

Probing new physics with rare hyperon and kaon decays involving light invisible particles

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Based on

JT, arXiv:1901.10447 [JHEP 04 (2019) 104]

G Li, JY Su, JT, arXiv:1905.08759

New Physics with Exotic and Long-Lived Particles: A Joint ICISE-CBPF Workshop
ICISE, Quy Nhon, Vietnam

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- Introduction

- $|\Delta S|=1$ neutral-current hadron decays with missing energy (\cancel{E}) & their data

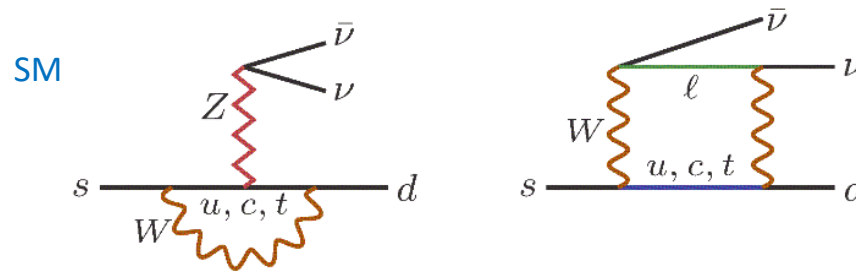
- New interactions ds quarks with invisible fermions

- Kaon & hyperon decays as complementary probes of new physics.
- Kaon constraints & enhanced hyperon rates.

- New ds quark interactions with invisible spin-0 bosons

- Conclusions

- In the standard model (SM) the **strangeness-changing** neutral current decays of light hadrons with missing energy ($\#$) arise mainly from the loop-induced quark transition $s \rightarrow d \nu \bar{\nu}$.



- Such decays are therefore **highly suppressed** in the SM, with branching fractions of order 10^{-10} or less

➤ E.g. SM predictions:

$$\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = \left(8.5_{-1.2}^{+1.0} \right) \times 10^{-11}$$

$$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) = \left(3.2_{-0.7}^{+1.1} \right) \times 10^{-11}$$

Bobeth & Buras, 2018

- Thus, observing significantly larger branching fractions of these processes at ongoing or upcoming experiments would likely be indicative of **new physics (NP)**.

- $K \rightarrow \pi \cancel{E}$

Measurements: $\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = 1.7(1.1) \times 10^{-10}$ E949 2008, PDG 2019
 $\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) < 3.0 \times 10^{-9}$ at 90% CL KOTO, 2019

- $K \rightarrow \pi \pi' \cancel{E}$

Measurements: $\mathcal{B}(K^+ \rightarrow \pi^+ \pi^0 \nu \bar{\nu}) < 4.3 \times 10^{-5}$ at 90% CL E787, 2001
 $\mathcal{B}(K_L \rightarrow \pi^0 \pi^0 \nu \bar{\nu}) < 8.1 \times 10^{-7}$ at 90% CL E391a, 2011

- $K_{L,S} \rightarrow \cancel{E}$ still have no direct-search limits, but indirectly limits can be inferred from the data on their **visible** decay channels:

$\mathcal{B}(K_L \rightarrow \cancel{E}) < 6.3 \times 10^{-4}$ & $\mathcal{B}(K_S \rightarrow \cancel{E}) < 1.1 \times 10^{-4}$ at 95% CL Gninenko, 2015

- No data yet in the baryon sector.

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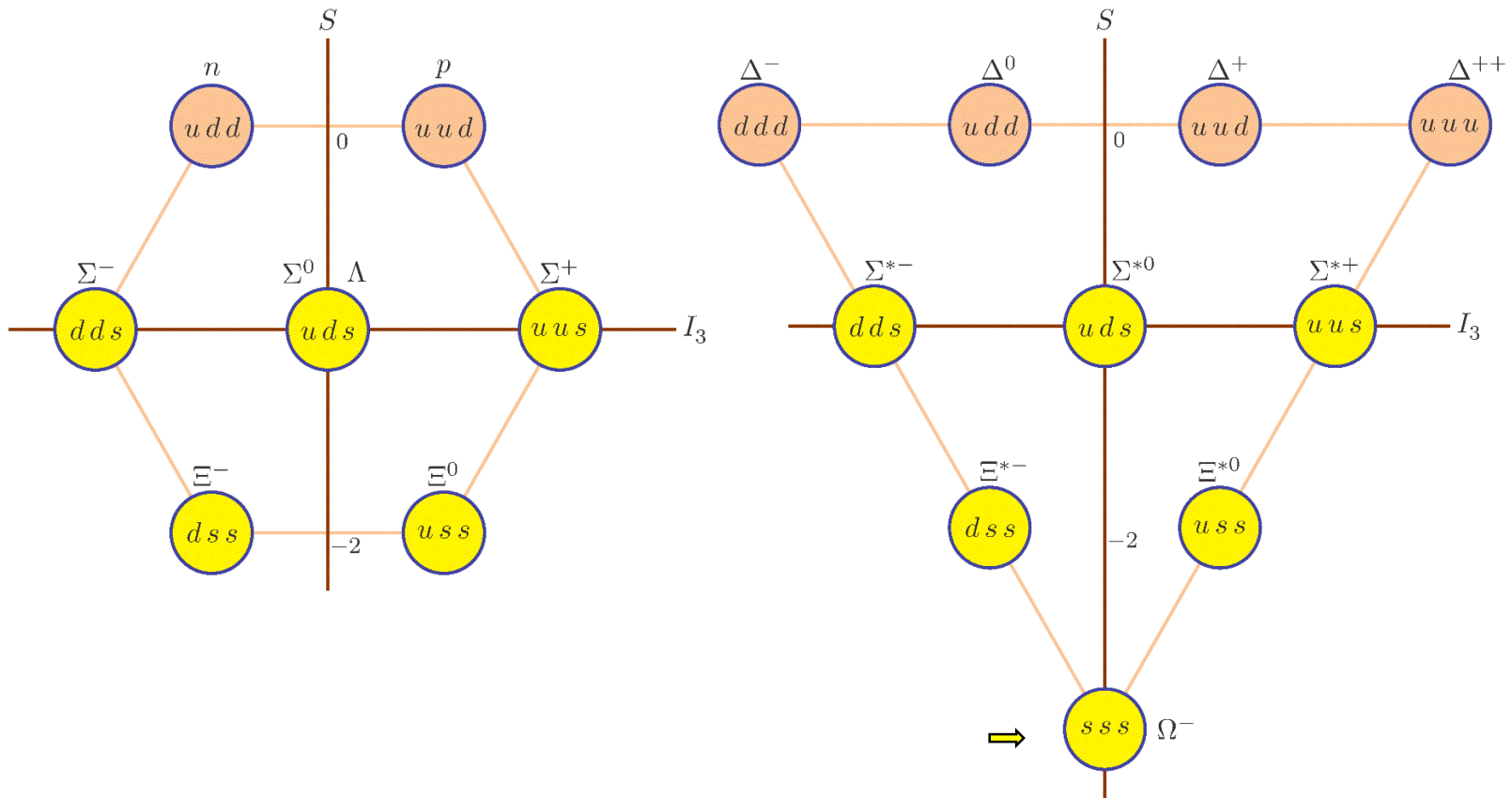
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- No data yet in the baryon sector.

- BESIII is going to search for hyperon decays with missing energy.

Flavor-SU(3) octet of spin-1/2 baryons & decuplet of spin-3/2 baryons



* Effective Lagrangian for $sd\bar{f}\bar{f}$ interactions at low energies

$$\mathcal{L}_f = - \left[\bar{d}\gamma^\eta s \bar{f}\gamma_\eta (\mathbf{C}_f^V + \gamma_5 \mathbf{C}_f^A) \mathbf{f} + \bar{d}\gamma^\eta \gamma_5 s \bar{f}\gamma_\eta (\tilde{\mathbf{C}}_f^V + \gamma_5 \tilde{\mathbf{C}}_f^A) \mathbf{f} \right. \\ \left. + \bar{d}s \bar{f} (\mathbf{C}_f^S + \gamma_5 \mathbf{C}_f^P) \mathbf{f} + \bar{d}\gamma_5 s \bar{f} (\tilde{\mathbf{C}}_f^S + \gamma_5 \tilde{\mathbf{C}}_f^P) \mathbf{f} \right] + \text{H.c.}$$

\mathbf{f} describes an electrically neutral, colorless, invisible, spin- $\frac{1}{2}$, Dirac particle.

Model-independently $\mathbf{C}_f^{V,A,S,P}$ & $\tilde{\mathbf{C}}_f^{V,A,S,P}$ are generally complex free parameters.

* It contributes to $|\Delta S| = 1$ kaon and hyperon decays with missing energy.

- $K \rightarrow \pi f \bar{f}$
- $K \rightarrow \pi \pi' f \bar{f}$
- $K \rightarrow f \bar{f}$
- $\mathcal{B} \rightarrow \mathcal{B}' f \bar{f}$, $\mathcal{B}\mathcal{B}' = \Lambda n, \Sigma^+ p, \Xi^0 \Lambda, \Xi^0 \Sigma^0, \Xi^- \Sigma^-$
- $\Omega^- \rightarrow \Xi^- f \bar{f}$

* \mathcal{L}_f can accommodate $s \rightarrow d\nu\bar{\nu}$ in the SM, with $\mathbf{C}_\nu^V = -\mathbf{C}_\nu^A = -\tilde{\mathbf{C}}_\nu^V = \tilde{\mathbf{C}}_\nu^A$ and $\mathbf{C}_\nu^{S,P} = \tilde{\mathbf{C}}_\nu^{S,P} = 0$

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- Mesonic matrix elements which don't vanish:

$$\langle 0 | \bar{d} \gamma^\eta \gamma_5 s | \bar{K}^0 \rangle = \langle 0 | \bar{s} \gamma^\eta \gamma_5 d | K^0 \rangle = -i f_K p_K^\eta, \quad \langle 0 | \bar{d} \gamma_5 s | \bar{K}^0 \rangle = \langle 0 | \bar{s} \gamma_5 d | K^0 \rangle = i B_0 f_K$$

$$\langle \pi^- | \bar{d} \gamma^\eta s | K^- \rangle = -\langle \pi^+ | \bar{s} \gamma^\eta d | K^+ \rangle = (p_K^\eta + p_\pi^\eta) f_+ + (f_0 - f_+) q_{K\pi}^\eta \frac{m_K^2 - m_\pi^2}{q_{K\pi}^2}$$

$$\langle \pi^- | \bar{d} s | K^- \rangle = \langle \pi^+ | \bar{s} d | K^+ \rangle = B_0 f_0, \quad B_0 = \frac{m_K^2}{\hat{m} + m_s}, \quad q_{K\pi} = p_K - p_\pi$$

$$\langle \pi^0(p_0) \pi^-(p_-) | \bar{d}(\gamma^\eta, 1) \gamma_5 s | K^- \rangle = \frac{i\sqrt{2}}{f_K} \left[(p_0^\eta - p_-^\eta, 0) + \frac{(p_0 - p_-) \cdot \tilde{q}}{m_K^2 - \tilde{q}^2} (\tilde{q}^\eta, -B_0) \right]$$

$$\langle \pi^0(p_1) \pi^0(p_2) | \bar{d}(\gamma^\eta, 1) \gamma_5 s | \bar{K}^0 \rangle = \frac{i}{f_K} \left[(p_1^\eta + p_2^\eta, 0) + \frac{(p_1 + p_2) \cdot \tilde{q}}{m_K^2 - \tilde{q}^2} (\tilde{q}^\eta, -B_0) \right]$$

f_K is the kaon decay constant, $f_{+,0}$ represent form factors depending on $q_{K\pi}^2$

$$\tilde{q} = p_{K^-} - p_0 - p_- = p_{\bar{K}^0} - p_1 - p_2$$

- Vanishing ones:

$$\langle 0 | \bar{d}(\gamma^\eta, 1) s | \bar{K}^0 \rangle = \langle 0 | \bar{s}(\gamma^\eta, 1) d | K^0 \rangle = (0, 0)$$

$$\langle \pi^- | \bar{d}(\gamma^\eta, 1) \gamma_5 s | K^- \rangle = \langle \pi^+ | \bar{s}(\gamma^\eta, 1) \gamma_5 d | K^+ \rangle = (0, 0)$$

$$\mathcal{L}_f = - \left[\bar{d} \gamma^\eta s \bar{f} \gamma_\eta (C_f^V + \gamma_5 C_f^A) f + \bar{d} \gamma^\eta \gamma_5 s \bar{f} \gamma_\eta (\tilde{C}_f^V + \gamma_5 \tilde{C}_f^A) f \right. \\ \left. + \bar{d} s \bar{f} (C_f^S + \gamma_5 C_f^P) f + \bar{d} \gamma_5 s \bar{f} (\tilde{C}_f^S + \gamma_5 \tilde{C}_f^P) f \right] + \text{H.c.}$$

Decay mode	$K \rightarrow \pi f \bar{f}$	$K \rightarrow f \bar{f}$	$K \rightarrow \pi \pi' f \bar{f}$
Couplings	$C_f^V, C_f^A, C_f^S, C_f^P$	$\tilde{C}_f^A, \tilde{C}_f^S, \tilde{C}_f^P$	$\tilde{C}_f^V, \tilde{C}_f^A, \tilde{C}_f^S, \tilde{C}_f^P$

New-physics couplings contributing to $K \rightarrow \pi \not{E}$, $K \rightarrow \not{E}$, and $K \rightarrow \pi \pi' \not{E}$ if \not{E} is carried by spin-1/2 fermions $f \bar{f}$ and their mass is nonzero, $m_f > 0$.

$$\tilde{C}_f^A \text{ no longer contributes to } K \rightarrow f \bar{f} \text{ if } m_f = 0.$$

- The baryonic matrix elements are estimated with aid of chiral perturbation theory (χ PT) at leading order:

$$\begin{aligned} \langle \mathcal{B}' | \bar{d} \gamma^n s | \mathcal{B} \rangle &= \mathcal{V}_{\mathcal{B}'\mathcal{B}} \bar{u}_{\mathcal{B}'} \gamma^n u_{\mathcal{B}}, & \langle \mathcal{B}' | \bar{d} \gamma^n \gamma_5 s | \mathcal{B} \rangle &= \bar{u}_{\mathcal{B}'} \left(\gamma^n \mathcal{A}_{\mathcal{B}'\mathcal{B}} - \frac{\mathcal{P}_{\mathcal{B}'\mathcal{B}}}{B_0} Q^n \right) \gamma_5 u_{\mathcal{B}}, \\ \langle \mathcal{B}' | \bar{d} s | \mathcal{B} \rangle &= \mathcal{S}_{\mathcal{B}'\mathcal{B}} \bar{u}_{\mathcal{B}'} u_{\mathcal{B}}, & \langle \mathcal{B}' | \bar{d} \gamma_5 s | \mathcal{B} \rangle &= \mathcal{P}_{\mathcal{B}'\mathcal{B}} \bar{u}_{\mathcal{B}'} \gamma_5 u_{\mathcal{B}}, & Q &= p_{\mathcal{B}} - p_{\mathcal{B}'} \end{aligned}$$

$\mathcal{B}'\mathcal{B}$	$n\Lambda$	$p\Sigma^+$	$\Lambda\Xi^0$	$\Sigma^0\Xi^0$	$\Sigma^-\Xi^-$
$\mathcal{V}_{\mathcal{B}'\mathcal{B}}$	$-\sqrt{\frac{3}{2}}$	-1	$\sqrt{\frac{3}{2}}$	$\frac{-1}{\sqrt{2}}$	1
$\mathcal{A}_{\mathcal{B}'\mathcal{B}}$	$\frac{-1}{\sqrt{6}}(D+3F)$	$D-F$	$\frac{-1}{\sqrt{6}}(D-3F)$	$\frac{-1}{\sqrt{2}}(D+F)$	$D+F$

$$\mathcal{S}_{\mathcal{B}'\mathcal{B}} = \frac{m_{\mathcal{B}} - m_{\mathcal{B}'}}{m_s - \hat{m}} \mathcal{V}_{\mathcal{B}'\mathcal{B}}, \quad \mathcal{P}_{\mathcal{B}'\mathcal{B}} = \mathcal{A}_{\mathcal{B}'\mathcal{B}} B_0 \frac{m_{\mathcal{B}'} + m_{\mathcal{B}}}{m_K^2 - Q^2}$$

$$\begin{aligned} \langle \Xi^- | \bar{d} \gamma^n \gamma_5 s | \Omega^- \rangle &= \mathcal{C} \bar{u}_{\Xi} \left(u_{\Omega}^n + \frac{\tilde{Q}^n \tilde{Q}_{\kappa}}{m_K^2 - \tilde{Q}^2} u_{\Omega}^{\kappa} \right), & \langle \Xi^- | \bar{d} \gamma_5 s | \Omega^- \rangle &= \frac{B_0 \mathcal{C} \tilde{Q}_{\kappa}}{\tilde{Q}^2 - m_K^2} \bar{u}_{\Xi} u_{\Omega}^{\kappa} \\ \langle \Xi^- | \bar{d} \gamma^n s | \Omega^- \rangle &= \langle \Xi^- | \bar{d} s | \Omega^- \rangle = 0, & \tilde{Q} &= p_{\Omega^-} - p_{\Xi^-} \end{aligned}$$

- Most of them don't vanish in leading-order χ PT.

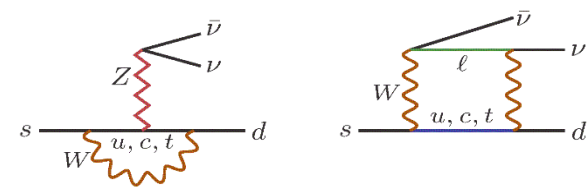
$$\square \mathcal{L}_f = - \left[\bar{d} \gamma^\eta s \bar{f} \gamma_\eta (C_f^V + \gamma_5 C_f^A) f + \bar{d} \gamma^\eta \gamma_5 s \bar{f} \gamma_\eta (\tilde{C}_f^V + \gamma_5 \tilde{C}_f^A) f \right. \\ \left. + \bar{d} s \bar{f} (C_f^S + \gamma_5 C_f^P) f + \bar{d} \gamma_5 s \bar{f} (\tilde{C}_f^S + \gamma_5 \tilde{C}_f^P) f \right] + \text{H.c.}$$

Decay mode	$K \rightarrow \pi f \bar{f}$	$K \rightarrow f \bar{f}$	$K \rightarrow \pi \pi' f \bar{f}$	$\mathcal{B} \rightarrow \mathcal{B}' f \bar{f}$	$\Omega^- \rightarrow \Xi^- f \bar{f}$
Couplings	$C_f^{V,A,S,P}$	$\tilde{C}_f^{A,S,P}$	$\tilde{C}_f^{V,A,S,P}$	$C_f^{V,A,S,P}, \tilde{C}_f^{V,A,S,P}$	$\tilde{C}_f^{V,A,S,P}$

NP couplings affecting FCNC kaon & hyperon decays with missing energy carried by spin-1/2 fermions $f \bar{f}$ with nonzero mass, $m_f > 0$.

\tilde{C}_f^A no longer contributes to $K \rightarrow f \bar{f}$ if $m_f = 0$.

SM predictions for hyperon decays with missing energy



* Lagrangian for $s \rightarrow d\nu\bar{\nu}$

$$\mathcal{L}_{\text{SM}} = \frac{-\alpha_e G_F}{\sqrt{8} \pi s_W^2} \sum_{l=e,\mu,\tau} (V_{td}^* V_{ts} X_t + V_{cd}^* V_{cs} X_c^l) \bar{d} \gamma^\eta (1 - \gamma_5) s \bar{\nu}_l \gamma_\eta (1 - \gamma_5) \nu_l + \text{H.c.}$$

$X_{t,c}$ are t - and c -quark contributions

* Branching fractions $\mathcal{B}(\mathcal{B} \rightarrow \mathcal{B}'\nu\bar{\nu})_{\text{SM}} = \sum_l \mathcal{B}(\mathcal{B} \rightarrow \mathcal{B}'\nu_l\bar{\nu}_l)_{\text{SM}}$

for $\mathcal{B}\mathcal{B}' = \Lambda n, \Sigma^+ p, \Xi^0 \Lambda, \Xi^0 \Sigma^0, \Xi^- \Sigma^-$

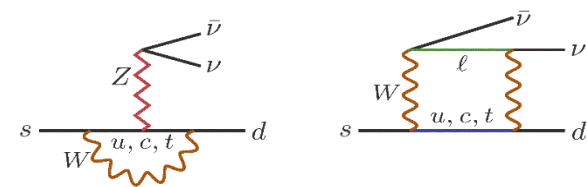
with $C_{\nu_l}^V = -C_{\nu_l}^A = -\tilde{c}_{\nu_l}^V = \tilde{c}_{\nu_l}^A = \frac{\alpha_e G_F}{\sqrt{8} \pi s_W^2} (\lambda_t X_t + \lambda_c X_c^l)$ and $C_{\nu_l}^{\text{S,P}} = \tilde{c}_{\nu_l}^{\text{S,P}} = 0$

Similarly for $\mathcal{B}(\Omega^- \rightarrow \Xi^- \nu\bar{\nu})_{\text{SM}}$

* Predictions for branching fractions

$\Lambda \rightarrow n\nu\bar{\nu}$	$\Sigma^+ \rightarrow p\nu\bar{\nu}$	$\Xi^0 \rightarrow \Lambda\nu\bar{\nu}$	$\Xi^0 \rightarrow \Sigma^0\nu\bar{\nu}$	$\Xi^- \rightarrow \Sigma^-\nu\bar{\nu}$	$\Omega^- \rightarrow \Xi^-\nu\bar{\nu}$
7.1×10^{-13}	4.3×10^{-13}	6.3×10^{-13}	1.0×10^{-13}	1.3×10^{-13}	4.9×10^{-12}

SM predictions for hyperon decays with missing energy



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for $\mathcal{B}\mathcal{B}' = \Lambda n, \Sigma^+ p, \Xi^0 \Lambda, \Xi^0 \Sigma^0, \Xi^- \Sigma^-$

with $C_{\nu_l}^V = -C_{\nu_l}^A = -\tilde{c}_{\nu_l}^V = \tilde{c}_{\nu_l}^A = \frac{\alpha_e G_F}{\sqrt{8} \pi s_W^2} (\lambda_t X_t + \lambda_c X_c)$ and $C_{\nu_l}^{\text{S,P}} = \tilde{c}_{\nu_l}^{\text{S,P}} = 0$

Similarly for $\mathcal{B}(\Omega^- \rightarrow \Xi^- \nu\bar{\nu})_{\text{SM}}$

* Predictions for branching fractions

$\Lambda \rightarrow n\nu\bar{\nu}$	$\Sigma^+ \rightarrow p\nu\bar{\nu}$	$\Xi^0 \rightarrow \Lambda\nu\bar{\nu}$	$\Xi^0 \rightarrow \Sigma^0\nu\bar{\nu}$	$\Xi^- \rightarrow \Sigma^-\nu\bar{\nu}$	$\Omega^- \rightarrow \Xi^-\nu\bar{\nu}$
7.1×10^{-13}	4.3×10^{-13}	6.3×10^{-13}	1.0×10^{-13}	1.3×10^{-13}	4.9×10^{-12}

* Estimated BESIII sensitivity for branching fractions

HB Li, 1612.01775

$\Lambda \rightarrow n\nu\bar{\nu}$	$\Sigma^+ \rightarrow p\nu\bar{\nu}$	$\Xi^0 \rightarrow \Lambda\nu\bar{\nu}$	$\Xi^0 \rightarrow \Sigma^0\nu\bar{\nu}$	$\Xi^- \rightarrow \Sigma^-\nu\bar{\nu}$	$\Omega^- \rightarrow \Xi^-\nu\bar{\nu}$
3×10^{-7}	4×10^{-7}	8×10^{-7}	9×10^{-7}	—	2.6×10^{-5}

★ $K \rightarrow \pi f \bar{f}$

 Measurements: $\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = 1.7(1.1) \times 10^{-10}$

PDG 2019

 $\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) < 3.0 \times 10^{-9}$ at 90% CL

KOTO, 2019

 SM predictions: $\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (8.5_{-1.2}^{+1.0}) \times 10^{-11}$
 $\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) = (3.2_{-0.7}^{+1.1}) \times 10^{-11}$

Bobeth & Buras, 2018

★ Implication: the effects of new physics on these modes cannot be substantial.

 NP that contributes via operators having mainly/only parity-even quark parts (and coupling constants $C_f^{V,A,S,P}$) is already well constrained.

$$\mathcal{L}_f = - \left[\bar{d} \gamma^\eta s \bar{f} \gamma_\eta (C_f^V + \gamma_5 C_f^A) f + \bar{d} \gamma^\eta \gamma_5 s \bar{f} \gamma_\eta (\tilde{C}_f^V + \gamma_5 \tilde{C}_f^A) f \right. \\ \left. + \bar{d} s \bar{f} (C_f^S + \gamma_5 C_f^P) f + \bar{d} \gamma_5 s \bar{f} (\tilde{C}_f^S + \gamma_5 \tilde{C}_f^P) f \right] + \text{H.c.}$$

Decay mode	$K \rightarrow \pi f \bar{f}$	$K \rightarrow f \bar{f}$	$K \rightarrow \pi \pi' f \bar{f}$
Couplings	$C_f^V, C_f^A, C_f^S, C_f^P$	$\tilde{C}_f^A, \tilde{C}_f^S, \tilde{C}_f^P$	$\tilde{C}_f^V, \tilde{C}_f^A, \tilde{C}_f^S, \tilde{C}_f^P$

$$m_f > 0$$

- ◆ $K_{L,S} \rightarrow \cancel{E}$ still have no direct-search limits, but indirectly upper limits on them can be inferred from the data on their **visible** decay channels:

Gninenko, 2015

$$\mathcal{B}(K_L \rightarrow \cancel{E}) < 6.3 \times 10^{-4} \quad \& \quad \mathcal{B}(K_S \rightarrow \cancel{E}) < 1.1 \times 10^{-4} \quad \text{both at 95\% CL}$$

$$\text{SM predictions: } \mathcal{B}(K_L \rightarrow \cancel{E}) \sim 1 \times 10^{-10} \quad \& \quad \mathcal{B}(K_S \rightarrow \cancel{E}) \sim 2 \times 10^{-14}$$

- ◆ $K \rightarrow \pi\pi' \cancel{E}$

$$\text{Measurements: } \mathcal{B}(K^+ \rightarrow \pi^+ \pi^0 \nu \bar{\nu}) < 4.3 \times 10^{-5} \quad \text{at 90\% CL}$$

$$\mathcal{B}(K_L \rightarrow \pi^0 \pi^0 \nu \bar{\nu}) < 8.1 \times 10^{-7} \quad \text{at 90\% CL}$$

PDG 2019

$$\text{SM predictions: } \mathcal{B}(K^+ \rightarrow \pi^+ \pi^0 \nu \bar{\nu}) \sim 10^{-14}$$

$$\mathcal{B}(K_L \rightarrow \pi^0 \pi^0 \nu \bar{\nu}) \sim 10^{-13}$$

Littenberg & Valencia, 1996

Chiang & Gilman, 2000

Kamenik & Smith, 2012

- ◆ Implication: NP effects on $K \rightarrow \cancel{E}$ and $K \rightarrow \pi\pi' \cancel{E}$ can still be large.

NP that contributes via operators having mainly/only parity-odd quark parts (and coupling constants $\tilde{\mathbf{c}}_f^{V,A,S,P}$) is not yet stringently constrained.

Decay mode	$K \rightarrow \pi f \bar{f}$	$K \rightarrow f \bar{f}$	$K \rightarrow \pi\pi' f \bar{f}$
Couplings	$\mathbf{C}_f^V, \mathbf{C}_f^A, \mathbf{C}_f^S, \mathbf{C}_f^P$	$\tilde{\mathbf{c}}_f^A, \tilde{\mathbf{c}}_f^S, \tilde{\mathbf{c}}_f^P$	$\tilde{\mathbf{c}}_f^V, \tilde{\mathbf{c}}_f^A, \tilde{\mathbf{c}}_f^S, \tilde{\mathbf{c}}_f^P$

$$m_f > 0$$

- Consider new physics contributing to hyperon decays with missing energy only via operators with parity-odd quark parts
 - assuming f to be a nonstandard particle with negligible mass.

$$\mathcal{L}_f \supset -\bar{d}\gamma_5 s \bar{f}(\tilde{c}_f^S + \gamma_5 \tilde{c}_f^P)f - \bar{d}\gamma^\eta \gamma_5 s \bar{f}\gamma_\eta(\tilde{c}_f^V + \gamma_5 \tilde{c}_f^A)f + \text{H.c.}$$

With $m_f \simeq 0$, for the two-body decays (\tilde{c}_f^A no longer affects $K \rightarrow f\bar{f}$ if $m_f = 0$)

$$\mathcal{B}(K_L \rightarrow f\bar{f}) = 2.9 \left[(\text{Im } \tilde{c}_f^S)^2 + (\text{Re } \tilde{c}_f^P)^2 \right] 10^{14} \text{ GeV}^4,$$

$$\mathcal{B}(K_S \rightarrow f\bar{f}) = 5.1 \left[(\text{Re } \tilde{c}_f^S)^2 + (\text{Im } \tilde{c}_f^P)^2 \right] 10^{11} \text{ GeV}^4$$

leading to

$$|\tilde{c}_f^S|^2 + |\tilde{c}_f^P|^2 = \frac{3.4 \times 10^{-15}}{\text{GeV}^4} \mathcal{B}(K_L \rightarrow f\bar{f}) + \frac{2.0 \times 10^{-12}}{\text{GeV}^4} \mathcal{B}(K_S \rightarrow f\bar{f})$$

and for the four-body decays

$$\mathcal{B}(K^- \rightarrow \pi^- \pi^0 f\bar{f}) = \left[6.3 \left(|\tilde{c}_f^V|^2 + |\tilde{c}_f^A|^2 \right) + 2.0 \left(|\tilde{c}_f^S|^2 + |\tilde{c}_f^P|^2 \right) \right] 10^5 \text{ GeV}^4,$$

$$\mathcal{B}(K_L \rightarrow \pi^0 \pi^0 f\bar{f}) = \left\{ 8.5 \left[(\text{Re } \tilde{c}_f^V)^2 + (\text{Re } \tilde{c}_f^A)^2 \right] + 16 \left[(\text{Im } \tilde{c}_f^S)^2 + (\text{Re } \tilde{c}_f^S)^2 \right] \right\} 10^6 \text{ GeV}^4$$

- NP contributing only via operators with pseudoscalar ds part.

$$\mathcal{L}_f \supset -\bar{d}\gamma_5 s \bar{f}(\tilde{\mathbf{c}}_f^S + \gamma_5 \tilde{\mathbf{c}}_f^P)\mathbf{f} + \text{H.c.}$$

- The constraints from $K \rightarrow \bar{E}$ are stronger than from $K \rightarrow \pi\pi'\bar{E}$

leading to
$$|\tilde{\mathbf{c}}_f^S|^2 + |\tilde{\mathbf{c}}_f^P|^2 < 2.2 \times 10^{-16} \text{ GeV}^{-4}$$

This translates into

$$\mathcal{B}(\Lambda \rightarrow n f \bar{f}) < 5.0 \times 10^{-9}, \quad \mathcal{B}(\Sigma^+ \rightarrow p f \bar{f}) < 3.0 \times 10^{-9}$$

$$\mathcal{B}(\Xi^0 \rightarrow \Lambda f \bar{f}) < 9.3 \times 10^{-10}, \quad \mathcal{B}(\Omega^- \rightarrow \Xi^- f \bar{f}) < 3.0 \times 10^{-7}$$

- NP contributing only via operators with pseudoscalar ds part.

$$\mathcal{L}_f \supset -\bar{d}\gamma_5 s \bar{f}(\tilde{c}_f^S + \gamma_5 \tilde{c}_f^P)f + \text{H.c.}$$

- The constraints from $K \rightarrow \cancel{E}$ are stronger than from $K \rightarrow \pi\pi'\cancel{E}$

leading to
$$|\tilde{c}_f^S|^2 + |\tilde{c}_f^P|^2 < 2.2 \times 10^{-16} \text{ GeV}^{-4}$$

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$$\mathcal{B}(\Lambda \rightarrow n f \bar{f}) < 5.0 \times 10^{-9}, \quad \mathcal{B}(\Sigma^+ \rightarrow p f \bar{f}) < 3.0 \times 10^{-9}$$

$$\mathcal{B}(\Xi^0 \rightarrow \Lambda f \bar{f}) < 9.3 \times 10^{-10}, \quad \mathcal{B}(\Omega^- \rightarrow \Xi^- f \bar{f}) < 3.0 \times 10^{-7}$$

- These numbers are still 2 to 3 orders of magnitude beyond the expected BESIII reach.

Estimated BESIII sensitivity for branching fractions

Li, 2017

$\Lambda \rightarrow n \nu \bar{\nu}$	$\Sigma^+ \rightarrow p \nu \bar{\nu}$	$\Xi^0 \rightarrow \Lambda \nu \bar{\nu}$	$\Xi^0 \rightarrow \Sigma^0 \nu \bar{\nu}$	$\Omega^- \rightarrow \Xi^- \nu \bar{\nu}$
3×10^{-7}	4×10^{-7}	8×10^{-7}	9×10^{-7}	2.6×10^{-5}

- NP contributing only via operators with axial-vector ds part
 - with the couplings assumed to be real.

$$\mathcal{L}_f \supset -\bar{d}\gamma^\eta\gamma_5 s \bar{f}\gamma_\eta(\tilde{c}_f^V + \gamma_5\tilde{c}_f^A)f + \text{H.c.}$$

- The constraints come mainly from $K_L \rightarrow \pi^0\pi^0 \cancel{E}$ and lead to

$$\left(\text{Re } \tilde{c}_f^V\right)^2 + \left(\text{Re } \tilde{c}_f^A\right)^2 < 9.4 \times 10^{-14} \text{ GeV}^{-4}$$

This translates into

$$\mathcal{B}(\Lambda \rightarrow n f \bar{f}) < 6.6 \times 10^{-6},$$

$$\mathcal{B}(\Sigma^+ \rightarrow p f \bar{f}) < 1.7 \times 10^{-6}$$

$$\mathcal{B}(\Xi^0 \rightarrow \Lambda f \bar{f}) < 9.4 \times 10^{-7},$$

$$\mathcal{B}(\Xi^0 \rightarrow \Sigma^0 f \bar{f}) < 1.3 \times 10^{-6}$$

$$\mathcal{B}(\Omega^- \rightarrow \Xi^- f \bar{f}) < 7.5 \times 10^{-5}$$

- NP contributing only via operators with axial-vector ds part
 - with the couplings assumed to be real.

$$\mathcal{L}_f \supset -\bar{d}\gamma^\eta\gamma_5 s \bar{f}\gamma_\eta(\tilde{c}_f^V + \gamma_5\tilde{c}_f^A)f + \text{H.c.}$$

- The constraints come mainly from $K_L \rightarrow \pi^0\pi^0 \cancel{E}$ and lead to

$$\left(\text{Re } \tilde{c}_f^V\right)^2 + \left(\text{Re } \tilde{c}_f^A\right)^2 < 9.4 \times 10^{-14} \text{ GeV}^{-4}$$

This translates into

$$\mathcal{B}(\Lambda \rightarrow n f \bar{f}) < 6.6 \times 10^{-6}, \quad \mathcal{B}(\Sigma^+ \rightarrow p f \bar{f}) < 1.7 \times 10^{-6}$$

$$\mathcal{B}(\Xi^0 \rightarrow \Lambda f \bar{f}) < 9.4 \times 10^{-7}, \quad \mathcal{B}(\Xi^0 \rightarrow \Sigma^0 f \bar{f}) < 1.3 \times 10^{-6}$$

$$\mathcal{B}(\Omega^- \rightarrow \Xi^- f \bar{f}) < 7.5 \times 10^{-5}$$

- The upper values of these limits exceed the BESIII sensitivity levels.

Estimated BESIII sensitivity for branching fractions

Li, 2017

$\Lambda \rightarrow n\nu\bar{\nu}$	$\Sigma^+ \rightarrow p\nu\bar{\nu}$	$\Xi^0 \rightarrow \Lambda\nu\bar{\nu}$	$\Xi^0 \rightarrow \Sigma^0\nu\bar{\nu}$	$\Omega^- \rightarrow \Xi^-\nu\bar{\nu}$
3×10^{-7}	4×10^{-7}	8×10^{-7}	9×10^{-7}	2.6×10^{-5}

- With $m_f > 0$, more possibilities could arise.

$$\mathcal{L}_f \supset -\bar{d}\gamma_5 s \bar{f}(\tilde{c}_f^S + \gamma_5 \tilde{c}_f^P)f - \bar{d}\gamma^n \gamma_5 s \bar{f}\gamma_\eta(\tilde{c}_f^V + \gamma_5 \tilde{c}_f^A)f + \text{H.c.}$$

Decay mode	$K \rightarrow f\bar{f}$	$K \rightarrow \pi\pi'f\bar{f}$	$\mathfrak{B} \rightarrow \mathfrak{B}'f\bar{f}$	$\Omega^- \rightarrow \Xi^-f\bar{f}$	$m_f > 0$ Ignoring $c_f^{V,A,S,P}$
Couplings	$\tilde{c}_f^A, \tilde{c}_f^S, \tilde{c}_f^P$	$\tilde{c}_f^V, \tilde{c}_f^A, \tilde{c}_f^S, \tilde{c}_f^P$	$\tilde{c}_f^V, \tilde{c}_f^A, \tilde{c}_f^S, \tilde{c}_f^P$	$\tilde{c}_f^V, \tilde{c}_f^A, \tilde{c}_f^S, \tilde{c}_f^P$	

- If NP contributes mainly via $\tilde{c}_f^{A,S,P}$ & m_f is nonnegligible, the $K \rightarrow f\bar{f}$ constraints turn out to be stricter than the $K \rightarrow \pi\pi'f\bar{f}$ ones & cause the hyperon rates to become smaller than their $m_f = 0$ values.

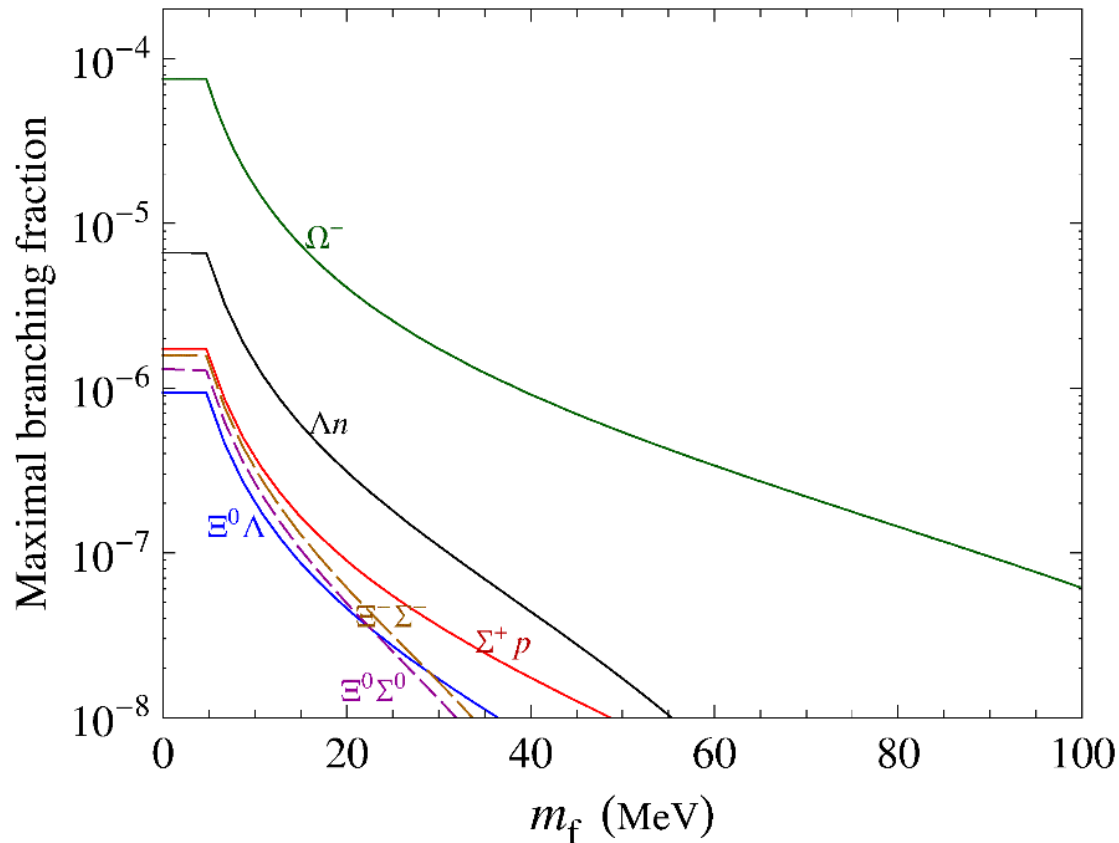


FIG. 2: The maximal branching fractions of $\mathcal{B} \rightarrow \mathcal{B}' f \bar{f}$ with $\mathcal{B}\mathcal{B}' = \Lambda n, \Sigma^+ p, \Xi^0 \Lambda, \Xi^0 \Sigma^0, \Xi^- \Sigma^-$ and of $\Omega^- \rightarrow \Xi^- f \bar{f}$ versus m_f , induced by the contribution of $\text{Re } \tilde{c}_f^A$ alone, subject to the $K_L \rightarrow \pi^0 \pi^0 \cancel{E}$ and $K_L \rightarrow \cancel{E}$ constraints, with the latter becoming more important for $m_f > 5$ MeV.

- With $m_f > 0$, even more interesting possibilities could arise.

$$\mathcal{L}_f \supset -\bar{d}\gamma_5 s \bar{f}(\tilde{c}_f^S + \gamma_5 \tilde{c}_f^P)f - \bar{d}\gamma^n \gamma_5 s \bar{f}\gamma_\eta(\tilde{c}_f^V + \gamma_5 \tilde{c}_f^A)f + \text{H.c.}$$

Decay mode	$K \rightarrow f\bar{f}$	$K \rightarrow \pi\pi'f\bar{f}$	$\mathfrak{B} \rightarrow \mathfrak{B}'f\bar{f}$	$\Omega^- \rightarrow \Xi^-f\bar{f}$	$m_f > 0$ Ignoring $c_f^{V,A,S,P}$
Couplings	$\tilde{c}_f^A, \tilde{c}_f^S, \tilde{c}_f^P$	$\tilde{c}_f^V, \tilde{c}_f^A, \tilde{c}_f^S, \tilde{c}_f^P$	$\tilde{c}_f^V, \tilde{c}_f^A, \tilde{c}_f^S, \tilde{c}_f^P$	$\tilde{c}_f^V, \tilde{c}_f^A, \tilde{c}_f^S, \tilde{c}_f^P$	

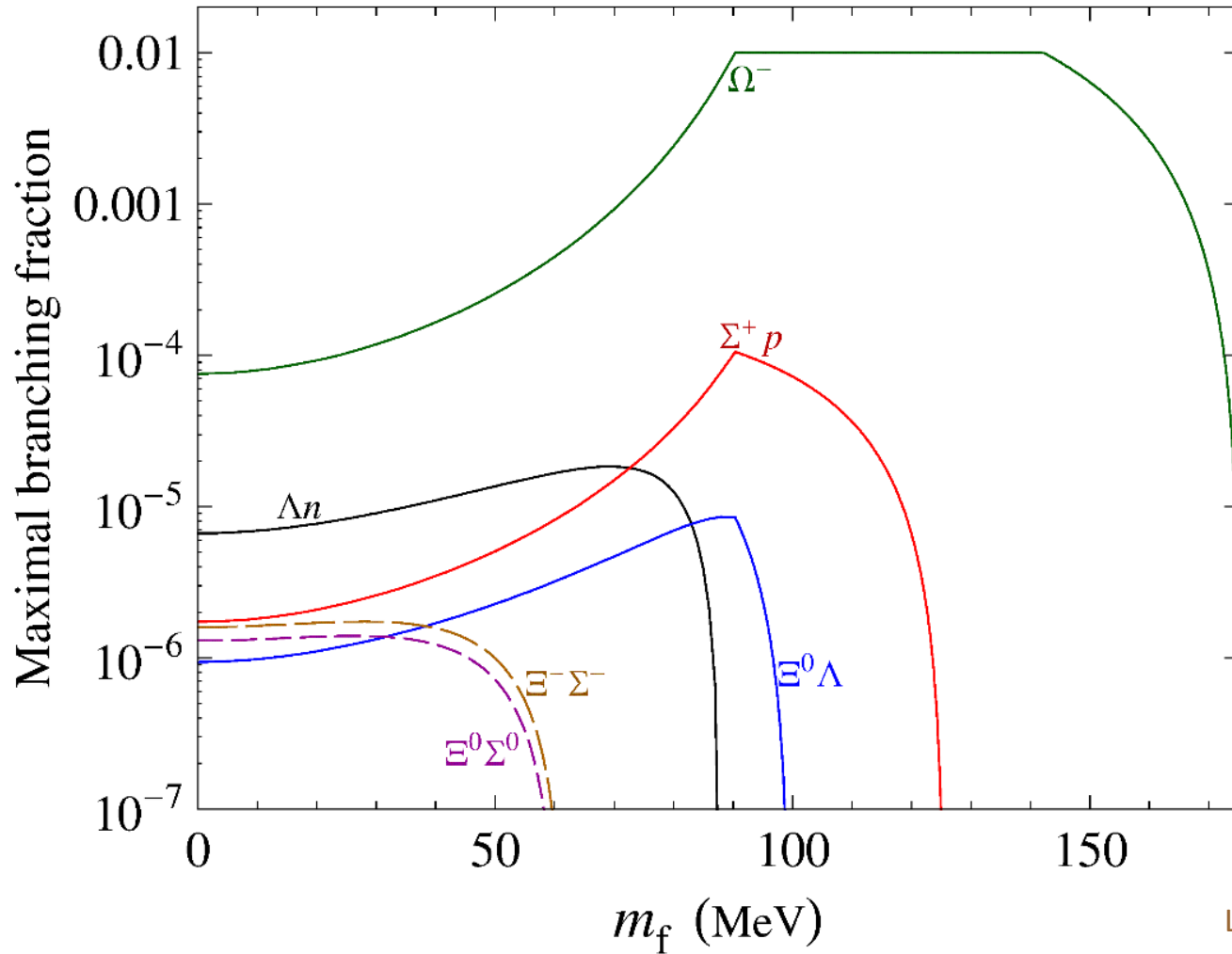
- If instead only \tilde{c}_f^V is nonvanishing, it evades the $K \rightarrow f\bar{f}$ constraints completely & is subject only to the milder $K \rightarrow \pi\pi'f\bar{f}$ ones.

- With $m_f > 0$, even more interesting possibilities could arise.

$$\mathcal{L}_f \supset -\bar{d}\gamma_5 s \bar{f}(\tilde{c}_f^S + \gamma_5 \tilde{c}_f^P)f - \bar{d}\gamma^n \gamma_5 s \bar{f}\gamma_\eta(\tilde{c}_f^V + \gamma_5 \tilde{c}_f^A)f + \text{H.c.}$$

Decay mode	$K \rightarrow f\bar{f}$	$K \rightarrow \pi\pi'f\bar{f}$	$\mathcal{B} \rightarrow \mathcal{B}'f\bar{f}$	$\Omega^- \rightarrow \Xi^-f\bar{f}$	$m_f > 0$ Ignoring $c_f^{V,A,S,P}$
Couplings	$\tilde{c}_f^A, \tilde{c}_f^S, \tilde{c}_f^P$	$\tilde{c}_f^V, \tilde{c}_f^A, \tilde{c}_f^S, \tilde{c}_f^P$	$\tilde{c}_f^V, \tilde{c}_f^A, \tilde{c}_f^S, \tilde{c}_f^P$	$\tilde{c}_f^V, \tilde{c}_f^A, \tilde{c}_f^S, \tilde{c}_f^P$	

- If instead only \tilde{c}_f^V is nonvanishing, it evades the $K \rightarrow f\bar{f}$ constraints completely & is subject only to the milder $K \rightarrow \pi\pi'f\bar{f}$ ones.
 - As m_f grows, the $K_L \rightarrow \pi^0\pi^0f\bar{f}$ constraint gets increasingly weaker and finally no longer applies for $m_f > 114$ MeV.
 - Consequently, as m_f grows, the upper limits of the hyperon branching fractions also rise & for $m_f > 114$ MeV only $\Sigma^+ \rightarrow pf\bar{f}$ & $\Omega^- \rightarrow \Xi^-f\bar{f}$ can serve as direct probes of \tilde{c}_f^V .
 - The size of \tilde{c}_f^V cannot be too large & needs to be consistent with perturbativity and Ω^- data requirements.



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FIG. 3: The maximal branching fractions of $\mathcal{B} \rightarrow \mathcal{B}' f \bar{f}$ with $\mathcal{B}\mathcal{B}' = \Lambda n, \Sigma^+ p, \Xi^0 \Lambda, \Xi^0 \Sigma^0, \Xi^- \Sigma^-$ and of $\Omega^- \rightarrow \Xi^- f \bar{f}$ versus m_f , induced by the contribution of $\text{Re } \tilde{\mathbf{c}}_f^Y$ alone, subject to the $K_L \rightarrow \pi^0 \pi^0$ constraint and the perturbativity and Ω^- data requirements for $m_f > 90$ MeV.

- Effective Lagrangian for $ds\phi\phi$ interactions at low energies

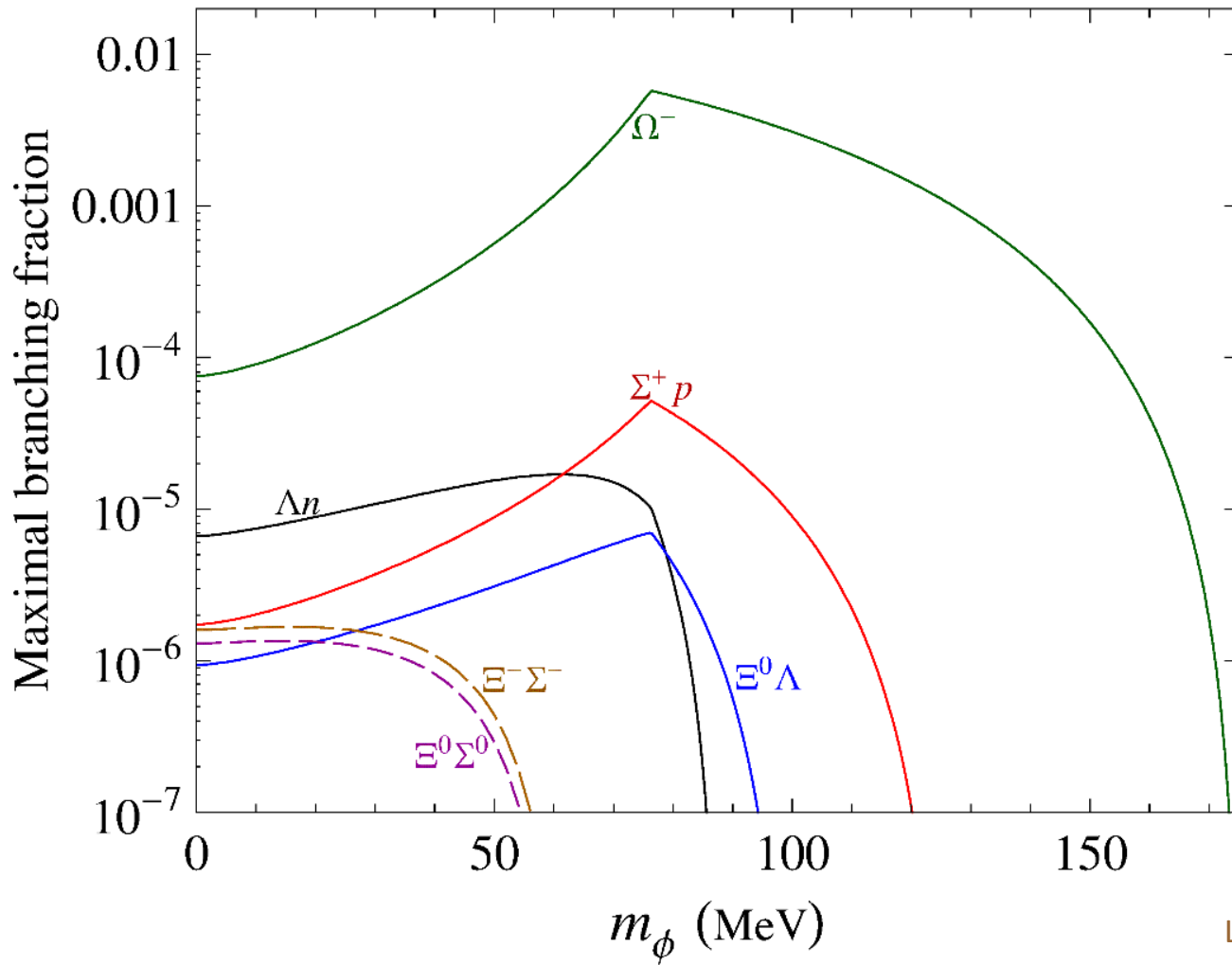
$$\mathcal{L}_\phi = - \left[(\mathbf{c}_\phi^V \bar{d}\gamma^\eta s + \mathbf{c}_\phi^A \bar{d}\gamma^\eta \gamma_5 s) i(\phi^\dagger \partial_\eta \phi - \partial_\eta \phi^\dagger \phi) + (\mathbf{c}_\phi^S \bar{d}s + \mathbf{c}_\phi^P \bar{d}\gamma_5 s) \phi^\dagger \phi \right] + \text{H.c.}$$

ϕ is a complex SM-gauge-singlet field charged under some symmetry of a nonstandard dark sector or odd under a Z_2 symmetry which does not affect SM particles.

Model-independently $\mathbf{c}_\phi^{V,A,S,P}$ are generally complex free parameters.

Kaon mode	$K \rightarrow \phi\bar{\phi}$	$K \rightarrow \pi\pi'\phi\bar{\phi}$	$K \rightarrow f\bar{f}$	$K \rightarrow \pi\pi'f\bar{f}$
Couplings	\mathbf{c}_ϕ^P	$\mathbf{c}_\phi^A, \mathbf{c}_\phi^P$	$\tilde{\mathbf{c}}_f^A, \tilde{\mathbf{c}}_f^S, \tilde{\mathbf{c}}_f^P$	$\tilde{\mathbf{c}}_f^V, \tilde{\mathbf{c}}_f^A, \tilde{\mathbf{c}}_f^S, \tilde{\mathbf{c}}_f^P$

TABLE II: New-physics couplings contributing to $K \rightarrow \cancel{E}$ and $K \rightarrow \pi\pi'\cancel{E}$ if \cancel{E} is carried away by spinless bosons $\phi\bar{\phi}$ or spin-1/2 fermions $f\bar{f}$ and their masses are nonzero, $\mathbf{m}_{\phi,f} > \mathbf{0}$. All these couplings belong to operators involving parity-odd ds quark bilinears.



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FIG. 1: The maximal branching fractions of $\mathcal{B} \rightarrow \mathcal{B}' \phi \bar{\phi}$ with $\mathcal{B}\mathcal{B}' = \Lambda n, \Sigma^+ p, \Xi^0 \Lambda, \Xi^0 \Sigma^0, \Xi^- \Sigma^-$ and of $\Omega^- \rightarrow \Xi^- \phi \bar{\phi}$, indicated on the plot by the $\mathcal{B}\mathcal{B}'$ and Ω^- labels, respectively, versus m_ϕ , induced by the contribution of $\text{Re } \mathbf{c}_\phi^A$ alone, subject to the $K_L \rightarrow \pi^0 \pi^0 \cancel{E}$ constraint and the perturbativity requirement for $m_\phi > 76$ MeV.

Conclusions

- Flavor-changing neutral current hyperon & kaon decays with missing energy are potentially sensitive to physics beyond the SM, but they do not probe the same set of the underlying NP operators.
- The proposed BESIII measurements on the hyperon modes may test parts of the NP parameter space better than present kaon data can.
- Two of the hyperon modes serve as the only direct probes of certain types of NP involving invisible particles in the 114-175 MeV mass range.
- Ongoing & future experiments on these rare hyperon decays can offer useful information on possible NP effects which is complementary to that gained from the kaon sector.