Supercooling in Theories with Strong Dynamics at the TeV scale

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$$M_P \equiv$$
 scale of gravity  $\sim G_N^{-1/2}$ 

 $v_{EW} \equiv$  scale of electroweak breaking  $\approx 10^{-16} M_P$ 

# Hierarchy problem: lack of understanding of the smallness of $v_{EW}$ with respect to $M_P$

 $\Lambda_{QCD} \equiv$  where strong interactions <u>become</u> strong  $\approx 10^{-19} M_P$ 



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$$\Lambda_{QCD}=\exp\left(-8\pi^2/7g_s^2(M_P)
ight)M_P$$

Easy to generate large hierarchies with  $g_s(M_P) \lesssim 1$ 

We <u>do</u> understand the smallness of  $\Lambda_{QCD}/M_P$ !

Speculation: also  $v_{EW}$  is generated by some coupling becoming strong

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### Speculation: also $v_{EW}$ is generated by some coupling becoming strong

 $\Lambda_{QCD}$  sets the mass of the QCD resonances and the binding energy of its constituents the quarks

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## Speculation: also $v_{EW}$ is generated by some coupling becoming strong

 $\Lambda_{QCD}$  sets the mass of the QCD resonances and the binding energy of its constituents the quarks

<u>Phase transition</u> for  $T > \Lambda_{QCD}$ : bounds break and quarks deconfine

 $\Rightarrow \Rightarrow$  Plasma Phase

We expect an analogous confinement p.t. in the Electro-Weak sector, with  $T_c \sim v_{EW}$ 

Phase transitions are relevant in early Universe evolution

This can be well described by equilibrium thermodynamics (with occasional deviations)

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#### supercooling

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The supercooled phase ends when *bubbles* of the stable phase form, expand and meet

Confinement EW phase transition: predicted to be generically 1st order and slow

Not enough bubbles of the stable phase form  $\rightarrow$  the Universe keeps expanding and cooling in the wrong phase (plasma)

At low enough temperature (  $\mathcal{T} \ll v_{EW})$  an  $\underline{\textit{inflationary expansion}}$  starts

## Eventually the Universe must have transitioned to the confined phase

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Followed by entropy release (reheating)







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- I. Look for possible cosmic imprints of the supercooling epoch
- II. Exit form supercooling:
  - When? (number of e-folds  $N_e$ )
  - How? (microscopic mechanism that induced efficient bubble formation)

III. Cosmic traces of reheating? e.g. gravitational waves (LISA range of sensitivity)

T is a clock during inflation (not just de Sitter space)

• different physical scales are explored

Eventually one reaches the QCD scale: confinement phase transition (the QCD one!)

Quark condensation can be a seed for the formation of bubble of the  $\underline{EW}$  confined phase ( $\sim$  Witten '80)

 $T_{exit} \sim \Lambda_{QCD}$ 







### Axion: required by the Peccei-Quinn solution to the *strong CP problem*

Non-trivial potential  $V(\theta)$  for  $T < \Lambda_{QCD}$ , with minimum at  $\theta = 0$ 

Initial misalignment  $(\theta_{in} \neq 0) \rightarrow$  axion contribution to energy density (dark matter-like)



### Avoiding overproduction of axion DM puts a constraint on f, the scale of PQ breaking

$$f \lesssim 10^{11} GeV$$

Assumes  $\theta_{in} = O(1)$  at the QCD p.t. (the "standard" one)

With supercooling down to  $\, {\cal T} < \Lambda_{QCD}, \, there \, is an \, \underline{earlier} \, \, QCD \, p.t.! \,$ 

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-  $\theta$  can be relaxed to  $\theta \ll 1$ 

With supercooling down to  $\, {\cal T} < \Lambda_{QCD}, \, there \, is an \, \underline{earlier} \, \, QCD \, p.t.! \,$ 

• heta can be relaxed to  $heta\ll 1$ 

Relax bounds on f: as large as  $10^{13} GeV$  in some regions of parameter space