Signatures in Directional Dark Matter Searches
Asymmetries and the Diurnal Variation

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The Direct Detection of Dark Matter

• Is crucial to both particle physics and cosmology

• The standard experiments attempt to measure the energy of the recoiling nucleus

• These experiments are hard to analyze since the sought signature cannot be distinguished from the background

• The backgrounds are formidable for the expected low counting rates

• So ingenious experimental approaches are needed
Differential (time averaged) event rates cannot be distinguished from background, e.g. for WIMP mass of 30 GeV, as functions of the recoil energy in keV, and $\sigma_{p,\chi} = 10^{-7}$ pb we get:

Heavy Nucleus, e.g. $^{127}$I

Light Nucleus, e.g. $^{19}$F
Novel approaches: Exploitation of other signatures of the reaction

- **The modulation effect:** The seasonal, due to the motion of the Earth, dependence of the rate.
- **Detection of other particles (electrons, X-rays), produced during the LSP-nucleus collision**
- **The excitation of the nucleus** (in some cases: heavy WIMP, low excitation energy etc.) and detection of the subsequently emitted de-excitation γ rays.
- **Asymmetry measurements in directional experiments** (the direction of the recoiling nucleus must also be measured) → DIURNAL VARIATION.
Fortunately the rate depends on the relative velocity:

\[ V_{\text{June}} = 235 + 15 = 250 \text{ km/s}; \quad V_{\text{Dec}} = 235 - 15 = 220 \text{ km/s}; \]

\[ \rightarrow \text{ Modulation Effect (time dependence)} \]
II: THE MODULATION EFFECT
(standard recoil experiments)

- The total Rate is parametrized as:
  \[ R = R_0 (1 + h \cos \alpha) \]
  (\(\alpha\) is the phase of the Earth; \(\alpha = 0\) around June 3rd)

- \(h\) = modulation amplitude.

- \(R_0\) = time averaged rate.

- The relative difference between the minimum and the maximum is 2\(h\)

- The location of the maximum depends on the sign of \(h\)
Iia: The Modulation amplitude (As a function of WIMP mass in GeV). It is small. Note its sign for large reduced mass.

Light System (e.g. $A=32$, $A=19$)  Heavy system (e.g. $A=127$)
D. Santos, LTPC Conference, Paris Dec. 17, 2012

- Measure the energy and direction of the recoiling nucleus
- They require track reconstruction of recoiling nuclei down to a few keV (preferably 3D reconstruction)
- Candidates:
  - DM-TPC, NEWAGE, DRIFT: low pressure gaseous detectors CF$_4$, CS$_2$, C$_4$H$_{10}$+$^3$He $\leftrightarrow$ dE/dx $\leftrightarrow$ head-tail problem
  - $\mu$TPC detectors (MIMAC): Low threshold, good 3D reconstruction of 3 mm tracks with gas $^3$He +CF$_4$
  - Most recently DNA detectors (A. Drukier & K. Freese): Easy 3-D reconstruction. Can use heavy target, e.g. Au.
E: Directional Experiments*

Assuming that such experiments become feasible we will show that the observed events:

- Will exhibit **asymmetry** due to the motion of the Sun
- On top of this they will exhibit **characteristic large annual modulation** due to the annual motion of the Earth
- Both of these will exhibit **periodic diurnal variation** due to the rotation of the Earth.

* Also gaseous μTPC detectors (arXiv:1001.2983 (astro-ph.CO)
WIMP flux, “The solar wind” (signal towards the Cygnus constellation), Spergel (88), vergados (02), Morgan-Green-Spooner (04), Battat et al (IJMP A, 2009), Bozorgnia, Gelmini, Gondolo (2012).

Flux variation (MB distr.) Morgan-Green-Spooner (04).
WIMP mass dependence of the flux

\[ \Phi_0 = \left( \frac{\rho_0}{m_\chi} \right) u_0 \]
WIMP Flux: unconventional velocity distributions (maximum at $\Theta=\pi/2$ !)

Saggitarius stream  

Sukivies’s Caustic Rings

![Graphs showing unconventional velocity distributions](image-url)
The calculation will proceed in two steps:

A) Evaluation of the event rate in a direction \((\Theta, \Phi)\), taking the sun’s direction of motion as polar axis (polar angle \(\Theta\)); \(\Phi\) is measured on a plane perpendicular to the sun’s velocity from \(x\) (\(x\) is radially out of the galaxy). The direction of recoil is due to the Sun’s motion the rate depends only on \(\Theta\) -->

\[
\hat{e} = (e_x, e_y, e_z) = (\sin \Theta \cos \Phi, \sin \Theta \sin \Phi, \cos \Theta).
\]

- due to the Sun’s motion the rate depends only on \(\Theta\) -->

Asymmetry.

- due to the Earth’s annual motion it will show a modulation, dependent on \((\Theta, \Phi)\) with very characteristic signature.

B) For a given direction of observation fixed in the lab.

- Then Diurnal variation due to the rotation of the Earth
Comparison of the usual (\(R\)) and directional (\(dR/d\Omega\) or \((dR/d\Xi)\)) coherent rates (\(\Xi = \cos \Theta\)).

\[ R_{coh} = \frac{\rho_\chi}{m_\chi} \frac{m_t}{Am_p} \left( \frac{\mu_\tau}{\mu_p} \right)^2 v_0 A^2 \sigma_N^{coh} t_{coh} (1 + h_{coh, \cos \alpha}) , \]

\[ \frac{dR}{d\Omega} = \frac{\rho(0)}{m_{\chi^0}} \frac{m}{Am_p} \left( \frac{\mu_\tau}{\mu_{\tau(p)}} \right)^2 v_0 \frac{1}{2\pi} \left[ \sigma_{p,\chi^0}^S A^2 t_{coh, \text{dir}} \left(1 + h_{coh, \text{dir}, \cos \alpha} + h_{coh, \text{dir}, \sin \alpha}^s \right) \right] \] (40)

The factor \(\frac{1}{2\pi}\) enters, since, in order to better compare with the standard experiments, we used in the previous expression the total nucleon cross section. Note, however, that:

\[ \frac{dR}{d\Xi} = \frac{\rho(0)}{m_{\chi^0}} \frac{m}{Am_p} \left( \frac{\mu_\tau}{\mu_{\tau(p)}} \right)^2 v_0 \left[ \sigma_{p,\chi^0}^S A^2 t_{coh, \text{dir}} \left(1 + h_{coh, \text{dir}, \cos \alpha}^c + h_{coh, \text{dir}, \sin \alpha}^s \right) \right] \] (41)
The directional event rate
(The direction of recoil is observed)

• The event rate as a function of the direction angles $(\Theta, \Phi)$ is:
  \[\frac{dR}{d\Omega} = (\kappa/2\pi)R_0[1 + h_c \cos \alpha + h_s \sin \alpha]\], \(\kappa = t / t_{\text{dir}}\)

• $R_0$ is the average usual (non-dir) rate, $\alpha$ the phase of the Earth

• $\kappa/2\pi$ is the reduction factor (it depends on the direction of observation, but it is independent of the angle $\Phi$). This factor becomes $\kappa$, after integrating over $\Phi$. $dR/d\Omega \rightarrow dR/d(\cos \Theta)$

• It can also be written as:
  \[\frac{dR}{d\Omega} = (\kappa/2\pi)R_0[1 + h_m \cos(\alpha + \alpha_0)]\], \(\kappa = t / t_{\text{dir}}\)

• $h_m$ is the modulation amplitude (it strongly depends on the direction of observation)

• $\alpha_0$ is the shift in the phase of the Earth (it strongly depends on the direction of observation)

• $\kappa$, $h_c$, $h_s$, or $h_m$ and $\alpha_0$, depend only slightly on the particle model (e.g. SUSY) parameters and $\mu_r$
κ vs Θ for MB Distr. For a light system slight dependence on the WIMP mass

Light target (e.g. A=32)  Heavy target (e.g. A=127)

Windows on the Universe
Quy Nhon, Aug. 14, 2013
κ vs Θ for a light system.

Sagittarius Stream

Sikivie’s Caustic Rings

Windows on the Universe
Quy Nhon, Aug. 14, 2013
The modulation amplitudes (directional) for M-B distr., e.g. for $m_\chi=50$ GeV. solid, dashed, thick $\leftrightarrow \Theta=\pi/4$, $\pi/2$, $3\pi/4$.
The modulation pattern (relative to the time averaged). $\alpha$ is the phase of the Earth

$\Theta=\pi/4$ (a), $\Theta=\pi/2$ (b)

$\Theta=3\pi/4$ (c), $\Theta=\pi$ (d)
The Diurnal variation of the rate in Directional Experiments

- We have seen that:

- the parameters $\kappa$ and $h_m$ depend on the direction of observation relative to the sun’s velocity

- In a directional experiment the direction of observation is fixed with respect to the earth.

- Due to the rotation of the Earth during the day this direction points in different parts of the galactic sky. So the angles $(\Theta, \Phi)$ change and the rate becomes time dependent. It will show a periodic behavior.
Schematic time dependence of the rate as may be seen in a directional experiment. Battat et al (IJMP A, 2009)
From the celestial \((\alpha = \text{ascension}, \delta = \text{inclination})\) to galactic coordinates

A vector oriented by \((\alpha, \delta)\) in the laboratory is given in the galactic frame by a unit vector with components:

\[
\begin{pmatrix}
y \\ x \\ z
\end{pmatrix}
=
\begin{pmatrix}
-0.868 \cos \alpha \cos \delta - 0.198 \sin \alpha \cos \delta + 0.456 \sin \delta \\
0.055 \cos \alpha \cos \delta + 0.873 \sin \alpha \cos \delta + 0.4831 \sin \delta \\
0.494 \cos \alpha \cos \delta - 0.445 \sin \alpha \cos \delta + 0.747 \sin \delta
\end{pmatrix}
\]
Diurnal Variation of the rate ($\kappa$) for a light target & fully directional

WIMP MASS 10 GeV  WIMP MASS 50 GeV

Quy Nhon, Aug. 14, 2013
CONCLUSIONS: Non modulated rate in directional Experiments (for both modes, coherent and spin)

- A useful parameter is $\kappa$, the reduction factor relative to the non-directional rate.
- $\kappa$ strongly depends on the polar angle $\Theta$ (the angle between the direction of observation and the sun’s velocity).
- $\kappa \approx 1$ in the most favored direction ($\Theta \approx \pi$ in MB).
- As the Earth rotates, the detector samples a different angle $\Theta$.
- The event rate ($\kappa$) exhibits a periodic variation with a period of 24 hours.
- The form of the variation depends on the WIMP mass.
- The amplitude of this variation depends on the inclination of the line of observation. It can be quite large.
- The variation persists, even if the sense of direction is not known. Then, however, the effect is smaller.
CONCLUSIONS: The modulation in directional Experiments (preliminary)

- The modulation amplitude in the most favored direction ($\kappa \approx 1$) is $0.02 < h_m < 0.1$ (bigger than in non-directional case) depending on the WIMP mass.

- In plane perpendicular to the sun’s velocity ($\kappa \approx 0.3$) $h_m$ is much bigger:
  - $|h_m| \approx 0.25$ (50% difference between maximum and minimum).

- Both its magnitude and its sign depend on the azimuthal angle $\Phi$.

- We are currently computing its time variation. Preliminary results show a spectacular signal, which cannot be mimicked by other seasonal effects.
An alternative way to settle controversies!

Once all mighty God gave 5 golden cows, made of pure gold, to be divided among the Dark Matter Searches as follows:

- 1/3 goes to Direct the Experiments (CoGeNT/COUP, PICASSO, DAMA, EDELWEISS, CDMS, CRESST, ZEPLIN-3, XENON, KIMS etc).
- 1/3 goes to the Indirect Measurements (neutrinos, gamma-rays, astrophysics etc)
- 1/6 goes to future experiments (directional, e-detection, γ or X-ray detection etc)

Condition: No cow should be carved.

Obviously the three groups did not know how to do this.
So they went, where else?, to Mulah Nasrudin.
He thought for a while and ordered his wife to bring into the pack their own cow, which he valued more than golden.
Now there are 6 cows in the pack. It was easy for the first two groups to get 2 each and the future experiments to get 1.
His cow was left and his wife took it back to the stable.
Was this a fair deal?
Was it a fair deal? After the fact theory pops in!

- Mullah Nasrudin did not know how to sum up infinite series. However theorists do:

\[
\frac{5}{3} + \frac{1}{3} \left( \frac{1}{6} + \frac{1}{6^2} + \frac{1}{6^3} \cdots \right) = \frac{5}{3} + \frac{1}{3} = 2
\]

\[
\frac{5}{6} + \frac{1}{5} \left( \frac{1}{6} + \frac{1}{6^2} + \frac{1}{6^3} \cdots \right) = \frac{5}{6} + \frac{1}{6} = 1
\]
COMMON WISDOM!

Are Physicists optimists or Don Quixotes?

Once the wise Mullah Nasrudin was seen beating a lake with a huge spoon. Evidently in the hope of transforming the lake into gold. When his fellow villagers teased him:

-Mullah! You surely are wasting your time!

He sternly replied:

-Imagine, though, that it works!
(Such a reward!)
THE END