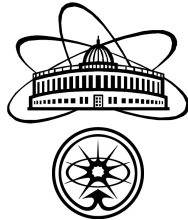


The effective nucleon axial mass approach and quasielastic neutrino event rates in NO ν A and Super-Kamiokande

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Outline

- The nucleon axial mass:
 - the problem
 - the solution concept: effective axial mass
- QES event rate calculation examples:
 - the Near Detector of $\text{NO}\nu\text{A}$
 - Super-Kamiokande
- Conclusions

QES of neutrino on the nucleon

QES section:

$$d\sigma = \frac{G_F^2 M}{16\pi^2 (kp)} \left(1 + \frac{Q^2}{M_W^2}\right)^{-2} L^{\alpha\beta} W_{\alpha\beta} \frac{d^3 \vec{k}'}{2k'_0}.$$

Lepton tensor:

$$L^{\alpha\beta}(k, k') = \begin{cases} j^\alpha(k, k') j^{*\beta}(k, k') & \text{for } \nu; \\ \bar{j}^\alpha(k, k') \bar{j}^{*\beta}(k, k') & \text{for } \bar{\nu}. \end{cases}$$

Weak lepton currents:

$$j^\alpha(k, k') = \bar{u}(k') \gamma^\alpha \frac{1 - \gamma_5}{2} u(k), \quad \bar{j}^\alpha(k, k') = \bar{v}(k) \gamma^\alpha \frac{1 - \gamma_5}{2} v(k').$$

Hadron tensor:

$$W_{\alpha\beta}(p, q) = \frac{1}{4} \int J_\alpha(p, p') J_\beta^*(p, p') \delta^4(k' + p' - k - p) \frac{d^3 p'}{2p'_0}.$$

Weak form factors of the nucleon

Weak hadron current is given by

$$J_\alpha(p, p') = V_{ud}^{\text{CKM}} \bar{u}_p(p') \Gamma_\alpha(p, q) u_n(p).$$

Basis expansion of $\Gamma_\alpha(p, q)$ comes to

$$\Gamma_\alpha(p, q) = \gamma_\alpha F_V + i\sigma_{\alpha\beta} \frac{q^\beta}{2M} F_M + \frac{q_\alpha}{M} F_S + \left(\gamma_\alpha F_A + \frac{p_\alpha + p'_\alpha}{M} F_T + \frac{q_\alpha}{M} F_P \right) \gamma_5.$$

Standard dipole parametrization of the **axial** form factor is

$$F_A(Q^2) = g_A \left(1 + \frac{Q^2}{M_A^2} \right)^{-2}, \quad g_A = -1.2695.$$

PCAC gives the formula for **pseudoscalar** form factor:

$$F_P(Q^2) = \frac{2M^2}{m_\pi^2 + Q^2} F_A(Q^2).$$

World survey of M_A

The current **best-fit** value (with 1σ and 2σ st. deviations) derived on hydrogen, deuterium and high-energy data¹:

$$M_A = 1.012 \pm 0.031 \left(\begin{smallmatrix} +0.061 \\ -0.06 \end{smallmatrix} \right) \text{ GeV.}$$

Experimental results:

NOMAD (with **stat.** and **syst.** errors)²: $M_A = 1.05 \pm 0.02 \pm 0.06 \text{ GeV.}$

K2K³: $M_A = 1.2 \pm 0.12 \text{ GeV.}$

MiniBooNE⁴: $M_A = 1.35 \pm 0.17 \text{ GeV.}$

T2K shape-fit⁵: $M_A = 1.38 \left(\begin{smallmatrix} +0.39 \\ -0.27 \end{smallmatrix} \right) \text{ GeV.}$

¹Kuzmin, Lyubushkin & Naumov, 2008; Kuzmin & Naumov, in preparation.

²Lyubushkin (NOMAD Collaboration), 2009.

³Gran (The K2K Collaboration), 2006.

⁴Aguilar-Arevalo *et al.* (The MiniBooNE Collaboration), 2010.

⁵Hadley (The T2K Collaboration), 2013.

MiniBooNE

The flux-weighted double differential cross sections for the $\nu_\mu n \rightarrow \mu^- p$ reaction.

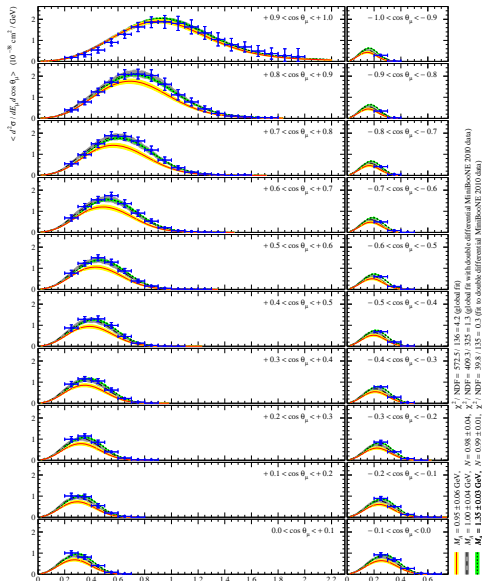
The MiniBooNE result¹:
 $M_A = 1.35 \pm 0.17 \text{ GeV}$.

The gray bands are calculated by using the nuclear model of Martini *et al.*².

Does the RFG model³ work at low energies?

¹Aguilar-Arevalo *et al.* (The MiniBooNE Collaboration), 2010.

²Martini, Ericson & Chanfray, 2011.

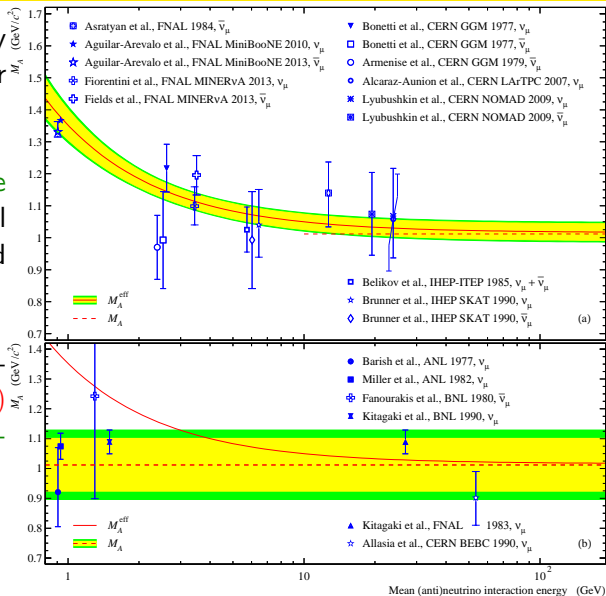


Effective (RFG) and constant M_A

We **do not have** properly working nuclear model for all energy ranges!

There is some **dependence** on E_ν in experimental values of M_A extracted with the RFG model.

So, we can fit experimental data to get $M_A^{\text{eff}}(E_\nu)$ using which **will compensate** nuclear effects.



Effective (RFG) and constant M_A

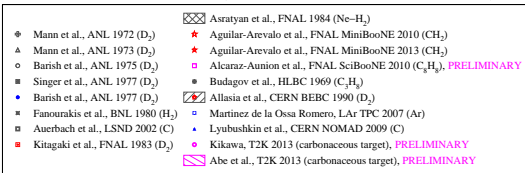
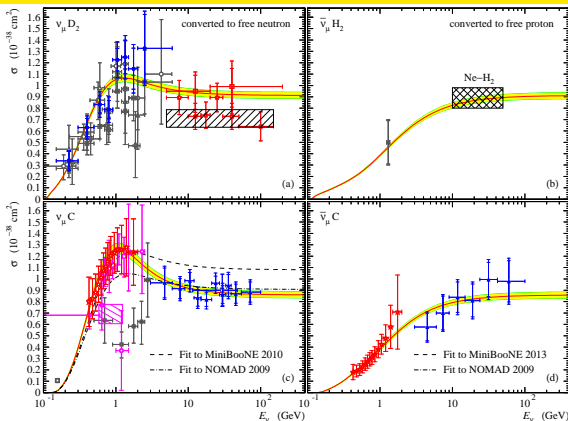
$$M_A^{\text{eff}} = M_0 \left(1 + \frac{E_0}{E_\nu} \right),$$

$$M_0 = 1.015 \pm 0.026 \begin{pmatrix} +0.032 \\ -0.031 \end{pmatrix} \text{ GeV},$$

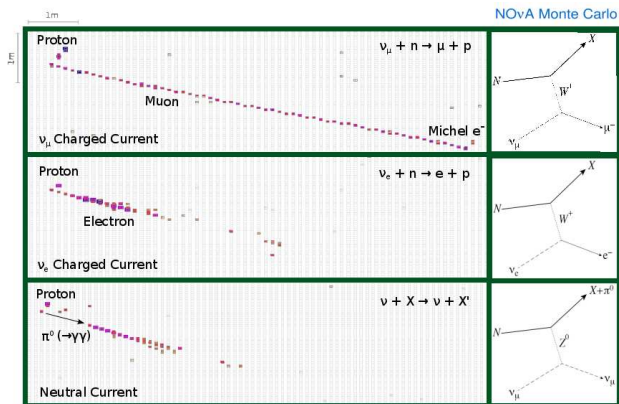
$$E_0 = 0.331 \begin{pmatrix} +0.06 \\ -0.056 \end{pmatrix} \begin{pmatrix} +0.072 \\ -0.066 \end{pmatrix} \text{ GeV}.$$

Total QES $\nu_\mu n$ & $\bar{\nu}_\mu p$ cross sections measured in experiments with deuterium, hydrogen & carbon/propane targets.¹

¹Kuzmin & Naumov, in preparation.



NO ν A event topology



ν_μ CC

- long well-defined μ -track
- short p -track with large energy deposition at the end

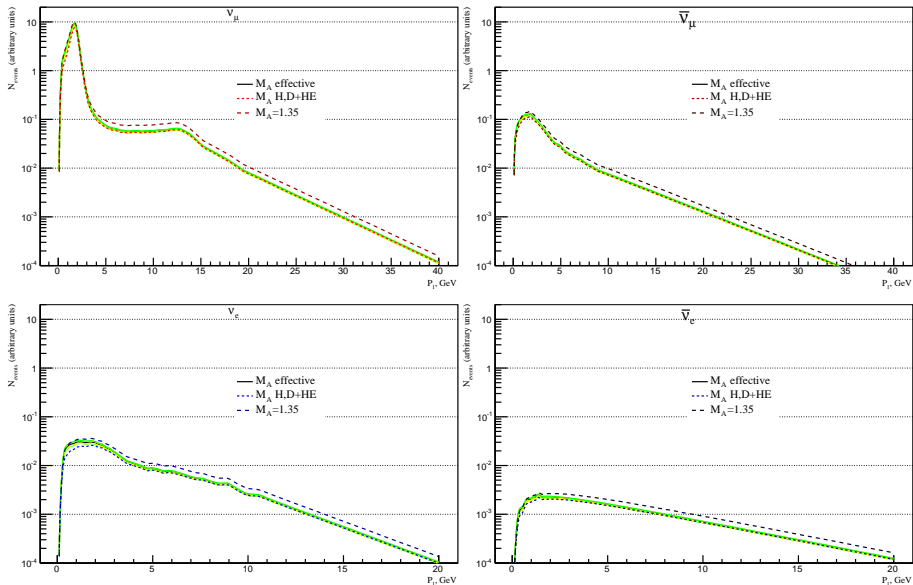
ν_e CC

- single EM shower
- characteristic development of EM shower

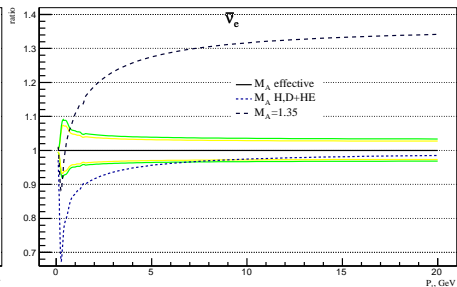
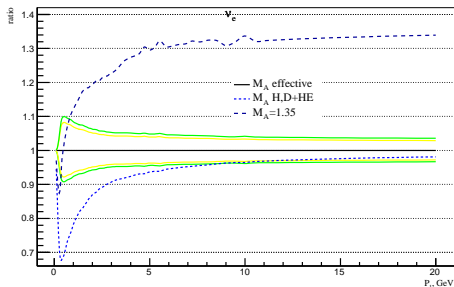
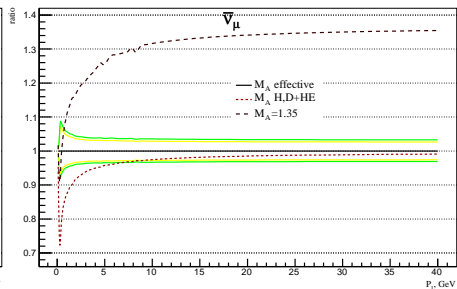
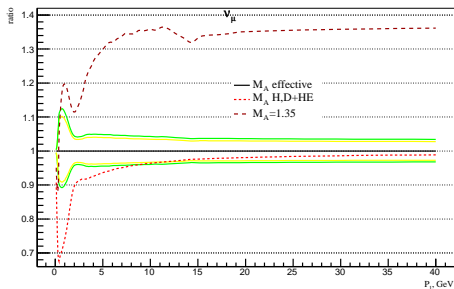
NC with π^0 final state

- multiple displaced EM showers
- possible gaps near event vertex

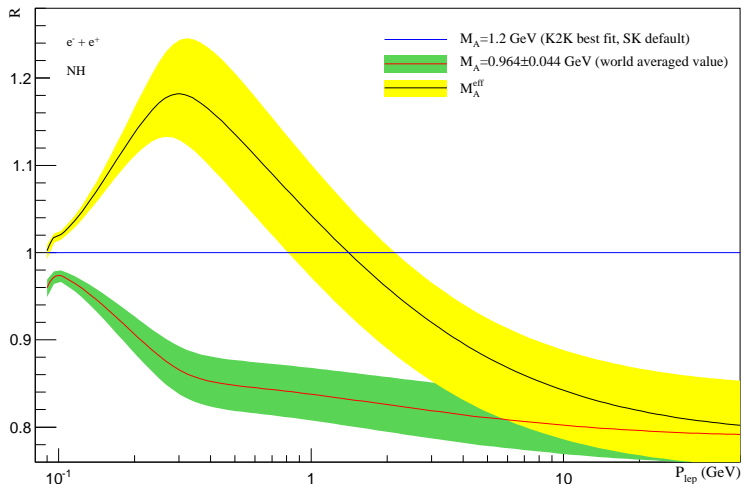
QES event rates in the Near Detector of NO ν A (ν mode)



QES event rates in the Near Detector of NO ν A (ν mode)

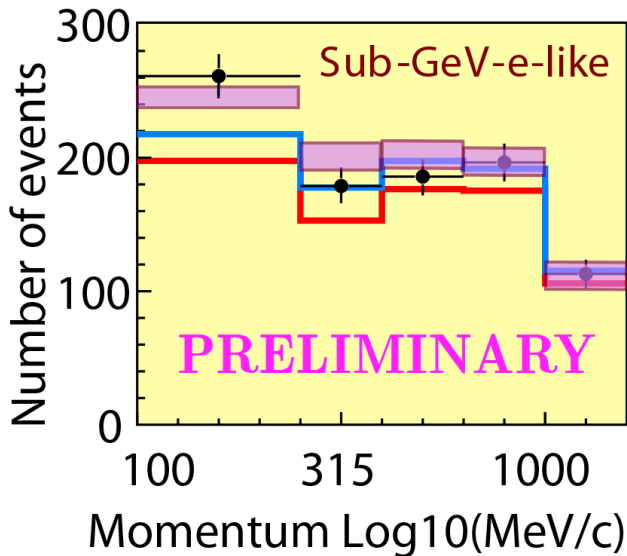


QES event rates in Super-Kamiokande



Electron QES event rates in the SK detector evaluated with several values of constant M_A and normalized to the rates calculated with the M_A^{eff} . The calculations are done for NH.

QES event rates in Super-Kamiokande



Conclusions

- The M_A value **essentially affects** the predicted count rates.
- The effect **should be taken into account**.
- Using the **effective** axial mass instead of the constant values like:
 - **1.35 GeV** (MiniBooNE)¹ or **1.38 GeV** (T2K)²
 - **1.05 GeV** (NOMAD)³should **improve the validity** of the mixing parameter values.
- The estimations presented herein are **preliminary**.

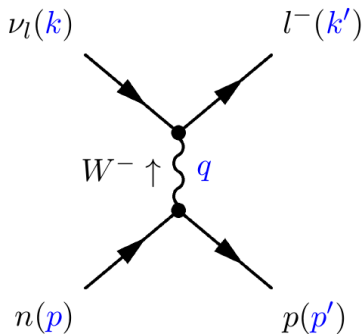
¹Aguilar-Arevalo *et al.* (The MiniBooNE Collaboration), 2010.

²Hadley (The T2K Collaboration), 2013.

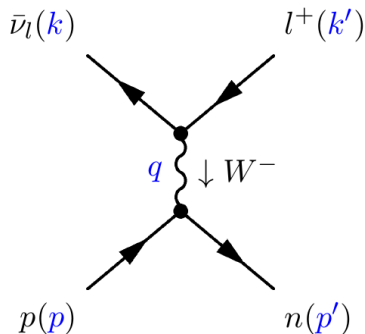
³Lyubushkin (NOMAD Collaboration), 2009.

THANK YOU!

QES of neutrino on the nucleon



$$\nu_l + n \rightarrow l^- + p$$



$$\bar{\nu}_l + p \rightarrow l^+ + n$$

$$Q^2 = -q^2$$

Electroweak form factors of the nucleon

$$\Gamma_\alpha(p, q) = \gamma_\alpha F_V + i\sigma_{\alpha\beta} \frac{q^\beta}{2M} F_M + \frac{q_\alpha}{M} F_S + \left(\gamma_\alpha F_A + \frac{p_\alpha + p'_\alpha}{M} F_T + \frac{q_\alpha}{M} F_P \right) \gamma_5.$$

C and T invariance of the hadron current \Rightarrow

$$\text{scalar } F_S = \text{tensor } F_T = 0.$$

Dirac and Pauli electromagnetic form factors:

$$F_V = \frac{G_E + x' G_M}{1 + x'}, \quad F_M = \frac{G_M - G_E}{1 + x'} \quad \text{where } x' = \frac{Q^2}{4M^2}.$$

Sachs form factors:

$$G_E = G_E^p - G_E^n, \quad G_M = G_M^p - G_M^n,$$

BBBA(2007) model is used for $G_E^{p,n}$ & $G_M^{p,n}$.

Martini *et al.* model

Martini *et al.* model incorporates relativistic corrections in the nuclear response functions and includes the multinucleon component of the “particle-hole” (2p-2h and 3p-3h contributions) processes. The model describes parameters of the “particle-hole” force which governs the collective aspect of the nuclear response via the random phase approximation. In the case of the MiniBooNE experiment multinucleon ejection is not distinguishable from single-nucleon production. The quasielastic cross section thus defined contains a certain proportion of 2p-2h and 3p-3h excitations. This proportion is large for neutrinos, which may be the interpretation of the increase in the axial cutoff mass needed to describe the data in the relativistic Fermi gas.¹

¹Martini, Ericson & Chanfray, 2011.

Neutrino oscillation theory

$$P_{\alpha\beta}(E_\nu, L) = \sum_{ij} V_{\alpha i} V_{\beta j} (V_{\alpha j} V_{\beta i})^* \exp\left(2\pi i \frac{L}{L_{ij}}\right)$$

$$L_{ij} = \frac{4\pi E_\nu}{\Delta m_{ij}^2}$$

$$V = O_{23} \Gamma_D O_{13} \Gamma_D^\dagger O_{12} \Gamma_M$$

$$\Gamma_D = \text{diag}(1, 1, e^{i\delta}), \quad \Gamma_M = \text{diag}(e^{i\phi_1}, e^{i\phi_2}, 1)$$

$$O_{12} = \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}, \quad O_{13} = \begin{pmatrix} c_{13} & 0 & s_{13} \\ 0 & 1 & 0 \\ -s_{13} & 0 & c_{13} \end{pmatrix}, \quad O_{23} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix}$$

$$s_{ij} = \sin \theta_{ij}, \quad c_{ij} = \cos \theta_{ij}$$

RFG model

$$d\sigma^b = \frac{G_F^2 M_t}{16\pi^2 (kp)} \left(1 + \frac{Q^2}{M_W^2}\right)^{-2} L^{\alpha\beta} T_{\alpha\beta} \frac{d^3 \vec{k}'}{2k'_0}$$

$$T_{\alpha\beta}(p_{\text{lab}}, q) = \int f(\vec{p}, \vec{q}) W_{\alpha\beta}(p, q) d\vec{p}$$

$$f(\vec{p}, \vec{q}) = v_{\text{rel}}^{-1} \bar{n}_i(\vec{p}) [1 - n_f(\vec{p}')]]$$

$$v_{\text{rel}} = \frac{(kp)}{M_t E_\nu}$$

Event rates

Flux of leptons l generated by QES of neutrino on one atom of ${}^Z_A\text{El}$ per second:

$$\frac{dN_l^{\text{El}}}{dp_l} = \begin{cases} \int \frac{d\sigma_{\bar{\nu}_l}}{dp_l} \bar{\nu}_l(E_\nu) dE_\nu, & \text{if El} = \text{H}; \\ \int \left(Z \frac{d\sigma_{\nu_l}^{\text{El}}}{dp_l} \nu_l(E_\nu) + (A - Z) \frac{d\sigma_{\bar{\nu}_l}^{\text{El}}}{dp_l} \bar{\nu}_l(E_\nu) \right) dE_\nu, & \text{if El} \neq \text{H}, \end{cases}$$

on one gramm $\text{El}_{n_1}^1 \text{El}_{n_2}^2 \dots \text{El}_{n_m}^m$ per second:

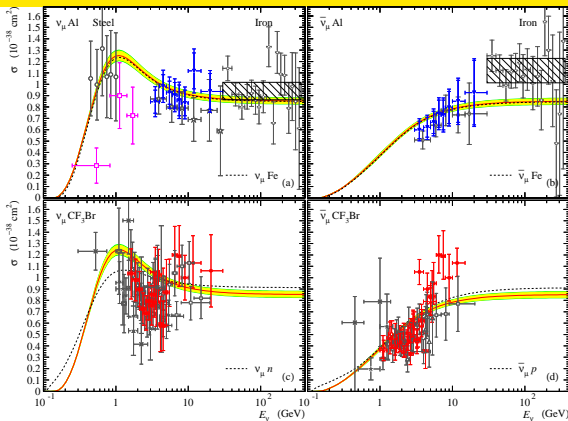
$$\frac{dN_l}{dp_l} = \frac{N_A}{\mu} \sum n_k \frac{dN_l^{\text{El}^k}}{dp_l}.$$

QES cross section analysis

QES of $\nu_\mu n$ & $\bar{\nu}_\mu p$ on aluminium, iron/steel & freon targets.

The gray points are excluded from the global fit being either superseded by newer experiments, or not satisfying selection criteria.¹

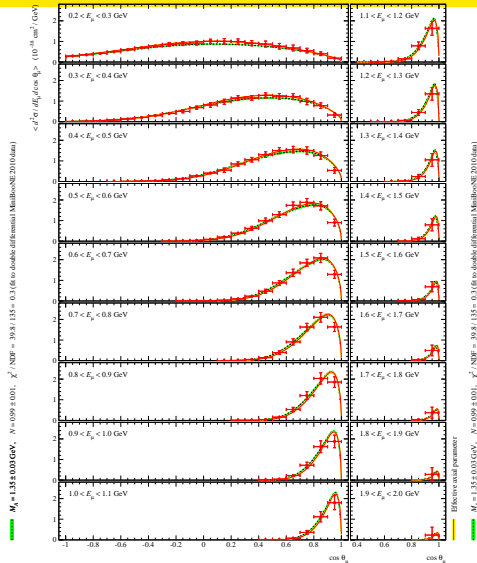
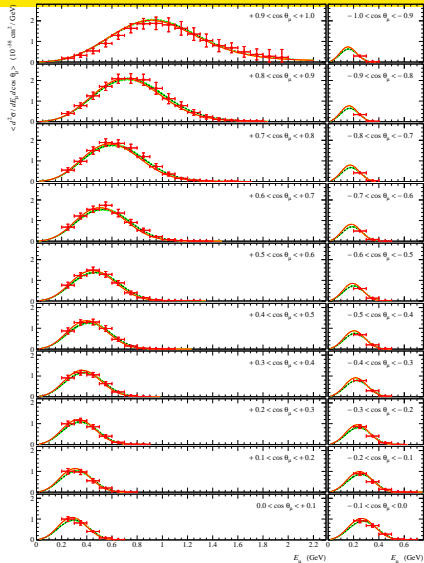
¹Kuzmin & Naumov, in preparation.



○ Kustom et al., ANL 1969 (Steel)	▽ Pohl et al., CERN GGM 1979 ($C_3H_8-CF_3Br$)
▨ Suwonjandee, FNAL NuTeV 2004 (Fe)	◊ Makeev et al., IHEP SKAT 1981 (CF_3Br)
◻ Mayer et al., FNAL MINOS 2013 (Fe), PRELIMINARY	◻ Grabosch et al., IHEP SKAT 1988 (CF_3Br)
■ Franzinetti et al., CERN HLBC 1966 (CF_3Br)	● Brunner et al., IHEP SKAT 1990 (CF_3Br)
✱ Young, CERN HLBC 1967 (CF_3Br)	◇ Belikov et al., IHEP-ITEP 1981 (Al)
■ Eichten et al., CERN GGM 1973 (CF_3Br)	★ Belikov et al., IHEP-ITEP 1982 (Al)
▲ Rollier et al., CERN GGM 1975 (CF_3Br)	● Belikov et al., IHEP-ITEP 1985 (Al)
● Bonetti et al., CERN GGM 1977 (CF_3Br)	
● Rollier et al., CERN GGM 1978 ($C_3H_8-CF_3Br$)	
▲ Armenise et al., CERN GGM 1979 ($C_3H_8-CF_3Br$)	

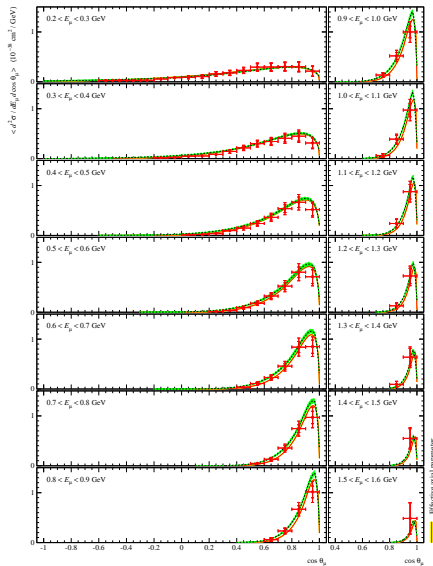
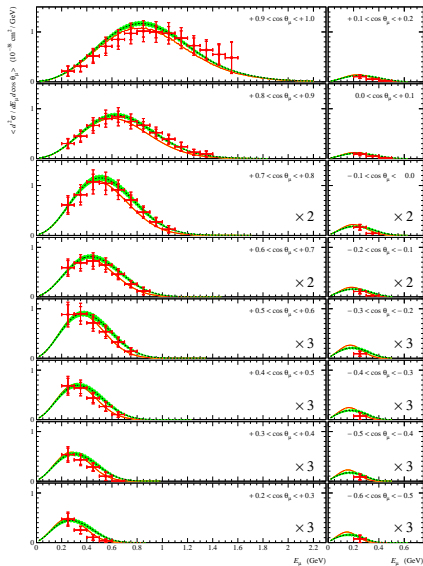
* converted to free nucleons

MiniBooNE ν

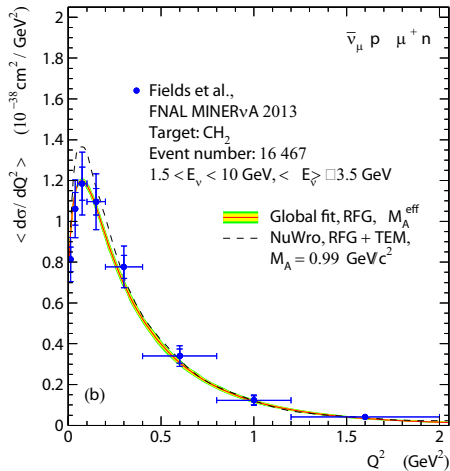
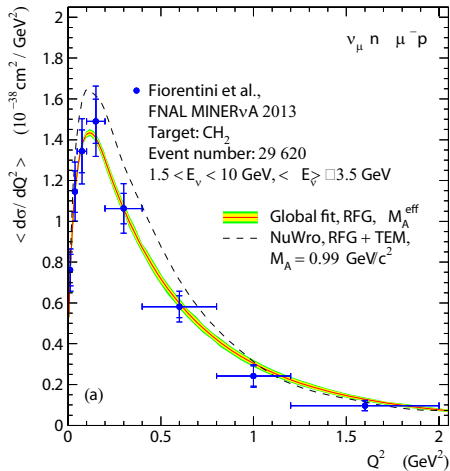


The red curves with the yellow bands are calculated by using M_A^{eff} .

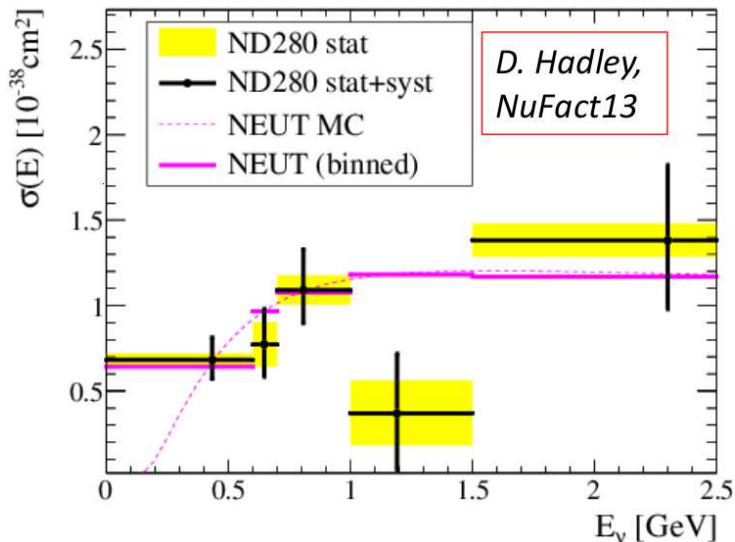
MiniBooNE $\bar{\nu}$



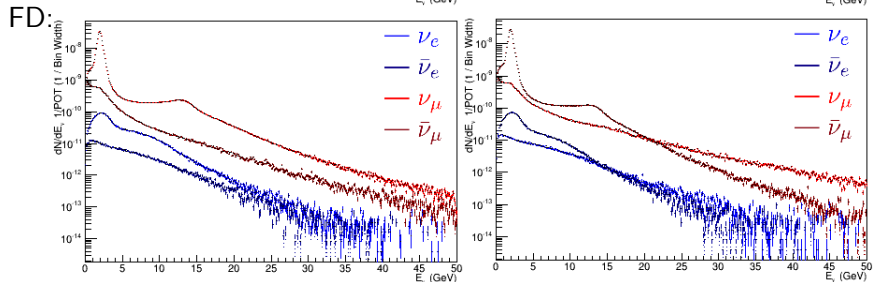
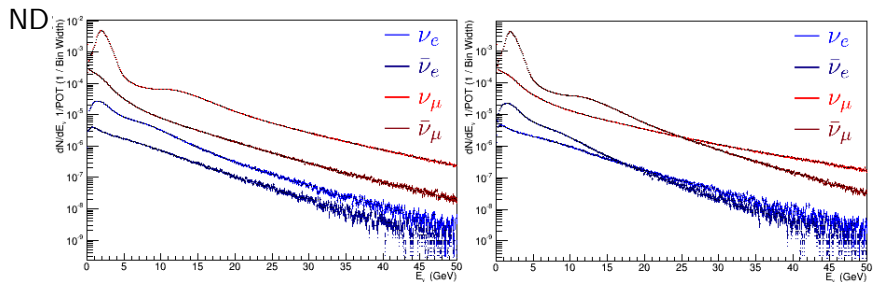
QES cross section in Minerva



QES cross section in T2K



Fluxes in $\text{NO}\nu\text{A}$

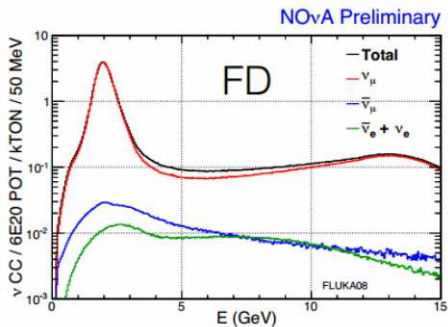


ν mode

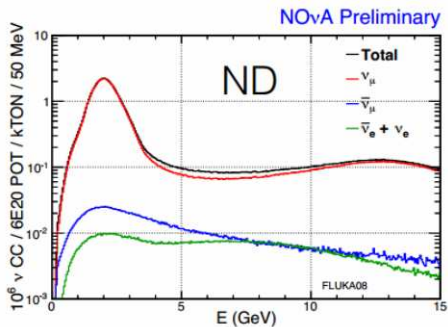
$\bar{\nu}$ mode

ν_μ CC in $\text{NO}\nu\text{A}$

ν mode:



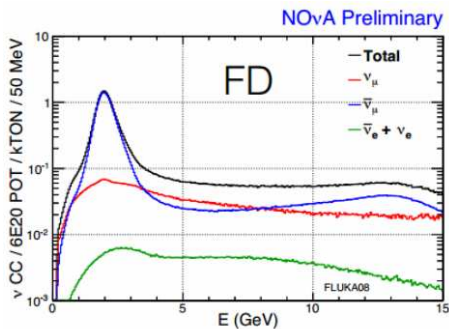
	[1,3]GeV	[0,120]Gev
Total	63.5	103.8
Numu	62.1	97.6
Anti-Numu	1.0	3.9
Nue+Anti-Nue	0.4	2.3



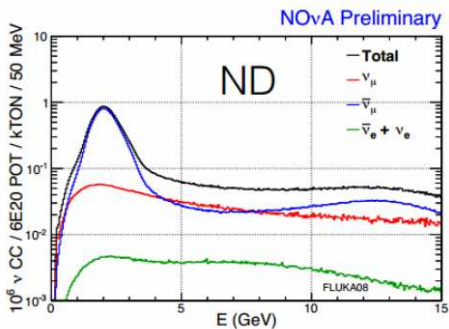
	[1,3]GeV	[0,120]Gev
Total	53.9	95.0
Numu	52.6	89.5
Anti-Numu	0.9	3.5
Nue+Anti-Nue	0.4	2.0

$\bar{\nu}_\mu$ CC in $\text{NO}\nu\text{A}$

$\bar{\nu}$ mode:

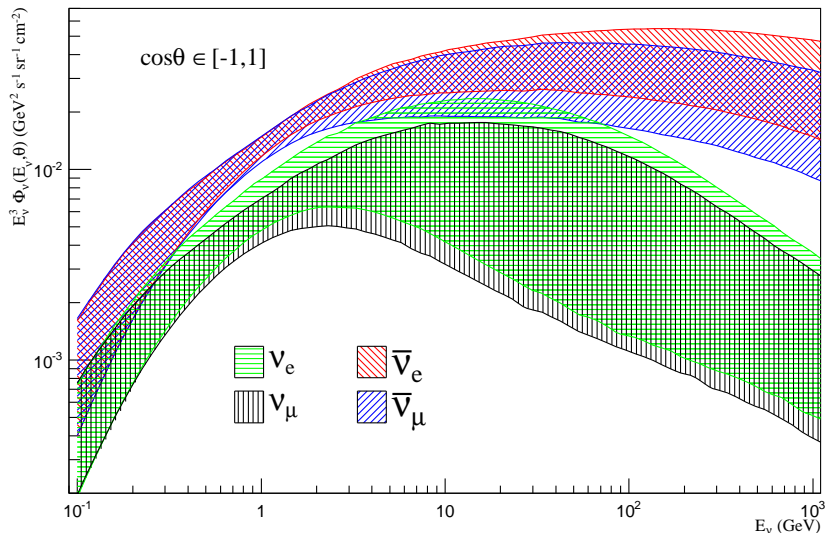


	[1,3]GeV	[0,120]GeV
Total	25.1	46.7
Numu	2.4	13.2
Anti-Numu	22.5	32.2
Nue+Anti-Nue	0.2	1.3



	[1,3]GeV	[0,120]GeV
Total	21.4	42.3
Numu	2.1	11.9
Anti-Numu	19.1	29.3
Nue+Anti-Nue	0.2	1.1

Atmospheric neutrino spectra



Atmospheric neutrino energy spectra at the Kamioka site by Honda et al.¹

¹Honda et al., 2011.

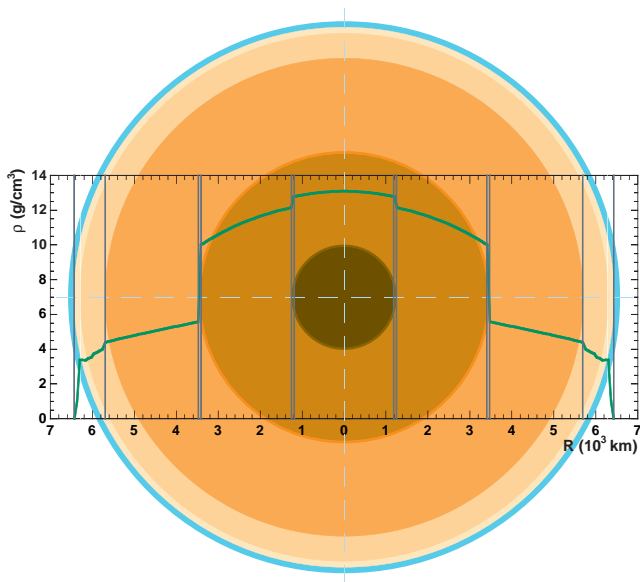
Density profile in the Earth

PREM: the Preliminary Reference Earth Model¹.

The Wolfenstein equations for the Earth density profile are solved².

¹Dziewonski & Anderson, 1981.

²Naumov, 1992.



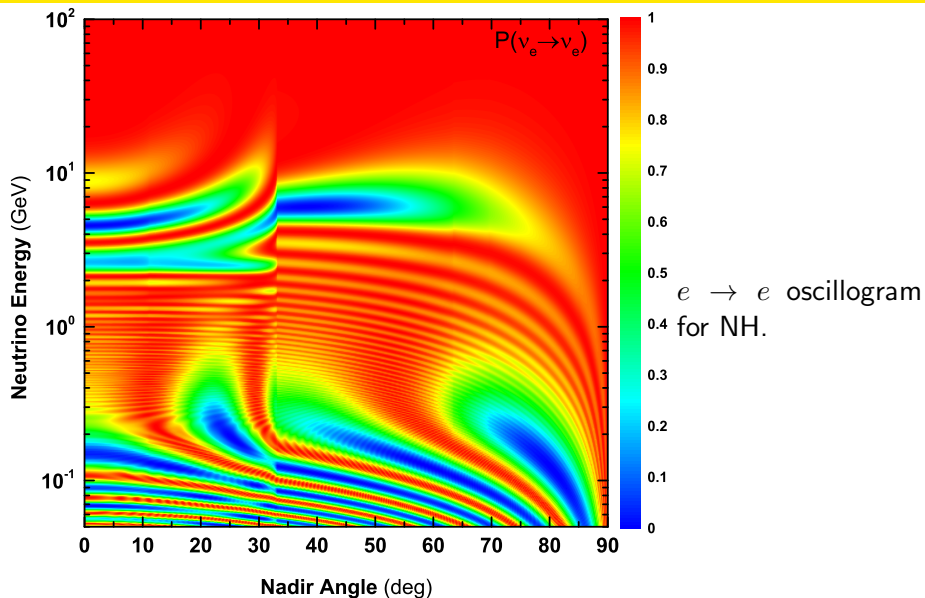
Neutrino oscillation parameters

Table: Neutrino oscillation parameters for **normal** and **inverse** mass hierarchy¹

parameter	best fit	1σ	2σ	3σ
Δm_{21}^2 [10^{-5}eV^2]	7.62	7.43 – 7.81	7.27 – 8.01	7.12 – 8.20
$ \Delta m_{31}^2 $ [10^{-3}eV^2]	2.55 2.43	2.46 – 2.61 2.37 – 2.50	2.38 – 2.68 2.29 – 2.58	2.31 – 2.74 2.21 – 2.64
$\sin^2 \theta_{12}$	0.320	0.303 – 0.336	0.29 – 0.35	0.27 – 0.37
$\sin^2 \theta_{23}$	0.613 0.600	0.400 – 0.461 0.573 – 0.635 0.569 – 0.626	0.38 – 0.66 0.39 – 0.65	0.36 – 0.68 0.37 – 0.67
$\sin^2 \theta_{13}$	0.0246 0.0250	0.0218 – 0.0275 0.0223 – 0.0276	0.019 – 0.030 0.020 – 0.030	0.017 – 0.033
δ	0.80π -0.03π	$0 - 2\pi$	$0 - 2\pi$	$0 - 2\pi$

¹Forero, Tortola & Valle, 2012.

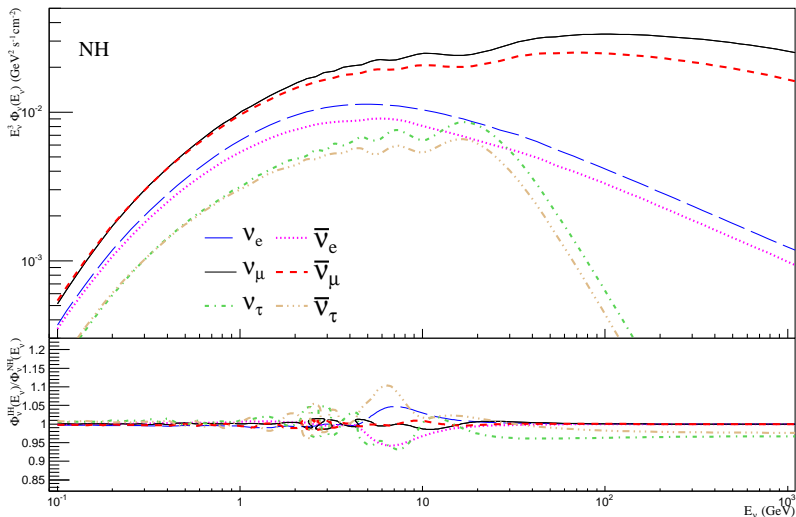
Oscillograms



Neutrino spectra

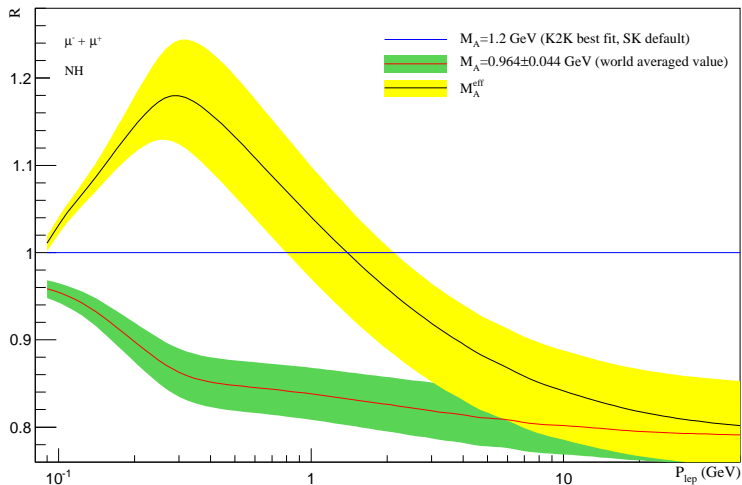
Top: NH.

Bottom: IH/NH.



Flavor transition modulated angle averaged energy spectra of atmospheric neutrinos at the Kamioka site.

QES event rates in Super-Kamiokande



Muon QES event rates in the SK detector evaluated with several values of constant M_A and normalized to the rates calculated with the M_A^{eff} . The calculations are done for NH.