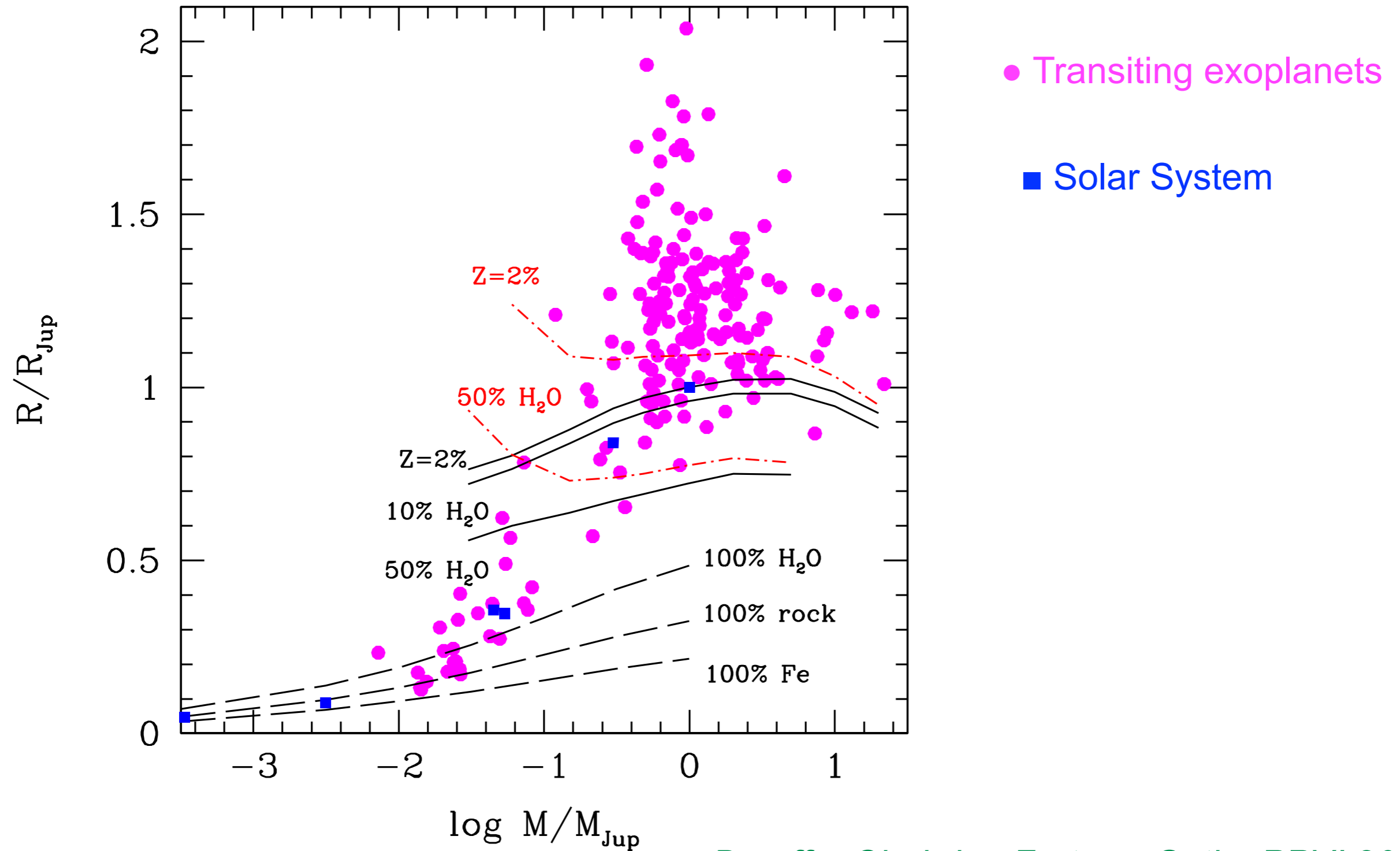


# **The diversity of exoplanet bulk compositions: Modelling structure and evolution of (exo)planets**

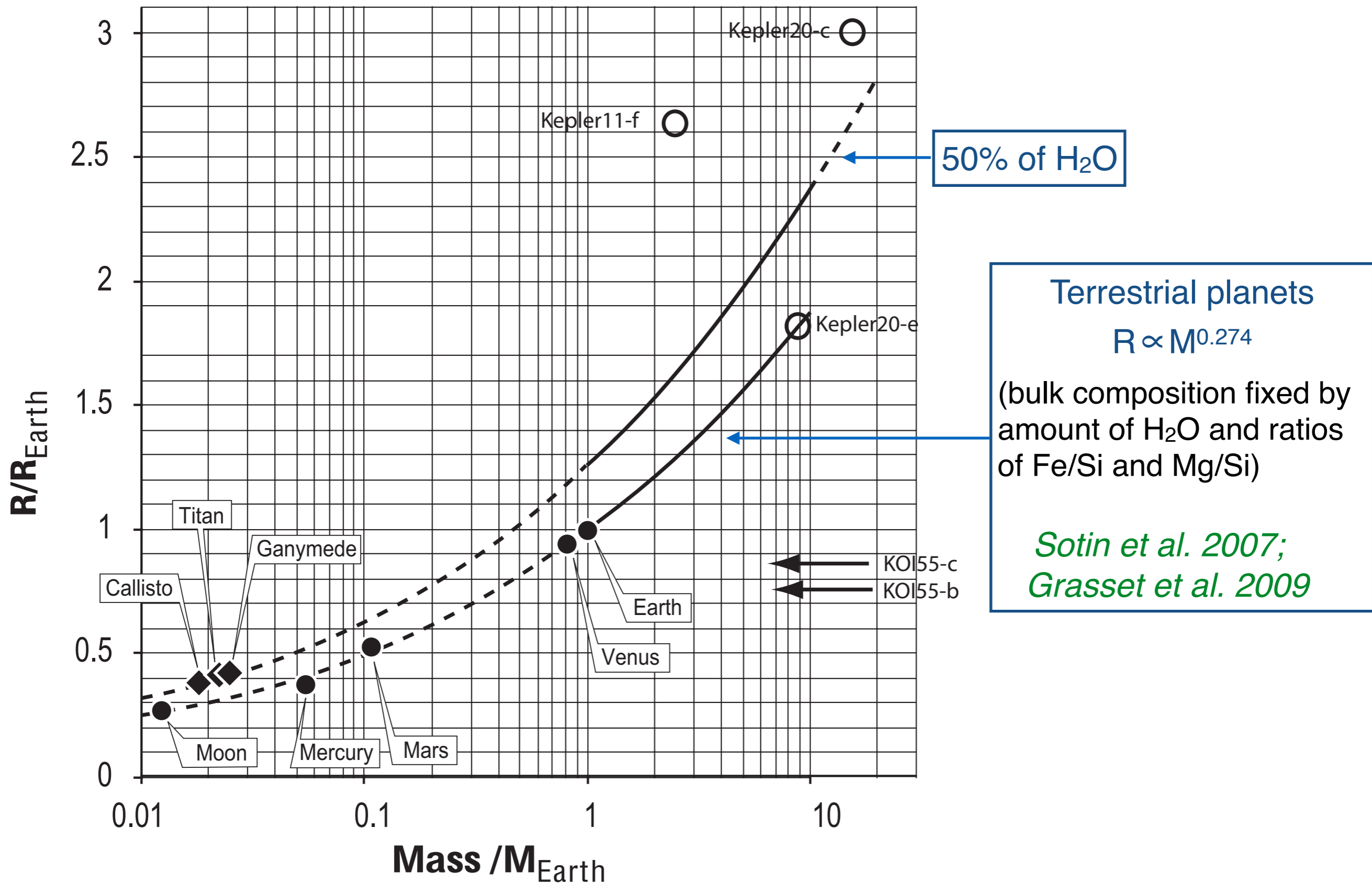
I. Baraffe (University of Exeter)



# The fact: Huge diversity of bulk compositions according to the mass-radius relationship of known planets



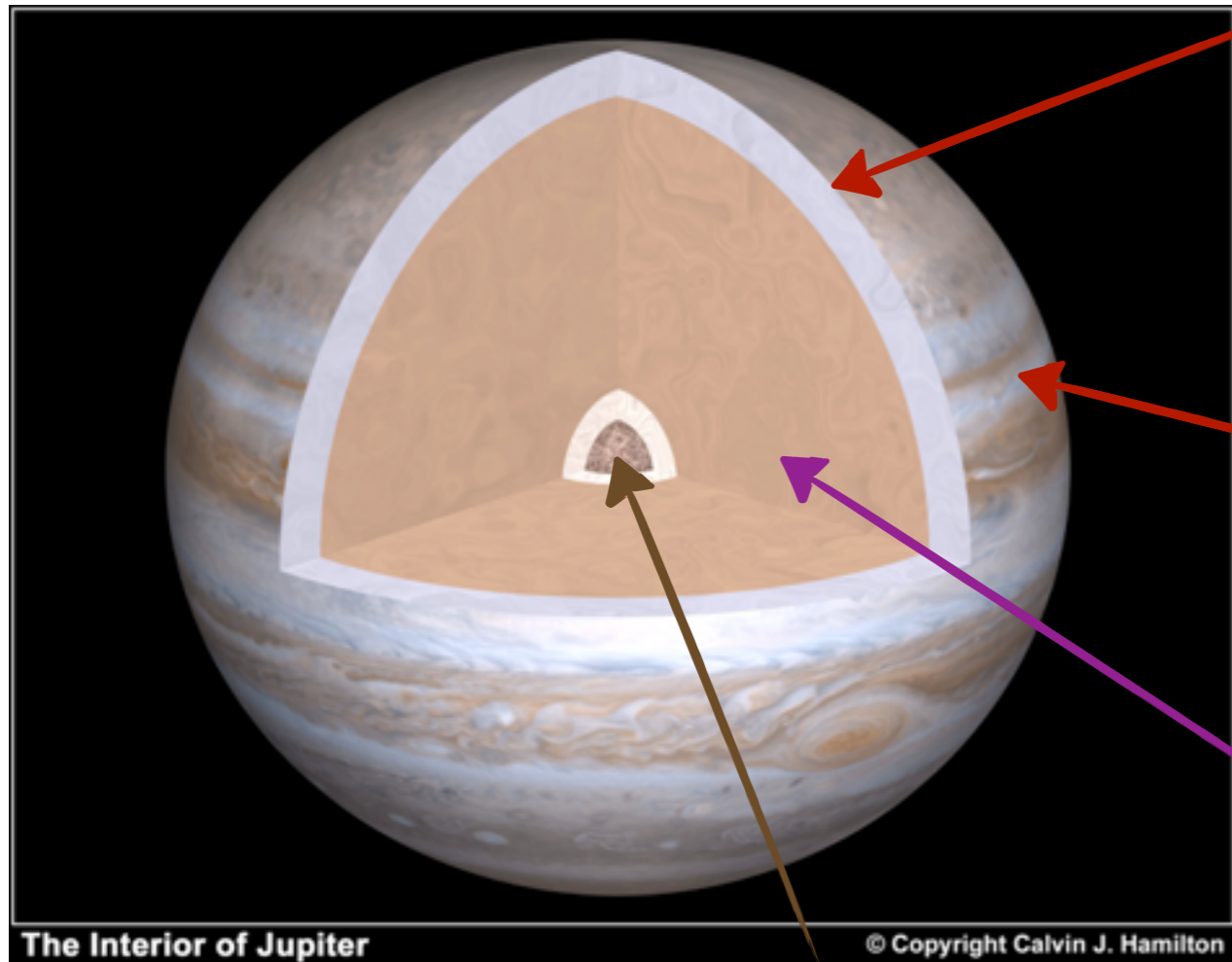
# In the realm of rocky planets: diversity seems to be also there



**The big question: Are theoretical/numerical tools ready to interpret the observed diversity?**

- I) Some lessons from our solar system planets**
- II) Exoplanets: Interior structure and evolutionary models**

# The building blocks for modelling (exo)planets



Atmospheres (1D static, irradiated/non irradiated)  
Boundary conditions for interior

Atmospheric dynamics (GCM)  
Heating processes; Ohmic dissipation; Mixing

H/He envelope  
Equation of State for H/He/Z  
Evolutionary models  
Tidal processes

Rocky/icy core  
«Ices» ( $\text{H}_2\text{O}$ ,  $\text{CH}_4$ ,  $\text{NH}_3$ ),  
silicates ( $\text{MgSiO}_4$ ,  $\text{MgSiO}_3$ , ...),  
Iron (Fe)  
☛ Earth-like: internal dynamics  
(plate tectonics, volcanism, melting)

**I) Some lessons from our solar system planets**

II) Exoplanets: Interior structure and evolutionary models:

# What do we learn from our own planets

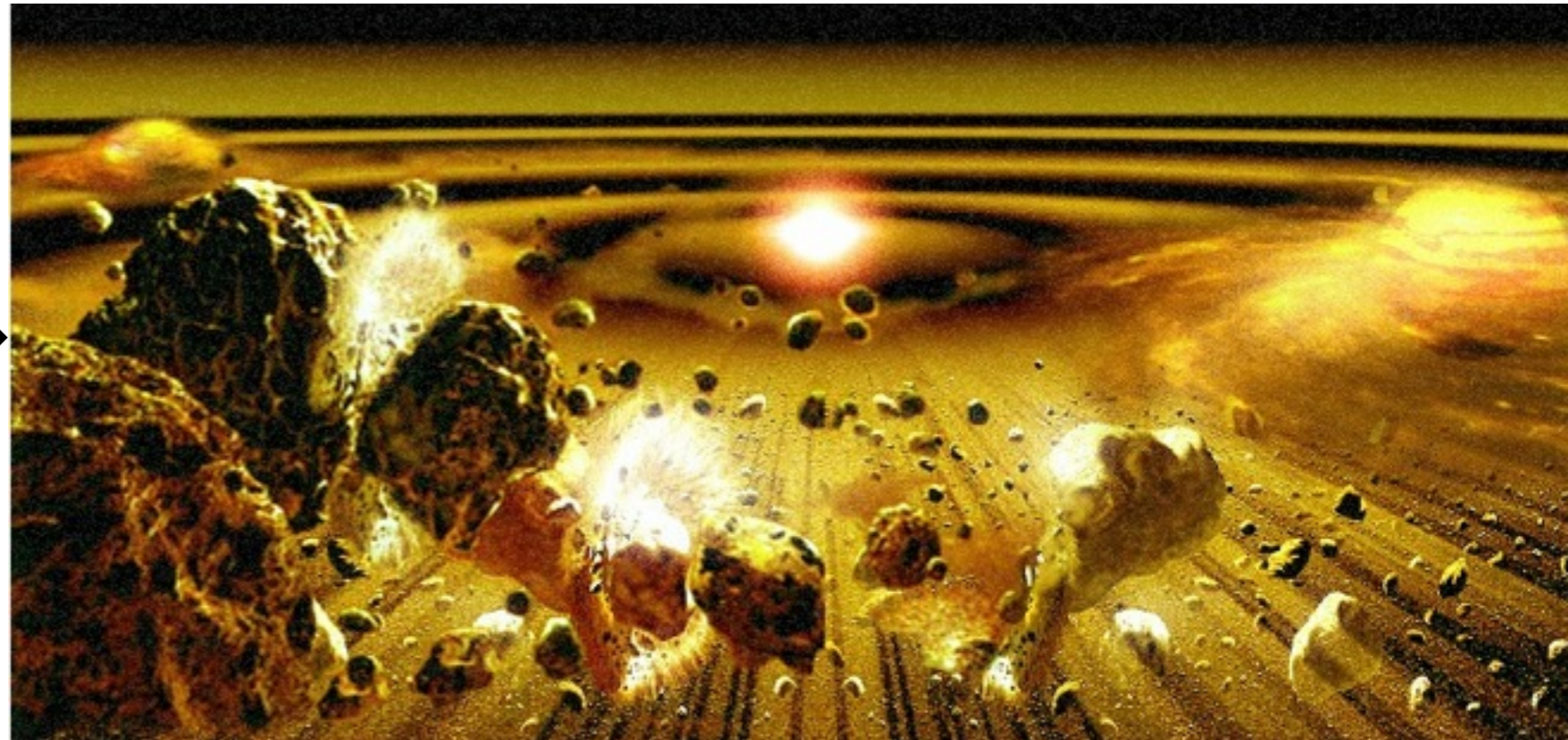
## Jupiter:

- Atmosphere depleted in He ( $Y = 0.234$ )
- Enrichment of Ar, Kr, Xe, C, N, S by a factor 2-4 over solar

## Saturn:

- He depleted, but more uncertain ( $Y = 0.18-0.25$ )
- C ( $\text{CH}_4$ ) and N ( $\text{NH}_3$ ) significantly enriched

Metal enrichment expected because of the formation in a “dirty” proto-planetary disk



## ***The standard picture for our giant planets:***

- Internal structure models commonly based on the “three-layer” picture

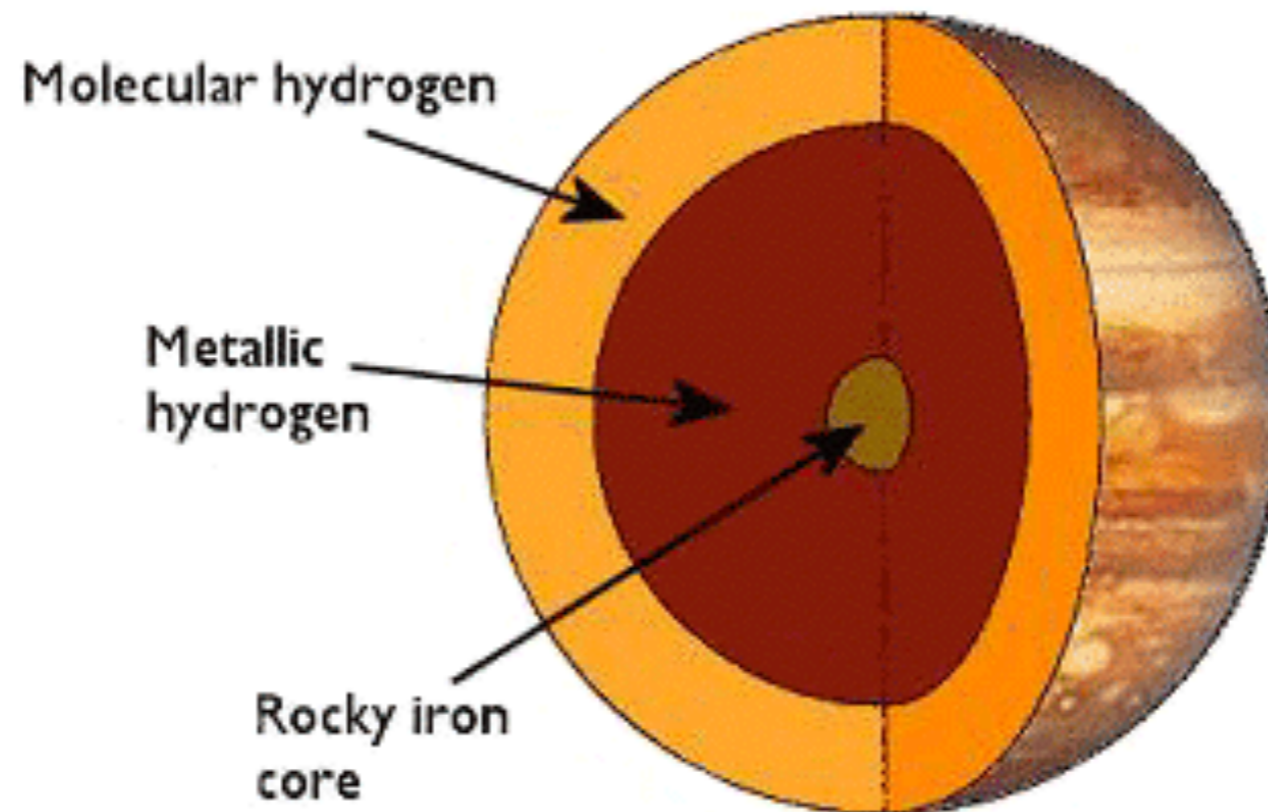
**Layer 1:** outer envelope with H<sub>2</sub>, depleted He and Z<sub>1</sub>

**Layer 2:** inner envelope with metallic H + He + Z<sub>2</sub>

**Layer 3:** central core (rock/water)

### **Different composition between layer 1 and layer 2 :**

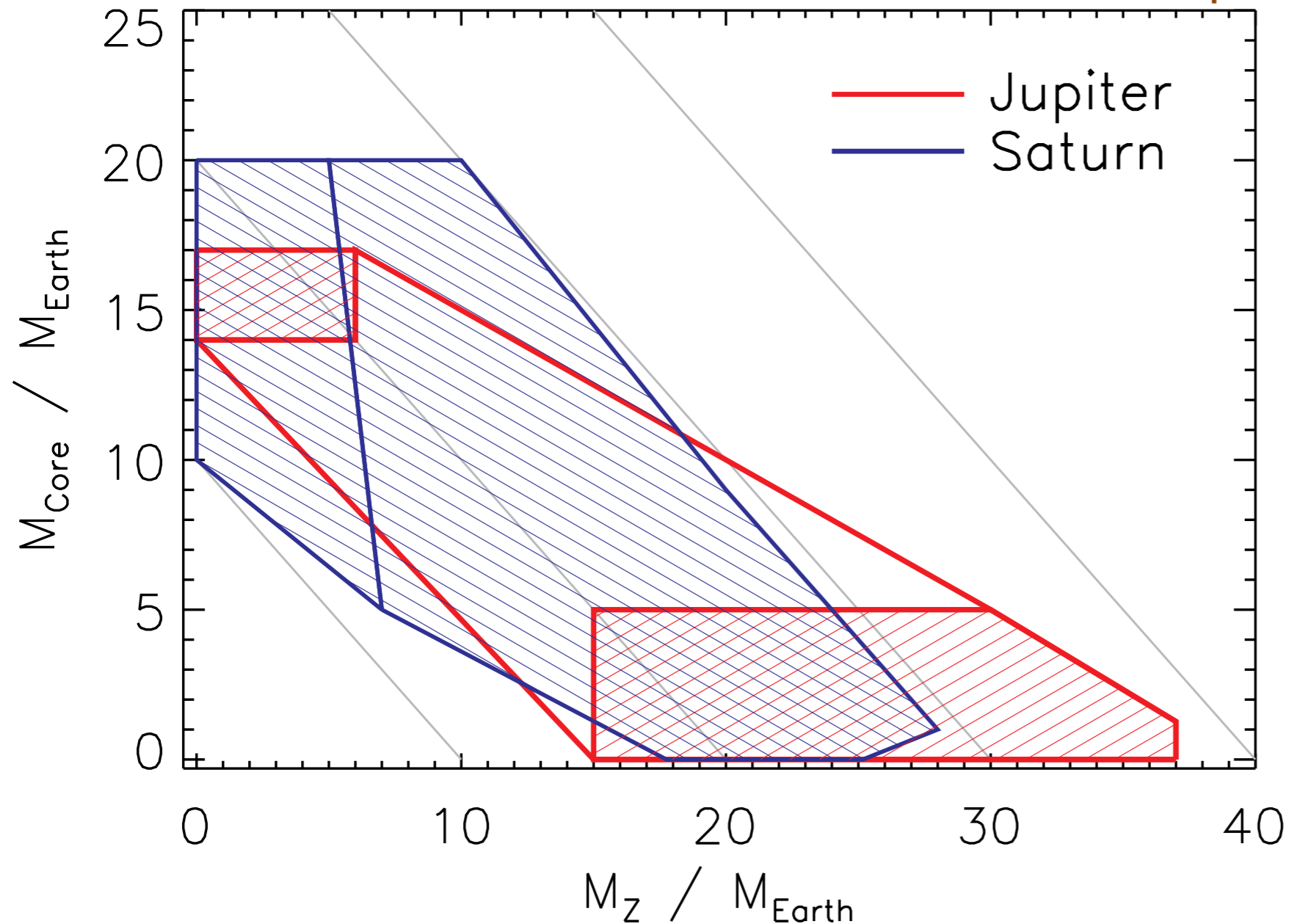
- First order transition metallic H - molecular H<sub>2</sub> (P ~ 1-2 Mbar) *Saumon & Chabrier*
  - Phase separation between H and He (He droplets rain out) *Smolugovsky 1973; Salpeter 1973*
- Layers fully convective (i.e adiabatic)



# Compositions from various modern “adiabatic” models:

Based on improved EOS (first-principle) and two- or three-layers  
(*Militzer et al. 2008; Fortney & Nettelmann 2010; Helled & Guillot 2013*)

## Metals in the core versus metals in the envelope



(see *PPVI review Baraffe et al. 2014*)

### Global enhancement in metals (compared to solar):

- Jupiter: factor  $\sim 3$  to  $8$  (if solar composition  $\Rightarrow 4.5 M_{\oplus}$  of metals)
- Saturn: factor  $\sim 12$  to  $21$  (if solar composition  $\Rightarrow 1.3 M_{\oplus}$  of metals)

## An illustration of current uncertainties from EOS:

➡ Predictions based on first-principle EOS for H/He (continuous molecular to metallic H transition) and a **2-layer** model (core of rock/H<sub>2</sub>O and isentropic mantle of H/He)

⇒ Find a core for Jupiter of  $M_{\text{core}} = 14-18 M_{\oplus}$  (*Militzer et al. 2008*)

⇒ Previous idea of a **small core** for Jupiter **challenged** by those recent calculations

➡ **Strong disagreement** with another study also based on ab initio EOS calculations for H, He and H<sub>2</sub>O (*Nettelmann et al. 2008*)

based on a **3-layer** model: core of rocks/ice + inner isentropic envelop (Metallic H, He,  $Z_{\text{met}}$ ) + outer isentropic envelope (molecular H<sub>2</sub>, He,  $Z_{\text{mol}}$ )

⇒ Find a core for Jupiter of  $M_{\text{core}} = 0-7 M_{\oplus}$

**Key takeaway:** better understanding of H/H<sub>2</sub> transition and of H-He demixing from first-principle EOSs is key to predict more accurate giant planet structures.

# Adiabatic interior (fully convective): revisiting the standard picture?

## Reduced heat transport in planetary interiors:

(Stevenson & Salpeter 1977; Stevenson 1979; Chabrier & Baraffe 2007)

- **Idea:** reduced heat transport in planetary interior due to **molecular weight gradient**

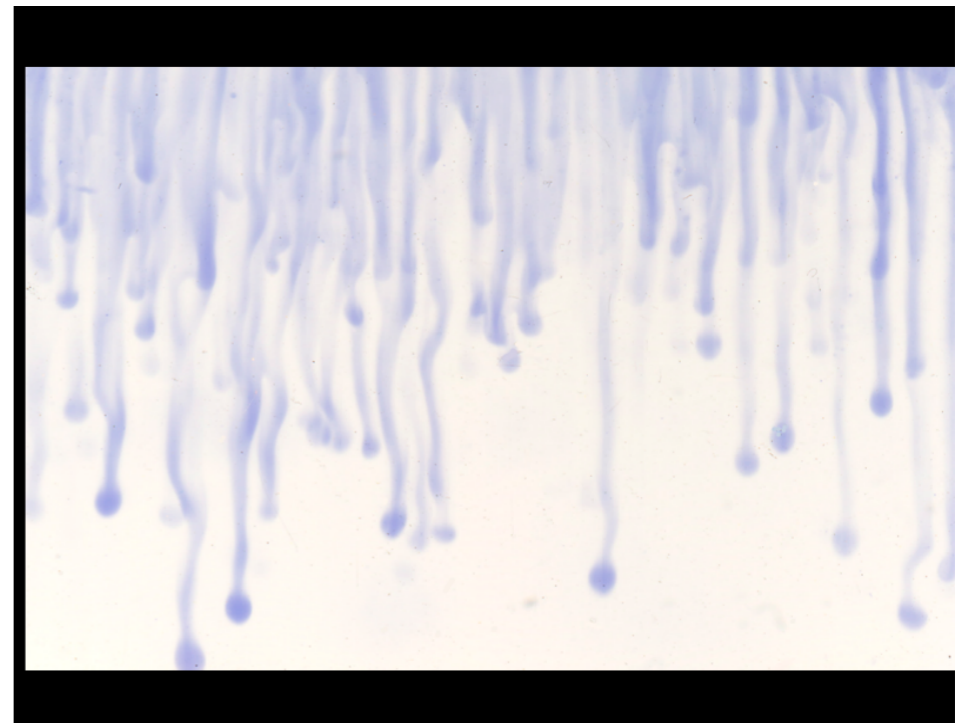
Presence of  $\nabla_{\mu}$  ---> Stabilizing effect against convection

$$\nabla_{\text{ad}} > \nabla_{\text{T}} + \nabla_{\mu} \chi_{\mu} / \chi_{\text{T}} \quad (\text{Ledoux criterion})$$

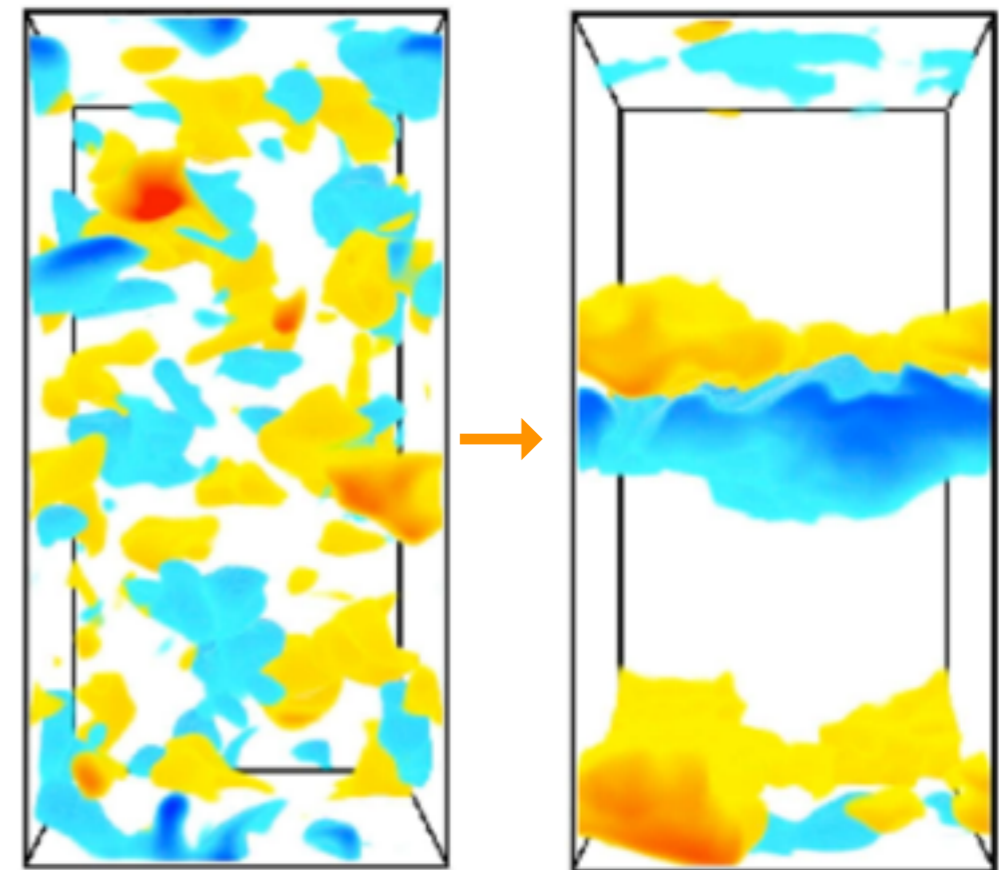
⇒ « **layered convection** » : system of convective layers + thin diffusive layers  
(*double diffusive convection or semiconvection*)

Process which may occur in a medium where two substances diffuse at a different rate

- When the **fastest** diffusive substance is **stabilizing**  
-----> **salt fingers**



- When the **fastest** diffusive substance is **destabilizing**  
-----> **formation of diffusive layers**



**In ocean, planets and stars:**  
**heat is the fastest diffusive substance**

**Layers formation** are **observed** in oceans and laboratory experiments

**3D numerical simulations:**

- ➔ Layers can form in low-Pr ( $< 1$ ) double diffusive convection (*Rosenblum et al. 2011*)

- Origin of the molecular weight gradient:
  - **Formation process:** during accretion of planetesimals in the gaseous envelope  
*But can such a gradient survive few Gyr?*  
May affect the luminosity of young planets (the GPI & SPHERE targets)  
➡ much fainter planets
  - **Core erosion:**  
recent Molecular Dynamics simulations suggest immiscibility effects at T-P  
relevant to the core-envelope boundary of jovian planets (*Watson & Millitzer 2012*)  
➡ H<sub>2</sub>O and MgO (e.g rocky material) are soluble in hydrogen

## Double-diffusive convection in Jupiter and Saturn?

(Leconte & Chabrier 2012, 2013 Nature Geosc.)

- ➡ Non conventional interior model for J and S  
core + inhomogeneous, “semiconvective” envelope
- ➡ Reproduce the gravitational moments  $J_2$  and  $J_4$ 
  - **Jupiter:**  $M_{\text{core}} = 0 - 0.5 M_{\oplus}$   
 $Z_{\text{tot}} = 13\% - 20\%$  (previous:  $Z_{\text{tot}} = 2.5\% - 12\%$ )
  - **Saturne:**  $M_{\text{core}} = 12 - 21 M_{\oplus}$   
 $Z_{\text{tot}} = 28\% - 44\%$  (previous:  $Z_{\text{tot}} = 13\% - 29\%$ )
- ➡ **Layered convection** could explain Saturn’s luminosity anomaly  
(*anomalously high intrinsic flux that adiabatic models cannot reproduce*)

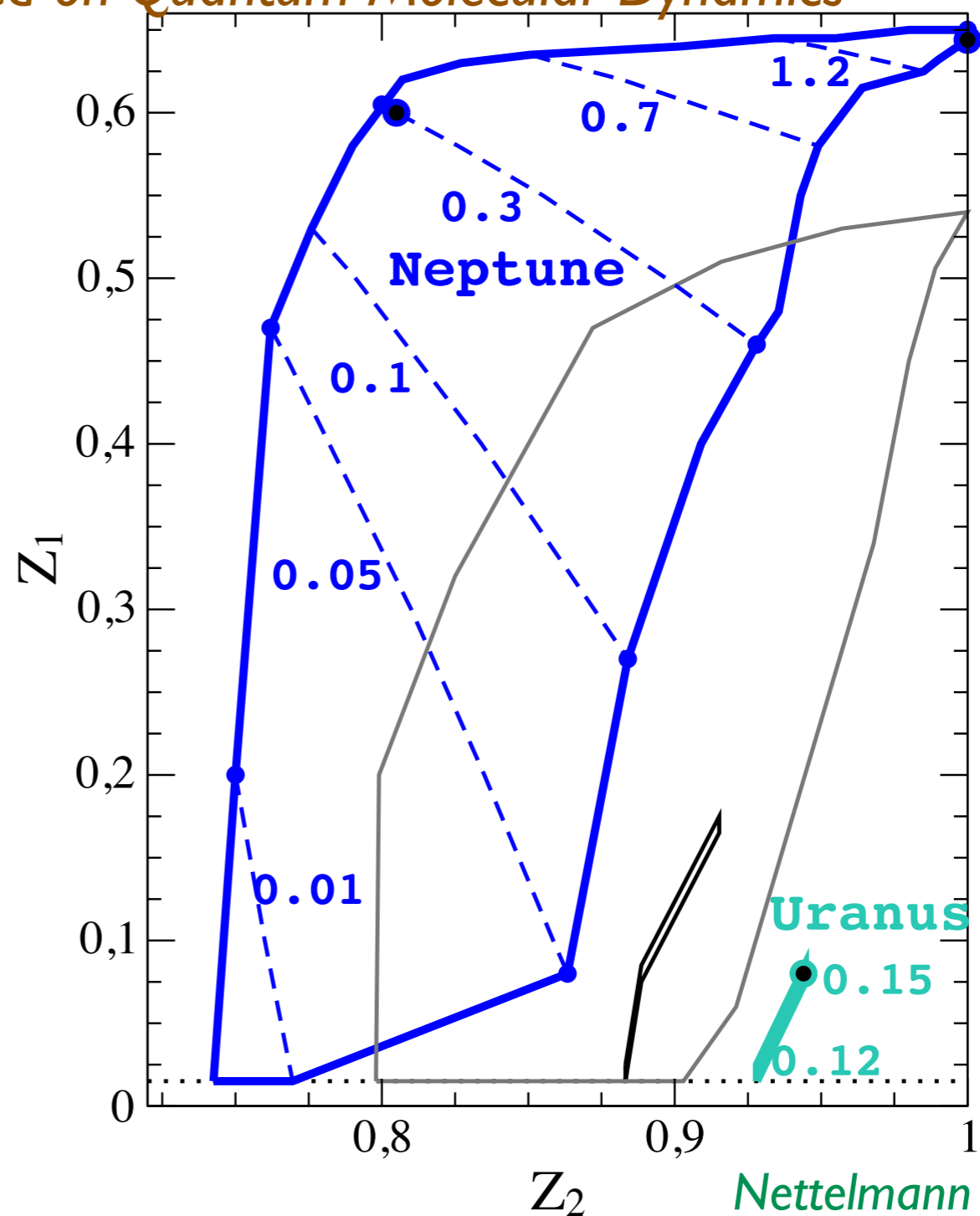
**Inhomogeneous models for Jupiter and Saturn would be significantly more enriched in heavy material (30%-60% more) than adiabatic models.**

# Recent models for Uranus & Neptune:

Recent models by Nettelmann et al. 2013: constraint the metallicity of the “water-rich” inner envelope with  $Z_2$  and the H-He rich outer envelope with  $Z_1$

*(water EOS of French et al. (2009) based on Quantum Molecular Dynamics simulations)*

- Improved gravity field data (long term observations of planet's satellite motions)
- Modified shape and rotational periods compared to Voyager data



# First conclusions of planetary interior structures:

➡ Remaining uncertainties on interior structure models of our own giant planets (EOS, amount of heavy elements, size of core)

⇒ large uncertainties on the determination of exoplanet internal compositions from observed mass-radius

➡ Progress are coming with **improved EOS** of H/He and heavy materials (water, silicates, etc) at high pressure and high temperature (*see next talk by S. Mazevet*)

- ➡ **First applications to our Solar System Planets**
- ➡ **Preliminary application to exoplanets**

# Future missions in the Solar System to improve planetary models

- **Juno (2016): for Jupiter**

- Mapping accurately gravitational moments up to  $J_{12}$

- constraint on the density distribution and internal structure

- constraints on differential or solid body rotation of the outer layers

- Mapping of the magnetic field

- Spectroscopy of thermal emission down to 100 bars

- measure of  $H_2O$  and  $NH_3$  mixing ratios

- **Final stages of Cassini (2017): for Saturn**

- Precision mapping of gravitational moments (up to  $J_{10}$ ) and magnetic fields

- Possible in situ sampling of atmospheric mixing ratios

- (heroic death with the craft manoeuvred down in the atmosphere)*

- **Seismology:**

- First detection of Jupiter's oscillations by SYMPA (*Gaulme et al. 2011*)

- Detection by Cassini of spiral structures in Saturn's ring which could be due to perturbations from Saturn's free oscillations

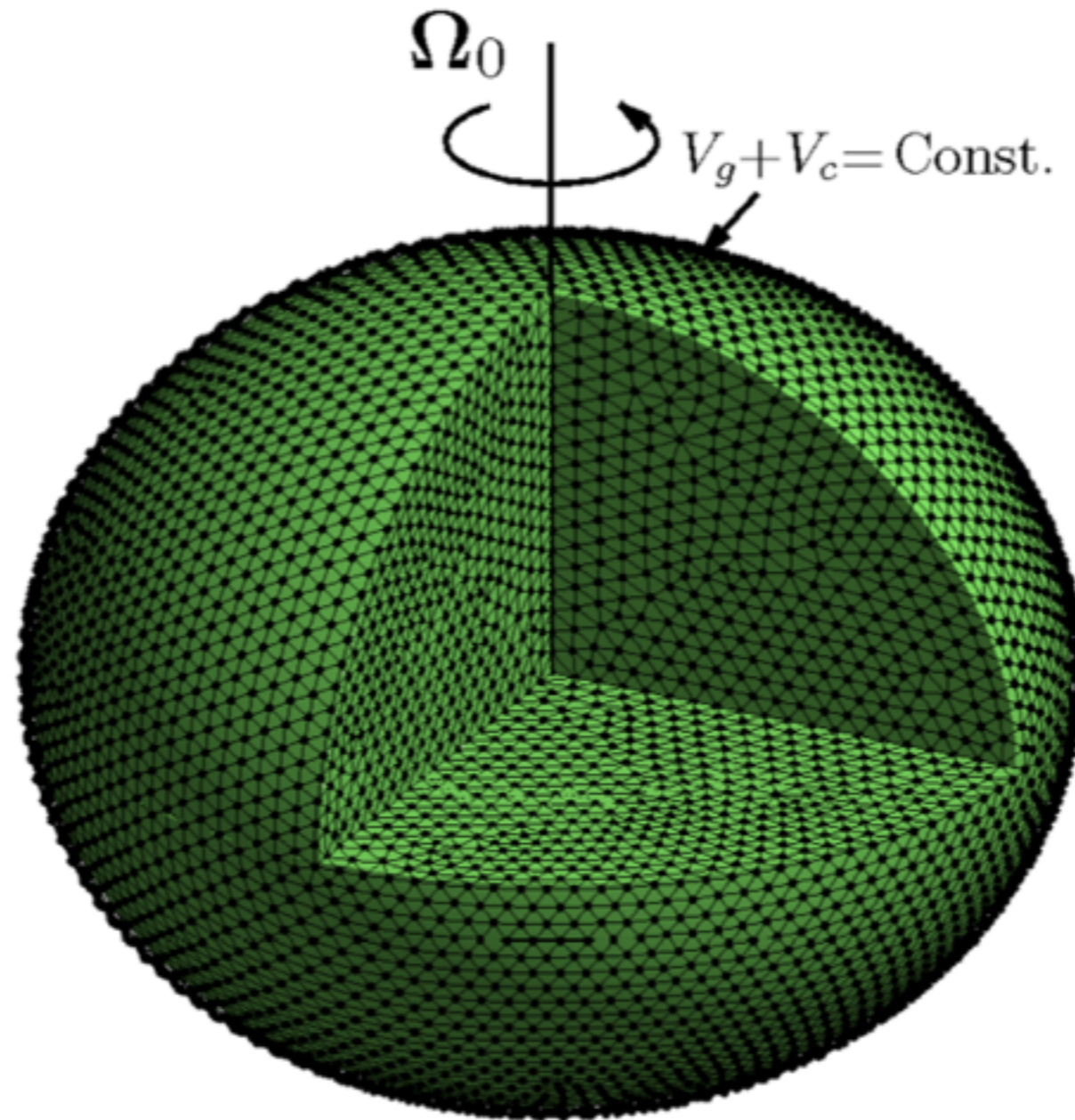
- seismology studies should be pursued!

## Future improvement:

Beyond the standard approach of the theory of figures (Zharkov & Trubitsyn 1978) based on an expansion around spherical geometry:

development of 3D numerical solutions for the shape of rotationally distorted planets

➡ higher accuracy for high order gravitational moments  $J$

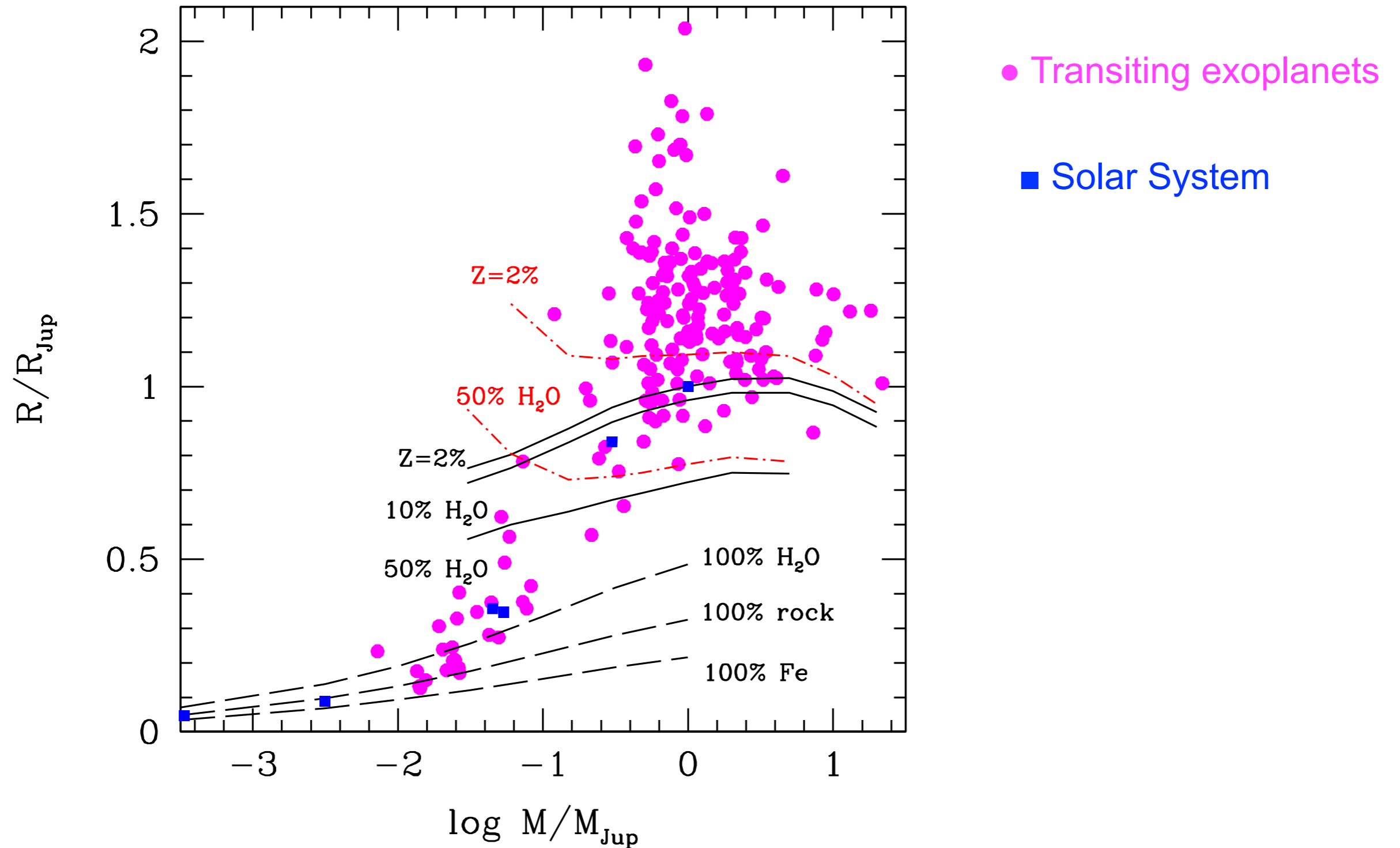


Sketch of a 3D tetrahedral mesh for oblate spheroidal Jupiter/Saturn *Kong et al. 2013*

I) Some lessons from our solar system planets

**II) Exoplanets: Interior structure and evolutionary models**

# Knowledge of Solar System necessary to understand the huge diversity of planetary structures from the mass-radius relationship of exoplanets



## ■ Distribution of heavy elements in exoplanets

- > Current assumptions (Fortney et al. ; Burrows et al. etc...):
- **All heavy elements located in the central core**
  - **Metal-free or solar metallicity H/He envelope**

*Equivalent to a distribution of Z over the entire planet?*

Planet with Z=50%

----> Comparison between planet with  
**Z in a core** versus planet with **no core**:  
up to ~ 30 % effect on R at a given age

*Baraffe, Chabrier, Barman 2008, 2010*

EOSs ANEOS (Sandia) /SESAME (Los Alamos):

*Relevant regime  $P \sim 1 \text{ Mbar} - 100 \text{ Mbar}$ :*

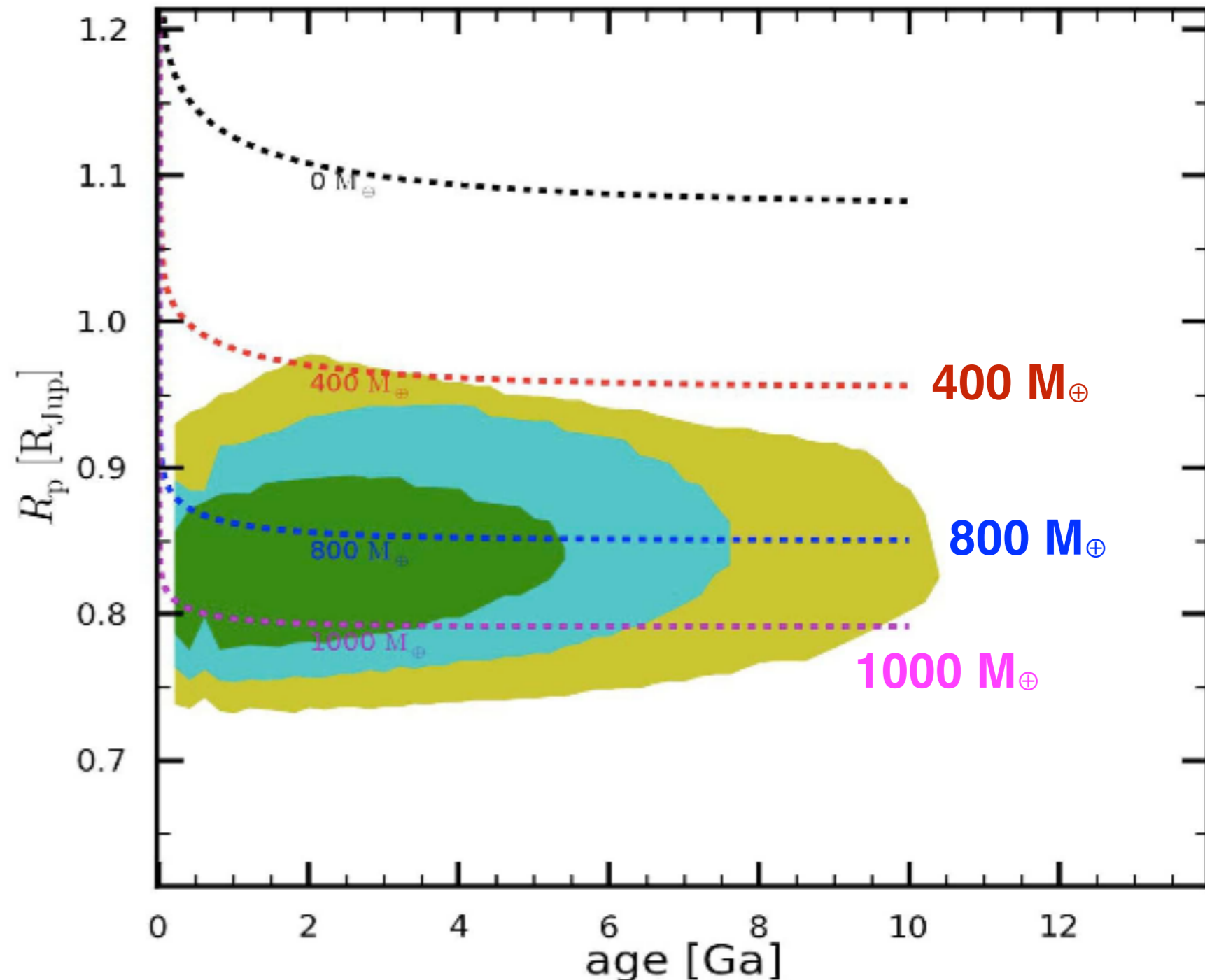
*interpolated between experiments and asymptotic limits in the very high density, fully ionised limit)*

**Reduction of those uncertainties are expected from improved EOSs**

A very interesting case: **CoRoT-20b** (Deleuil et al. 2012)

4  $M_{\text{Jup}}$  0.8  $R_{\text{Jup}}$

Requires **too massive core** of heavy material to explain its radius (maximum amount of heavy material in the disk  $\sim 800 M_{\oplus}$ )



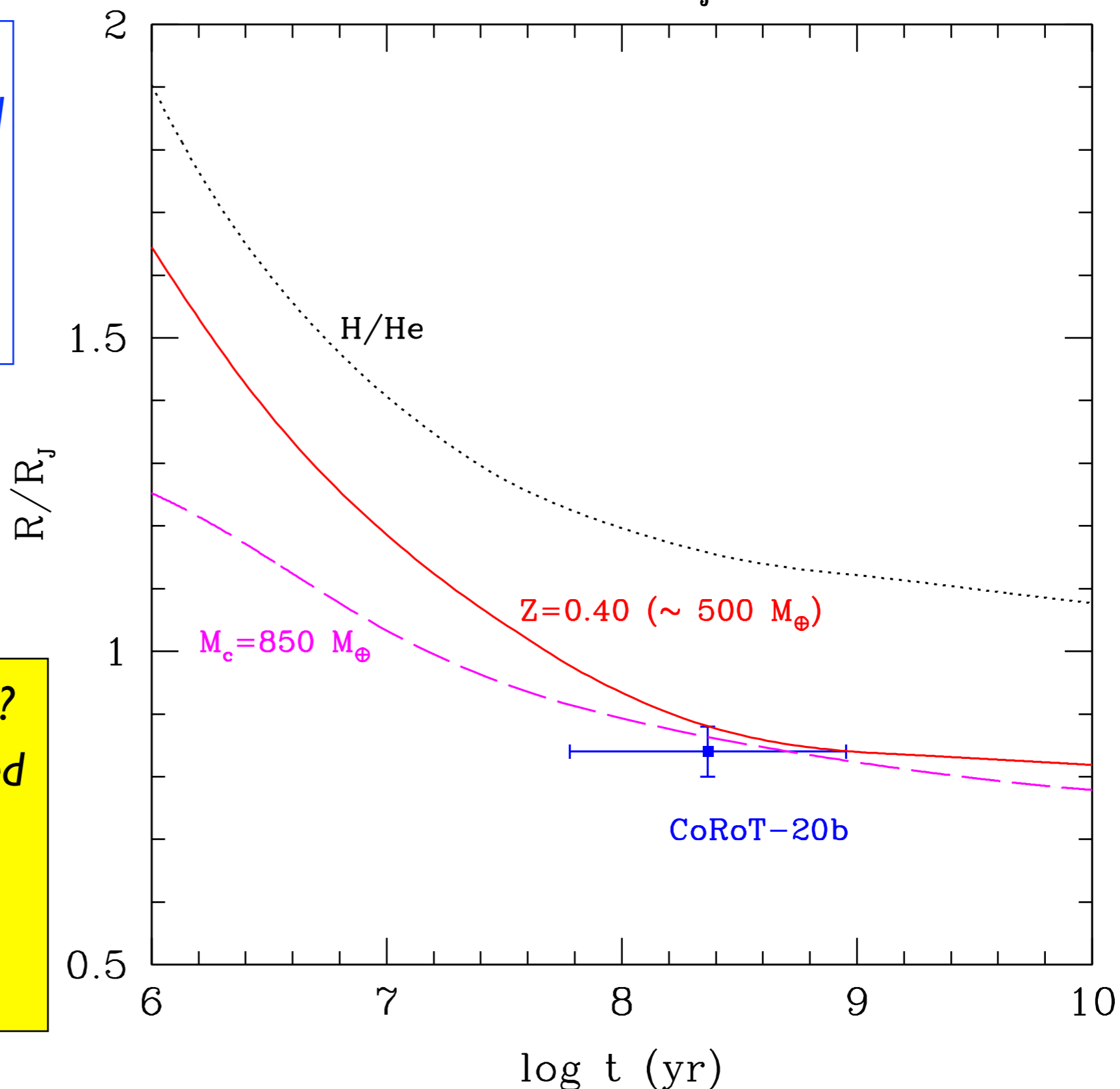
Uncertainty ellipse within  
**1sigma**, **2sigma**, **3sigma**

# Effect of heavy element distribution?

4  $M_J$  CoRoT-20b

Requires a **smaller amount** of heavy material if distributed in the whole planet ( $\sim 500 M_{\text{earth}}$ ) (models of Baraffe et al. 2008)

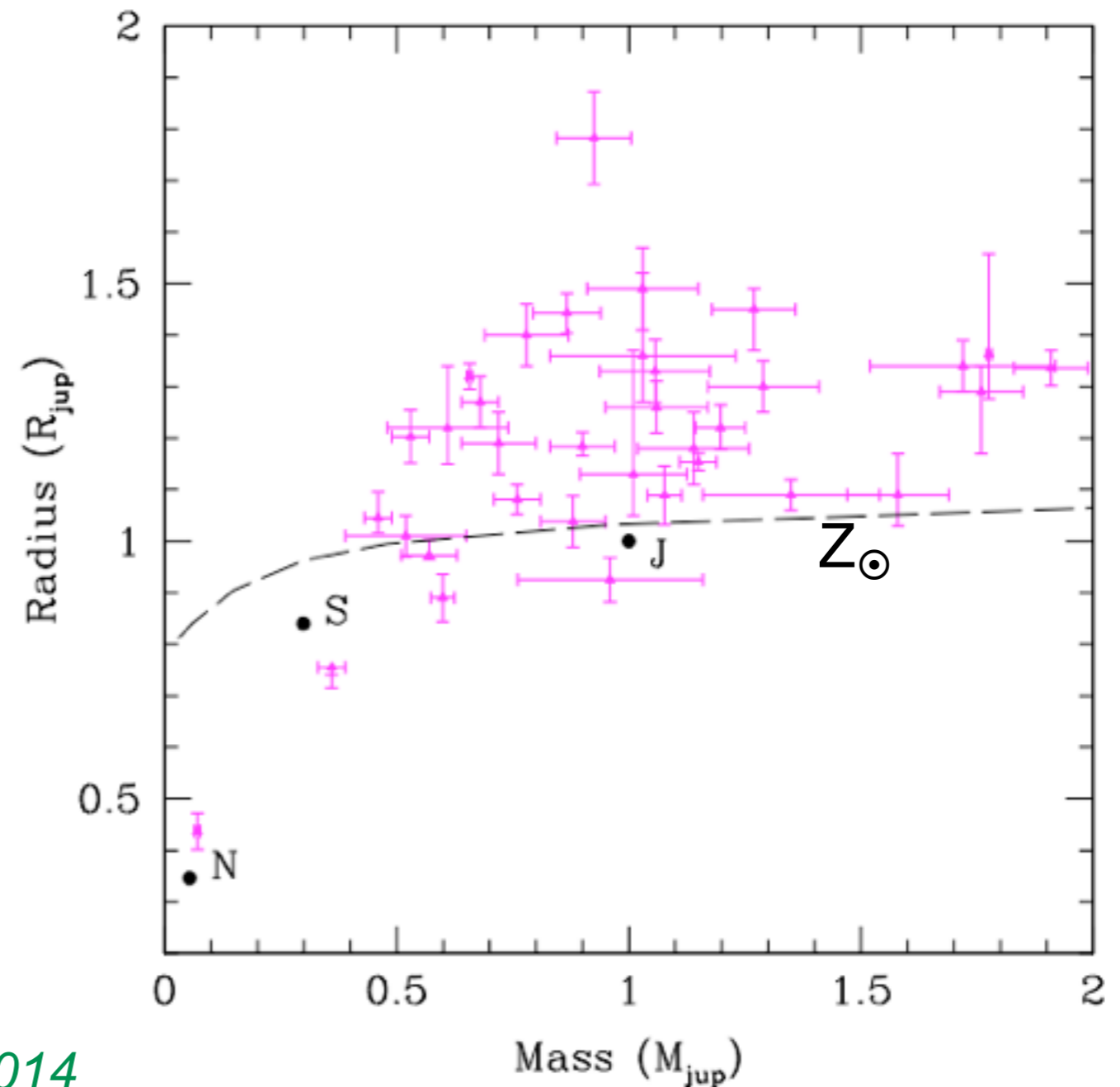
Wrong estimate of radius?  
Heavy material distributed all over the planet?  
Pb with EOS used (could ab-initio EOS improve that?)



# The problem of inflated planets

Significant fraction of exoplanets with abnormally large radius

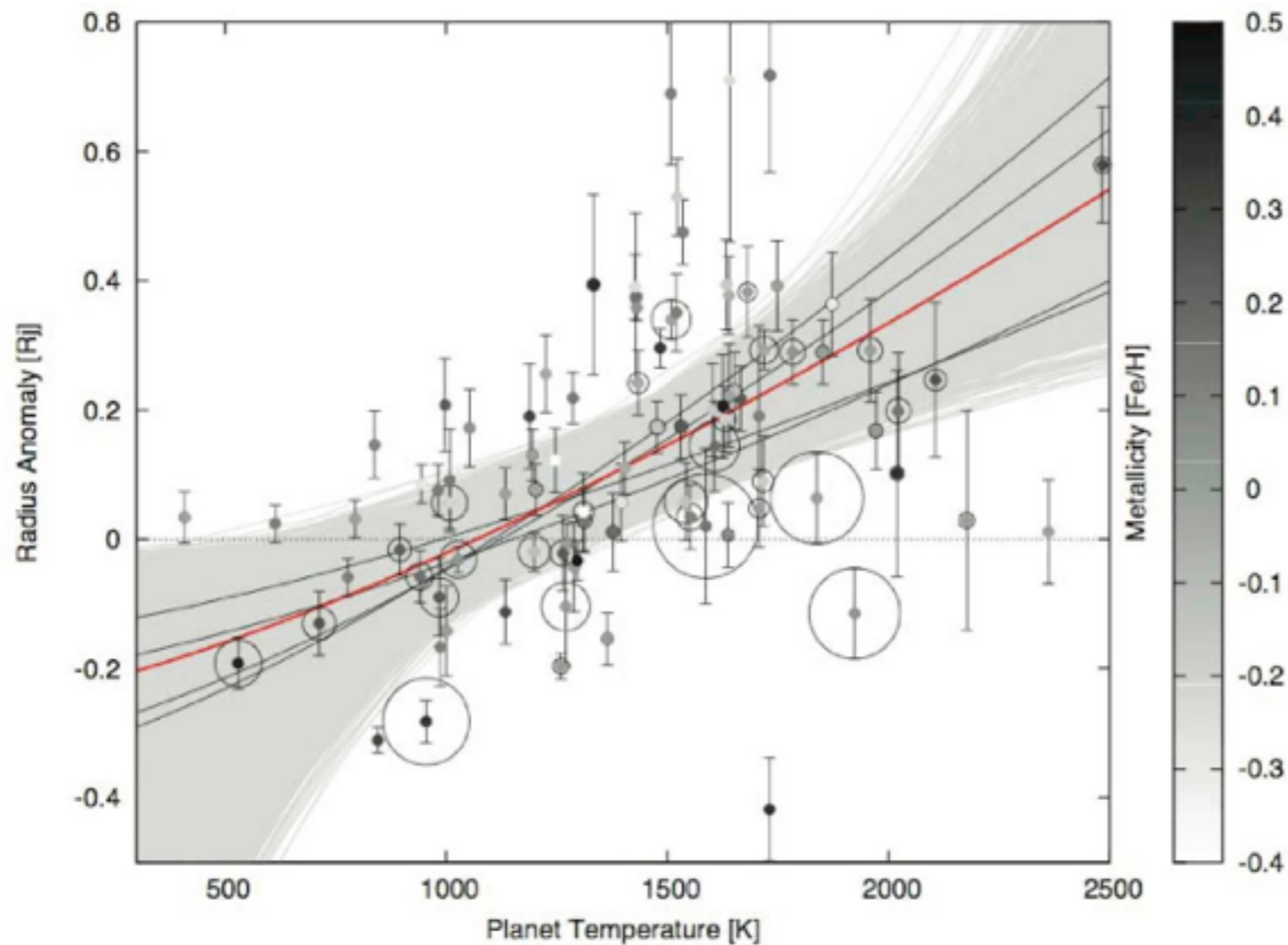
Missing physics in planetary interior models?



Summary in Baraffe et al. PPVI 2014

**Correlation of the radius anomaly  $R = (R_{\text{obs}} - R_{\text{pred}}) \propto T_p^{1.4}$**

*Laughlin, Crismani, Adams 2011*



Similarly, Kepler data: reveal a lack of inflated radii for giant planets receiving modest stellar irradiation

*(Miller and Fortney, 2011; Demory and Seager, 2011)*

## a) Incident stellar flux driven mechanism

😎😎 **Atmospheric circulation:** (*Showman & Guillot 2002*)

-----> **downward** transport of **kinetic energy** down to the internal adiabat  
*Heats the planet and slows down the contraction*

😎 **Ohmic dissipation:** (*Batygin & Stevenson 2010; Perna et al. 2010*)

-----> **Atmospheric winds** produce **currents** penetrating in the interior  
*Ohmic heating in the interior  $\dot{E} = J^2/(\rho\sigma)$*

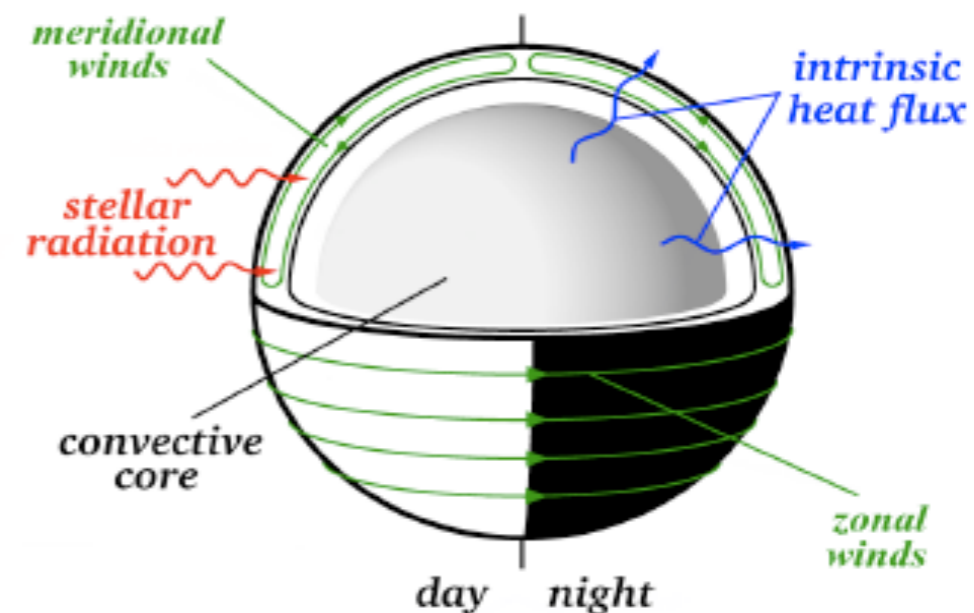


Atmospheric circulation models (GCM: 3D hydrodynamics + radiative transfer + magnetic drag on a full sphere) (*Cho et al., Forget et al.; Heng et al., Mayne et al.; Menou et al.; Showman et al.*)

👉 **Study the interaction between outer and deep circulation pattern**

👉 **Effect of circulation on planet spectral signatures**

*(link with observations: HST, Spitzer, JWST, ELT)*



## b) Tidal mechanisms (*Bodenheimer et al. 2001*)

😞 *Difficult to explain with tidal effects alone properties of several inflated planets (HD209458b, WASP-12b, etc..) (Leconte et al. 2010)*

## c) Delayed contraction

😞 **Enhanced atmospheric opacities:** (*Burrows et al. 2007*)

😞 **Double diffusive convection (semiconvection):** (*Chabrier & Baraffe 2007*)

## The future:

- **Development of ab-initio EOS** of H/He and heavy materials (water, silicates, etc) at high pressure and high temperature
  - ☞ new generation of planetary models are coming
- Development of **numerical simulations** to confirm the existence of **layered convection** in planetary interiors (*Rosenblum et al. 2011; Mirouh et al. 2012*)
  - ☞ Planets are not necessarily fully adiabatic and homogeneous
  - ☞ Important impact on our own giant planets!
    - *Potential observable signature for young planets or discovery of an inflated giant exoplanet at  $a \gg 0.1$  AU)*
- Development of **sophisticated dynamical atmospheric models** (outer/deep circulation + radiative transfer + chemistry + magnetic drag)
  - ☞ Solution for abnormally large radii of close-in planets?
  - ☞ Effect on spectral signatures
    - *Need for more observational constraints: wind velocity (cf Snellen et al.), shift of substellar point, heat redistribution.*

**The big question: Are theoretical/numerical tools ready to interpret the observed diversity?**

*They are on the right track!*

*Because we know what to do....*