

#### CMB lensing results from PLANCK

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on behalf of the Planck Collaboration





### CMB lensing from Planck

mostly based on 2 Planck papers:

#### Planck 2015 results. XV. Gravitational lensing



Planck lensing potential map: dark matter distribution at  $z^2$ 

## **CMB** lensing from Planck

mostly based on 2 Planck papers:

#### Planck 2015 results. XV. Gravitational lensing Lensing-induced *B*-mode map with Planck (internal reviewing)



Planck lensing-induced B-mode map

#### **CMB** lensing from Planck

mostly based on 2 Planck papers:

#### Planck 2015 results. XV. Gravitational lensing

Planck Collaboration: P. A. R. Ade<sup>91</sup>, N. Aghanim<sup>64</sup>, M. Arnaud<sup>78</sup>, M. Ashdown<sup>74,6</sup>, J. Aumont<sup>64</sup>, C. Baccigalupi<sup>90</sup>, A. J. Banday<sup>101,10</sup>, R. B. Barreiro<sup>70</sup>, J. G. Bartlett<sup>1,72</sup>, N. Bartolo<sup>33,71</sup>, E. Battaner<sup>103,104</sup>, K. Benabed<sup>65,100</sup>, A. Benoît<sup>62</sup>, A. Benoit-Lévy<sup>25,65,100</sup>, J.-P. Bernard<sup>101,10</sup> M. Bersanelli<sup>36,53</sup>, P. Bielewicz<sup>101,10,90</sup>, A. Bonaldi<sup>73</sup>, L. Bonavera<sup>70</sup>, J. R. Bond<sup>9</sup>, J. Borrill<sup>15,95</sup>, F. R. Bouchet<sup>65,93</sup>, F. Boulanger<sup>64</sup>, M. Bucher<sup>1</sup> C. Burigana<sup>52,34,54</sup>, R. C. Butler<sup>52</sup>, E. Calabrese<sup>98</sup>, J.-F. Cardoso<sup>79,1,65</sup>, A. Catalano<sup>80,77</sup>, A. Challinor<sup>67,74,13</sup>, A. Chamballu<sup>78,17,64</sup>, H. C. Chiang<sup>29,7</sup> P. R. C Coulais<sup>77</sup>. B P The scientific results that we present today are a product of the Planck otti<sup>49,90</sup>. J. Delabrou Collaboration, including individuals from more than 100 scientific . X. Dupac<sup>43</sup> Fraisse<sup>29</sup> G. Efstat institutes in Europe, the USA and Canada. Nuevo<sup>70,90</sup> E. France Harrison<sup>67,74</sup> K. M. Górsk Planck is a project folmes<sup>72</sup>. S. Henr of the European A. Horns Space Agency, with leihänen<sup>28</sup>. planck instruments ıäki<sup>2,48</sup> R. Ke provided by two I. Liguori<sup>33,71</sup> J.-M. Lama scientific Consortia undolesi52,34. P. B. Lilje<sup>6</sup> funded by ESA inhold<sup>31</sup> A. Mai member states (in Montier<sup>101,10</sup> A. Melchic particular the lead agenzia spaziale italiana countries: France erfield<sup>21</sup>. G. Mo DTU Space HEI PLANCK and Italy) with Paoletti<sup>52,54</sup> H. U. Nørg National Space Institute contributions from F. Pasian<sup>5</sup> Pietrobon<sup>72</sup>. Science & Technology CSIC NASA (USA), and Facilities Council Rachen<sup>22,84</sup> S. Plaszczy elescope reflectors National Research Council of Italy W. T. Reacl C. Rosset<sup>1</sup>. provided in a M. Rossetti collaboration avelainen<sup>28,48</sup> Deutsches Zentrum between ESA and a Sunvaev<sup>84,94</sup> für Luft- und Raumfahrt eV G. Savini<sup>88</sup> UK SPACE scientific D. Sutton<sup>67</sup> M. Tucci<sup>19</sup>. Consortium led and J. Tuovi Wehus<sup>72</sup>, funded by Denmark. NERSC SDC 1 - C 0 SUBM UNIVERSITÉ DE GENÈVE esa TORONTO

- CMB lensing reconstruction: data and hint of methodology
- Lensing potential results
- Lensing potential implications for Cosmology
- Lensing-induced B-mode, results and implications

#### Gravitational Lensing by large-scale Structure



Remapping:  $X(\mathbf{n}) = X^{\text{primo}}(\mathbf{n} + \nabla \phi(\mathbf{n})), \quad X \in \{T, Q \pm iU\}$ 

Lensing potential: 
$$\phi(\hat{\mathbf{n}}) = -2 \int_{0}^{\chi_{*}} d\chi \left( \frac{\chi_{*} - \chi}{\chi_{*} \chi} \right) \Psi(\chi \hat{\mathbf{n}}; \eta_{0} - \chi)$$
 • max. efficiency at z~2  
• typical size ~300 Mpc  
• linear growth

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#### **Observational signature**



Lensing typical scales:

- deflection scale  $\simeq$  2.5 arcmin (rms)
- correlation length  $\simeq$  2 degrees

Signatures:

- power spectra smoothing ( $\simeq$ 10% at high-I)
- secondary B-mode (dominates at I > few 100)
- inducing NG

$$\delta X(\mathbf{n}) \sim \nabla \phi(\mathbf{n}) \cdot \nabla X^{\text{primo}}(\mathbf{n}), \quad X \in \{T, Q \pm iU\}$$

Using the NG signature in the maps, the underlying phi potential can be reconstructed

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# **CMB Lensing Reconstruction Basics**

 $\phi$  map reconstruction using *quadratic estimators* 

T. Okamoto & W. Hu [ astro-ph/0301031 ]

$$\hat{\phi}_{LM}^{(XZ)} = A_L^{(XZ)} \sum_{\ell_1 m_1} \sum_{\ell_2 m_2} \mathcal{G}_{LM\ell_1 m_1 \ell_2 m_2}^{(XZ)} \bar{X}_{\ell_1 m_1} \bar{Z}_{\ell_2 m_2} \quad (X, Z) \in \{T, E, B\}$$
filtered versions of  $\{T, E, B\}$  maps
normalisation and filters optimisation  $\Rightarrow$  unbiased, minimum variance estimator
NB: tractable computation in real-space :  $\hat{\phi}_{LM}^{(XZ)} = A_L^{(XZ)} \int d\mathbf{n} \nabla_s Y_{LM}^*(\mathbf{n}) \cdot [\bar{X}(\mathbf{n}) \nabla_s \bar{Z}(\mathbf{n})] \quad (X, Z) \in \{T, Q \pm iU\}$ 
 $\hat{\phi}_{LM}^{(\mathrm{mv})} = \sum_{XZ} w_L^{XZ} \hat{\phi}_{LM}^{(XZ)}$  Minimum-Variance combination (TT, TE, EE, EB, TB)
 $\hat{C}_L^{\phi\phi}$  reconstruction using the 4-point correlator information
 $\hat{C}_L^{\phi\phi} = \frac{1}{(2L+1)} \sum_M |\hat{\phi}_{LM}|^2 - N_L^{(0)} - \mathcal{O}(C_L^{\phi})$ 
Gaussian bias: disconnected part of the 4-pt correlator
 $\frac{\delta_L^{\phi}}{M} = \frac{1}{M} =$ 

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# Reconstruction from the data

1. data processing steps from timelines to map are critical



2. Astrophysical foregrounds are the major concern

We exploit Planck frequency coverage to clean them (component separation)

- Masks:
  - detected point sources radio/IR galaxies using PCCS I/II Planck 2013 results. XXVIII / 2015
    - SZ clusters using PCC I/II Planck 2013 results. XXIX / 2015 XXVII
    - Cold Cores using CC I/II Planck Early Results. VII / 2015 XXVIII
  - diffuse emission • galactic plane Planck 2013 results. XII / 2015 X
    - CO regions Planck 2013 results. XIII / 2015 VIII
- $\rightarrow$  masks induce the dominant bias at  $\phi$  map level

#### **Reconstruction from the data**

Debiasing at the map level :

Any effects breaking the spatial isotopy of the maps (e.g. masks, inhomogeneous noise) induce spurious  $\phi$ Bias correction using Monte-Carlo simulation (that includes all known bias sources) :

$$\hat{\phi}^{(\mathrm{c})} = \hat{\phi} - \langle \hat{\phi} \rangle_{\mathrm{MC}}$$

Our power spectrum estimator :



# Data (2013 vs 2015)

Planck lensing 2013 baseline T map:

- 15.5 months of data integration
- MV combination of 143 and 217 GHz maps
- corrected for a dust template using the 857GHz map
- $\simeq$  60% of the sky (after apodization)

Planck lensing 2015 baseline {T, Q, U} maps:

- about 30 months of data
- foreground cleaned maps using SMICA
- ICA using the 9 frequency maps Planck 2015 results. XII
- $\simeq$  70% of the sky
- bandpass filtering  $~100 \leq \ell \leq 2000$



## Reconstructed $\boldsymbol{\varphi}$ map











# Correlation with other LSS tracers

External data Planck 2014 XVII (Lensing)

- 20 sigma correlation with NVSS radio galaxies and quasars ( $z_{mean} = 1.1$ )
- 10 sigma with SDSS Luminous Red Galaxies ( $z_{mean} = 0.55$ )
- 7 sigma with the WISE satellite IR galaxies catalog ( $z_{mean} = 0.1$ )

Planck's Cosmic Infrared Background (CIB)

unresolved high-redshift dusty star-forming galaxies
dominant extra-galactic emission at > 353GHz

• first detection (42 sigma) of a correlation between 545GHz T and lensing maps :



Stacking of the φ map at the location of : 20 000 T hot spots 20 000 T cold spots 1° 1° Planck 2014 XVIII (CIB-Lensing)

• helps in probing the origin of the CIB hence in constraining the star formation history

# Correlation with the ISW effect

#### **ISW: Integrated Sachs-Wolfe effect** • At late-time, gravitational potentials induce a secondaries $\frac{\Delta T}{T_{\rm CMB}} = \frac{2}{c^3} \int_{\eta_*}^{\eta_0} d\eta \frac{d\Psi}{d\eta}$ credit K. Benabed ESLAB 2013 • that correlate to the $\phi$ map ISW-lensing bispectrum (T $\phi$ cross-correlation) 2ISW results Planck 2015 results XXI (ISW) Planck T x $\phi$ $: 3\sigma$ detection (20% improvement wrt 2013) $L^{3}C_{L}^{T\phi}$ $[10^{-2}\mu{\rm K}]$ Planck T x LSS : $2.9\sigma$ detection : $4\sigma$ detection Joint

Implications

- 3  $\sigma$  detection of  $\Omega_{\Lambda}$
- important bias to the CMB primordial non-Gaussianity (from inflation) that must be subtracted Planck 2015 results XVII (non-Gaussianity)

0

50

L

70

90

30

10

Shallowing of the potential due to

expansion driven by dark energy

-  $\hat{\phi}^{MV}$ 

# Other cross-correlation studies

Further cross-correlation between the released 2013 and 2015  $\phi$  maps to the community and...

- Thermal SZ (detection at 6.2  $\sigma$ )
  - Detection of Thermal SZ -- CMB Lensing Cross-Correlation in Planck Nominal Mission Data, J. Colin Hill, David N. Spergel, arXiv:1312.4525
- Herschel selected galaxies at z > 1.5 (detection at 20 σ) Cross-correlation between the CMB lensing potential measured by Planck and high-z sub-mm galaxies detected by the Herschel-ATLAS survey,
   F. Bianchini, P. Bielewicz, A. Lapi, J. Gonzalez-Nuevo, C. Baccigalupi, G. de Zotti, et al. arXiv:1410.4502
- Fermi-LAT  $\gamma\text{-ray}$  map (detection at 3  $\sigma\text{)}$

Evidence of cross-correlation between the CMB lensing and the gamma-ray sky, N. Fornengo, L. Perotto, M. Regis, S. Camera, arXiv:1410.4997

• CFHTLenS galaxy number density

Cross-Correlation of CFHTLenS Galaxy Number Density and Planck CMB Lensing, Y. Omori, G. Holder, arXiv:1502.03405

• CFHTLenS weak lensing

Cross-correlation of Planck CMB Lensing and CFHTLenS Galaxy Weak Lensing Maps, Jia Liu, J. Colin Hill, arXiv:1504.05598

## Main result: the lensing power spectrum



#### Individual estimators



15 consistent φφ measurements dominant contribution from TT and TE

#### **Robustness tests**



As in 2013, the 2015 results pass a wealth of consistency checks including:

- robustness to foregrounds
- data splitting consistency
- robustness to bias at map-level

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#### $\oint f_{\rm skv} = 0.8$ The conservative case $f_{\rm skv} = 0.6$ ٥ SNR = 10SNR = 4.20 $\diamond$ 2013 Comparison to results using different galactic/point sources masks (baseline : fsky=0.7, SNR=5) $\Delta/\sigma$ <u>\_\_\_\_\_</u>\_\_\_\_ 100 500 1000 1500 2000 10 2 Llarger scatter than expected (from MC sims) 2015

 $[L(L+1)]^2 C_L/2\pi \ [ imes 10^7]$ curl-modes null test 2 Namikawa et al. [astro-ph/1110.1718]  $\mathbf{d} = \nabla \phi$  : curl-free we construct an estimator of  $\mathbf{d}^{\mathrm{curl}} = \star \nabla \psi$ -2  $TT(\times 10)$ 500 1000 10 100 $\sim 3\sigma$  non-zero feature over 400<L<2000 conservative interval Large map-level Large  $N_1^{(0)}$  correction used for Cosmology 400 2000 L = 840 debiasing retains 90% of the S/N

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15 /27

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방법은 1월 20일 (1997) - 1997 - 199 1997 - 1 1997 - 19 - 1997

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#### Consistency with the Planck base LCDM model

16/2

• Measure of a freely floating A that scales  $C_L^{\varphi\varphi}$ 

 $A_{\text{lens}} = 0.95 \pm 0.04$  Planck TT + lowP + lensing

LCDM6 model: good description of the universe at  $z \leq 5$ 

• Measure of a freely floating A that scales the lensing smoothing of  $CI^{TT}$ ,  $CI^{TE}$ ,  $CI^{EE}$ 

$$A_{\text{lens}}^{\text{smooth}} = 1.22 \pm 0.10 \quad \text{Planck TT} + \text{lowP}$$

 $C_{I}^{TT}$  favors higher lensing power amplitude to accomodate the tension to the « 20<I<30 dip »



# Constraints on the LCDM model

Information on the matter up to last-scattering  $\xrightarrow{}$  constraints on the post-recombination evolution



## Constraints on extension to the base LCDM model

Geometrical degeneracy breaking in a non-flat Universe

CMB alone (Planck TT + lowP + lensing)

- imposes a flat-geometry at sub-percent level;
- x3 improvement of errors over TT+lowP alone
- $\lesssim 3\sigma$  evidence of Dark Energy
- Constaints on the neutrino sector
  - for  $\sum_{\nu} m_{\nu} \lesssim 1.3 \,\text{eV}$  (i.e. v still relativistic at recombinaison): tiny constraints from TT alone
  - oscillation measure:  $\sum_{\nu} m_{\nu} \ge 0.06 \, \mathrm{eV}$  at least 2  $\nu$  non-relativistic (NR) today
  - After the NR transition: contribution to the expansion rate but not to the clustering of small-scale structure.
  - $\bullet$  Step-like signature in  $C_L{}^{\varphi\varphi}$

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#### Constraints on neutrino masses

In a 
$$\Lambda$$
CDM6 +  $\sum_{\nu} m_{\nu}$  model with  $N_{\text{eff}} = 3$  degenerate massive neutrinos:  
 $\sum m_{\nu} < 0.72$  95%; Planck TT + lowP  
 $\sum m_{\nu} < 0.68$  95%; Planck TT + lowP + lensing

mild improvement (whereas we expected a x2 improvement !)

Explanation: a combination of 2 effects:

 $\bullet$  TT disfavors large  $m_{\!_{\rm V}}$ 

large  $m_v$  yields

- $\rightarrow$  lower lensing smoothing
- → less level-arm to accomodate to the « low-ell dip »
- $\varphi\varphi$  autorises large  $m_{\nu}$  slight trough at around L=200

Best limit:

 $\sum m_{\nu} < 0.23$  95%; Planck TT + lowP + lensing + external data

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# Lensing-induced B-mode

Iensing-B polarization maps:

At first-order in  $\boldsymbol{\varphi}$ 

$$\left(Q^{\text{lens}} \pm iU^{\text{lens}}
ight) = \nabla \left(Q^{\text{primo}} \pm iU^{\text{primo}}
ight) \cdot \nabla \phi$$
  
 $B_{\ell m}^{\text{lens}} = \sum_{LM} \sum_{\ell' m'} \phi_{LM} E_{\ell' m'}^{\text{primo}} \mathcal{G}_{\ell L \ell'}^{mMm'}$   
W. Hu [ astro-ph/0001303 ]

A lensing-B map template can be synthesized using

• the PLANCK polarization maps (keeping pure E-mode contribution)

- and PLANCK lensing potential estimate (or another  $\boldsymbol{\varphi}$  tracer)

Iensing-B power spectrum:

When cross-correlated to the observed polarization maps, the lensing-B polarization maps provide a lensing B-mode power spectrum measurement :

$$\hat{C}_{\ell}^{B_{\text{lens}}} = \frac{f_{\text{sky}}^{-1}}{2\ell + 1} \sum_{m} B_{\ell m}^* \hat{B}_{\ell m}^{\text{lens}}$$

# The lensing-B synthesis methods

We developped 2 independent methods...

main difference in the sky cuts treatment; different implementions / same mathematics

- spherical-harmonics space-based method
  - used in the Planck 2015 lensing paper
  - mask treatment: minimum-variance filtering of T and P
  - based on the baseline lensing extraction of Planck 2015 lensing

$$\hat{B}_{\ell m}^{\text{lens}} = \mathcal{B}^{-1} \sum_{LM} \sum_{\ell' m'} \tilde{\phi}_{LM} \tilde{E}_{\ell' m'} \mathcal{W}_{\ell L \ell'}^{mMm'}$$
weight function

(geometrical terms)

- real-space based method
- developped for the Planck 2015 lensing B-mode map paper
- mask treatment: inpainting of T and apodization
- based on the Planck 2013 lensing METIS extraction method applied to full-mission data

$$\left(\hat{Q}^{\text{lens}} \pm i\hat{U}^{\text{lens}}\right) = \mathcal{B}^{-1}\nabla\left(\tilde{Q}^E \pm i\tilde{U}^E\right)\cdot\nabla\tilde{\phi}$$

Filtered version of pure E-mode Q, U maps

filtered lensing potential map

- filters are optimised to minimise the map variance
- $\mathcal{B}^{-,1}$  the analytical filtering transfer function ensures the estimator is unbiased

...that give equivalent results

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## The lensing-B map

 $ilde{B}^{
m lens} = \sum_{\ell m} \mathcal{F}_{\ell} \hat{B}^{
m lens}_{\ell m} Y_{\ell m}$  using 2 different filters

Full-resolution Wiener-filtered B-lensing, nside=2048, FWHM=10 arcmin

Large scales Wiener-filtered B-lensing, nside=256, FWHM=60 arcmin

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-0.50

.0 micro Rencontres du Vietnam, August 16-22, 2015

30152

0.50 micro K

PRELIMINARY

#### Lensing B power spectrum measurements

Results using different mass tracers:



#### Foreground residuals robustness tests

PRELIMINARY Using foreground-cleaned T, Q, U from different component separation methods [Ref: Planck results XI 2015] with a common  $f_{
m skv}\simeq 70\%$  mask



#### **Comparison to external measurements**

direct B-mode measurements (i. e. auto-Cl of the observed B-mode)



- → no bias at multipole relevant for primordial B-mode search
- $\twoheadrightarrow$  the most accurate B-lensing measurement to date up to  $\ell \lesssim 1000$

PRELIMINARY

# What is the lensing B map useful for ?

 Measuring the lensing B at the largest angular scales

better than rebuilding a template using  $\varphi^{\text{MV}}$ 

Bicep2/Keck :  $\Delta A_{Blens} = 0.15$   $A_{lens} = 1.13 \pm 0.18$  [BKP analysis] POLARBEAR SPTpol lensing B at 100<ell<300



BK + Planck dust + B-lensing

4

-

1.6

4.

. ₽ <u>1</u>.2 uncertainty BK LiteBIRD  $A_{\rm lens}$  $A_{\rm lens}$ 1.0 <u>1</u>.0 reduction [Ade++ 2015] [Matsumura++ 2014] 0.8 ω [see M. Hazumi's talk] o. 0.6 0.6  $\delta(\Delta A_{\text{lens}})$ 36% ( $\Delta A_{lens} = 0.12$ ) 20% ( $\Delta A_{lens} = 0.03$ ) LB + Planck dust 0.4 0.4 B-lensing  $\delta(\Delta r)$ 34 0.00 0.10 0.15 0 2 5 0.05 6 5% ( $\Delta r = 0.03$ ) 1 15% ( $\Delta r = 1.8 \times 10^{-3}$ )  $A_{\rm dust}$ rL. Perotto 26/27 Rencontres du Vietnam, August 16-22, 2015

# Conclusions

Planck has measured the first nearly full-sky map of the integrated mass distribution (thanks to its observational performancies + high systematic control in the data-processing)

- S/N ≈ 1 at large angular scales (35% uncertainties improvement over the 2013 results)
- valuable dark matter tracer for corss-correlation studies: e.g. first detection of the CIB-Lensing (46s) and ISW-lensing

The lensing power spectrum is measured at 2.5% precision level (best measurement to date)

- passes an extensive suites of cross-checks and robustness tests
- our cleanest multipole range is 40-400 (retains 90% of the S/N)

Several important cosmological impacts (probing the post-recombination history with CMB alone)

- alternative τ measurement (independently of the polarization)
- imposing flatness at the sub-percent level
- weaker constraining power on the extension to LCDM than expected (e.g. low-ell dip tensions)
- mild precision improvement yet important accuracy improvement

First nearly all-sky map of the lensing induced B-modes

- Planck φ as mass tracer: including all the lensing information
- >10 $\sigma$  measurement of the lensing B power spectrum (indirect method)
- useful tool for other experiments : measurement of the lensing B at the lowest accessible ell and (A\_lens, r) degeracy breaking.

Lensing results are a stricking success of the whole PLANCK collaboration.

The scientific results that we present today are a product of the Planck Collaboration, including individuals from more than 100 scientific institutes in Europe, the USA and Canada.





### Additional material for answering questions

# Consistency with alternative method



We use the same setup:



## The real-space based alternative pipeline

Further details on the real-space pipeline [Ref: Planck B-lensing paper] :

- 1. Masking foreground-contaminated areas in the temperature map and inpainting
- 2. Extracting  $\phi$  using Okamoto&Hu estimator and subtracting for the *Mean-Field*
- 3. Generating pure E-mode  $Q^E \& U^E$  by nullifying the B-mode component in spherical harmonic space
- 4. Filtering  $\phi$ ,  $Q^E \& U^E$  and implementing :  $\nabla \left( \tilde{Q}^E \pm i \tilde{U}^E \right) \cdot \nabla \tilde{\phi}$
- 5. deconvolving from the filtering transfer function

#### The lensing potential extraction

PRELIMINARY The consistency of the 2 lensing extraction methods is discussed in Planck 2013 lensing Quick check on Planck 2014 data:

- the official  $\phi$  of Planck 2014 lensing
  - T+P (25% less uncertainties)
  - minimum-variance filtering of T and P
- $\rightarrow$  used in the harmonics-space method

- the alternative  $\phi$  :
  - T-only
  - mask treated by inpainting
  - Ref: Planck 2013 lensing
  - → targeted to real-space implementation



# Correlation with other LSS tracers

#### External data Planck 2013 Lensing

- 20 sigma correlation with NVSS radio galaxies and quasars ( $z_{mean} = 1.1$ )
- 10 sigma with SDSS Luminous Red Galaxies ( $z_{mean} = 0.55$ )
- 7 sigma with the WISE satellite IR galaxies catalog ( $z_{mean} = 0.1$ )

Planck's Cosmic Infrared Background (CIB)

unresolved high-redshift dusty star-forming galaxies
dominant extra-galactic emission at > 353GHz

• first detection (42 sigma) of a correlation between high-frequency maps and lensing



• helps in probing the origin of the CIB hence in constraining the star formation history