

# Connecting **CMB** and **dark matter** through **reheating**: Minimal plateau inflation



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DM, Pankaj Saha, [PRD98, 103525 \(2018\)](#)

[Phy.Dark.Univ. 25, 100317\(2019\)](#)

[CQG 36 \(2019\) 045010](#)

[JCAP 1907, 018 \(2019\)](#)

# Tornado



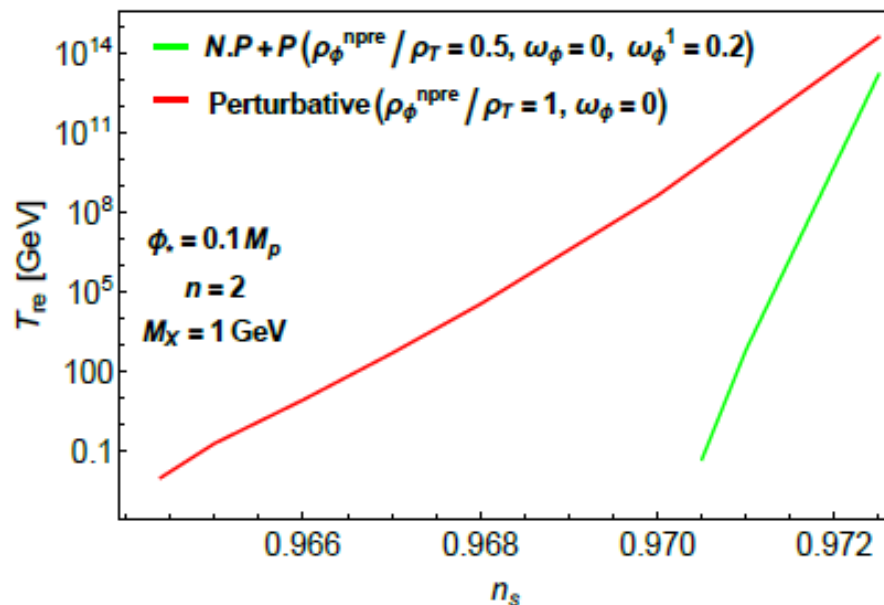
# CMB, dark matter through reheating

$$n_s - 1 \equiv \frac{d \ln \Delta_s^2}{d \ln k}$$

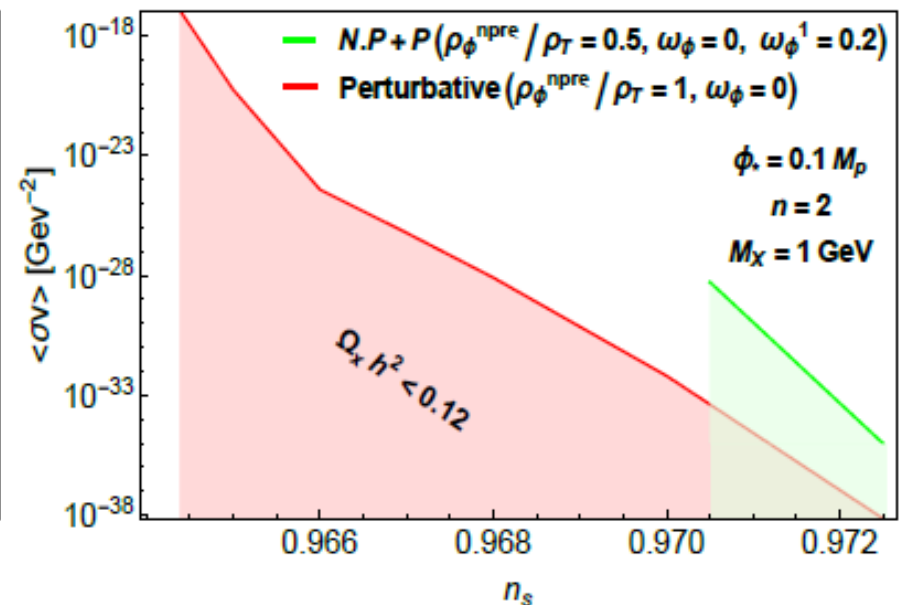
$$\Delta_s^2(k) \equiv \frac{k^3}{2\pi^2} P_\zeta(k)$$

$$C_\ell^{TT} = \frac{2}{\pi} \int k^2 dk \underbrace{P_\zeta(k)}_{\text{Inflation}} \underbrace{\Delta_{T\ell}(k)\Delta_{T\ell}(k)}_{\text{Anisotropies}}$$

## CMB-reheating

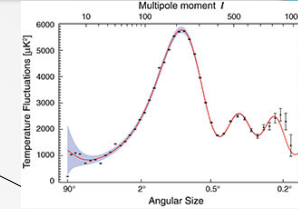
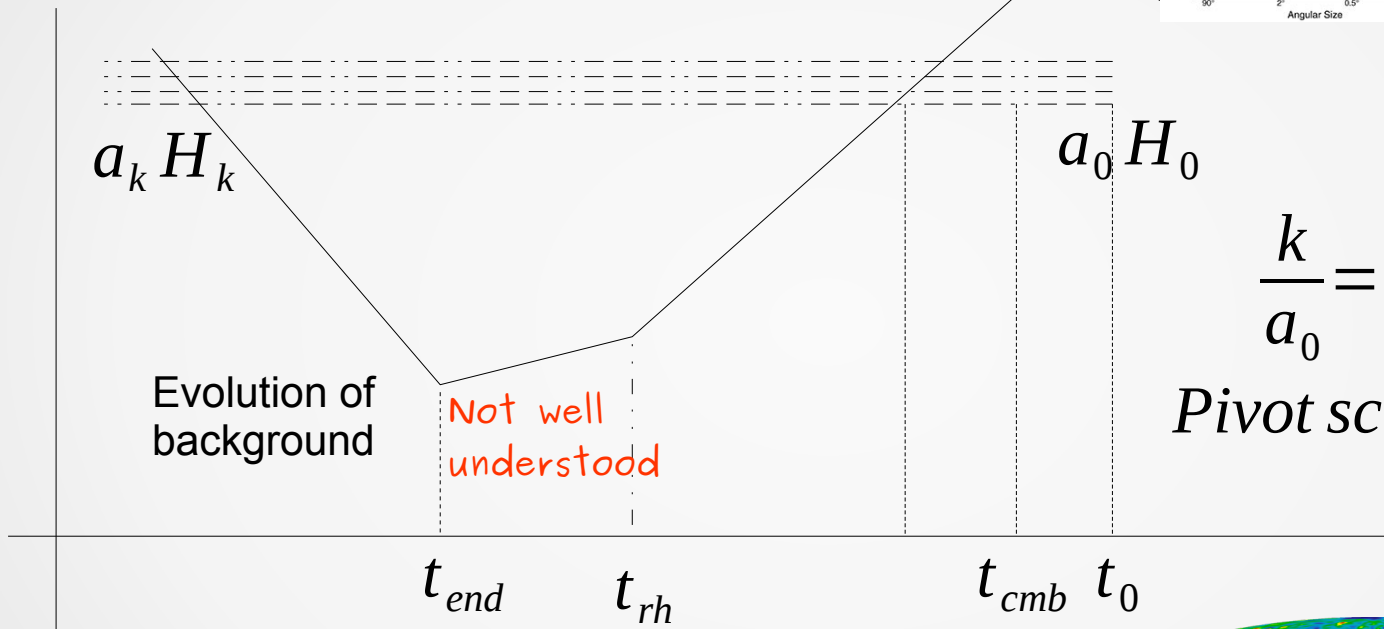


## CMB-dark matter



# Assuming the following Background+fluctuation

Evolution of fluctuation scale

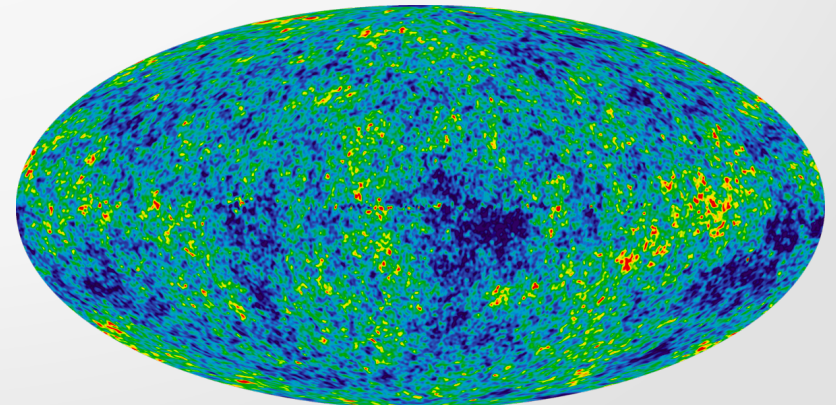


$\langle \delta T \delta T \rangle$

$$\frac{k}{a_0} = 0.002 \text{ Mpc}^{-1}$$

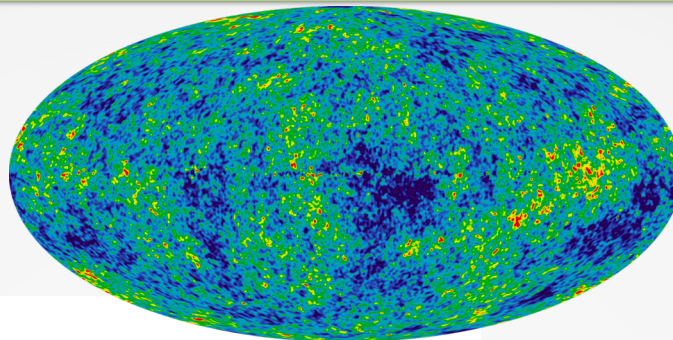
Pivot scale of *PLANCK*

$$\frac{\delta T}{T_0} \sim 10^{-5}$$

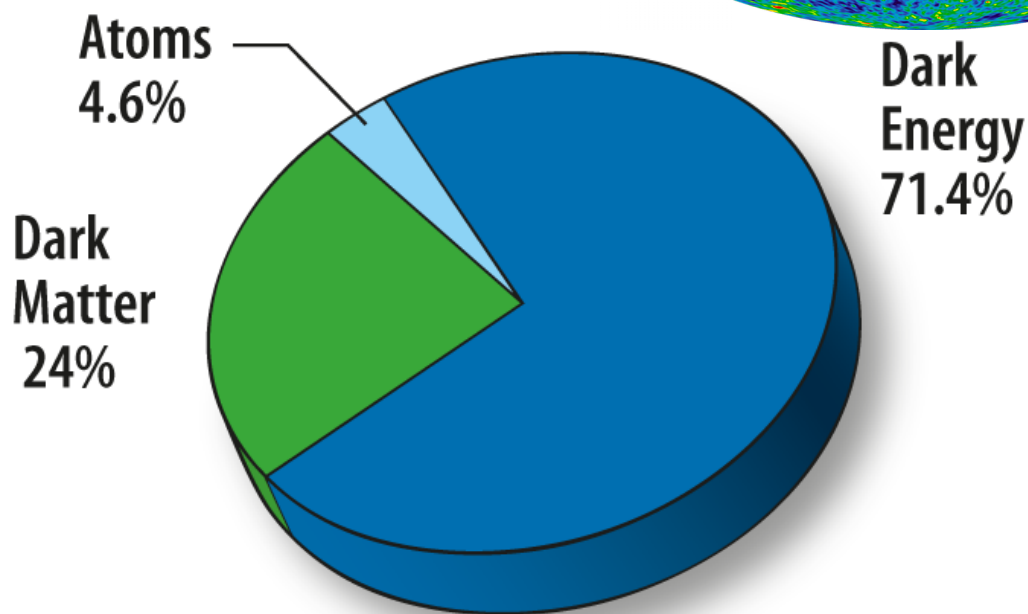


# Given the inflationary background what do we observe today?

Extremely homogeneous CMB  
Many more...



P.A.R Ade et. al.  
ArXiv:1502:01589



TODAY

No understanding of dark energy  
(Cosmological constant,  
Quintessence ...)

No understanding of Dark matter  
(WIMP, axion...)

Talks on CMB observation:  
T. Ghosh, K. Ichiki, O. Tajima, T.  
Hoang

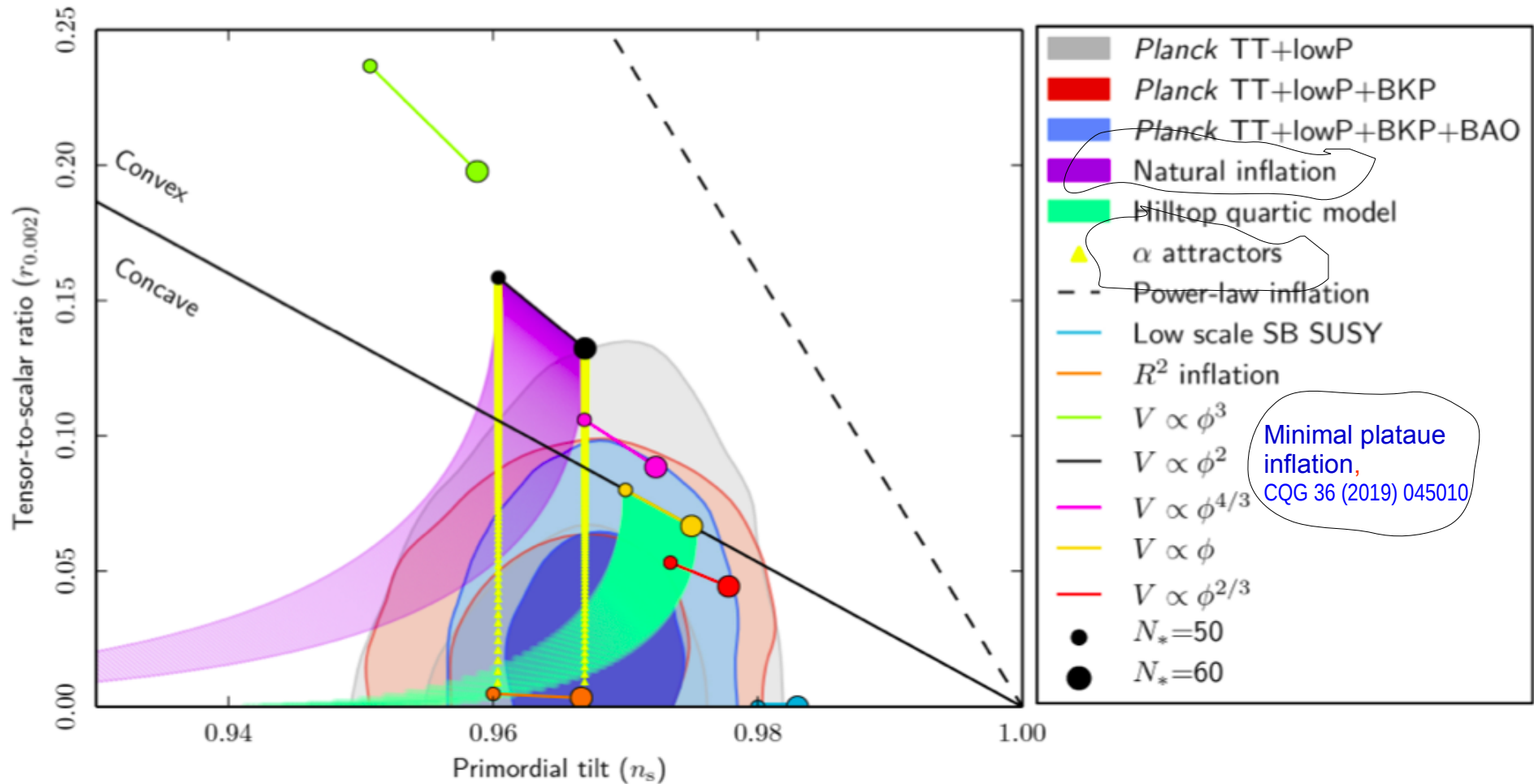
emptiness

## What inflation models

# Planck-2015: Where do we stand?

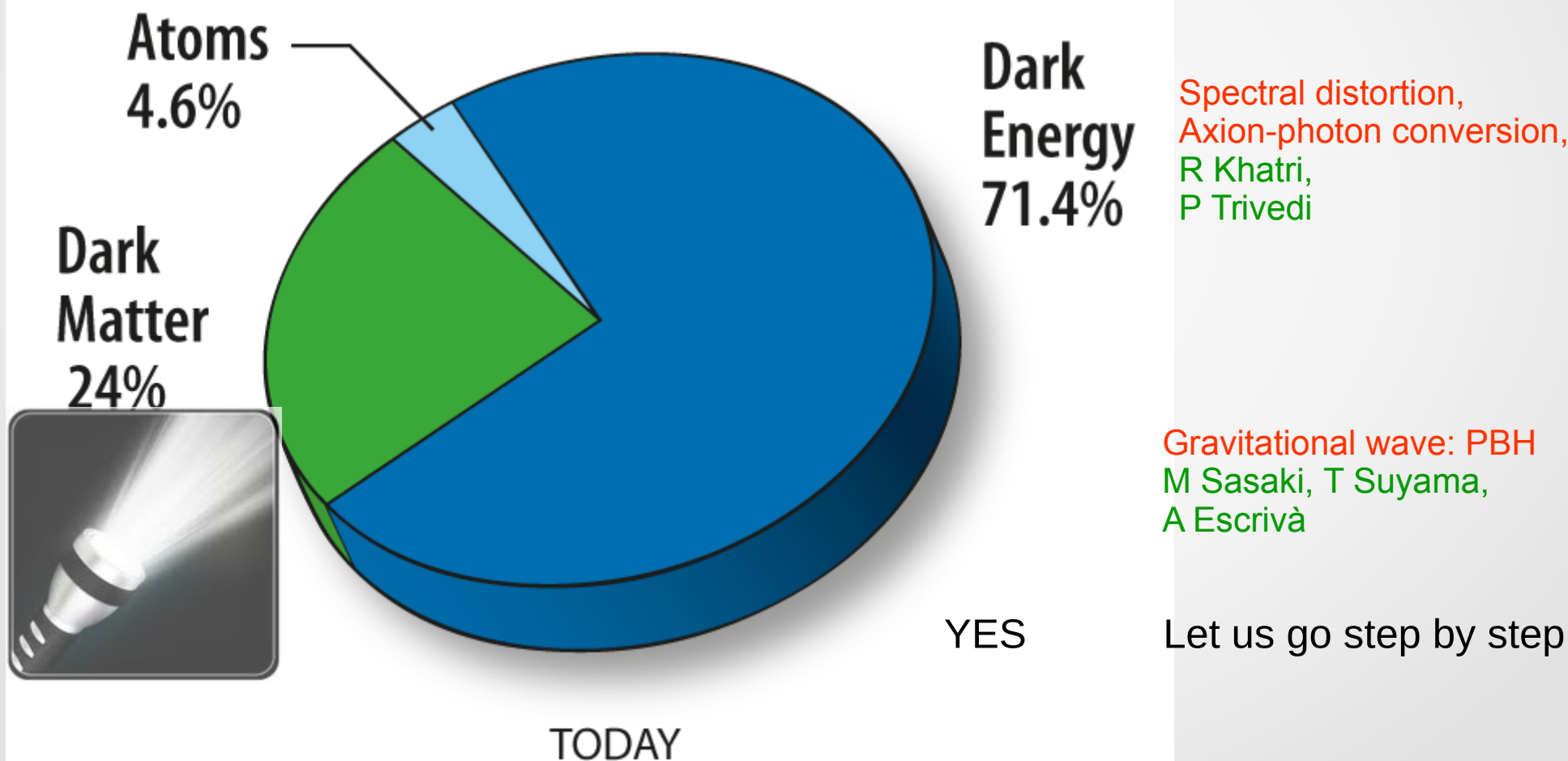


P. A. R Ade et. al. ArXiv:1502:01589



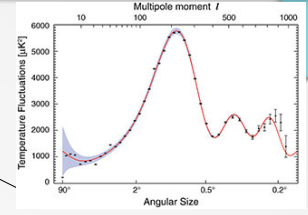
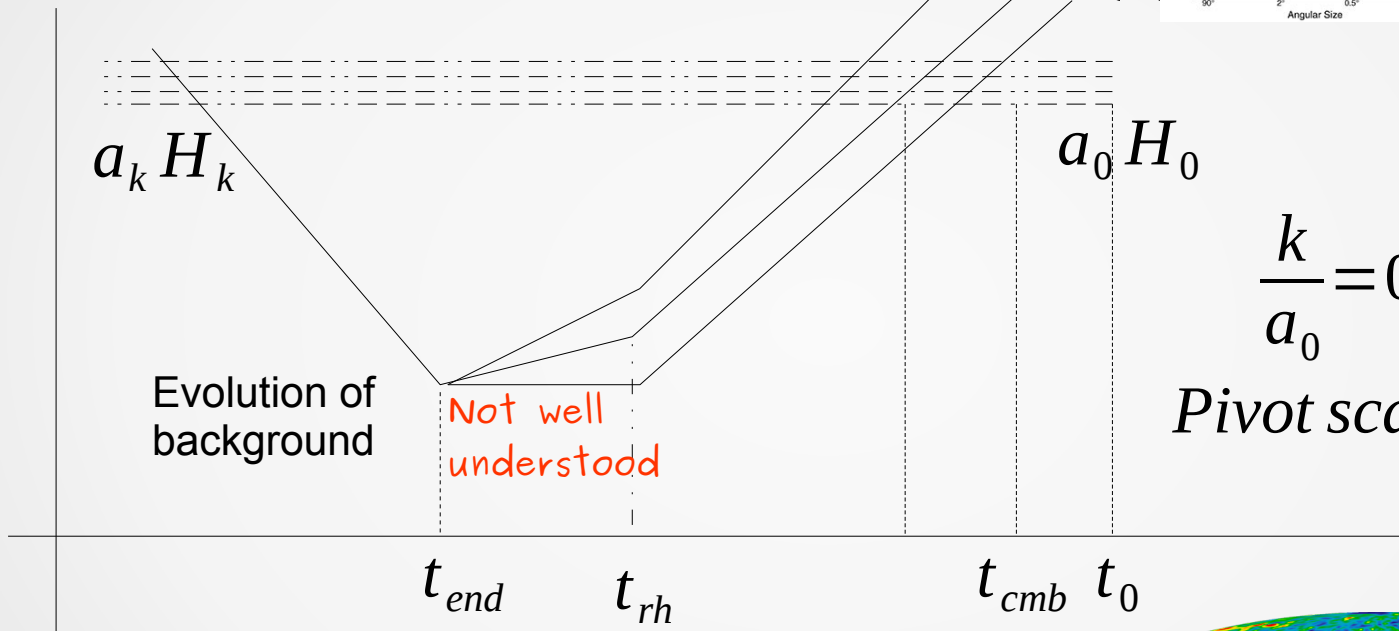
## Given the inflationary background

Does CMB have any role to play in understanding the dark matter phenomenology?



# Play with reheating era

Evolution of fluctuation scale

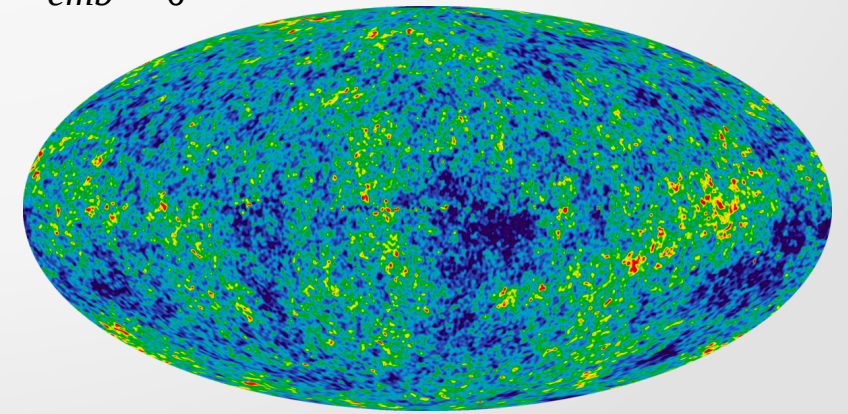


$$\langle \delta T \delta T \rangle$$

$$\frac{k}{a_0} = 0.002 \text{ Mpc}^{-1}$$

Pivot scale of PLANCK

$$\frac{\delta T}{T_0} \sim 10^{-5}$$





# Plan



- Formalism

CMB vs reheating temperature

CMB, reheating and dark matter

- Particular model

Minimal plateau inflation, Results

- Further generalisation

- conclusions

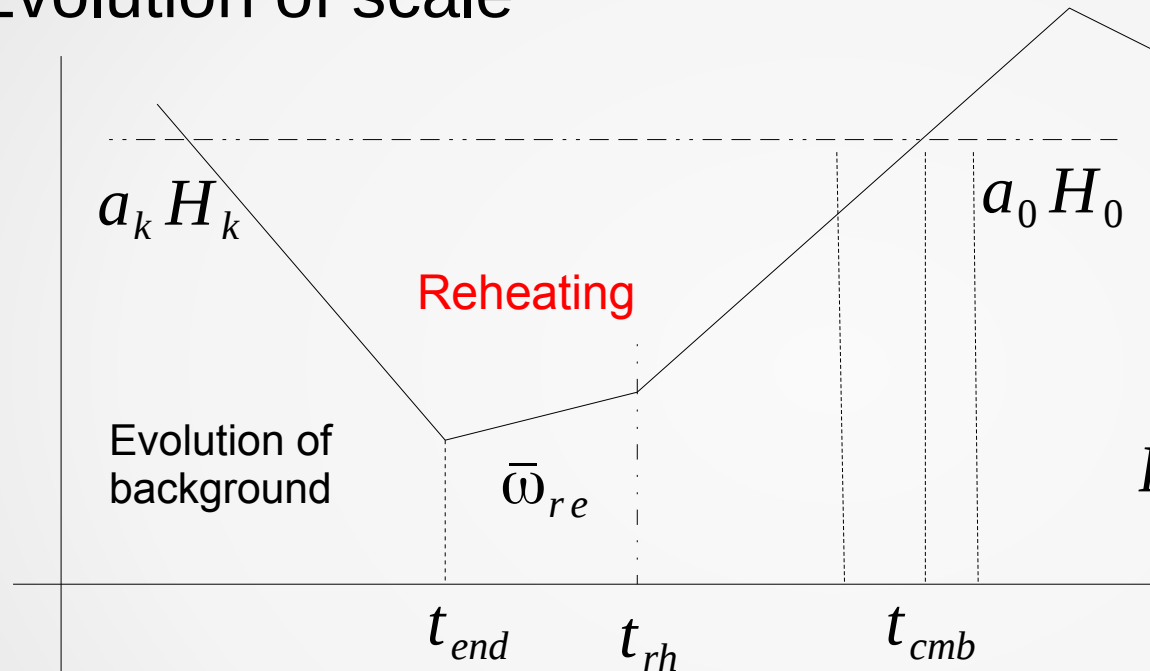
# CMB and reheating

$n_s$  vs  $T_{re}$



L. Dai, M. Kamionkowski and J. Wang, PRL. 113, 041302 (2014), J. L. Cook, etal JCAP 1504 (2015) 047; J. Ellis etal, JCAP 1507 (2015,, 050; Y. Ueno and K. Yamamoto, PRD 93 (2016), 083524; M. Eshaghi etal, PRD 93 (2016), 123517, A. Di Marco, etal, PRD 95 (2017),, 103502, S. Bhattacharya etal, PRD 96 (2017), 083522, ...

- Evolution of scale



$$\rho(t) = \rho_{\phi}^i a^{3(1+\bar{\omega}_{re})}$$

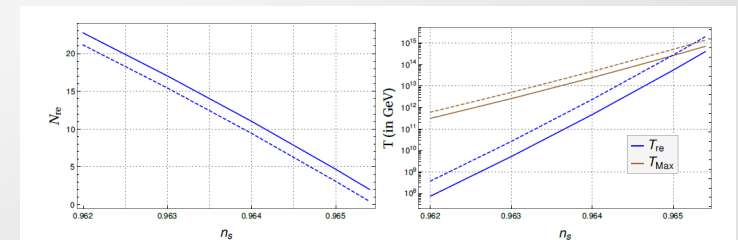
$k = 0.02 \text{ Mpc}^{-1}$   
Pivot scale of PLANCK

$N_{re}, T_{re}, \bar{\omega}_{re}$

$$\ln \left( \frac{a_k H_k}{a_0 H_0} \right) = -N_k - N_{re} - \ln \left( \frac{a_{re} H_k}{a_0 H_0} \right)$$

$$g_{re} T_{rad}^3 = \left( \frac{a_0}{a_{re}} \right)^3 \left( 2T_0^3 + 6 \times \frac{7}{8} T_{\nu 0}^3 \right)$$

$$T_{re} = \left( \frac{43}{11g_{re}} \right)^{\frac{1}{3}} \left( \frac{a_0 T_0}{k} \right) H_k e^{-N_k} e^{-N_{re}}$$



# CMB and reheating- Decaying inflaton

L. Dai, M. Kamionkowski and J. Wang, PRL. 113, 041302 (2014)  
DM, arXiv:1709.00251

- Reheating is model dependent: Inflaton  $\rightarrow$  radiation

$$\ddot{n}_{re} = -2\dot{n}_{re}^2 + \frac{1-3w}{6M_P^2} \rho_\phi$$

$$n_{re} = \ln \left( \frac{a(t)}{a(t_i)} \right)$$

$$\frac{\rho_{rad}^f}{\rho_\phi^i} = e^{-4N_{re}} - \frac{\rho_\phi^f}{\rho_\phi^i} + (1-3w)e^{-4N_{re}} \int_i^f \dot{n}_r \left( \frac{\rho_\phi}{\rho_\phi^i} \right) e^{4n_r} dt$$

$$N_{re} = \ln \left( \frac{a(t_f)}{a(t_i)} \right)$$

$$\rho_{rad}(t_i) = 0 ; \quad \dot{n}_{re}(t_i) = \sqrt{\frac{\rho_\phi^i}{3M_P^2}}$$

$$\rho_\phi(t) = \rho_\phi^i e^{-3(1+w)n_{re}} e^{-\Gamma(t-t_i)}$$

At  $t=t_f$   
 $\Gamma = \dot{n}_{re}(t_f) = H_{re}$

$$T_{re} = \left( \frac{43}{11g_{re}} \right)^{\frac{1}{3}} \left( \frac{a_0 T_0}{k} \right) H_k e^{-N_k} e^{-N_{re}}$$

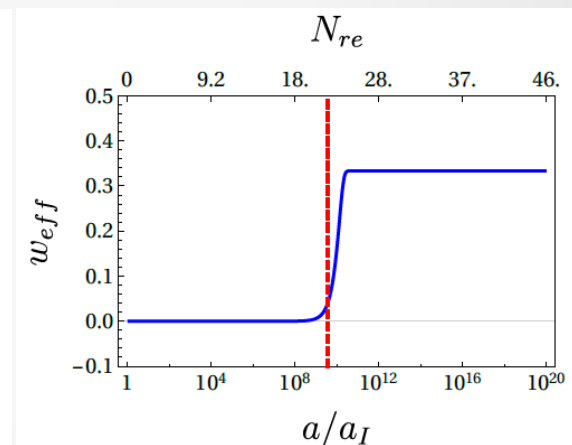
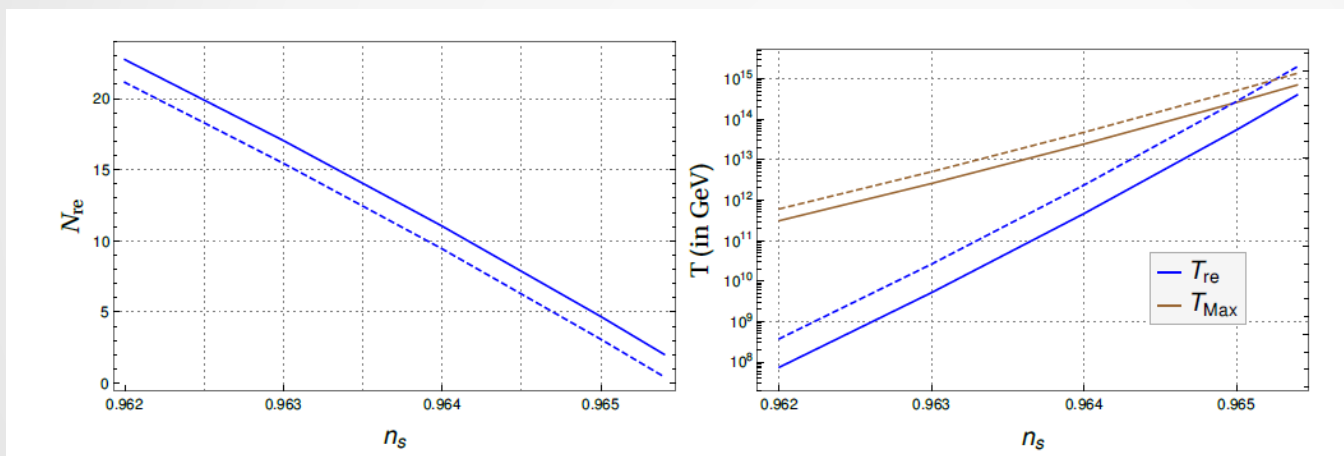
$$\rho_{rad}^f = \pi^2 (g_{re}/30) T_{rad}^4$$

# $n_s$ vs $T_{re}$ with inflaton decay

- Radiation is decaying into radiation field (For chaotic inflation)

- $\rho_\phi(t) = \rho_\phi^i e^{-3(1+w)n_{re}} e^{-\Gamma(t-t_i)}$  (Solid lines) DM, arXiv:1709.00251

Chaotic  
inflation



$$w_{eff} = \left\langle \frac{3p_\phi + \rho_{rad}}{3(\rho_\phi + \rho_{rad})} \right\rangle$$

$$\omega \rightarrow \bar{\omega}_{re}$$

Dotted lines: complete conversion, inflaton energy  $\rightarrow$  radiation

L. Dai, M. Kamionkowski and J. Wang, PRL. 113, 041302 (2014)

$$\rho_\phi(t) = \rho_\phi^i e^{-3(1+w)n_{re}} e^{-\Gamma(t-t_i)}$$



## Going beyond: dark matter (perturbative)

- Assumption: Dark matter coupled to radiation field
- Inflaton  $\rightarrow$  radiation  $\rightarrow$  (radiation + dark matter)

$$\Phi = \frac{\rho_\phi a^{3(1+w_\phi)}}{m_\phi^{(1-3w_\phi)}}; \quad R = \rho_R a^4; \quad X = n_X a^3. \quad A = a/a_I$$

Unitarity limit

$$\langle \sigma v \rangle_{MAX} = 8\pi/M_X^2$$

Parameters

$$T_{re} = \Gamma, M_X, \langle \sigma v \rangle$$

$$\begin{aligned} \frac{d\Phi}{dA} &= -c_1(1+w_\phi) \frac{A^{1/2}\Phi}{\mathbb{H}}; \quad \mathbb{H} = (\Phi/A^{3w_\phi} + R/A + X \langle E_X \rangle / m_\phi)^{1/2} \\ \frac{dR}{dA} &= c_1(1+w_\phi) \frac{A^{3(1-2w_\phi)/2}}{\mathbb{H}} \Phi + c_2 \frac{A^{-3/2} \langle E_X \rangle \langle \sigma v \rangle M_{pl}}{\mathbb{H}} (X^2 - X_{eq}^2) \\ \frac{dX}{dA} &= -c_2 \frac{A^{-5/2} \langle E_X \rangle \langle \sigma v \rangle M_{pl}}{\mathbb{H}} (X^2 - X_{eq}^2); \end{aligned}$$

$$\begin{aligned} \Omega_X h^2 &= \frac{\rho_X(T_F)}{\rho_R(T_F)} \frac{T_F}{T_{now}} \Omega_R h^2, \\ &= \langle E_X \rangle \frac{X(T_F)}{R(T_F)} \frac{T_F}{T_{now}} \frac{A_F}{m_\phi} \Omega_R h^2 \end{aligned}$$

# Parameter counting

Unique Initial conditions:

$$\Phi(1) = \frac{3}{8\pi} \frac{M_{pl}^2 H_I^2}{m_\phi^4}; \quad R(1) = X(1) = 0.$$

Boundary conditions:

$$\Omega_X h^2 = 0.12$$

$$T_{re} = \left( \frac{43}{11g_{re}} \right)^{\frac{1}{3}} \left( \frac{a_0 T_0}{k} \right) H_k e^{-N_k} e^{-N_{re}}$$

3 Parameters

$$T_{re} \approx \Gamma, M_X, \langle \sigma v \rangle$$

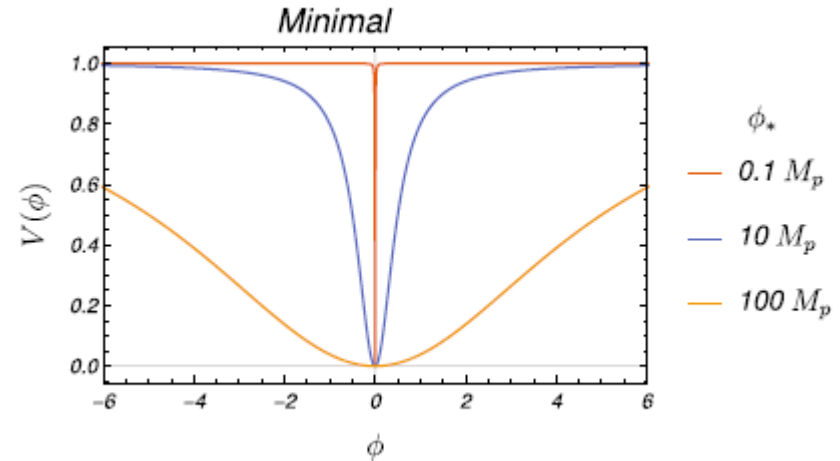
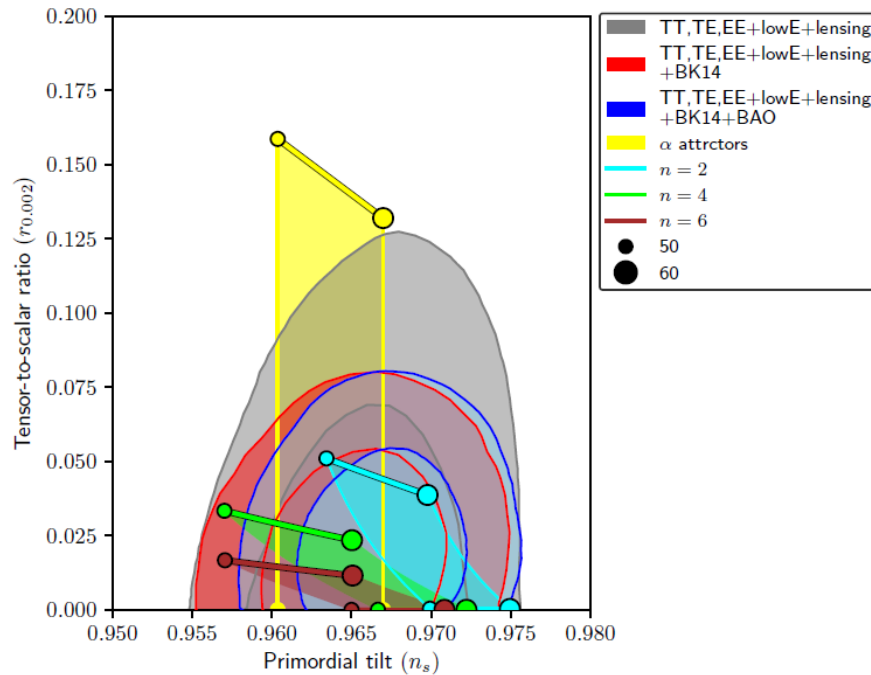
$$T_{re} \equiv T_{rad}^{end} = [30/\pi^2 g_*(T)]^{1/4} \rho_R(\Gamma, n_s, M_X)^{1/4}.$$

Therefore **GIVEN** a dark matter mass, all other parameters are uniquely fixed: Therefore, we can successfully establish the connection we were looking for.

# Model: Minimal Plateau Inflation

CQG 36 (2019) 045010

$$V_{\min}(\phi) = \frac{m^{4-n}\phi^n}{1 + \left(\frac{\phi}{\phi_*}\right)^n}$$



$\frac{\phi_*}{M_p}$	$n$	$n_s$	$r$	$dn_s^k$	$\Delta\phi$
0.01	2	0.969	$4 \times 10^{-5}$	-0.00066	0.39
	4	0.966	$2 \times 10^{-6}$	-0.00066	0.12
	6	0.965	$3 \times 10^{-7}$	-0.00069	0.06
1.00	2	0.969	$4 \times 10^{-3}$	-0.0006	3.53
	4	0.966	$9.6 \times 10^{-4}$	-0.0007	2.13
	6	0.964	$3.5 \times 10^{-4}$	-0.0007	1.47

All these prediction are for  $\phi_* = 0.01M_p$ .

$n$	$n_s$	$T_{re}$ (GeV)	$N_{re}$	$N_k$
2	0.9723	$1 \times 10^{15}$	0.4	54
	0.9702	$1 \times 10^3$	32	50
6	0.9670	$1 \times 10^{14}$	00	53
	0.9679	$2 \times 10^3$	23	55
8	0.9659	$7 \times 10^{13}$	0.6	53
	0.9673	$1 \times 10^3$	23	55

The spectral quantities for different values of  $n$  for 50 e folding.

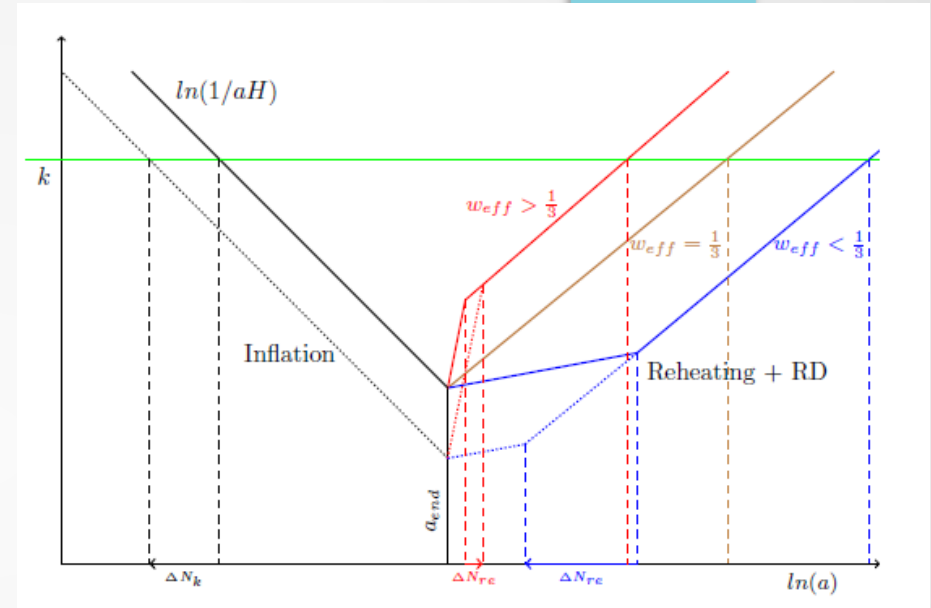
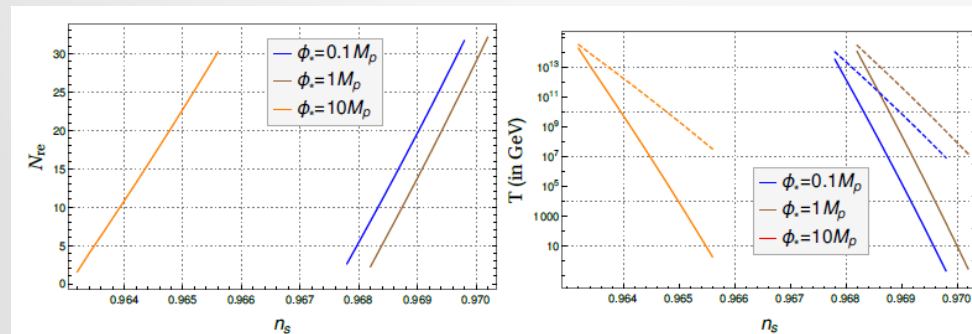
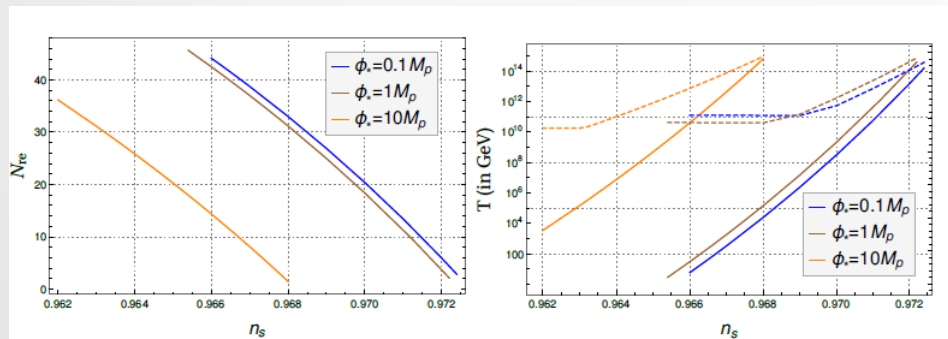
$$w_\phi \equiv \frac{P_\phi}{\rho_\phi} \simeq \frac{\langle \phi V'(\phi) \rangle - \langle 2V \rangle}{\langle \phi V'(\phi) \rangle + \langle 2V \rangle} = \frac{n-2}{n+2}$$

# Minimal Plateau inflation: Perturbative reheating

PRD98, 103525 (2018)  
 Phy.Dark.Univ. 25, 100317(2019)

$$w_\phi \equiv \frac{P_\phi}{\rho_\phi} \simeq \frac{\langle \phi V'(\phi) \rangle - \langle 2V \rangle}{\langle \phi V'(\phi) \rangle + \langle 2V \rangle} = \frac{n-2}{n+2}$$

Effect of different inflaton equation of state during reheating

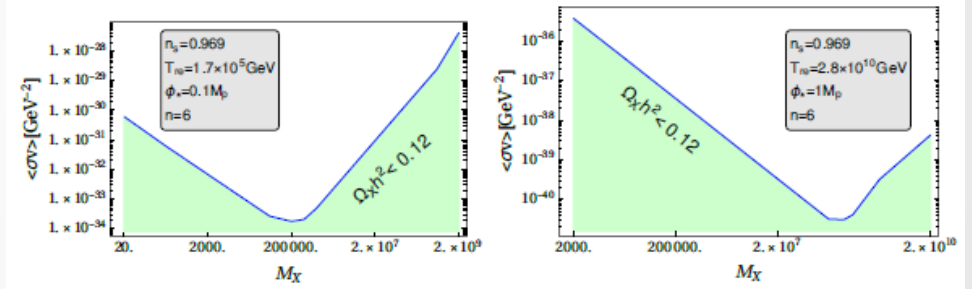
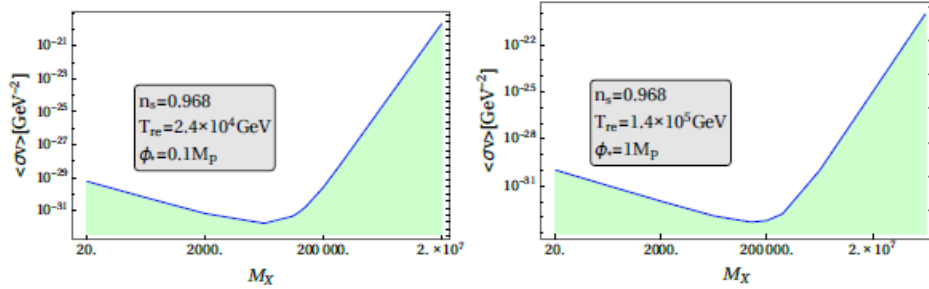
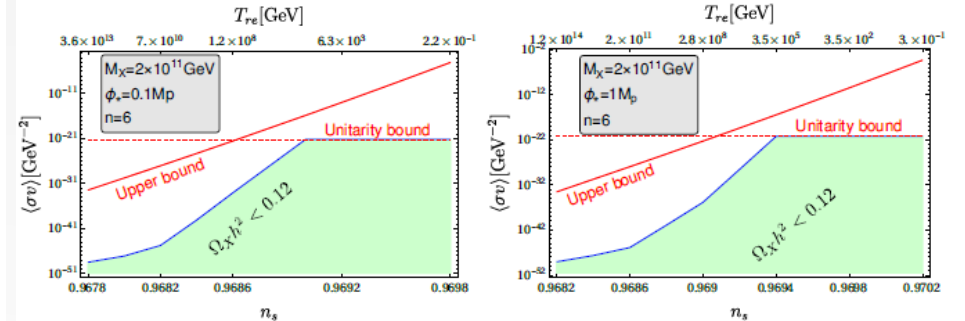
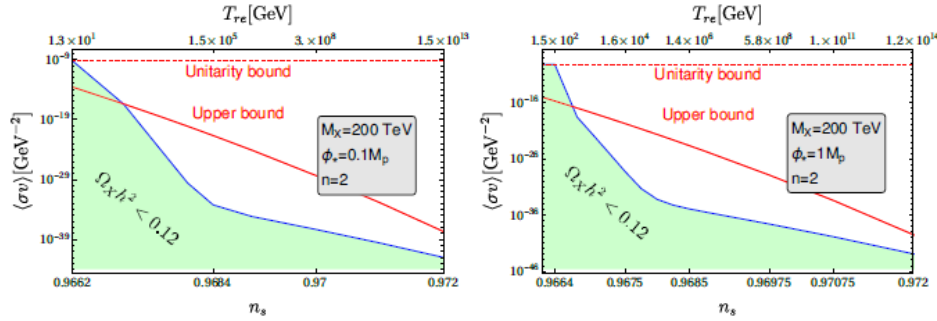


All these prediction are for  $\phi_* = 0.01 M_p$ .

$n$	$n_s$	$T_{re}$ (GeV)	$N_{re}$	$N_k$
2	0.9723	$1 \times 10^{15}$	0.4	54
	0.9702	$1 \times 10^3$	32	50
6	0.9670	$1 \times 10^{14}$	00	53
	0.9679	$2 \times 10^3$	23	55
8	0.9659	$7 \times 10^{13}$	0.6	53
	0.9673	$1 \times 10^3$	23	55



# Constraining dark matter parameter space



$$\Omega_X h^2 \propto \langle\sigma v\rangle M_X^4 \exp\left[-\frac{(17+w)M_X}{(1+w)T_{\max}}\right] \text{ for } M_X \gtrsim T_{\max}$$

$$\Omega_X h^2 \propto \langle\sigma v\rangle \frac{T_{re}^{\frac{7+3w_\phi}{1+w_\phi}}}{M_X^{\frac{2(1+w_\phi)}{1+w_\phi}}} \propto \frac{\langle\sigma v\rangle}{M_X^{\frac{2(1+w_\phi)}{1+w_\phi}}} \left[\left(\frac{a_0 T_0}{k}\right) H_k e^{-N_k} e^{-N_{re}}\right]^{\frac{7+3w_\phi}{1+w_\phi}} \text{ for } T_{\max} > M_X > T_{re}$$

$$\Omega_X h^2 \propto \langle\sigma v\rangle M_X T_{re} \propto \langle\sigma v\rangle M_X \left(\frac{a_0 T_0}{k}\right) H_k e^{-N_k} e^{-N_{re}} \text{ When } M_X < T_{re}. \quad (24)$$

TABLE X:  $\phi_* = 0.1 M_p$

$n$	$N_{re}$	$T_{re}(\text{GeV})$	$\langle\sigma v\rangle \text{GeV}^{-2}$ $M_X(200\text{TeV})$
2	33	$2.4 \times 10^4$	$3 \times 10^{-30}$
4	-	-	-
6	5	$1.6 \times 10^{12}$	$7 \times 10^{-42}$
8	-	-	-

TABLE XI:  $\phi_* = 1 M_p$

$n_s$	$N_{re}$	$T_{re}(\text{GeV})$	$\langle\sigma v\rangle \text{GeV}^{-2}$ $M_X(200\text{TeV})$
2	31	$1.4 \times 10^5$	$6 \times 10^{-34}$
4	-	-	-
6	13	$1.3 \times 10^8$	$7 \times 10^{-38}$
8	8	$6 \times 10^{10}$	$2 \times 10^{-40}$

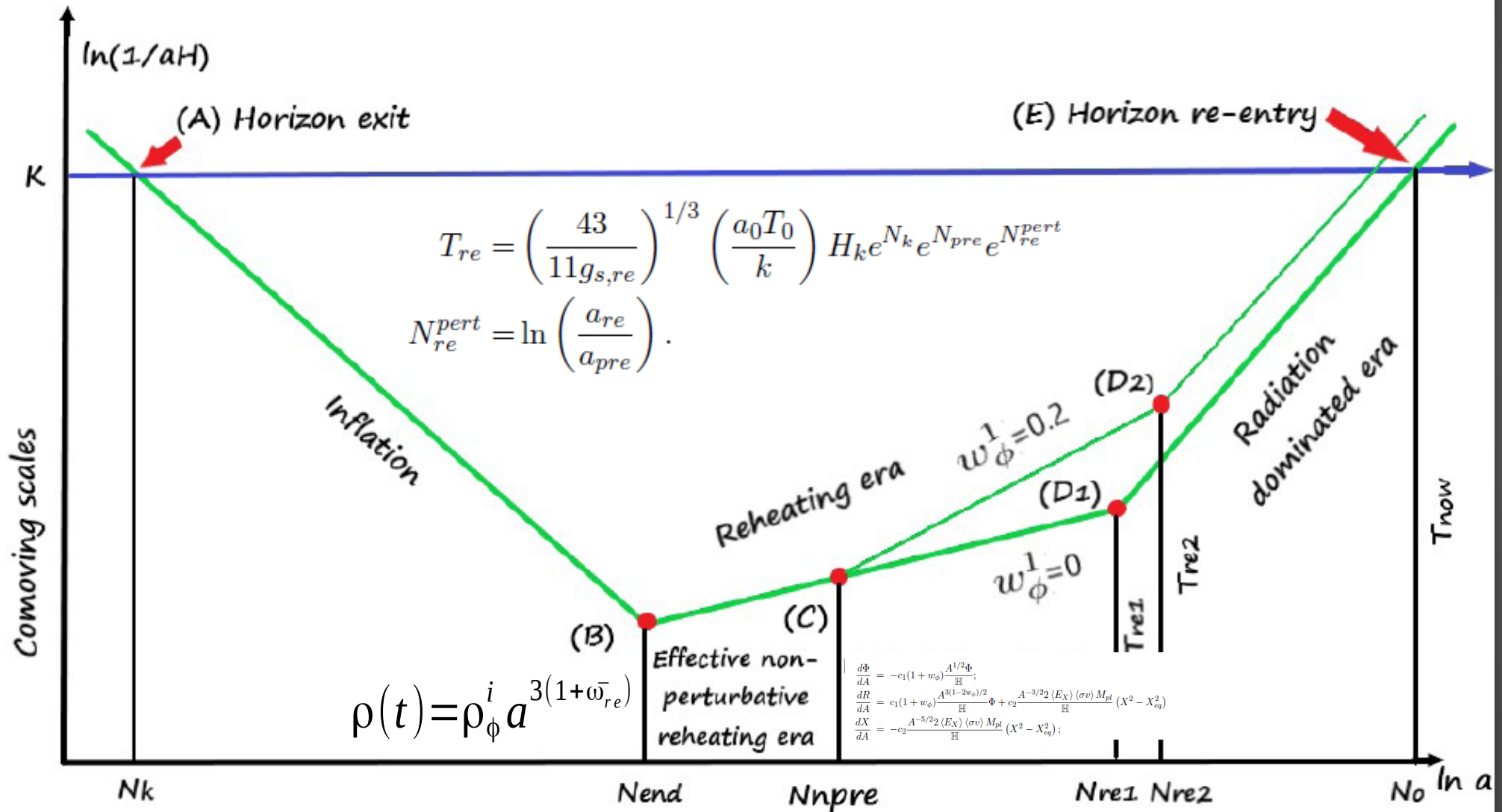
TABLE XII:  $\phi_* = 10 M_p$

$n$	$N_{re}$	$T_{re}(\text{GeV})$	$\langle\sigma v\rangle \text{GeV}^{-2}$ $M_X(200\text{TeV})$
2	1.5	$6 \times 10^{14}$	$3 \times 10^{-44}$
4	-	-	-
6	-	-	-
8	-	-	-

$$\log_{10}(T_{re} \text{ GeV}) \simeq Q_p [A + B(n_s - 0.962) + C(n_s - 0.962)^2]$$

$$n_s = 0.968$$

# Non perturbative effects: Boltzmann framework



# Nonperturbative aspects(Lattice result)

JCAP 1907 (2019) no.07, 018

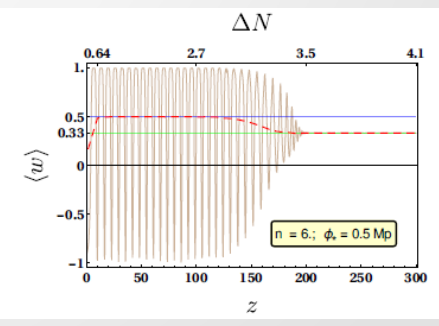
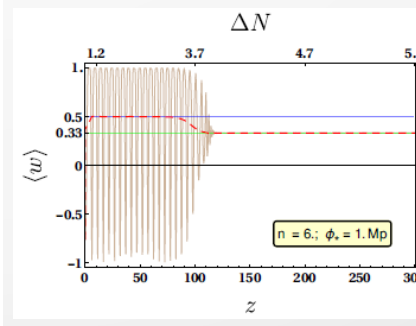
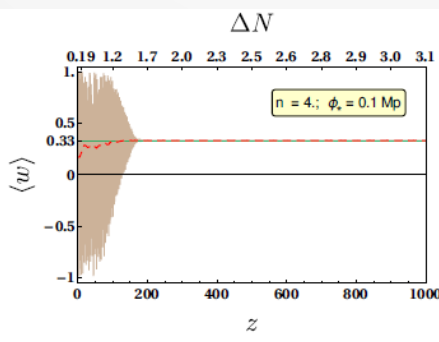
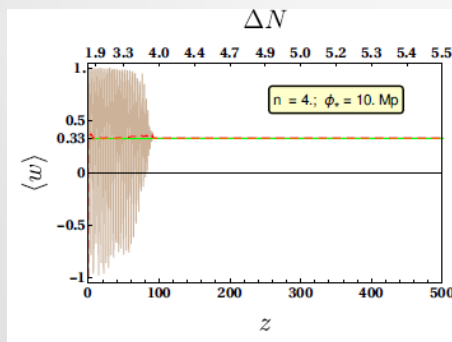
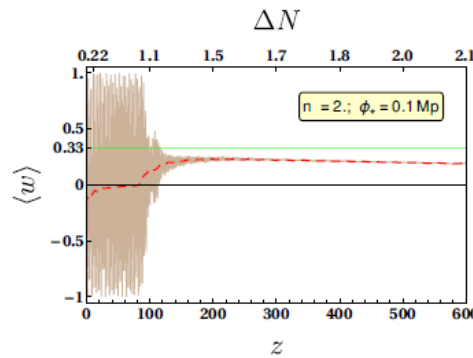
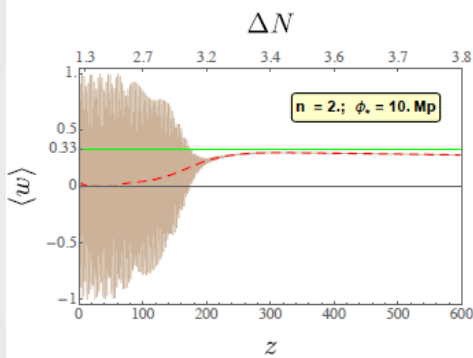
$$V(\phi, \chi) = \frac{1}{n} \frac{\lambda m^{4-n} \phi^n}{\left[1 + \left(\frac{\phi}{\phi_*}\right)^n\right]} + \frac{1}{2} g^2 \phi^2 \chi^2.$$

$$\omega_\phi^1 \approx 0.22 \quad \text{for } n=2$$

$$\omega_\phi^1 \approx 0.33 \quad \text{for } n=4,6,$$

$$T_{re} = \left(\frac{43}{11g_{s,re}}\right)^{1/3} \left(\frac{a_0 T_0}{k}\right) H_k e^{N_k} e^{N_{pre}} e^{N_{re}^{pert}}$$

$$N_{re}^{pert} = \ln\left(\frac{a_{re}}{a_{pre}}\right).$$

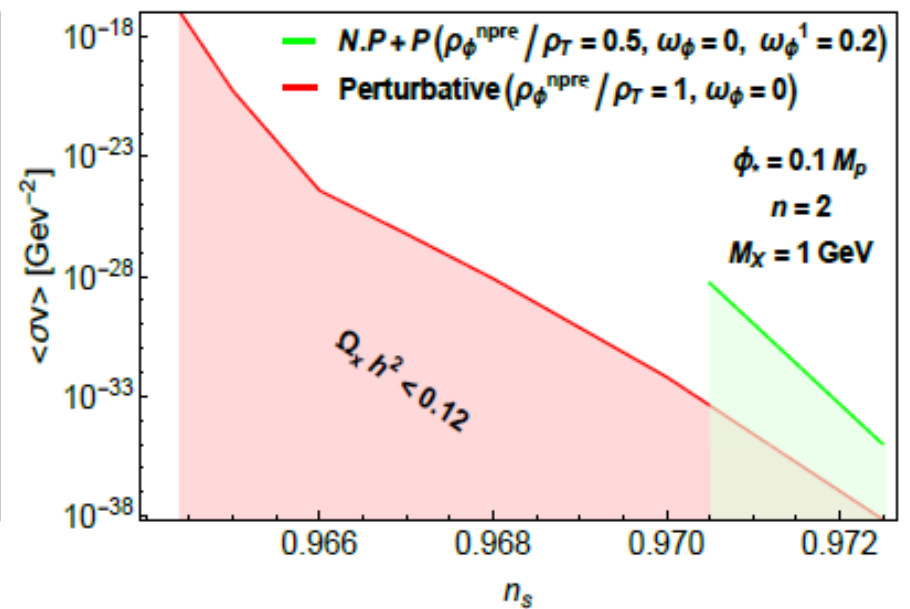
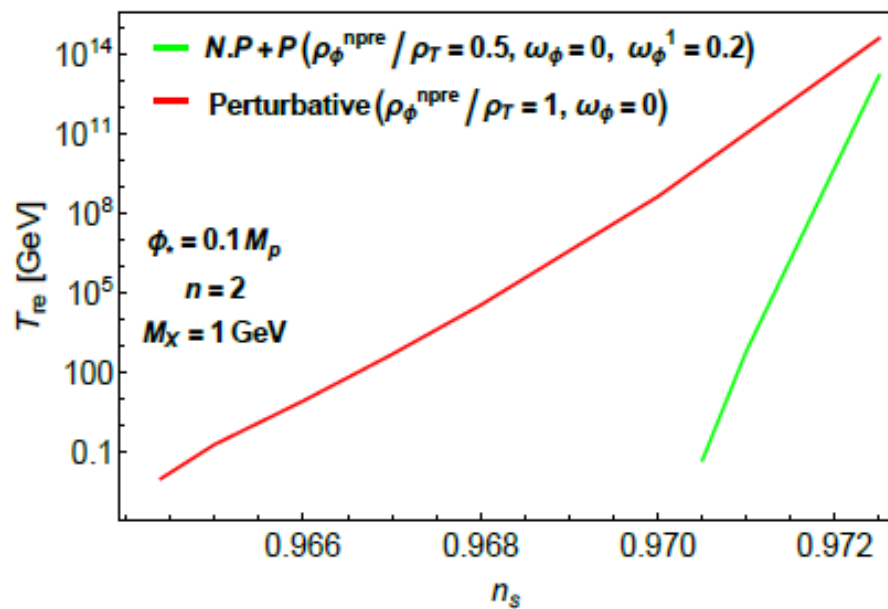


# Non-perturbative: n=2 case

$$T_{re} = \left( \frac{43}{11g_{s,re}} \right)^{1/3} \left( \frac{a_0 T_0}{k} \right) H_k e^{N_k} e^{N_{pre}} e^{N_{re}^{pert}}$$

$$N_{re}^{pert} = \ln \left( \frac{a_{re}}{a_{pre}} \right).$$

$$T_{re} \equiv T_{rad}^{end} = [30/\pi^2 g_*(T)]^{1/4} \rho_R(\Gamma, n_s, M_X)^{1/4}.$$



# Conclusions and future directions



- Assuming the **perturbative reheating** scenario, CMB can constrain the dark matter phenomenology.
- Pin pointing the value of **scalar spectral** index is very important
- Full non-linear evolution: Effect of non-perturbative dynamics will be necessary
- Inflaton-dark matter model construction

Thank you