{\text{had}}^{\text{reco}} = \left( \sum_{i=p} E_{\text{kin}}^i \right) + \left( \sum_{i=\pi^\pm, \pi^0, \gamma} E_{\text{total}}^i \right)$$

$$E_{\text{avail}} = \left( \sum_{i=\pi^\pm, p} E_{\text{kin}}^i \right) + \left( \sum_{i=\pi^0, \gamma} E_{\text{total}}^i \right)$$

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  - Missed neutrons
- Define three  $q_0$  proxy variables
  - Perfect detector, measures all hadrons
  - Optimistic detector, can't see neutrons but tags every pion
  - **Calorimetric detector, misses all neutrons and charged-pion masses**



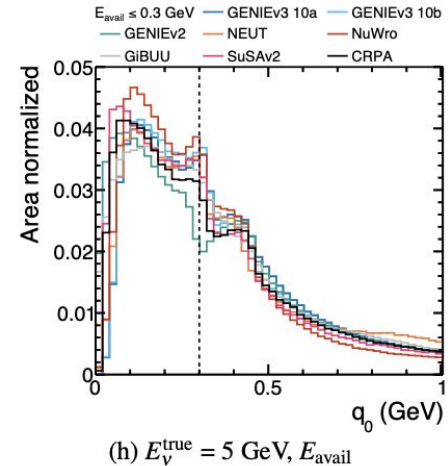
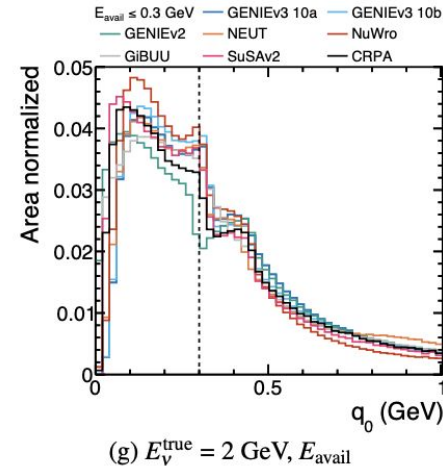
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# $E_{\text{avail}}$ Smearing

Shows the ranges of true  $q_0$  values that pass  $E_{\text{avail}} < 0.3$  cut for two neutrino energies.

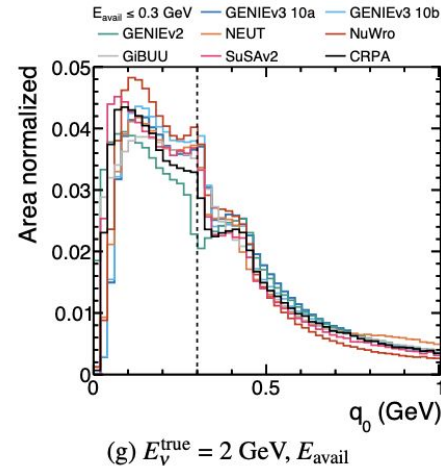


# $E_{\text{avail}}$ Smearing

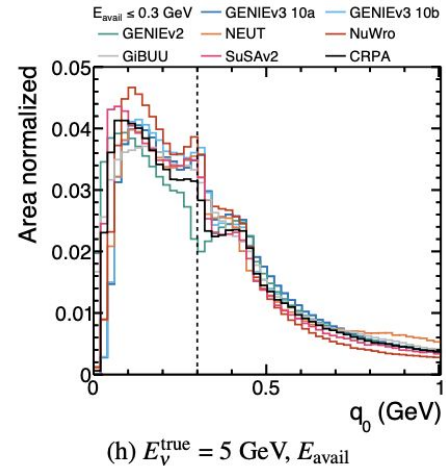
Shows the ranges of true  $q_0$  values that pass  $E_{\text{avail}} < 0.3$  cut for two neutrino energies.

Observations:

- "feed down" predicted from higher  $q_0$
- Significant model spread near the cut value



(g)  $E_v^{\text{true}} = 2$  GeV,  $E_{\text{avail}}$



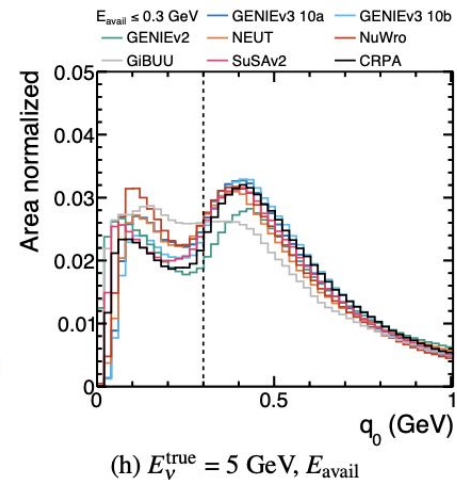
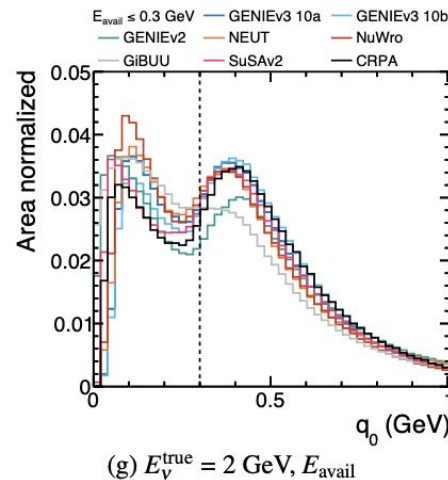
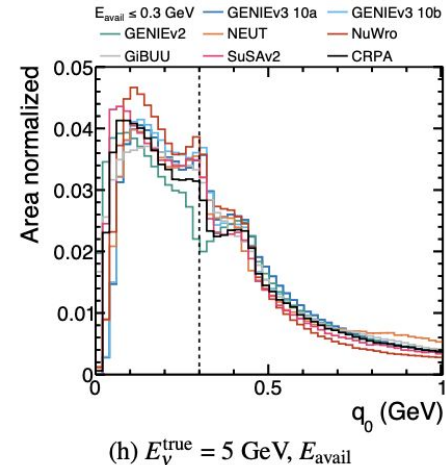
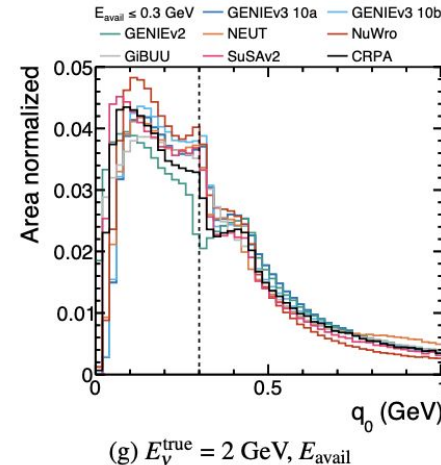
(h)  $E_v^{\text{true}} = 5$  GeV,  $E_{\text{avail}}$

# $E_{\text{avail}}$ Smearing

Shows the ranges of true  $q_0$  values that pass  $E_{\text{avail}} < 0.3$  cut for two neutrino energies.

Observations:

- "feed down" predicted from higher  $q_0$
- Significant model spread near the cut value
- Feed-down is worse for antineutrino



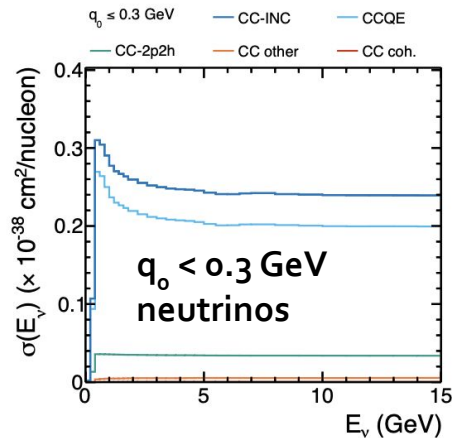


# An $E_{\text{avail}}$ Sample

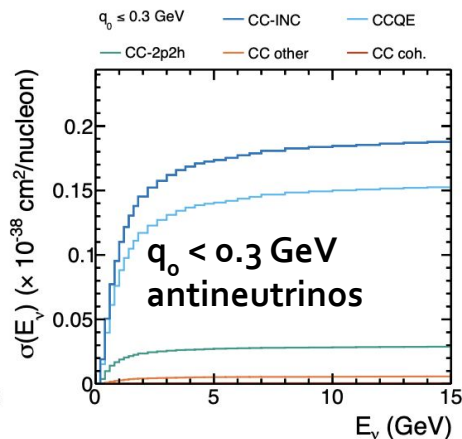
L. Pickering 41

## Observations:

- True QE fraction is much lower
- Cross-section is not predicted to become flat for neutrinos or antineutrinos

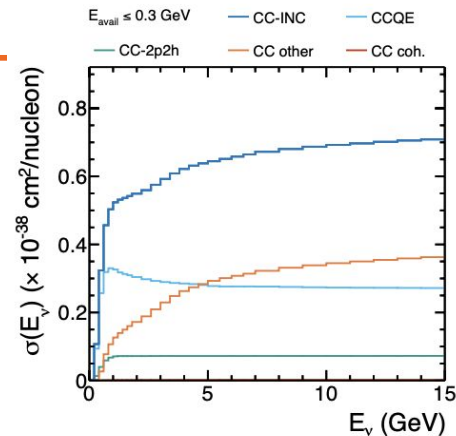


(b)  $\nu_\mu - {}^{40}\text{Ar}$ ,  $q_0 \leq 0.3 \text{ GeV}$

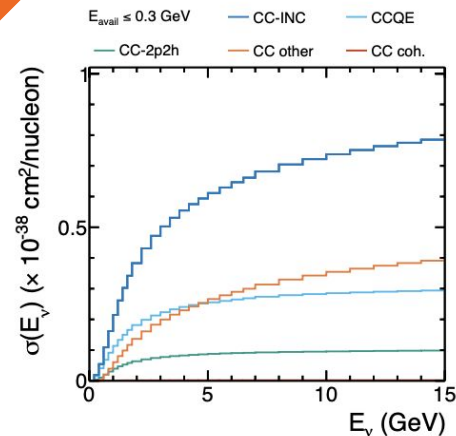


(e)  $\bar{\nu}_\mu - {}^{40}\text{Ar}$ ,  $q_0 \leq 0.3 \text{ GeV}$

Select with  $E_{\text{avail}}$



(c)  $\nu_\mu - {}^{40}\text{Ar}$ ,  $E_{\text{avail}} \leq 0.3 \text{ GeV}$



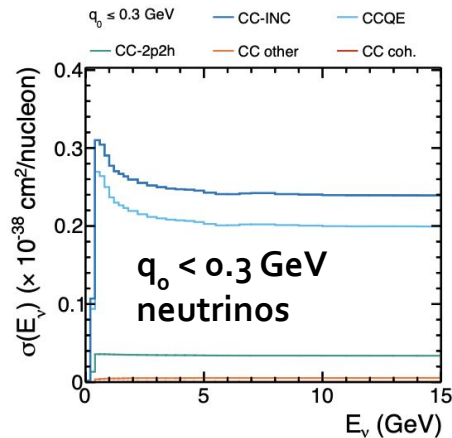
(f)  $\bar{\nu}_\mu - {}^{40}\text{Ar}$ ,  $E_{\text{avail}} \leq 0.3 \text{ GeV}$

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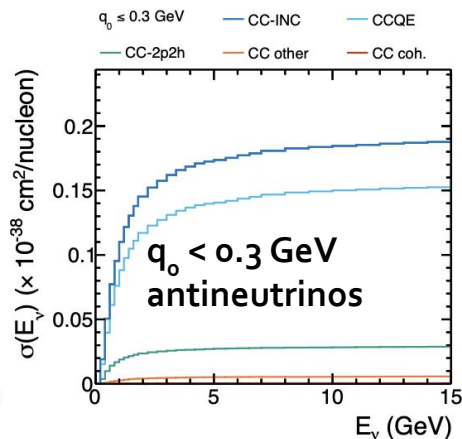
L. Pickering 42

## Observations:

- True QE fraction is much lower
- Cross-section is not predicted to become flat for neutrinos or antineutrinos
- → Rely on model-dependent corrections to use Low- $\nu$

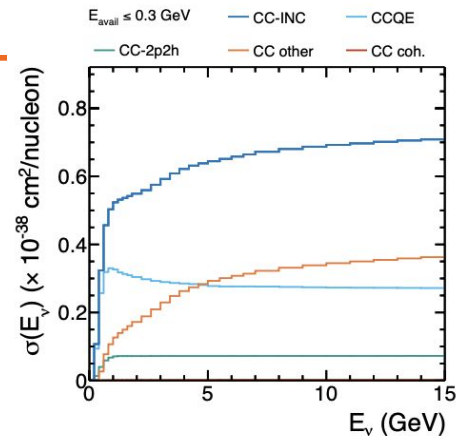


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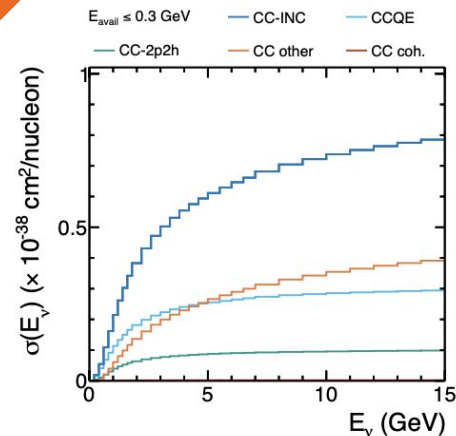


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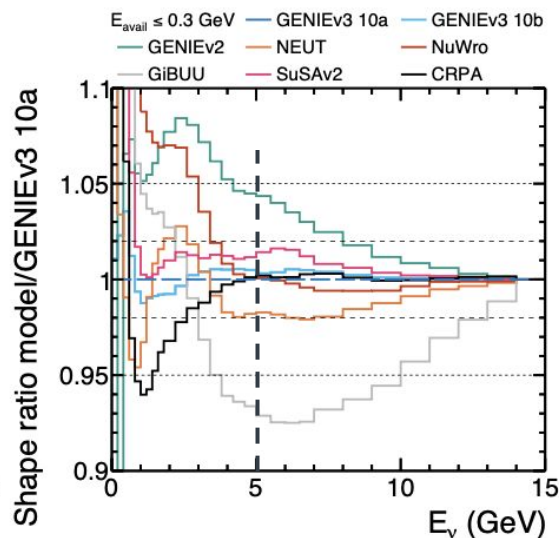
(c)  $\nu_\mu - {}^{40}\text{Ar}$ ,  $E_{\text{avail}} \leq 0.3 \text{ GeV}$



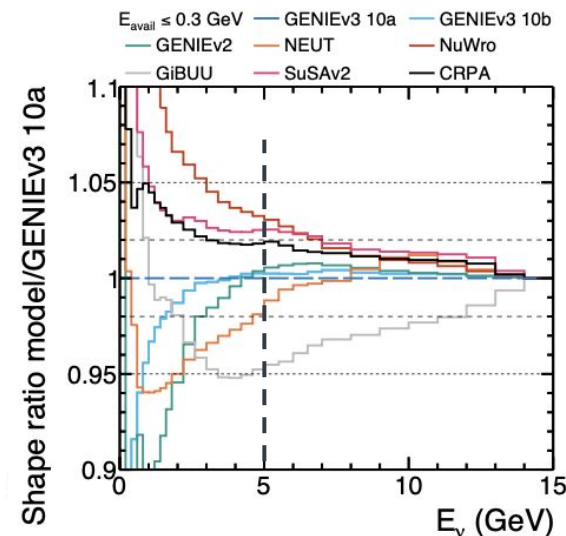
(f)  $\bar{\nu}_\mu - {}^{40}\text{Ar}$ ,  $E_{\text{avail}} \leq 0.3 \text{ GeV}$

# A More Realistic Energy-transfer Analysis

- In the important region, we see model-spread of 5%
  - Performs similarly to current indirect flux constraints
  - Hadron-production measurements are expected to continue to improve before DUNE/HK are systematics limited
- This is not a motivation of systematic uncertainty:
  - It is almost certainly an underestimate of the uncertainty
  - But it is a more comprehensive study of available predictions than has been published by any Low- $\nu$  at few GeV  $E_\nu$  proponents

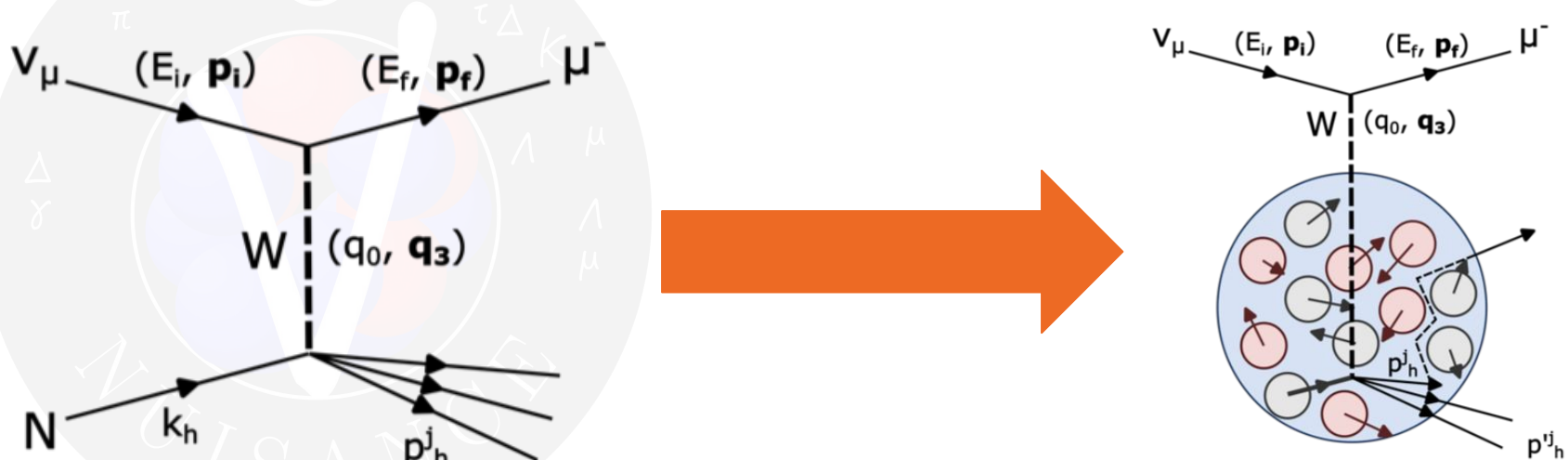


(c)  $\nu_\mu-^{40}\text{Ar}$ ,  $E_{\text{avail}} \leq 0.3 \text{ GeV}$



(f)  $\bar{\nu}_\mu-^{40}\text{Ar}$ ,  $E_{\text{avail}} \leq 0.3 \text{ GeV}$

# The Implicit Assumptions

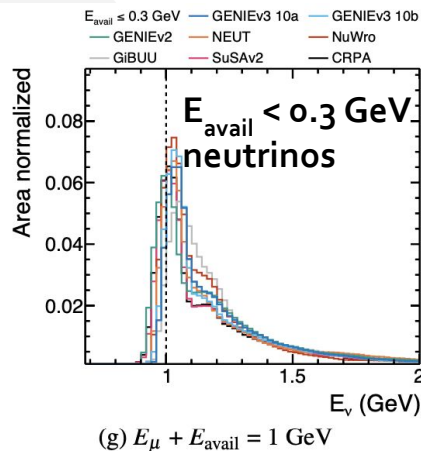


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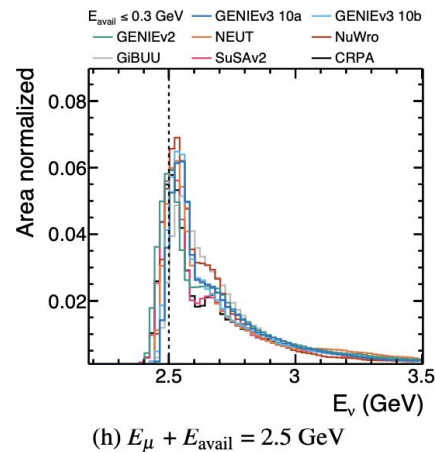
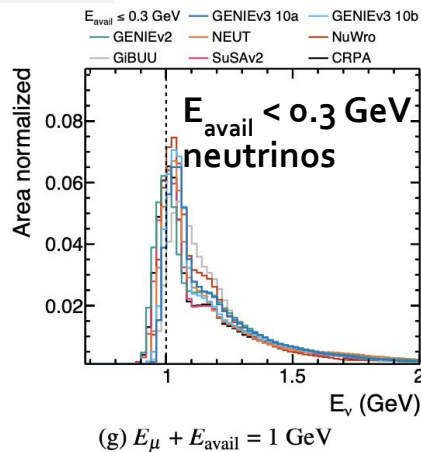
# Neutrino Energy Smearing

Still cannot measure  $E_\nu$



# Neutrino Energy Smearing

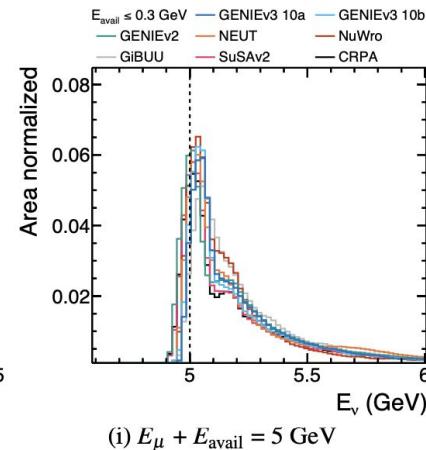
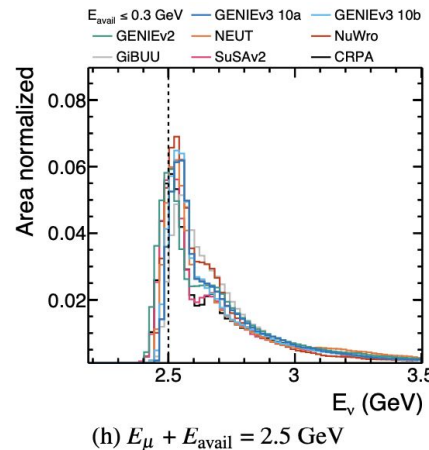
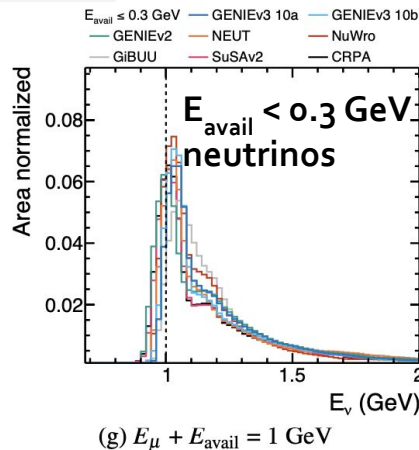
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Still cannot measure  $E_\nu$

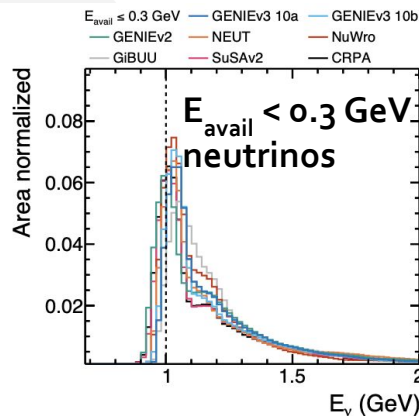
- Will observe significant smearing when trying to bin a Low- $q_0$  sample to measure the flux shape.



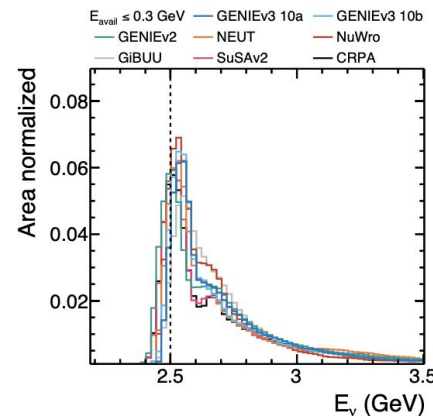
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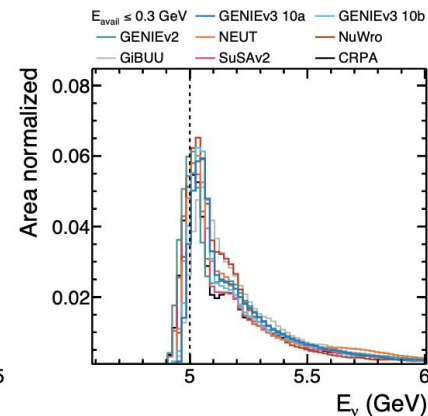
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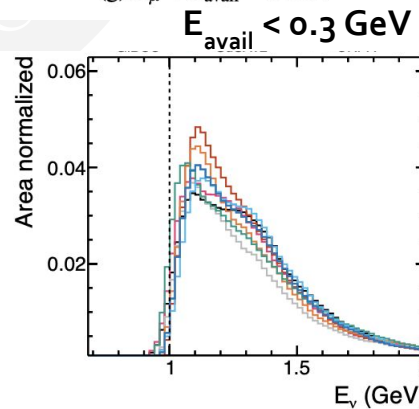
(g)  $E_\mu + E_{\text{avail}} = 1$  GeV



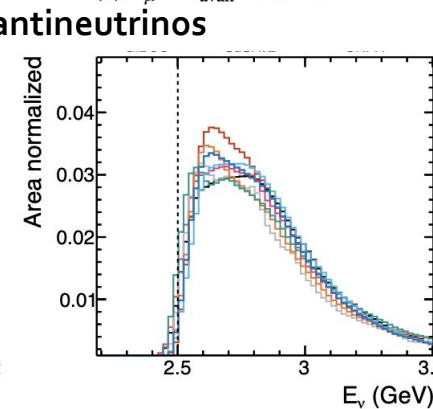
(h)  $E_\mu + E_{\text{avail}} = 2.5$  GeV



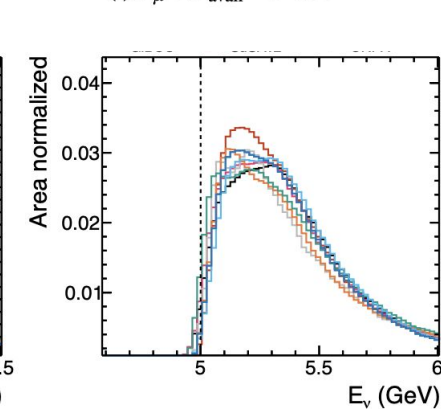
(i)  $E_\mu + E_{\text{avail}} = 5$  GeV



(g)  $E_\mu + E_{\text{avail}} = 1$  GeV



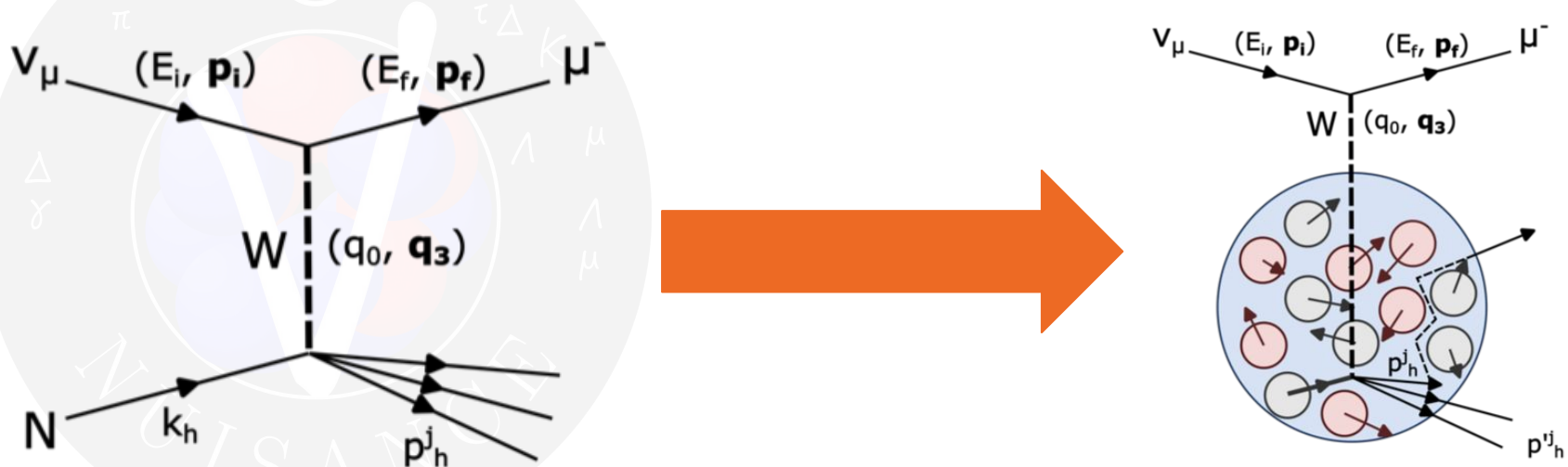
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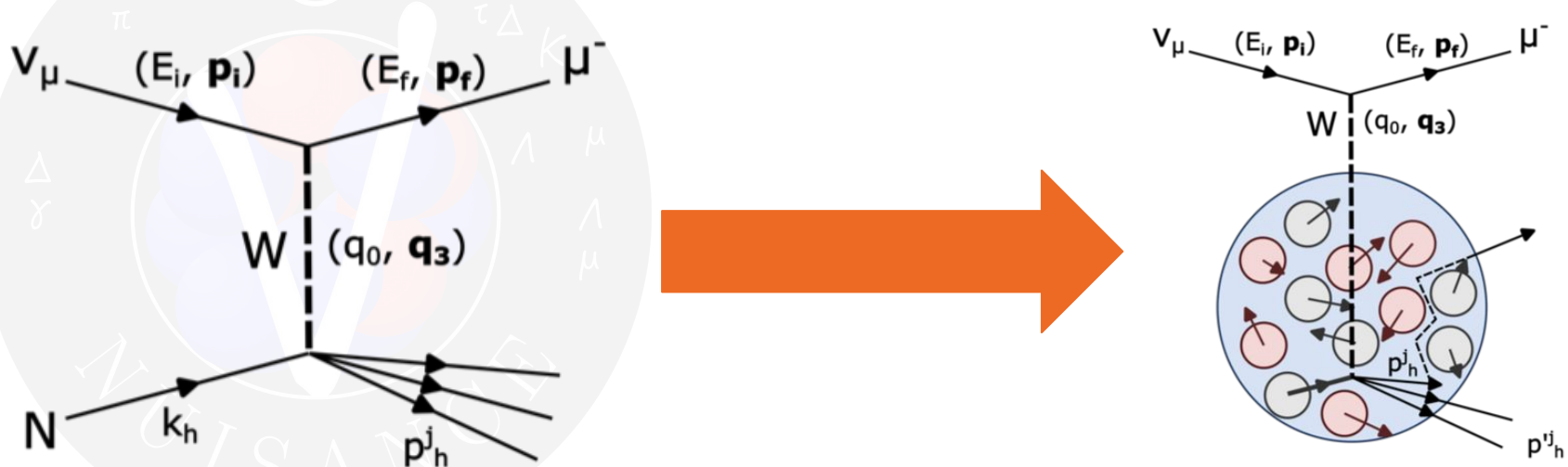
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# The Implicit Assumptions

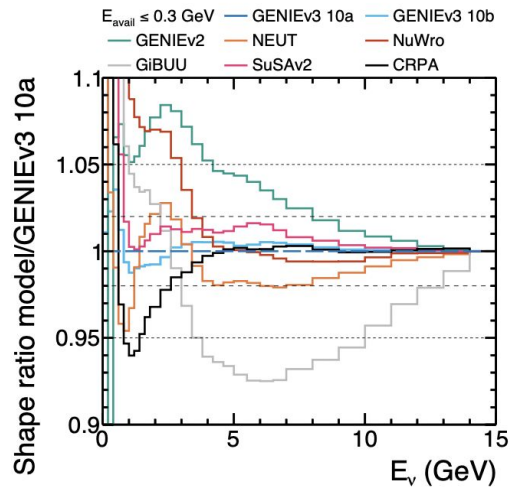


The "low- $\nu$ " method works well if:

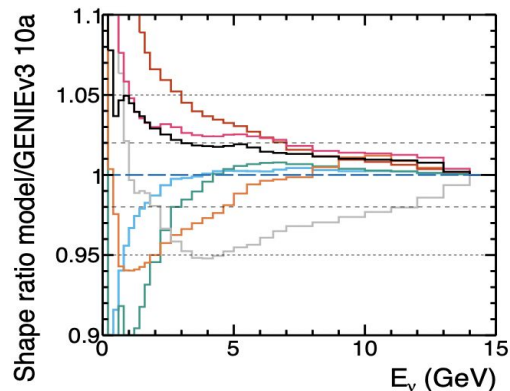
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# Conclusions

- Far from relying on well-understood cross-section to detangle flux  $\otimes$  cross-section the "Low- $\nu$ " method at low  $E_\nu$  is strongly neutrino interaction and nuclear response model dependent



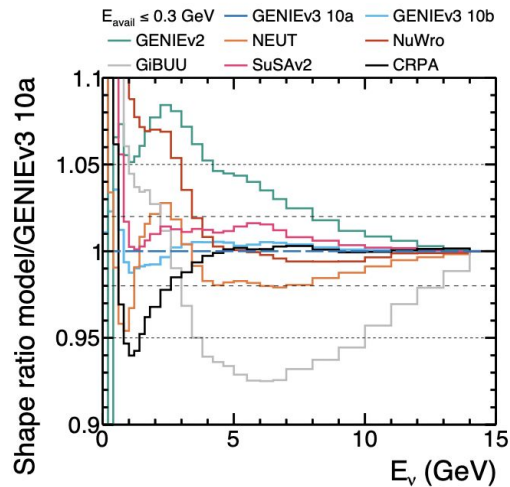
(c)  $\nu_\mu - {}^{40}\text{Ar}$ ,  $E_{\text{avail}} \leq 0.3$  GeV



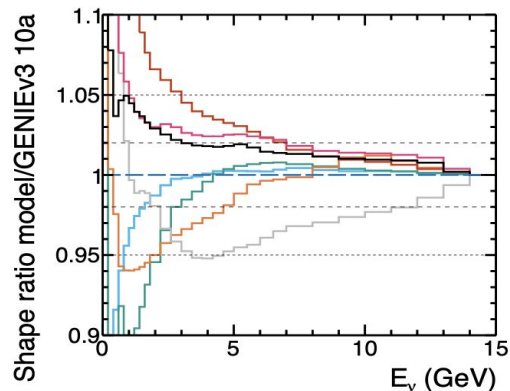
(f)  $\bar{\nu}_\mu - {}^{40}\text{Ar}$ ,  $E_{\text{avail}} \leq 0.3$  GeV

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  - A real detector is likely to be even more messy.



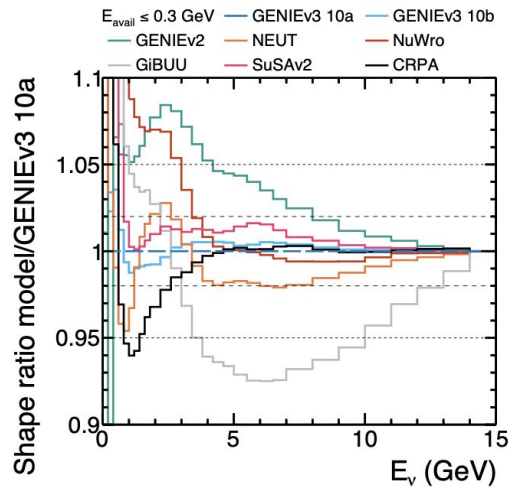
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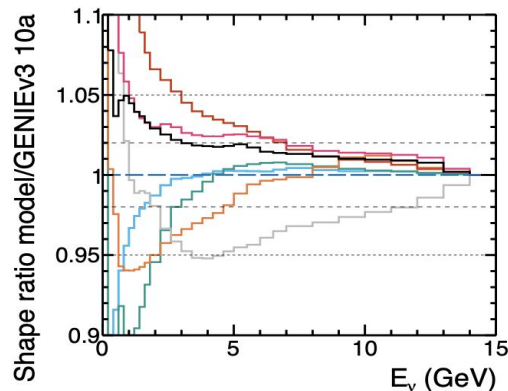
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- Even in simple MC truth studies, it is difficult to justify relying on "Low- $\nu$ " for flux constraints below  $\sim 5$  GeV for  $\nu_\mu$  or 15 GeV for  $\bar{\nu}_\mu$ 
  - A real detector is likely to be even more messy.
- Hadron-production measurements and other *in situ* techniques should be preferred as the main source of flux constraints



(c)  $\nu_\mu - {}^{40}\text{Ar}$ ,  $E_{\text{avail}} \leq 0.3$  GeV



(f)  $\bar{\nu}_\mu - {}^{40}\text{Ar}$ ,  $E_{\text{avail}} \leq 0.3$  GeV



# Thanks For Listening



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# The Low- $\gamma$ Success Stories

- CCFR
- NuTeV
- ~NOMAD: Cut  $E_{\text{Had}} < 20 \text{ GeV}$  and  $E_{\nu} > 30 \text{ GeV}$

