



# Measurements of lepton flavor non-universality in B decays at Belle

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*for the Belle Collaboration*

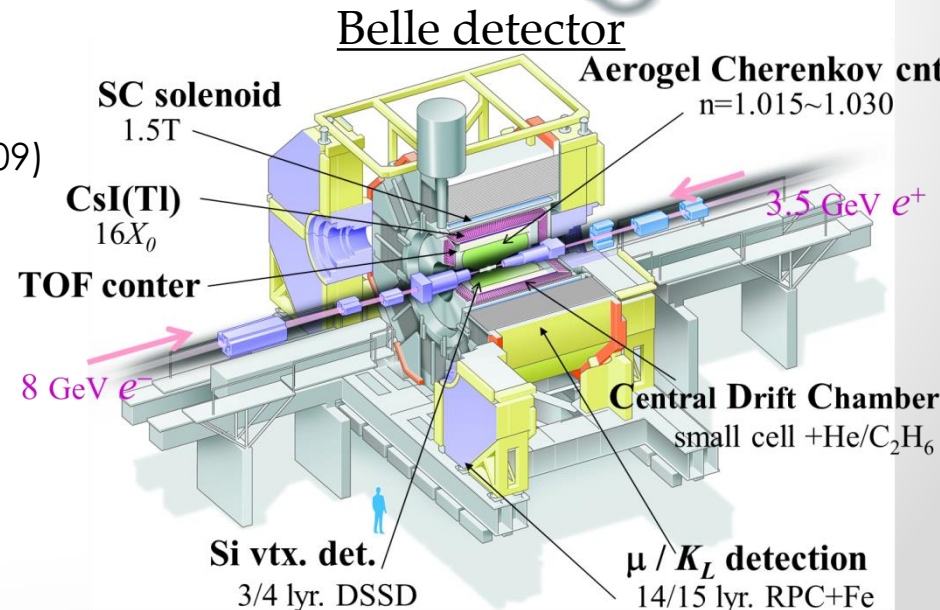
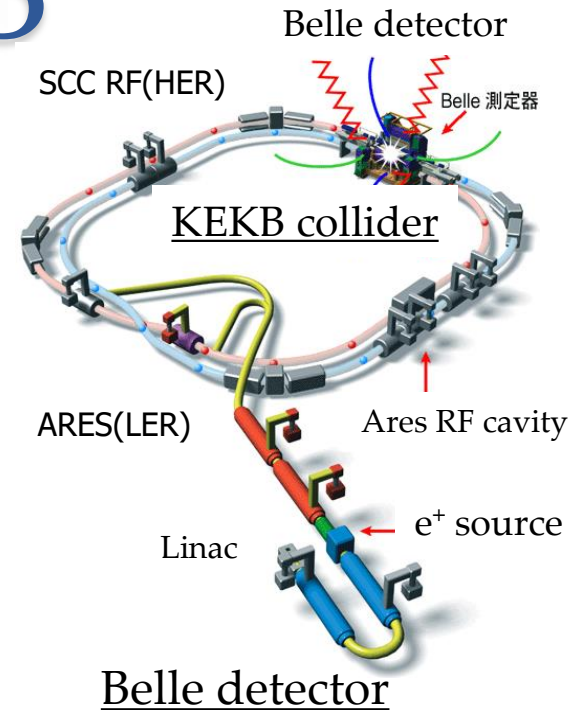
Aug. 8, 2018

25<sup>th</sup> Anniversary of the Rencontres du Vietnam

# Outline

- $R(D)$  and  $R(D^*)$  measurement with  $B \rightarrow D^{(*)} \tau \nu$
- Test of lepton universality in  $B \rightarrow K^* \ell \ell$
- Search for Lepton flavor violating decay  $B \rightarrow K^* \mu e$

# Belle and KEKB

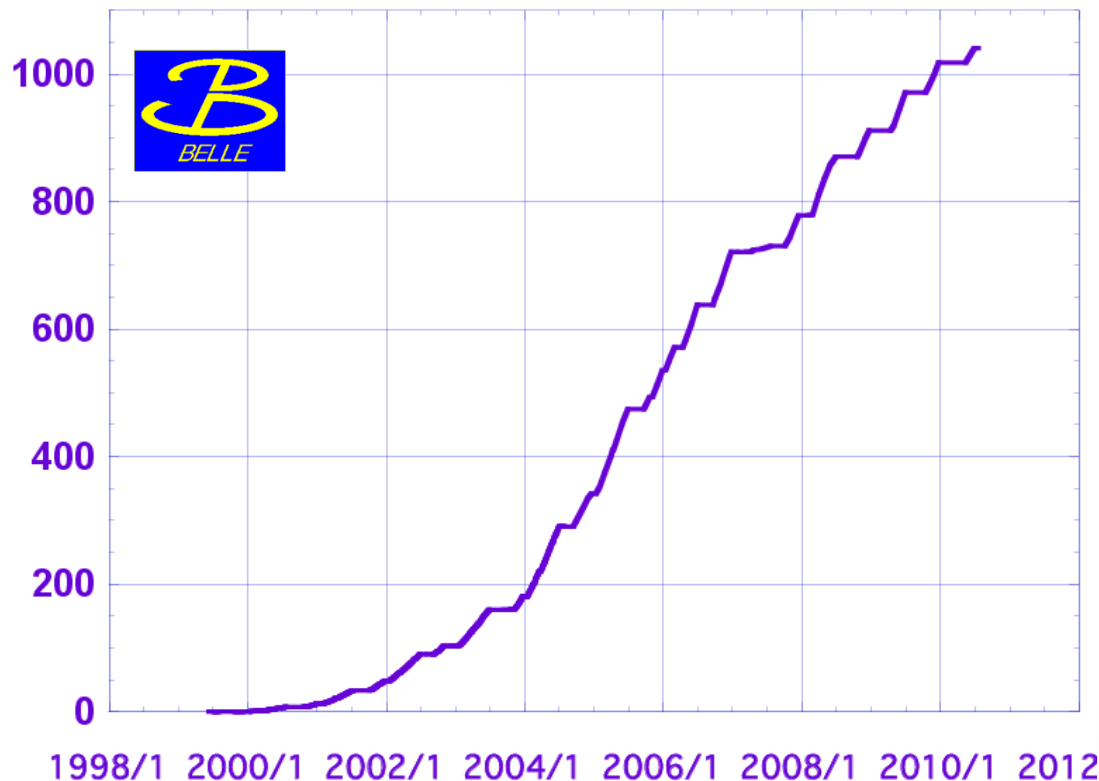


- KEKB
  - Achieved World Highest Luminosity (as of 2009)
    - $L = 2.1 \cdot 10^{34} / \text{cm}^2/\text{sec} \sim 20 \overline{B\overline{B}}$  pairs / sec
  - Asymmetric energy to boost B mesons
    - $8.0\text{GeV } e^- \times 3.5\text{GeV } e^+$
- Belle
  - Multi-purpose  $4\pi$  detector
  - Vertexing, tracking, EM calorimeter, PID
- Data taking for 1999-2010

# Belle Integrated Luminosity

- The world largest integrated luminosity of  $> 1 \text{ ab}^{-1}$
- $711 \text{ fb}^{-1}$  on  $Y(4S)$  resonance  $\rightarrow$   **$772 \times 10^6 \text{ BB pairs}$**

Integrated Luminosity[fb<sup>-1</sup>]



**On resonance:**

Y(5S): 121 fb<sup>-1</sup>

Y(4S): 711 fb<sup>-1</sup>

Y(3S): 3 fb<sup>-1</sup>

Y(2S): 25 fb<sup>-1</sup>

Y(1S): 6 fb<sup>-1</sup>

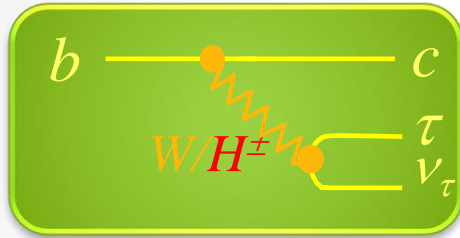
**Off reson./scan:**

~100 fb<sup>-1</sup>

# Semi-tauonic B decay:



- Sensitive to new physics



Ratio of  $\tau$  to  $\mu, e$  could be reduced/enhanced

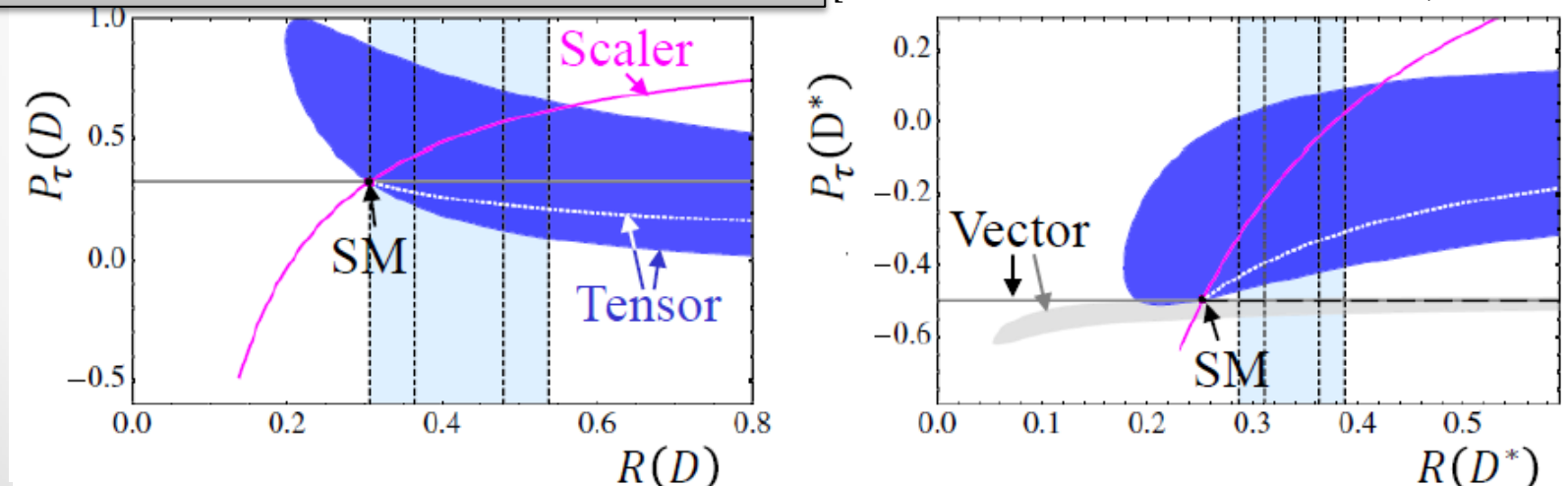
$$R(D^{(*)}) = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \nu)}{\mathcal{B}(B \rightarrow D^{(*)} \ell \nu)}$$

Polarization of tau could probe the NP model

$$P_{\tau}(D^{(*)}) = \frac{\Gamma^{+} - \Gamma^{-}}{\Gamma^{+} + \Gamma^{-}}$$

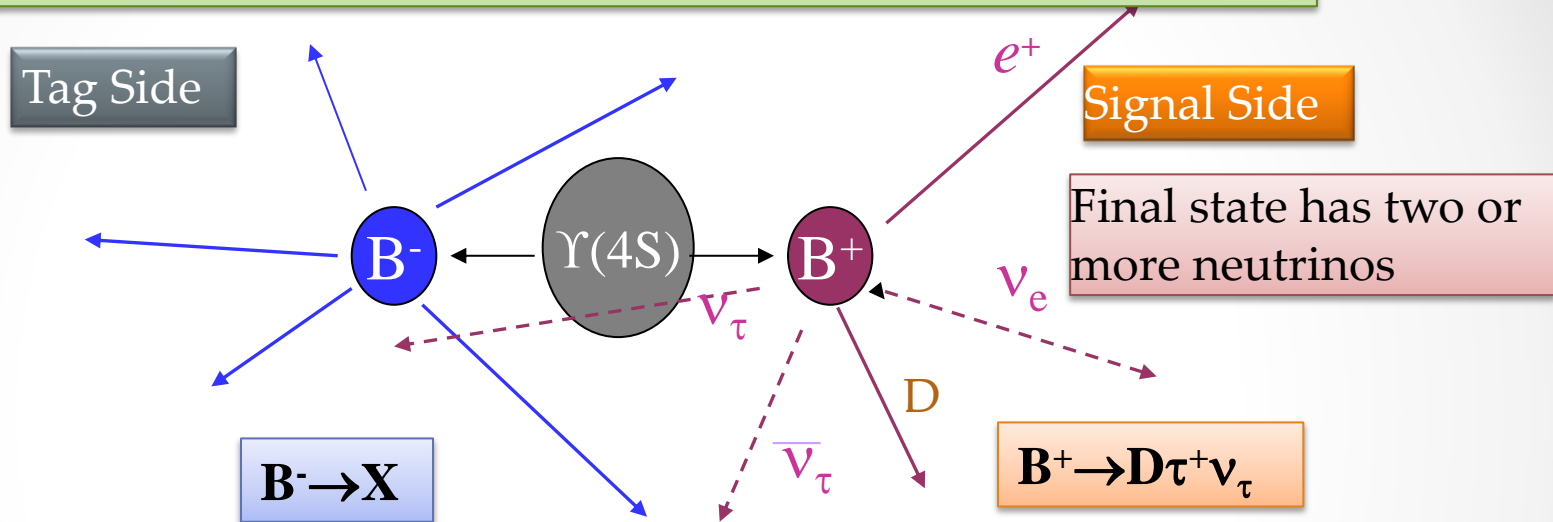
NP model (vector, scalar, tensor) dependence

[M. Tanaka and R. Watanabe PRD 87, 034028 (2013)]



# B → D(\*)τν Analysis at Belle

Utilize the B factory specific feature :  
only one B-meson pair is produced

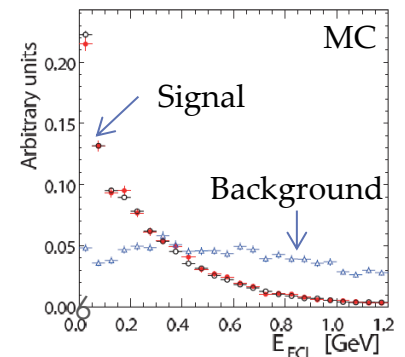


Tag B pair event by reconstructing one B meson in hadronic or semileptonic B Decay

→ Provide pure single B event

Require no particle remains after removing products of tagging B and the particle(s) from signal decays

← Remaining energy in the calorimeter ( $E_{ECL}$ )



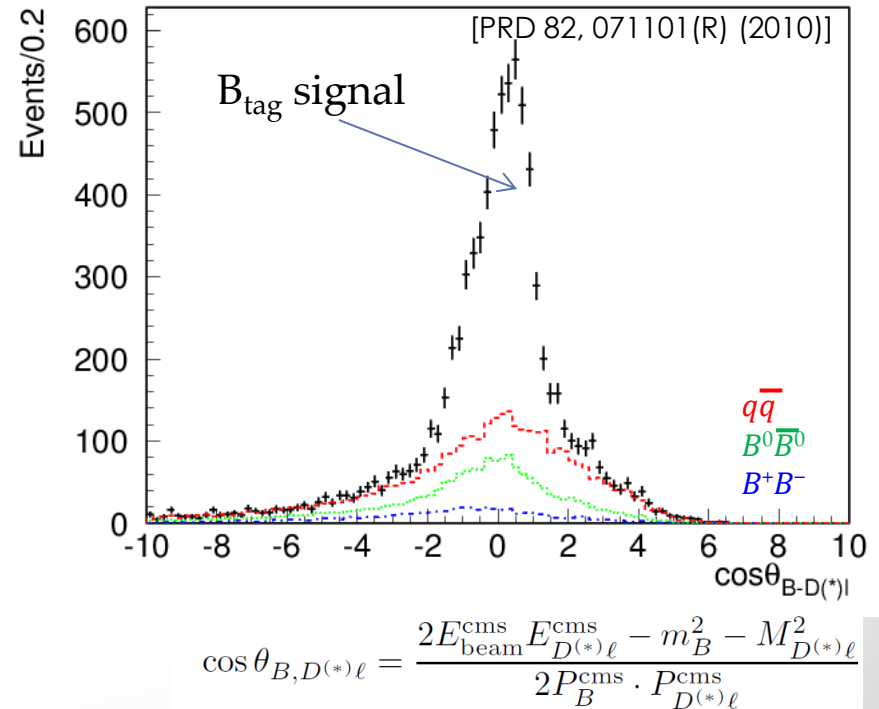
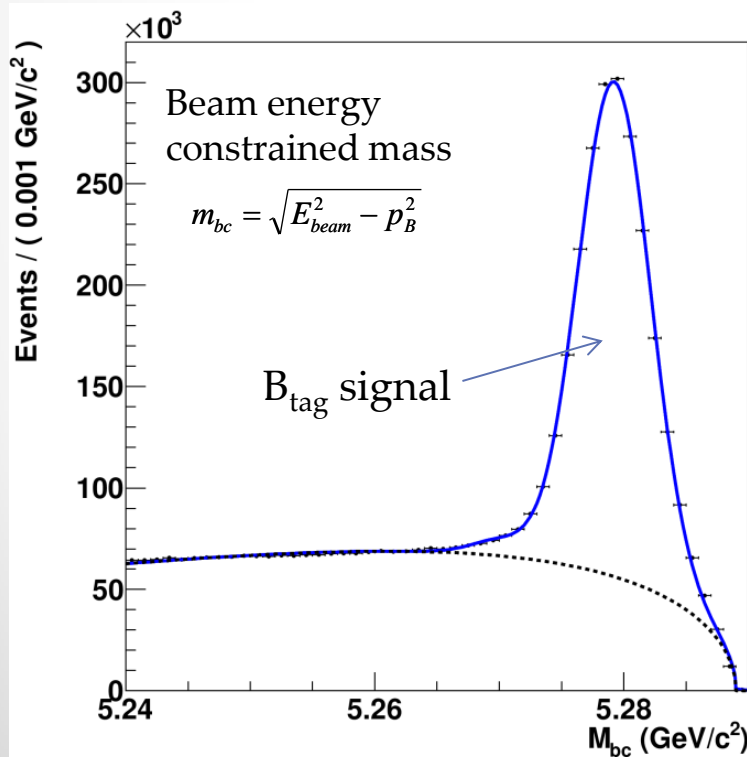
# Tagging Methods

## Hadronic Tag

- Fully reconstruct in  $B \rightarrow DX$  decays
  - ~1100 exclusive decay channels  
[NIM A 654, 432 (2011)]
- Tagging efficiency ~ 0.2 %
- Less background

## Semileptonic Tag

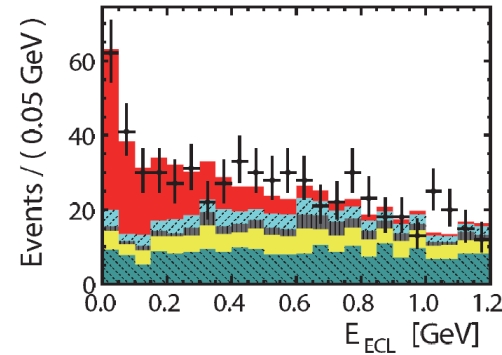
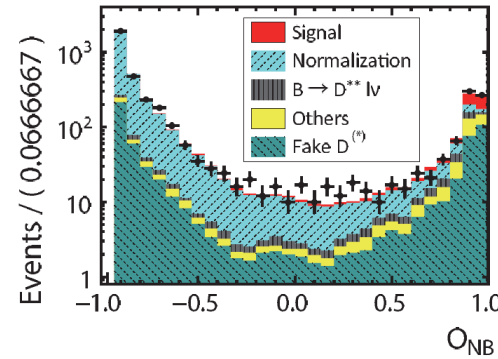
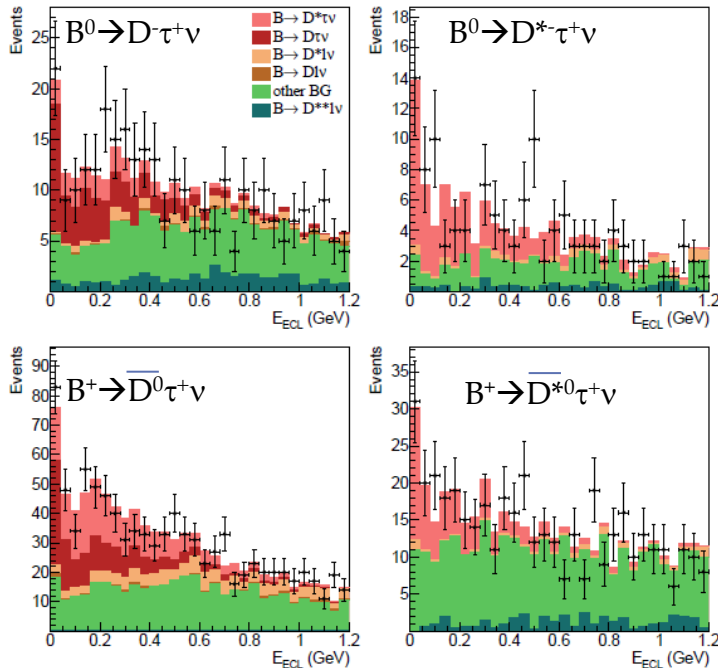
- Reconstruct  $B \rightarrow D^{(*)}l\nu$ 
  - $E_B = E_{\text{beam}}$
  - Undetected neutrino mass  $\sim 0$
- Tagging efficiency ~ 0.5%
- More background



# Results with leptonic tau decays

## Hadronic Tag [PRD92,072014(2015)]

## Semileptonic Tag [PRD94,072007(2016)]



$$\mathcal{R}(D^*) = 0.302 \pm 0.030 \pm 0.011$$

Consistent with, but higher than the SM predictions:  
 $R(D) = 0.299 \pm 0.003$   
 $R(D^*) = 0.258 \pm 0.005$   
 [SM average of HFLAV Summer 2018]

$$R(D) = 0.375 \pm 0.064 \pm 0.026$$

$$R(D^*) = 0.293 \pm 0.038 \pm 0.015$$



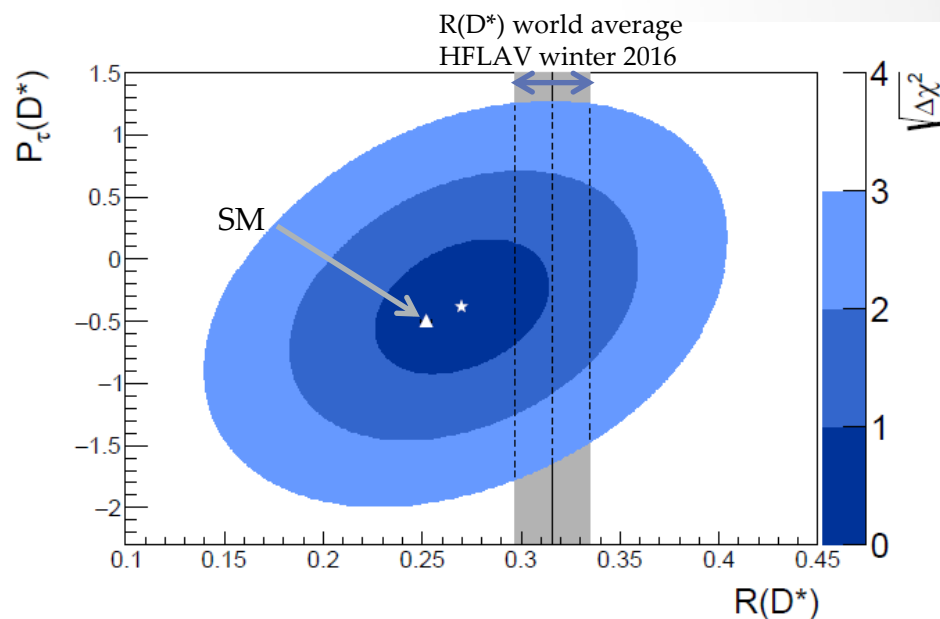
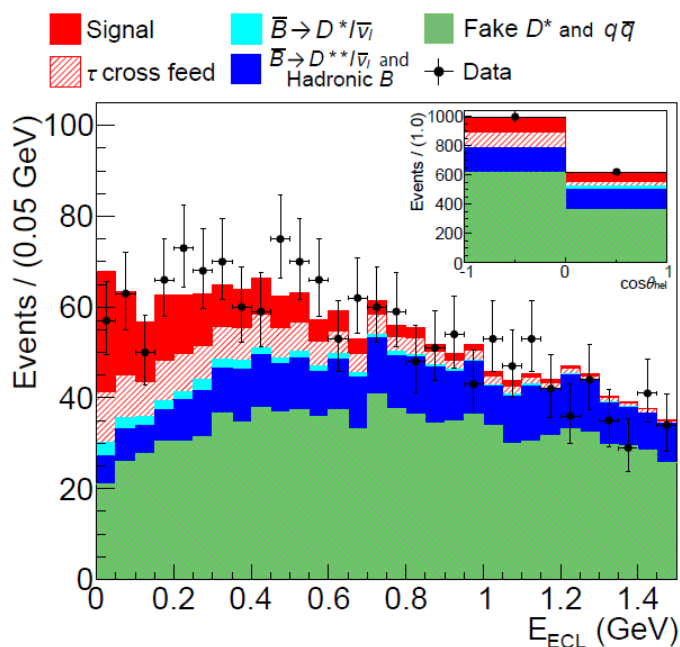
# Results of Polarization Measurement

- Hadronic tag
- Two body tau decays :  $\tau \rightarrow \pi \nu, \rho \nu$ 
  - Helicity angle sensitive to the tau polarization

[PRL118, 211801 (2017) PRD97, 012004 (2018)]

$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta_{\text{hel}}} = \frac{1}{2} (1 + \alpha \cdot \mathcal{P}_\tau \cos \theta_{\text{hel}})$$

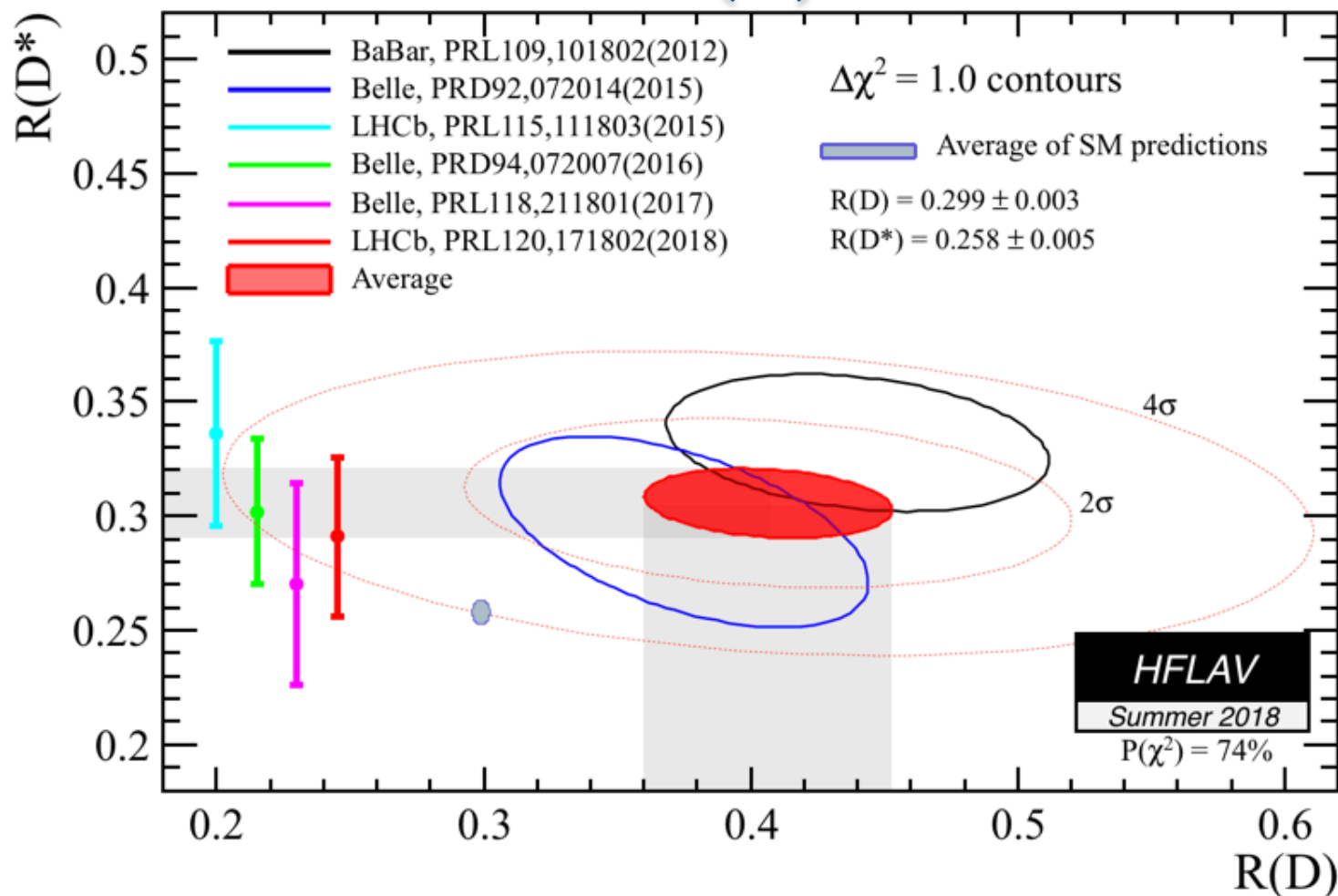
$$\alpha = \begin{cases} 1 & \text{for } \tau \rightarrow \pi^- \nu \\ 0.45 & \text{for } \tau \rightarrow \rho^- \nu \end{cases}$$



$$R(D^*) = 0.270 \pm 0.035(\text{stat})_{-0.025}^{+0.028}(\text{syst}),$$

$$P_\tau(D^*) = -0.38 \pm 0.51(\text{stat})_{-0.16}^{+0.21}(\text{syst}),$$

# Current $B \rightarrow D(^*)\tau\nu$ Situation

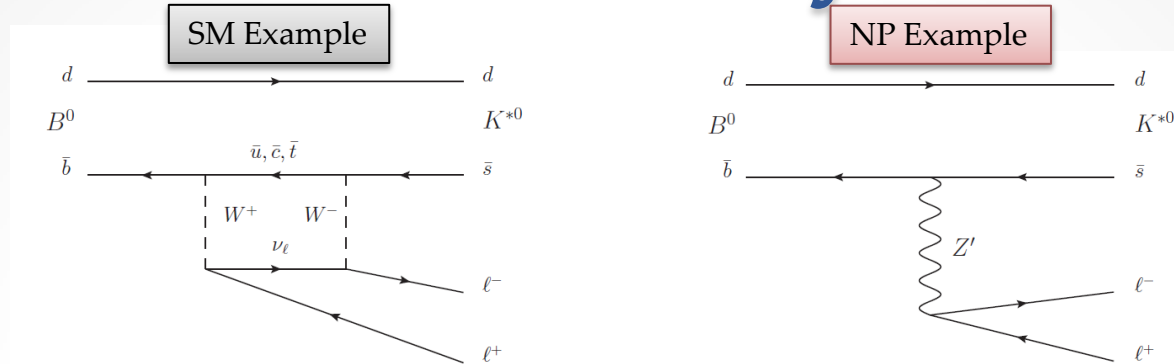


3.8  $\sigma$  deviation from the SM prediction !

Additional Belle results will come soon

Belle II has started  $\rightarrow$  Significant improvement in near future

# Lepton Universality in $B \rightarrow K^* \ell \ell$



- LHCb reported 2.6  $\sigma$  tension in

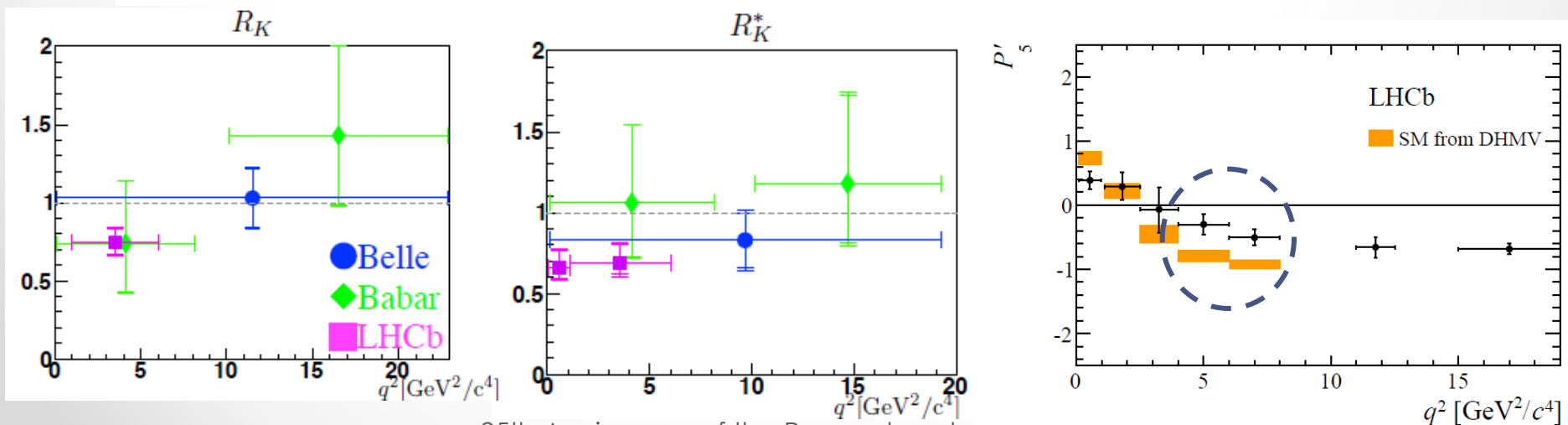
[PRL 113,151601(2014), JHEP 08(2017), 055]

$$R_K \equiv \frac{\mathcal{B}(B \rightarrow K^+ \mu^+ \mu^-)}{\mathcal{B}(B \rightarrow K^+ e^+ e^-)} \quad R_K^* \equiv \frac{\mathcal{B}(B \rightarrow K^* \mu^+ \mu^-)}{\mathcal{B}(B \rightarrow K^* e^+ e^-)}$$

- also in angular observable

[JHEP 02(2016), 104]

$$P'_{i=4,5,6,8} = \frac{S_{j=4,5,7,8}}{\sqrt{F_L(1-F_L)}} \quad \frac{1}{d\Gamma/dq^2} \frac{d^4\Gamma}{d\cos\theta_L d\cos\theta_K d\phi dq^2} : \theta_K, \theta_L, \phi, F_L, S_i$$

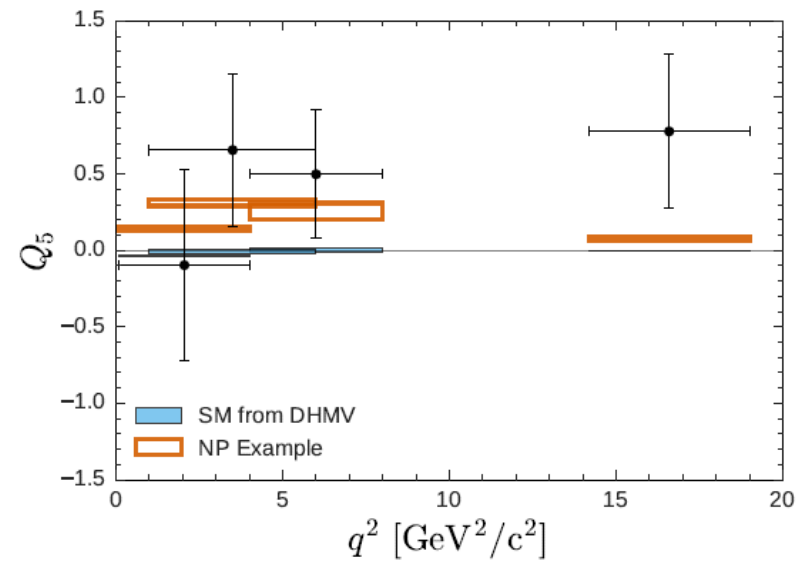
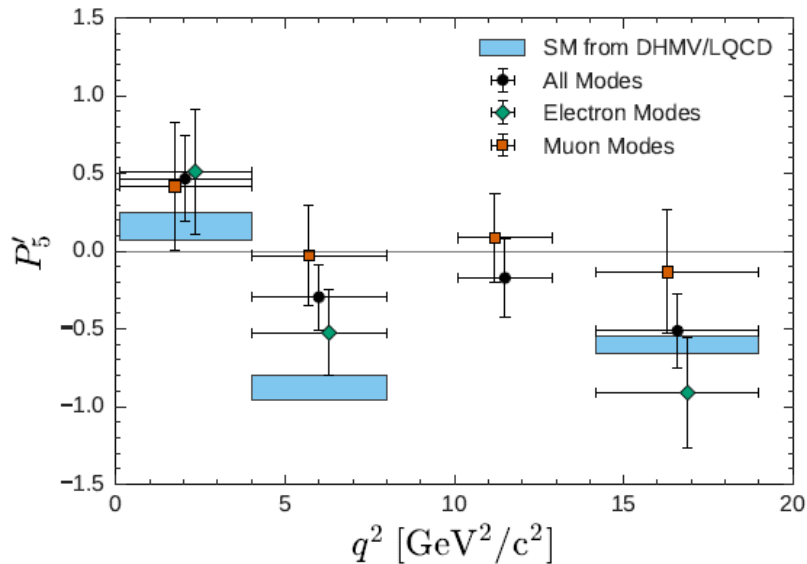
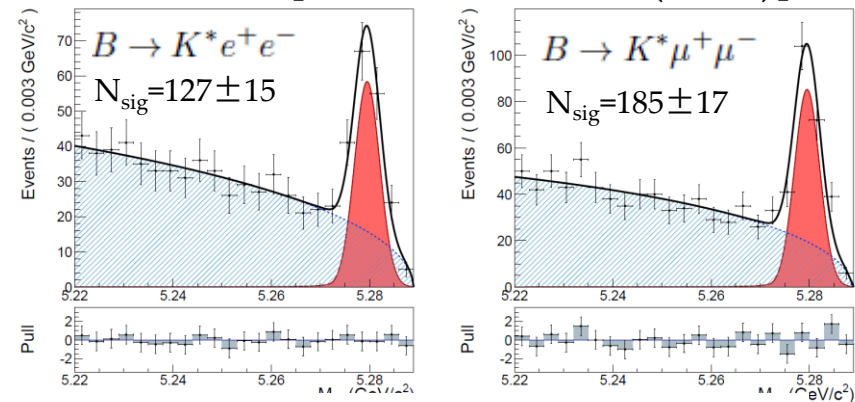


# B → K\*ll Angular Analysis Results

[PRL118, 111801 (2017)]

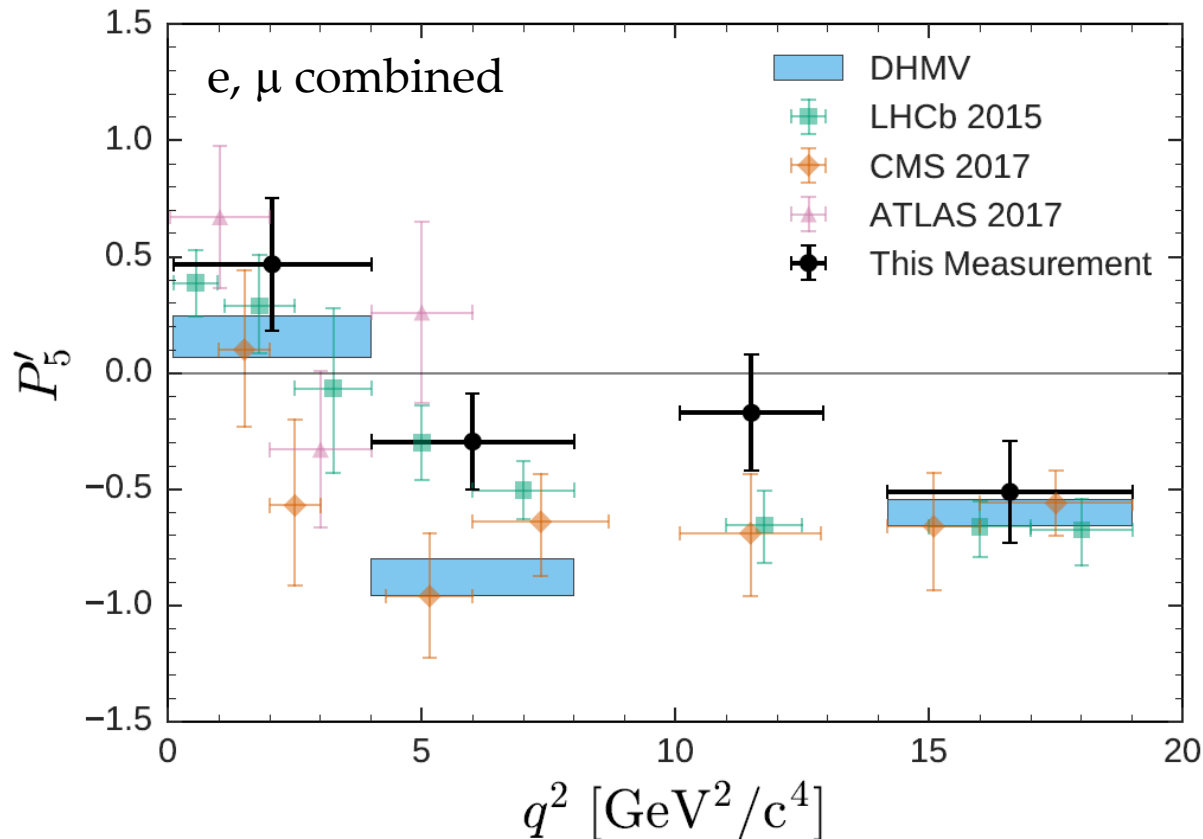
- B → K\*μμ, K\*ee reconstructed with Belle full data
- Angular analysis performed in four bins to obtain angular observables
  - $P'_i$
  - the difference between the lepton flavors

$$Q_i = P_i^\mu - P_i^e$$



Largest deviation in  $P'_5$  of muon mode with  $2.6\sigma$

# Comparison with other measurements

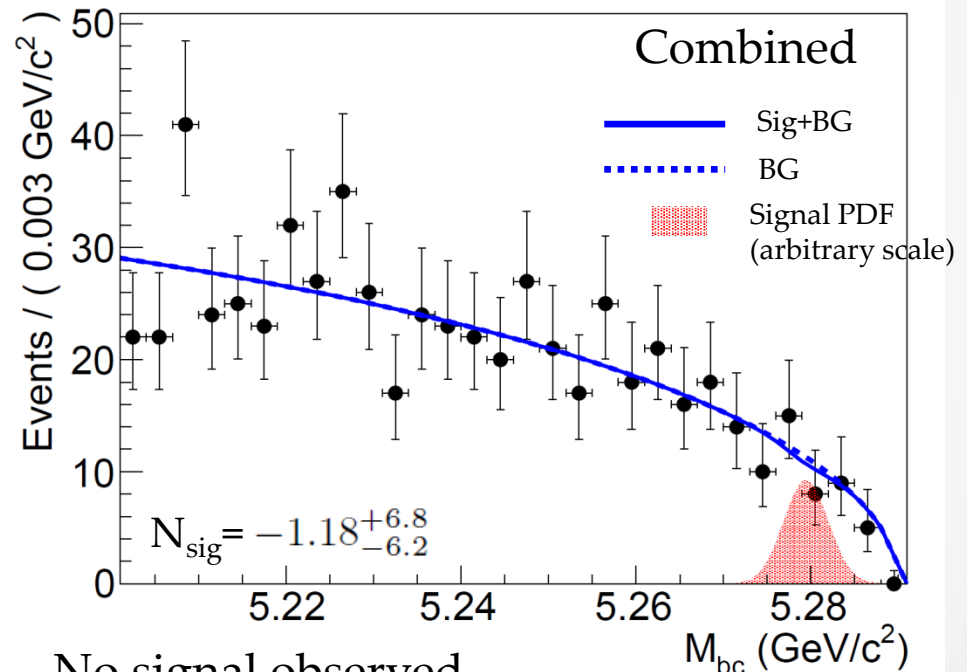
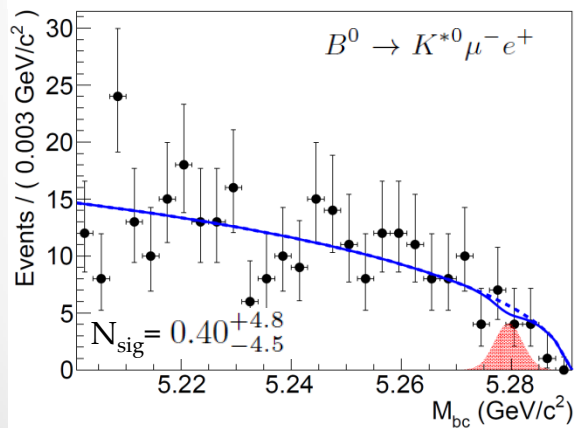
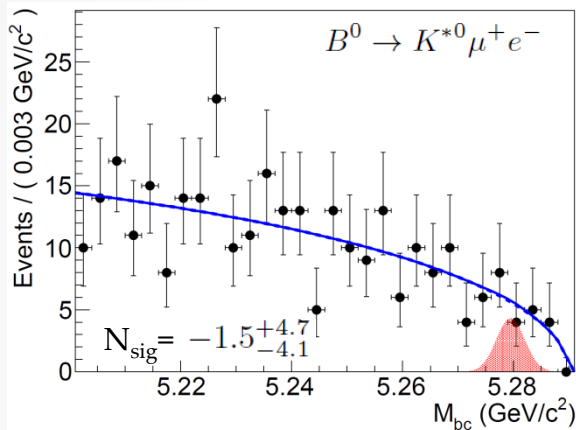


- Measurements are compatible with the SM
- Similar central values for the  $P'_5$  anomaly with  $2.5s$  tension

# Search for lepton flavor violating decay $B^0 \rightarrow K^{*0} \mu e$

- 2018 New Belle Result with 772M  $B\bar{B}$**

[arXiv:1807.03267 submitted to PRD]



No signal observed

Set most stringent limit of these decays

$$B(B^0 \rightarrow K^{*0} \mu^+ e^-) < 1.2 \times 10^{-7}$$

$$B(B^0 \rightarrow K^{*0} \mu^- e^+) < 1.6 \times 10^{-7}$$

$$B(B^0 \rightarrow K^{*0} \mu^\pm e^\mp) < 1.8 \times 10^{-7}$$

# Summary

- Belle measured lepton universality using the data sample of the world largest luminosity
- **Tensions from the SM** exist in the measurements of  $B \rightarrow D^{(*)} \tau \nu$  and  $B \rightarrow K^* \ell \ell$
- New search for the LFV decay  $B \rightarrow K^* \mu e$  has been performed and set the most stringent limits
- Still need more results to be conclusive
  - Still some more analyses on going at Belle
  - Significant improvement from BelleII in near future





# B → D(\*)τν Systematic Errors

## Hadronic Tag

TABLE IV. Overview of relative systematic uncertainties in percent. The last column gives the correlation between  $R(D)$  and  $R(D^*)$ .

	$R(D)$ [%]	$R(D^*)$ [%]	Correlation
$D^{(*)}\ell\nu$ shapes	4.2	1.5	0.04
$D^{**}$ composition	1.3	3.0	-0.63
Fake $D$ yield	0.5	0.3	0.13
Fake $\ell$ yield	0.5	0.6	-0.66
$D_s$ yield	0.1	0.1	-0.85
Rest yield	0.1	0.0	-0.70
Efficiency ratio $f^{D^+}$	2.5	0.7	-0.98
Efficiency ratio $f^{D^0}$	1.8	0.4	0.86
Efficiency ratio $f_{\text{eff}}^{D^{*+}}$	1.3	2.5	-0.99
Efficiency ratio $f_{\text{eff}}^{D^{*0}}$	0.7	1.1	0.94
CF double ratio $g^+$	2.2	2.0	-1.00
CF double ratio $g^0$	1.7	1.0	-1.00
Efficiency ratio $f_{\text{wc}}$	0.0	0.0	0.84
$M_{\text{miss}}^2$ shape	0.6	1.0	0.00
$o_{\text{NB}}$ shape	3.2	0.8	0.00
Lepton PID efficiency	0.5	0.5	1.00
Total	7.1	5.2	-0.32

## Semileptonic Tag

TABLE I. Summary of the systematic uncertainties on  $\mathcal{R}(D^*)$  for electron and muon modes combined and separated. The uncertainties are relative and are given in percent.

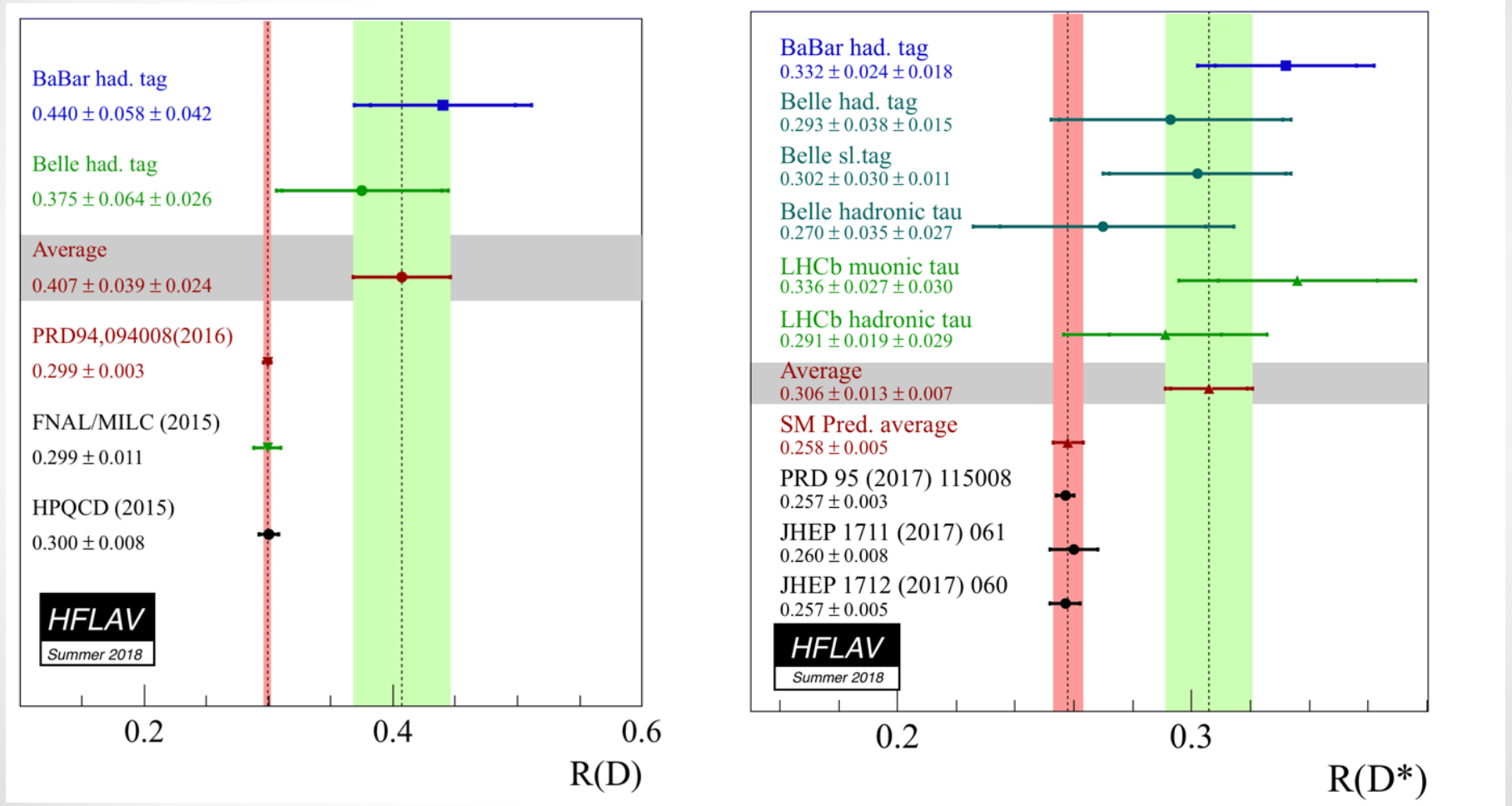
Sources	$\mathcal{R}(D^*)$ [%]		
	$\ell^{\text{sig}} = e, \mu$	$\ell^{\text{sig}} = e$	$\ell^{\text{sig}} = \mu$
MC size for each PDF shape	2.2	2.5	3.9
PDF shape of the normalization in $\cos\theta_{B-D^*\ell}$	+1.1	+2.1	+2.8
	-0.0	-0.0	-0.0
PDF shape of $B \rightarrow D^{**}\ell\nu$	+1.0	+0.7	+2.2
	-1.7	-1.3	-3.3
PDF shape and yields of fake $D^{(*)}$	1.4	1.6	1.6
PDF shape and yields of $B \rightarrow X_c D^*$	1.1	1.2	1.1
Reconstruction efficiency ratio $\varepsilon_{\text{norm}}/\varepsilon_{\text{sig}}$	1.2	1.5	1.9
Modeling of semileptonic decay	0.2	0.2	0.3
$\mathcal{B}(\tau^- \rightarrow \ell^- \bar{\nu}_\ell \nu_\tau)$	0.2	0.2	0.2
Total systematic uncertainty	+3.4	+4.1	+5.9
	-3.5	-3.7	-5.8

## Hadronic Tag, hadronic tau decay

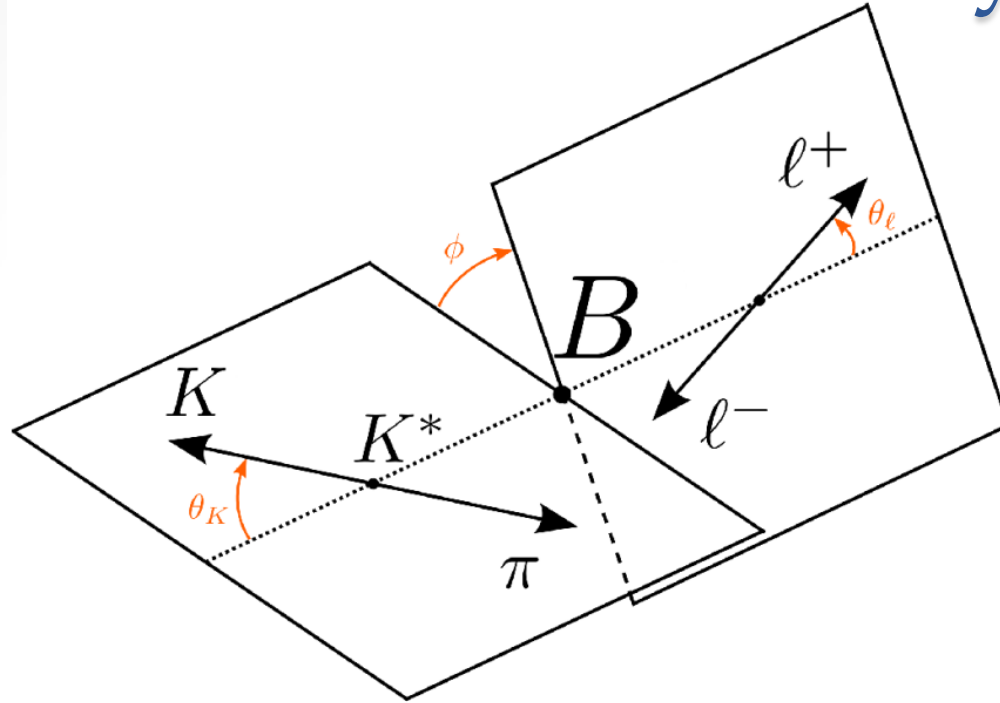
TABLE II. The systematic uncertainties in  $R(D^*)$  and  $P_\tau(D^*)$ , where the values for  $R(D^*)$  are relative errors. The group “common sources” identifies the common systematic uncertainty sources in the signal and the normalization modes, which cancel to a good extent in the ratio of these samples. The reason for the incomplete cancellation is described in the text.

Source	$R(D^*)$	$P_\tau(D^*)$
Hadronic $B$ composition	+7.7%	+0.134
	-6.9%	-0.103
MC statistics for PDF shape	+4.0%	+0.146
	-2.8%	-0.108
Fake $D^*$	3.4%	0.018
$\bar{B} \rightarrow D^{**}\ell^- \bar{\nu}_\ell$	2.4%	0.048
$\bar{B} \rightarrow D^{**}\tau^- \bar{\nu}_\tau$	1.1%	0.001
$\bar{B} \rightarrow D^*\ell^- \bar{\nu}_\ell$	2.3%	0.007
$\tau$ daughter and $\ell^-$ efficiency	1.9%	0.019
MC statistics for efficiency estimation	1.0%	0.019
$\mathcal{B}(\tau^- \rightarrow \pi^- \nu_\tau, \rho^- \nu_\tau)$	0.3%	0.002
$P_\tau(D^*)$ correction function	0.0%	0.010
Common sources		
Tagging efficiency correction	1.6%	0.018
$D^*$ reconstruction	1.4%	0.006
Branching fractions of the $D$ meson	0.8%	0.007
Number of $B\bar{B}$ and $\mathcal{B}(\Upsilon(4S) \rightarrow B^+ B^- \text{ or } B^0 \bar{B}^0)$	0.5%	0.006
Total systematic uncertainty	+10.4%	+0.21
	-9.4%	-0.16

# R(D) and R(D\*) Measurements



# B → K\*ll Differential Decay Rate



$$\frac{1}{d\Gamma/dq^2} \frac{d^4\Gamma}{d\cos\theta_\ell d\cos\theta_K d\phi dq^2} = \frac{9}{32\pi} \left[ \frac{3}{4}(1 - F_L) \sin^2\theta_K + F_L \cos^2\theta_K + \frac{1}{4}(1 - F_L) \sin^2\theta_K \cos 2\theta_\ell \right. \\ \left. - F_L \cos^2\theta_K \cos 2\theta_\ell + S_3 \sin^2\theta_K \sin^2\theta_\ell \cos 2\phi + S_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi \right. \\ \left. + S_5 \sin 2\theta_K \sin \theta_\ell \cos \phi + S_6 \sin^2\theta_K \cos \theta_\ell + S_7 \sin 2\theta_K \sin \theta_\ell \sin \phi \right. \\ \left. + S_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi + S_9 \sin^2\theta_K \sin^2\theta_\ell \sin 2\phi \right],$$

$$P'_{i=4,5,6,8} = \frac{S_{j=4,5,7,8}}{\sqrt{F_L(1 - F_L)}}$$

# B → K\*ll Results and Syst. Errors.

TABLE I. Fit results for  $P'_4$  and  $P'_5$  for all decay channels and separately for the electron and muon modes. The first uncertainties are statistical and the second systematic.

$q^2$ in $\text{GeV}^2/c^2$	$P'_4$	$P_4^{e'}$	$P_4^{\mu'}$	$P'_5$	$P_5^{e'}$	$P_5^{\mu'}$
[1.00, 6.00]	$-0.45^{+0.23}_{-0.22} \pm 0.09$	$-0.72^{+0.40}_{-0.39} \pm 0.06$	$-0.22^{+0.35}_{-0.34} \pm 0.15$	$0.23^{+0.21}_{-0.22} \pm 0.07$	$-0.22^{+0.39}_{-0.41} \pm 0.03$	$0.43^{+0.26}_{-0.28} \pm 0.10$
[0.10, 4.00]	$0.11^{+0.32}_{-0.31} \pm 0.05$	$0.34^{+0.41}_{-0.45} \pm 0.11$	$-0.38^{+0.50}_{-0.48} \pm 0.12$	$0.47^{+0.27}_{-0.28} \pm 0.05$	$0.51^{+0.39}_{-0.46} \pm 0.09$	$0.42^{+0.39}_{-0.39} \pm 0.14$
[4.00, 8.00]	$-0.34^{+0.18}_{-0.17} \pm 0.05$	$-0.52^{+0.24}_{-0.22} \pm 0.03$	$-0.07^{+0.32}_{-0.31} \pm 0.07$	$-0.30^{+0.19}_{-0.19} \pm 0.09$	$-0.52^{+0.28}_{-0.26} \pm 0.03$	$-0.03^{+0.31}_{-0.30} \pm 0.09$
[10.09, 12.90]	$-0.18^{+0.28}_{-0.27} \pm 0.06$	-	$-0.40^{+0.33}_{-0.29} \pm 0.09$	$-0.17^{+0.25}_{-0.25} \pm 0.01$	-	$0.09^{+0.29}_{-0.29} \pm 0.02$
[14.18, 19.00]	$-0.14^{+0.26}_{-0.26} \pm 0.05$	$-0.15^{+0.41}_{-0.40} \pm 0.04$	$-0.10^{+0.39}_{-0.39} \pm 0.07$	$-0.51^{+0.24}_{-0.22} \pm 0.01$	$-0.91^{+0.36}_{-0.30} \pm 0.03$	$-0.13^{+0.39}_{-0.35} \pm 0.06$

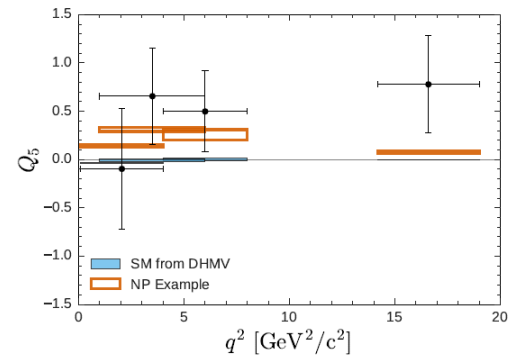
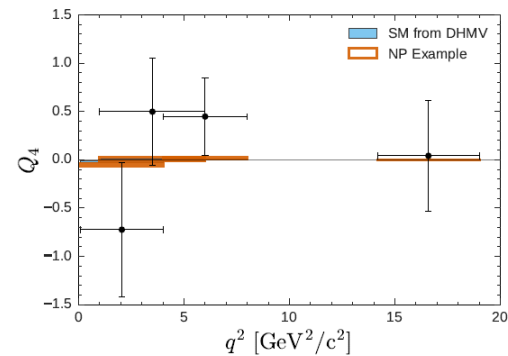
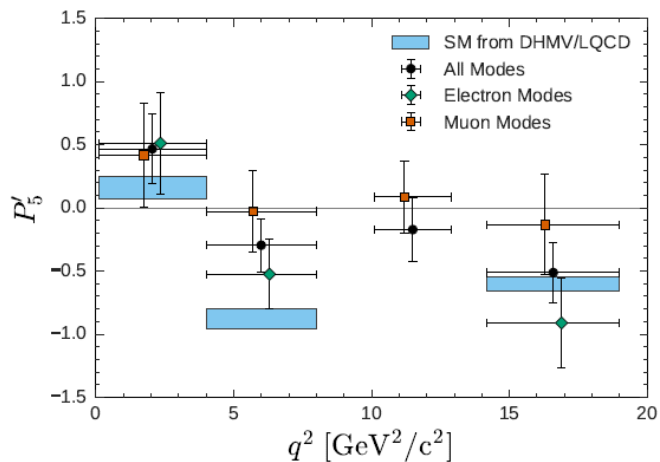
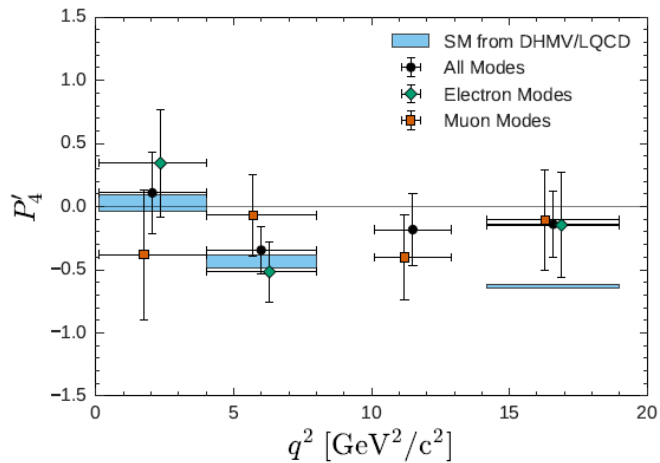


TABLE II. Results for the lepton-flavor-universality-violating observables  $Q_4$  and  $Q_5$ . The first uncertainty is statistical and the second systematic.

$q^2$ in $\text{GeV}^2/c^2$	$Q_4$	$Q_5$
[1.00, 6.00]	$0.498 \pm 0.527 \pm 0.166$	$0.656 \pm 0.485 \pm 0.103$
[0.10, 4.00]	$-0.723 \pm 0.676 \pm 0.163$	$-0.097 \pm 0.601 \pm 0.164$
[4.00, 8.00]	$0.448 \pm 0.392 \pm 0.076$	$0.498 \pm 0.410 \pm 0.095$
[14.18, 19.00]	$0.041 \pm 0.565 \pm 0.082$	$0.778 \pm 0.502 \pm 0.065$

# $B \rightarrow K^* \mu e$ Upper Limits

