

X<sup>th</sup> RENCONTRES DU VIETNAM  
Very High Energy Phenomena in the Universe

Quy Nhon, 3-9 August 2014

# Ultrahigh-Energy Cosmic Rays and Neutrinos from Gamma-Ray Bursts

**Soebur Razzaque**



UNIVERSITY  
OF  
JOHANNESBURG



## Fourth Vietnam School of Particle Physics

Nha Trang 1997-1998





Patrick  
Aurenche

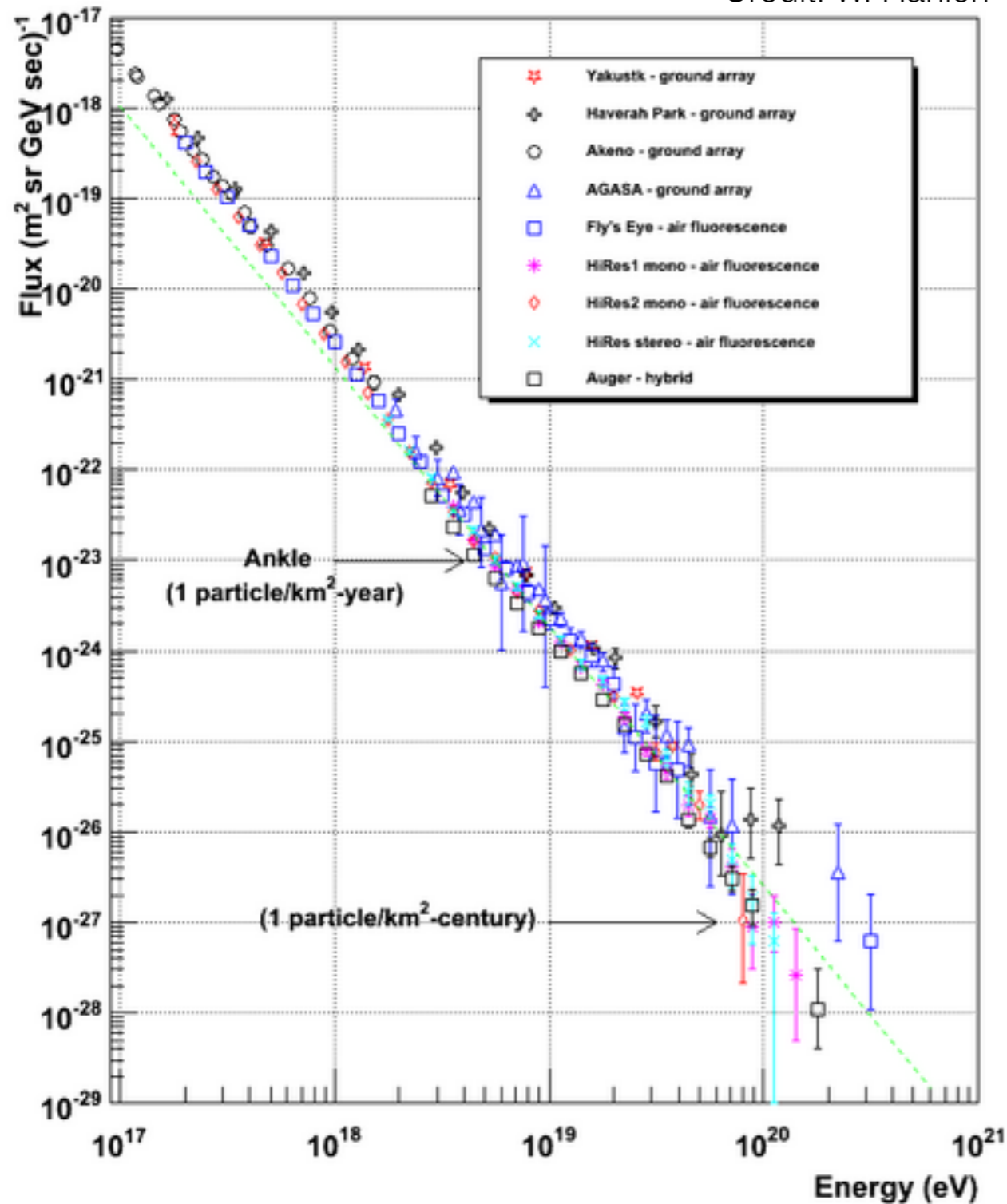
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# Ultrahigh-Energy Cosmic Rays

Cosmic Ray Spectra of Various Experiments

Credit: W. Hanlon

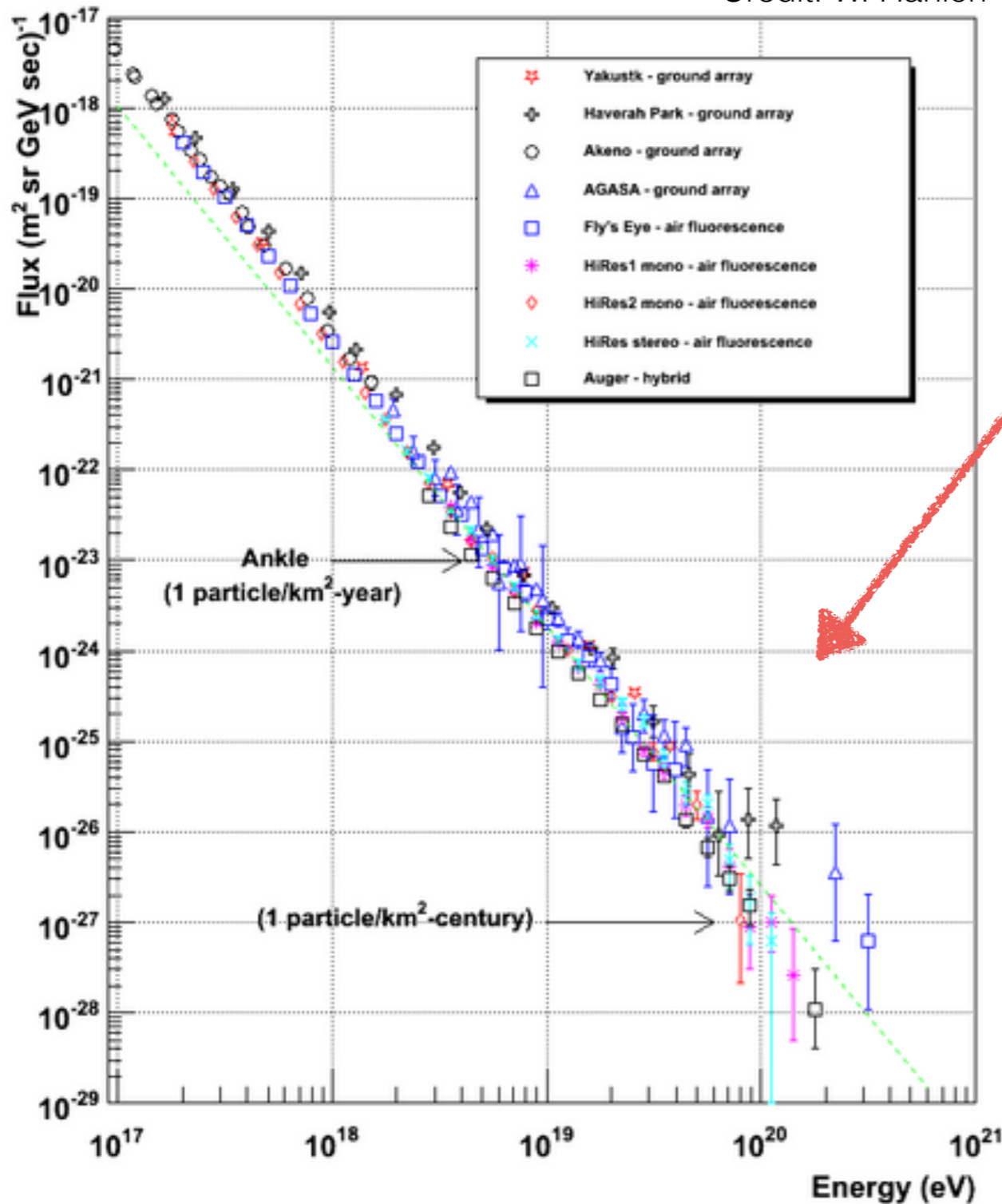


AUGER Collab. 2010

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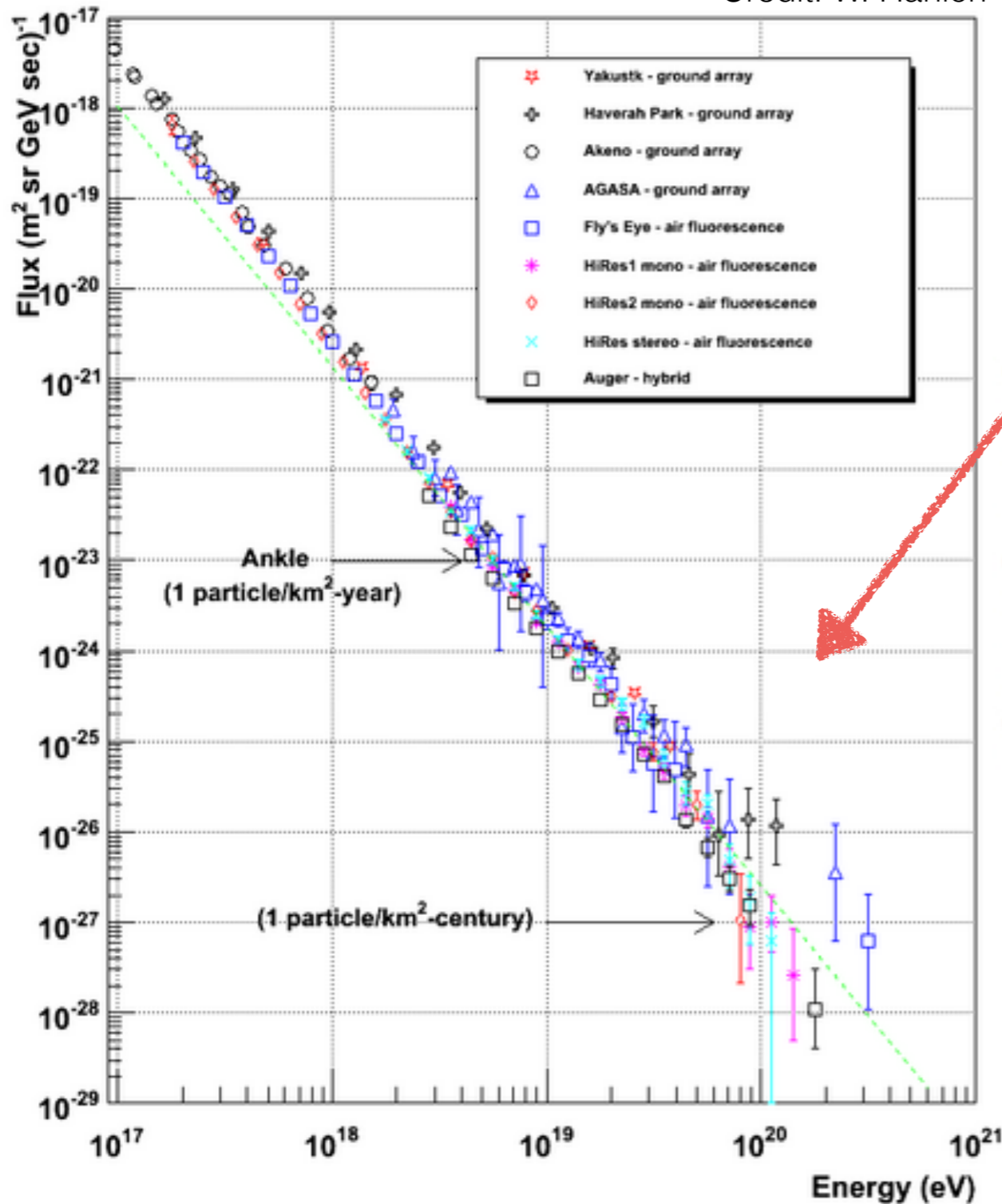
Ultrahigh-Energy Range



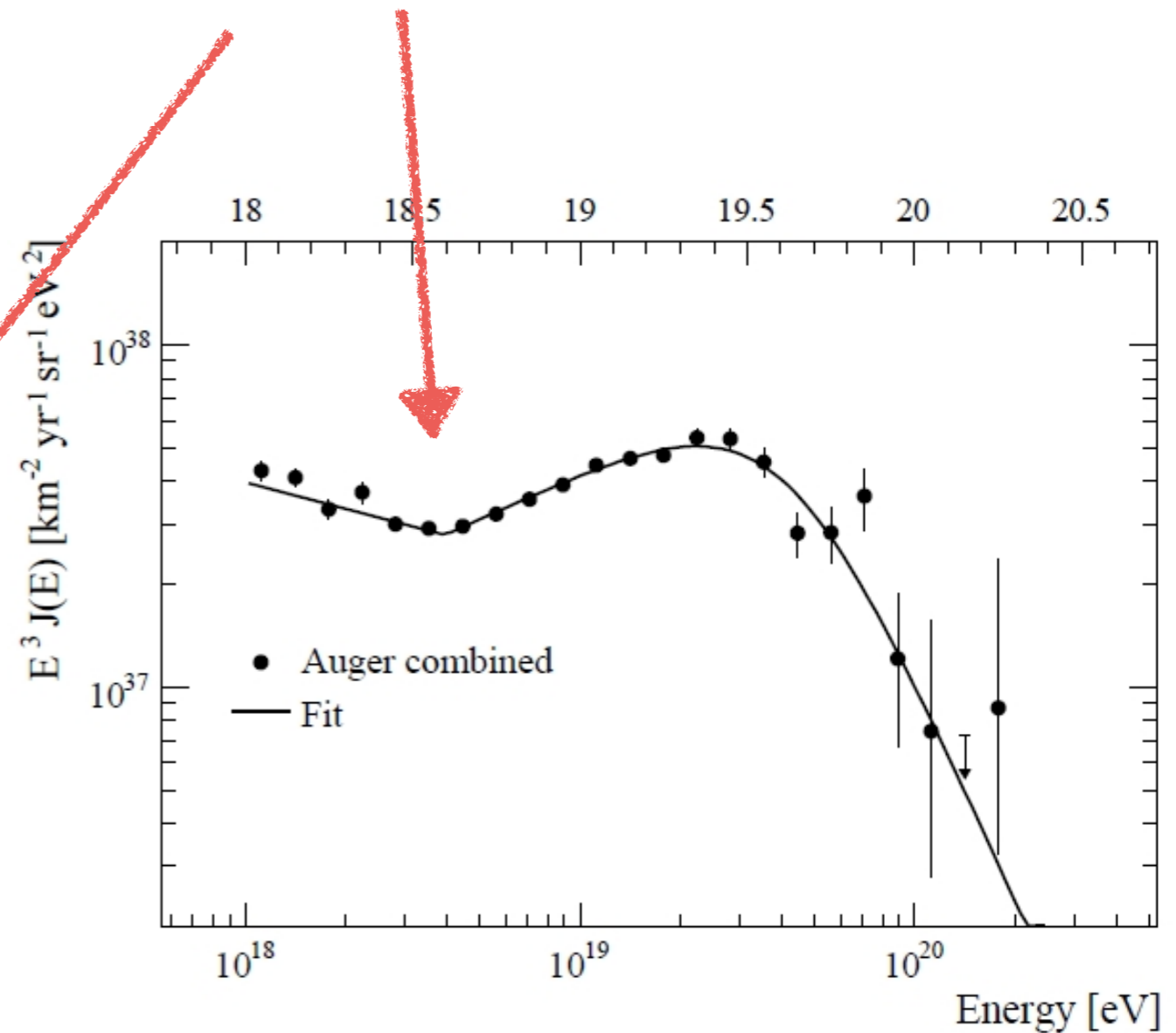
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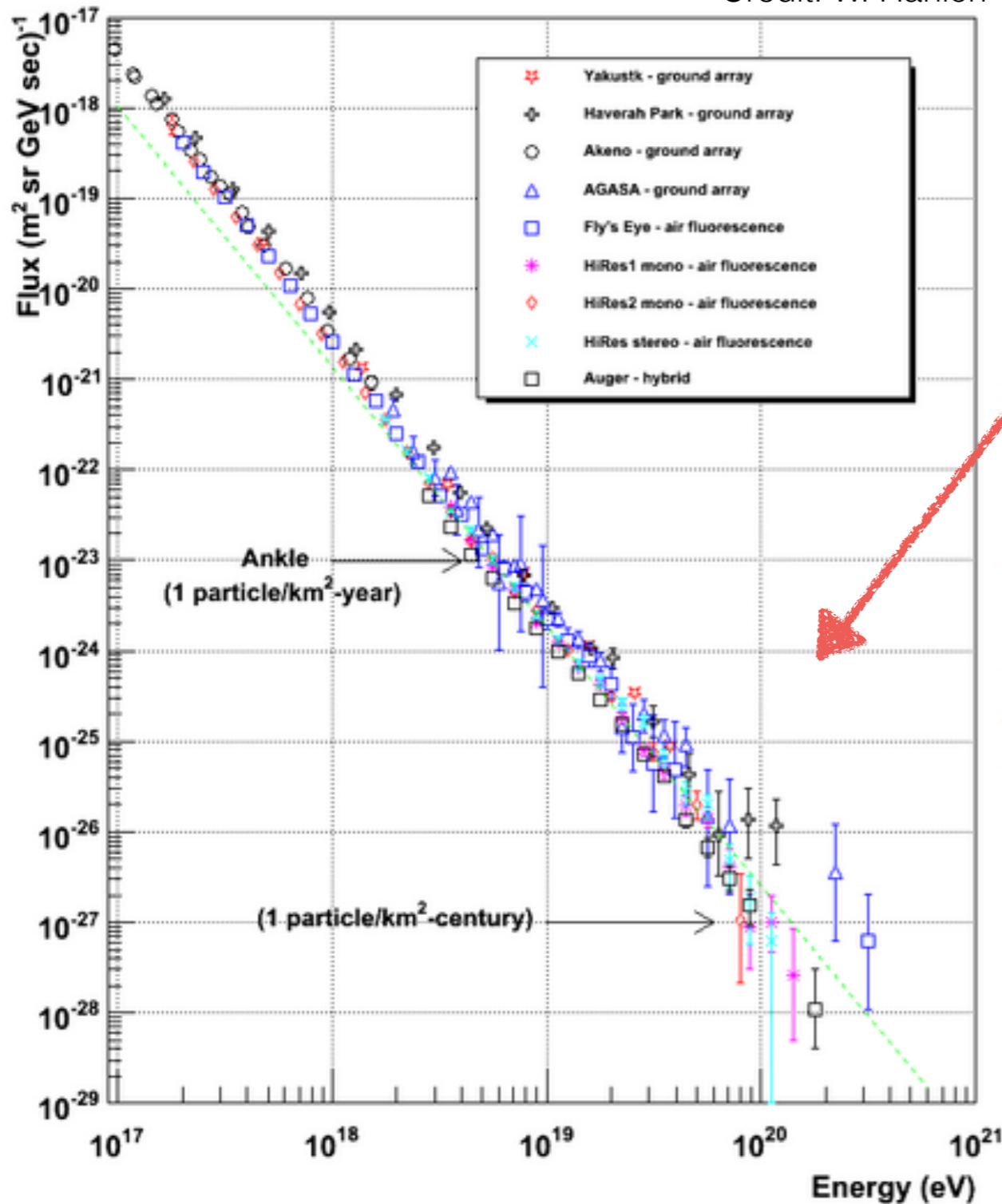


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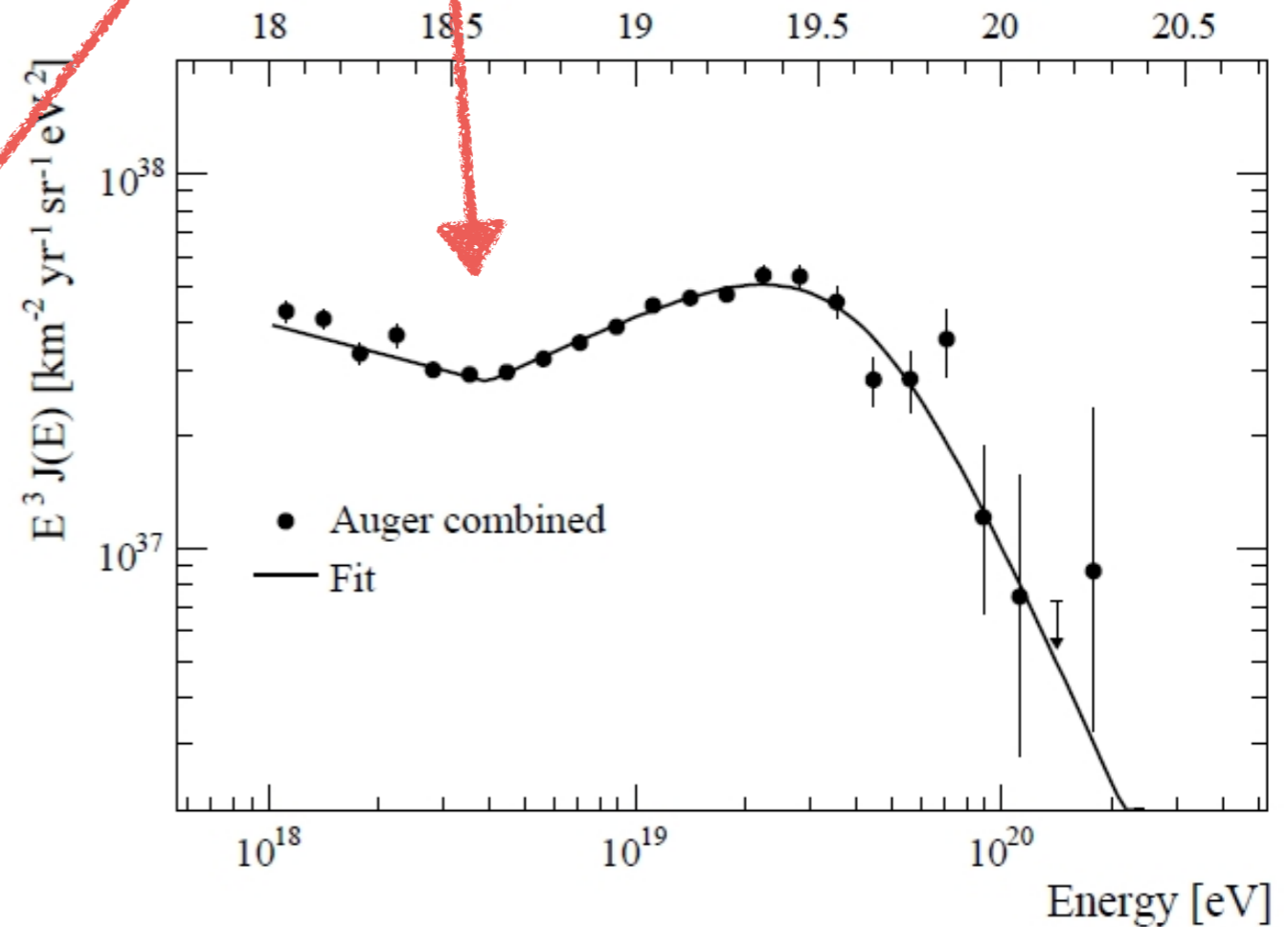
Cosmic Ray Spectra of Various Experiments

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## Ultrahigh-Energy Range

**What is the origin?**



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# Why Gamma-Ray Bursts?

Long-duration ( $> 2$  s) GRBs are the most  
luminous objects in the gamma-ray sky

$L_\gamma \sim 10^{51}$  erg/s

Non-thermal

Isotropic-equivalent

particle acceleration

→ GRBs as sources of UHECRs: Waxman 1995; Vietri 1995



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Energy injection rate in UHECRs

Baryon loading  $> 1$

$$\dot{E}_{\text{CR}} \sim 10^{51} \frac{\text{erg}}{\text{GRB}} \cdot \frac{20 \text{ GRB}}{\text{Gpc}^3 \text{ yr}} \eta_{\text{bol}} \eta_p \sim 2 \times 10^{43} \eta_{\text{bol}} \eta_p \frac{\text{erg}}{\text{Mpc}^3 \text{ yr}}$$

Local true GRB rate

Bolometric factor  $< 1$

# Energy in UHECRs

Energy injection rate in UHECRs from data

$$\dot{E}_{\text{UHECR}} \approx 10^{44} \text{ erg Mpc}^{-3} \text{ yr}^{-1}$$

Need baryon-loading factor  $> \sim 50$

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How many GRBs within the GZK volume (100 Mpc)?

→ Depends on the Inter-Galactic Magnetic Field (IGMF)

$$\Delta t_{\text{CR}} \sim 3.2 \times 10^4 Z^2 \left( \frac{B_{\text{IG}}}{1 \text{ nG}} \right)^2 \left( \frac{E_{\text{CR}}}{60 \text{ EeV}} \right)^{-2} \left( \frac{\lambda_{\text{IG}}}{1 \text{ Mpc}} \right)^{3/2} \text{ yr}$$

$$\rightarrow N_{\text{GRB}} \sim \frac{20 \text{ GRB}}{\text{Gpc}^3 \text{ yr}} \cdot V_{\text{GZK}} \Delta t_{\text{CR}} \sim 3 \times 10^3$$



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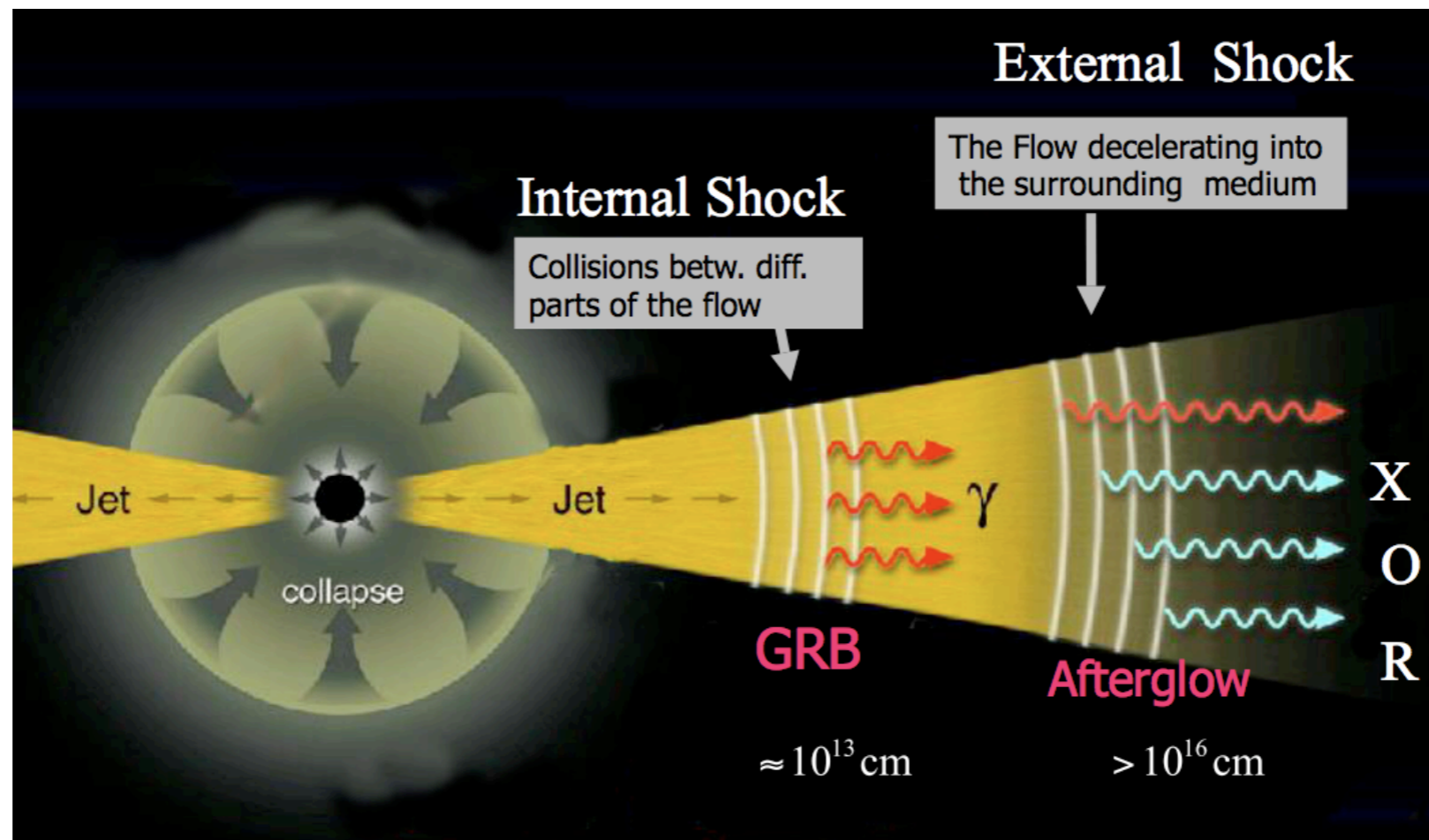
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A fraction ( $\sim 1/200$ ) of these GRBs have their jets pointing to us

beaming angle correction

# When UHECRs are made in GRBs?

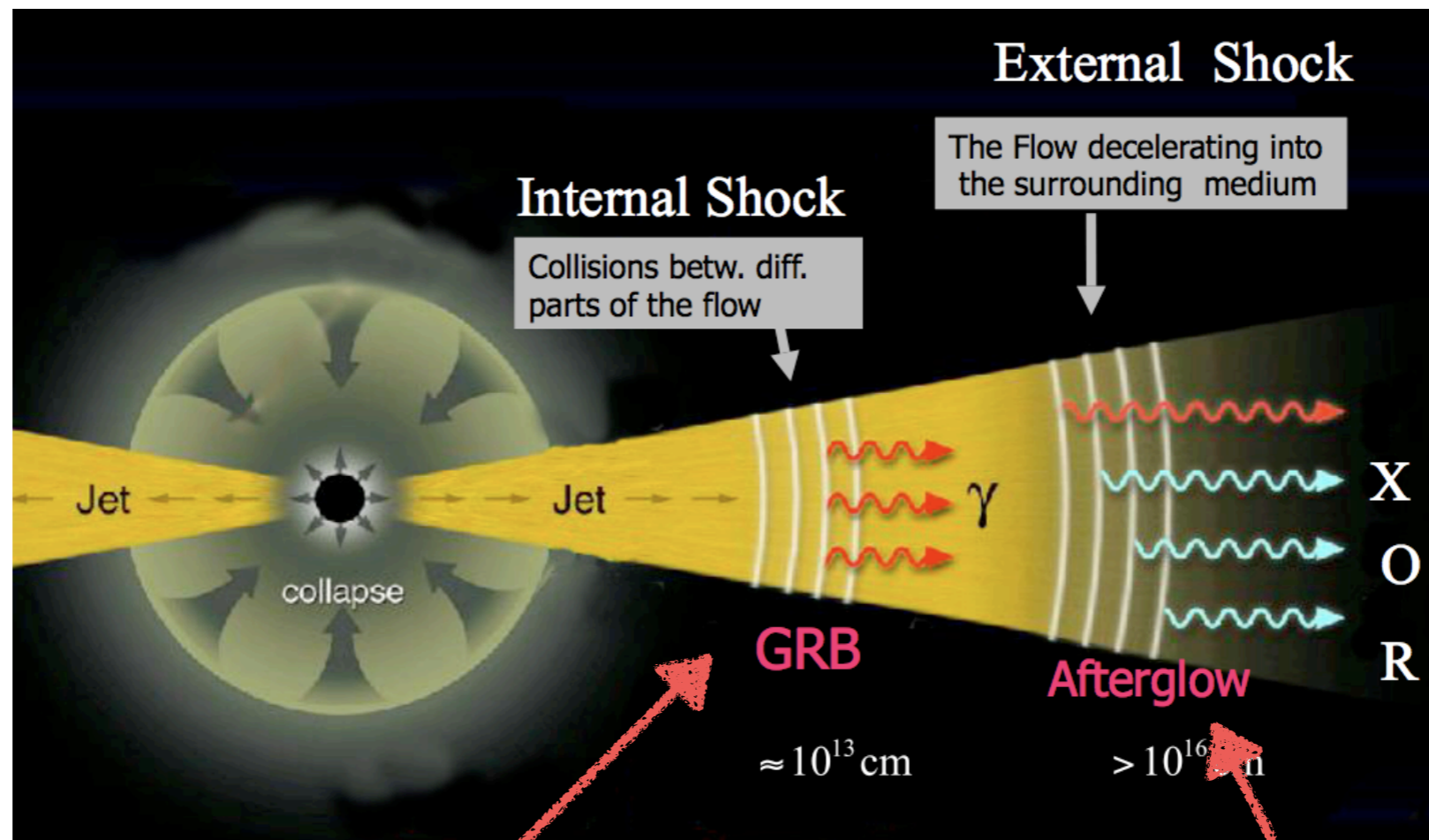
## Fireball shock model of long-duration GRBs



*Rees, Meszaros, Shemi, Piran, Daigne, Mochkovitch, ...*

# When UHECRs are made in GRBs?

## Fireball shock model of long-duration GRBs



Prompt gamma-ray  
emission  $\sim 10$  s

Afterglow emission  
 $\sim 10$  s - year

*Rees, Meszaros, Shemi, Piran, Daigne, Mochkovitz, ...*



# Acceleration in Internal Shocks

**Chain of logic**

**Comoving frame**

**Energy density for gamma rays:**

$$u'_\gamma \approx \frac{L_\gamma}{4\pi r_{\text{sh}}^2 \Gamma_b^2 c}$$

Isotropic-equivalent  
gamma-ray luminosity

Shock radius

Bulk Lorentz factor

# Acceleration in Internal Shocks

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Shock radius  $r_{\text{sh}}$       Bulk Lorentz factor  $\Gamma_b$       Isotropic-equivalent gamma-ray luminosity  $L_\gamma$

Energy density for particles:  $u'_e = u'_\gamma \Rightarrow$  **electrons (fast-cooling)**

Baryons (n/p) loaded jet:  $u'_e = u'_\gamma = \epsilon_e u'_p$       energy density in p/n

**Dominant (kinetic) energy carrier**

fraction  $< 1$

# Acceleration in Internal Shocks

## Chain of logic

Energy density for magnetic field:  $u'_B \equiv \frac{B'^2}{8\pi} = \epsilon_B u'_p$  fraction < 1

## Magnetic field:

Typical values for prompt gamma rays

$$B' \approx \sqrt{\frac{2\epsilon_B L_\gamma}{\epsilon_e r_{\text{sh}}^2 \Gamma_b^2 c}} \sim 8 \times 10^4 \sqrt{\frac{\epsilon_B}{\epsilon_e}} \left( \frac{L_\gamma}{10^{51} \text{ erg/s}} \right)^{1/2} \left( \frac{r_{\text{sh}}}{10^{13} \text{ cm}} \right)^{-1} \left( \frac{\Gamma_b}{316} \right)^{-1} \text{ G}$$



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Maximum CR energy:  $E_{\text{max}} \sim ZeB'r_{\text{sh}}$

$$E_{\text{max}} \sim 2 \times 10^{20} \sqrt{\frac{\epsilon_B}{\epsilon_e}} \left( \frac{L_\gamma}{10^{51} \text{ erg/s}} \right)^{1/2} \left( \frac{\Gamma_b}{316} \right)^{-1} \text{ eV}$$

# Acceleration in External Shocks

**External forward shock - Blast wave**

**Relativistic jet running into surrounding environment**

Deceleration time scale from total energy in blast wave equal to kinetic energy

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**Constant density medium**

$$t_{\text{dec},i} \approx 33.3 (1+z) \left( \frac{n}{1 \text{ cm}^3} \right)^{-1/3} \left( \frac{\Gamma_b}{316} \right)^{-8/3} \left( \frac{E_k}{10^{55} \text{ erg}} \right)^{1/3} \text{ s}$$

**Wind medium,  $R^{-2}$  density**

$$t_{\text{dec},w} \approx 1.5 \frac{1+z}{A_\star} \left( \frac{\Gamma_b}{316} \right)^{-4} \left( \frac{E_k}{10^{55} \text{ erg}} \right) \text{ s}$$

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*Blandford &  
McKee 1976*

### Self-similar evolution of the blast wave

#### Bulk Lorentz factor

$$\begin{aligned} \Gamma_{ad,i}(t) &= \Gamma_0 (t_{\text{dec},i}/4t)^{3/8}, & \Gamma_{ad,w}(t) &= \Gamma_0 (t_{\text{dec},w}/4t)^{1/4}, \\ \Gamma_{ra,i}(t) &= \Gamma_0 (t_{\text{dec},i}/7t)^{3/7}, & \Gamma_{ra,w}(t) &= \Gamma_0 (t_{\text{dec},w}/7t)^{1/3}, \end{aligned}$$

# Acceleration in External Shocks

## Adiabatic blast wave in constant density

$$\Gamma_{\text{ad},i} \approx 124 (1+z)^{3/8} \left( \frac{n}{1 \text{ cm}^3} \right)^{-1/8} \left( \frac{E_k}{10^{55} \text{ erg}} \right)^{1/8} \left( \frac{t}{100 \text{ s}} \right)^{-3/8}$$

**Blast wave radius:**  $r_{\text{sh}} \approx \frac{4 \times 10^{17}}{(1+z)^{1/4}} \left( \frac{n}{1 \text{ cm}^3} \right)^{-1/4} \left( \frac{E_k}{10^{55} \text{ erg}} \right)^{1/4} \left( \frac{t}{100 \text{ s}} \right)^{1/4} \text{ cm}$



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**Magnetic energy from shock energy:**  $B'^2/8\pi = \epsilon_B (4\pi r_{\text{sh}}^2 n m_p c^2 \Gamma_{\text{ad},i}^2)$

$$B' \approx 15 (1+z)^{3/8} \left( \frac{\epsilon_B}{0.1} \right)^{1/2} \left( \frac{n}{1 \text{ cm}^3} \right)^{3/8} \left( \frac{E_k}{10^{55} \text{ erg}} \right)^{1/8} \left( \frac{t}{100 \text{ s}} \right)^{-3/8} \text{ G}$$

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# Energy in UHECRs

**Minimum CR energy:**  $E_{\min} \sim m_p c^2 \Gamma^2 \sim 10^{14} - 10^{15} \text{ eV}$  **early on**

**Total cosmic-ray energy:**  $\mathcal{E}_{\text{CR}} \approx \epsilon_p \frac{4}{3} \pi r_{\text{sh}}^3 m_p c^2 \Gamma^2 = \frac{1}{2} \epsilon_p E_k$  fraction < 1

**Energy extraction rate by cosmic rays is quite slow**

$$\Gamma_{\text{ad},i} \approx 1 (1+z)^{3/8} \left( \frac{n}{1 \text{ cm}^3} \right)^{-1/8} \left( \frac{E_k}{10^{55} \text{ erg}} \right)^{1/8} \left( \frac{t}{1 \text{ yr}} \right)^{-3/8}$$

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# High Energy Neutrinos from GRBs

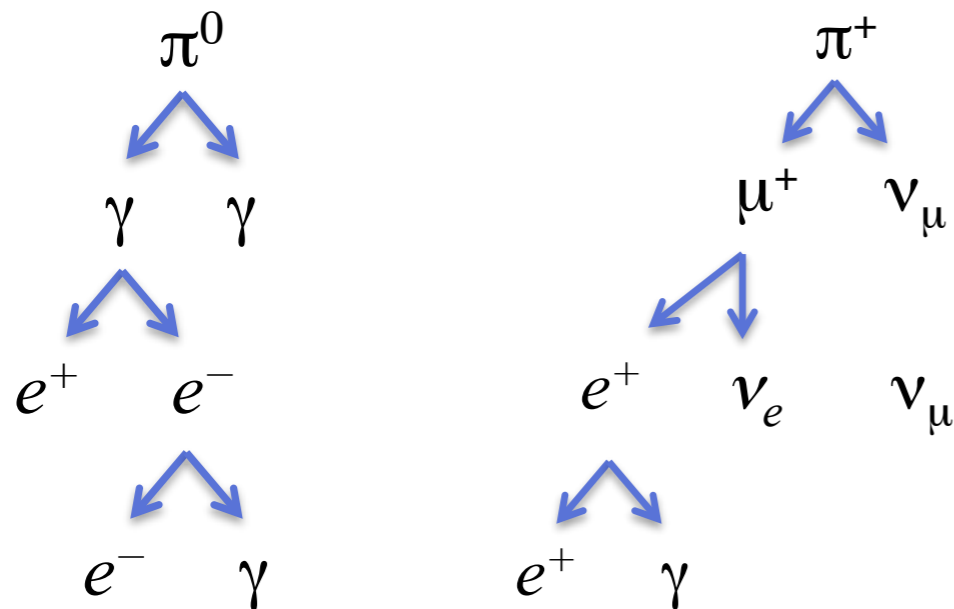
## Interaction channels for cosmic rays in the vicinity

$$p\gamma \rightarrow \pi^0, \pi^+, \pi^-, K^+, K^-, \text{etc.}$$

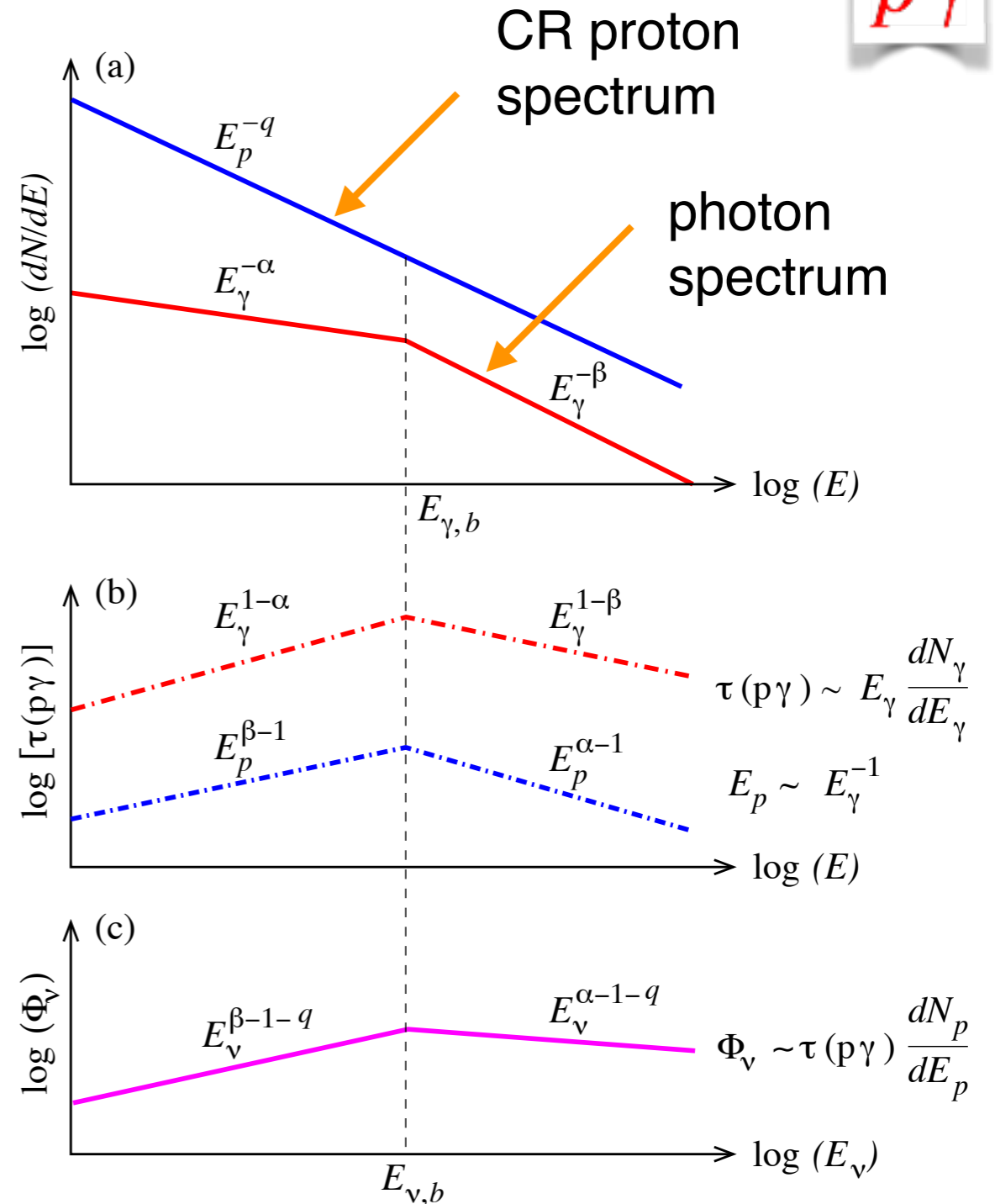
$$pp \rightarrow \pi^0, \pi^+, \pi^-, K^+, K^-, \text{etc.}$$



### Pion decay chain



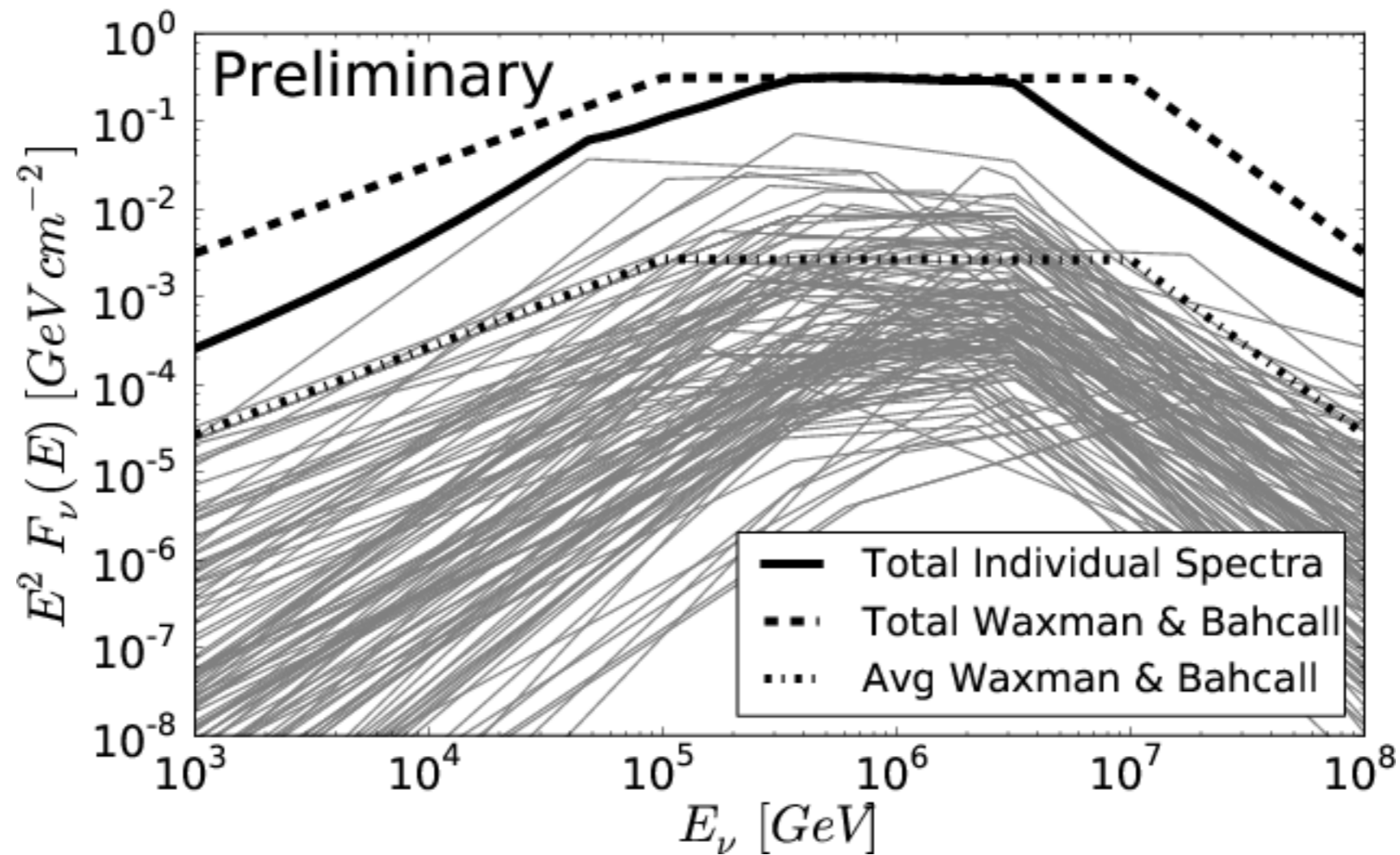
Energy for each neutrino flavor  
 $\sim 5\%$  of CR energy





# Neutrinos from Internal Shocks

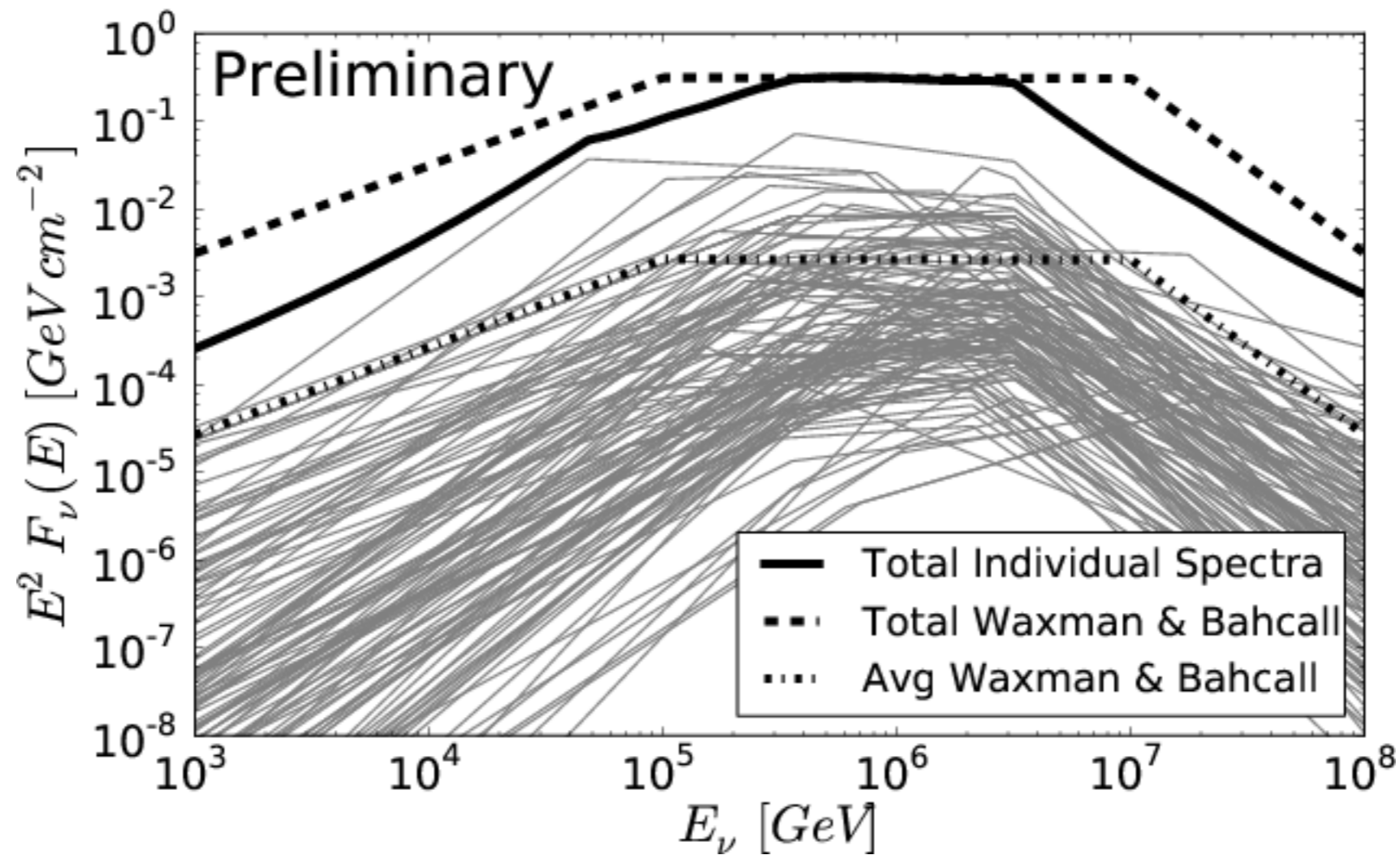
Calculation after Waxman & Bahcall



*IceCube Collab.*

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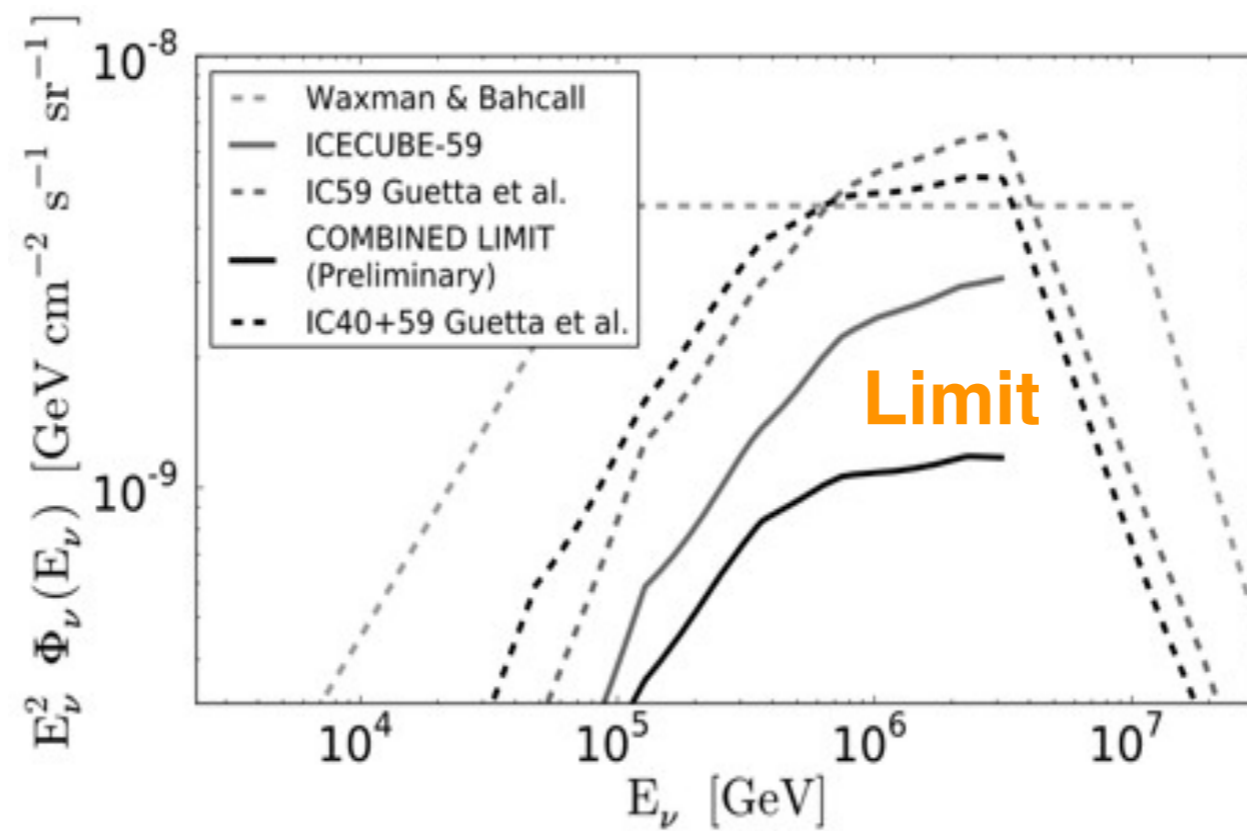
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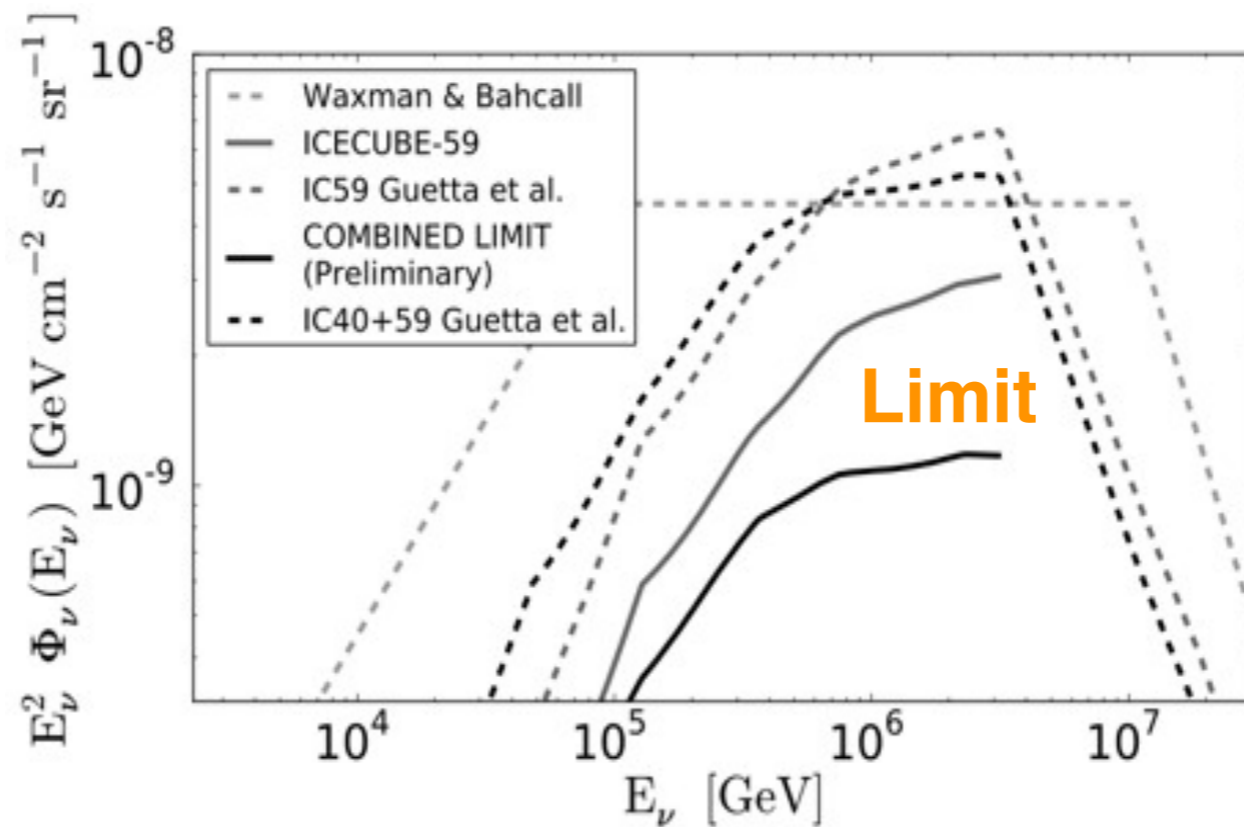
**Yet no detection!**

# IceCube limit on prompt neutrinos



*IceCube Collab.*

# IceCube limit on prompt neutrinos



*IceCube Collab.*

**What's going on?**

- **UHECRs are not accelerated in internal shocks**
- **Neutrinos are not produced significantly**

# Constraint on Bulk Lorentz factor

Number density of target photons  
for p-gamma interaction in IS

$$n'_\gamma \approx \frac{L_\gamma / \epsilon_e}{4\pi r_{\text{sh}}^2 c \Gamma_b \epsilon_{\text{pk}}} \propto \Gamma_b^{-5}$$

p-gamma interaction opacity/efficiency;  $\tau_{p\gamma} \sim n'_\gamma \sigma_{p\gamma} r'_{\text{sh}} \propto \Gamma_b^{-4}$



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Large bulk Lorentz factor



Extremely low efficiency

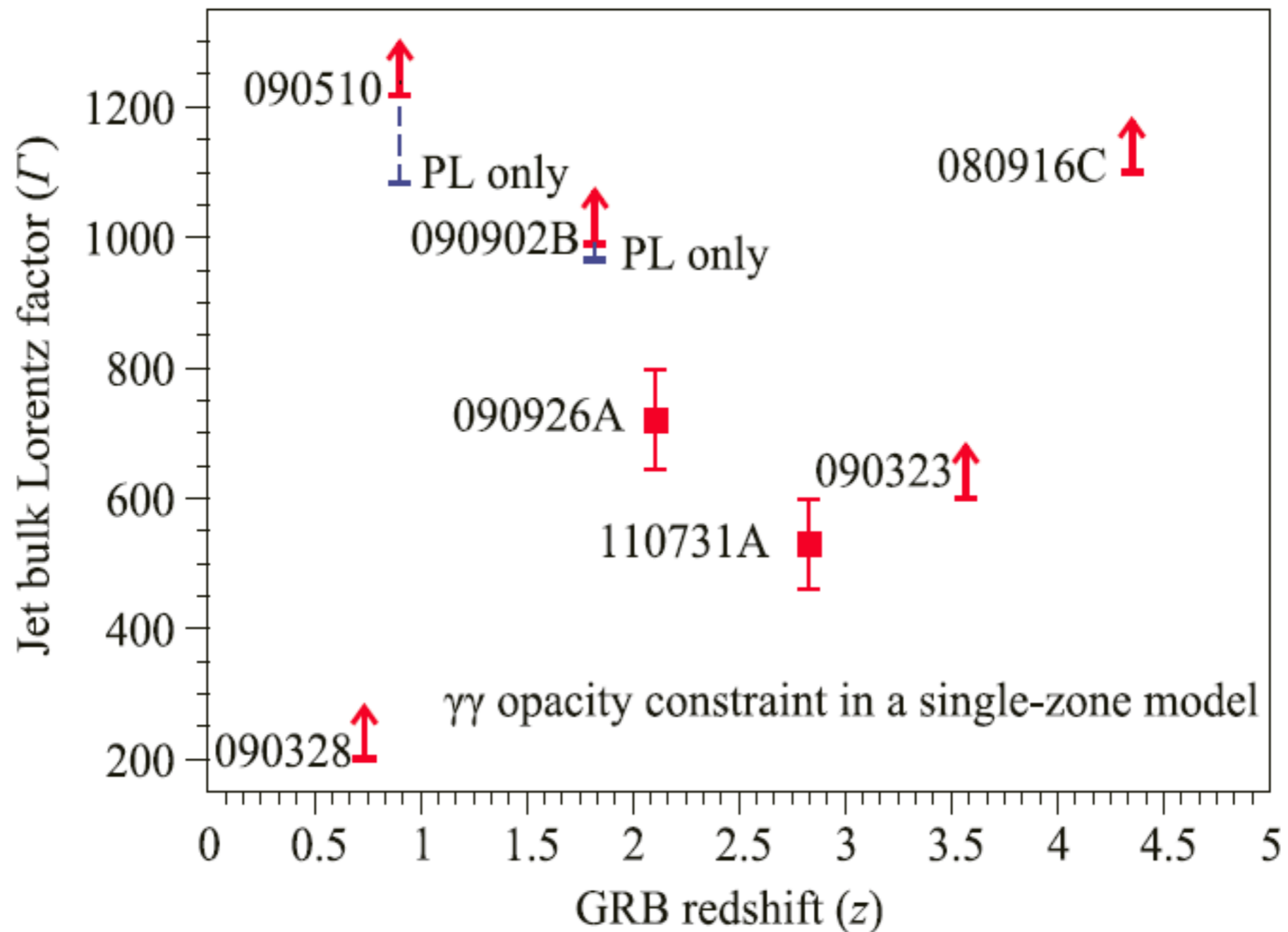
Typical

$$\tau_{p\gamma} \sim 0.2(\Gamma_b/316)^{-4}$$

Independently from gamma-ray data

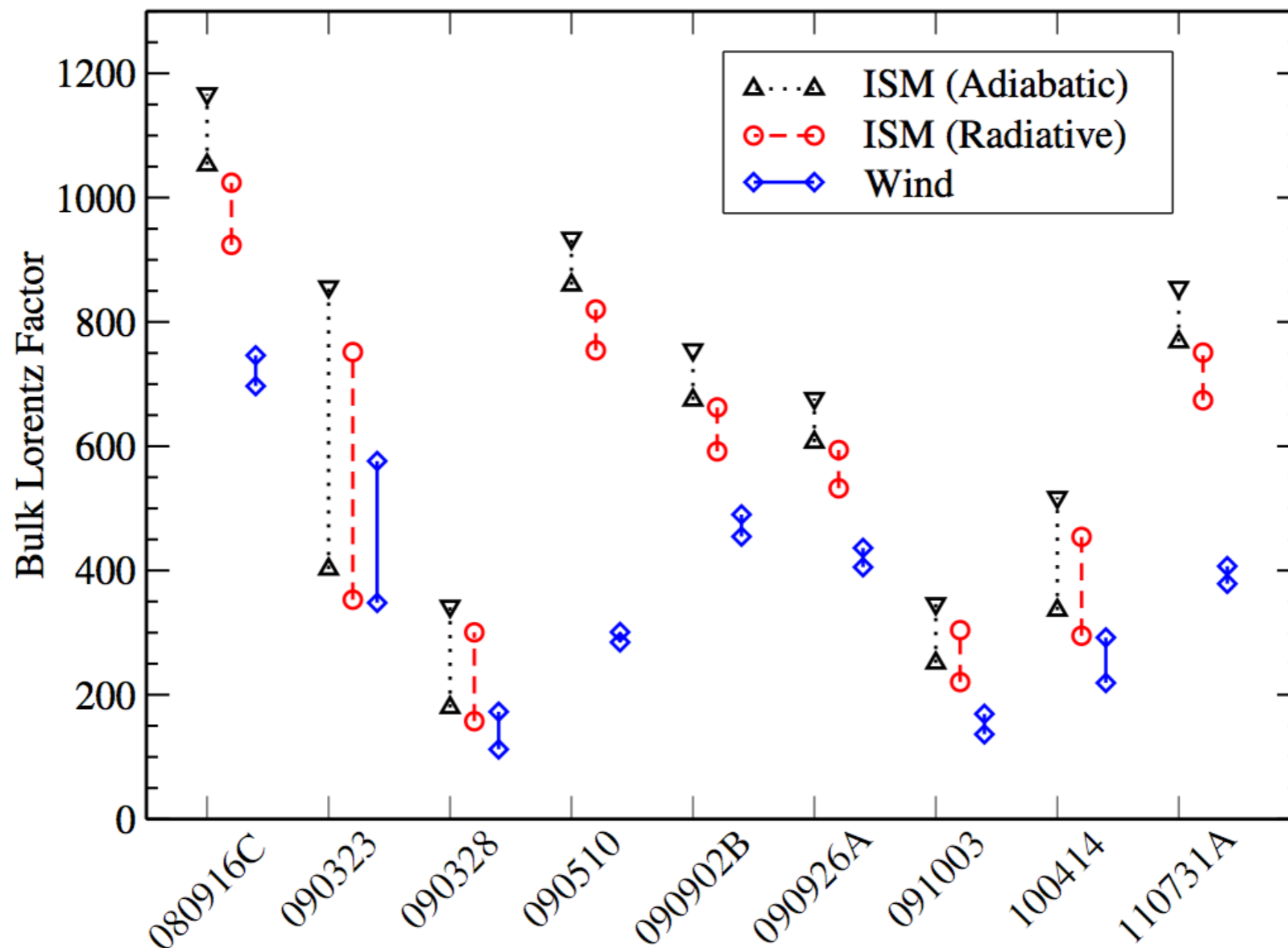
# Constraint on Bulk Lorentz factor

Constraint on the bulk Lorentz factor from gamma-gamma pair production opacity from  $>10$  GeV photons



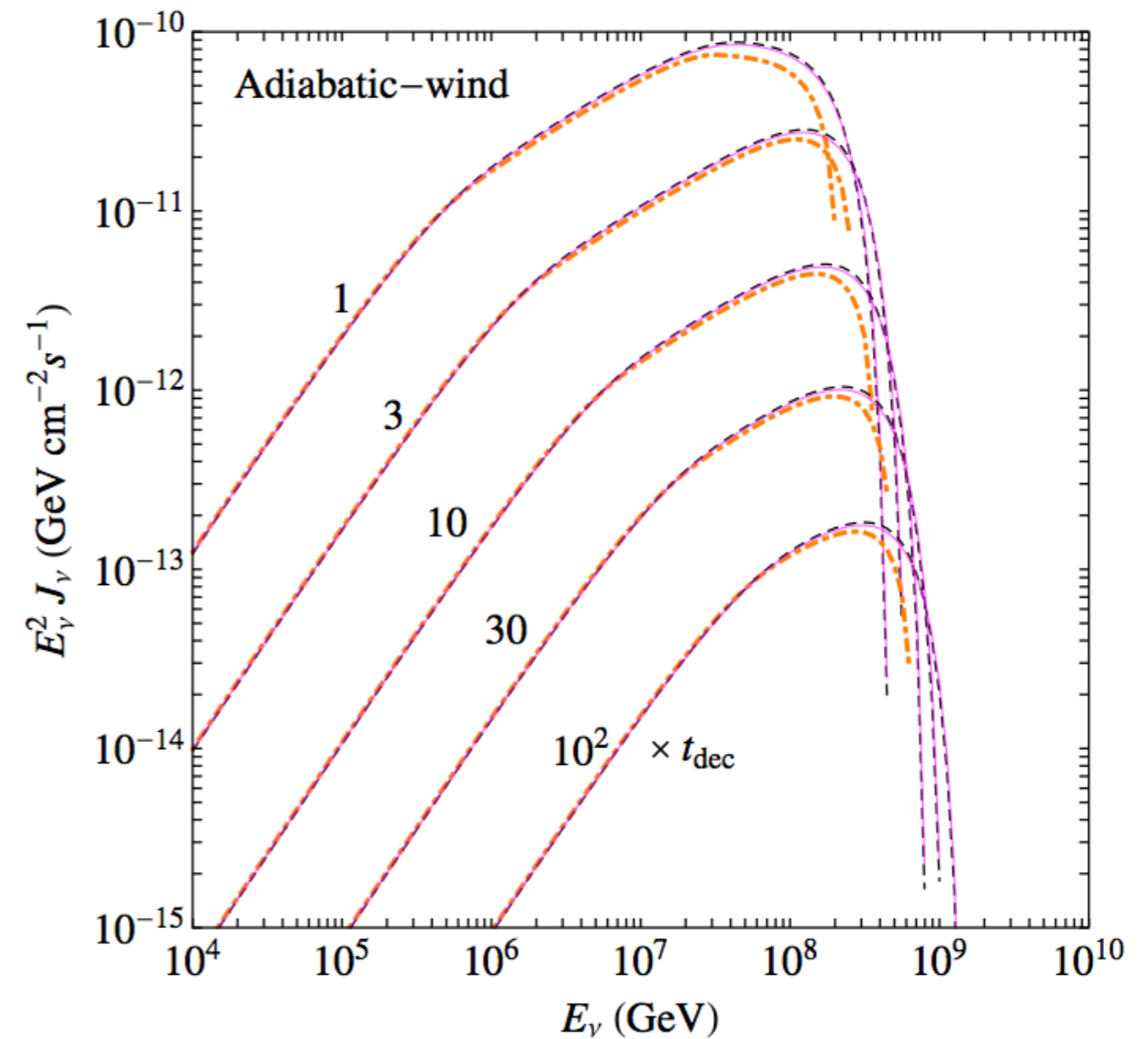
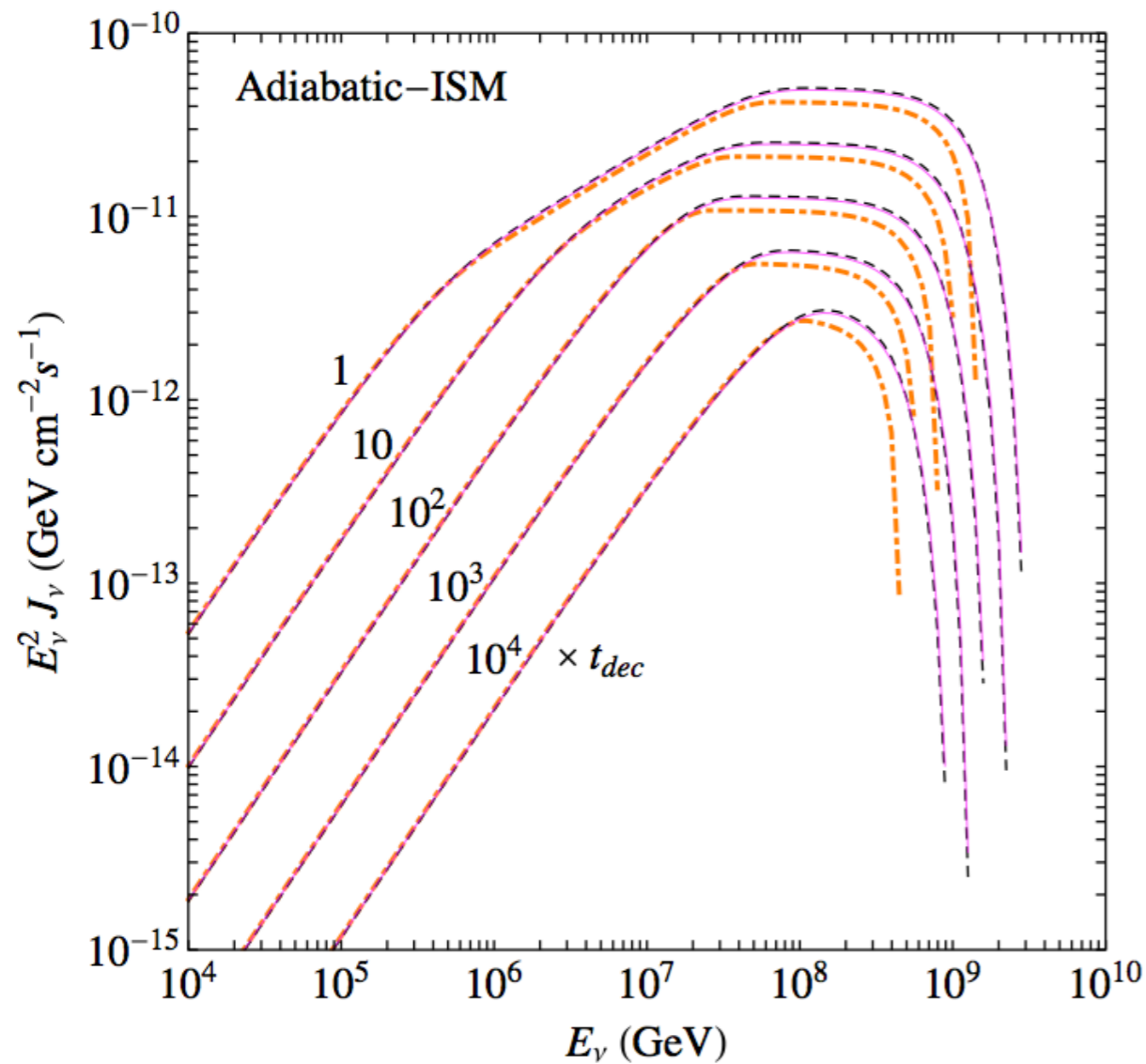
# Constraint on Bulk Lorentz factor

Constraint on the bulk Lorentz factor from onset time of the afterglow



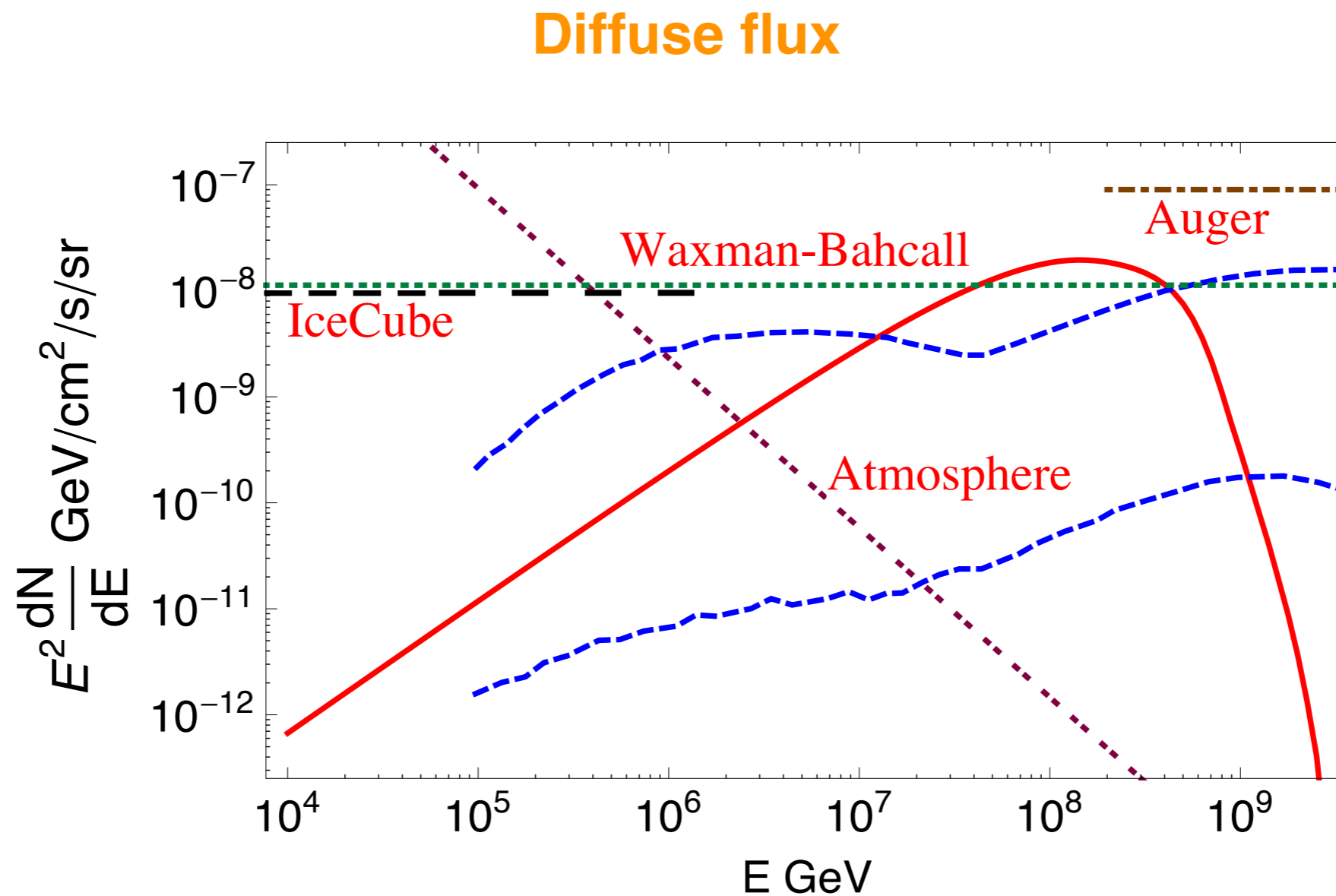
# Neutrinos from external FS

Long-lived neutrino flux from interaction of UHECR and afterglow photon



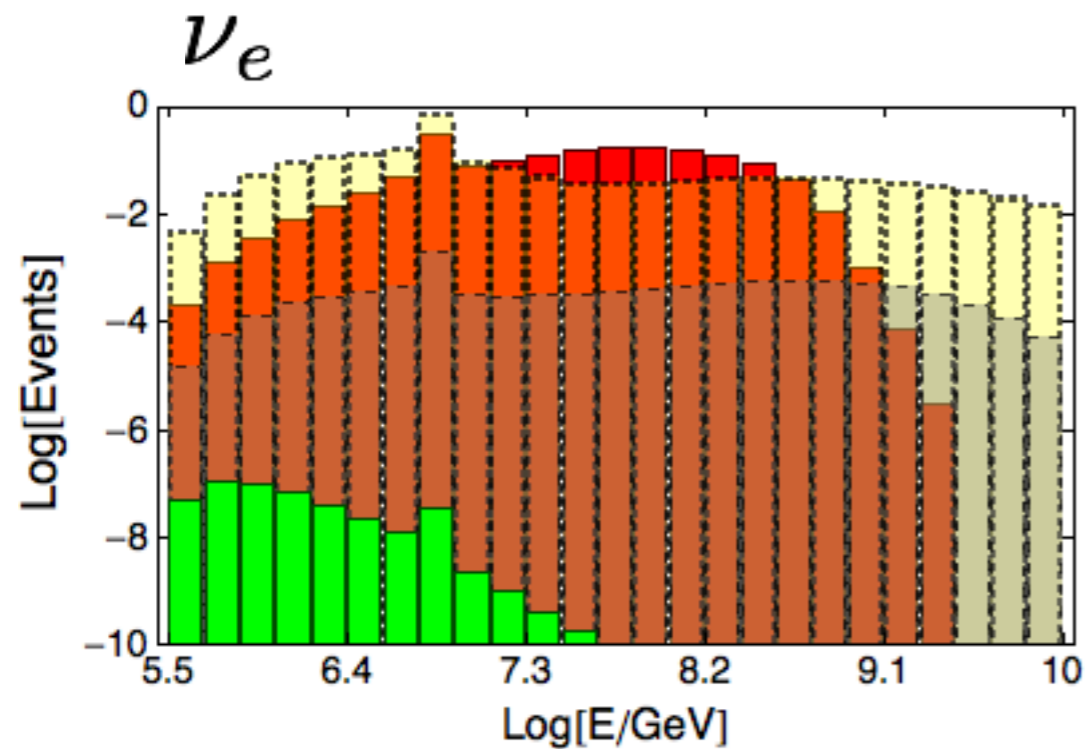
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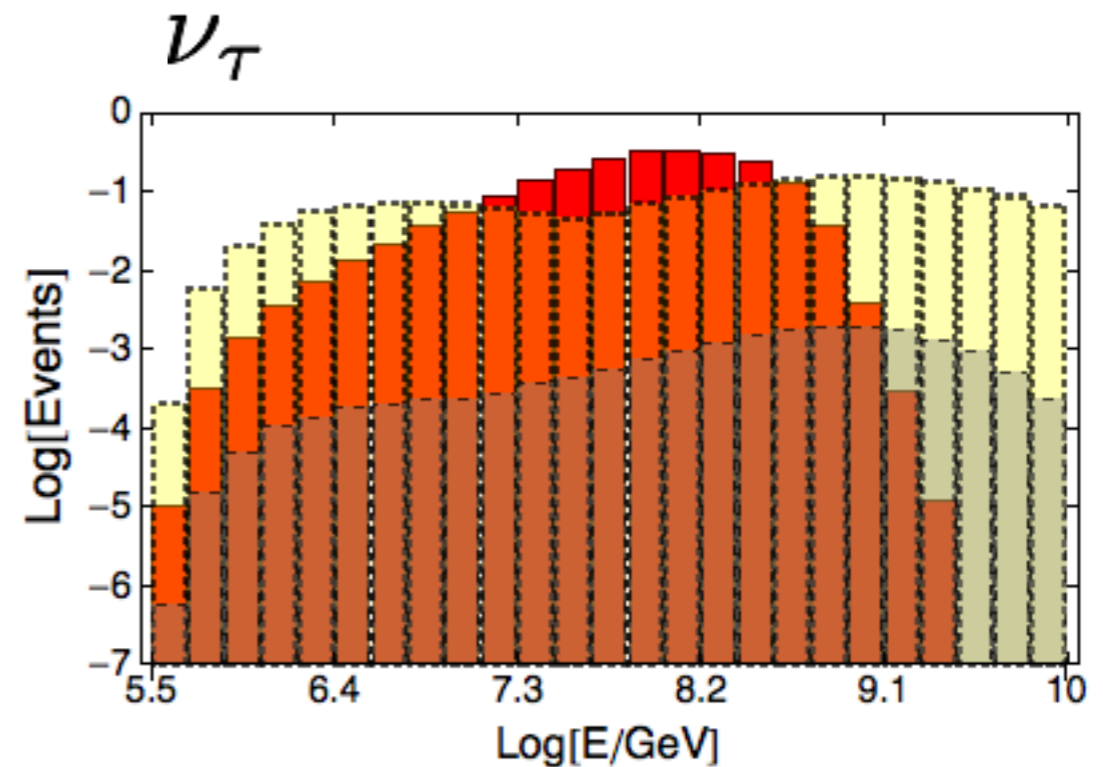
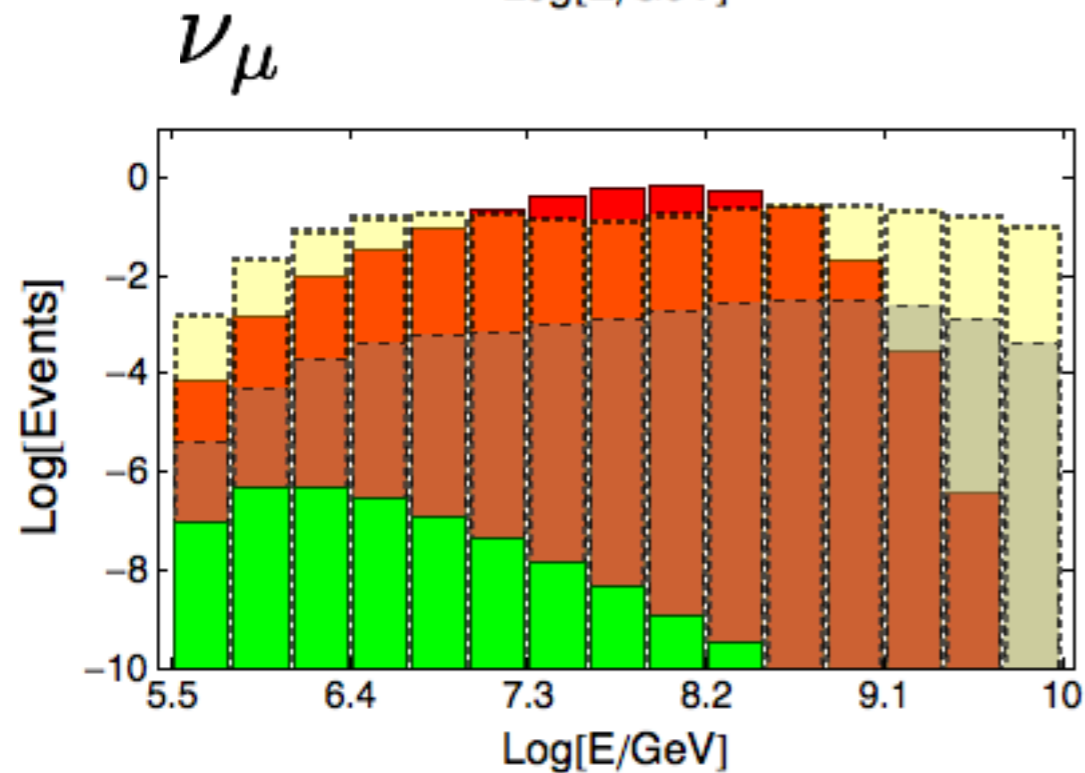
# Neutrinos from external FS



10 year  
events in  
IceCube

Preliminary

*Razzaque & Yang, in prep.*



# Neutrinos from external FS

3 year events in IceCube

Preliminary

$Log_{10}E(\text{GeV})$	5.5-7	7-8.5	8.5-10
GRB	0.38 (0.13) [0.09]	1.00 (2.25) [1.63]	0.07 (0.24) [0.21]
Atm.	$3.97 \times 10^{-7}$ ( $1.36 \times 10^{-6}$ ) [—]	$2.78 \times 10^{-9}$ ( $5.86 \times 10^{-8}$ ) [—]	$2.32 \times 10^{-12}$ ( $1.10 \times 10^{-10}$ ) [—]
$GZK_{Fe}$	$3.31 \times 10^{-3}$ ( $3.58 \times 10^{-6}$ ) [ $8.94 \times 10^{-4}$ ]	$2.95 \times 10^{-3}$ ( $4.68 \times 10^{-5}$ ) [ $5.05 \times 10^{-3}$ ]	$2.7 \times 10^{-3}$ ( $1.8 \times 10^{-4}$ ) [ $9.7 \times 10^{-3}$ ]
$GZK_p$	1.45 ( $1.32 \times 10^{-3}$ ) [0.31]	0.36 (0.02) [0.54]	0.25 (0.07) [0.92]

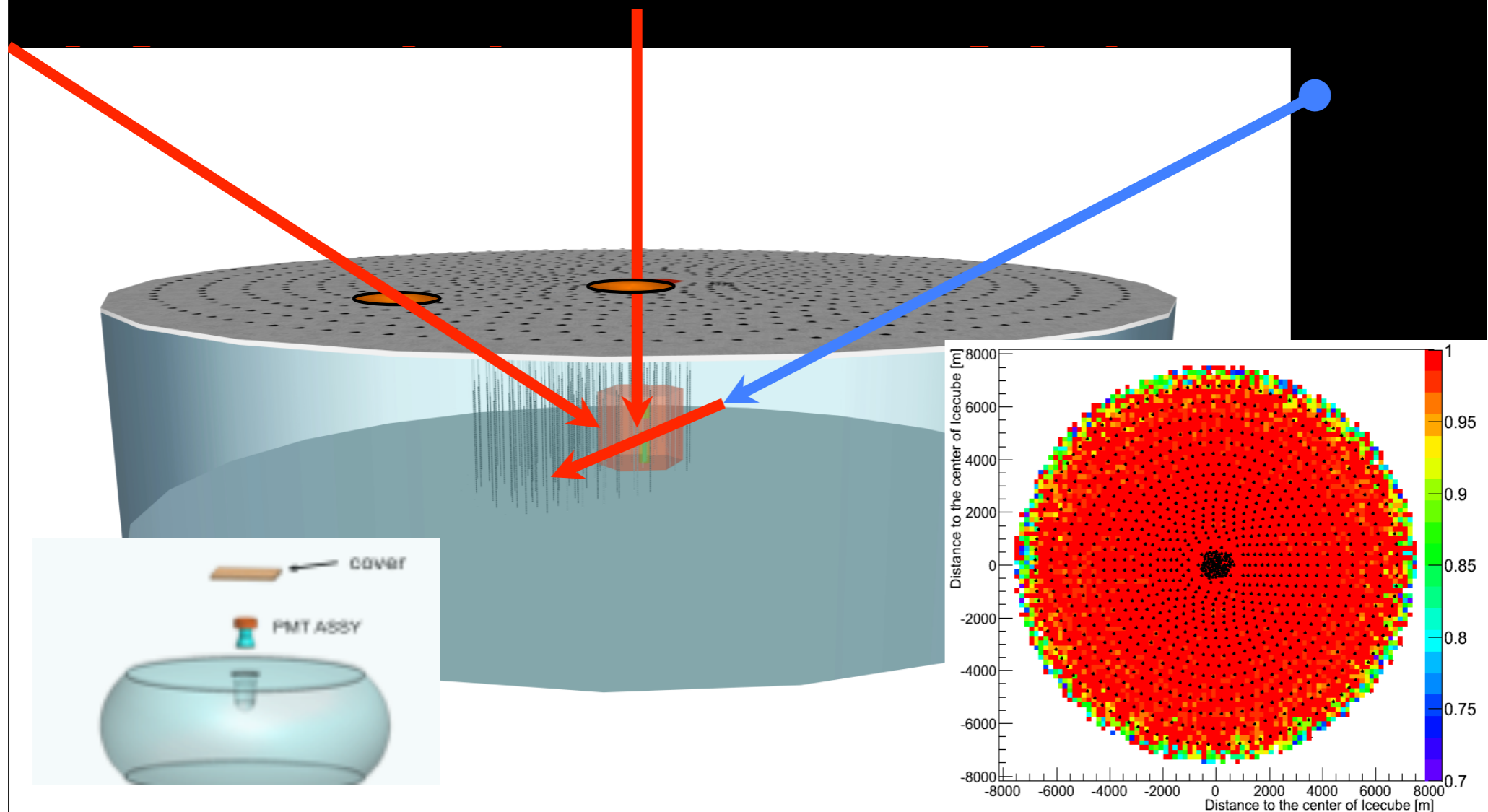
Razzaque & Yang, in prep.

# Future IceCube HE Extension

Slide from Garry Hill in NEUTRINO 2014, Boston

1 PeV (cosmic primary) veto: reject most atmospheric muon AND neutrino background above 100 TeV.

An efficient surface veto, 100 km<sup>2</sup>, for 3–5 sr background free cosmic muon neutrino and some shower detection

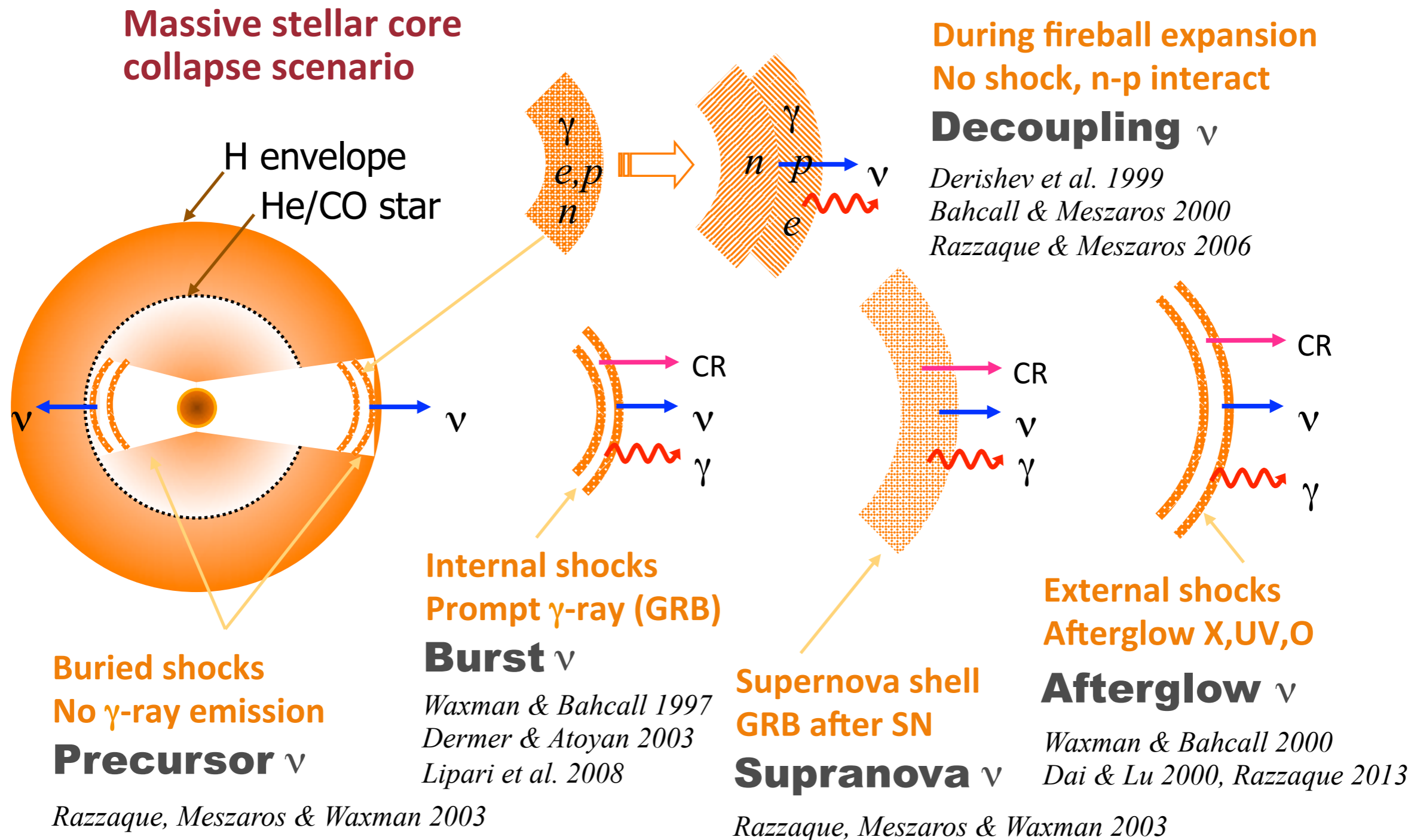


# Summary and Outlook

- **Acceleration of UHECRs in GRB jets is possible**
  - **Both internal shocks and external shocks**
  - **Requires large baryon loading / kinetic energy**
- **UHE neutrinos are expected to be produced at the acceleration sites**
  - **IceCube limit on prompt  $\sim 100$  TeV-10's of PeV flux is consistent with large jet bulk Lorentz factor**
  - **Long-lived PeV-EeV neutrinos from external shocks may be detectable with IceCube and future experiments**

Backup Slides

# High-Energy Neutrinos from GRBs



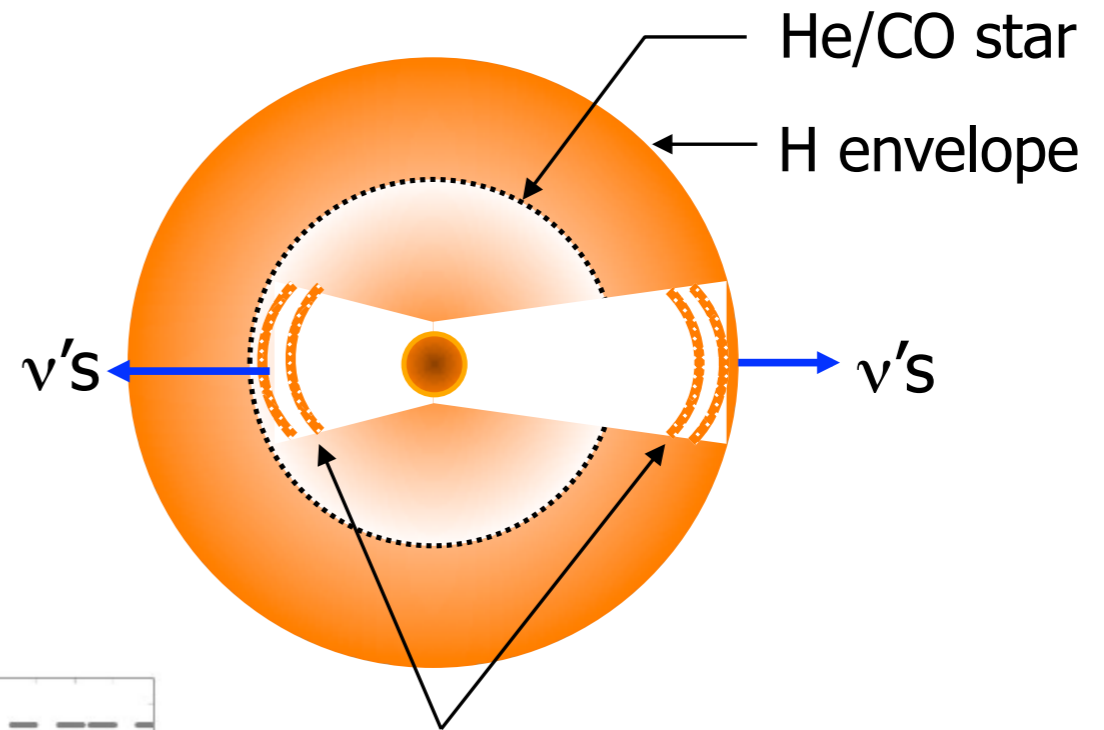


# Jet buried inside collapsing star

*Razzaque, Meszaros & Waxman 2003*

- Optically thick shocks
- High density of thermal  $\gamma$ -rays and target protons

$\leftarrow$   $pp \rightarrow \nu's$        $p\gamma \rightarrow \nu's$   $\rightarrow$   
 Low energy                  High energy

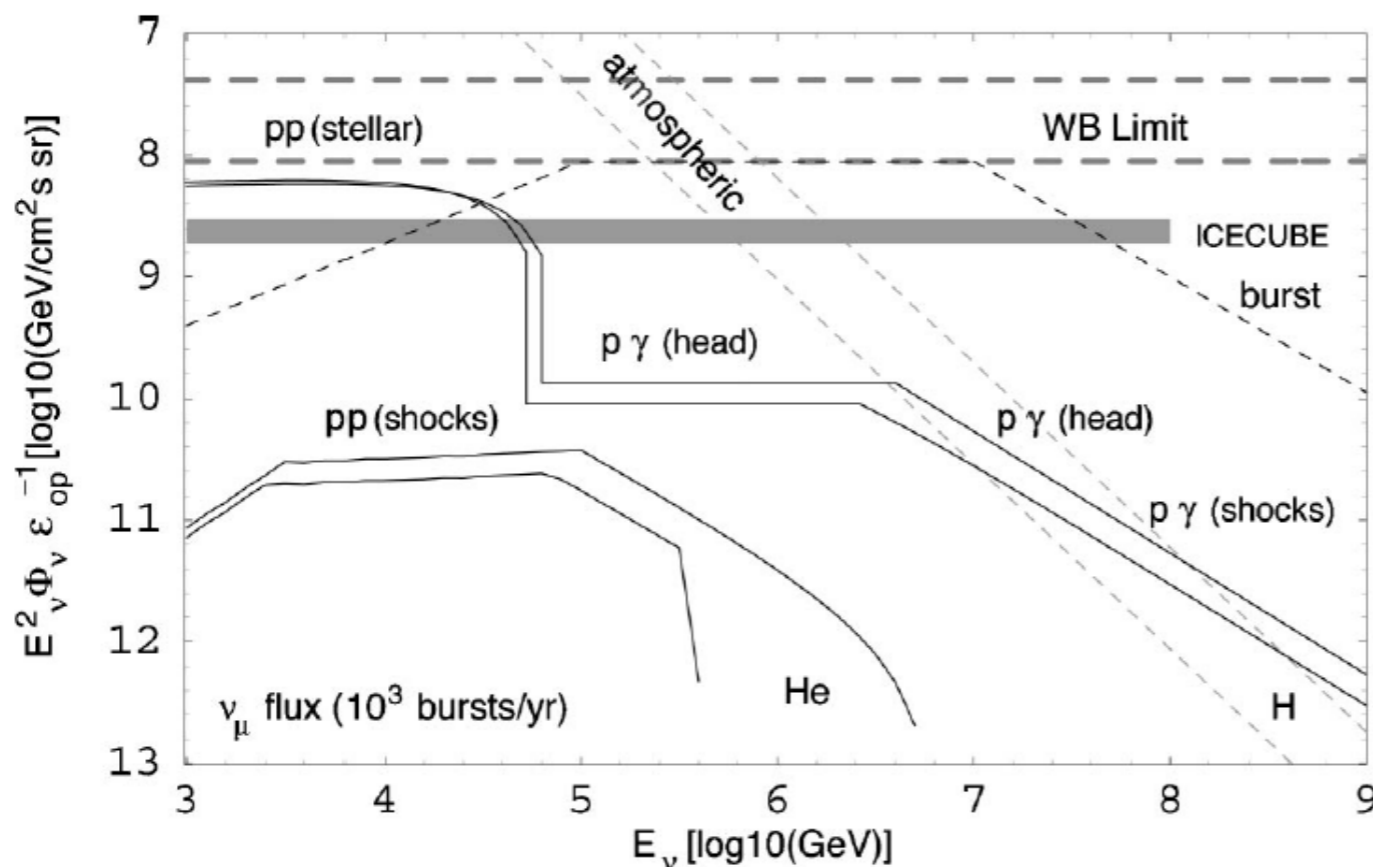


Internal shocks

$$R_i < R_* \approx \begin{cases} 10^{11} \text{ cm (He)} \\ 10^{12.5} \text{ cm (H)} \end{cases}$$

$\leftarrow$  **Diffuse flux**

No. of choked jets can be Larger than the no. of GRBs



# Prospects for HE neutrino detection

## Projected $\nu$ events for IceCube

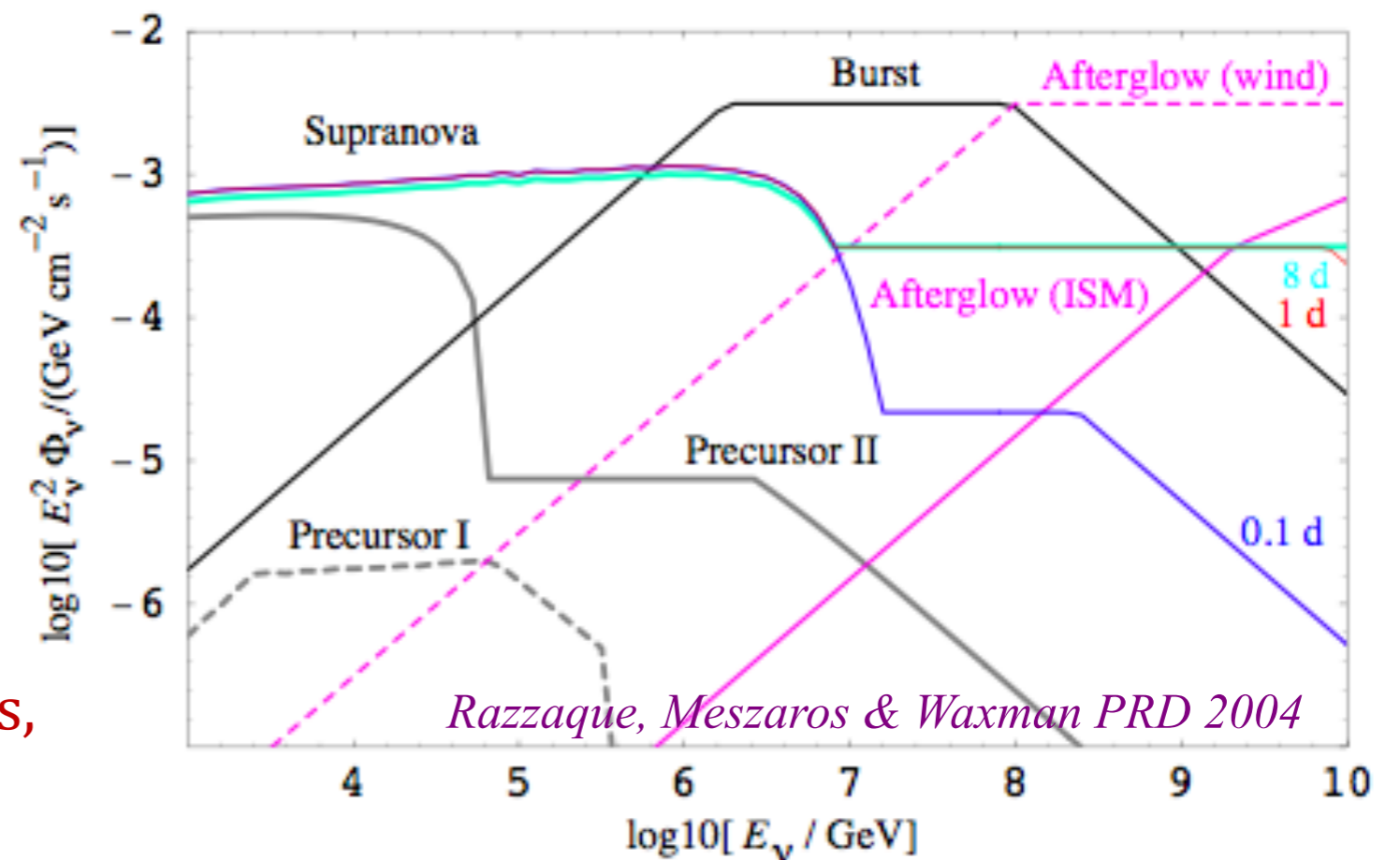
Flux model	$\nu_\mu$	$\nu_e$
Precursor I (He)	-	-
Precursor II (H)	4.1	1.1
Burst/prompt	3.2	0.3
Afterglow (ISM)	-	-
Afterglow (wind)	0.1	-
Supranova (>0.1 d)	13	2.4

$E_\nu > \text{TeV}$ , no oscillation

- Expected prompt muon neutrinos, after oscillation  $\sim 1.6$
- Current non-detection of neutrinos from GRB 130427A ( $z=0.34$ ) is consistent with prediction

## GRB 030329/SN 2003dh

Typical long duration GRB with bright SN  
 $\sim 10^{51}$  ergs/s luminosity at redshift  $z = 0.17$



Neutrino flux models:

*Dai & Lu 2000 (afterglow wind)*

*Razzaque, Meszaros & Waxman, PRL 2003 (supranova)*

*Razzaque, Meszaros & Waxman, PRD 2003 (precursor)*

*Waxman & Bahcall 2000 (afterglow ISM)*

*Waxman & Bahcall 1997 (burst/prompt)*

# Heavy Nuclei in GRBs

Nuclei from stellar core

