



# The Dark Energy and Massive Neutrino Universe simulations

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# Neutrinos: Physics beyond the standard model

Neutrino astronomy: account for neutrino oscillations to estimate expected fluxes

## NOBEL PRIZE IN PHYSICS 2015

The Nobel Prize in Physics 2015 was awarded to **Takaaki Kajita** and **Arthur B. McDonald** for discovery of neutrino oscillations, which shows neutrinos have mass.

### WHAT IS A NEUTRINO?

Neutrinos are tiny subatomic particles, produced by nuclear reactions that take place in stars, including our sun, as well as in radioactive decay processes. They come in three 'flavours'.



ELECTRON NEUTRINO



MUON NEUTRINO



TAU NEUTRINO



The nuclear reactions in the sun produce neutrinos, which we can detect.

The number of neutrinos detected was only a third of the expected value.

Neutrinos 'flip' between the three flavours, and only one type was being detected.

### WHY DOES IT MATTER?

If neutrinos oscillate between types, they must have mass, even if this mass is incredibly small. This contradicts the standard model of particle physics, which states they are massless.

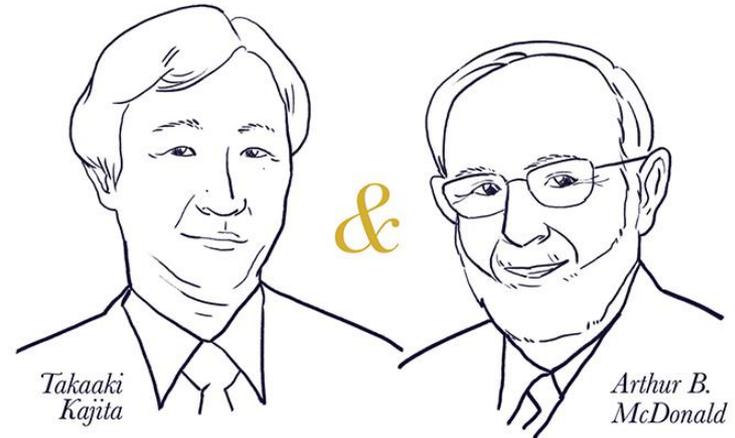


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2015 NOBEL PRIZE

*in Physics*



## NEUTRINO OSCILLATIONS

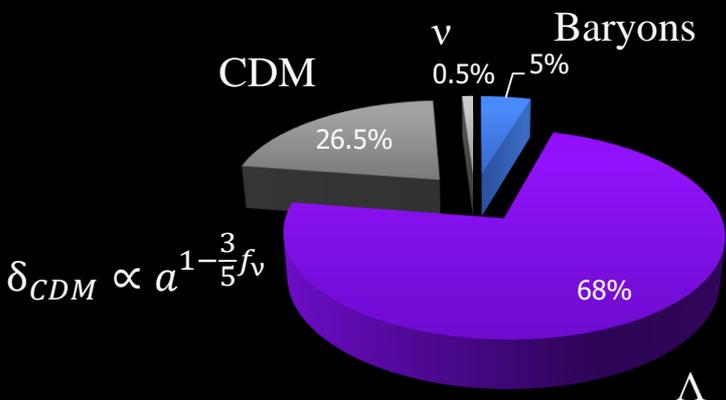
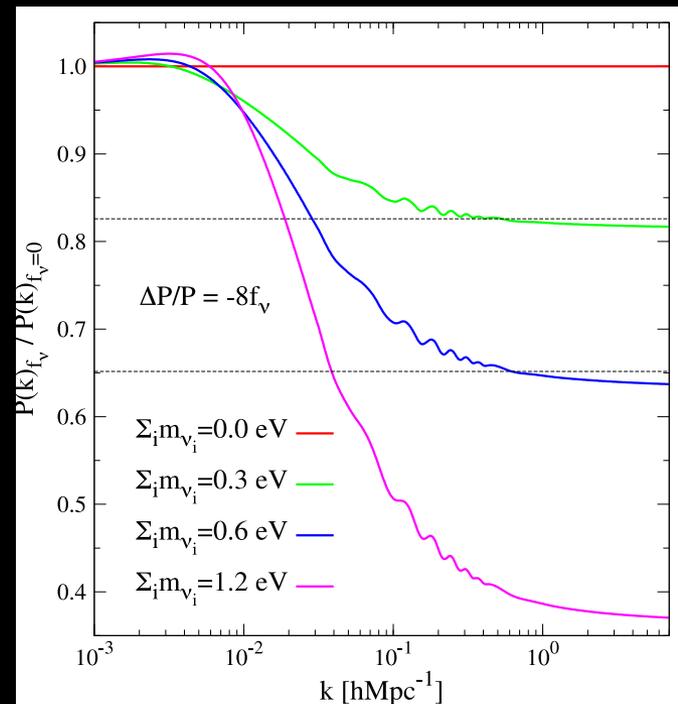
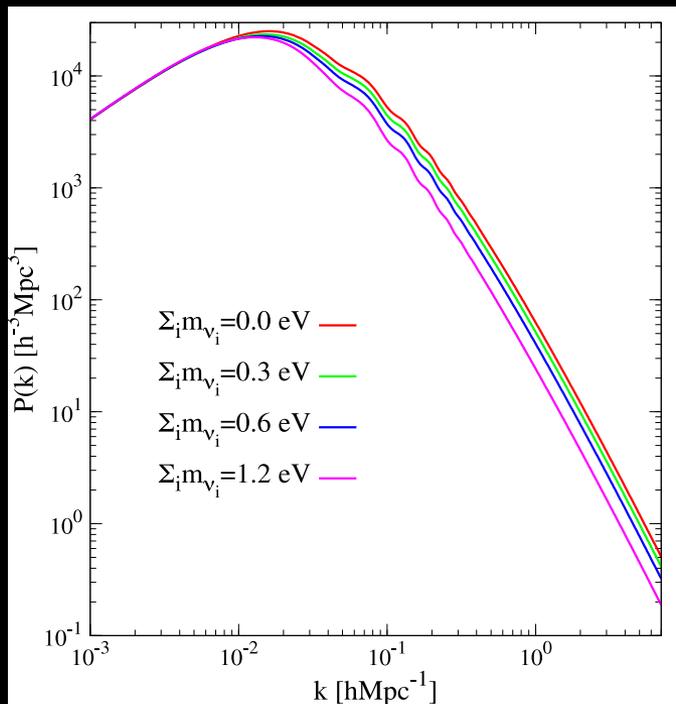
The discovery of these oscillations shows that neutrinos have mass.

Image by Abigail Malate



Cosmology: LSS gives constraints on neutrino absolute mass. Degeneracy with other cosmological parameters.

# Massive neutrino effects in the linear regime

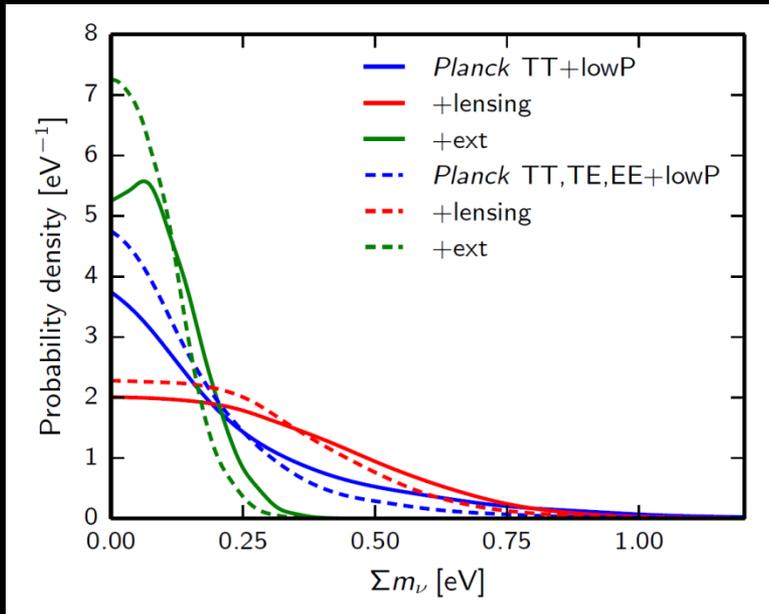


$$\Omega_{\text{DM}} = \Omega_{\text{CDM}} + \Omega_\nu = \text{fixed}$$

1. Modification of the Matter-Radiation equality time
2. Slow down the growth of matter perturbations

# Planck constraints on neutrinos (95% CL)

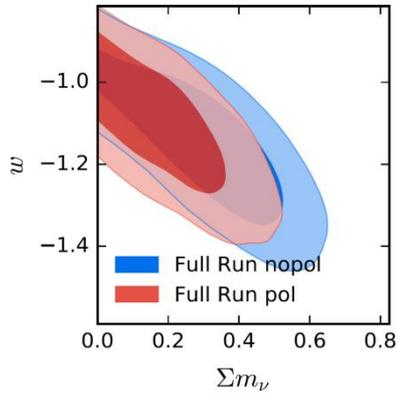
Parameter	TT	TT+lensing	TT+lensing+ext	TT, TE, EE	TT, TE, EE+lensing	TT, TE, EE+lensing+ext
$\Omega_K$ .....	$-0.052^{+0.049}_{-0.055}$	$-0.005^{+0.016}_{-0.017}$	$-0.0001^{+0.0054}_{-0.0052}$	$-0.040^{+0.038}_{-0.041}$	$-0.004^{+0.015}_{-0.015}$	$0.0008^{+0.0040}_{-0.0039}$
$\Sigma m_\nu$ [eV] .....	$< 0.715$	$< 0.675$	$< 0.234$	$< 0.492$	$< 0.589$	$< 0.194$
$N_{\text{eff}}$ .....	$3.13^{+0.64}_{-0.63}$	$3.13^{+0.62}_{-0.61}$	$3.15^{+0.41}_{-0.40}$	$2.99^{+0.41}_{-0.39}$	$2.94^{+0.38}_{-0.38}$	$3.04^{+0.33}_{-0.33}$
$Y_p$ .....	$0.252^{+0.041}_{-0.042}$	$0.251^{+0.040}_{-0.039}$	$0.251^{+0.035}_{-0.036}$	$0.250^{+0.026}_{-0.027}$	$0.247^{+0.026}_{-0.027}$	$0.249^{+0.025}_{-0.026}$
$dn_s/d \ln k$ .....	$-0.008^{+0.016}_{-0.016}$	$-0.003^{+0.015}_{-0.015}$	$-0.003^{+0.015}_{-0.014}$	$-0.006^{+0.014}_{-0.014}$	$-0.002^{+0.013}_{-0.013}$	$-0.002^{+0.013}_{-0.013}$
$r_{0.002}$ .....	$< 0.103$	$< 0.114$	$< 0.114$	$< 0.0987$	$< 0.112$	$< 0.113$
$w$ .....	$-1.54^{+0.62}_{-0.50}$	$-1.41^{+0.64}_{-0.56}$	$-1.006^{+0.085}_{-0.091}$	$-1.55^{+0.58}_{-0.48}$	$-1.42^{+0.62}_{-0.56}$	$-1.019^{+0.075}_{-0.080}$



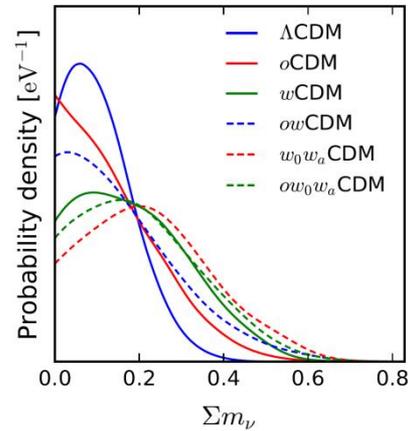
Planck-XIII (2015): the lensing reconstruction data, which directly probes the lensing power, prefers lensing amplitudes slightly below (but consistent with) the base  $\Lambda$ CDM prediction. The Planck+lensing constraint therefore pulls the constraints slightly away from zero towards higher neutrino masses. Extending the analysis up to  $L < 900$ , Planck lensing gives non-zero best-fit value for the neutrino mass:

$$\Sigma m_\nu = 0.16^{+0.08}_{-0.11} \text{ eV} \quad (\text{Planck TT+lowP+aggressive lensing + BAO; 68\%})$$

# Pellejero-Ibanez et al 2016 (BOSS collaboration)



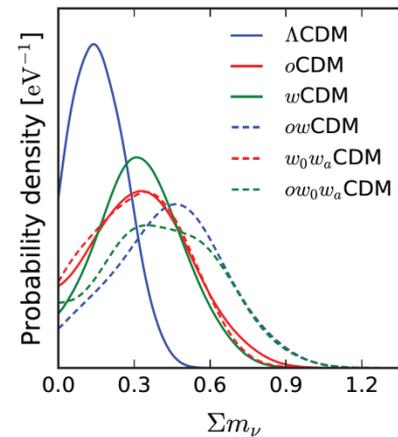
**Figure 10.** 2D marginalized contours for 68% and 95% confidence level for  $w$  and  $\Sigma m_\nu$  ( $w$ CDM model assumed) from Planck+BOSS. The blue contours are from full-likelihood-analysis without using a polynomial function to remove the overall shape information of monopole; the red contours are from the analysis removing overall shape information with a polynomial function. One can see that the overall shape information shift the  $\Sigma m_\nu$  to a larger value.



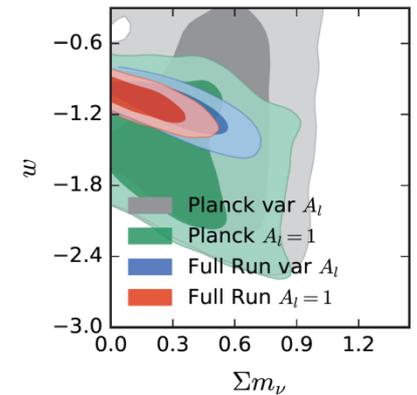
**Figure 11.** Probability density for  $\Sigma m_\nu$  from the full-likelihood-analysis of the joint data set.  $\Sigma m_\nu$  is one of the parameters to be constrained. Planck data includes lensing with  $A_L = 1$ . The overall shape information of the monopole of the correlation function from the BOSS galaxy clustering is removed with a polynomial function (see Sec. 7.2 and Table 10).

$M_\nu < 0.16$  eV from BOSS

Full shape measurement of the monopole of the galaxy 2-point correlation function introduces some detection of neutrino mass but non-linear modelling is needed.

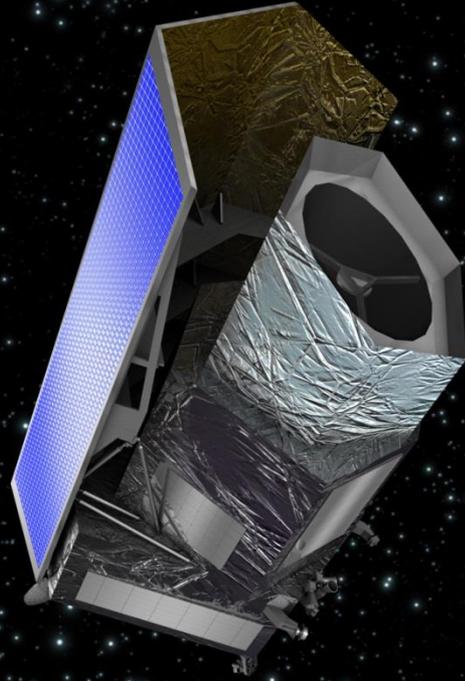


**Figure 12.** Probability density for  $\Sigma m_\nu$  from full-likelihood-analysis from the joint data set. Both  $\Sigma m_\nu$  and  $A_L$  are the parameters to be constrained. The overall shape information of the monopole of the correlation function from the BOSS galaxy clustering is removed with a polynomial function (see Sec. 7.2 and Table 11). One can see that the maximum of  $\Sigma m_\nu$  increases comparing to the cases with fixing  $A_L = 1$  (see Fig. 11).



**Figure 13.** 2D marginalized contours for 68% and 95% confidence level for  $w$  and  $\Sigma m_\nu$  ( $w$ CDM model assumed) from full run methodology and Planck only for different lensing information used. Gray contours and green contours are from Planck only with varying  $A_L$  and fixing  $A_L = 1$  respectively; the blue contours and the red contours are from Planck+BOSS with varying  $A_L$  and fixing  $A_L = 1$  respectively using full-likelihood-analysis. One can see that  $\Sigma m_\nu$  shift to a large value when varying  $A_L$  for both data combinations.

## *Euclid: Mapping the geometry of the dark Universe*



**Euclid** is an ESA M-class mission selected for launch in 2020 in the Cosmic Vision 2015-2025 programme. The main goal of Euclid is to understand the origin of the accelerating expansion of the Universe. To achieve this goal, it is proposed to build a satellite equipped with a 1.2 m telescope and three imaging and spectroscopic instruments working in the visible and near-infrared wavelength domains. These instruments will explore the expansion history of the Universe and the evolution of cosmic structures by measuring shapes and redshifts of galaxies as well as the distribution of galaxy-clusters as function of redshift  $0.5 < z < 2$ , over  $15000 \text{ deg}^2$  of the sky. The satellite will be launched by a Soyuz ST-2.1B rocket and transferred to the L2 Lagrange point for a 6 years mission.

# Spectro-Euclid forecasts

**Table 5:**  $\sigma(M_\nu)$  and  $\sigma(N_{\text{eff}})$  marginalised errors from LSS+CMB

	General cosmology					
fiducial→	$M_\nu=0.3 \text{ eV}^a$	$M_\nu=0.2 \text{ eV}^a$	$M_\nu=0.125 \text{ eV}^b$	$M_\nu=0.125 \text{ eV}^c$	$M_\nu=0.05 \text{ eV}^b$	$N_{\text{eff}}=3.04^d$
slitless+BOSS+Planck	0.035	0.043	0.031	0.044	0.053	0.086
	$\Lambda$ CDM cosmology					
slitless+BOSS+Planck	0.017	0.019	0.017	0.021	0.021	0.023

<sup>a</sup>for degenerate spectrum:  $m_1 \approx m_2 \approx m_3$ ; <sup>b</sup>for normal hierarchy:  $m_3 \neq 0, m_1 \approx m_2 \approx 0$

<sup>c</sup>for inverted hierarchy:  $m_1 \approx m_2, m_3 \approx 0$ ; <sup>d</sup>fiducial cosmology with massless neutrinos

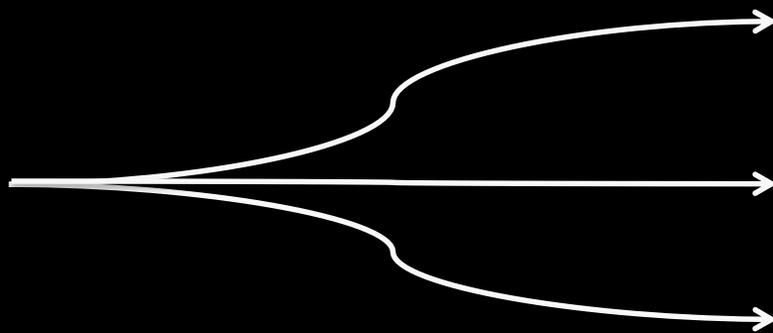
Only 3 active neutrinos for  $M_\nu$  errors

Carbone et al. 2011

If  $M_\nu$  is  $> 0.1 \text{ eV}$ , spectroscopic Euclid will be able to determine the neutrino mass scale independently of the model cosmology assumed. If  $M_\nu$  is  $< 0.1 \text{ eV}$ , the sum of neutrino masses, and in particular the minimum neutrino mass required by neutrino oscillations, can be measured in the context of a  $\Lambda$ CDM model. DE FoM decreases by a factor 2-3 wrt the massless case. Important to include NL info.

# Effects in the non-linear regime

Why?

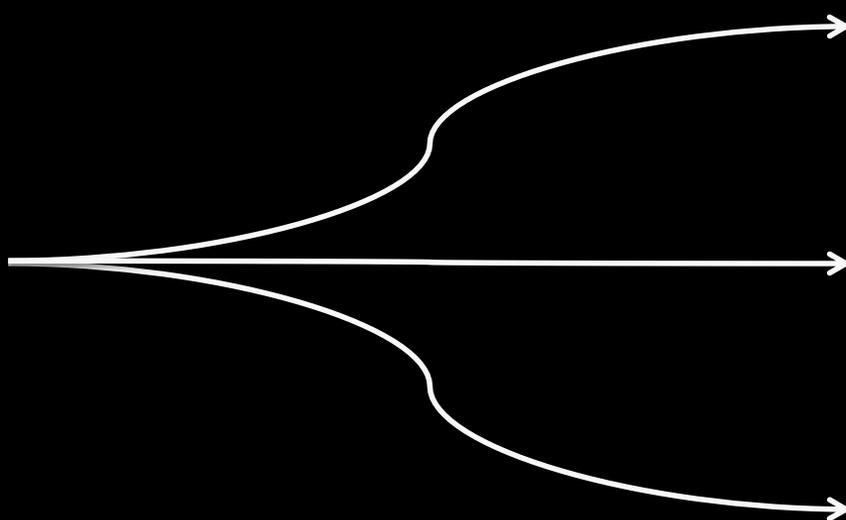


Important on small scales

Important at low redshift

Lots of modes in the middle—non-linear regime

How?



Semi-analytic methods

N-1-body, Ringwald & Wong, 2004  
(see also Singh & Ma, 2003)

Perturbation theory

Blas, Garny, Konstandin, Lesgourgues, 2014

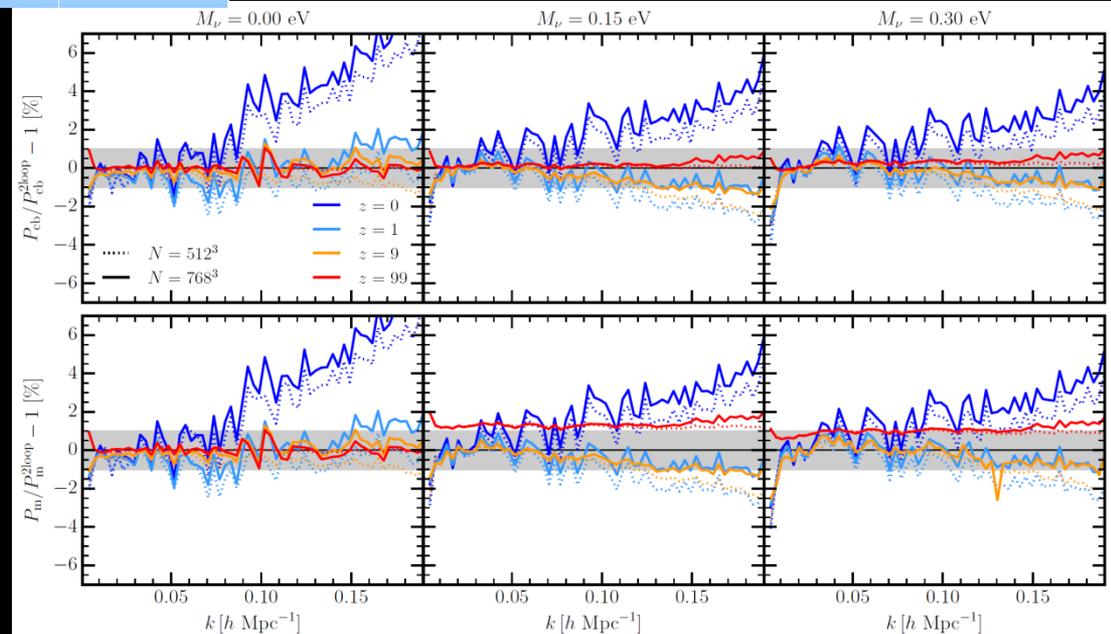
N-body simulations

Particle/Grid based/Boltzmann

# Initial Conditions improvements

S1: No radiation & constant initial growth rates $\Omega_{\gamma,0} = 0$ $f_{cb} = f_{\nu} = \Omega_m^{0.55}(z) = const$	4%
S2: No radiation $\Omega_{\gamma,0} = 0$	2%
S3: Constant initial growth rates $f_{cb} = f_{\nu} = \Omega_m^{0.55}(z) = const$	6% 1%
S4: No relativistic neutrino perturbations $\delta\rho_{\nu}^{rel} = 0 (M_{p,\nu} = const)$	0.6%
S5: No relativistic neutrinos $\delta\rho_{\nu}^{rel} = 0 (M_{p,\nu} = const)$ $\rho_{\nu}(z) = \rho_{\nu,0}(1+z)^3$	0.9%

MZ et al. 2016



MZ et al. 2016

# "Dark Energy and Massive Neutrino Universe" (DEMNUUni) simulations (PI Carmelita Carbone)

1. DEMNUUni-I: 5M cpu-hr on Fermi Tier-0 @CINECA (**COMPLETED**)
2. DEMNUUni-II: 8M cpu-hr on Fermi Tier-0 @CINECA (**COMPLETED**)

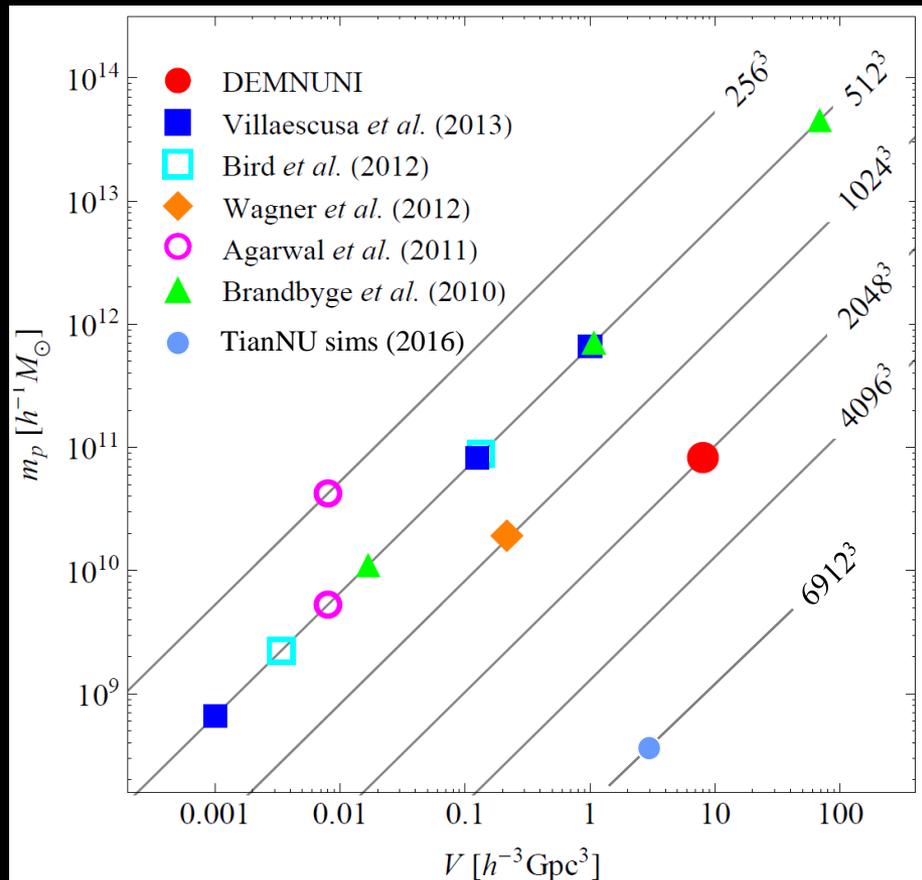
14 cosmological simulations with volume:  $(2 \text{ Gpc/h})^3$  and  $N_{\text{part}}: 2 \times 2048^3$  (CDM+v)  
baseline Planck cosmology +  
 $M_\nu=0, 0.17, 0.3, 0.53 \text{ eV}$  &  $(M_\nu, w_0, w_a)=(0 \div 0.16, -0.9, \pm 0.3), (0 \div 0.16, -1.1, \pm 0.3)$

3. DEMNUUni-Covariances: 3M cpu-hr on Marconi Tier-0 @CINECA (**STARTED**)

→ 300 cosmological simulations with  $V=1 \text{ (Gpc/h)}^3$  and  $N_{\text{part}}=2 \times 1024^3$  (CDM+v)

# Simulation outputs

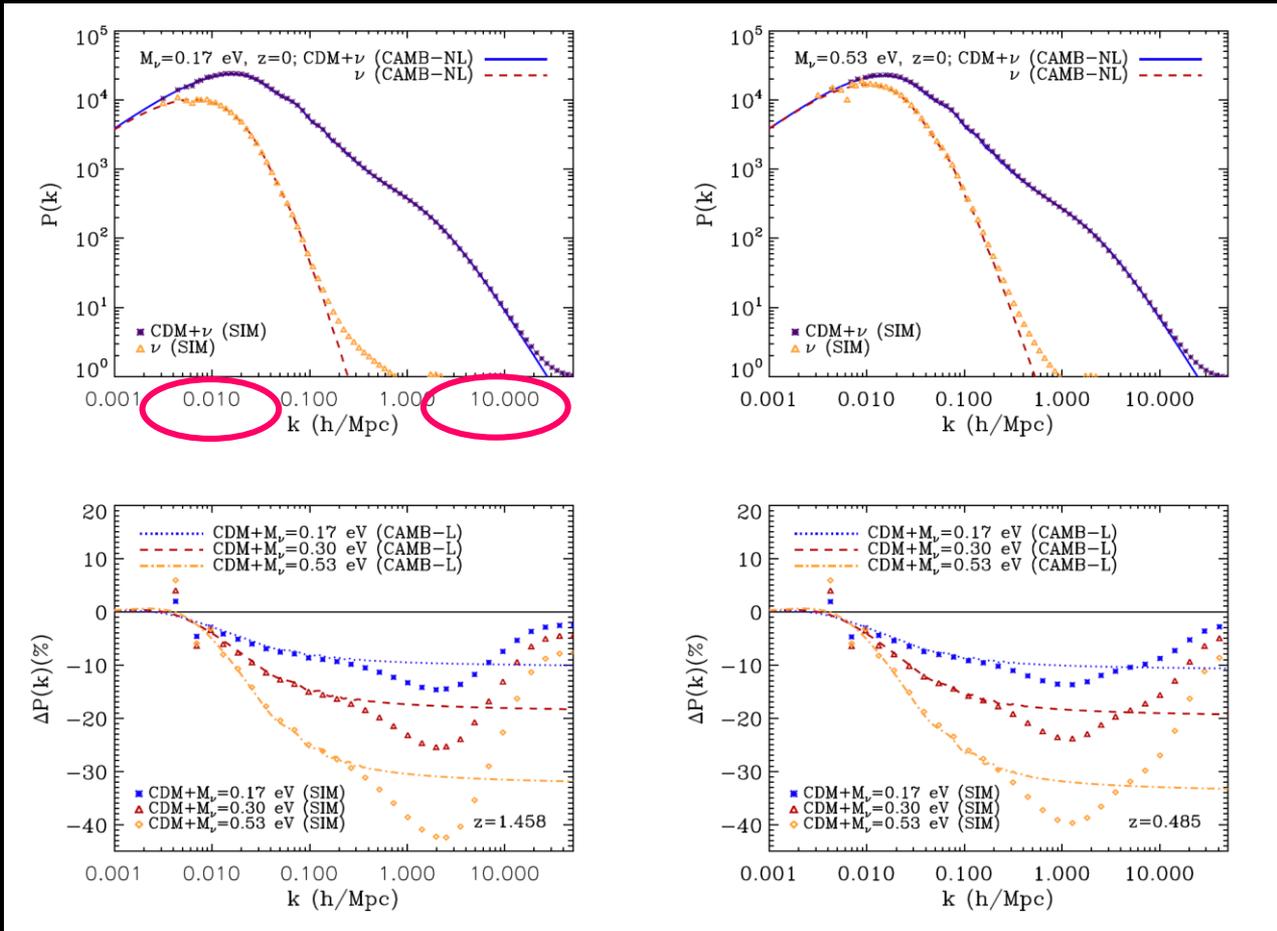
- **90 TB/sim of data**
- **62 temporary snapshots per simulation:  $\sim 0.54$  TB/snap (CDM+  $\nu$ )**
- **62 halo-catalogs**
- **62 sub-halo catalogs**
- **Matter power-spectra and correlation functions for all the 62 snapshots**
- **62 temporary gravitational potential grids of size  $4096^3$  (for CMB weak-lensing)**
- **62 temporary grids of size  $4096^3$  for the derivative of the gravitational potential (for ISW/Rees-Sciama)**



Comparison between the DEMNUni runs and recent simulations of massive neutrino cosmologies in terms of cold dark matter mass resolution and volume

# DEMNUi matter power spectra for $M_\nu=0.3$ eV

Carbone et al. 2016

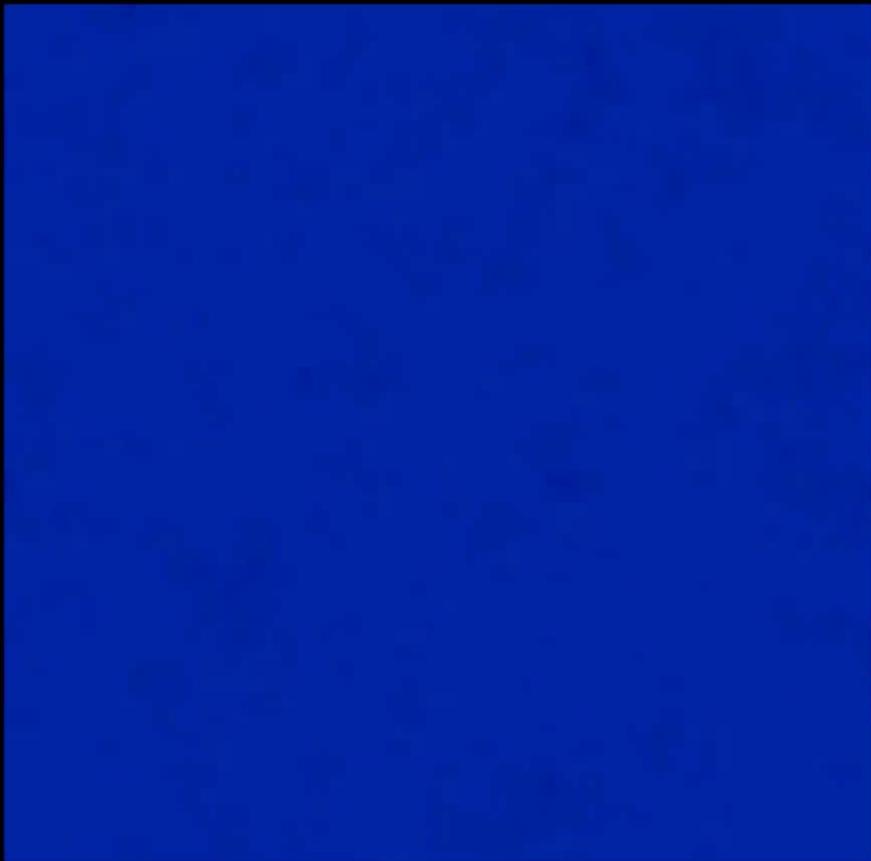


The large volume and mass resolution of the DEMNUi simulations allow to test different probes, and their combinations, in massive neutrino cosmologies, at the level of accuracy required by current and future galaxy surveys up to  $k=1$   $h/\text{Mpc}$ .

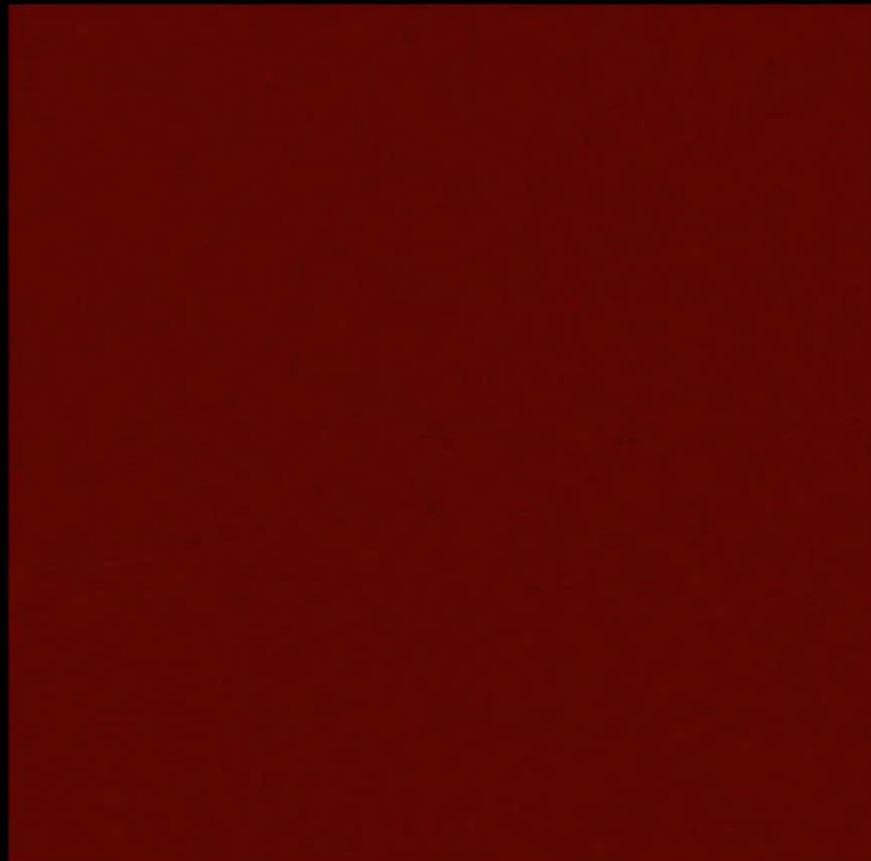
$$k_{\text{fs}}(z) = 0.82H(z)/H_0/(1+z)^2(m_\nu/1\text{eV}) h\text{Mpc}^{-1}$$

# CDM/ $\nu$ clustering in high resolution simulations (2400 times smaller than DEMNUni)

Dark Matter



Neutrino



$a=0.02$

Courtesy of Villaescusa-Navarro

$L=150 \text{ Mpc}/h$

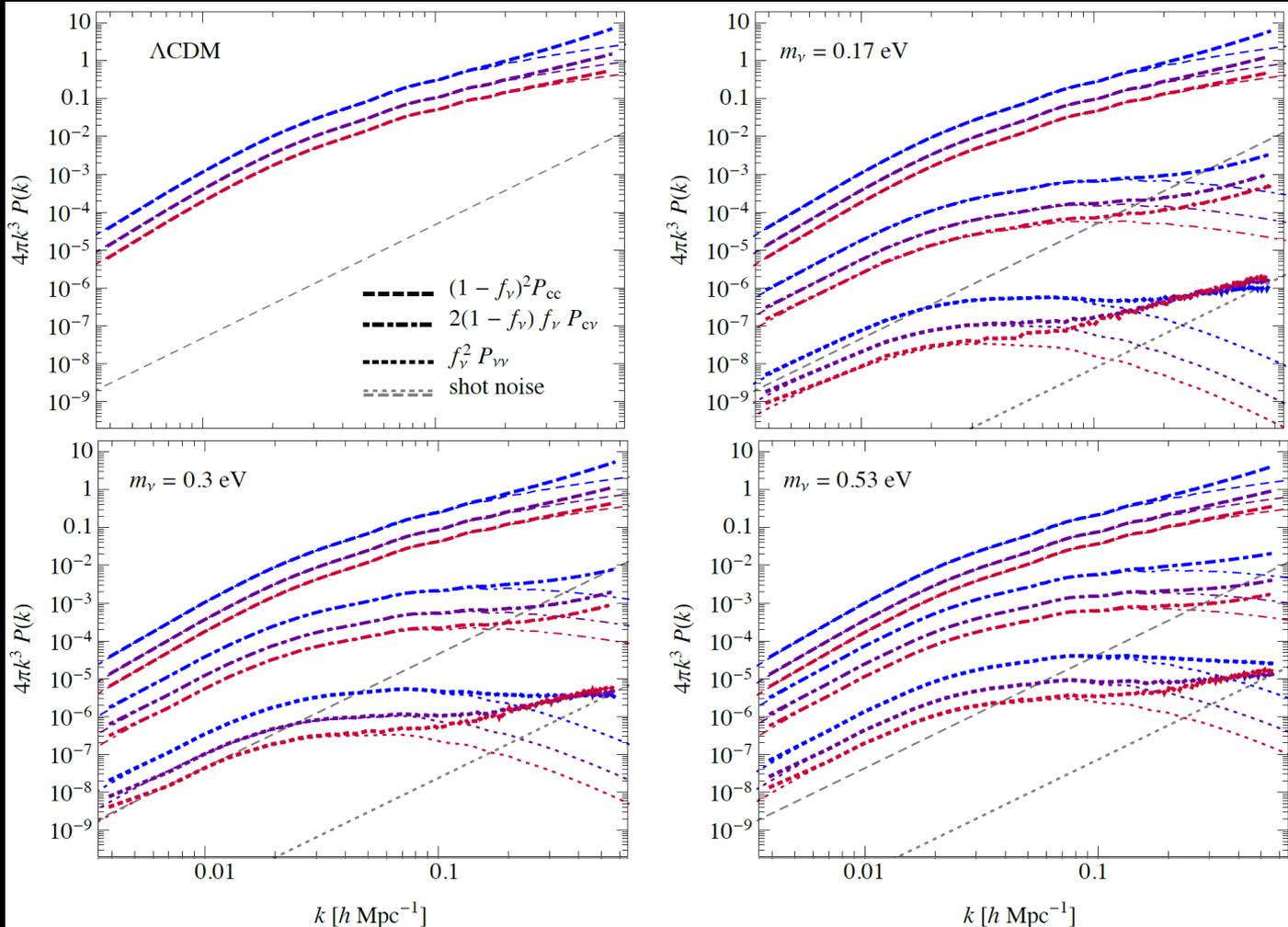
$N_{\text{cdm}}=512^3$

$N_{\nu}=1024^3$

$z_{\text{in}}=49$

# Different contributions to the total matter $P(k)$

Castorina, Carbone et al. 2015

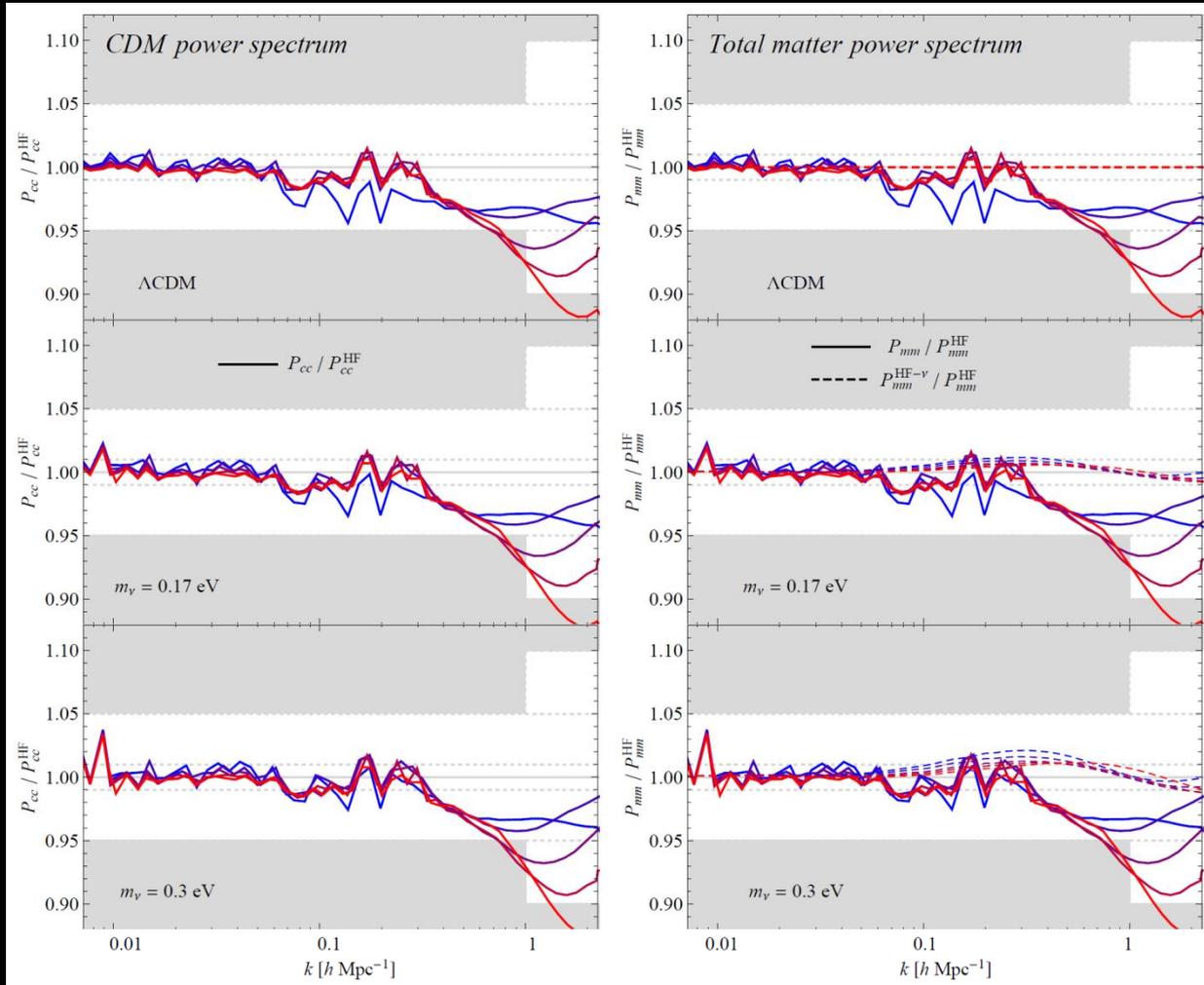


$$P_m(k; z) = (1 - f_\nu)^2 P_{cb}(k; z) + 2(1 - f_\nu)f_\nu P_{cb,\nu}(k; z) + f_\nu^2 P_\nu(k; z)$$

$P_m(k)$  is described at the 1% level accuracy up to  $k=1h/\text{Mpc}$ , assuming the nonlinear evolution of CDM alone, and the linear prediction for the other components

# Modifications to Halofit

Castorina, Carbone et al. 2015



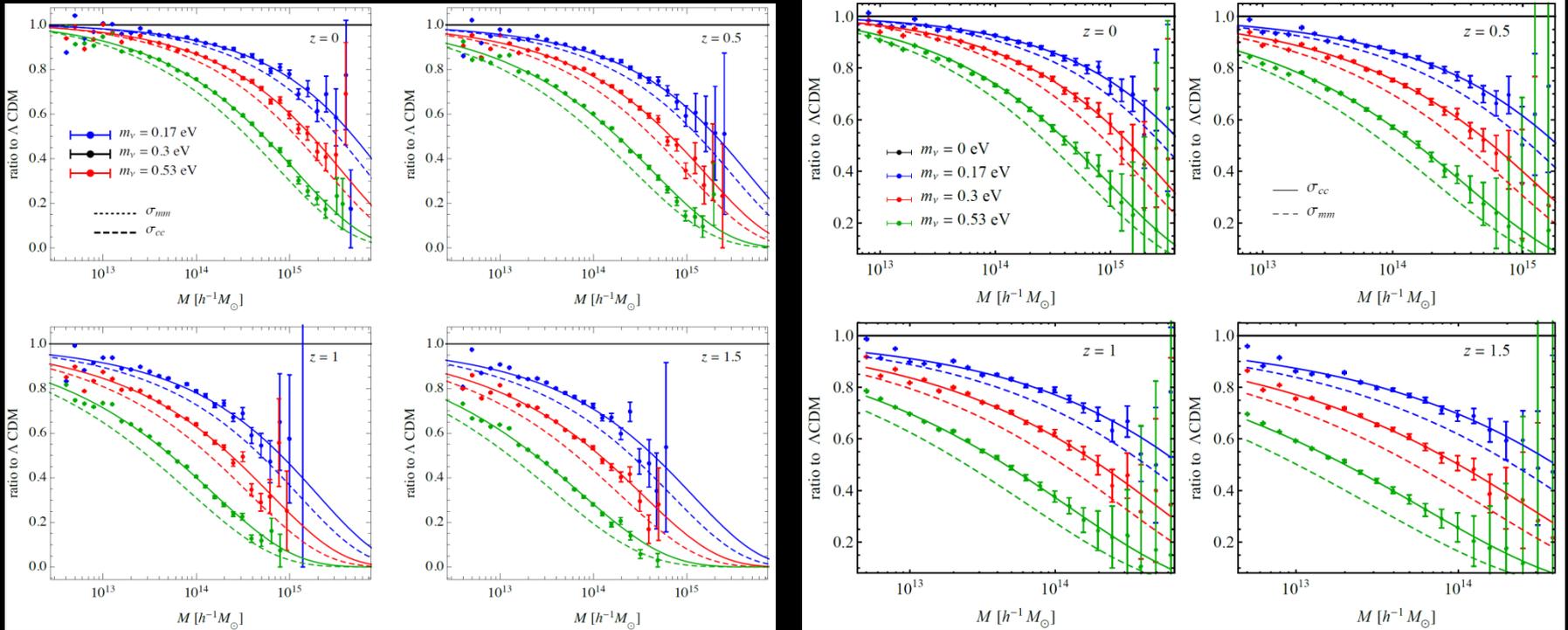
$$P_{mm}^{HF}(k) \equiv (1 - f_\nu)^2 P_{cc}^{HF}(k) + 2 f_\nu (1 - f_\nu) P_{c\nu}^L(k) + f_\nu^2 P_{\nu\nu}^L(k)$$

$$P_{cc}^{HF}(k) = \mathcal{F}_{HF}[P_{cc}^L(k)]$$

**HALOFIT mapping only for CDM, other contributions are assumed to be linear.**  
**Shaded areas denote regions beyond the accuracy expected from Halofit.**

# Halo Mass Function: FoF (MICE) vs SO (Tinker)

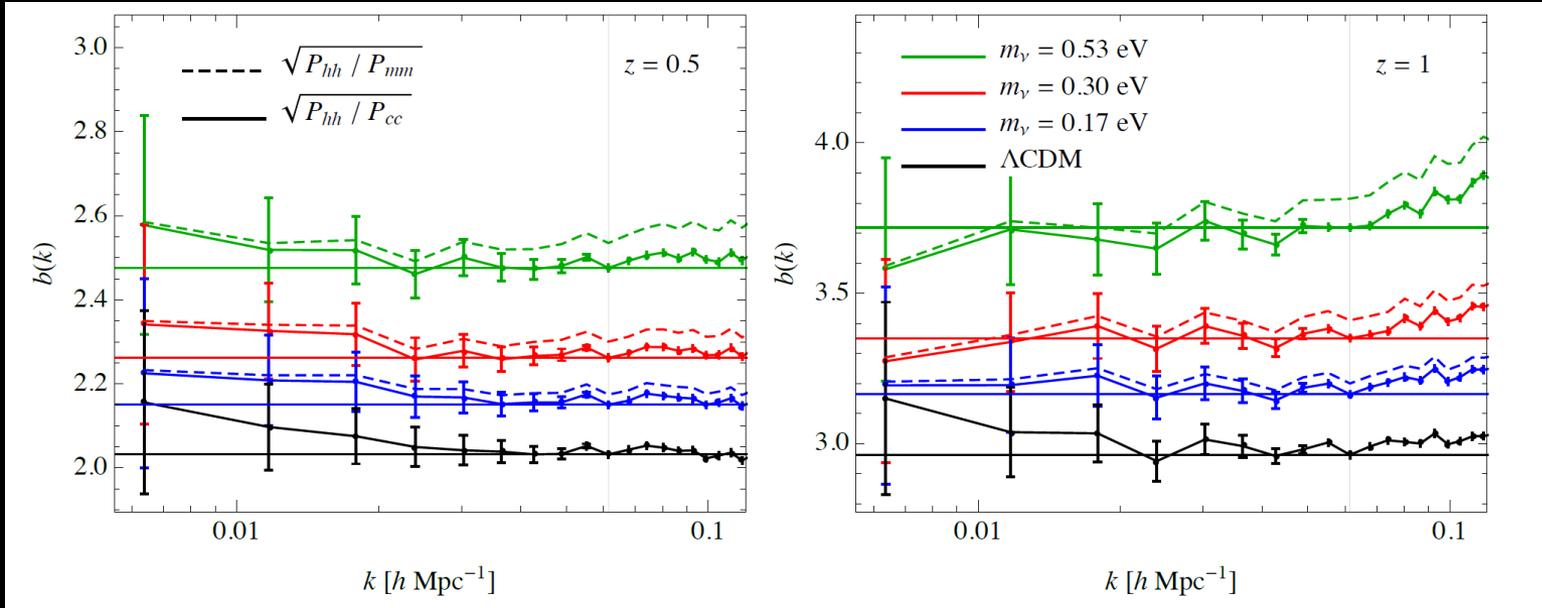
Castorina, Carbone et al. 2015



The  $\rho_{cc}$  and  $\sigma_{cc}$  prescriptions (Ichiki&Takada, 2012 & Castorina et al, 2014) allow to recover the theoretical MF for both FoF and SO halos

# Same conclusions for the bias

Castorina, Carbone et al. 2015

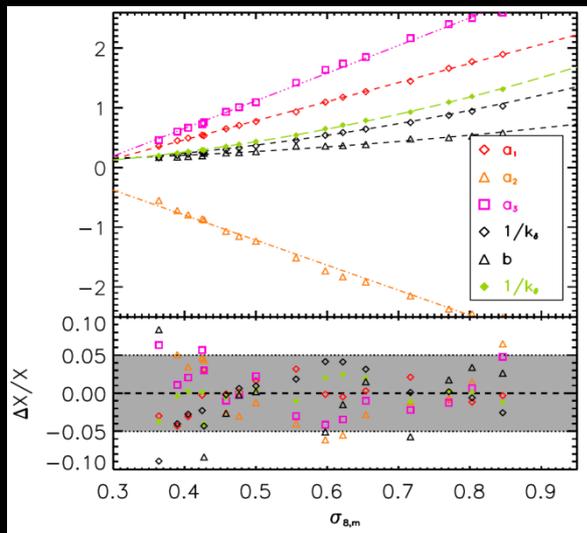


$$b_c = \sqrt{\frac{P_{hh}}{P_{cc}}}$$

$$b_m = \sqrt{\frac{P_{hh}}{P_{mm}}}$$

The  $\sigma_{cc}$  prescription mitigates the  $\nu$ -induced scale dependence of the bias at intermediate scales. The halo bias defined with respect to DM presents a spurious scale-dependence due to the difference between the cold and total matter power spectra.

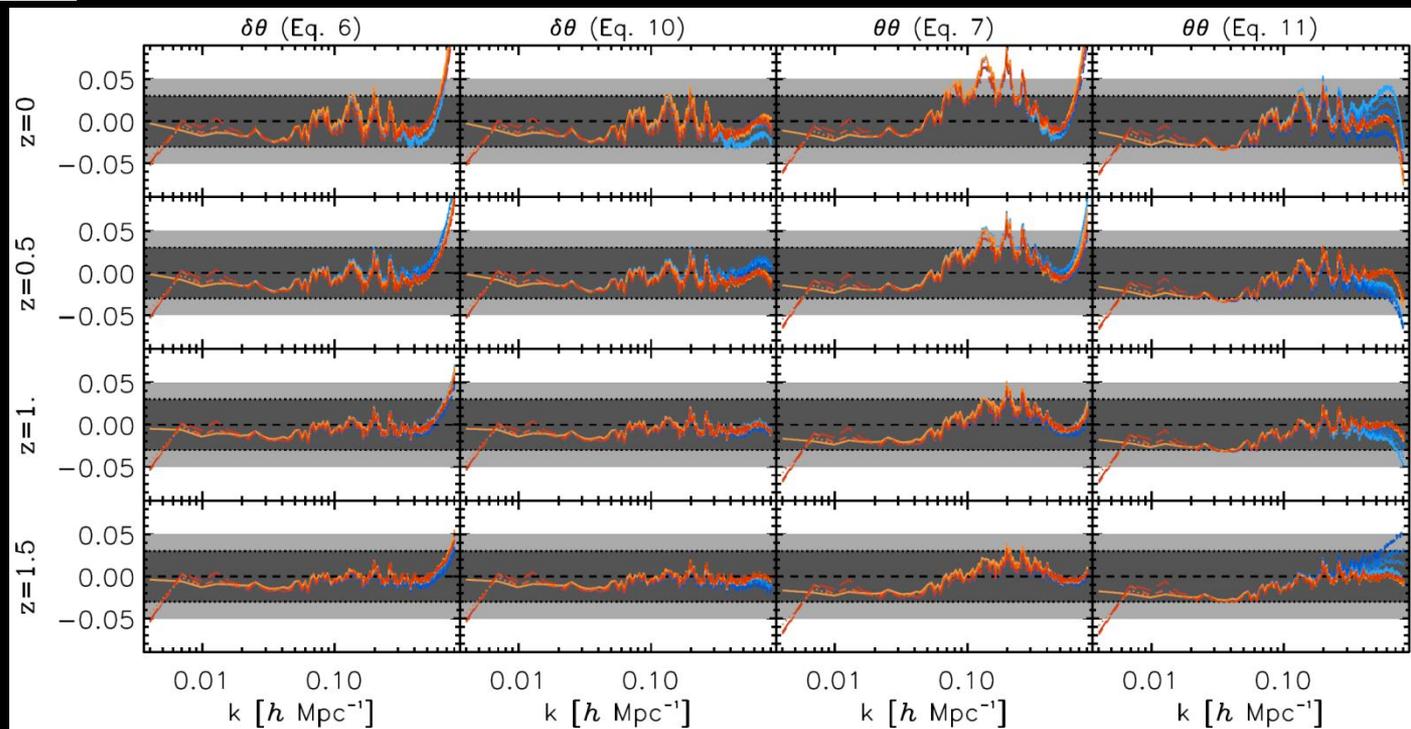
# Velocity spectra from DEMNUni: no $\sigma_{cc}$ prescription



$$\begin{aligned}
 a_1 &= -0.817 + 3.198\sigma_{8,m} \\
 a_2 &= 0.877 - 4.191\sigma_{8,m} \\
 a_3 &= -1.199 + 4.629\sigma_{8,m} \\
 1/k_\delta &= 0.111 + 3.811\sigma_{8,m}^2 \\
 b &= 0.091 + 0.702\sigma_{8,m} \\
 1/k_\theta &= -0.048 + 1.917\sigma_{8,m}^2
 \end{aligned}$$

$$P_{\delta\theta}(k) = \left\{ (P_{\delta\delta}^{\text{HF}}(k) P_{\theta\theta}^{\text{Lin}}(k)) \right\}^{\frac{1}{2}} e^{-\frac{k}{k_\delta}}$$

$$P_{\theta\theta}(k) = P_{\theta\theta}^{\text{Lin}}(k) e^{-\frac{k}{k_\theta}}$$



$$P_{\delta\theta}(k) = \left\{ (P_{\delta\delta}^{\text{HF}}(k) P_{\theta\theta}^{\text{Lin}}(k)) \right\}^{\frac{1}{2}} e^{-\frac{k}{k_\delta} - bk^6}$$

$$P_{\theta\theta}(k) = P_{\theta\theta}^{\text{Lin}}(k) e^{-k(a_1 + a_2 k + a_3 k^2)}$$

Bel et al. in prep

# Lensing and ISW-RS: no $\sigma_{cc}$ prescription

$$\Psi(\hat{\mathbf{n}}) \equiv -2 \int_0^{r_*} \frac{r_* - r}{r_* r} \frac{\Phi(r\hat{\mathbf{n}}; \eta_0 - r)}{c^2} dr$$

Lensing potential in the small-angle scattering limit (Born approximation)

$r$  = comoving distance  
from the observer

$$\Delta T(\hat{n}) = \frac{2}{c^3} \bar{T}_0 \int_0^{r_L} \dot{\Phi}(r, \hat{n}) a dr,$$

Total ISW-RS effect

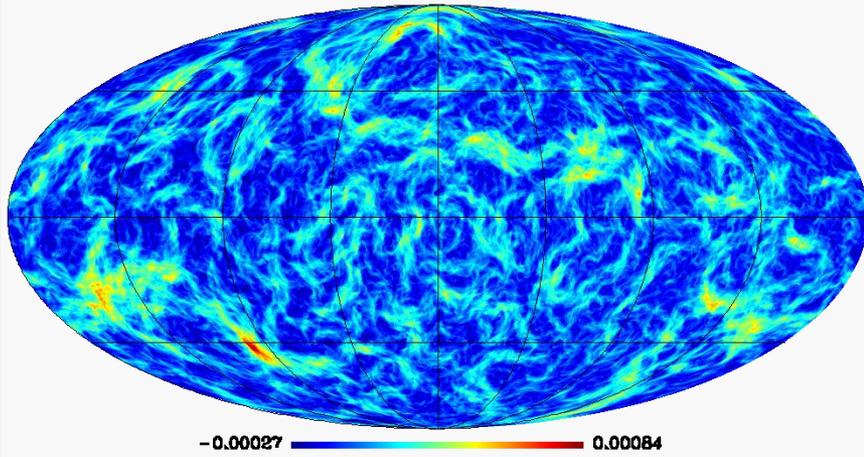
$$\tilde{X}(\hat{\mathbf{n}}) = X(\hat{\mathbf{n}} + \nabla\psi(\hat{\mathbf{n}}))$$

$$X = T, Q, U$$

Gradients in the grav. potential generated by LSS cause deviations in the CMB photon propagation from LS to us:

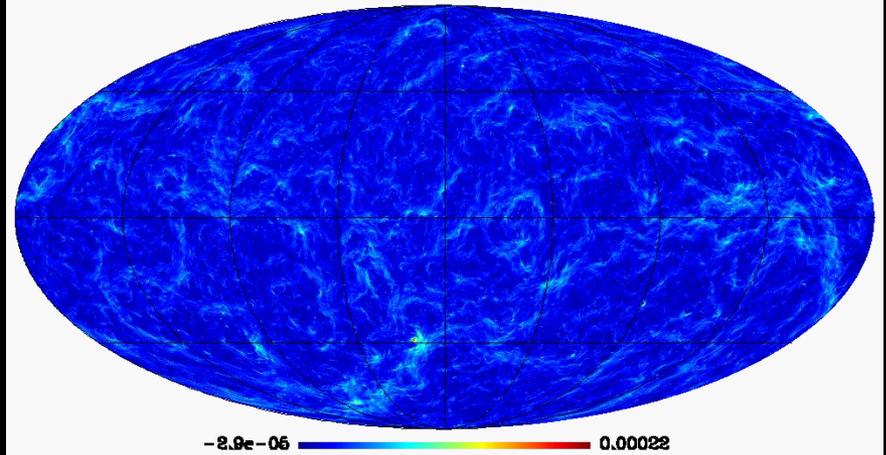
points in a direction  $\hat{\mathbf{n}}$  actually come from points on the last scattering surface in a displaced direction  $\hat{\mathbf{n}} = \mathbf{n} + \nabla\psi$

Planck-LCDM weak-lensing  $\alpha$ -modulus ( $z_s=1$ )

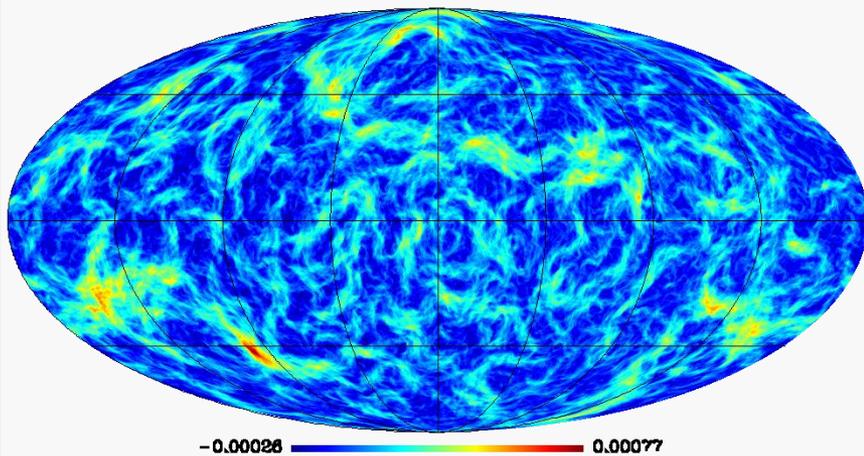


## Deflection angle maps for $z_s=1$

Difference between the LCDM and  $M_\nu=0.53$  eV deflections ( $z_s=1$ )

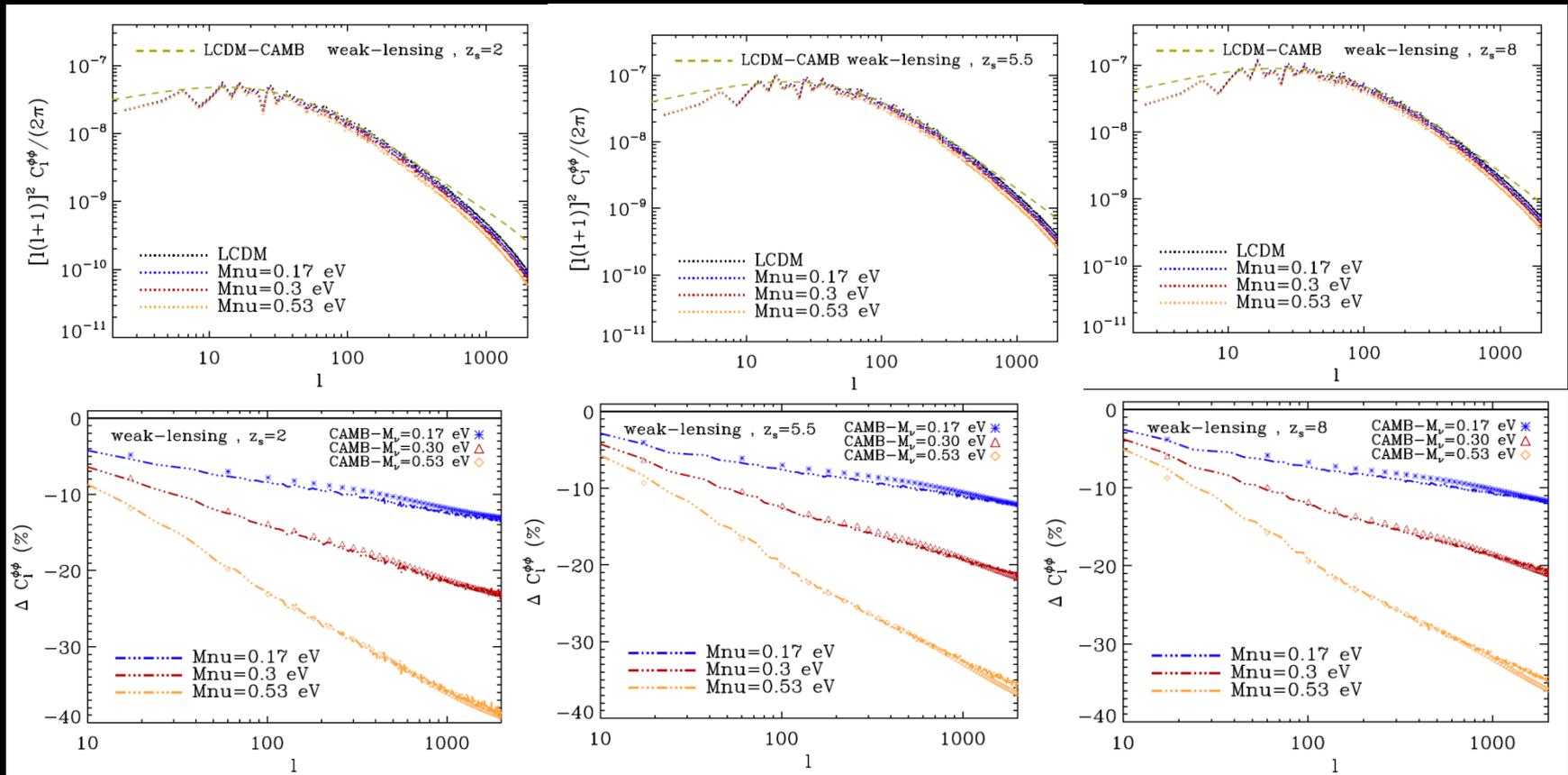


Planck- $M_\nu=0.53$  eV weak-lensing  $\alpha$ -modulus ( $z_s=1$ )



Carbone et al. 2016

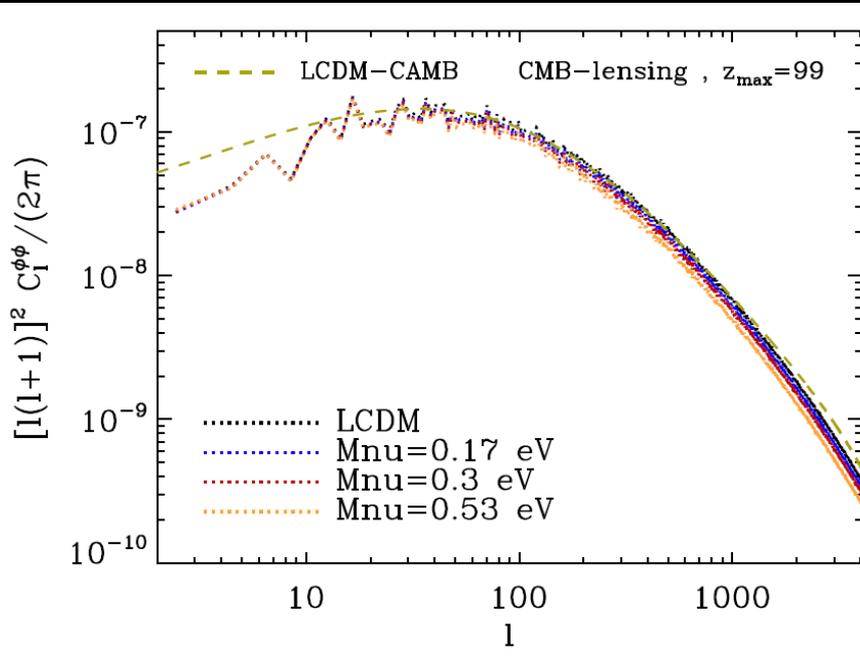
# Weak-lensing angular power spectra at different redshifts



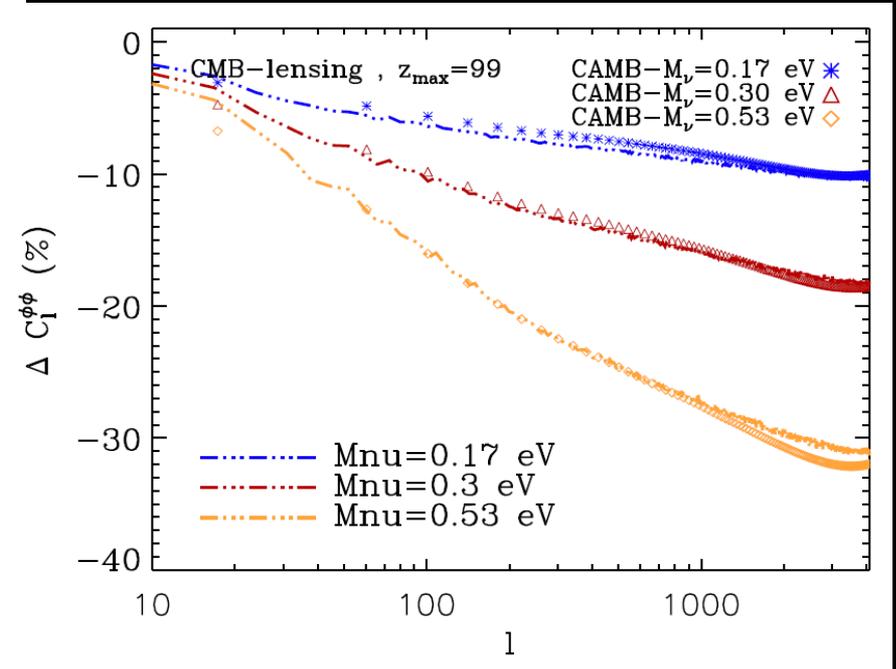
Carbone et al. 2016

**Lack of power on small scales due to grid resolution.  
The neutrino damping effect is correctly recovered up to  $l=2000$**

# CMB-lensing angular power spectra



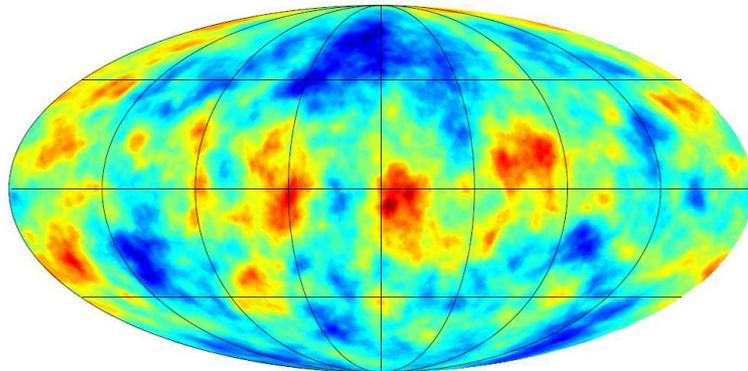
Power suppression is less than in the weak-lensing case since there is the contribution from higher  $z$



Carbone et al. 2016

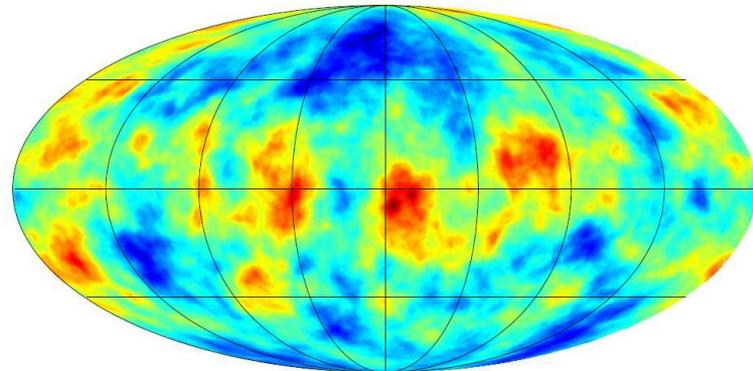
# CMB-lensing vs ISW/Rees-Sciama

Planck-LCDM ISW/RS map



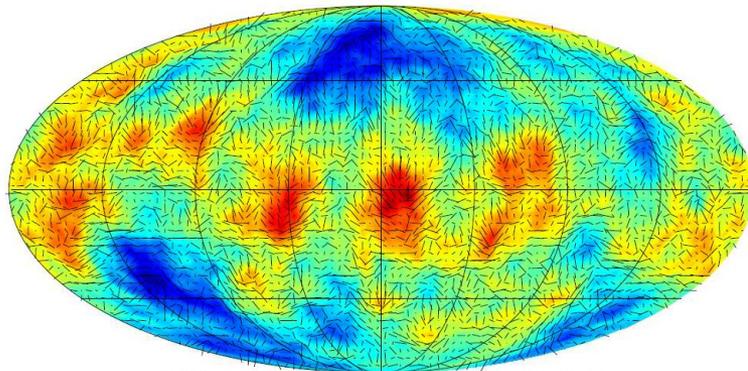
-43.5 50.3  $\mu\text{K}$

Planck- $M_\nu=0.53$  eV ISW/RS map



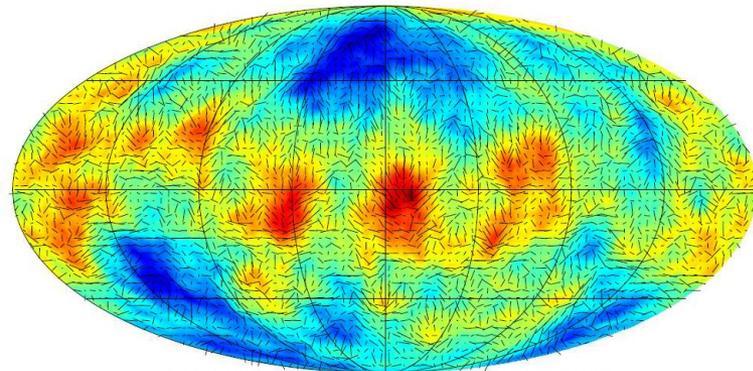
-44.2 51.6  $\mu\text{K}$

Planck-LCDM CMB-lensing potential map



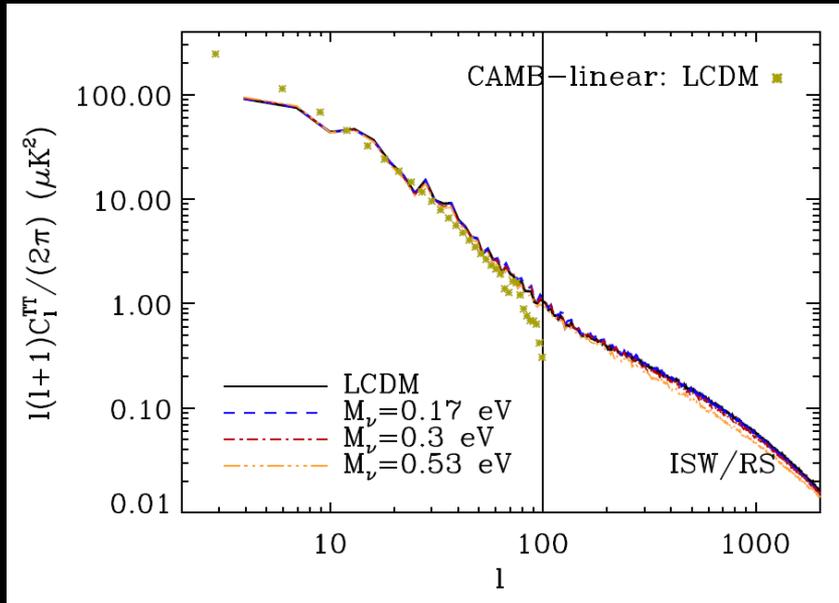
0.0028 -0.00022 0.00022

Planck- $M_\nu=0.53$  eV CMB-lensing potential map



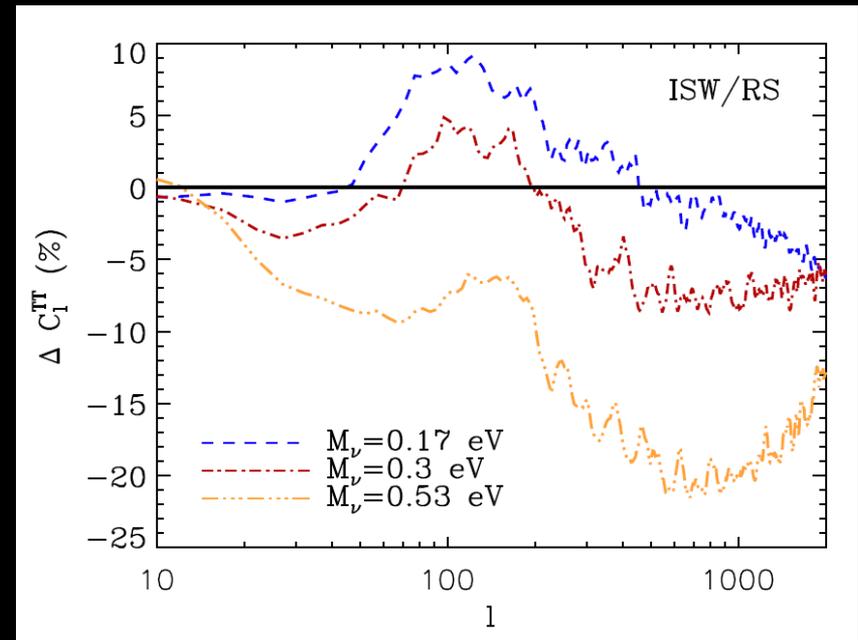
0.0027 -0.00022 0.00022

# ISW/Rees-Sciama angular power spectra



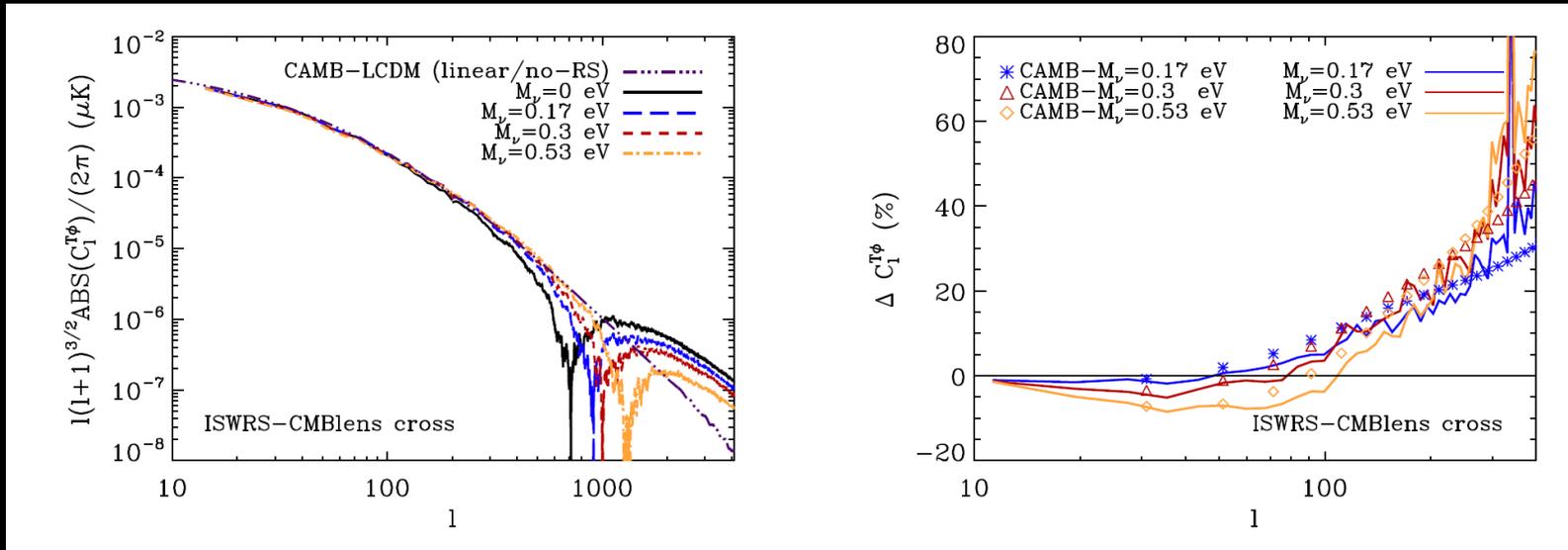
Carbone et al. 2016

At high redshift, the ISW effect would be null on all scales for  $M_\nu=0$ , while for  $M_\nu>0$  it is still active on small scales because of free-streaming.



$$k_{\text{fs}}(z) = 0.82H(z)/H_0/(1+z)^2(m_\nu/1\text{eV}) h\text{Mpc}^{-1}$$

# ISWRS-CMBlens cross correlation

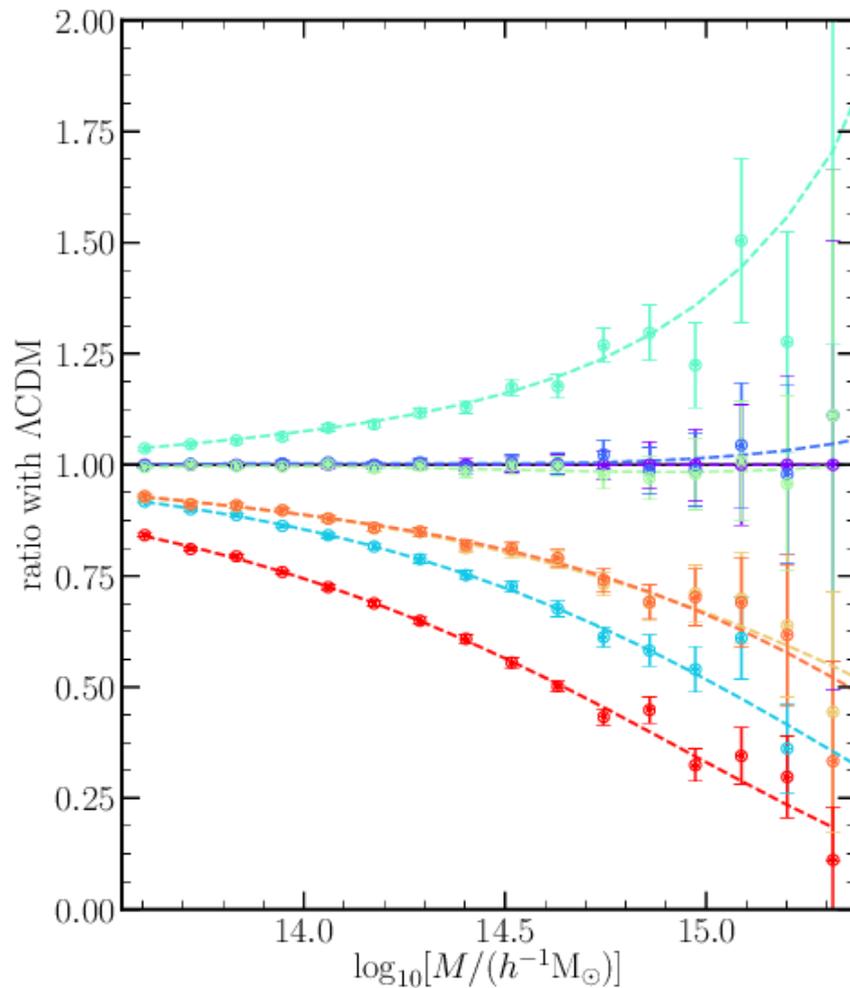
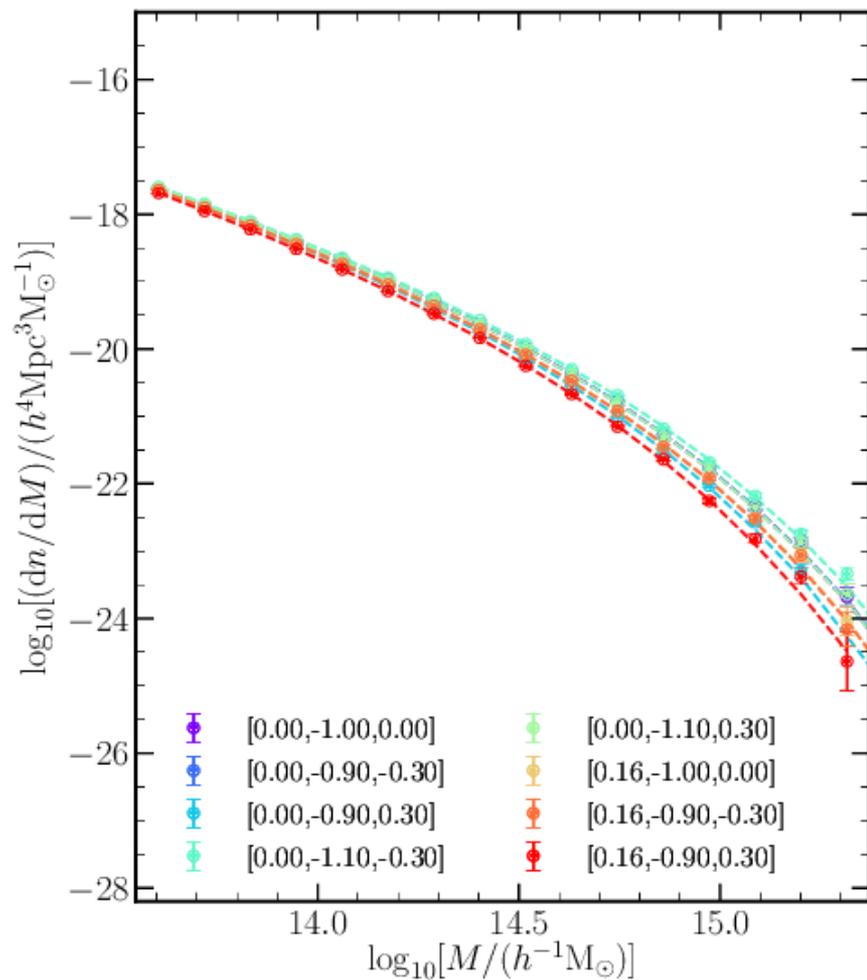


Carbone et al. 2016

**Sign inversion: the non-linear transition moves toward smaller scales with increasing neutrino mass**

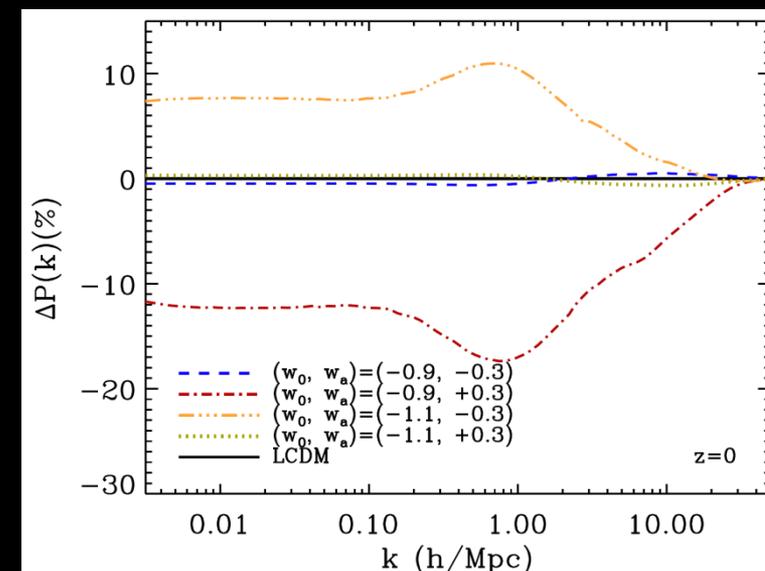
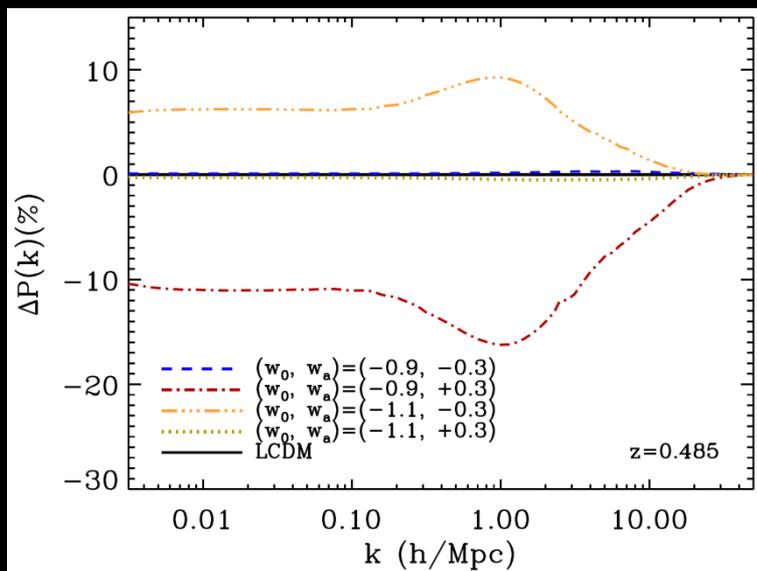
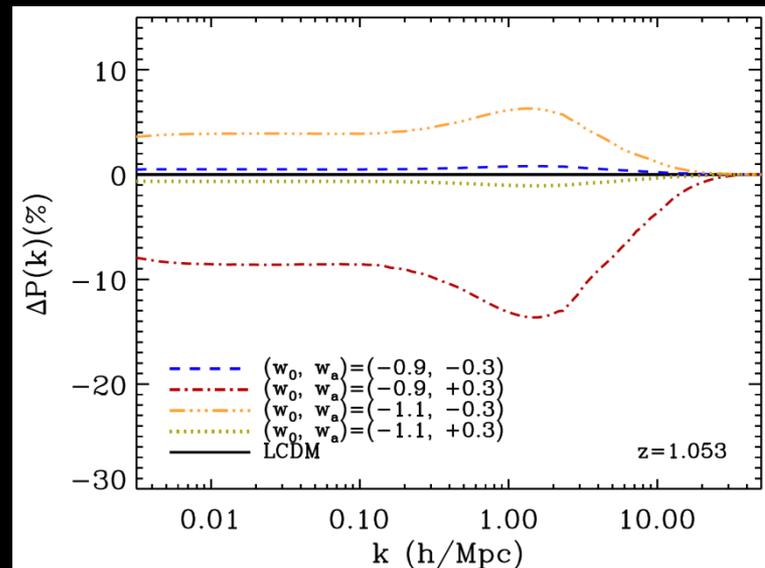
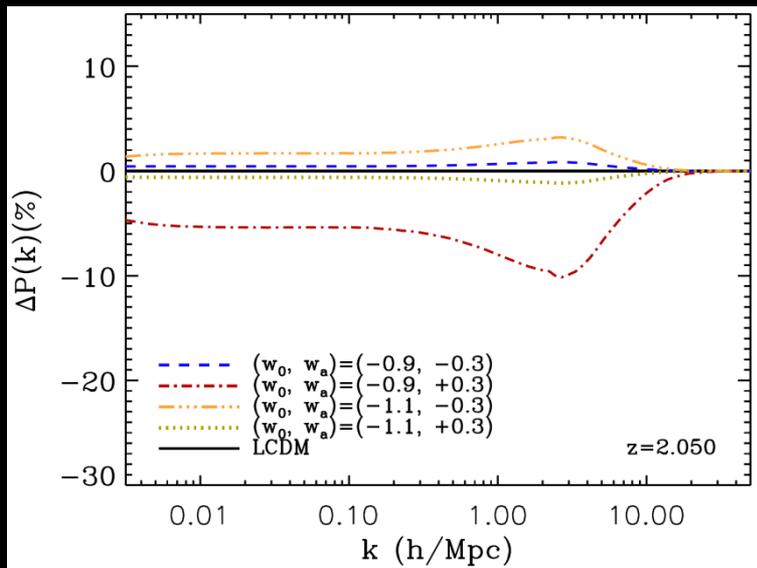
# DEMNUi-II: first results

FoF at  $z = 0.48551$

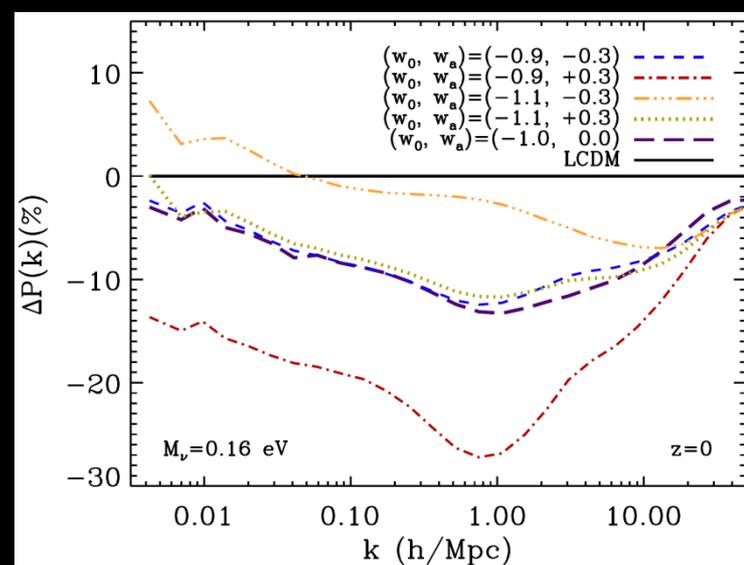
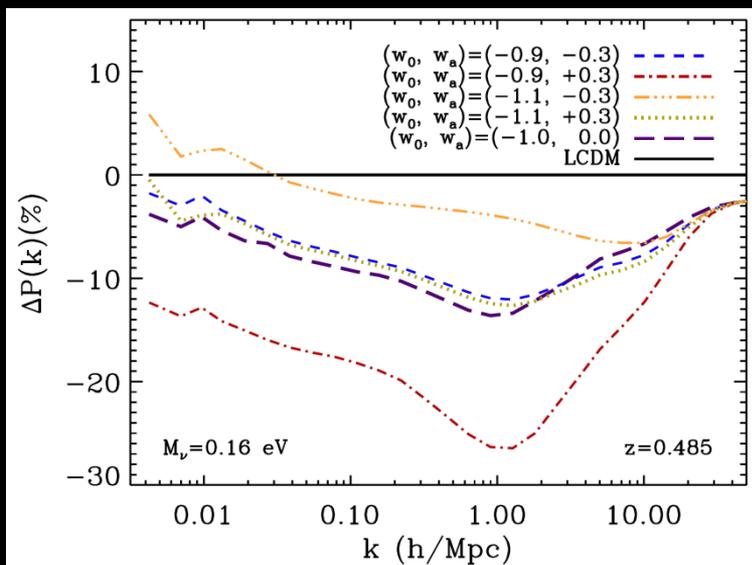
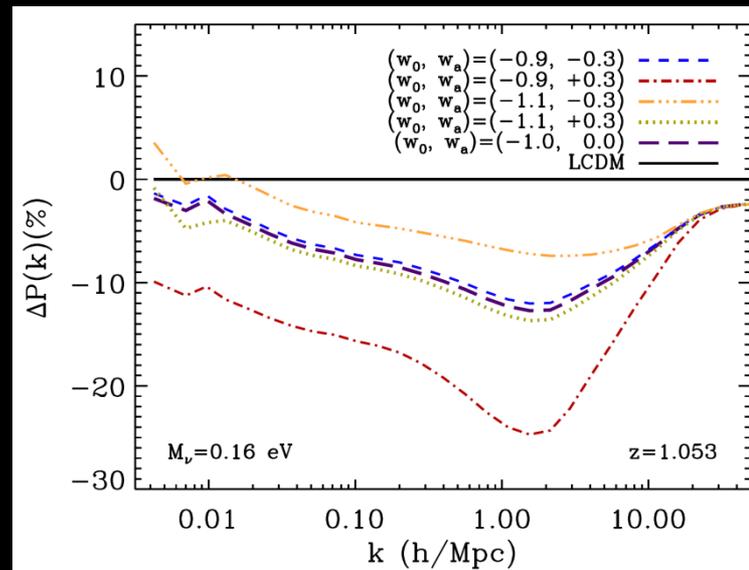
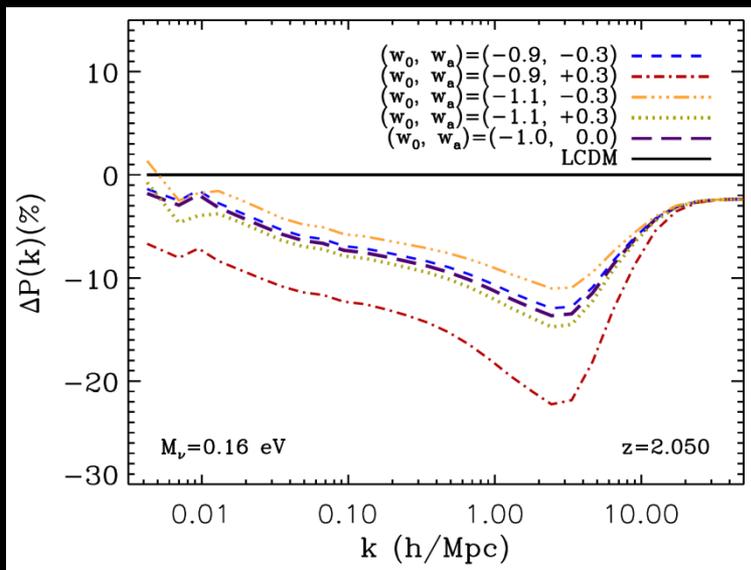


Carbone et al (in prep)

# DEMNUi-II: first results

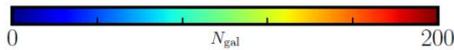
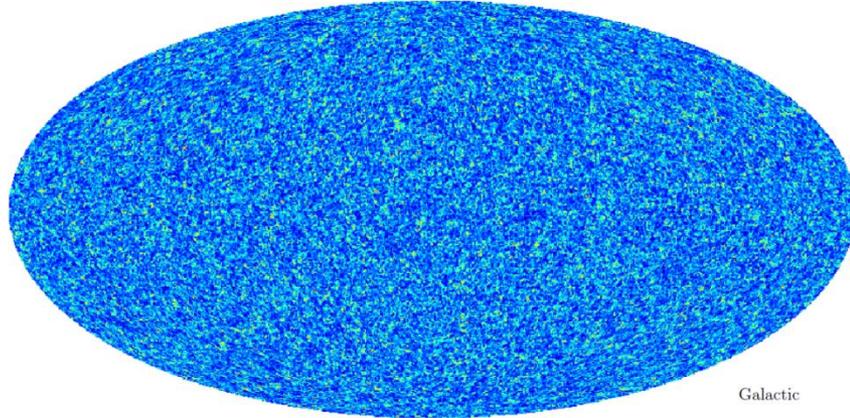


# DEMNUni-II: first results

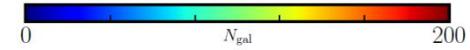
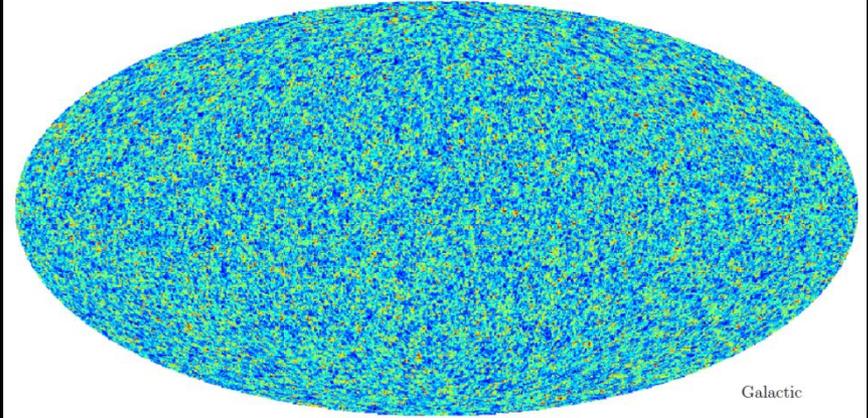


# DEMNUni: populating with galaxies

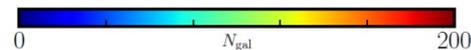
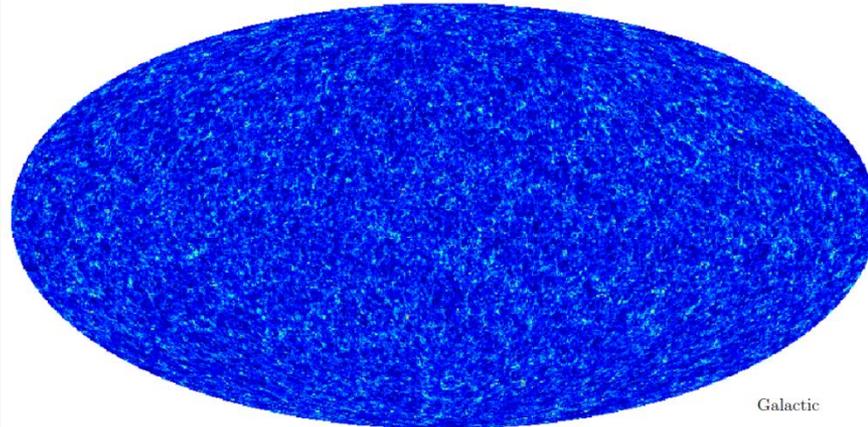
DEMNUni-I  $\Lambda$ CDM, snap 032,  $z = 2.05053$



DEMNUni-I  $\Lambda$ CDM, snap 040,  $z = 1.05352$



DEMNUni-I  $\Lambda$ CDM, snap 048,  $z = 0.48551$



HOD a la Zheng et al. (2007), fitting HOD parameters against SDSS galaxies with magnitude  $M_r < -20$

**MZ et al. in prep**

# Conclusion

- DEMNUni simulations – massive neutrinos and dynamical dark energy
- Confirmed nonlinear prescription for power spectrum applies to cold component alone
- Confirmed  $\sigma_{\text{cc}}$  prescription for mass functions
- Velocities and lensing require the total matter contribution (cold + neutrinos)
- Allows for the study of nonlinear ISW/RS
- Cross correlations of CMB/weak lensing with ISW/RS
- Soon → cross correlations with LSS
- Soon → calibration of emulators & study of covariances