Binary pulsars as resonant detectors of

Ultra-Light Dark Matter

Diana L. López Nacir



Based on work with Diego Blas and Sergey Sibiryakov [PRL118, 261102 (2017)]

13th Rencontres du Vietnam: Cosmology 2017

Motivations and brief overview of ULDM

- Motivations and brief overview of ULDM
- Why binary pulsars could be useful to constraint ULDM models?

- Motivations and brief overview of ULDM
- Why binary pulsars could be useful to constraint ULDM models?
- Our results, and comparison with other constraints

- Motivations and brief overview of ULDM
- Why binary pulsars could be useful to constraint ULDM models?
- Our results, and comparison with other constraints
- Conclusions and future prospects

Motivations

Standard cosmological model: $\Lambda CDM \rightarrow Dark$ contributions

Dark Matter (DM):

- DM could consist of some ``cold" (small velocity dispersion) undiscovered particles
- An alternative model: DM consist of very light bosons or axion-like particles with high occupation numbers $n=\rho_{DM}/m$

Motivations

Standard cosmological model: $\Lambda CDM \rightarrow Dark$ contributions

Dark Matter (DM):

- DM could consist of some ``cold" (small velocity dispersion) undiscovered particles
- An alternative model: DM consist of very light bosons or axion-like particles with high occupation numbers $n=\rho_{DM}/m$

To what extend is it possible to discriminate among the different models?

Motivations

Standard cosmological model: $\Lambda CDM \rightarrow Dark$ contributions

Dark Matter (DM):

- DM could consist of some ``cold" (small velocity dispersion) undiscovered particles
- An alternative model: DM consist of very light bosons or axion-like particles with high occupation numbers $n=\rho_{DM}/m$

To what extend is it possible to discriminate among the different models?

We need

- to identify and characterize observable signatures
- to confront with data all calculable predictions (on diverse scales)

Ultra-Light Dark Matter as a classical scalar field

Very light DM with large $n = \rho_{DM}/m_{\Phi}$

Classical solution to the Klein-Gordon equation $[-\Box + m_{\Phi}^2]\Phi(\vec{x},t) = 0$

 $ds^{2} = -(1+2\phi)c^{2}dt^{2} + a^{2}(1-2\psi)\delta_{ij}dx^{i}dx^{j}$

Ultra-Light Dark Matter as a classical scalar field

Very light DM with large $n = \rho_{DM}/m_{\Phi}$

Classical solution to the Klein-Gordon equation $[-\Box + m_{\Phi}^2]\Phi(\vec{x},t) = 0$ $ds^{2} = -(1+2\phi)c^{2}dt^{2} + a^{2}(1-2\psi)\delta_{ij}dx^{i}dx^{j}$ Initial conditions set by inflation (very homogeneous) After $H < m_{\Phi} \longrightarrow \Phi \sim \Phi_0 \cos(m_{\Phi}t + \Upsilon)$ $T_{\mu\nu} \longrightarrow \rho_{DM} = \frac{m_{\Phi}^2 \Phi_0^2}{2} + \text{oscillations}$ $p_{DM} = -\rho_{DM} \cos(2m_{\Phi}t + 2\Upsilon)$ Potential Energy scalar field

(oscillations are irrelevant on long time scales)

All DM $\rightarrow m_{\Phi} > H(a_{eq}) \sim 10^{-28} \text{eV}$

CMB + LSS $\longrightarrow m_{\Phi} \gtrsim 10^{-24} \text{eV} (\times 10 \text{ in the future})$

 $a\partial_t \rho_{DM} \ll c |\nabla \rho_{DM}|$ Collection of plane waves: $\Phi = e^{-ict/\lambda_c} \Psi + e^{ict/\lambda_c} \Psi^*$

$$\Psi = \sqrt{\frac{c\rho_{DM}(\vec{x},t)}{2}}\lambda_c \exp\left\{-i\frac{\pi(\vec{x},t)}{c\lambda_c}\right\}$$

$$\left(\lambda_c = \frac{\hbar}{m_{\Phi}c}\right)$$

 $\left. \frac{t}{2} \right\}$ Compton wavelength

 $a\partial_t \rho_{DM} \ll c |\nabla \rho_{DM}|$ Collection of plane waves: $\Phi = e^{-ict/2}$

$$\begin{array}{l} \varphi_{DM} \\ \varphi \text{ waves:} \quad \Phi = e^{-ict/\lambda_c} \Psi + e^{ict/\lambda_c} \Psi^* & \left(\begin{array}{c} \lambda_c = \frac{\hbar}{m_{\Phi}c} \end{array} \right) \\ \Psi = \sqrt{\frac{c\rho_{DM}(\vec{x},t)}{2}} \lambda_c \exp\left\{ -i\frac{\pi(\vec{x},t)}{c\lambda_c} \right\} & \begin{array}{c} \text{Compton wave} \end{array} \end{array}$$

Compton wavelength

Coherence of the oscillations require

 $|\partial_t \pi|, |\nabla \pi|^2 \ll c^2$

 $a\partial_t \rho_{DM} \ll c |\nabla \rho_{DM}|$ $\begin{array}{ll} a \partial_t \rho_{DM} \ll c |\nabla \rho_{DM}| \\ \text{Collection of plane waves:} & \Phi = e^{-ict/\lambda_c} \Psi + e^{ict/\lambda_c} \Psi^* & \begin{pmatrix} \lambda_c = \frac{\hbar}{m_{\Phi}c} \end{pmatrix} \\ \Psi = \sqrt{\frac{c \rho_{DM}(\vec{x},t)}{2}} \lambda_c \exp\left\{-i\frac{\pi(\vec{x},t)}{c\lambda_c}\right\} & \text{Compton wavelength} \end{array}$

$$\Psi = \sqrt{\frac{c\rho_{DM}(\vec{x},t)}{2}}\lambda_c \exp\left\{-i\frac{\pi(\vec{x},t)}{c\lambda_c}\right\}$$

Coherence of the oscillations require

Oscillations relevant at time scales ~ Compton time

$$|\partial_t \pi|, |\nabla \pi|^2 \ll c^2$$

 $t_c = \lambda_c / c$

 $a\partial_t \rho_{DM} \ll c |\nabla \rho_{DM}|$ Collection of plane waves: $\Phi = e^{-ict/\lambda_c}\Psi + e^{ict/\lambda_c}\Psi^* \qquad \begin{pmatrix} \lambda_c = \frac{\hbar}{m_{\Phi}c} \end{pmatrix}$ $\Psi = \sqrt{\frac{c\rho_{DM}(\vec{x},t)}{2}}\lambda_c \exp\left\{-i\frac{\pi(\vec{x},t)}{c\lambda_c}\right\} \qquad \text{Compton wavelength}$ Coherence of the oscillations require Oscillations relevant at time $|\partial_t \pi|, |\nabla \pi|^2 \ll c^2$ scales ~ Compton time $\bullet \langle T_{00} \rangle \simeq c^2 \rho_{DM}$ $t_c = \lambda_c / c$ $T_{\mu\nu}$ $\downarrow \langle T_{ij} \rangle \simeq \rho_{DM} \partial_i \pi \partial_j \pi + \frac{\hbar^2}{m^2} \partial_i \sqrt{\rho_{DM}} \partial_j \sqrt{\rho_{DM}}$ <...> "Fast" oscillations + leading order in 1/c (a = 1) $-\frac{\delta_{ij}}{2} \left[\frac{\hbar^2}{m^2} \partial_i \sqrt{\rho_{DM}} \partial_i \sqrt{\rho_{DM}} + \rho_{DM} \partial_i \pi \partial_i \pi \right]$ $+\rho_{DM}\phi_N - \rho_{DM}\dot{\pi}\Big] \qquad (\phi_N = c^2\phi)$

 $a\partial_t \rho_{DM} \ll c |\nabla \rho_{DM}|$ e waves: $\Phi = e^{-ict/\lambda_c}\Psi + e^{ict/\lambda_c}\Psi^* \qquad \begin{pmatrix} \lambda_c = \frac{\hbar}{m_{\Phi}c} \end{pmatrix}$ $\Psi = \sqrt{\frac{c\rho_{DM}(\vec{x},t)}{2}}\lambda_c \exp\left\{-i\frac{\pi(\vec{x},t)}{c\lambda_c}\right\} \qquad \text{Compton wavelength}$ Collection of plane waves: Coherence of the oscillations require Oscillations relevant at time $|\partial_t \pi|, |\nabla \pi|^2 \ll c^2$ scales ~ Compton time $\bullet \langle T_{00} \rangle \simeq c^2 \rho_{DM}$ $t_c = \lambda_c / c$ $\langle T_{0i} \rangle \simeq c \rho_{DM} \partial_i \pi \rightarrow v = |\nabla \pi|$ $T_{\mu\nu}$ $\langle T_{ij} \rangle \simeq \rho_{DM} \partial_i \pi \partial_j \pi + \frac{\hbar^2}{m^2} \partial_i \sqrt{\rho_{DM}} \partial_j \sqrt{\rho_{DM}}$ <...> "Fast" oscillations + leading order in 1/c (a = 1) $-\frac{\delta_{ij}}{2} \left[\frac{\hbar^2}{m^2} \partial_i \sqrt{\rho_{DM}} \partial_i \sqrt{\rho_{DM}} + \rho_{DM} \partial_i \pi \partial_i \pi \right]$ Gradients are relevant at length $+\rho_{DM}\phi_N - \rho_{DM}\dot{\pi}$ ($\phi_N = c^2\phi$) $\lambda_{db} = \lambda_c \frac{c}{n} = \frac{h}{m-n}$

Observation on diverse scales can probe different mass ranges



Observation on diverse scales can probe different mass ranges



Goal: To add more observables to this list, both to constraint other mass ranges and to have complementary tests for same masses

Observation on diverse scales can probe different mass ranges



Goal: To add more observables to this list, both to constraint other mass ranges and to have complementary tests for same masses

- These observations can probe ULDM *interacting only through gravity*
- If ULDM is <u>directly coupled to the Standard Model</u>-> many other (but <u>model-dependent</u>) possibilities: atomic clocks, accelerometers, resonantmass detectors, laser and atom interferometry

Binary pulsars

• Radio pulsar: rapidly rotating neutron star (NS) with coherent radio emission along their magnetic poles and highly stable spin frequency

 M_2

- Pulsar timing techniques provide very precise measurements of the orbital motion
- Ideal systems to constraint alternatives theories of gravity and the presence of gravity waves
- Are they also useful to explore the nature of DM?

Binary pulsars

- Radio pulsar: rapidly rotating neutron star (NS) with coherent radio emission along their magnetic poles and highly stable spin frequency
- Pulsar timing techniques provide very precise measurements of the orbital motion
- Ideal systems to constraint alternatives theories of gravity and the presence of gravity waves
- Are they also useful to explore the nature of DM?

Some numbers:

$$L \sim 10^8 \text{km} \left(\frac{\text{P}_{\text{b}}}{100 \text{ days}}\right)^{2/3} \left(\frac{\text{M}_1 + \text{M}_2}{\text{M}_{\text{sun}}}\right)^{1/3}$$

$$v \sim 10^{-3}c, c m_{\Phi} \sim 10^{-18} \div 10^{-22} eV$$

$$\lambda_{db} \sim 10^{12} \mathrm{km} \left(\frac{10^{-3}c}{v}\right) \left(\frac{10^{-18} \mathrm{eV}}{c \, m_{\Phi}}\right)$$
$$t_c \sim 100 \, \mathrm{days} \left(\frac{10^{-22} \mathrm{eV}}{c \, m_{\Phi}}\right)$$

$$M_2$$

Binary pulsars

- Radio pulsar: rapidly rotating neutron star (NS) with coherent radio emission along their magnetic poles and highly stable spin frequency
- Pulsar timing techniques provide very precise measurements of the orbital motion
- Ideal systems to constraint alternatives theories of gravity and the presence of gravity waves
- Are they also useful to explore the nature of DM?

Some numbers:

$$L \sim 10^8 {\rm km} \left(\frac{{\rm P_b}}{100 \, {\rm days}} \right)^{2/3} \left(\frac{{\rm M_1 + M_2}}{{\rm M_{sun}}} \right)^{1/3}$$

L

 M_2

$$v \sim 10^{-3}c, c m_{\Phi} \sim 10^{-18} \div 10^{-22} \text{eV}$$

 $\lambda_{db} \sim 10^{12} \text{km} \left(\frac{10^{-3}c}{v}\right) \left(\frac{10^{-18} \text{eV}}{c m_{\Phi}}\right)$
 $t_c \sim 100 \text{ days} \left(\frac{10^{-22} \text{eV}}{c m_{\Phi}}\right)$

• Coherence:
$$v^2 \ll c^2$$
 \checkmark
• Homogeneity: $\lambda_{db} \gg L$ \checkmark
• Fast oscillations: $t_c \ll P_b$???

ULDM interacting only through gravity



ULDM interacting only through gravity

$$\begin{split} \hbar &= c = 1 \\ \Phi(\vec{x}, t) &= \Phi_0 \cos(m_{\Phi}t + \Upsilon(\vec{x})) \\ \rho_{DM} &= \frac{m_{\Phi}\Phi_0^2}{2} \\ p_{DM} &= -\rho_{DM} \cos(2m_{\Phi}t + 2\Upsilon) \\ \phi_{DM} &= -\rho_{DM$$

ULDM interacting only through gravity

$$h = c = 1$$

$$\Phi(\vec{x}, t) = \Phi_{0} \cos(m_{\Phi}t + \Upsilon(\vec{x}))$$

$$\rho_{DM} = \frac{m_{\Phi}\Phi_{0}^{2}}{2}$$
Only gravity!

$$p_{DM} = -\rho_{DM} \cos(2m_{\Phi}t + 2\Upsilon) \quad h_{ij} \sim -\frac{2\pi G\rho_{DM}}{m_{\Phi}^{2}} \delta_{ij} \cos(2m_{\Phi}t + 2\Upsilon)$$
Geodesic deviation eq.
$$\delta \vec{r}^{i} = -\delta R^{i}_{0j0} r^{j} \quad \delta E_{b} = \mu \int_{0}^{P_{b}} \vec{r}^{i} \delta \vec{r}^{i} dt \quad (P_{b} \propto |E_{b}|^{-3/2})$$

$$\mu = M_{1}M_{2}/(M_{1} + M_{2}) = 4\pi G\rho_{DM}\mu \int_{0}^{P_{b}} \vec{r}(t)r(t) \cos(2m_{\Phi}t + 2\Upsilon) dt$$
Resonances:

$$\delta \omega = 2m_{\Phi} - 2\pi N/P_{b}, \quad |\delta \omega| \ll 2m_{\Phi} \quad (N \in \mathbb{N})$$

$$\left\langle \dot{P}_{b} \right\rangle \simeq -1.6 \times 10^{-17} \left(\frac{\rho_{DM}}{0.3 \frac{\text{GeV}}{\text{cm}^{3}}}\right) \left(\frac{P_{b}}{100 \text{ d}}\right)^{2} \frac{J_{N}(Ne)}{N} \sin \gamma_{g}(t)$$

 $(P_b/N \ll \Delta t \ll 2\pi/\delta\omega)$ For $e \ll 1$, $J_N(Ne) \sim \frac{\left(\frac{Ne}{2}\right)^N}{\Gamma[N+1]}$

 $\gamma_g(t) = \delta \omega \left(t - t_0 \right) + 2m_{\Phi} t_0 + 2\Upsilon$ [PRL118, 261102 (2017)]



E. g. Double Pulsar (PSR J0737-3039) $\langle \Delta \dot{P}_b \rangle \sim \mathcal{O}(10^{-16})$, but $P_b \simeq 0.1$ days

Pulsar Timing Array (PTA)

[Khmelnitsky & Rubakov (2014)]

ULDM affects the propagation of the signal

$$\begin{split} h_{ij} &\sim -\frac{2\pi G\rho_{DM}}{m_{\Phi}^2} \delta_{ij} \cos(2m_{\Phi}t + 2\Upsilon) \\ \Delta t(t) &= \pi \frac{G\rho_{DM}}{m_{\Phi}^3} \sin(m_{\Phi}D + \Upsilon(x) - \Upsilon(x_p)) \cos(2m_{\Phi}t + \Upsilon(x) + \Upsilon(x_p) - m_{\Phi}D) \\ & \text{Oscillations} \end{split}$$

Pulsar Timing Array (PTA)

[Khmelnitsky & Rubakov (2014)]

ULDM affects the propagation of the signal

$$\begin{split} h_{ij} \sim &-\frac{2\pi G\rho_{DM}}{m_{\Phi}^2} \delta_{ij} \cos(2m_{\Phi}t+2\Upsilon) \\ \Delta t(t) &= \pi \frac{G\rho_{DM}}{m_{\Phi}^3} \sin(m_{\Phi}D+\Upsilon(x)-\Upsilon(x_p)) \cos(2m_{\Phi}t+\Upsilon(x)+\Upsilon(x_p)-m_{\Phi}D) \\ \text{Same as a GW with} \\ h_c &= 2 \times 10^{-15} \left(\frac{\rho_{DM}}{0.3 \frac{\text{GeV}}{\text{cm}^3}}\right) \left(\frac{10^{-23}\text{eV}}{m_{\Phi}}\right)^2 \frac{10^{-10}}{10^{-10}} \\ f &= 5 \times 10^{-9}\text{Hz} \left(\frac{m_{\Phi}}{10^{-23}\text{eV}}\right) \\ f &= 5 \times 10^{-9}\text{Hz} \left(\frac{m_{\Phi}}{10^{-23}\text{eV}}\right) \\ \text{Oscillations} \\ f &= 5 \times 10^{-9}\text{Hz} \left(\frac{m_{\Phi}}{10^{-23}\text{eV}}\right) \\ f &= 5 \times 10^{-9}\text{Hz} \left(\frac{m_{\Phi}}{10^{-23}\text{eV}}\right) \\ \text{Oscillations} \\ f &= 5 \times 10^{-9}\text{Hz} \left(\frac{m_{\Phi}}{10^{-23}\text{eV}}\right) \\ f &= 5 \times 10^$$

ULDM interacting directly coupled to matter

$$L = M_1(\Phi) \left(1 + \frac{v_1^2}{2}\right) + M_2(\Phi) \left(1 + \frac{v_2^2}{2}\right) + \frac{GM_1(\Phi)M_2(\Phi)}{r}$$

Universal coupling:

 $M_{1,2}(\Phi) = M_{1,2}(1 + \alpha(\Phi)), \ |\alpha(\Phi)| \ll 1$

$$\ddot{\delta \vec{r}} = -\frac{d\alpha}{d\Phi} \dot{\Phi} \dot{\vec{r}} - \alpha(\Phi) \frac{G(M_1 + M_2)}{r^3} \vec{r}$$

ULDM interacting directly coupled to matter

$$L = M_1(\Phi) \left(1 + \frac{v_1^2}{2}\right) + M_2(\Phi) \left(1 + \frac{v_2^2}{2}\right) + \frac{GM_1(\Phi)M_2(\Phi)}{r}$$

Universal coupling: $M_{1,2}(\Phi) = M_{1,2}(1 + \alpha(\Phi)), \quad |\alpha(\Phi)| \ll 1$ $\ddot{\delta \vec{r}} = -\frac{d\alpha}{d\Phi} \dot{\Phi} \dot{\vec{r}} - \alpha(\Phi) \frac{G(M_1 + M_2)}{m^3} \vec{r}$ Quadratic coupling $\alpha(\Phi) = \Phi^2/(2\Lambda_2^2)$ Linear coupling $\alpha(\Phi) = \Phi/\Lambda_1$ Different resonance conditions $\delta\omega = m_{\Phi} - 2\pi N/P_b, \ |\delta\omega| \ll m_{\Phi} \ (N \in \mathbb{N}) \quad \delta\omega = 2m_{\Phi} - 2\pi N/P_b, \ |\delta\omega| \ll 2m_{\Phi} \ (N \in \mathbb{N})$ $\langle \dot{P}_b \rangle \simeq 1.1 \times 10^{-11} \frac{J_N(Ne)}{N} \sin \gamma_q(t)$ $\langle \dot{P}_b \rangle \simeq 2.5 \times 10^{-12} J_N(Ne) \sin \gamma_l(t)$ $\times \left(\frac{\rho_{DM}}{0.3 \frac{\text{GeV}}{3}}\right)^{\frac{1}{2}} \left(\frac{P_b}{100 \text{ d}}\right) \left(\frac{10^{23} \text{GeV}}{\Lambda_1}\right) \times \left(\frac{\rho_{DM}}{0.3 \frac{\text{GeV}}{3}}\right) \left(\frac{P_b}{100 \text{ d}}\right)^2 \left(\frac{10^{16} \text{GeV}}{\Lambda_2}\right)^2$ $\gamma_l(t) = \delta\omega \left(t - t_0\right) + m_{\Phi} t_0 + \Upsilon$ $\gamma_a(t) = \delta\omega \left(t - t_0\right) + 2m_{\Phi} t_0 + 2\Upsilon$ [PRL118, 261102 (2017)]





↓ J1740-3052 ▶ J1518+4904 ★ J1756-2251
 Binary ↓ J1903+0327 ◆ B1516+02B ♣ J1141-6545
 pulsars ★ J1748-2021B ‡ B1534+12 ▼ J1906+0746
 ● J1807-2500B ■ B1913+16 ♠ J0737-3039A

Solid (empty) symbols $\rightarrow N = 1 \ (N \ge 2)$ Black symbols \rightarrow Current data Orange symbols $\rightarrow \langle \Delta \dot{P}_b \rangle = 10^{-16}$



Binary ▲ J1903+0327 ◆ B1516+02B ♣ J1141-6545 pulsars * J1748-2021B ‡ B1534+12 ▼ J1906+0746 ● J1807-2500B ■ B1913+16 ♠ J0737-3039A

 $\delta m_{\Phi} \sim 5 \times 10^{-23} \, \mathrm{eV}/(\mathrm{years of observation})$

Solid (empty) symbols $\rightarrow N = 1$ ($N \ge 2$) Black symbols \rightarrow Current data Orange symbols $\rightarrow \langle \Delta \dot{P}_b \rangle = 10^{-16}$

Conclusions & future prospects

- ULDM could yield secular variations of the orbital parameters of Binary Pulsars (BPs):
- because its stress-energy tensor modifies the spacetime metric
- if it is directly coupled to the Standard Model
- The secular effect leads to potentially observable signatures in high precision timing measurements of pulsars in binaries
- Exquisitely precise measurements are already ongoing for many systems
- For the system to stay in resonance during the whole observational campaign, we estimate $\delta m_{\Phi} \sim 5 \times 10^{-23} \, {\rm eV}/({
 m years of observation})$

So, a given BP is sensitive to ULDM masses only in a few narrow bands

- New (~1000) BPs are expected to be discovered by SKA -> significant coverage
- Beyond the orbital period derivative: there will also be secular variations of other orbital parameters (D.Blas, DLN, and S. Sibiryakov, to appear) ...
- Other resonant effects? Dipolar radiation? ...

THANKS!

Beyond the orbital period derivative?

Phenomenological Timing model \supset secular change of orbital parameters

[Blandford & Teukolsky (1976), Damour & Daruelle (1986)]

 $P_b \rightarrow P_b + \dot{P}_b(T - T_0), \ e \rightarrow e + \dot{e}(T - T_0), \ \omega \rightarrow \omega + \dot{\omega}(T - T_0), \ \dots$



E.g. Hulse-Taylor [B1913+16] [from Weisberg & Huang (2016)]

T_0 (MJD)	52144.90097849(3)
P_b (d)	0.322997448918(3)
e	0.6171340(4)
$\omega ~(\text{deg})$	292.54450(8)
$x = a_1 \sin \iota \ (s)$	2.341776(2)
\dot{P}_{b}^{obs}	$-2.423(1) \times 10^{-12}$
$\dot{\omega} (\text{deg} / \text{yr})$	4.226585(4)
$\dot{e}^{obs}\left(s^{-1}\right)$	$0.0006(7) \times 10^{-12}$
\dot{x}^{obs}	$-0.014(9) \times 10^{-12}$

$$\omega_0 = \frac{2\pi}{P_b} = \sqrt{\frac{GM_T}{a^3}}$$

semi-major axis
$$a_1 = a M_2/M_T, \ (M_T = M_1 + M_2)$$

Beyond the orbital period derivative?

Phenomenological Timing model \supset secular change of orbital parameters

[Blandford & Teukolsky (1976), Damour & Daruelle (1986)]

 $P_b \rightarrow P_b + \dot{P}_b(T - T_0), e \rightarrow e + \dot{e}(T - T_0), \omega \rightarrow \omega + \dot{\omega}(T - T_0), \dots$



E.g. Hulse-Taylor [B1913+16] [from Weisberg & Huang (2016)]

$T_0 (\mathrm{MJD})$	52144.90097849(3)
P_b (d)	0.322997448918(3)
e	0.6171340(4)
ω (deg)	292.54450(8)
$x = a_1 \sin \iota \ (s)$	2.341776(2)
\dot{P}_{b}^{obs}	$-2.423(1) \times 10^{-12}$
$\dot{\omega} (\text{deg} / \text{yr})$	4.226585(4)
$\dot{e}^{obs}\left(s^{-1}\right)$	$0.0006(7) \times 10^{-12}$
\dot{x}^{obs}	$-0.014(9) \times 10^{-12}$

$$\frac{\bar{G}M_T}{a^3} \qquad \dot{P}_b^{intr} = \dot{P}_b^{obs} - \dot{P}_b^{gal} = -(2.398 \pm 0.004) \times 10^{-12}
\dot{P}_b^{gal} = -(0.025 \pm 0.004) \times 10^{-12}
\dot{P}_b^{GW} = -(2.40263 \pm 0.00005) \times 10^{-12}$$

 $a_1 = a M_2 / M_T, \ (M_T = M_1 + M_2)$

 $\omega_0 = \frac{2\pi}{P_b} = \sqrt{\frac{GM_T}{a^3}}$

Beyond the orbital period derivative?



[Kehl, et.al. (2016)]

A rough estimation:

• If secular drift ~ constant \rightarrow accuracy increases with $T_{\rm obs}$

(E.g.,
$$\delta \dot{P}_b \sim T_{\rm obs}^{-5/2}$$
, $\delta \dot{e} \sim T_{\rm obs}^{-3/2}$)

A rough estimation:

• If secular drift ~ constant \rightarrow accuracy increases with $T_{\rm obs}$

(E.g.,
$$\delta \dot{P}_b \sim T_{\rm obs}^{-5/2}$$
, $\delta \dot{e} \sim T_{\rm obs}^{-3/2}$)

This applies for ~ at most for
$$\Delta T \sim \frac{T_{\rm mod}}{2} = \frac{\pi}{\delta \omega}$$

A rough estimation:

• If secular drift ~ constant \rightarrow accuracy increases with $T_{\rm obs}$

(E.g.,
$$\delta \dot{P}_b \sim T_{\rm obs}^{-5/2}$$
, $\delta \dot{e} \sim T_{\rm obs}^{-3/2}$)

This applies for ~ at most for
$$\Delta T \sim \frac{T_{\rm mod}}{2} = \frac{\pi}{\delta \omega}$$

The closer the system is to the resonance the better

A rough estimation:

• If secular drift ~ constant \rightarrow accuracy increases with $T_{\rm obs}$

(E.g.,
$$\delta \dot{P}_b \sim T_{\rm obs}^{-5/2}$$
, $\delta \dot{e} \sim T_{\rm obs}^{-3/2}$)

This applies for ~ at most for
$$\ \Delta T \sim rac{T_{
m mod}}{2} = rac{\pi}{\delta \omega}$$

The closer the system is to the resonance the better

• To see a modulation we need $T_{\rm obs} > \frac{T_{\rm mod}}{2}$

A rough estimation:

• If secular drift ~ constant \rightarrow accuracy increases with $T_{\rm obs}$

(E.g.,
$$\delta \dot{P}_b \sim T_{\rm obs}^{-5/2}$$
, $\delta \dot{e} \sim T_{\rm obs}^{-3/2}$)

This applies for ~ at most for
$$\ \Delta T \sim rac{T_{
m mod}}{2} = rac{\pi}{\delta \omega}$$

The closer the system is to the resonance the better

• To see a modulation we need $T_{\rm obs} > \frac{T_{\rm mod}}{2}$



Large $T_{\rm mod}$ but with $T_{\rm mod} \lesssim 2T_{\rm obs}$