

NUMERICAL SIMULATIONS OF CORE-COLLAPSE SUPERNOVAE

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PLAN

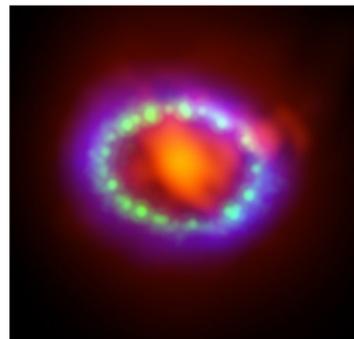
- 1 MODELS
- 2 RECENT DEVELOPMENTS
- 3 CONCLUSIONS

CORE-COLLAPSE SUPERNOVAE

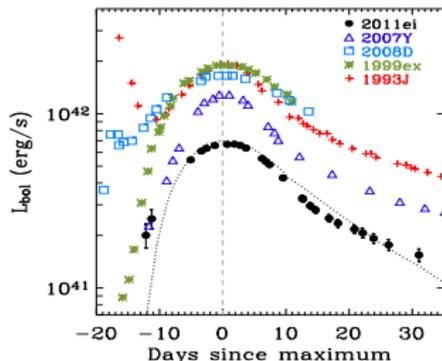
Observations of “supernovae” reported since Antiquity (SN185) \Rightarrow explosions common

Categories, depending on the spectrum:

- **Type I:** no hydrogen. Ia: ionized silicon, Ib/Ic : strong/weak presence of helium.
- **Type II:** presence of hydrogen. IIP/IIl depending on the light curve shape, IIb: spectrum changing from II to Ib.



ALMA/Hubble/Chandra

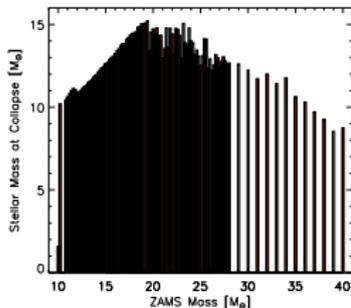


Two kinds of theoretical models:

- **Thermonuclear** supernovae: explosion of a white dwarf (runaway nuclear reactions).
- **Core-collapse** supernovae: collapse-bounce-explosion of a massive main-sequence star.

OPEN QUESTIONS...

- Why / How do massive stars explode?
- What are the properties of the final compact object at the center?
- How / Where do heavy elements form?
- What are observable signals?
- What can we learn for fundamental physics?



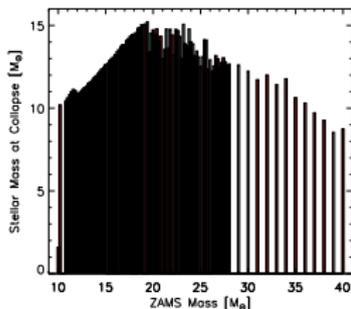
Ugliano et al. 2012

Growing number of groups:

MPA Garching (H.-T. Janka), Princeton (A. Burrows), Oak Ridge (T. Mezzacappa), Univ. Basel (M. Liebendörfer), Tokyo (S. Yamada), NAOJ/Fukuoka (K. Kotake), Caltech (C. Ott), Los Alamos (C. Fryer), France (T. Foglizzo), Univ. Valencia (M.-A. Aloy), ...

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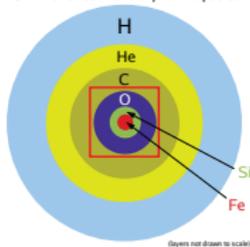
Model description

COLLAPSE AND BOUNCE

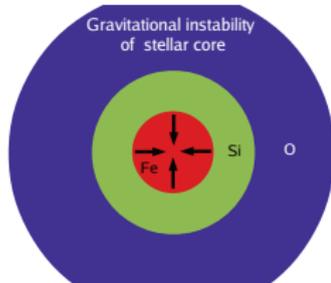
Massive ($\gtrsim 10M_{\odot}$) main-sequence star with onion-like structure:

- Iron core becomes unstable (electron degeneracy pressure)
- Collapse with electron captures on nuclei/free protons
$$p + e^{-} \rightarrow n + \nu_e$$
- Central density \sim nuclear density \Rightarrow nuclear repulsion
- Shock wave expanding outwards...

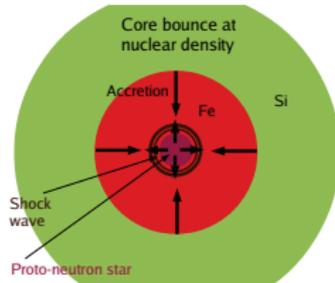
Onion-shell structure of pre-collapse star



Gravitational instability of stellar core

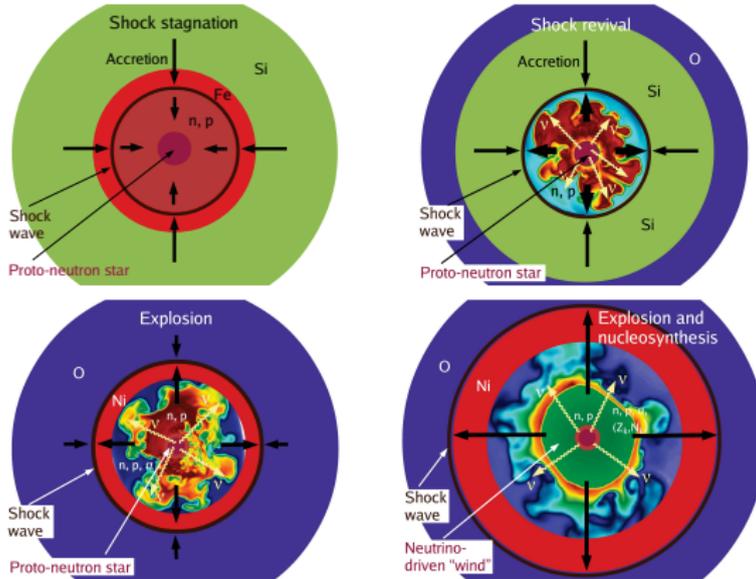


Core bounce at nuclear density



SHOCK EVOLUTION

Shock stalls, due to energy loss by iron nuclei photodissociation

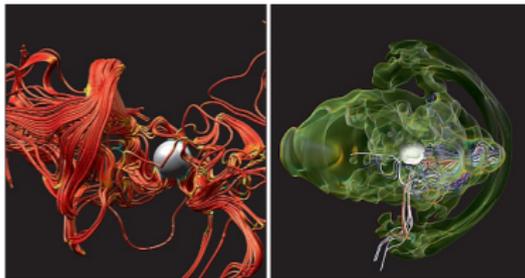


Janka et al. 2012

⇒ there must be some mechanism to **revive** the shock: transfer energy from the gravitational well to the shock.

PHYSICAL INGREDIENTS

- Progenitor model
⇒ evolution for massive stars
- Gravitation – hydrodynamics
⇒ relativistic?
- Microphysics: equation of state for hot, dense matter, out of β -equilibrium : $p(\rho, T, Y_e)$
⇒ very large range of densities, temperatures and asymmetry
- Microphysics: electron capture and neutrino reaction rates (opacities)
- Neutrino transport
⇒ 6+1 dimensions ?
- Magnetic field evolution
⇒ resistivity?



NUMERICAL CHALLENGES

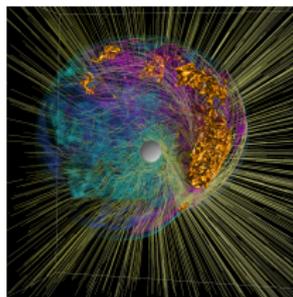
Most of supernova core-collapse simulations run on HPC centers, with millions of CPU-hours used (sometimes) for a single run:



PRACE/Curie

⇒ need for exaflop?

- Neutrino transport: ~ 100 points in each dimension $\rightarrow 10^{12}$ points ...
- Hydrodynamics: high-resolution shock-capturing methods need CPU and have poor convergence properties near the shock (unavoidable?)
- Some physical processes may need many hydro time scales to appear (e.g. SASI)
⇒ millions of time-steps (implicit for ν s)



Blondin & Mezzacappa

2007

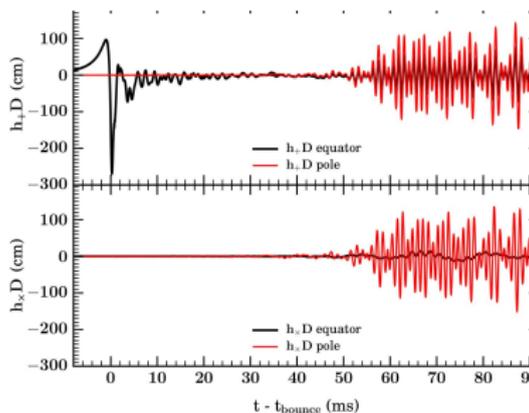
GRAVITATIONAL WAVES

SEE ALSO TALK BY M. WAS

Core-collapse supernovae are good sources of GW, although not the best ones (talk by U. Sperhake) : too close to spherical symmetry!

3 phases of GW emission associated with current simulations:

- bounce,
- post-bounce convective instabilities,
- long-term instabilities (SASI-like)



Ott 2009

What can we learn from core-collapse GW?

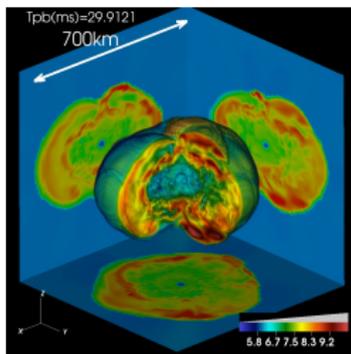
⇒ multiple bounces?

⇒ importance of convection?

⇒ development/saturation of long-term instabilities. . .

WHAT IS MISSING?

Recent 2D/3D runs show at best weak explosions : the released energy is too small!



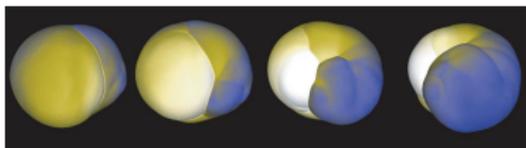
Kuroda et al. 2014

- Dimensionality: spherically symmetric simulation known not to succeed...
2D: weak explosions ... 3D?
- Resolution: are all features resolved? (turbulence, instabilities) or simulated long enough?
- Neutrino transport: too much simplified?
- More physics: Relativistic gravity (and hydro)? Magnetic field (MRI) ? Progenitor models (rotation)?
- Microphysics: are reaction rates and EoS controlled?
- ...

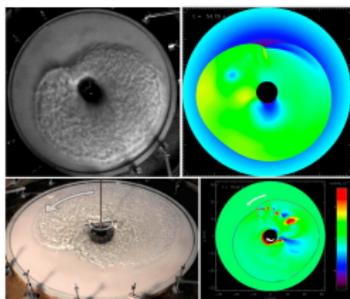
“Recent” developments

ANALOGUE SASI

Standing Accretion Shock Instability:
advective-acoustic cycle between the
proto-neutron star surface and the
stalled shock



Blondin & Mezzacappa 2007



Foglizzo et al. 2012

- Provides energy to the shock and helps neutrino heating
- Exhibited in the simplified adiabatic case (pure hydro)
- Analogy with shallow water 2D model, studied in laboratory with a simple experiment.

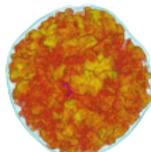
⇒ very strong indication for the existence of SASI in
supernovae: not numerical artifact

⇒ study of growth, saturation and properties of the instability,
much faster than with a code

⇒ public outreach...

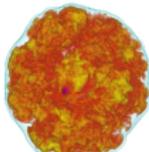
PROGENITOR DEPENDENCE

n0m0 1.02 100 ms



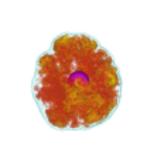
275 km

n5m2 1.02 100 ms



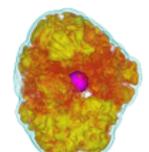
275 km

n0m0 1.02 200 ms



420 km

n5m2 1.02 200 ms



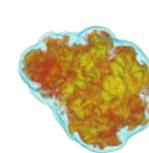
420 km

n0m0 1.02 300 ms



850 km

n5m2 1.02 300 ms



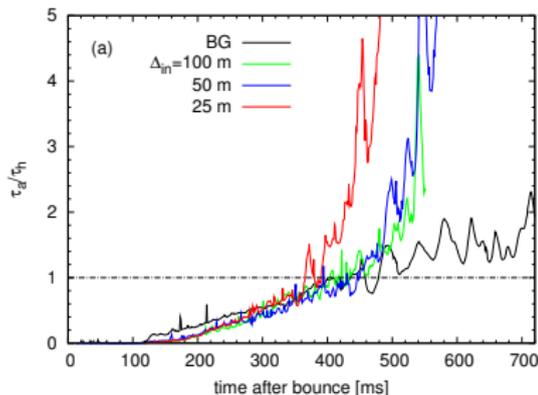
850 km

Models for progenitors very sophisticated but not enough : rotation, magnetic field, stellar atmosphere, advanced nuclear burning stages...

- Possibility of asymmetries from nuclear burning : deviation from spherical symmetry
- Study of generic asymmetries
- Evidence of more energy transmitted to the shock
- Help in explosion?

MAGNETIC FIELD

- Magnetic field is present in massive main-sequence stars
- By conservation of magnetic flux, can reach (usual) pulsar observed values ... what about magnetars?



Sawai & Yamada 2014

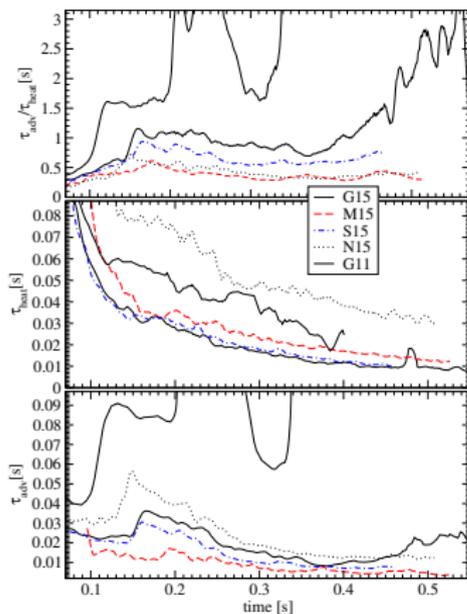
Magneto-rotational instability (MRI) is very likely to appear during core-collapse : differential rotation, magnetic field are present

⇒ Very poor knowledge on initial magnetic field and rotation profile

⇒ Need for very high numerical resolution in global simulations

⇒ What is the resistivity of matter at such densities and temperatures?

GENERAL RELATIVITY



Mueller et al. 2012

- Relativity is needed both for gravity $\left(\frac{2GM}{Rc^2} \sim 0.1\right)$ and hydrodynamics $\left(\frac{v}{c} \sim 0.3\right)$
- But difficult to build a code: coupling of dimensions in hydro, many non-linear equations for gravity, nightmare for neutrinos...

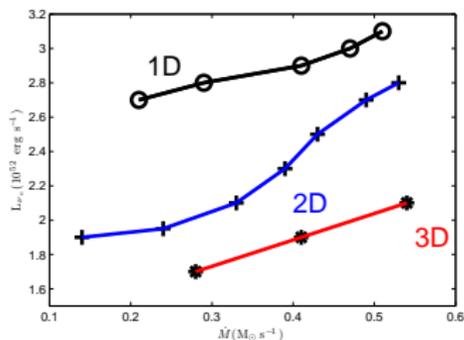
⇒ Deepening of gravitational well: more energy available Vs. more difficulties for the shock to escape ...

Unexpected : GR helps the shock !

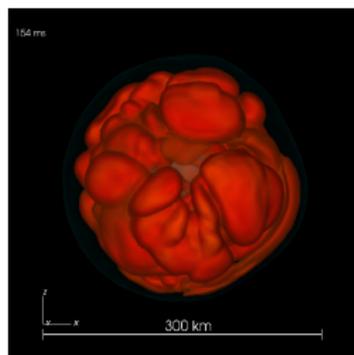
3D SIMULATIONS

Dimensionality can have great influence on the explosion mechanism:

- 1D (spherical symmetry) : no convective / turbulent motion
- 2D (axial symmetry) : inverse energy cascade for turbulence
- For neutrinos: exchange of energy in the radial directions



Nordhaus et al. 2010



Hanke et al. 2013

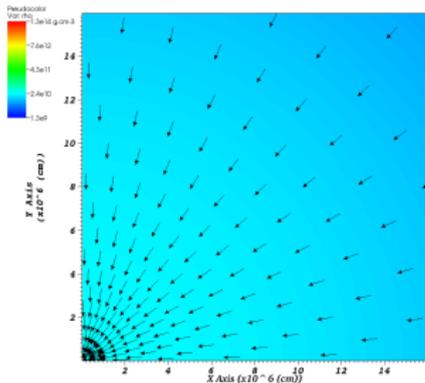
Debate on the necessity of full 3D simulations : does it help the shock to escape?

⇒ Recent simulations in 3D / GR, with sophisticated neutrino transport do not show any such trend...

MICROPHYSICS

Input from the nuclear and particle physics communities:

- New equations of state, considering full nuclear statistical equilibrium distribution (e.g. Hempel & Schaffner-Bielich 2010)
- or additional particles, as hyperons (e.g. Oertel et al. 2012)
- New electron capture rates change the shock energy (Fantina et al. 2012)

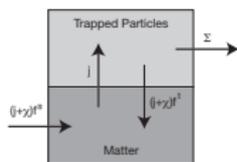


- Full nuclear distribution Vs. mean nucleus : not much effect
⇒ what about neutrino rates ?
- Phase transition to quarks or hyperons ⇒ second shock reviving the first? (Sagert et al. 2009)
⇒ Not expected in core-collapse to a neutron star; relevant for the collapse to a black hole?

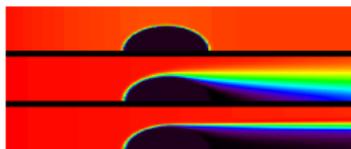
NEUTRINO TRANSPORT

Neutrino transport uses a distribution function $f(t, x^i, p^i)$:
almost impossible to solve without symmetry / approximation

- Leakage scheme (in GR: Sekiguchi 2010)
- Flux-limited diffusion (not relativistic, Bruenn et al. 1978)
- Momenta schemes + M1 closure relation (Gonzalez et al. 2007, possibly relativistic)
- Isotropic Diffusion Scheme Approximation (not relativistic, Liebendörfer et al. 2009)
- Spectral transport / ray-by-ray-plus (in GR: Müller et al. 2010)
- Full Boltzmann (in GR : Peres et al. 2014)



Liebendörfer et al.
2009



Gonzalez et al. 2007

CONCLUSIONS

- Rapidly evolving field: first 3D-GR runs, 3D-MHD approach, ...
- Multi-disciplinary field: collaborations with nuclear/particle physics \Rightarrow better microphysics
- Heavy numerical simulations, but also laboratory physics and/or analytic approaches on simplified problems
- Recent 3D simulations do not provide any definitive answer on the explosion mechanism (un)fortunately...

Possible answers:

- neutrino heating + SASI ?
- magnetic field (generic mechanism?)
- microphysics : ν -reaction rates, electron captures, ...
- ??? (not neutrino oscillations)

But we see them explode! Do we need more computer power, or a better physical model?

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