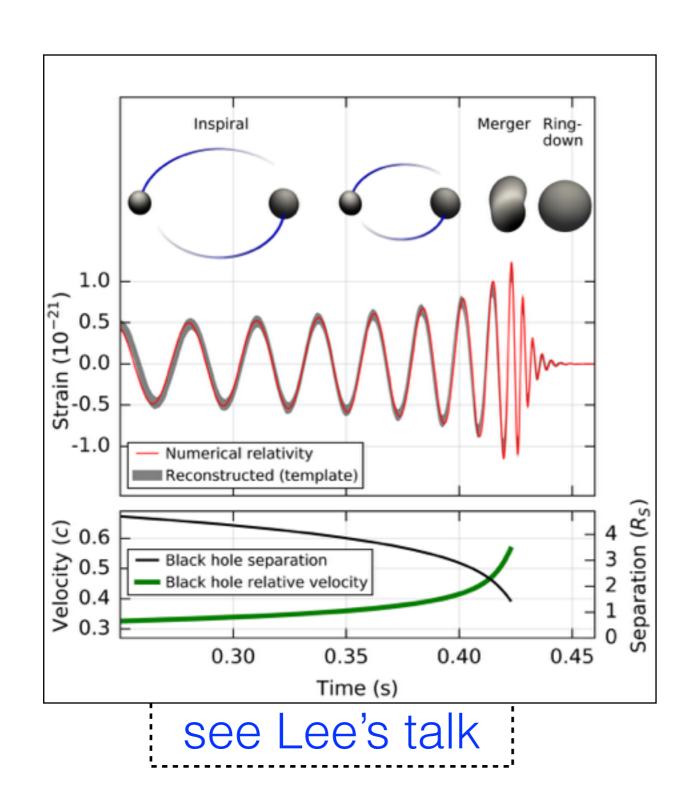
GRAVITATIONAL WAVES AS A PROBE OF HIGH ENERGY PHYSICS

DANIEL G. FIGUEROA EPFL, Lausanne, Switzerland

Einstein 1916 ... LIGO/VIRGO 2015/16/17



Gravitational
Waves (GWs)
detected I
Milestone

We can observe the Universe through GWs

Cosmology with GWs

- * Late Universe: Hubble diagram from Binaries
- * Early Universe: High Energy Particle Physics

Can we really probe High Energy Physics using Gravitational Waves (GWs)? How?

GWs: probe of the early Universe

WEAKNESS of GRAVITY:

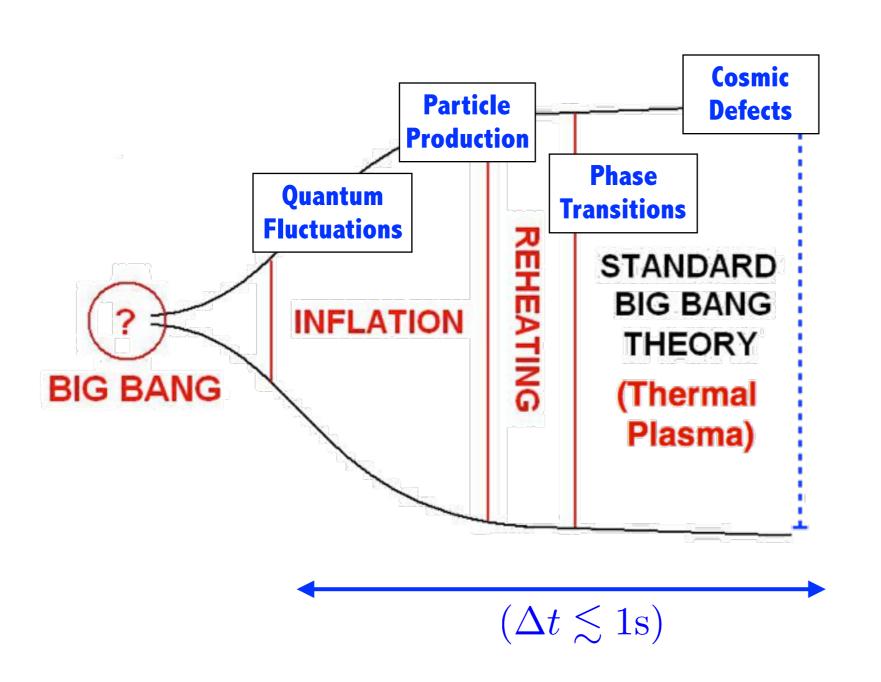
ADVANTAGE: GW DECOUPLE upon Production

DISADVANTAGE: DIFFICULT DETECTION

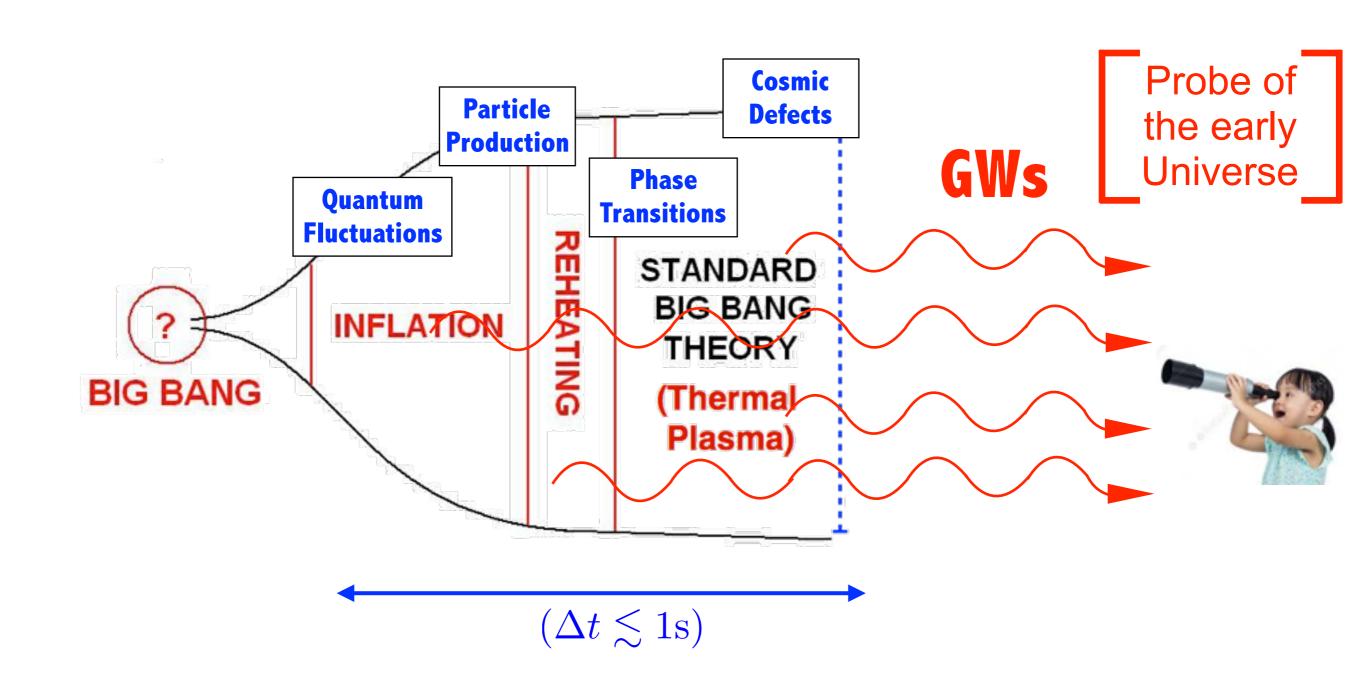
② ADVANTAGE: GW → Probe for Early Universe

```
\rightarrow \left\{ \begin{array}{l} \textbf{Decouple} \rightarrow \underline{Spectral\ Form\ Retained} \\ \textbf{Specific\ HEP} \Leftrightarrow \underline{Specific\ GW} \end{array} \right.
```

The Early Universe



The Early Universe



OUTLINE

O) GW definition

1) GWs from Inflation

Early Universe

- 2) GWs from Preheating
- 3) GWs from Phase Transitions
- 4) GWs from Cosmic Defects

Gravitational Waves in Cosmology

FRW:
$$ds^2 = a^2(-d\eta^2 + (\delta_{ij} + h_{ij})dx^i dx^j), \quad TT: \begin{cases} h_{ii} = 0 \\ h_{ij,j} = 0 \end{cases}$$

Transverse-Traceless (TT)

$$TT: \begin{cases} h_{ii} = 0 \\ h_{ij}, j = 0 \end{cases}$$

Creation/Propagation GWs

$$h_{ij}^{\prime\prime\prime} + 2\mathcal{H}h_{ij}^{\prime} - \nabla^2 h_{ij} = 16\pi G \Pi_{ij}^{\mathrm{TT}},$$

Source: Anisotropic Stress

$$\Pi_{ij} = T_{ij} - \langle T_{ij} \rangle_{FRW}$$

GW Source(s): (SCALARS , VECTOR , FERMIONS)

$$\Pi_{ij}^{TT} \propto \{\partial_i \chi^a \partial_j \chi^a\}^{TT}, \{E_i E_j + B_i B_j\}^{TT}, \{\bar{\psi} \gamma_i D_j \psi\}^{TT}$$

Gravitational Waves as a probe of the early Universe

OUTLINE

0) GW definition

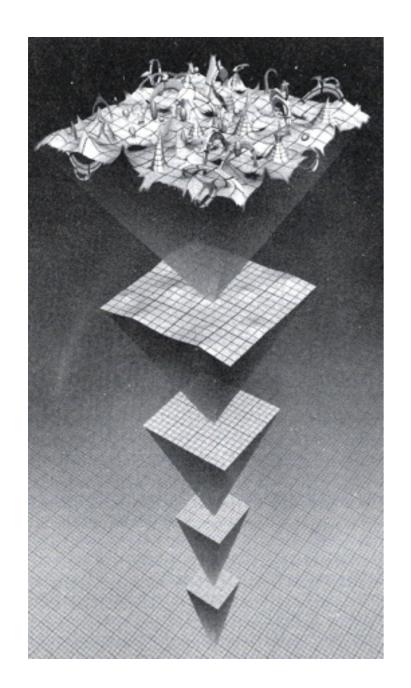


1) GWs from Inflation

Early Universe

- 2) GWs from Preheating
- 3) GWs from Phase Transitions
- 4) GWs from Cosmic Defects

recall Pryke's talk



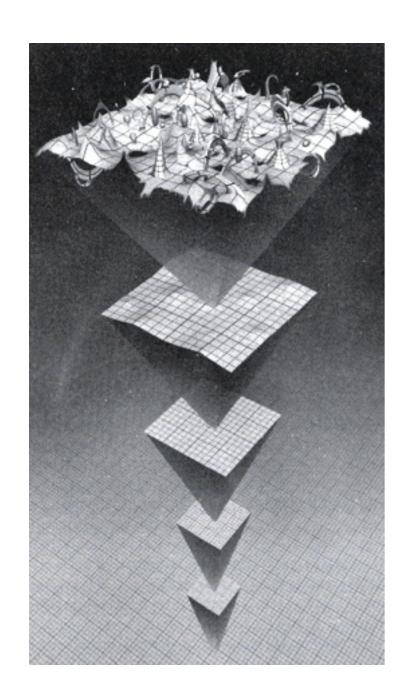


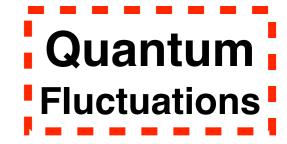
$$\Omega_{\text{GW}}^{(o)}(f) \equiv \frac{1}{\rho_c^{(o)}} \left(\frac{d \log \rho_{\text{GW}}}{d \log k} \right)_o = \frac{\Omega_{\text{Rad}}^{(o)}}{24} \Delta_{h_*}^2(k) \qquad \Delta_h^2(k) = \frac{2}{\pi^2} \left(\frac{H}{m_p} \right)^2 \left(\frac{k}{aH} \right)^{n_t}$$

$$\Delta_h^2(k) = \frac{2}{\pi^2} \left(\frac{H}{m_p}\right)^2 \left(\frac{k}{aH}\right)^{n_t}$$

$$energy \ scale$$

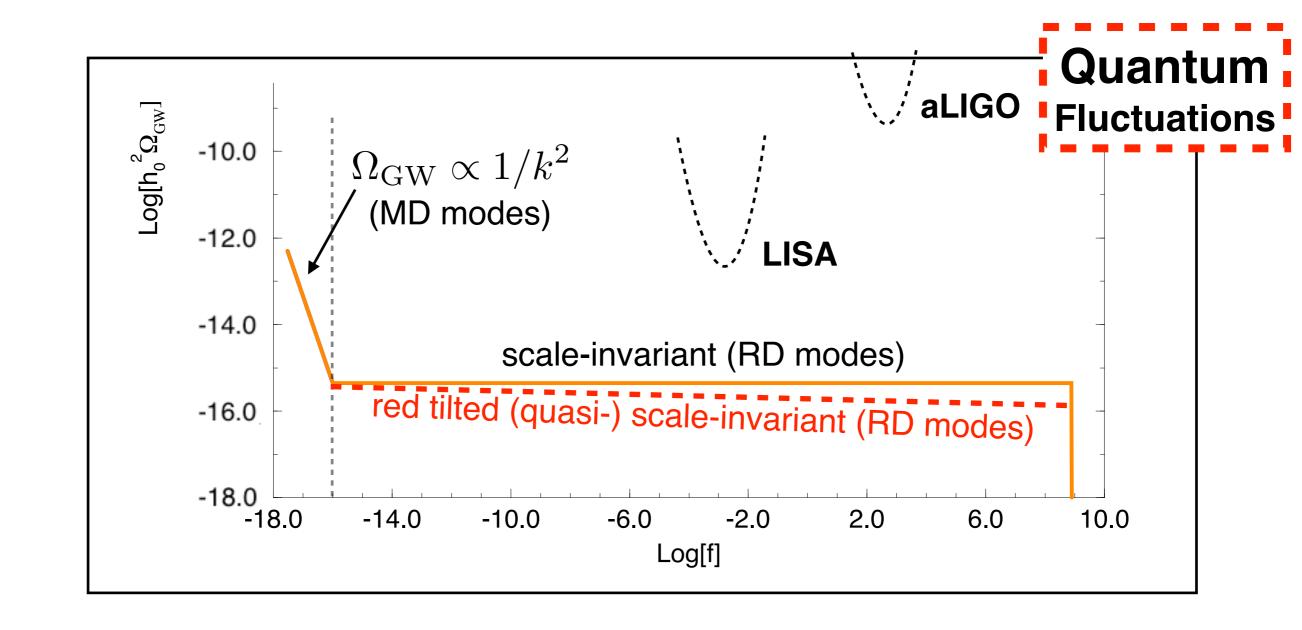
$$n_t \equiv -2\epsilon$$





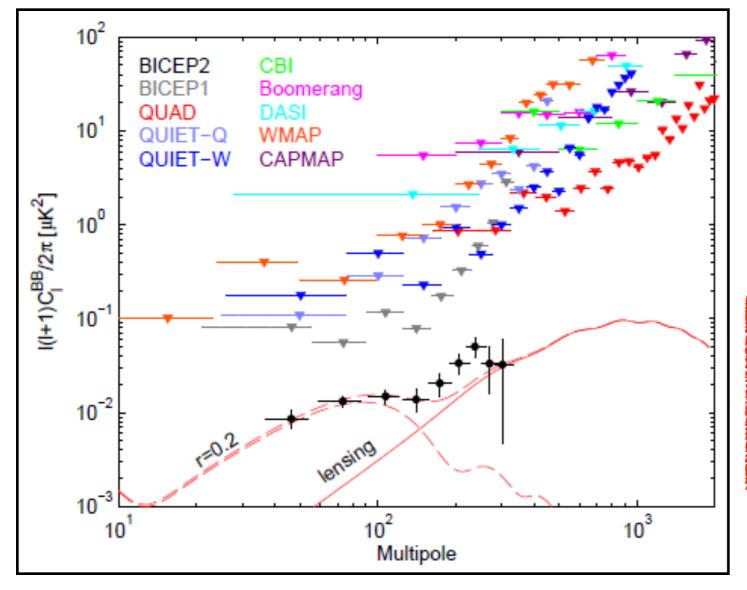
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$$\Delta_h^2(k) = \frac{2}{\pi^2} \left(\frac{H}{m_p}\right)^2 \left(\frac{k}{aH}\right)^{n_t}$$
 energy scale
$$n_t \equiv -2\epsilon$$



$$\langle \mathcal{E}^2 \rangle, \ \langle \mathcal{B}^2 \rangle \ \rightarrow \ \langle |e_{lm}|^2 \rangle \equiv C_l^E, \ \langle |b_{lm}|^2 \rangle \equiv C_l^B$$

B- MODE: Depends only on Tensor Perturbations!

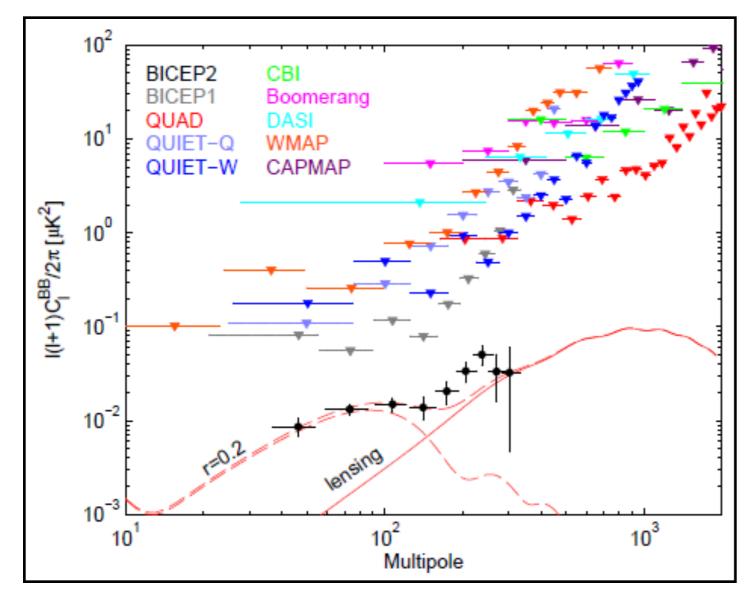


Pashed Line Theoretical Inflation Expectation

$$r\equiv\Delta_t^2/\Delta_s^2<0.07~(2\sigma)$$
 $r\sim10^{-2}-10^{-3}$ $\Rightarrow E_*\sim5\cdot10^{15}{
m GeV}$ next goal

$$\langle \mathcal{E}^2 \rangle, \ \langle \mathcal{B}^2 \rangle \ \rightarrow \ \langle |e_{lm}|^2 \rangle \equiv C_l^E, \ \langle |b_{lm}|^2 \rangle \equiv C_l^B$$

B- MODE: Depends only on Tensor Perturbations!



Search of B-modes @ CMB, might be only change to detect Inflationary Tensors!

Ground:

AdvACT, CLASS, Keck/BICEP3, Simons Array, SPT-3G

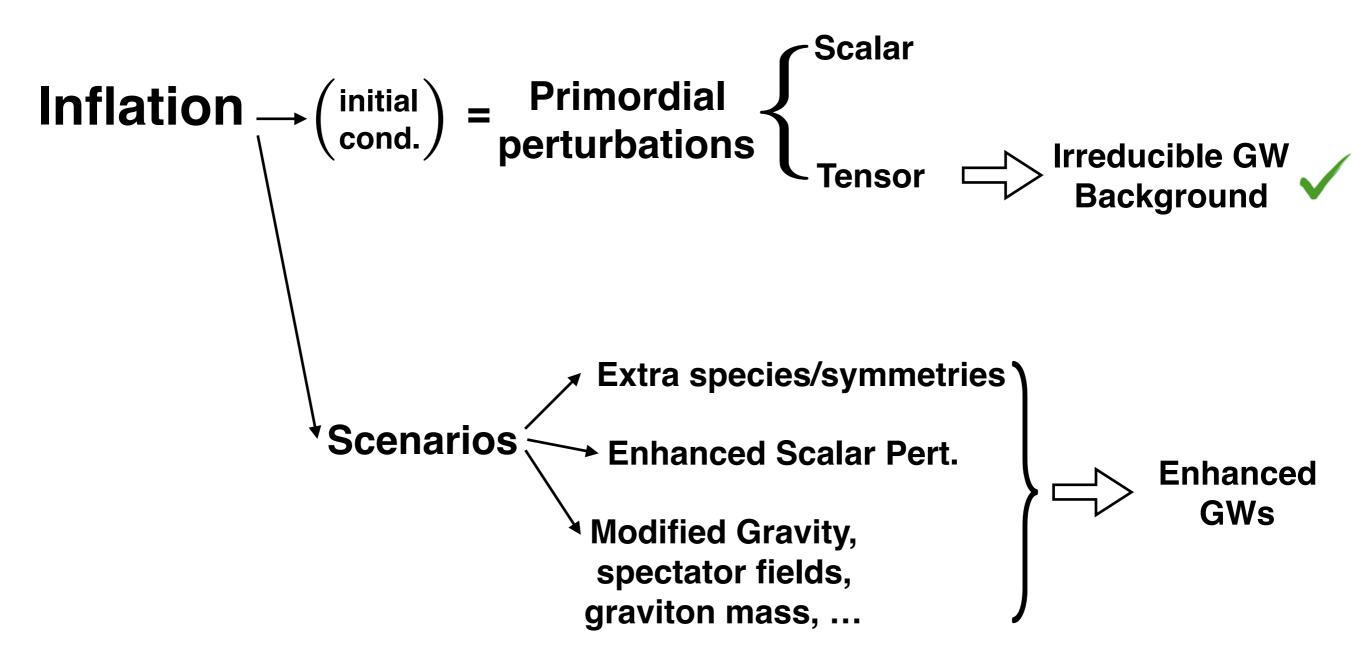
Balloons

Satellites

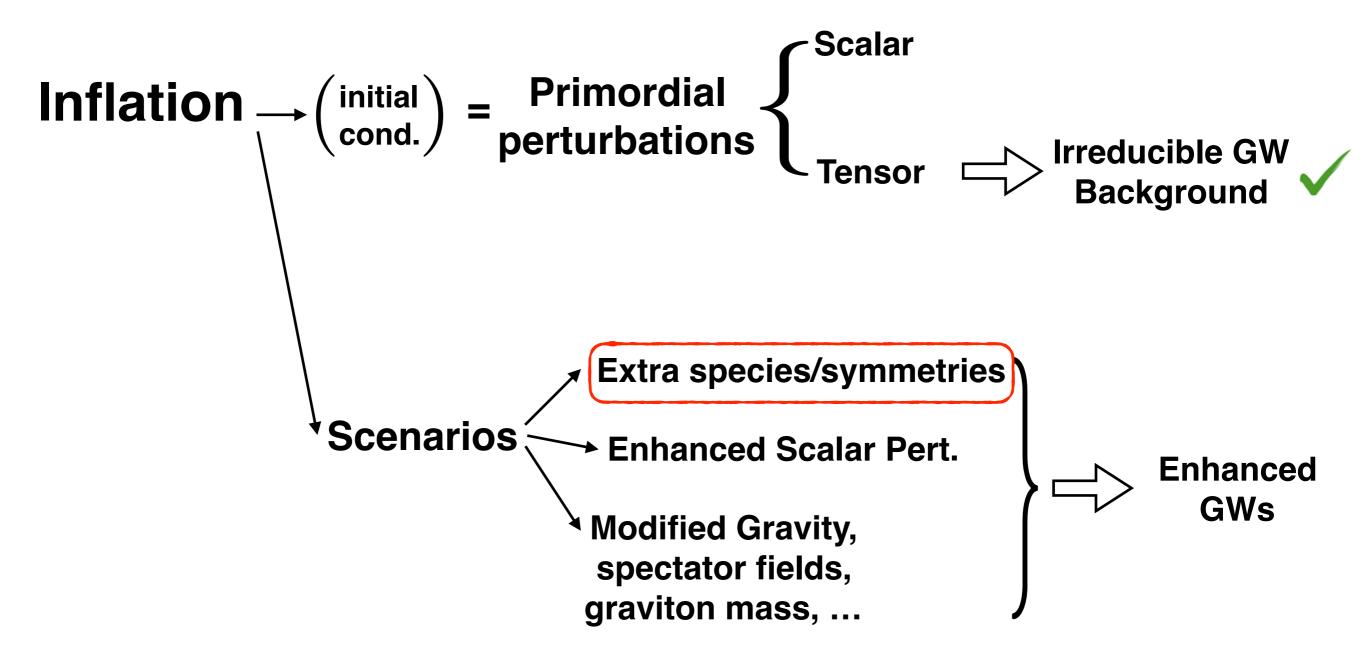
EBEX 10k, Spider

CMBPol, COrE, LiteBIRD,

INFLATIONARY COSMOLOGY



INFLATIONARY COSMOLOGY



INFLATION A POPULATION OF THE PROPERTY OF THE

Axion-Inflation ships the action of the contract of the contra



Flatness and gaussia
Constraints and gaussia



olings to oth ence values f

Free $\phi \to AA$ μυρισαιιν τωιτιτοιν reheasing a N (review Pajer, MP '13)

INFLATION AND THE SINGLE STATES

Axion-Inflation shift techniques, of its shift techniques, of the shift techniques, of its shift techniques.



[J. Cook, L. Sorbo (ar Sv: DW).06011 THE SECOND TO THE STATE OF THE SECOND TH

Photon: 2 helicities This is the property on a court of the control of t

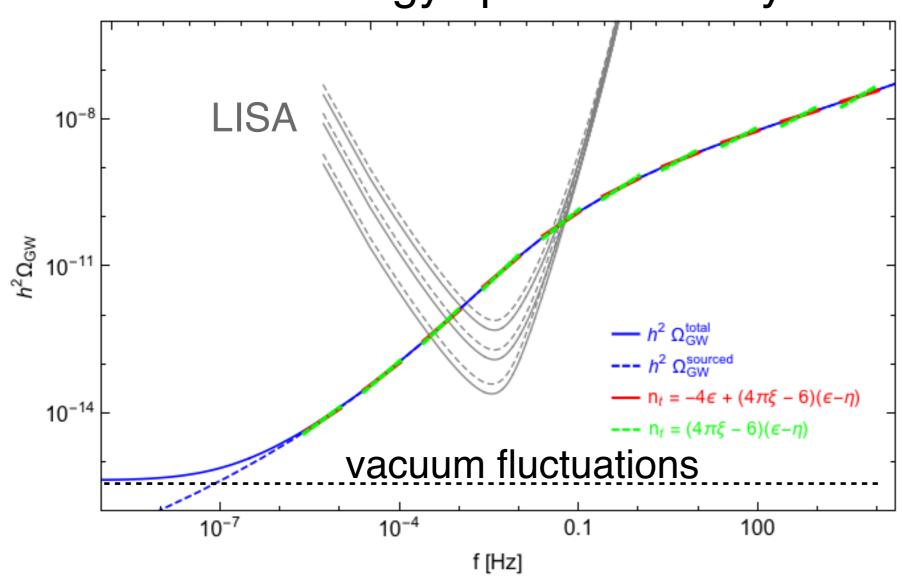
(review Pajer, MP '13)

Chiral instability

NFLATIONARY 2 MINISTER OF THE STATE OF THE S Axion* Inflation Shift geytham (reviews the advantage that) Ann P_{c} Axion-Inflation shift geytham φ and $V(\varphi) + \frac{\varphi}{f} F_{\mu\nu} \tilde{F}^{\mu\nu}$ * Not the OCD axion; reference Constrate Statutess and gaussianity AXWITH SIGNIFICATION OF THE PROPERTY AND A TO THE PROPERTY AND A T $h_{ij}^{\prime\prime}+2\mathcal{H}h_{ij}^{\prime}-\nabla^{2}h_{ij}=50$ if the symmetry operation of the symmetry operation operation of the symmetry operation operation of the symmetry operation op Freese, Freence values f $\phi \to AA$ typically controls reheasing a N (review Pajer, MP '13)

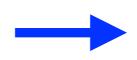
INFLATIONARY MODELS Axion-Inflation

GW energy spectrum today



Blue-Tilted
+ Chiral
+ Non-G
GW background

What if there are arbitrary fields coupled to the inflaton? (i.e. no need of extra symmetry)



large excitation of fields !? will they create GWs?

inflaton $\phi \longrightarrow V(\phi)$

$$-\mathcal{L}_{\chi} = (\partial \chi)^2/2 + g^2(\phi - \phi_0)^2\chi^2/2$$

Scalar Fld

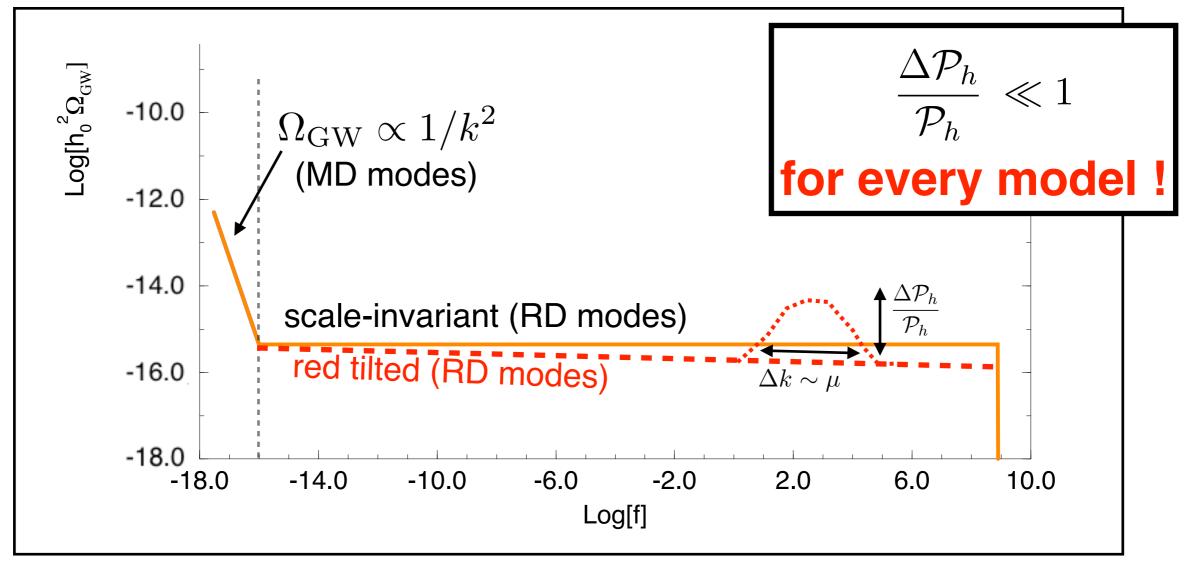
$$-\mathcal{L}_{\psi} = \bar{\psi}\gamma^{\mu}\partial_{\mu}\psi + g(\phi - \phi_0)\bar{\psi}\psi$$

Fermion Fld

$$\mathcal{L} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} - |(\partial_{\mu} - gA_{\mu})\Phi)|^2 - V(\Phi^{\dagger}\Phi)$$
 Gauge Fld ($\Phi = \phi e^{i\theta}$)

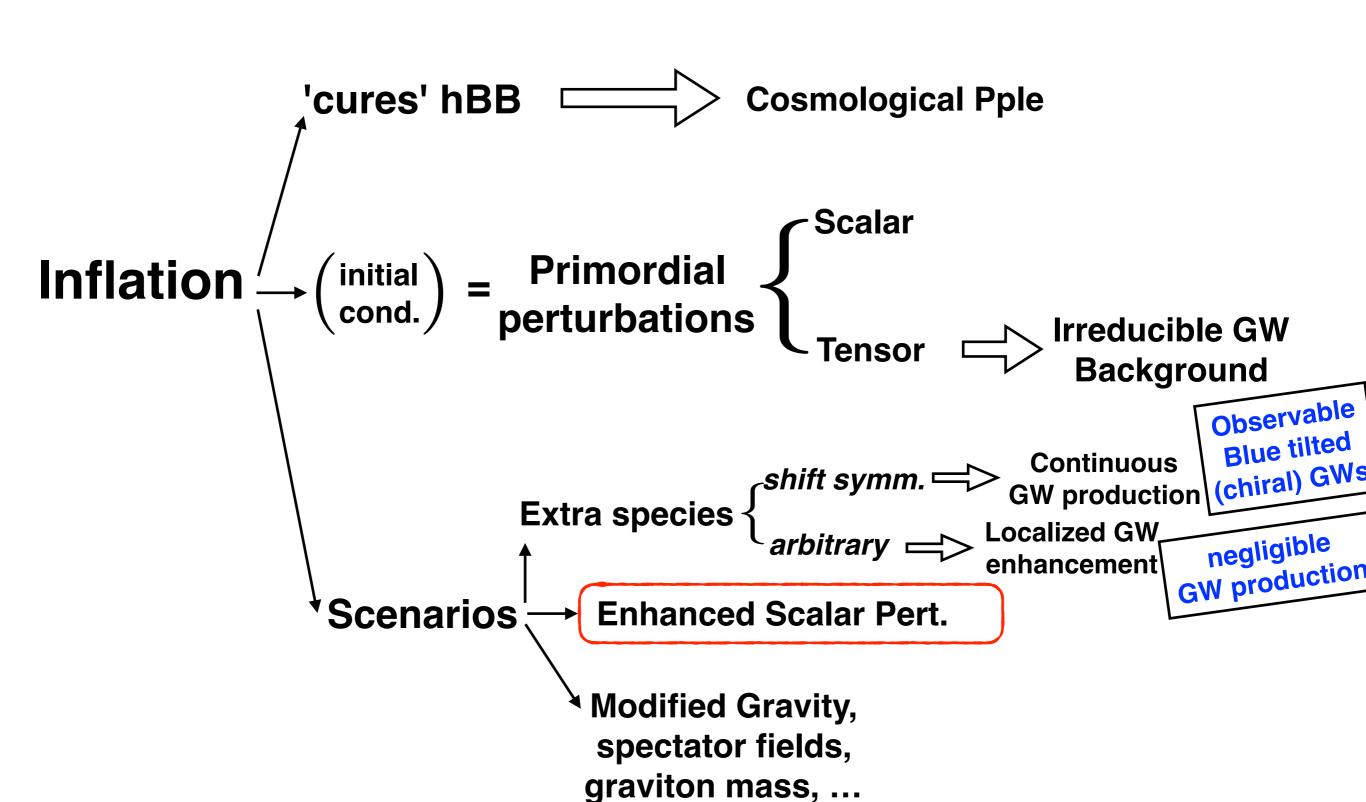
$$\frac{\Delta \mathcal{P}_h}{\mathcal{P}_h} \equiv \frac{\mathcal{P}_h^{(\text{tot})} - \mathcal{P}_h^{(\text{vac})}}{\mathcal{P}_h^{(\text{vac})}} \equiv \frac{\mathcal{P}_h^{(\text{pp})}}{\mathcal{P}_h^{(\text{vac})}} \sim few \times \mathcal{O}(10^{-4}) \frac{H^2}{m_{\text{pl}}^2} W(k\tau_0) \left(\frac{\mu}{H}\right)^3 \ln^2(\mu/H)$$

$$\mu^2 \equiv g\dot{\phi}_0$$



(Sorbo et al 2011, Peloso et al 2012-2013, Caprini & DGF 2018)

INFLATIONARY COSMOLOGY



Let us suppose
$$\left| \Delta_{\mathcal{R}}^2 \gg \Delta_{\mathcal{R}}^2 \right|_{\mathrm{CMB}} \sim 3 \cdot 10^{-9}$$
, @ small scales

$$h_{ij}'' + 2\mathcal{H}h_{ij}' + k^2h_{ij} = S_{ij}^{TT}$$
 $\sim \Phi * \Phi$ (2nd Order Pert.)

possible to enhance
$$\Delta^2_{\mathcal{R}}$$
 (at small scales)

BBN
$$\Omega_{gw,0} < 1.5 \times 10^{-5}$$
 \longrightarrow $\triangle_{\mathcal{R}}^2 < 0.1$

LIGO
$$\Omega_{gw,0} < 6.9 \times 10^{-6}$$
 _____ $\triangle_R^2 < 0.07$

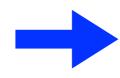
PTA
$$\Omega_{gw,0} < 4 \times 10^{-8}$$
 \longrightarrow $\triangle_{\mathcal{R}}^2 < 5 \times 10^{-3}$

LISA
$$\Omega_{gw,0} < 10^{-13}$$
 — $\triangle_{\mathcal{R}}^2 < 1 \times 10^{-5}$

BBO
$$\Omega_{gw,0} < 10^{-17}$$
 \longrightarrow $\Delta_{\mathcal{R}}^2 < 3 \times 10^{-7}$

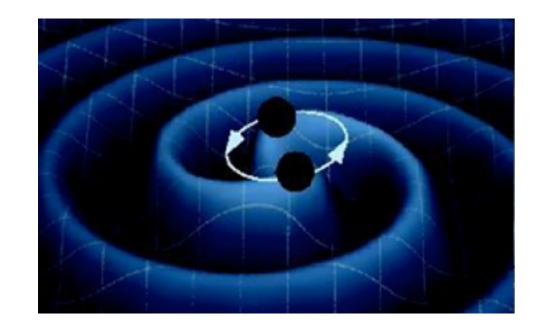
 $| \textbf{INFLATION} \longrightarrow \textbf{IF} \left\{ \begin{array}{l} \textbf{NON-MONOTONIC} \\ \textbf{multi-field} \end{array} \right\} \xrightarrow{\textbf{possible to}} \textbf{enhance } \Delta^2_{\mathcal{R}} \\ \textbf{(at small scales)}$

IF $\Delta^2_{\mathcal{R}}$ very enhanced



Primordial Black Holes (PBH) may be produced!

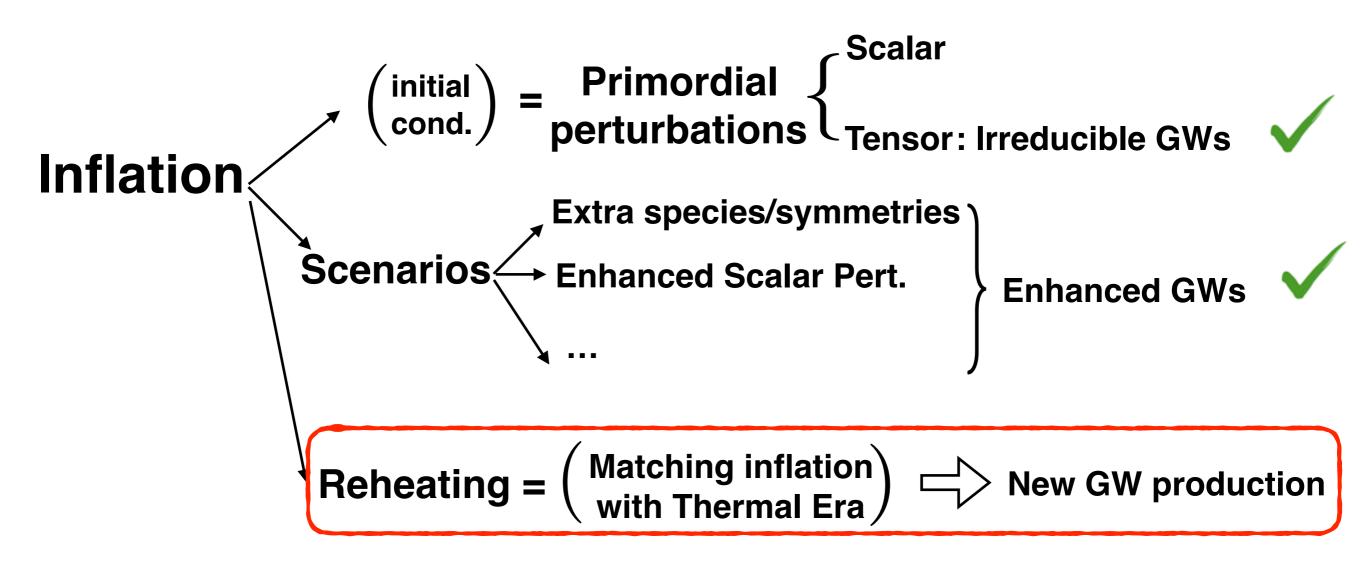
Has LIGO detected PBH's ?



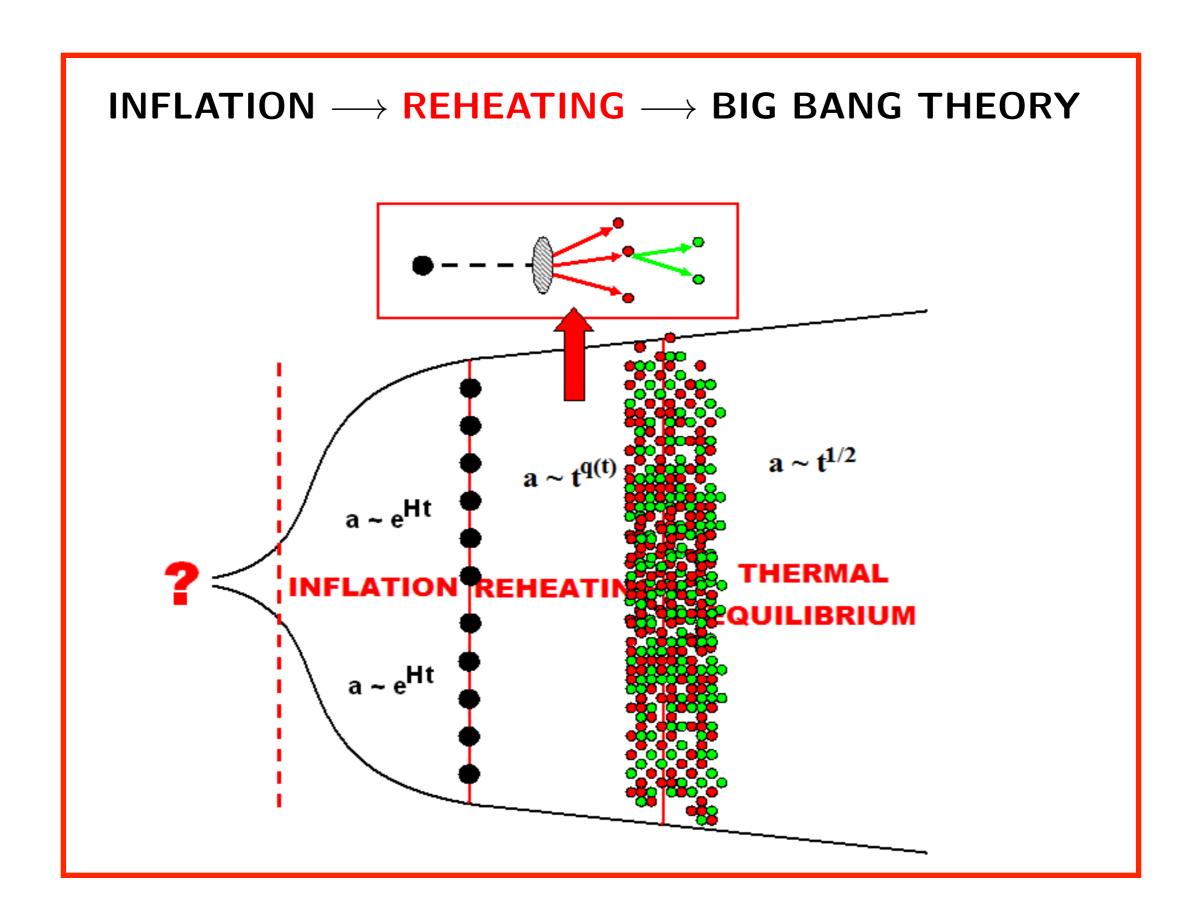
PBH candidate for Dark Matter?

See e.g. papers by Ali-Haimoud, Byrnes, Ga-Bellido, Sasaki, Zumalacarregui, ... et al

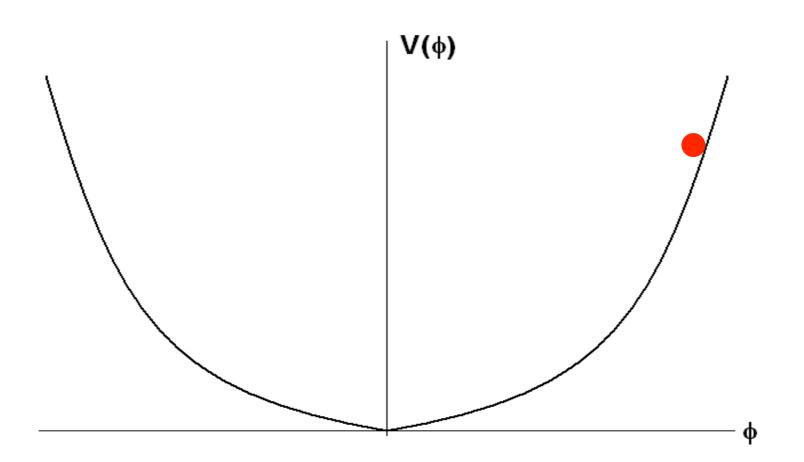
INFLATIONARY COSMOLOGY



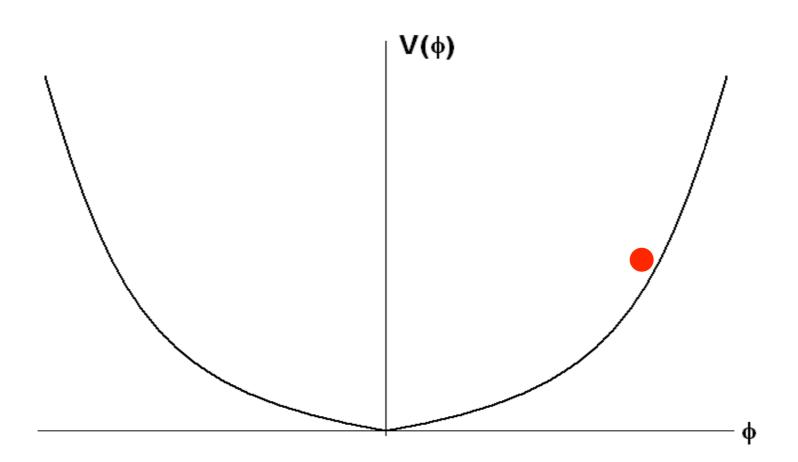
GWs from (p)Reheating



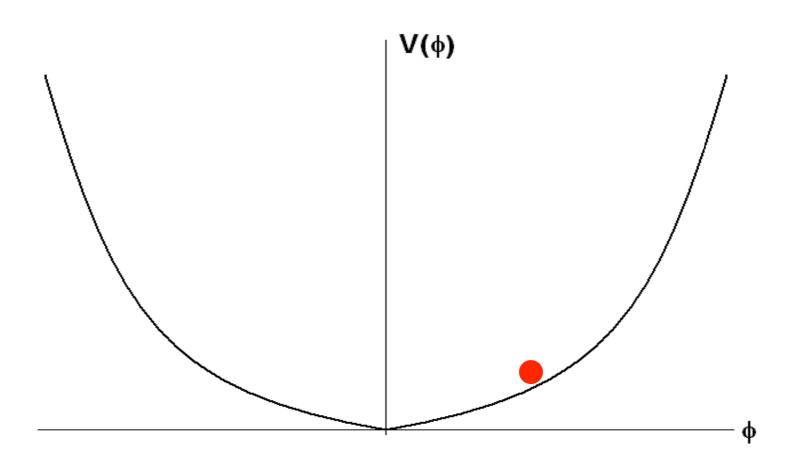
$$V(\phi,\chi)=$$
 $V(\phi)$ + $\frac{1}{2}m_\chi^2\chi^2$ + $\frac{1}{2}g^2\phi^2\chi^2$ (Chaotic Models)
$$X_k''+[\kappa^2+m^2(\phi)]X_k=0$$
 (Fluctuations of Matter)



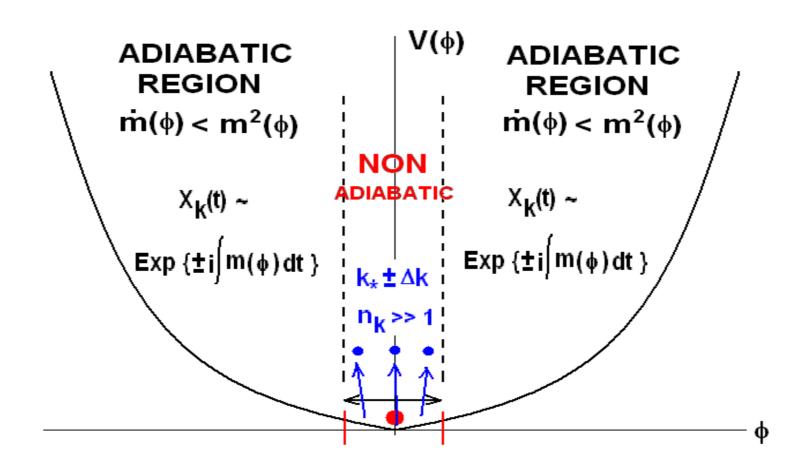
$$V(\phi,\chi)=V(\phi)+\frac{1}{2}m_\chi^2\chi^2+\frac{1}{2}g^2\phi^2\chi^2$$
 (Chaotic Models)
$$X_k''+[\kappa^2+m^2(\phi)]X_k=0 \quad \text{(Fluctuations of Matter)}$$



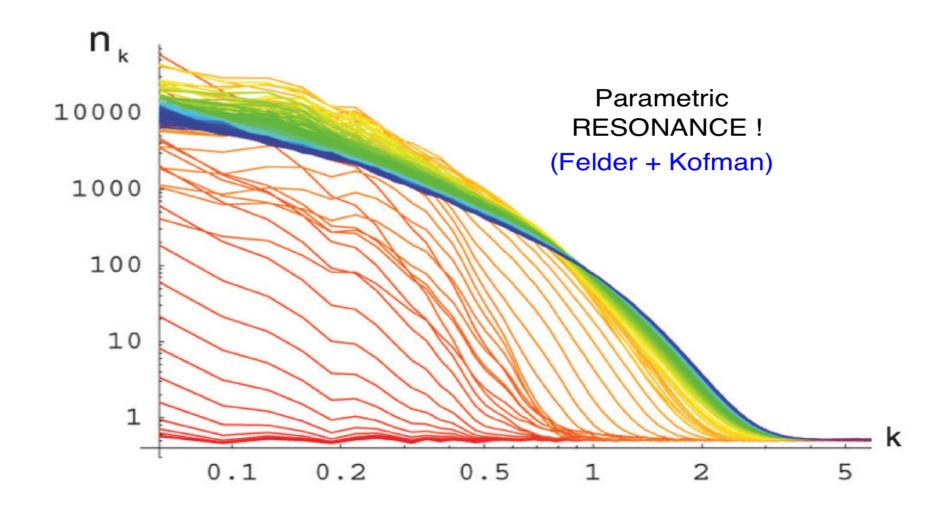
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$$V(\phi,\chi)=V(\phi)+\frac{1}{2}m_\chi^2\chi^2+\frac{1}{2}g^2\phi^2\chi^2$$
 (Chaotic Models)
$$X_k''+[\kappa^2+m^2(\phi)]X_k=0 \quad \text{(Fluctuations of Matter)}$$



2) Hybrid Scenarios: SPINODAL INSTABILITY

$$\ddot{\phi}(t) + (\mu^2 + g^2|\chi|^2)\phi(t) = 0$$

$$\ddot{\chi}_k + (k^2 + m^2 \left(\frac{\phi^2}{\phi_c^2} - 1\right) + \lambda|\chi|^2)\chi_k = 0$$

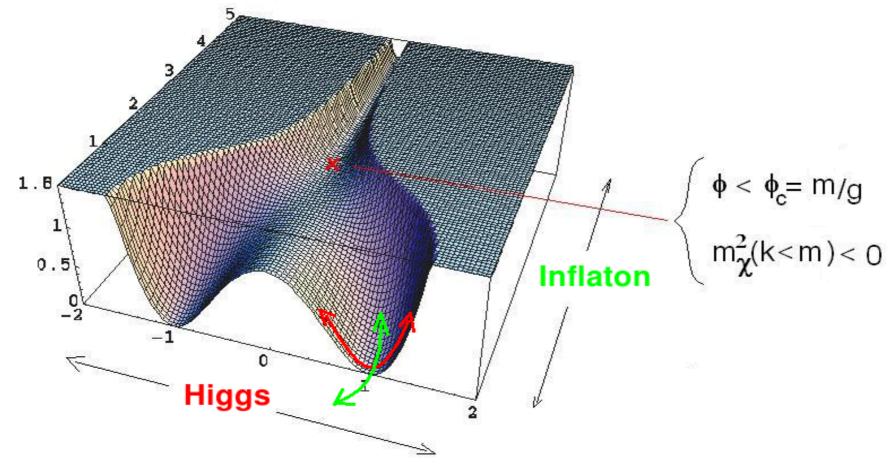
$$(k < m = \sqrt{\lambda}v)$$

$$\chi_k, n_k \sim e^{\sqrt{m^2 - k^2}t}$$

$$(k < m = \sqrt{\lambda}v)$$

$$\chi_k, n_k \sim e^{\sqrt{m^2 - k^2}t}$$

Hybrid Preheating



INFLATIONARY PREHEATING

Physics of (p)REHEATING:
$$\ddot{\varphi}_k + \omega^2(k,t)\varphi_k = 0$$

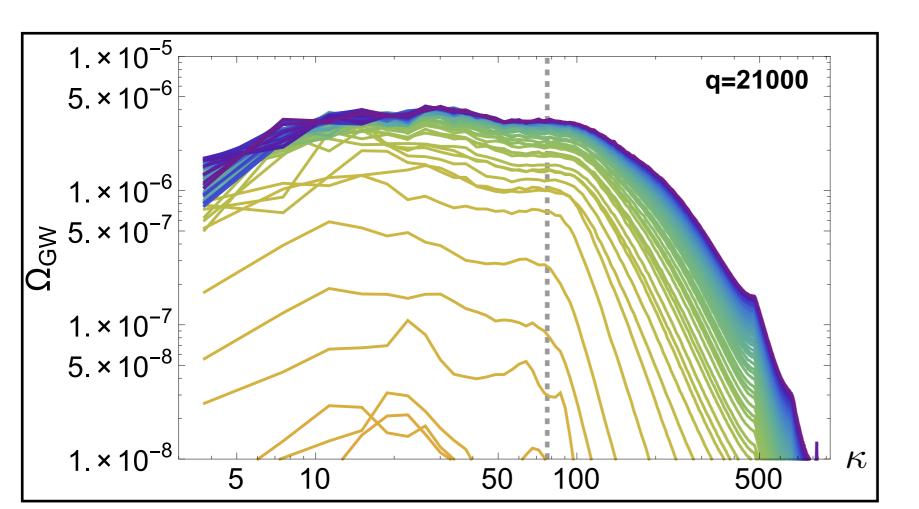
$$\left\{ \begin{array}{ll} \mbox{Hybrid Preheating}: & \omega^2 = k^2 + m^2(1 - V\,t) < 0 & (\mbox{Tachyonic}) \\ \mbox{Chaotic Preheating}: & \omega^2 = k^2 + \Phi^2(t)\sin^2\mu t & (\mbox{Periodic}) \end{array} \right.$$

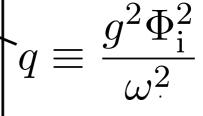
Preheating: Very Effective GW generator!

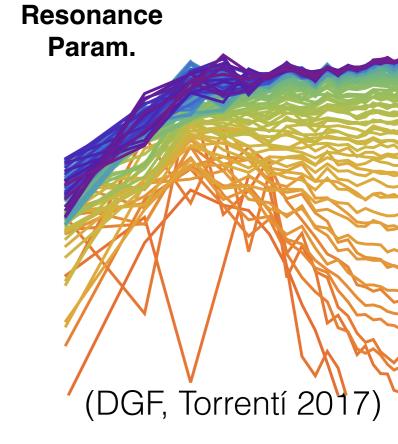
INFLATIONARY PREHEATING











Parameter Dependence (Peak amplitude)

Chaotic Models:
$$\Omega_{\rm GW}^{(o)} \sim 10^{-11} \,, \ @ \ f_o \sim 10^8 - 10^9 \ {\rm Hz}$$

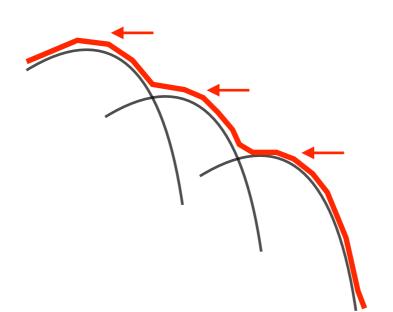
Large amplitude! ... but at high Frequency!

Parameter Dependence (Peak amplitude)

Chaotic Models:
$$\Omega_{\rm GW}^{(o)} \sim 10^{-11} \,, \quad @ \quad f_o \sim 10^8 - 10^9 \,\,{\rm Hz}$$

Large amplitude! ... but at high Frequency!

$$\Omega_{
m GW} \propto q^{-1/2}$$
 — Spectroscopy of particle couplings ?



different couplings ... different peaks?

Parameter Dependence (Peak amplitude)

Chaotic Models:
$$\Omega_{\rm GW}^{(o)} \sim 10^{-11} \,, \ @ \ f_o \sim 10^8 - 10^9 \ {\rm Hz}$$

Large amplitude! ... but at high Frequency!

Very unfortunate... no detectors there!



Parameter Dependence (Peak amplitude)

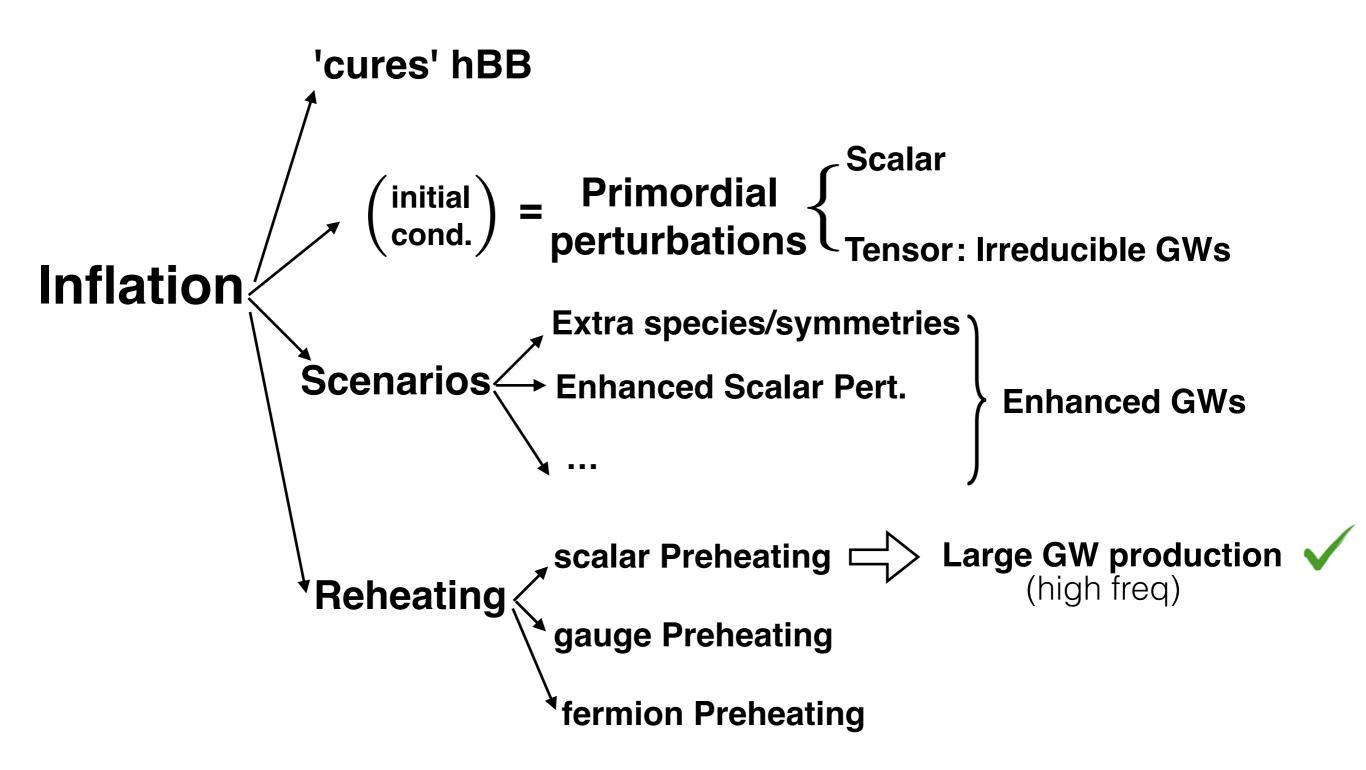
Hybrid Models:
$$\Omega_{
m GW}^{(o)} \propto \left(rac{v}{m_p}
ight)^2 imes f(\lambda,g^2)$$
 , $f_o \sim \lambda^{1/4} imes 10^9~{
m Hz}$

$$\Omega_{\rm GW}^{(o)} \sim 10^{-11} \,, \quad @ \qquad \begin{cases} f_o \sim 10^8 - 10^9 \; \rm Hz \quad 0.1 \\ f_o \sim 10^2 \; \rm Hz \quad 0.1 \end{cases}$$
 Large amplitude !
$$(\text{for } v \simeq 10^{16} \; \rm GeV)$$

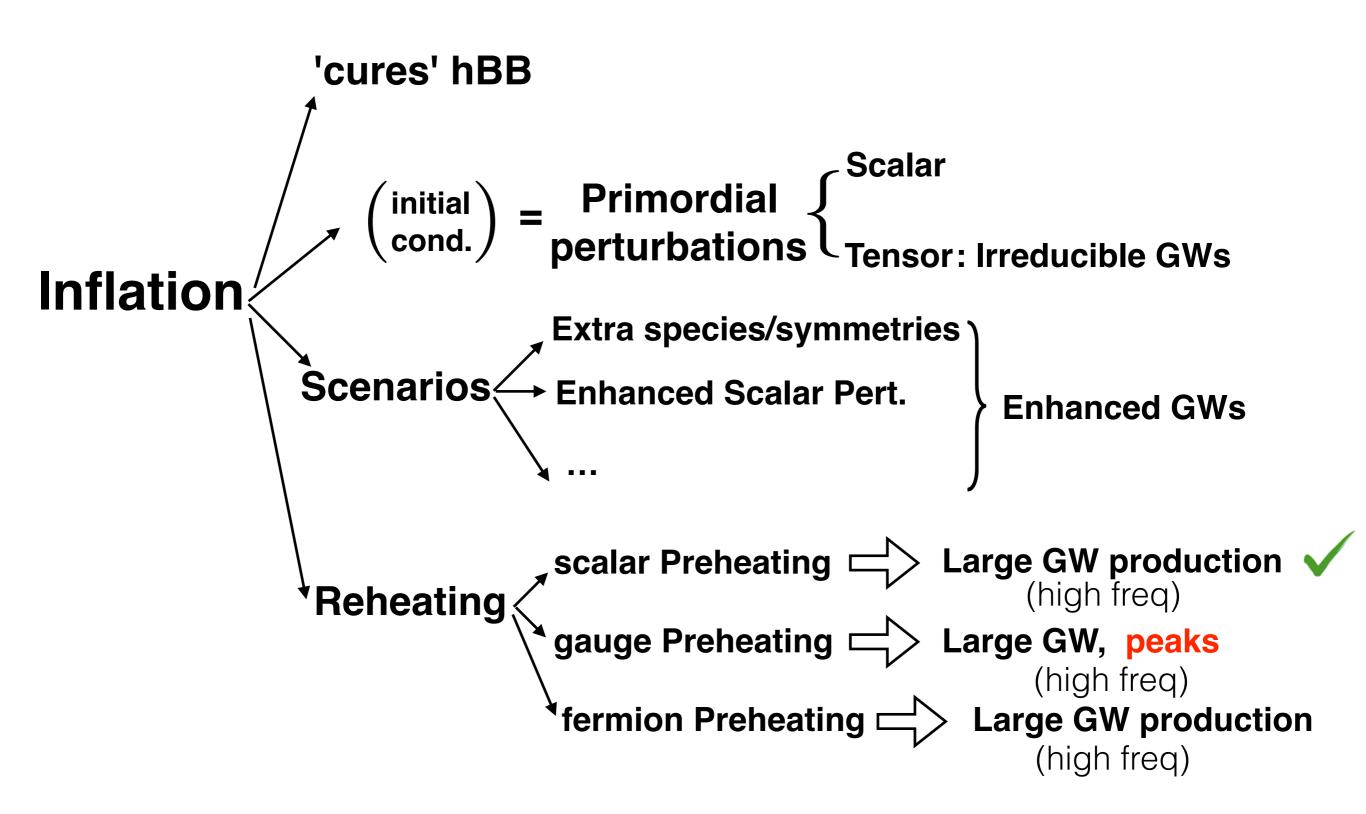
realistically speaking ...



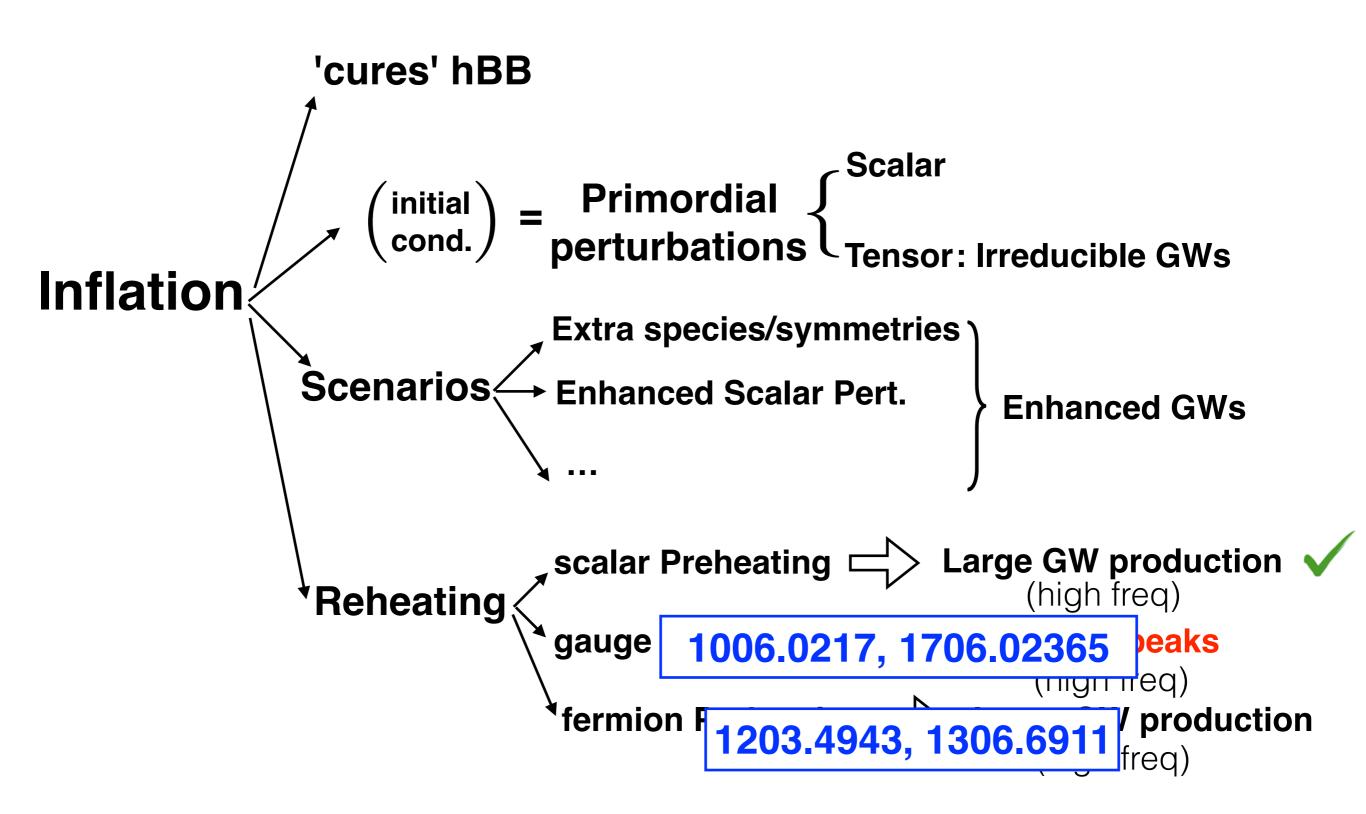
INFLATIONARY COSMOLOGY



INFLATIONARY COSMOLOGY



INFLATIONARY COSMOLOGY



Gravitational Waves as a probe of the early Universe

OUTLINE

0) GW definition <



1) GWs from Inflation



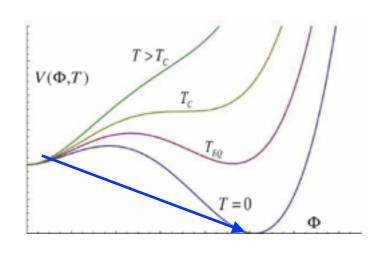
Early Universe

- 2) GWs from Preheating
- 3) GWs from Phase Transitions
- 4) GWs from Cosmic Defects

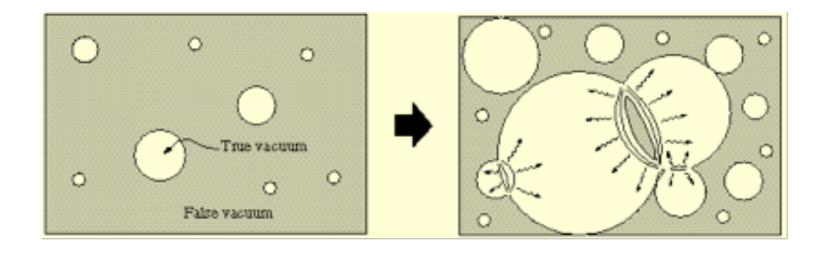
First order phase transitions

Universe expands, T decreases: phase transition triggered!

true and false vacua



quantum tunneling



$$\Pi_{ij} \sim \partial_i \phi \, \partial_j \phi$$
 (Bubble wall collisions)

source: Π_{ij} anisotropic stress

$$\Pi_{ij} \sim \gamma^2 (\rho + p) \, v_i v_j$$
 (Sound waves/Turbulence)

$$\Pi_{ij} \sim \frac{(E^2 + B^2)}{3} - E^i E^j - B^i B^j$$
 (MHD)

What is the freq. in 1st Order PhT's?

$$f_c = f_* \frac{a_*}{a_0} = \frac{2 \cdot 10^{-5}}{\epsilon_*} \frac{T_*}{1 \text{ TeV}} \text{ Hz}$$

GW generation <—> bubbles properties

BUBBLE COLLISIONs

 $\epsilon \simeq \frac{H_*}{\beta} , H_* R_*$

SOUND WAVES & MDH TURBULENCE

$$eta^{-1}$$
 : duration of PhT

$$\beta^{-1}$$
 : duration of PhT
$$v_b \leq 1 \colon \text{speed of bubble walls} \qquad R_* = v_b \, \beta^{-1} \quad \text{size of bubbles at collision}$$

Parameters determining the GW spectrum

$$f_c = f_* \frac{a_*}{a_0} = \frac{2 \cdot 10^{-5}}{\epsilon_*} \frac{T_*}{1 \text{ TeV}} \text{ Hz}$$

Parameter List (not independent)

$$\epsilon \simeq \frac{H_*}{\beta}$$
, $H_* R_*$ $\frac{\beta}{H_*}$, v_b , T_*

$$\frac{\beta}{H_*}$$
, v_b , T_*

$$\Omega_{\text{GW}} \sim \Omega_{\text{rad}} \, \epsilon_*^2 \left(\frac{\rho_{\text{s}}^*}{\rho_{\text{tot}}^*} \right)^2$$

$$\frac{\rho_{\text{s}}^*}{\rho_{\text{vac}}^*} = \frac{\kappa \, \alpha}{1 + \rho}$$

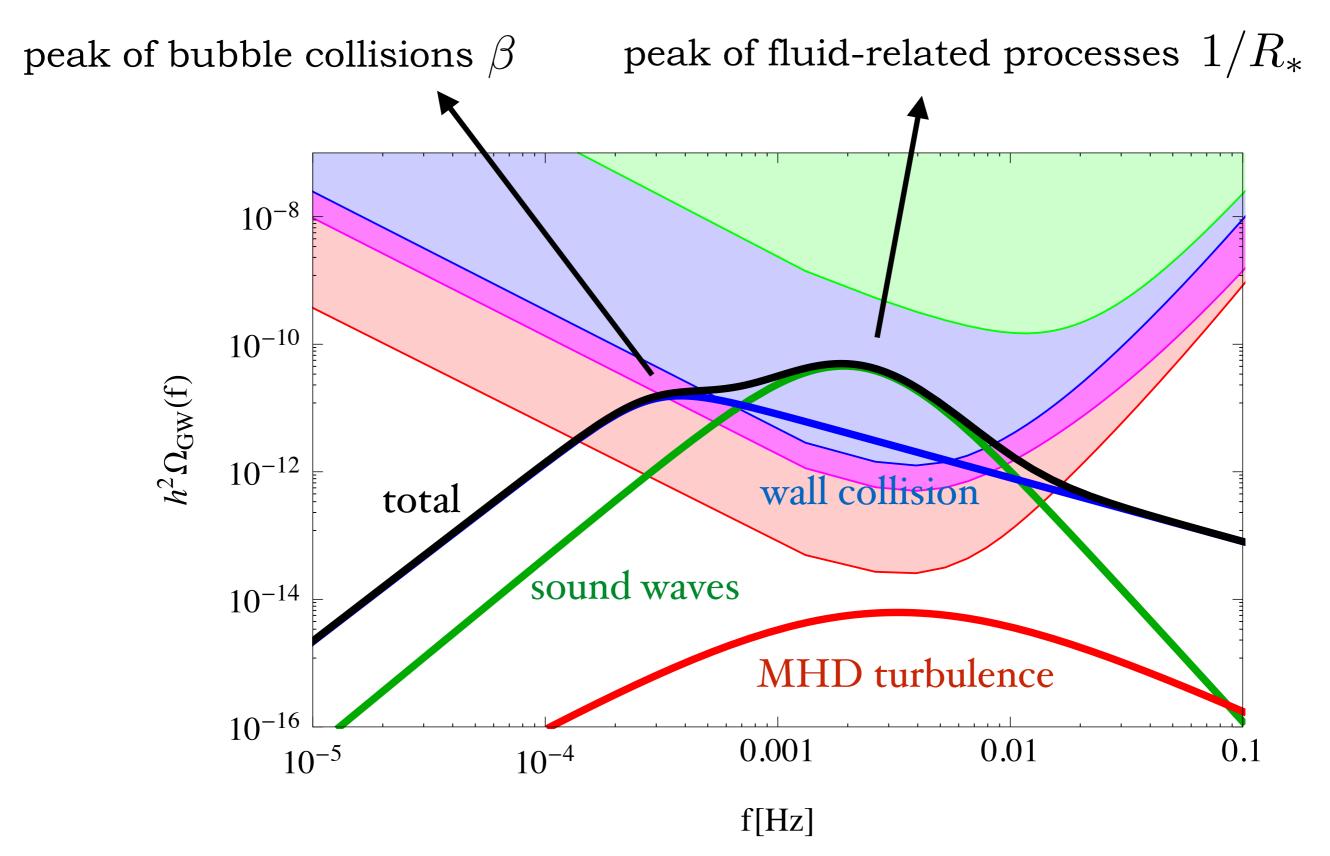
$$\kappa = \frac{\rho_{\text{kin}}}{\rho_{\text{vac}}}$$

$$\frac{\rho_{\rm S}^*}{\rho_{\rm tot}^*} = \frac{\kappa \alpha}{1 + \alpha}$$

$$\alpha = \frac{\rho_{\text{vac}}}{\rho_{\text{rad}}^*}$$

$$\kappa = \frac{\rho_{\mathrm{kin}}}{\rho_{\mathrm{vac}}}$$

Example of spectrum



Caprini et al, arXiv:1512.06239

Evaluation of the signal

• bubble collisions: analytical and numerical simulations
(Huber and Konstandin arXiv:0806.1828)

• **sound waves: numerical** simulations of scalar field and fluid (Hindmarsh et al arXiv:1504.03291)

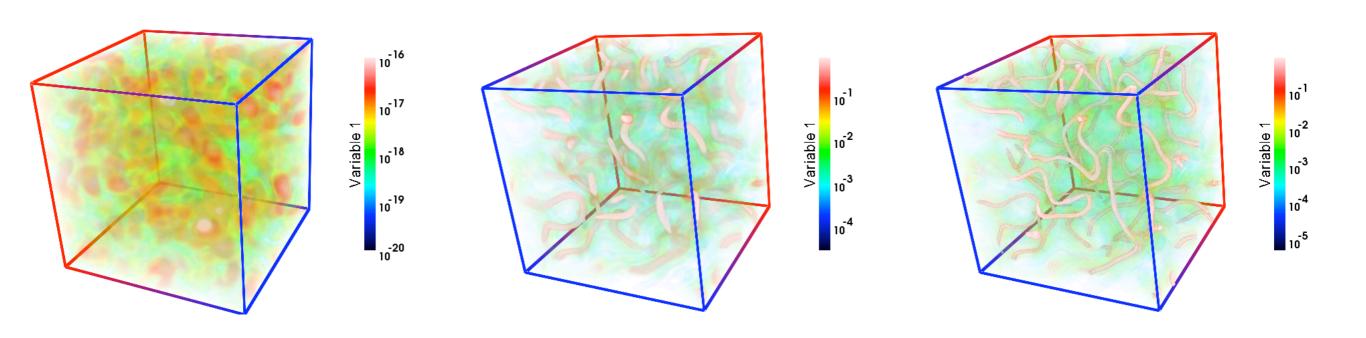
• MDH turbulence: analytical evaluation

(Caprini et al arXiv:0909.0622)

Evaluation of the signal

new probe of BSM physics! bubble collision tions n arXiv:0806.1828) fluid sound (complementary to particle colliders) (iv:1504.03291) MDH turb

What about Cosmic Defects? (aftermath products of a PhT)



U(1) Breaking (after Hybrid Inflation): Mag. Fields Dufaux et al, 2010

Cosmic Defects

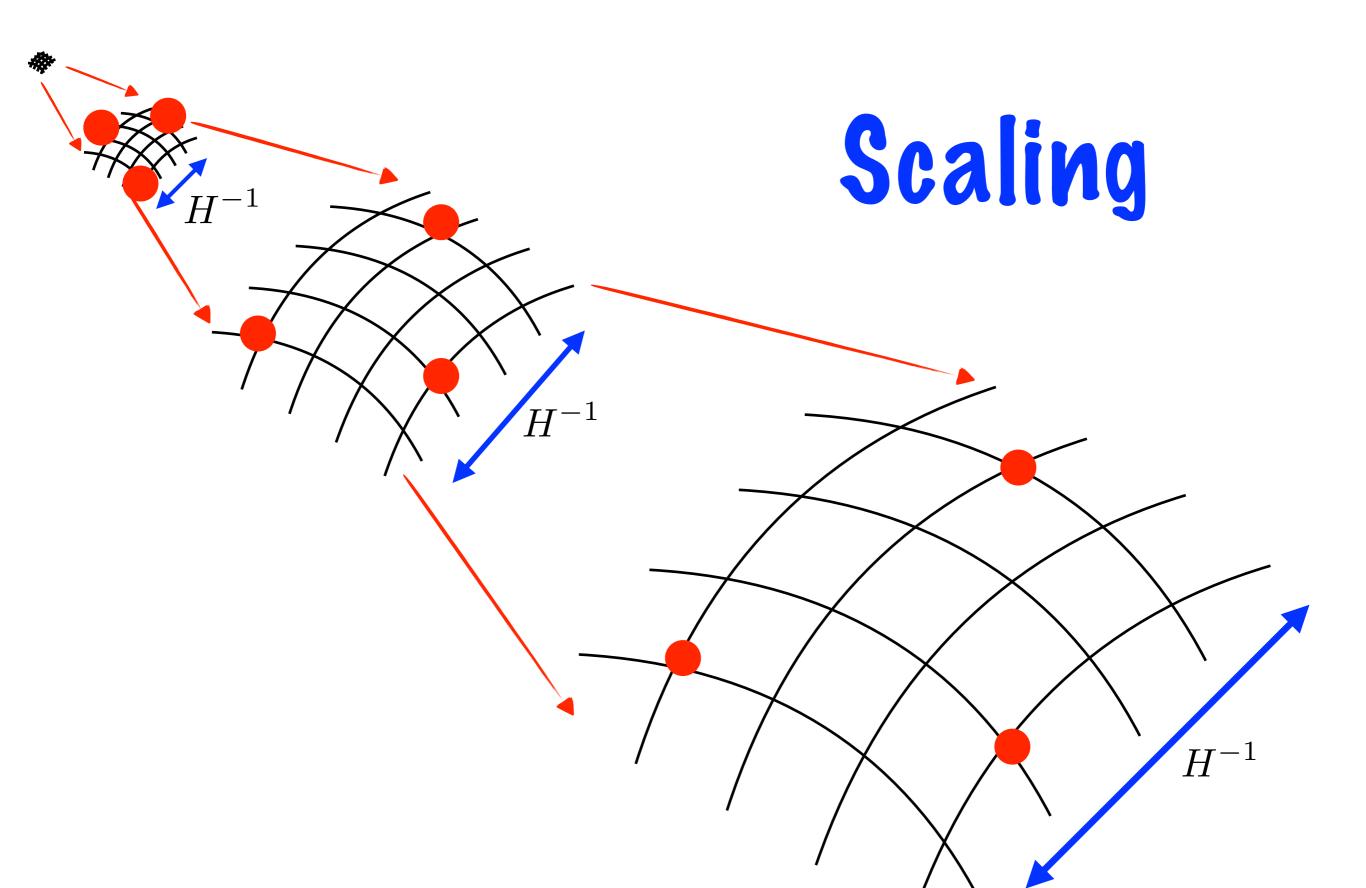
DEFECTS: Aftermath of PhT
$$\rightarrow \left\{ egin{array}{ll} Domain Walls \\ Cosmic Strings \\ Cosmic Monopoles \\ Non-Topological \\ \end{array} \right.$$

CAUSALITY & MICROPHYSICS \Rightarrow Corr. Length: $\xi(t) = \lambda(t) H^{-1}(t)$

(Kibble' 76)

SCALING: $\lambda(t) = \text{const.} \rightarrow \lambda \sim 1$

Cosmic Defects



GWs from a scaling network of cosmic defects

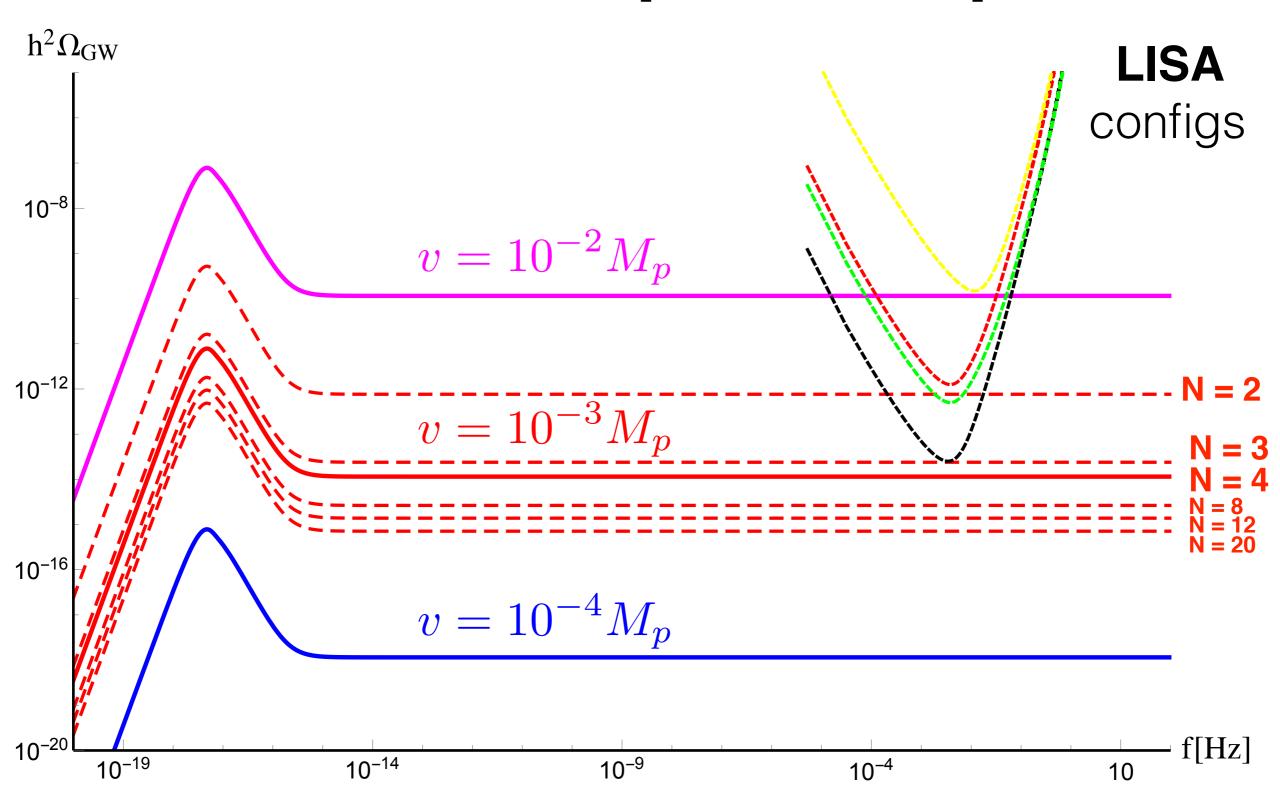
Total GW Spectrum
$$h^2\Omega_{\rm GW}^{\rm (o)}=h^2\Omega_{\rm rad}^{\rm (o)}\left(\frac{V}{M_p}\right)^4\left[F_U^{\rm (R)}+F_U^{\rm (M)}\left(\frac{k_{\rm eq}}{k}\right)^2\right]$$

RD
$$F_U^{(R)} \equiv \frac{32}{3} \int_0^x dx_1 dx_2 \, (x_1 x_2)^{1/2} \cos(x_1 - x_2) \, U_{RD}(x_1, x_2)$$

MD $F_U^{(M)} \equiv \frac{32}{3} \frac{(\sqrt{2} - 1)^2}{2} \int_x^x dx_1 dx_2 \, (x_1 x_2)^{3/2} \cos(x_1 - x_2) \, U_{MD}(x_1, x_2)$

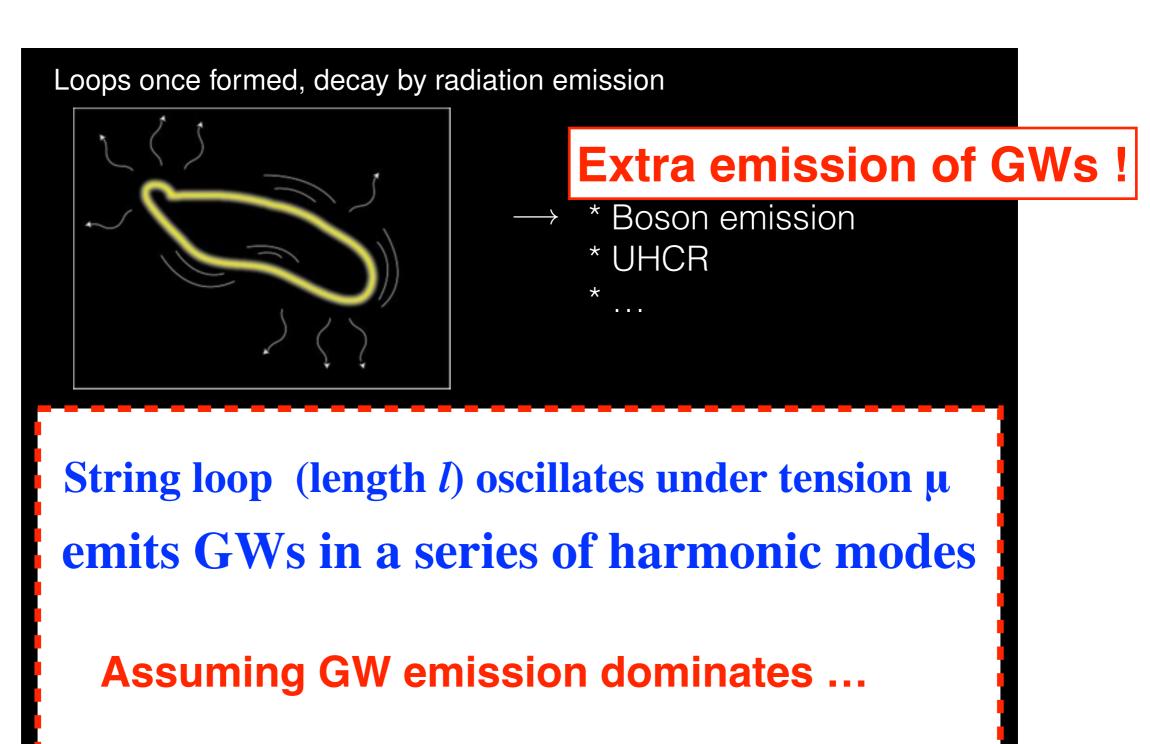
More on GW from Defect Networks

$$h^2 \Omega_{\text{GW}}^{(\text{o})} = h^2 \Omega_{\text{rad}}^{(\text{o})} \left(\frac{V}{M_p} \right)^4 \left[F_U^{(\text{R})} + F_U^{(\text{M})} \left(\frac{k_{\text{eq}}}{k} \right)^2 \right]$$

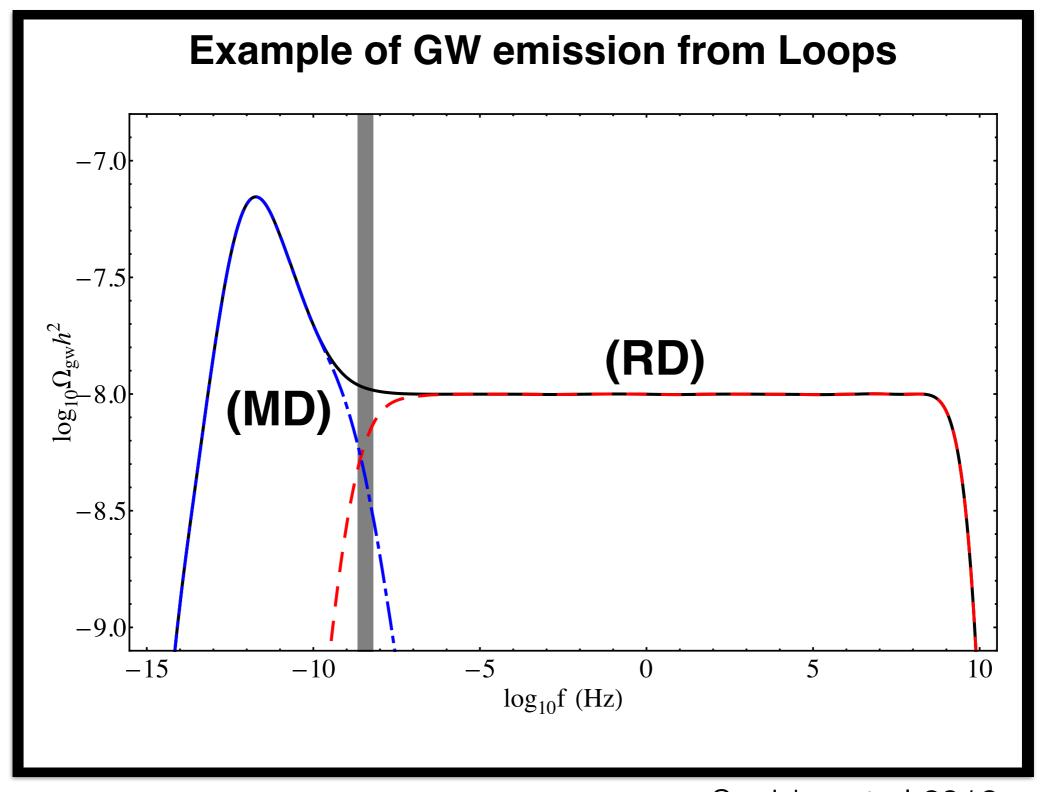


What about if Defects are Cosmic Strings?

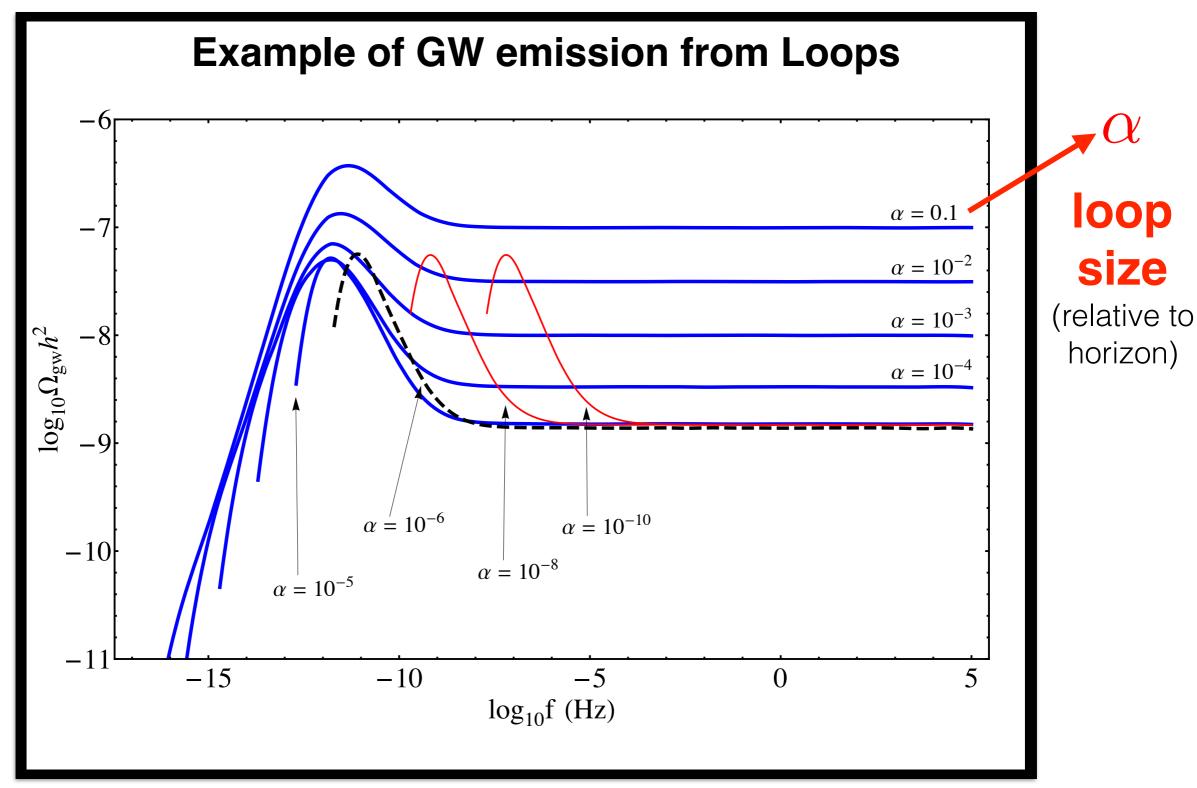
Extra emission of GWs! (Vilenkin '81)



Cosmic Strings Network: Loop configurations



Cosmic Strings Network: Loop configurations



Sanidas et al 2012

loop

size

horizon)

Cosmic Strings Network: Loop configurations

Results for 6 links, SNR=20

LISA Prospects

A1M2

Conservative limit: $G\mu/c^2 < 4.4 \times 10^{-10}$ Large loops: $G\mu/c^2 < 1.5 \times 10^{-16}$

A2M2

Conservative limit: $G\mu/c^2 < 1.1 \times 10^{-10}$ Large loops: $G\mu/c^2 < 2.1 \times 10^{-17}$

A2M5

Conservative limit: $G\mu/c^2 < 7.0 \times 10^{-11}$ Large loops: $G\mu/c^2 < 1.3 \times 10^{-17}$

A5M5

Conservative limit: $G\mu/c^2 < 1.4 \times 10^{-11}$ Large loops: $G\mu/c^2 < 4.4 \times 10^{-18}$ $\rightarrow v \lesssim 10^{10} GeV$

(From Sanidas et al, LISA GW cosmology 3rd encounter)

Gravitational Waves as a probe of the early Universe

SUMMARY

0) GW definition <



1) GWs from Inflation

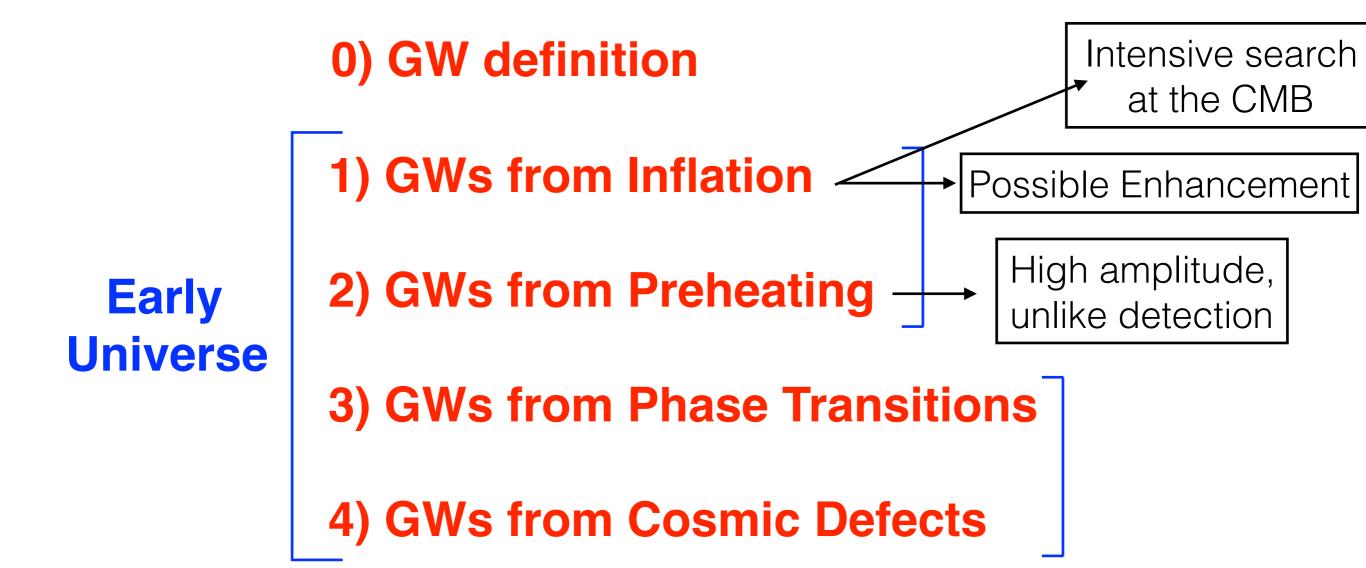
Early Universe

- 2) GWs from Preheating
- 3) GWs from Phase Transitions
- 4) GWs from Cosmic Defects



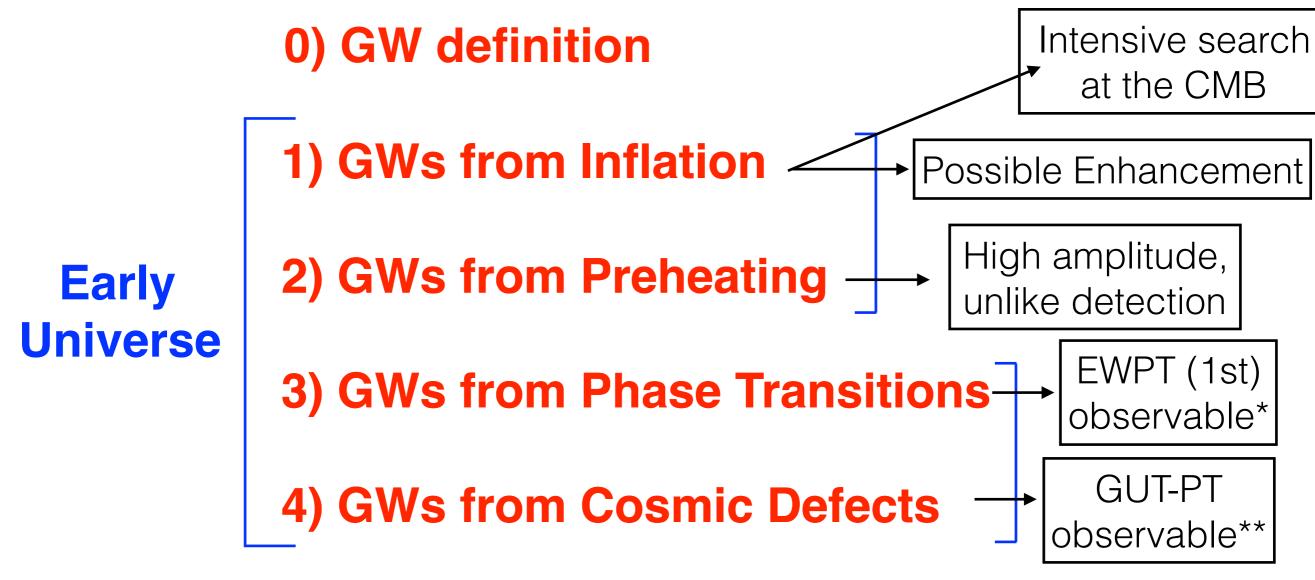
Gravitational Waves as a probe of the early Universe

SUMMARY



Gravitational Waves as a probe of the early Universe

SUMMARY



Propaganda, Part I

Review on Cosmological Gravitational Wave Backgrounds

Caprini & Figueroa arXiv:1801.04268

Propaganda, Part II

Almost Nothing

Première Sept 28th 2018, @ CERN Globe



Cảm ơn bạn rất nhiều vì sự chú ý của bạn!