

# ***H0 Tension: New Physics or Systematics?***

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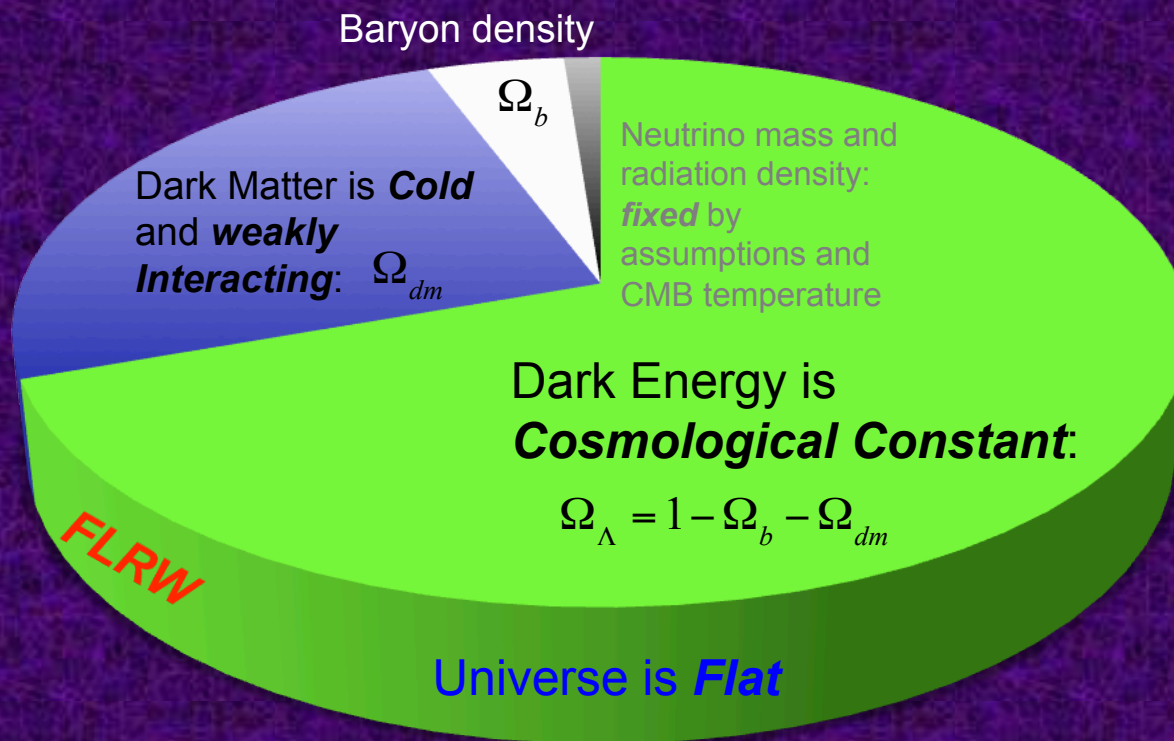
**University of Science and Technology (UST)**

**15<sup>th</sup> Recontres du Vietnam, Qui Nhon, Vietnam**

**11-17 August 2019**

# Standard Model of Cosmology

Using measurements and statistical techniques to place sharp constraints on parameters of the standard cosmological model.



Initial Conditions:  
Form of the Primordial Spectrum is **Power-law**

$$n_s, A_s$$

Epoch of reionization

$$\tau$$

Hubble Parameter and the Rate of Expansion

$$H_0$$

# Standard Model of Cosmology

Using measurements and statistical techniques to place sharp constraints on parameters of the standard cosmological model.

Baryon density

## Combination of Assumptions

Dark Energy is  
**Cosmological Constant:**

$$\Omega_{\Lambda} = 1 - \Omega_b - \Omega_{dm}$$

FLRW

Universe is *Flat*

Epoch of reionization

$\tau$

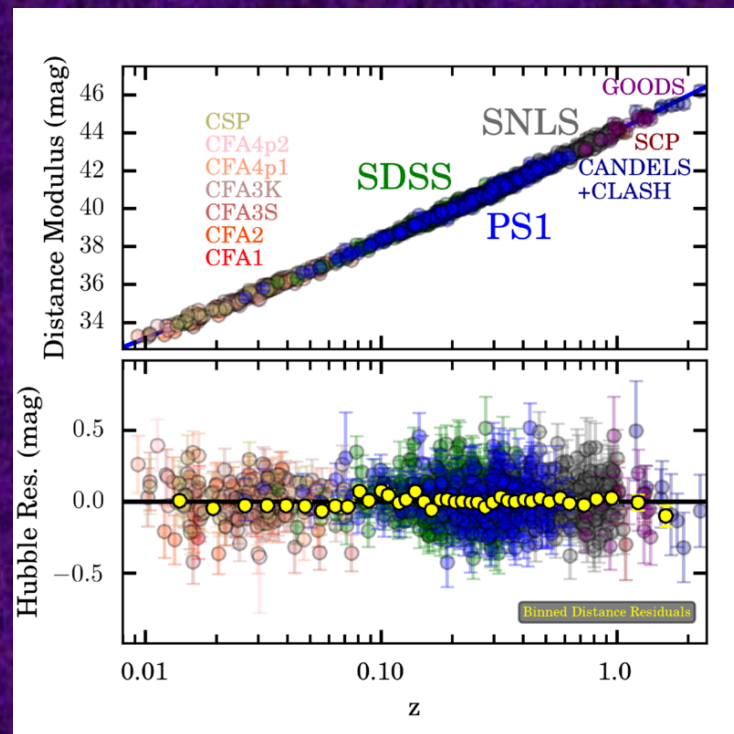
Hubble Parameter and  
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$H_0$

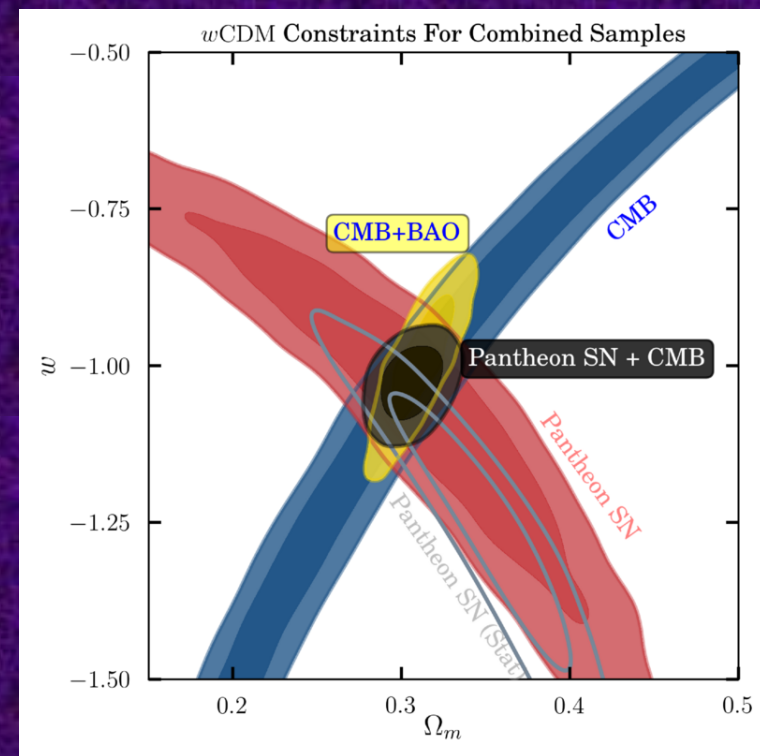
# Standard Model in 2019 SN

**20 years after discovery of the acceleration of the universe:**

From 60 Supernovae Ia at cosmic distances, we now have ~1000 published distances, with better precision, better accuracy, out to  $z \sim 2.0$ . **Accelerating universe in proper concordance to the data.**



1048 spectroscopically confirmed SNIa



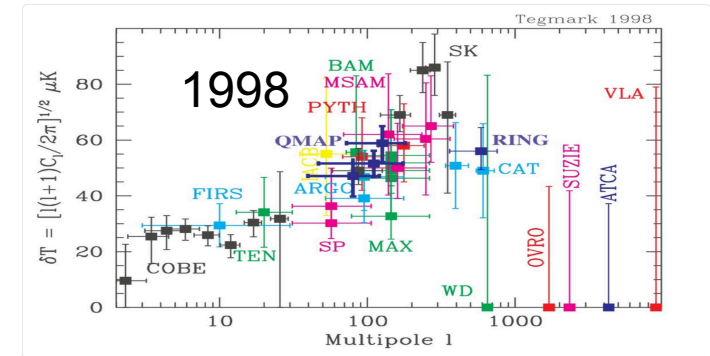
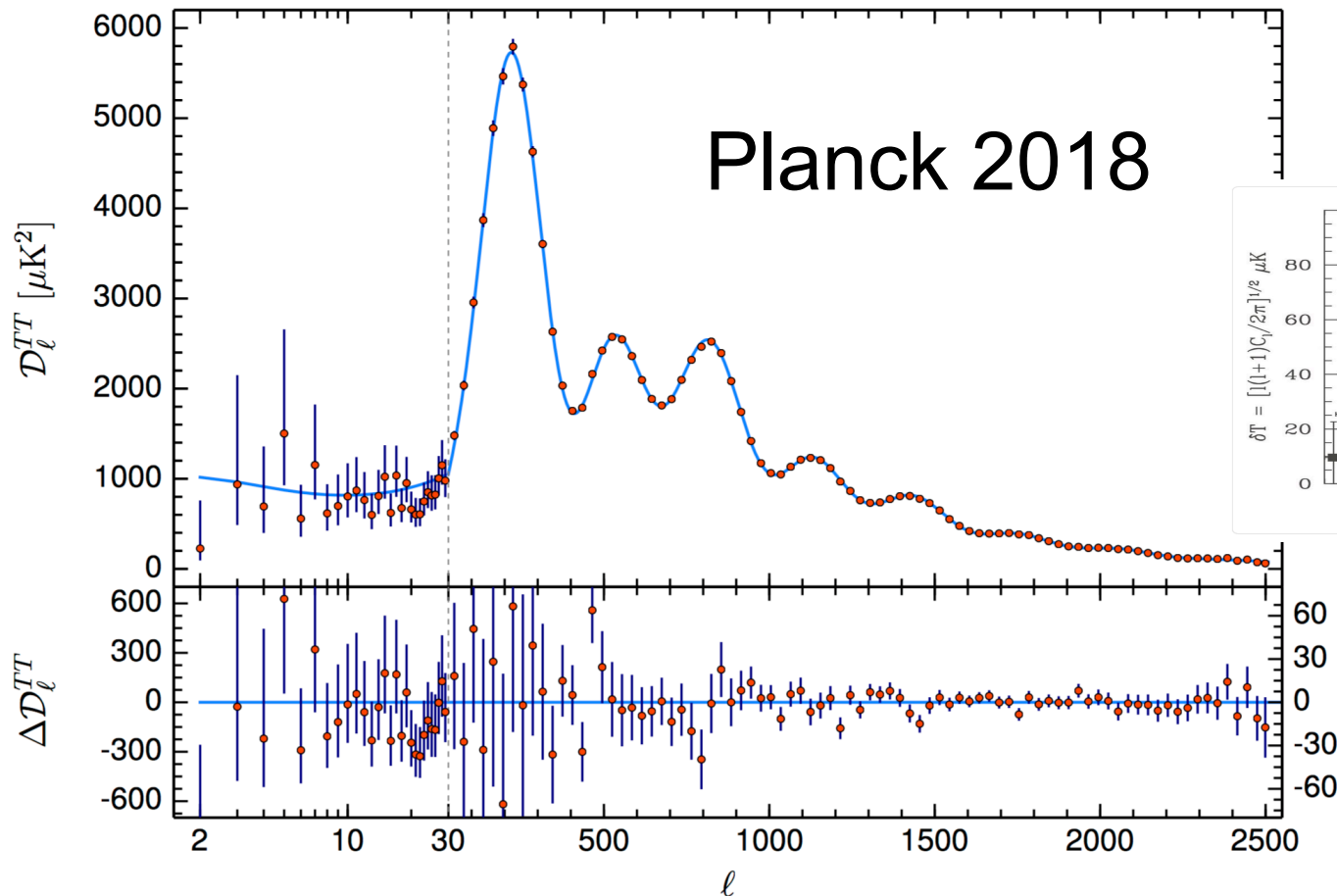
Pantheon Compilation  
Scolnic et al. (2018)

# Standard Model in 2019

# CMB

**Almost 20 years after discovery of the acceleration of the universe:**

**CMB directly points to acceleration.** Didn't even have acoustic peak in 1998!

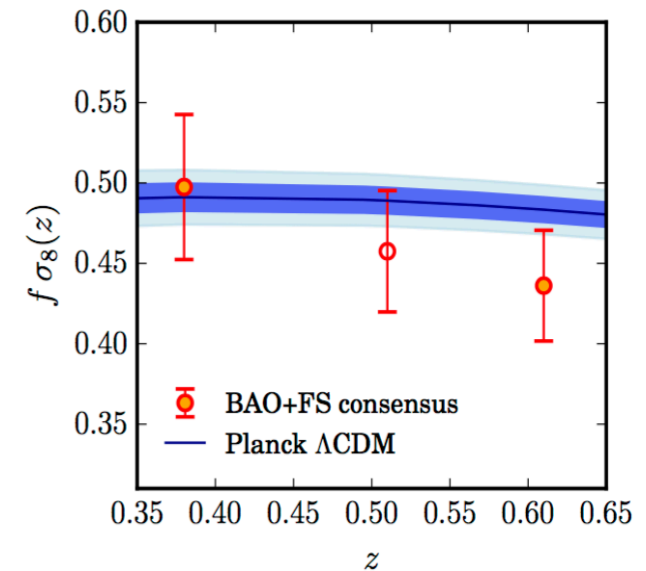
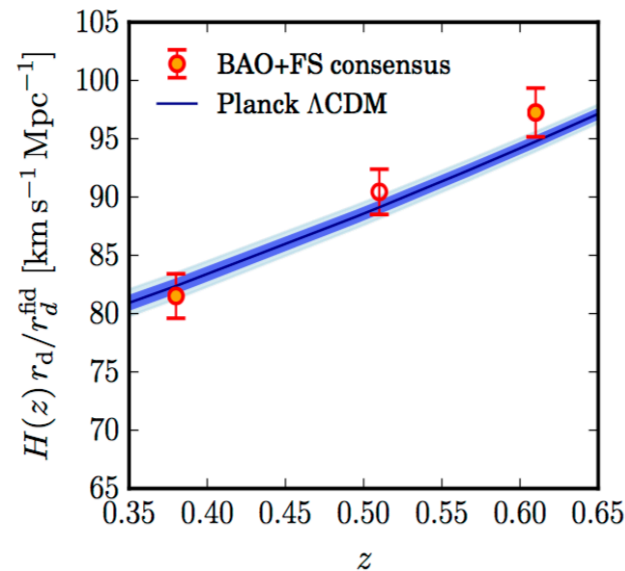
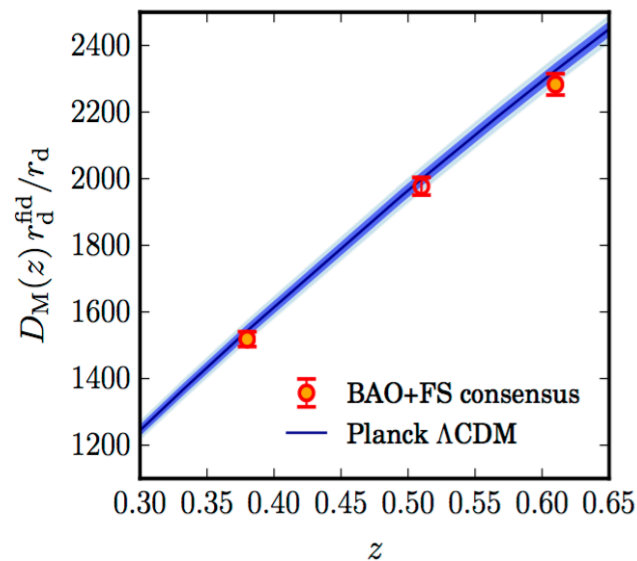
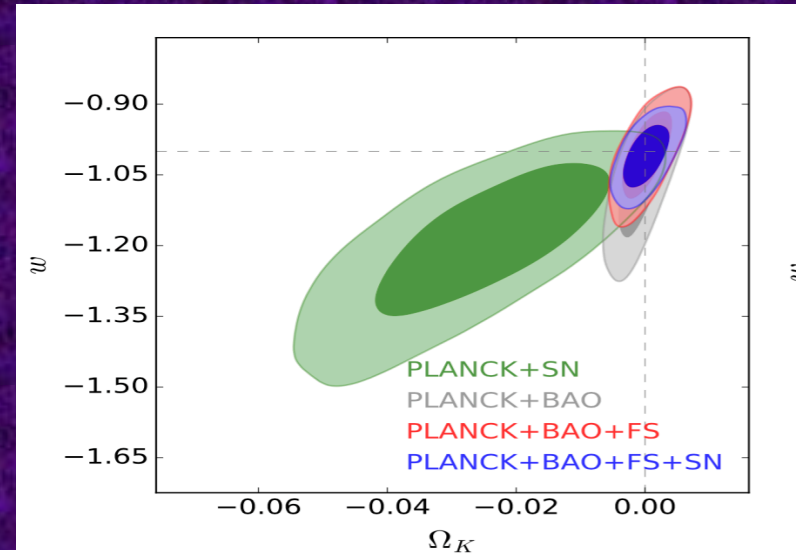


# Dark Energy in 2019

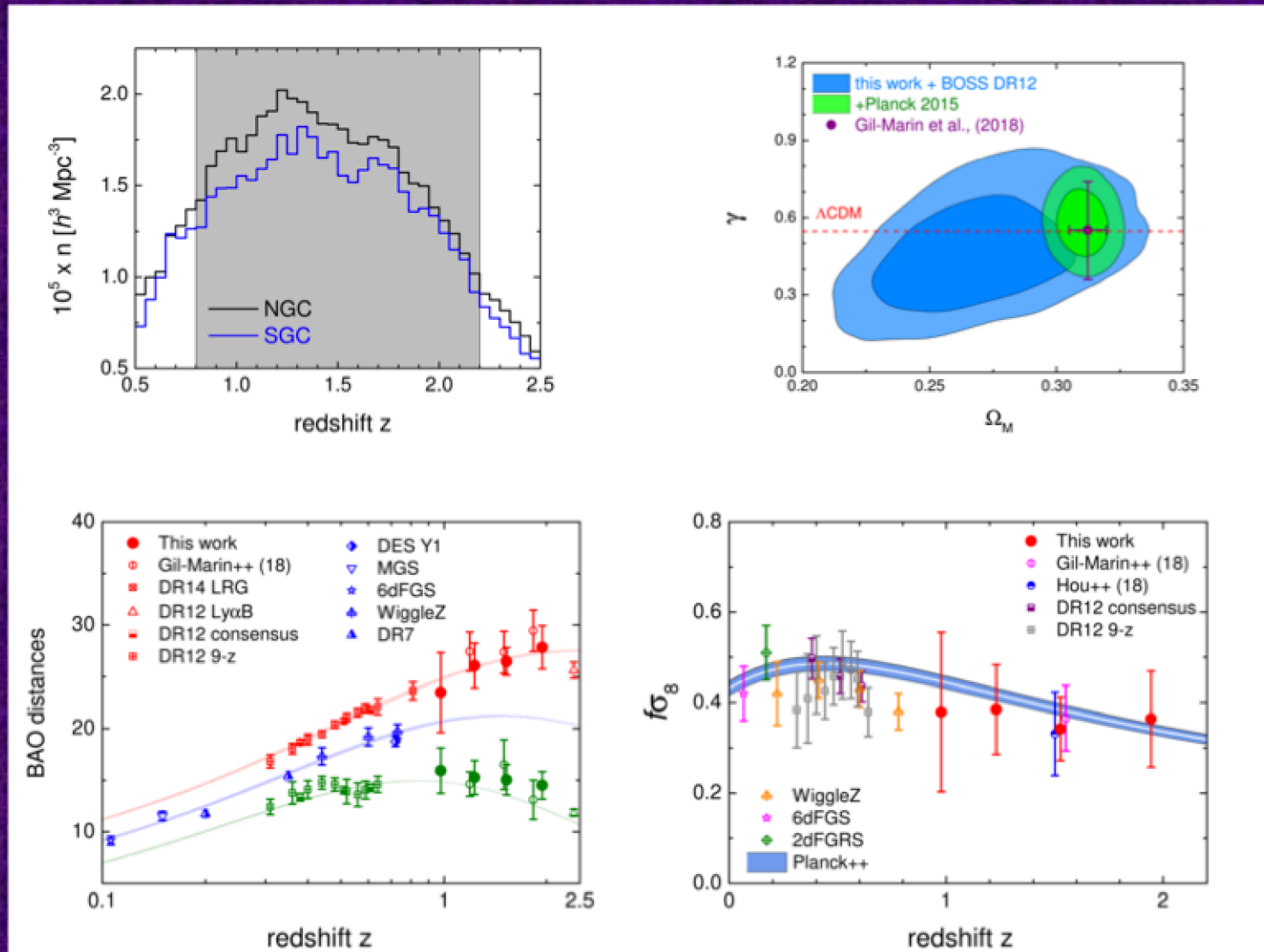
# LSS

Almost 20 years after discovery of the acceleration of the universe:

BOSS collaboration DR12 (2016),  
arXiv:Alam et al, MNRAS 2016

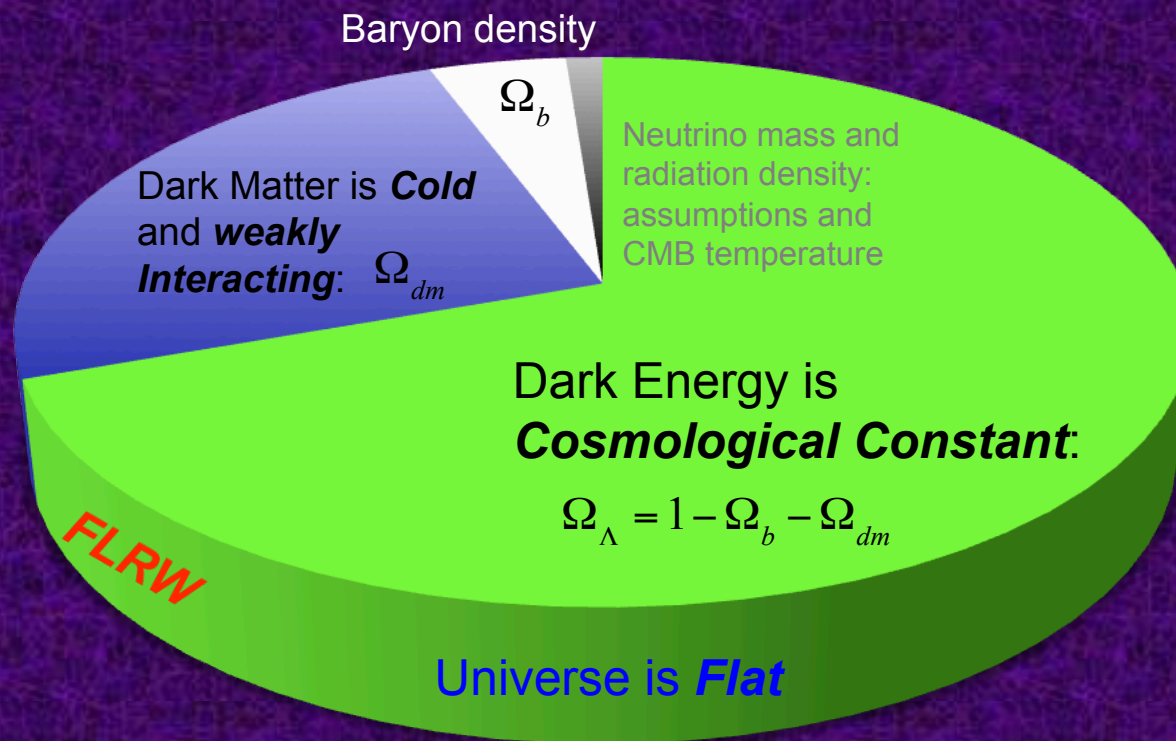


# BOSS DR14Q



# Standard Model of Cosmology

**combination of *reasonable* assumptions, but.....**



Initial Conditions:  
Form of the Primordial Spectrum is **Power-law**

$$n_s, A_s$$

Epoch of reionization

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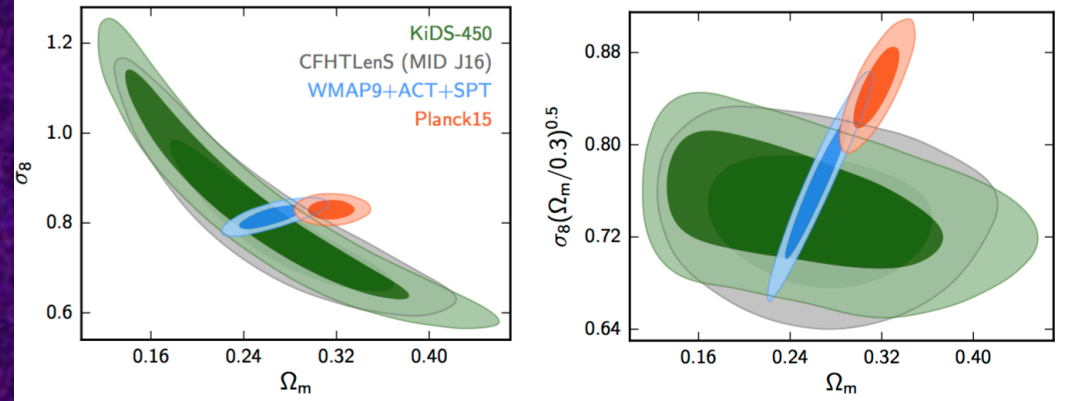
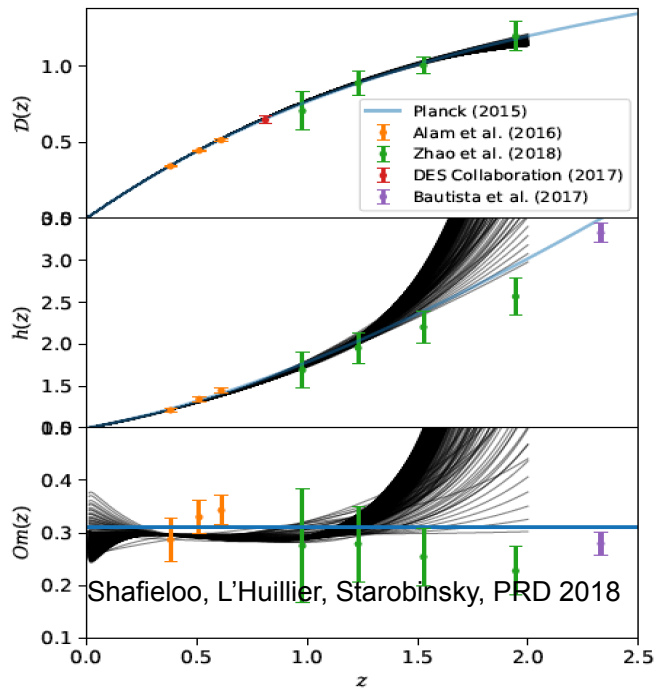


# Persistent Tensions in the Standard Model



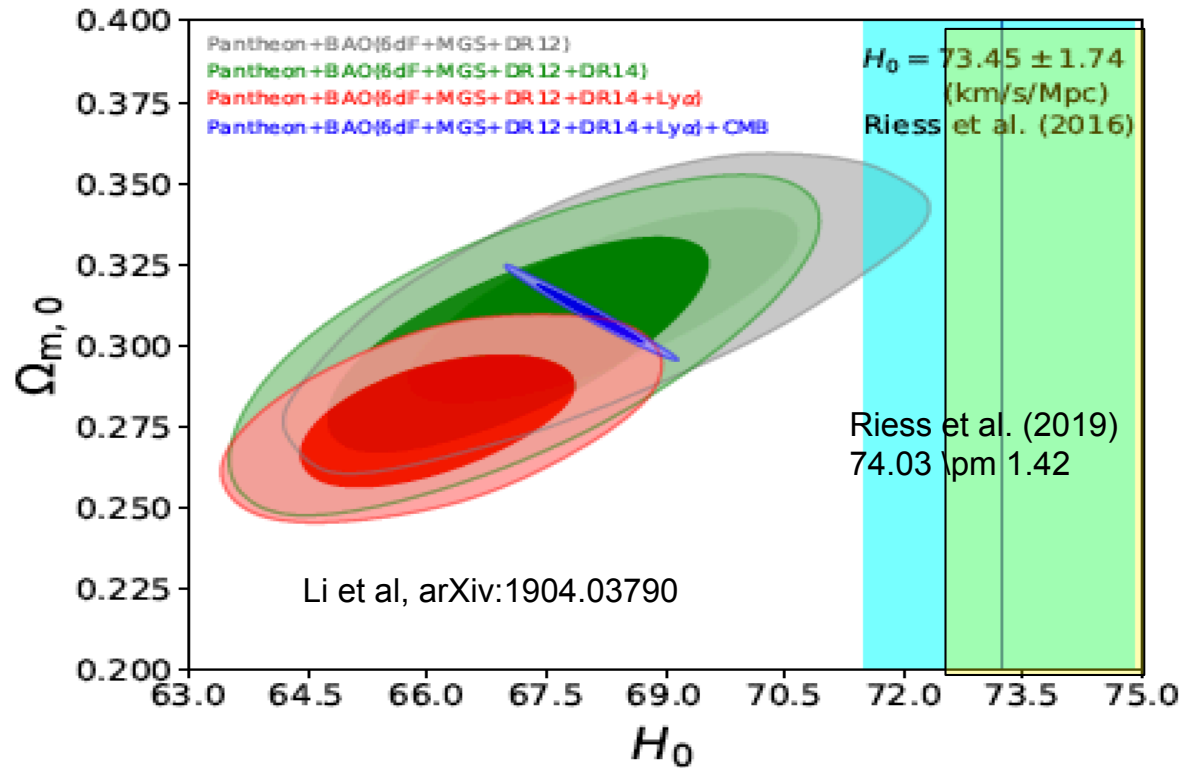
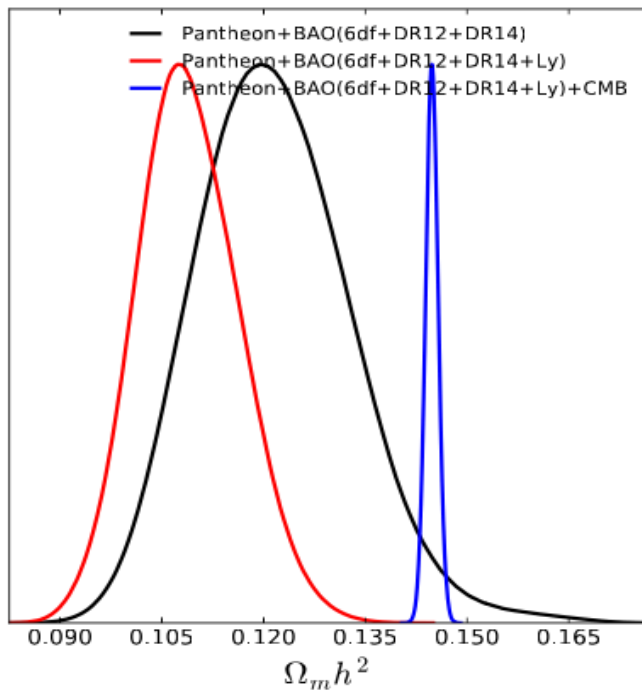
*Local estimation of the Hubble constant seems to be substantially higher than the expected values fitting the standard  $\Lambda$ CDM model to CMB.*

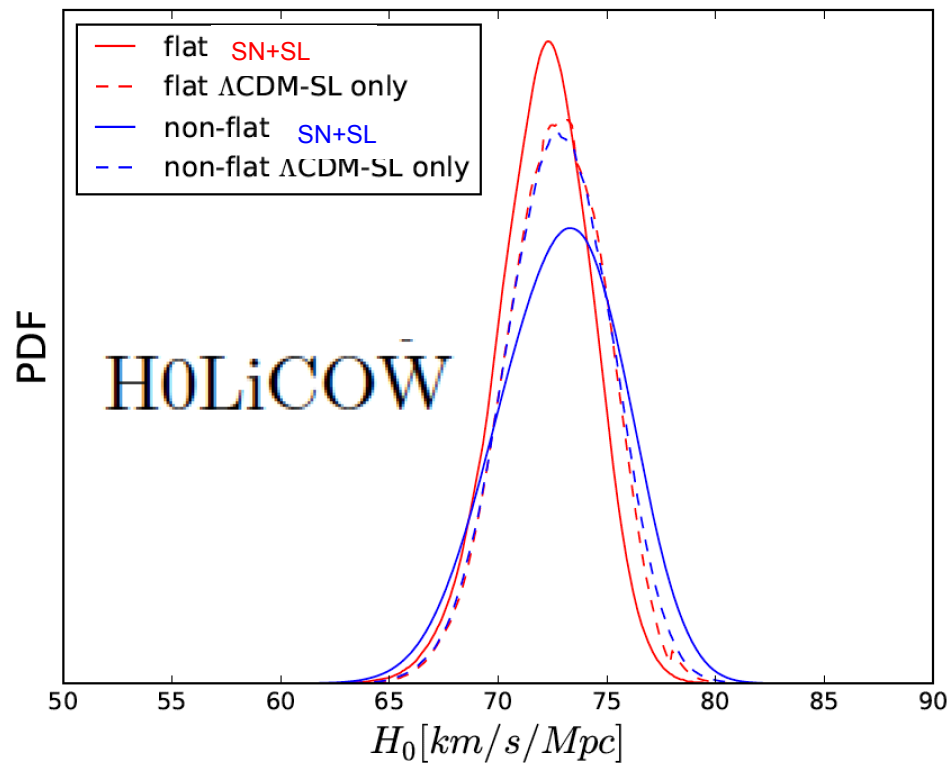
**67 or 73?**



Hildebrandt et al, MNRAS 2017

*It is not only about  $H_0$  and CMB.* Low  $H(z)r_d$  is suggested by BAO and low matter density by WL.





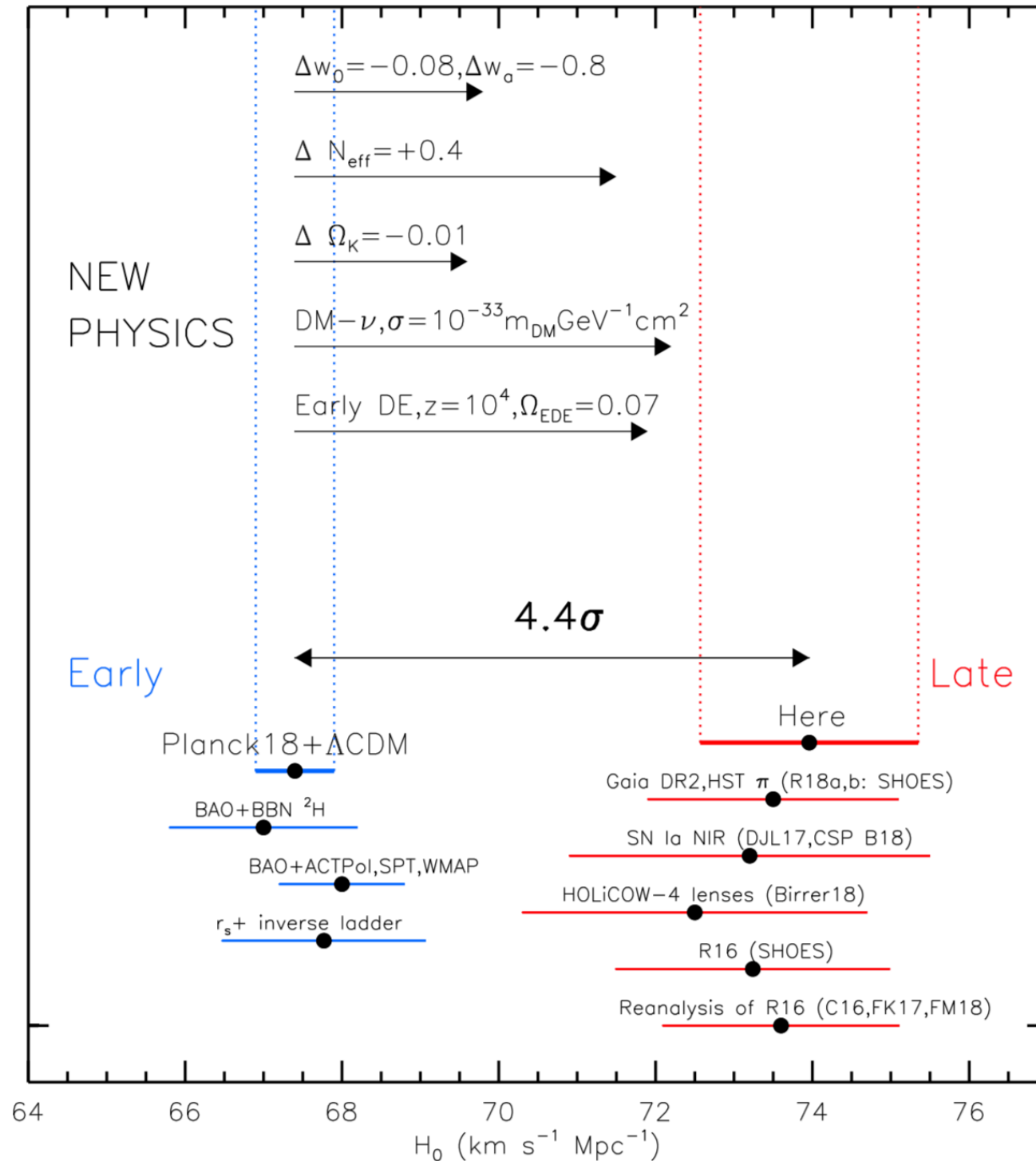
## H0 from Strongly Lensed systems

Kai et. al, in preparation

H0LiCOW I. H0 Lenses in  
COSMOGRAIL's Wellspring

Suyu et al. MNRAS 2017

Order	Name	$z_L$	$z_S$
1	RXJ1131-1231	0.295	0.654
2	HE 0435-1223	0.4546	1.693
3	B1608+656	0.6304	1.394
4	SDSS 1206+4332	0.745	1.789



## Tensions in the Standard Model

Riess et al,  
 arXiv:1903.07603

# How to go **Beyond** the Standard Model of Cosmology?



- Finding features/deviations in the data beyond the flexibility of the standard model using model-independent reconstructions.
- Falsifying the standard model using litmus tests.
- Introducing theoretical/phenomenological models that can explain the data better (statistically significant) than the standard model.
- Finding tension among different independent data assuming the standard model (making sure there is no systematic).

Implementing well cooked statistical approaches to get the most out of the data is essential!

# Om<sub>h</sub><sup>2</sup>

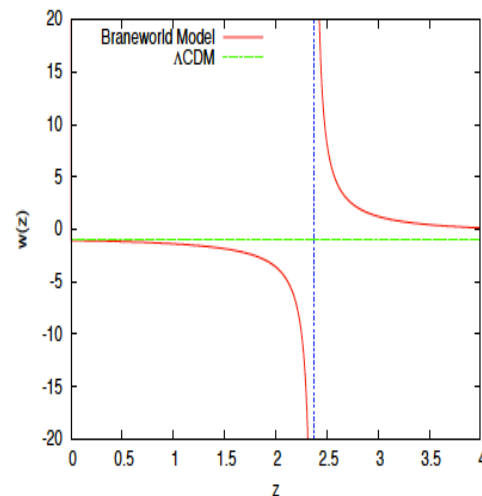
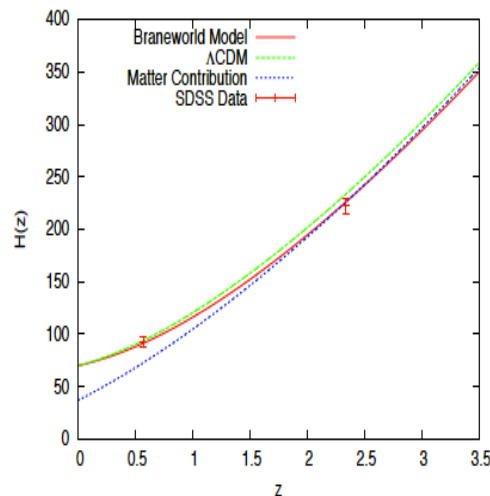
Important discovery if no systematic in the SDSS Quasar BAO data

## Model Independent Evidence for Dark Energy Evolution from Baryon Acoustic Oscillation

$$Om_h^2(z_1, z_2) = \frac{H^2(z_2) - H^2(z_1)}{(1+z_2)^3 - (1+z_1)^3} = \Omega_{0m} H_0^2$$

Sahni, Shafieloo, Starobinsky, ApJ Lett 2014

Only for LCDM



$$Om_h^2 = 0.1426 \pm 0.0025$$

LCDM  
+Planck+WP

$$Om_h^2(z_1; z_2) = 0.124 \pm 0.045$$

$$Om_h^2(z_1; z_3) = 0.122 \pm 0.010$$

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BAO+H0

$$H(z = 0.00) = 70.6 \pm 3.3 \text{ km/sec/Mpc}$$

$$H(z = 0.57) = 92.4 \pm 4.5 \text{ km/sec/Mpc}$$

$$H(z = 2.34) = 222.0 \pm 7.0 \text{ km/sec/Mpc}$$

# 2019

# Om $h^2$

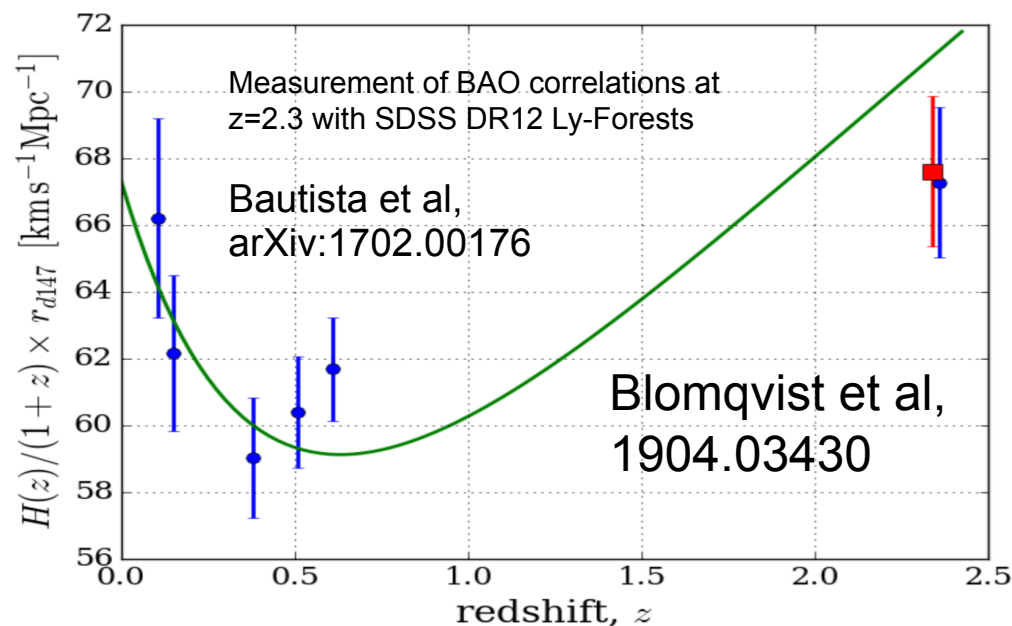
No systematic yet found,

## Model Independent Evidence for Dark Energy Evolution from Baryon Acoustic Oscillation

$$Om h^2(z_1, z_2) = \frac{H^2(z_2) - H^2(z_1)}{(1+z_2)^3 - (1+z_1)^3} = \Omega_{0m} H_0^2$$

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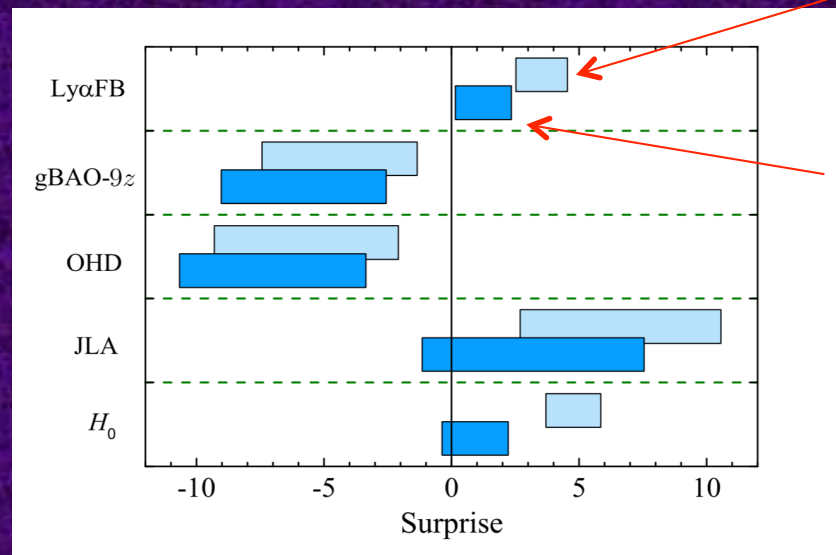
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# Comparing different data assuming a particular model

Zhao et al, Nature Astronomy, 2017

$$T \equiv \frac{S}{\Sigma} = \frac{(\theta_1 - \theta_2)^T \mathcal{C}_1^{-1} (\theta_1 - \theta_2) - \text{Tr}(\mathcal{C}_2 \mathcal{C}_1^{-1} + \mathbb{I})}{\sqrt{\text{Tr}(\mathcal{C}_2 \mathcal{C}_1^{-1} + \mathbb{I})^2}},$$



LCDM

w(z)CDM

Acronym	Meaning	References
P15	The <i>Planck</i> 2015 CMB power spectra	[6]
JLA	The JLA supernovae	[28]
6dF	The 6dFRS (6dF) BAO	[29]
MGS	The SDSS main galaxy sample BAO	[30]
$P(k)$	The WiggleZ galaxy power spectra	[31]
WL	The CFHTLenS weak lensing	[32]
$H_0$	The Hubble constant measurement	[10]
OHD	$H(z)$ from galaxy age measurements	[33]
gBAO-3z	3-bin BAO from BOSS DR12 galaxies	[34]
gBAO-9z	9-bin BAO from BOSS DR12 galaxies	[35, 36]
LyαFB	The Lyα forest BAO measurements	[2, 9]
B	P15 + JLA + 6dF + MGS	
ALL12	The combined dataset used in [27]	
ALL16-3z	B + $P(k)$ + WL + $H_0$ + OHD + gBAO-3z + LyαFB	
ALL16	B + $P(k)$ + WL + $H_0$ + OHD + gBAO-9z + LyαFB	
DESI++	P15 + mock DESI BAO [49] + mock SN [50]	

Kullback-Leibler (KL) divergence to quantify the degree of tension between different datasets assuming a model.

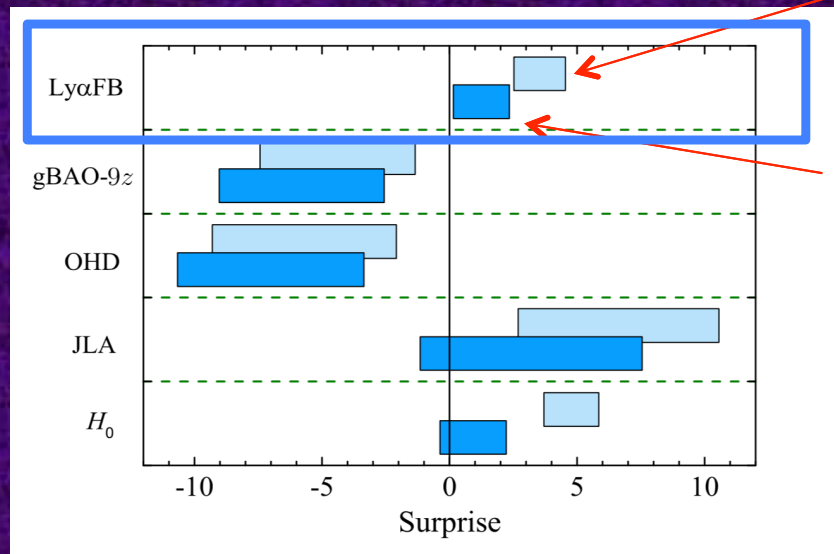
For LCDM;  $H_0$ , LyFB and JLA measurements are in tension with the combined dataset, with tension values of  $T = 4.4, 3.5, 1.7$ .



# Comparing different data assuming a particular model

Zhao et al, Nature Astronomy, 2017

$$T \equiv \frac{S}{\Sigma} = \frac{(\theta_1 - \theta_2)^T C_1^{-1} (\theta_1 - \theta_2) - \text{Tr}(C_2 C_1^{-1} + \mathbb{I})}{\sqrt{\text{Tr}(C_2 C_1^{-1} + \mathbb{I})^2}},$$



Bautista et al, [1702.00176]

Blomqvist et al, [1904.03430]

Found no systematic/mistake in the previous measurement

Label	Description	References
gBAO-3z	3-bin BAO from BOSS DR12 galaxies	[34]
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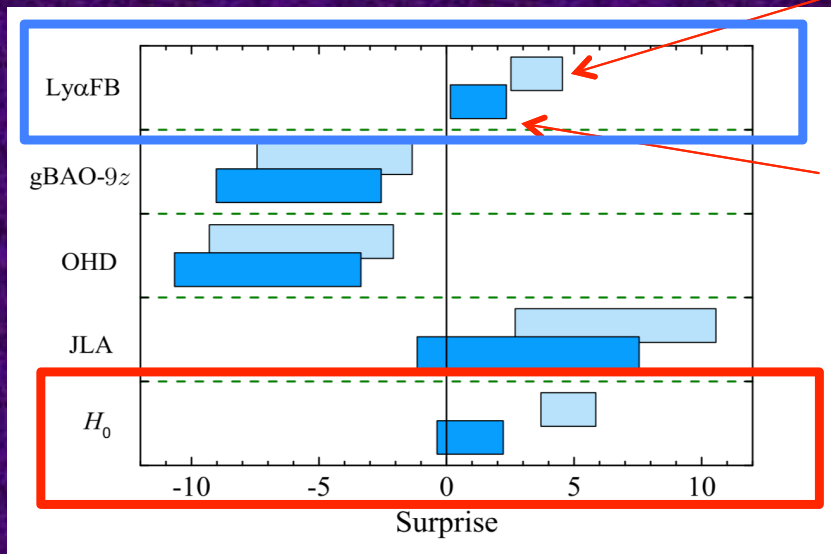
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Zhao et al, Nature Astronomy, 2017

$$T \equiv \frac{S}{\Sigma} = \frac{(\theta_1 - \theta_2)^T C_1^{-1} (\theta_1 - \theta_2) - \text{Tr}(C_2 C_1^{-1} + \mathbb{I})}{\sqrt{\text{Tr}(C_2 C_1^{-1} + \mathbb{I})^2}}$$



Kullback-Leibler (KL) divergence to quantify the degree of tension between different datasets assuming a model.

Bautista et al, [1702.00176]  
Blomqvist et al, [1904.03430]

Found no systematic/mistake in the previous measurement

Follin & Knox [1707.01175]  
Zhang et al, [1706.07573]

Both agrees with Riess et al 2016 H<sub>0</sub> measurement

New H<sub>0</sub> measurement Riess et al 2019  
**(situation has become worse)**

# How to resolve the tensions?



- Tensions may disappear by themselves if they are due to statistical fluctuations (*probably not anymore*)
- **Extended Models and/or New Physics:** such as proposing models with more degrees of freedom (having more parameters) and get larger confidence contours which looks like there are better consistencies (more overlap between larger contours). [OK to do that but better to avoid over-selling!]
- **Finding systematics in different data** [Sinful Adam? Not to be confused with primordial sin]

*Touching any aspect of the concordance model, means going beyond the standard cosmology (**which is great!**) and its time to consider different possibilities:*

- Current tensions seems to be persistent at the background level. So just touching GR (modified gravity models) cannot help.
- **Evolving dark energy?** Possible but not yet so easy to satisfy all observations.
- **Neutrinos?** As always they are a possibility (they may not be able to help much though)
- **Early Universe and seeds of fluctuations.**

(Present)<sub>t</sub>

## *Standard Model of Cosmology*

Universe is Flat

Universe is Isotropic

Universe is Homogeneous

Dark Energy is Lambda ( $w=-1$ )

Power-Law primordial spectrum ( $n_s=\text{const}$ )

Dark Matter is cold

All within framework of FLRW

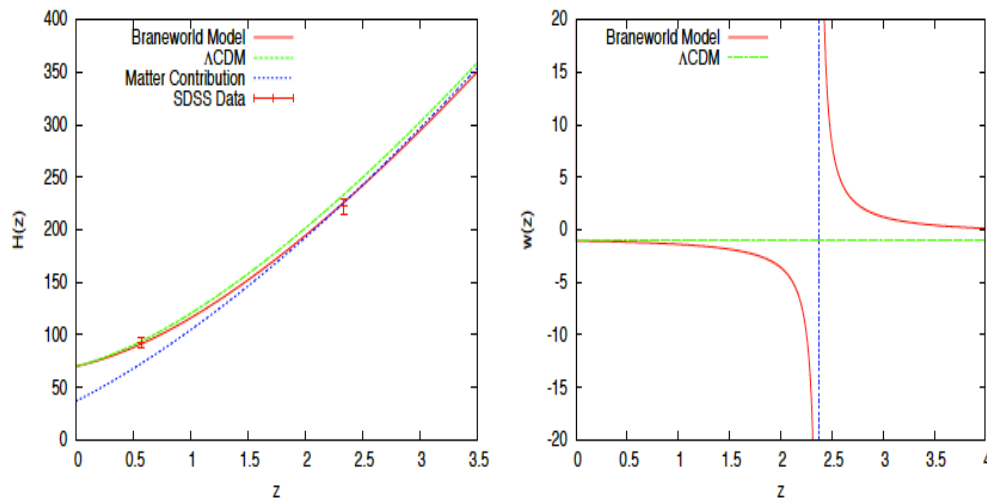
# Dark Energy Models

- **Cosmological Constant**
- Quintessence and k-essence (scalar fields)
- Exotic matter (Chaplygin gas, phantom, etc.)
- Braneworlds (higher-dimensional theories)
- Modified Gravity
- .....

**But which one is really responsible for the acceleration of the expanding universe?!**

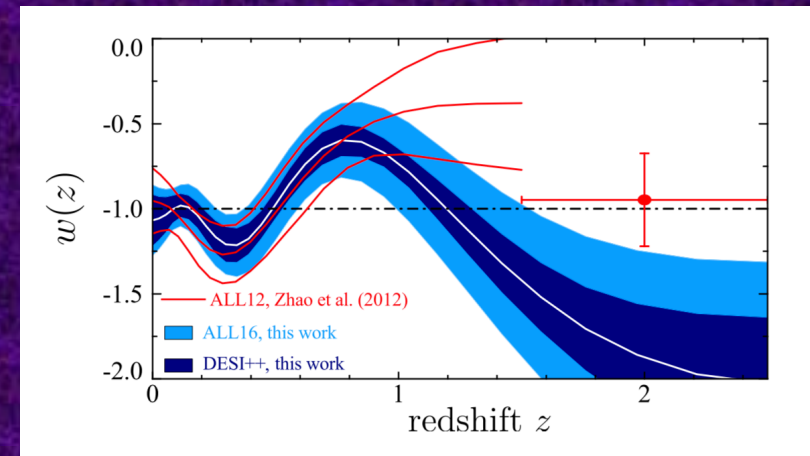
# Evolving Dark Energy?

*Not yet statistically significant*



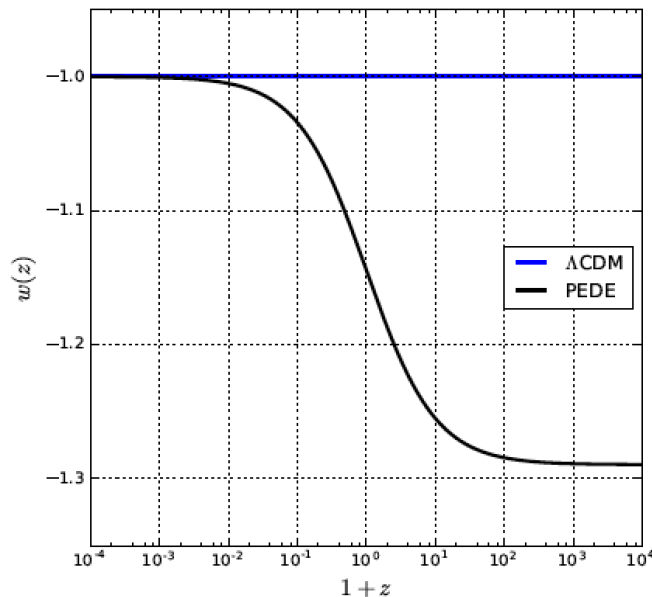
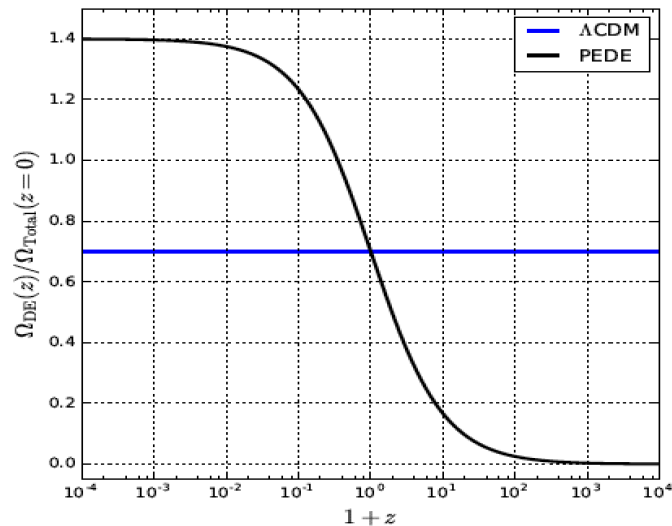
Sahni et al ApJ 2014

Zhao et al, Nature Astronomy, 2017



	P15	JLA	gBAO-9z	$P(k)$	WL	$H_0$	$\text{Ly}\alpha\text{FB}$	OHD
$\Delta\chi^2$	-0.7	-1.6	-2.8	+1.1	-0.1	-2.9	-3.7	-2.3
	ALL12			ALL16		DESI++		
S/N	2.5 $\sigma$			3.5 $\sigma$		6.4 $\sigma$		
$\Delta\text{AIC}$	-0.3			-4.3		-24.6		
$\Delta\ln E$	$-6.7 \pm 0.3$			$-3.3 \pm 0.3$		$11.3 \pm 0.3$		

# Phenomenologically Emergent Dark Energy (PEDE)

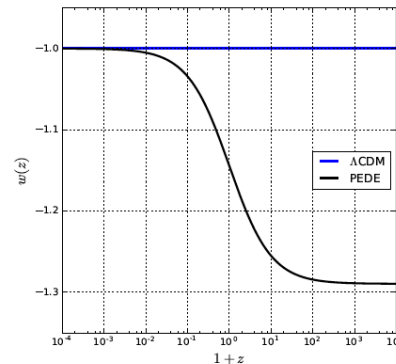
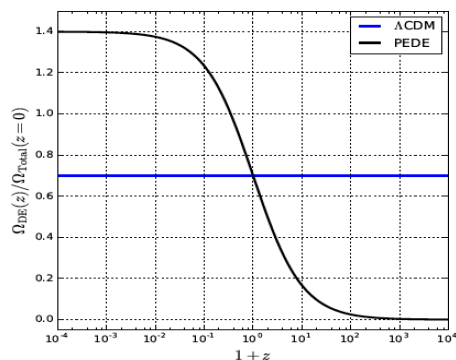


$$\Omega_{DE}(z) = \Omega_{DE,0} \times [1 - \tanh(\log_{10}(1+z))]$$

$$\begin{aligned} w(z) &= -\frac{1}{3\ln 10} \times \frac{1 - \tanh^2[\log_{10}(1+z)]}{1 - \tanh[\log_{10}(1+z)]} - 1 \\ &= -\frac{1}{3\ln 10} \times (1 + \tanh[\log_{10}(1+z)]) - 1. \end{aligned}$$

# Phenomenologically Emergent Dark Energy

Model	Data Parameters	Pantheon+BAO			Pantheon+BAO+Ly $\alpha$ +CMB		
		No $H_0$ Prior	$2\sigma$ $H_0$ Prior	$1\sigma$ $H_0$ Prior	No $H_0$ Prior	$2\sigma$ $H_0$ Prior	$1\sigma$ $H_0$ Prior
$\Lambda$ CDM	$\Omega_m$	$0.299^{+0.047}_{-0.043}$	$0.335^{+0.040}_{-0.036}$	$0.347^{+0.041}_{-0.036}$	$0.311^{+0.016}_{-0.014}$	$0.271^{+0.002}_{-0.003}$	$0.256^{+0.002}_{-0.002}$
	$H_0$	$66.94^{+3.721}_{-3.256}$	$71.19^{+1.890}_{0.0}$	$72.61^{+1.617}_{-0.000}$	$67.91^{+1.074}_{-1.150}$	$71.19^{+0.271}_{-0.000}$	$72.61^{+0.200}_{-0.000}$
	$\chi^2_{bf}$	1046.94	1054.76	1060.25	1056.12	1112.28	1168.98
	DIC	1051.00	1058.88	1064.27	1062.35	1127.03	1195.07
CPL	$\Omega_m$	$0.285^{+0.113}_{-0.180}$	$0.332^{+0.071}_{-0.050}$	$0.350^{+0.050}_{-0.043}$	$0.307^{+0.026}_{-0.021}$	$0.286^{+0.007}_{-0.011}$	$0.274^{+0.006}_{-0.009}$
	$H_0$	$64.84^{+14.49}_{-16.12}$	$71.30^{+5.561}_{-0.117}$	$72.70^{+2.746}_{-0.091}$	$68.49^{+2.302}_{-2.680}$	$71.19^{+1.277}_{-0.002}$	$72.61^{+0.918}_{-0.004}$
	$w_0$	$-0.82^{+0.193}_{-0.541}$	$-1.08^{+0.422}_{-0.347}$	$-1.05^{+0.350}_{-0.347}$	$-0.98^{+0.267}_{-0.218}$	$-1.07^{+0.259}_{-0.240}$	$-1.13^{+0.274}_{-0.206}$
	$w_a$	$0.675^{+0.547}_{-3.103}$	$-0.11^{+1.510}_{-3.192}$	$-0.46^{+1.830}_{-2.686}$	$-0.16^{+0.816}_{-1.189}$	$-0.20^{+0.986}_{-1.249}$	$-0.11^{+0.728}_{-1.391}$
	$\chi^2_{bf}$	1044.98	1048.84	1049.66	1055.52	1066.85	1080.83
	DIC	1052.59	1054.46	1056.23	1065.48	1085.06	1128.50
PEDE	$\Omega_m$	$0.341^{+0.045}_{-0.041}$	$0.341^{+0.041}_{-0.037}$	$0.341^{+0.041}_{-0.030}$	$0.291^{+0.015}_{-0.016}$	$0.289^{+0.002}_{-0.014}$	$0.274^{+0.002}_{-0.006}$
	$H_0$	$72.84^{+3.814}_{-3.530}$	$73.01^{+3.371}_{-1.8231}$	$72.79^{+2.652}_{-0.186}$	$71.02^{+1.452}_{-1.368}$	$71.19^{+1.306}_{-0.001}$	$72.61^{+0.651}_{-0.000}$
	$\chi^2_{bf}$	1050.04	1050.04	1050.04	1071.12	1071.20	1080.40
	DIC	1052.01	1053.33	1052.98	1091.15	1091.65	1100.94



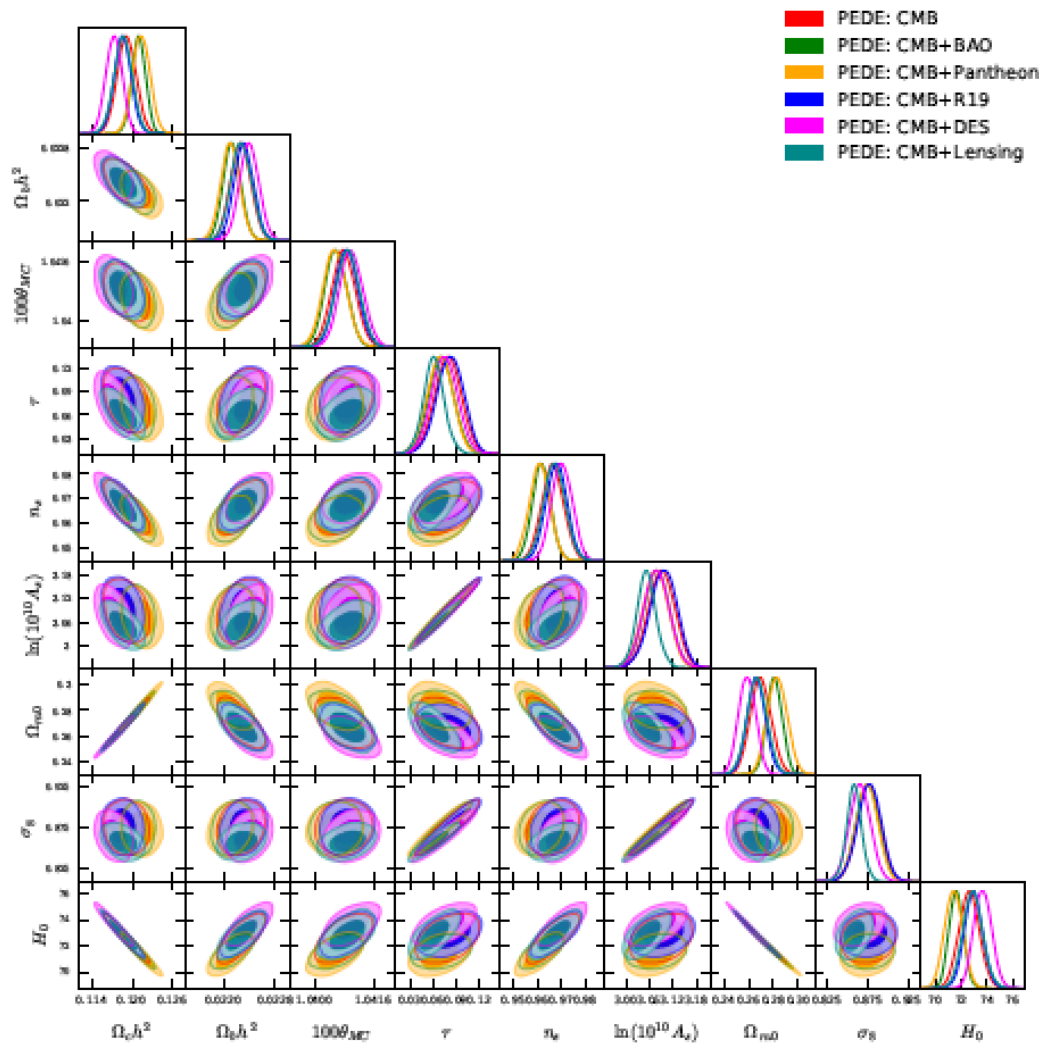
$$p_D = \overline{\chi^2(\theta)} - \chi^2(\bar{\theta}).$$

$$\text{DIC} \equiv D(\bar{\theta}) + 2p_D = \overline{D(\theta)} + p_D,$$

Li and Shafieloo, arXiv:1906.08275



# Phenomenologically Emergent Dark Energy (PEDE)



*Reconciling  $H_0$  tension in a 6 parameter space?*

Dataset	$\ln B_{ij}$	Strength of evidence
CMB	-0.2	Weak
CMB+BAO	-3.1	Strong
CMB+Pantheon	-5.8	Strong
CMB+R19	2.7	Definite/Positive
CMB+DES	-1.6	Definite/Positive
CMB+Lensing	-0.6	Weak

Pan, Yang, Di Valentino, Shafieloo and Chakraborty, arXiv: 1907.12551

(Present)<sub>t</sub>

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# Model Independent Estimation of Primordial Spectrum

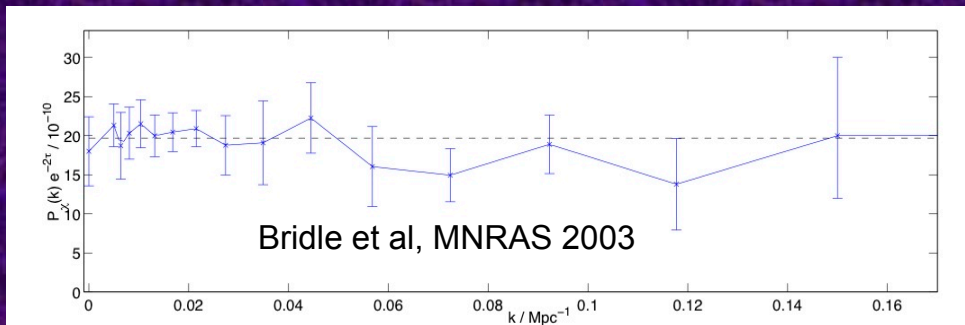
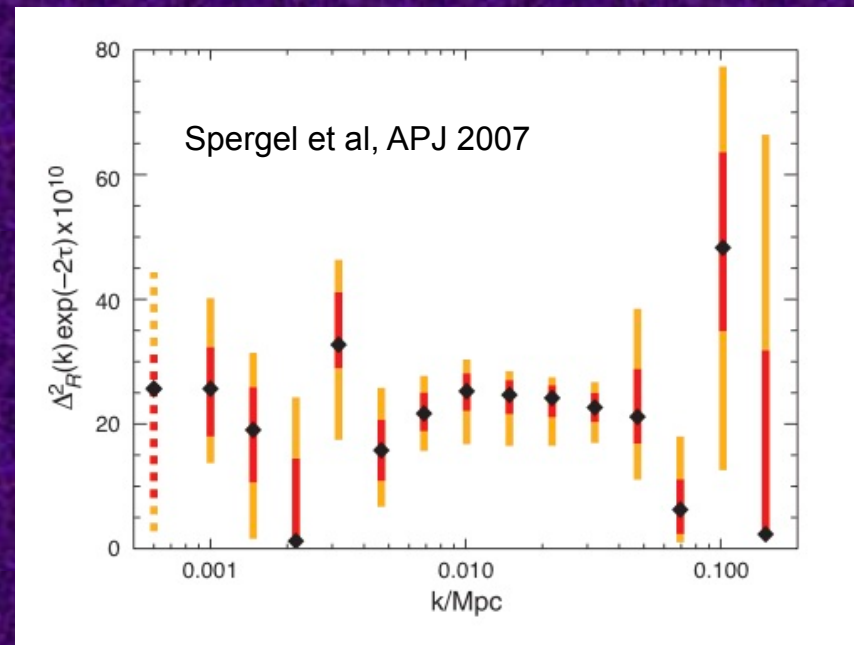
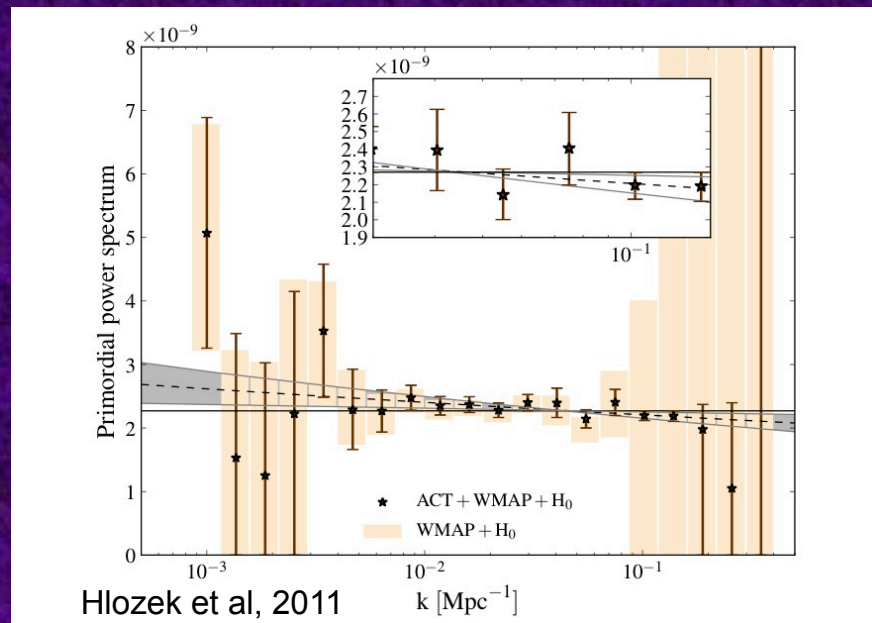
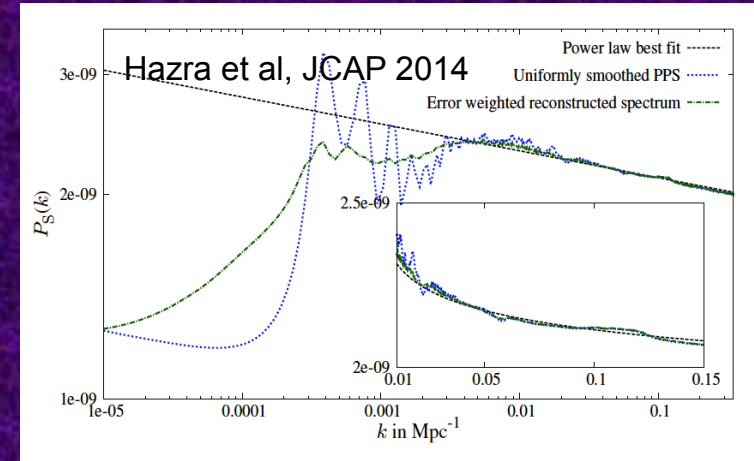
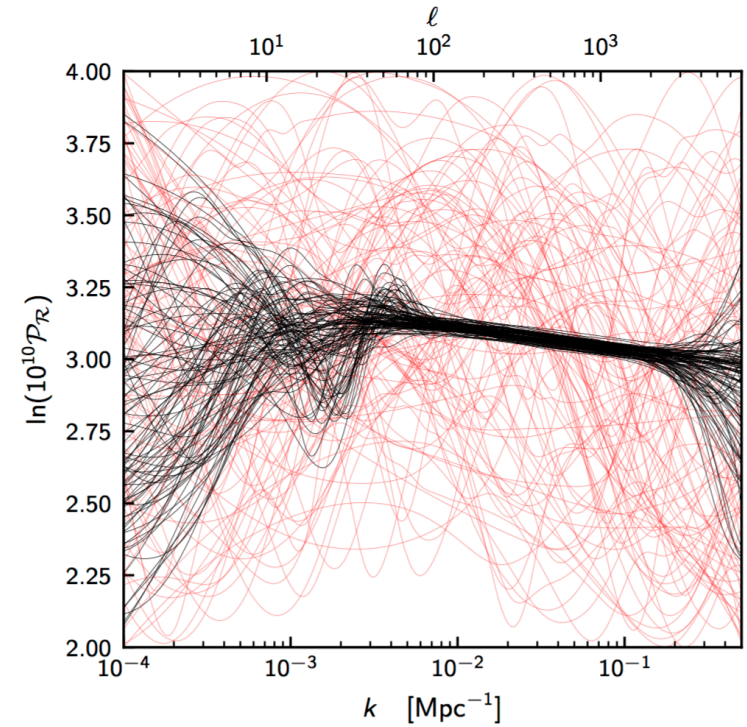
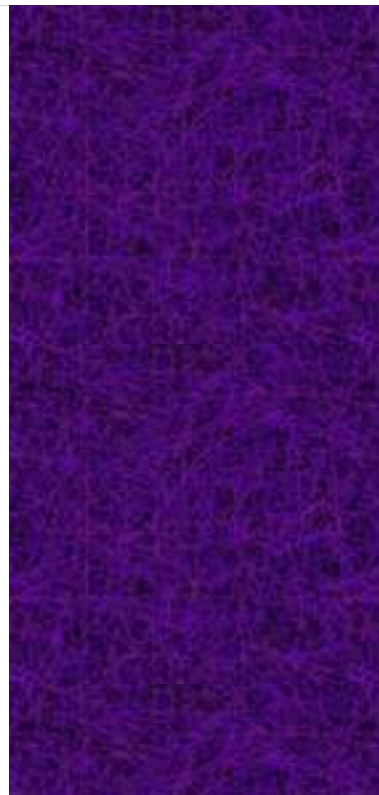
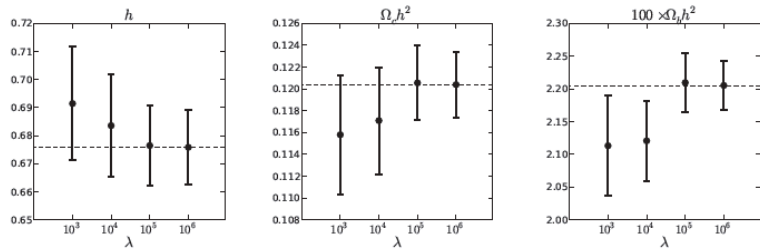
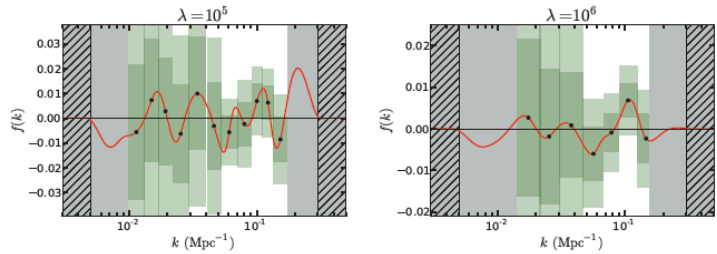
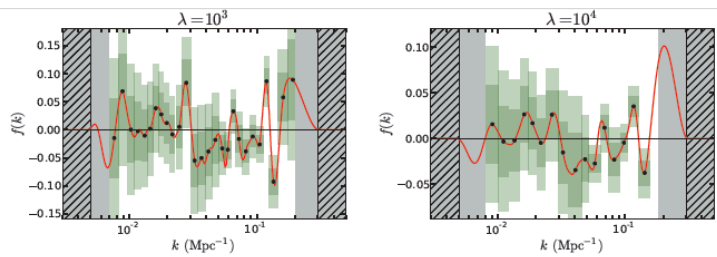


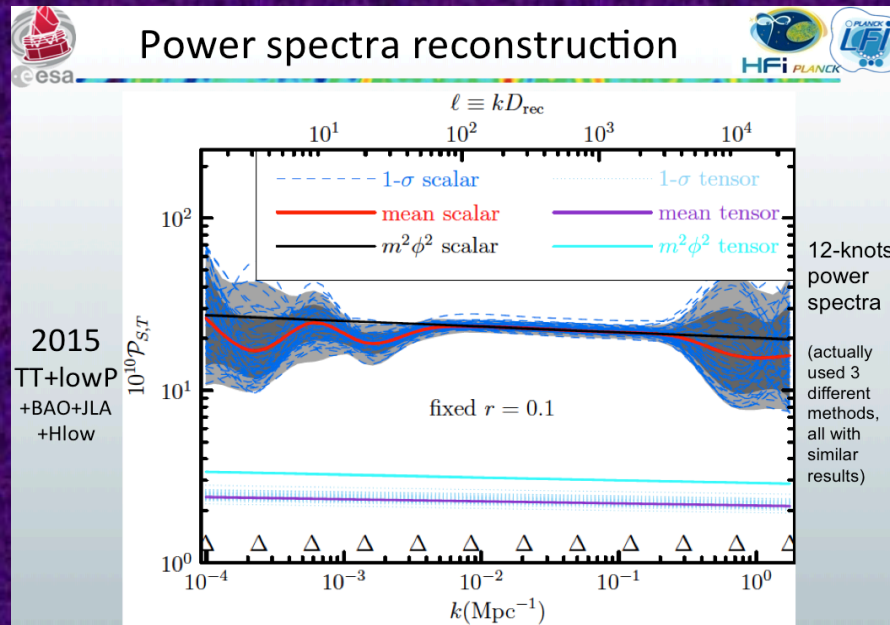
Figure 4. Reconstruction of the shape of the primordial power spectrum in 16 bands after marginalising over the Hubble constant, baryon and dark matter densities, and the redshift of reionization.





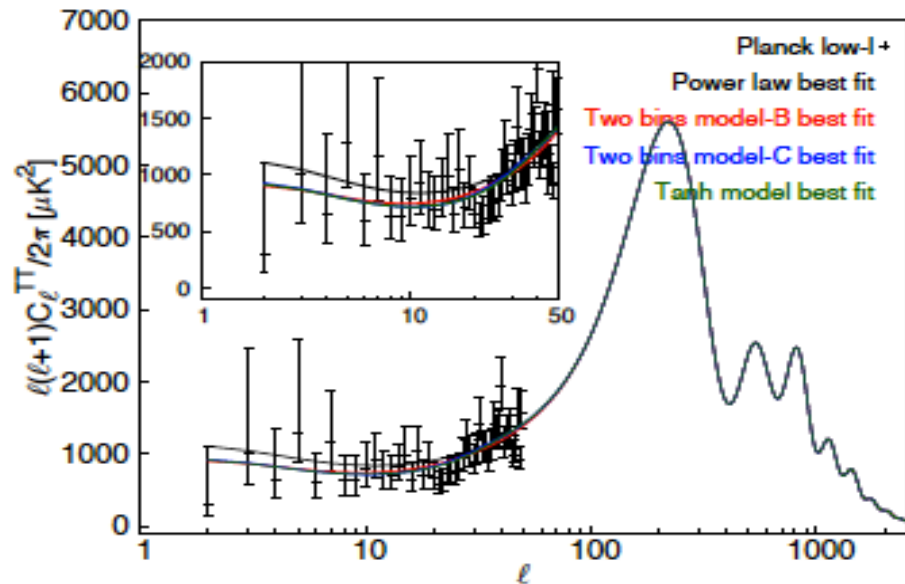
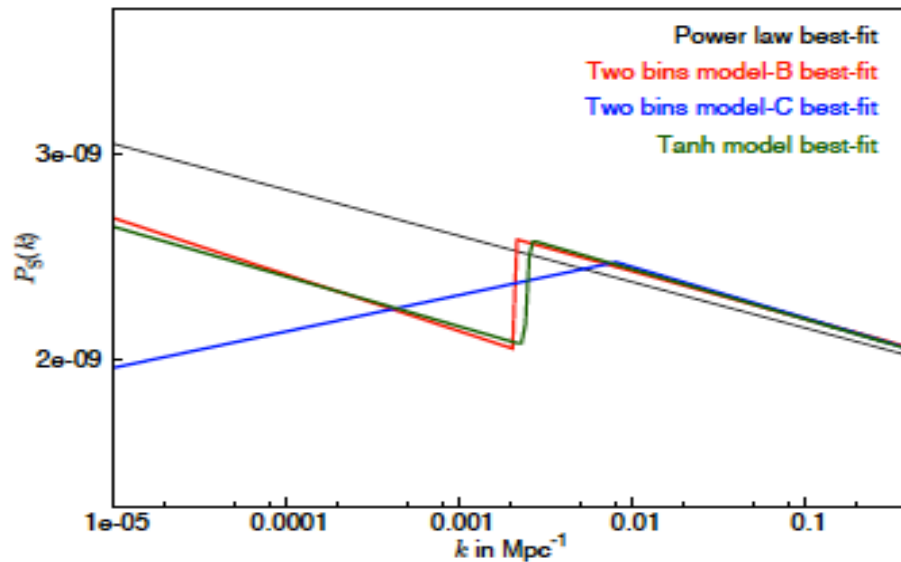
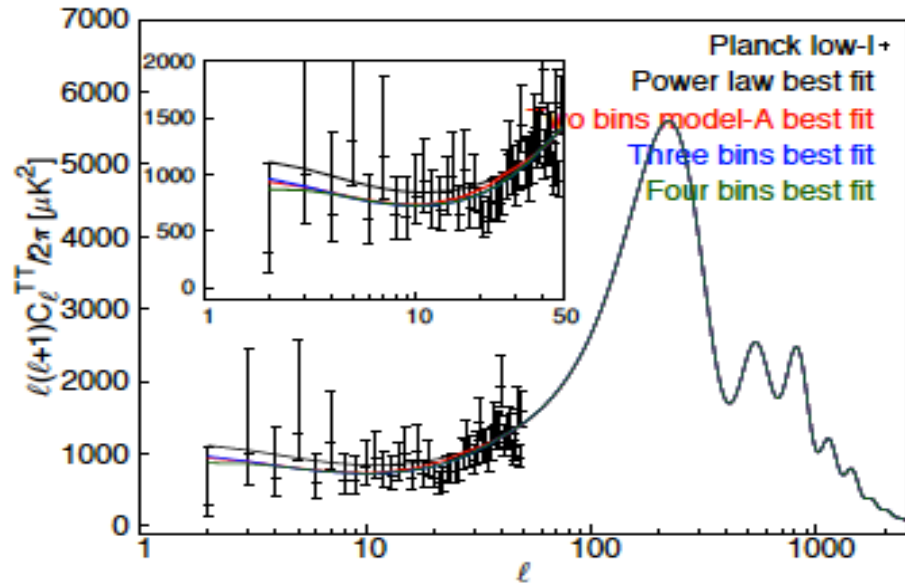
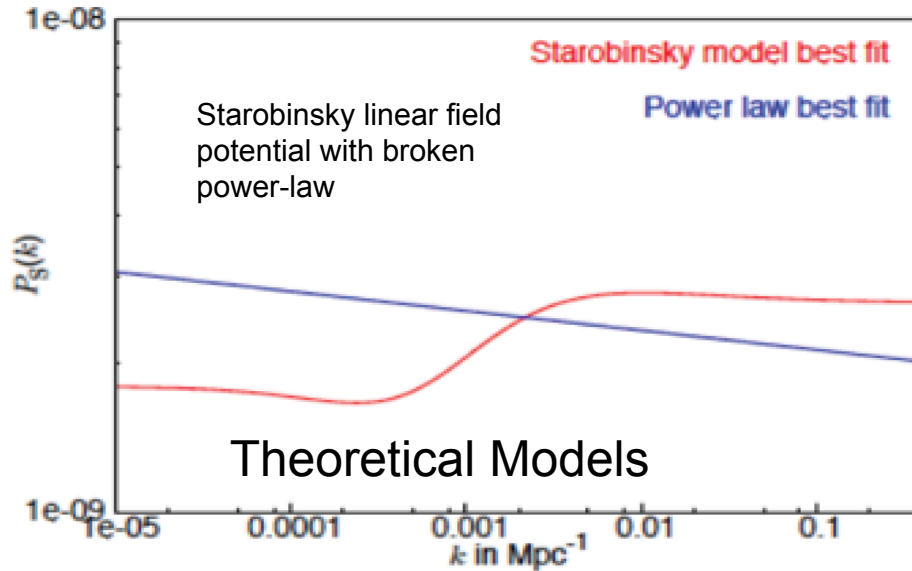
Planck 2013

Planck 2015



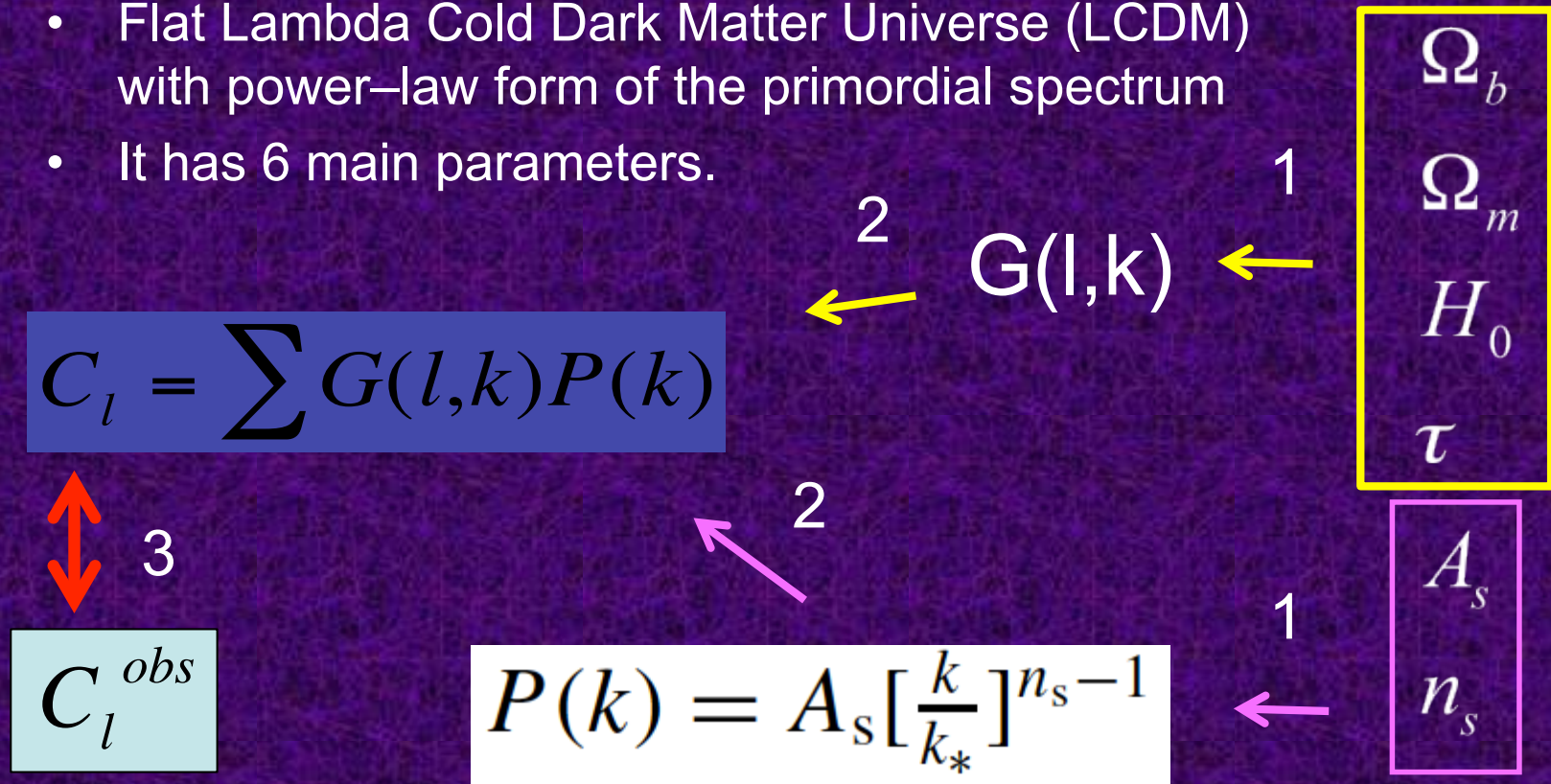
Planck 2018

# Beyond Power-Law: there are some other models consistent to the data.



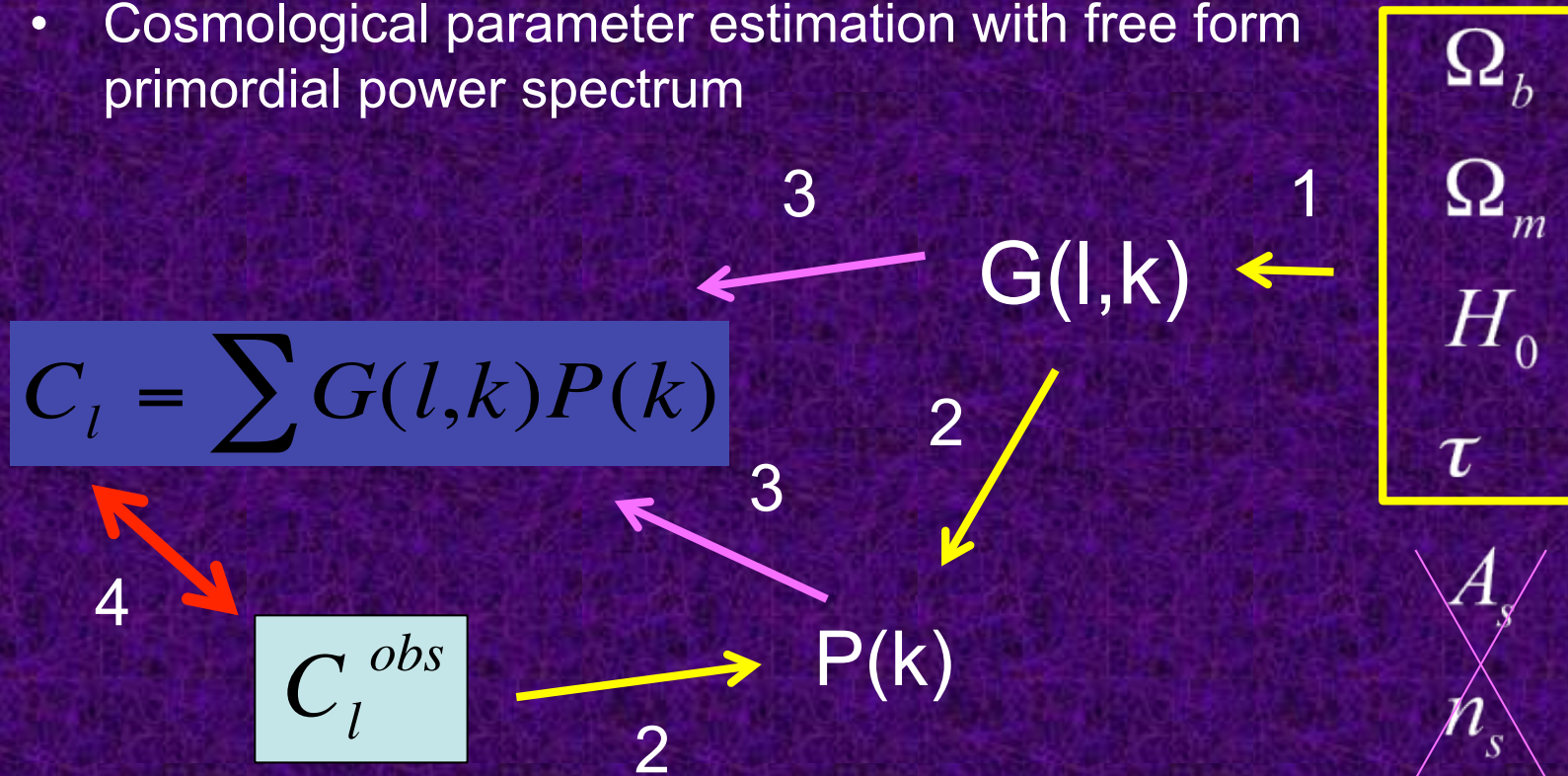
# Forms of PPS and Effects on the Background Cosmology

- Flat Lambda Cold Dark Matter Universe (LCDM) with power-law form of the primordial spectrum
- It has 6 main parameters.

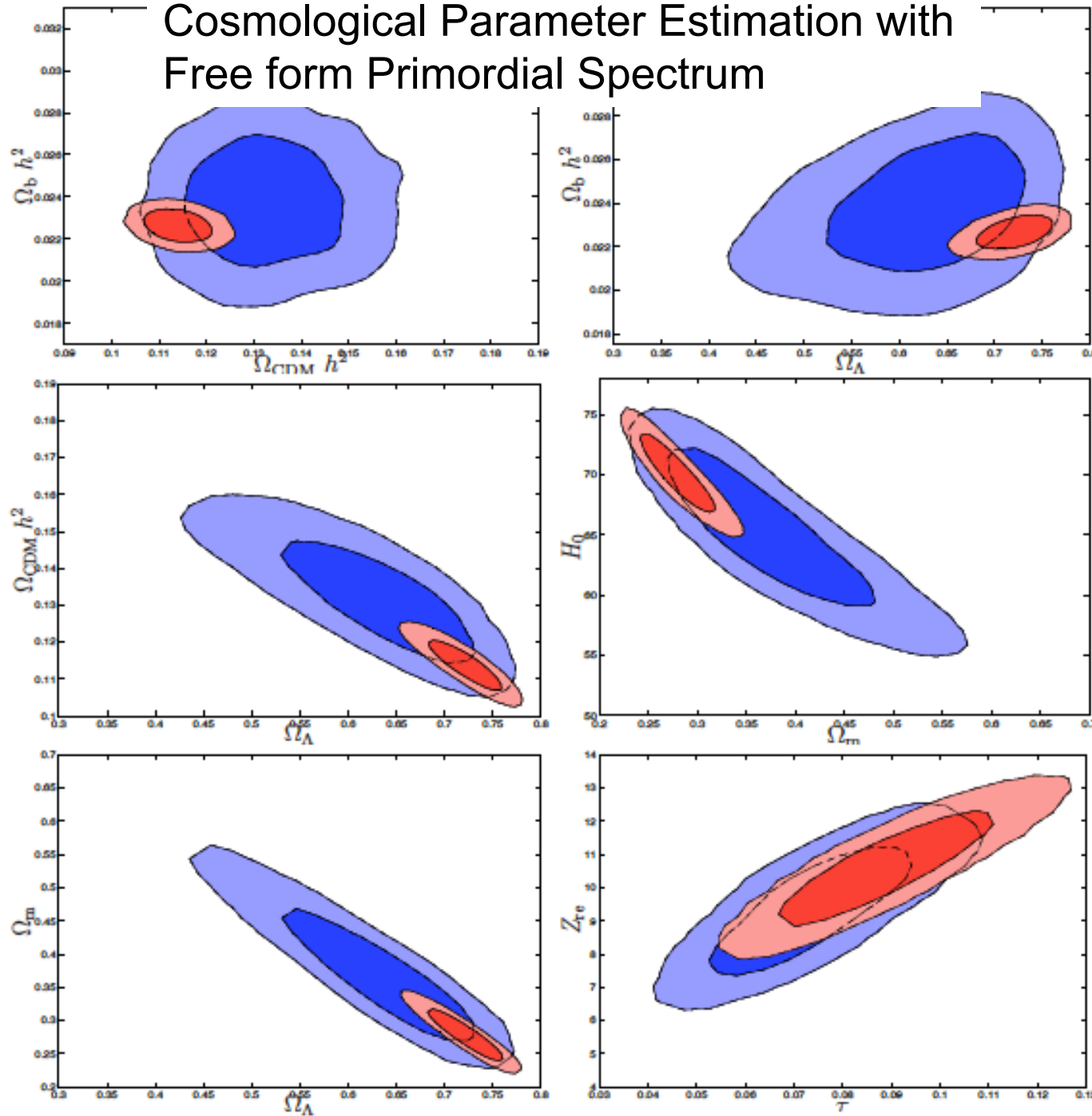


# Forms of PPS and Effects on the Background Cosmology

- Cosmological parameter estimation with free form primordial power spectrum



# Cosmological Parameter Estimation with Free form Primordial Spectrum



WMAP9 Data

Red Contours:  
Power Law PPS

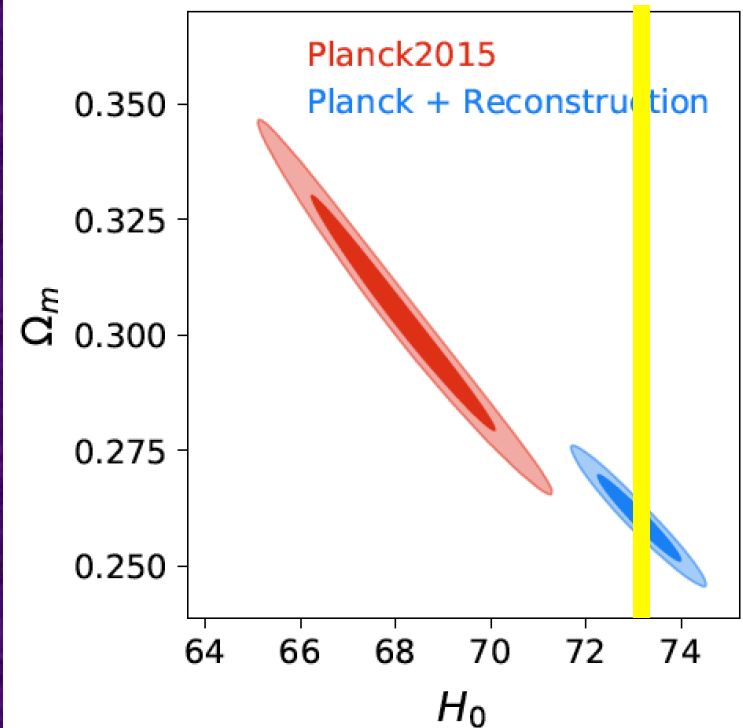
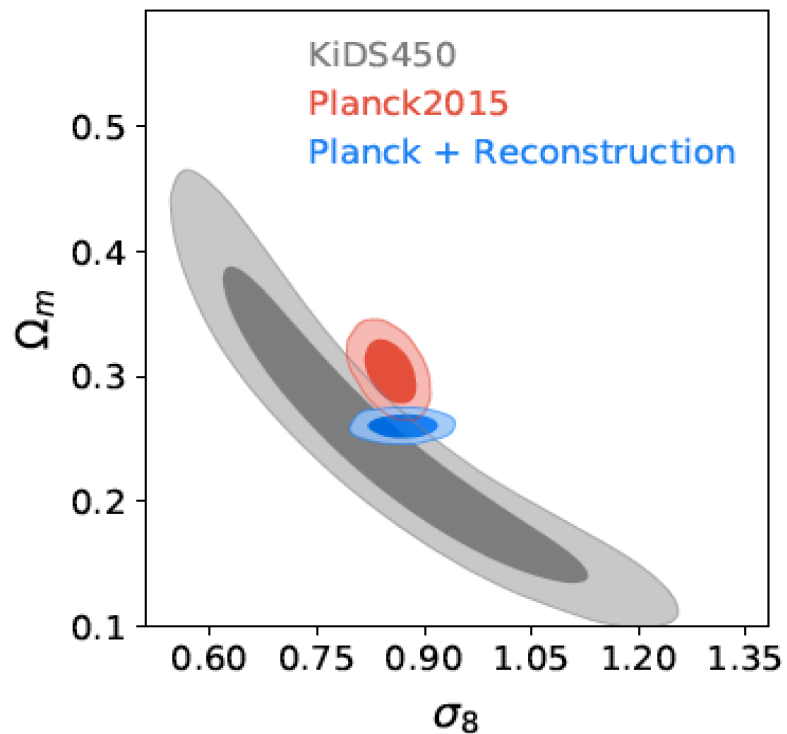
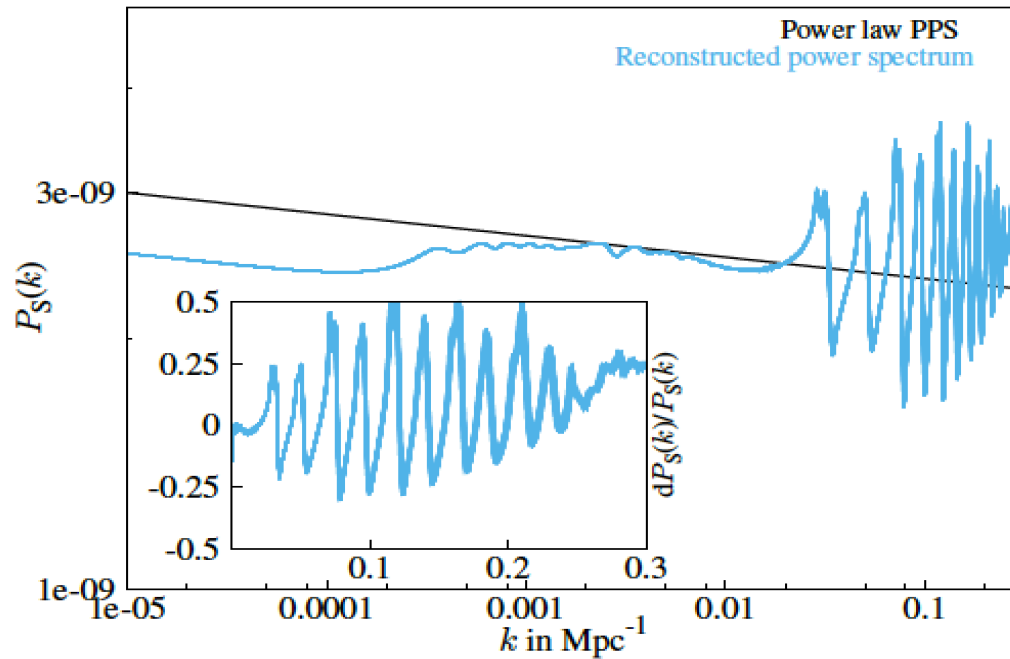
Blue Contours:  
Free Form PPS

Hazra, et al, PRD 2013



# Background Cosmological Parameters and PPS

We use the reconstructed PPS for parameter estimation, similar to what we do with PL.



# Systematics and Cosmology

High possibilities for systematics in different data

Need for independent measurements

Two key questions:

Power-law PPS?

Lambda DE?

# Future Perspective

## Full picture

Complete reconstruction analysis  
with polarization data

$$C_l^{TT} = \int \frac{dk}{k} P(k) G_l^{TT}(k)$$

$$C_l^{EE} = \int \frac{dk}{k} P(k) G_l^{EE}(k)$$

$$C_l^{BB} = \int \frac{dk}{k} P_t(k) G_l^{BB}(k)$$

$$C_l^{TE} = \int \frac{dk}{k} P(k) G_l^{TE}(k)$$

Searching for  
correlations!

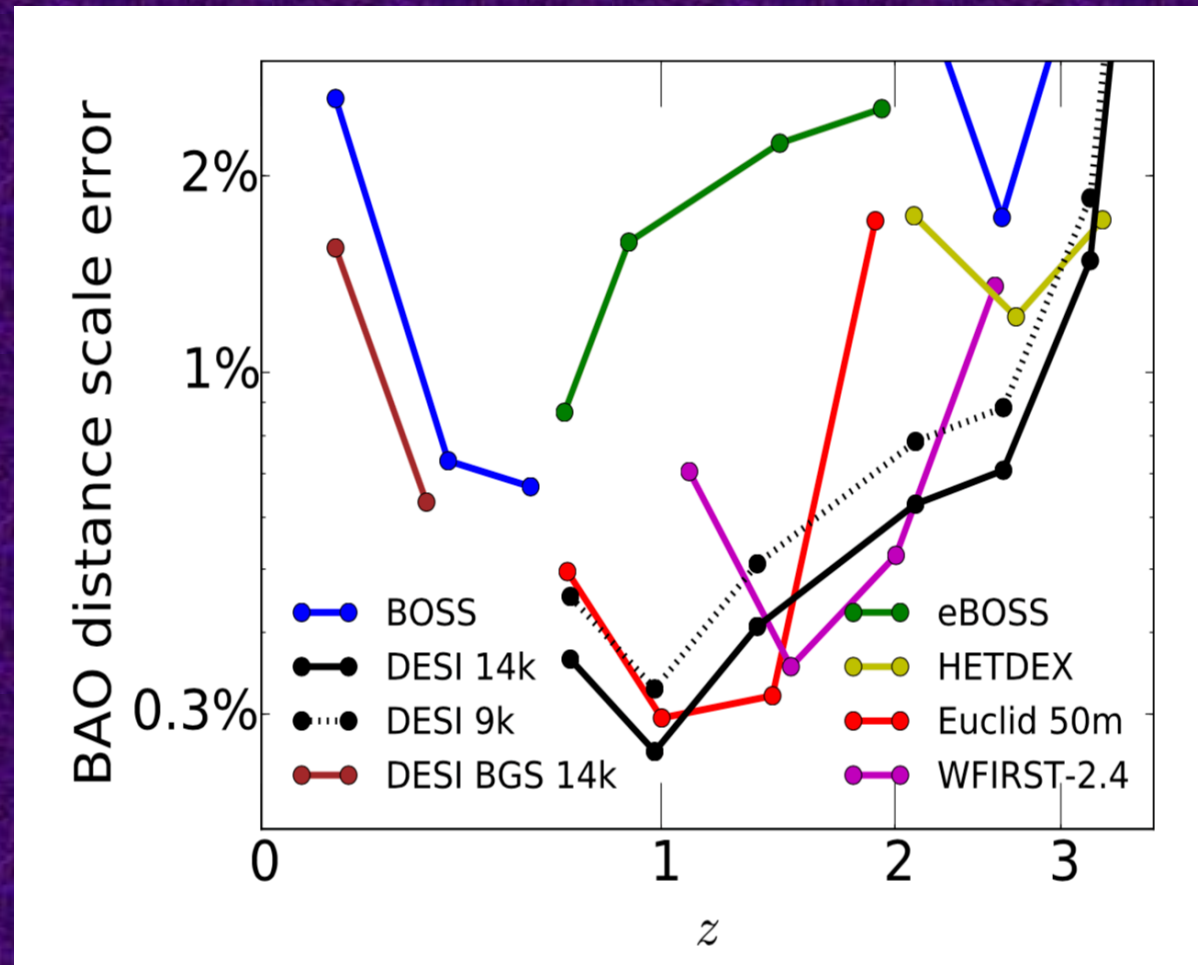
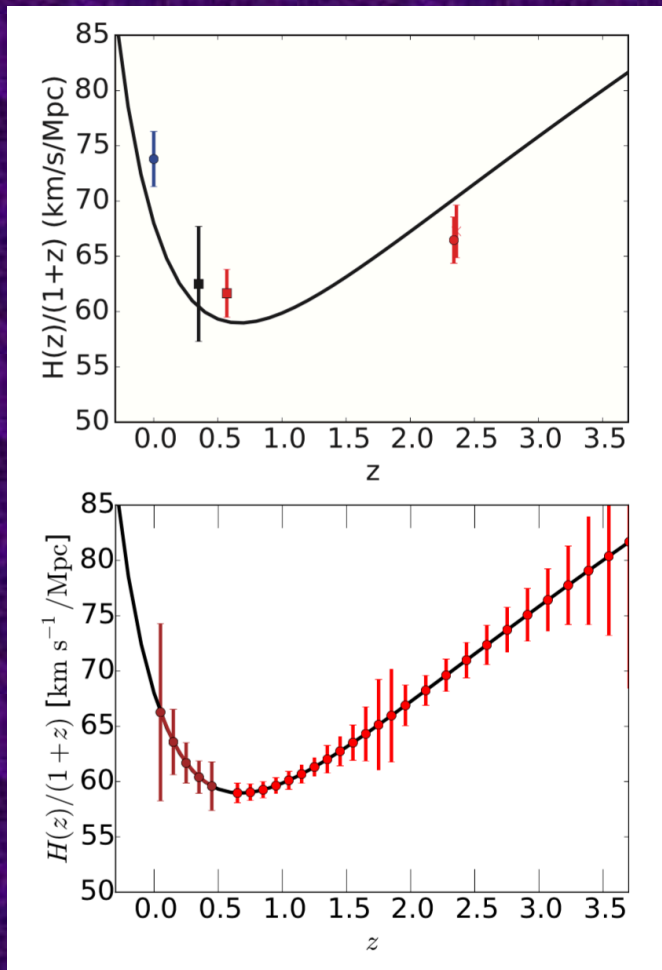
$$P_S(k), P_T(k), P_{iso}(k)$$

Primordial power spectra  
from Early universe

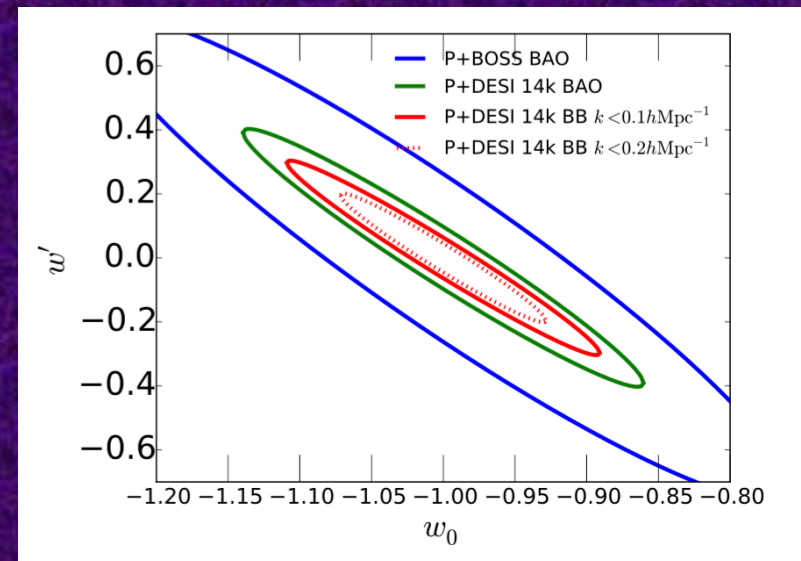
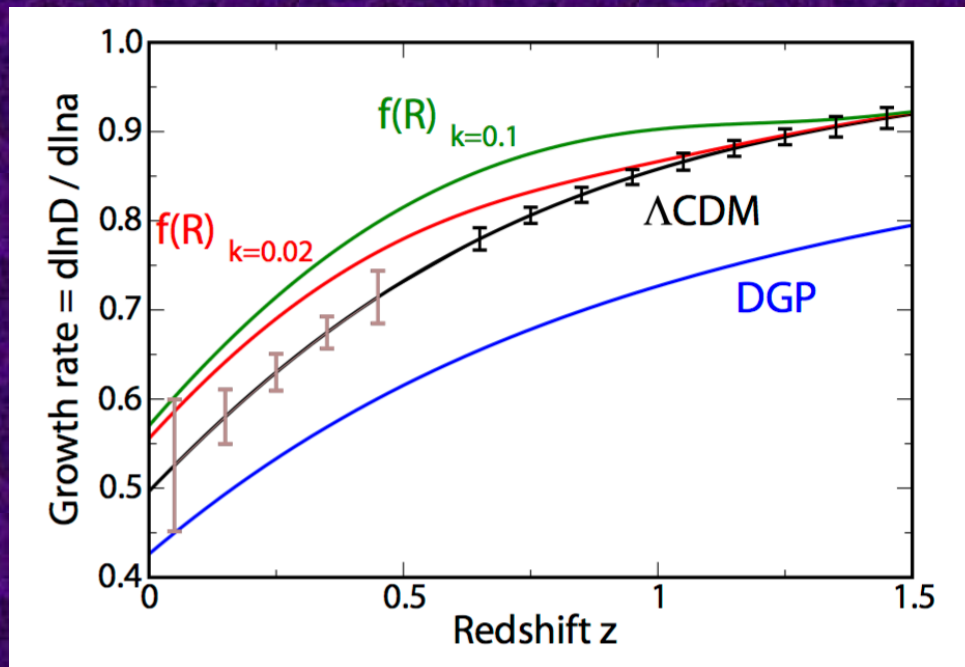
$$G_l^{TT}(k), G_l^{EE}(k), G_l^{BB}(k), G_l^{TE}(k)$$

Post recombination Radiative  
transport kernels in a given  
cosmology

# Future perspective (late universe)



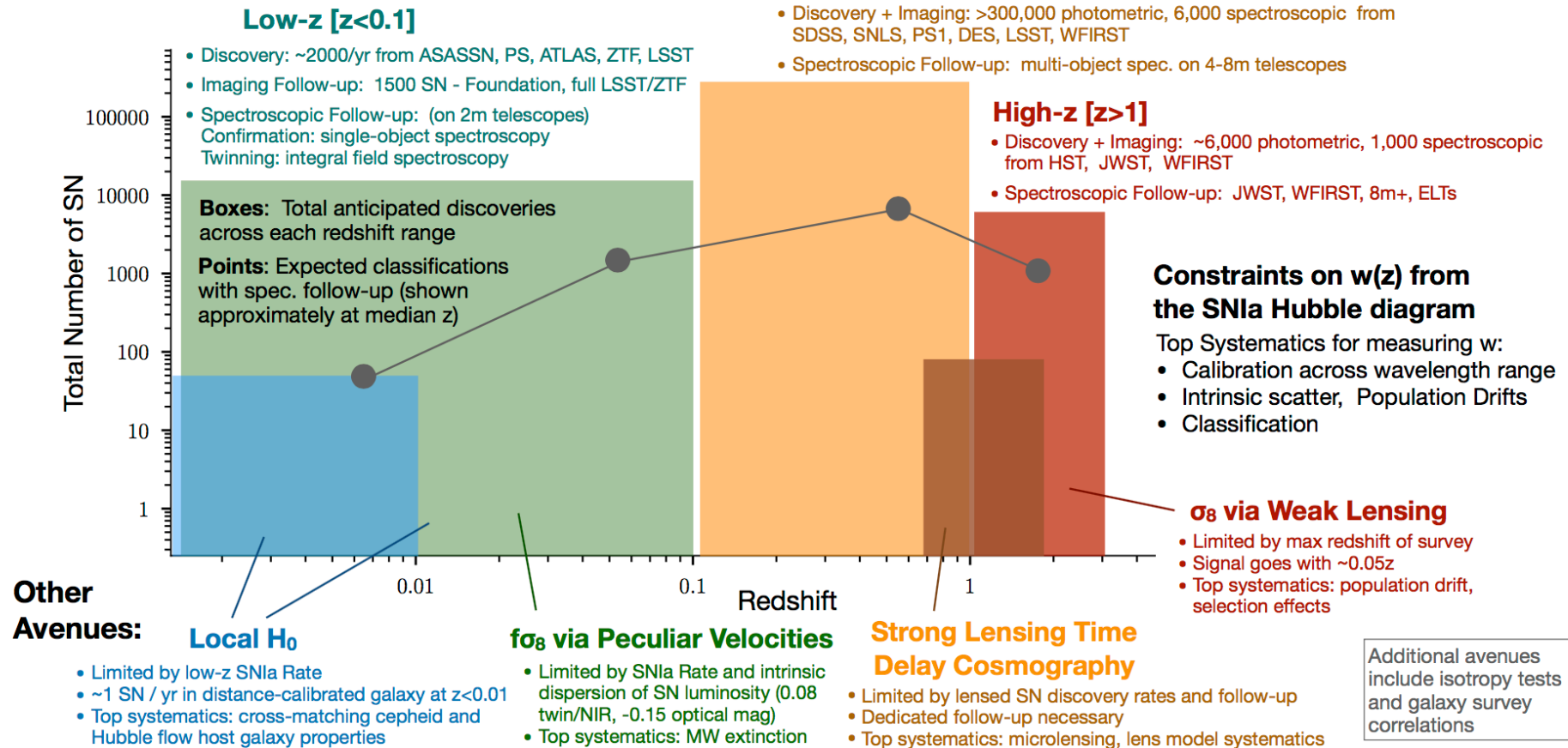
# Future perspective (late universe)



# Future perspective

# Astro2020

## The Future of SN Ia Cosmology at a Glance



# Cosmology vs Systematics vs Assumptions

- With higher quality of the data the role of systematics will become more and more prominent.
- Higher precision may cost us uncontrollable bias if we make wrong assumptions.

# Conclusion

- The current standard model of cosmology seems to work fine but this does not mean all the other models are wrong.
- $H_0$  tension seems remaining persistent in the context of the  $\Lambda$ CDM model. This can open ways for competitive alternatives (*PEDE?*).
- First target can be testing different aspects of the standard 'Vanilla' model. If it is not '*Lambda*' dark energy or power-law primordial spectrum then we can look further. It is possible to focus the power of the data for the purpose of the falsification. Next generation of astronomical/cosmological observations, (DESI, Euclid, LSST, WFIRST, SKA(?), etc) will make it clear about the *status of the concordance model in 2020s*.
- ***Combination of different cosmological data also hints towards some tension with  $\Lambda$ CDM model. If future data continues the current trend, we may have some exciting times ahead!***