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CP violation in B decays at LHCb

Windows on the Universe (Inaugural Conference of ICISE)

11–17 August 2013 – Quy Nhon, Vietnam

Florian Kruse – on behalf of the LHCb collaboration

CP violation

▶ Violation of CP symmetry:

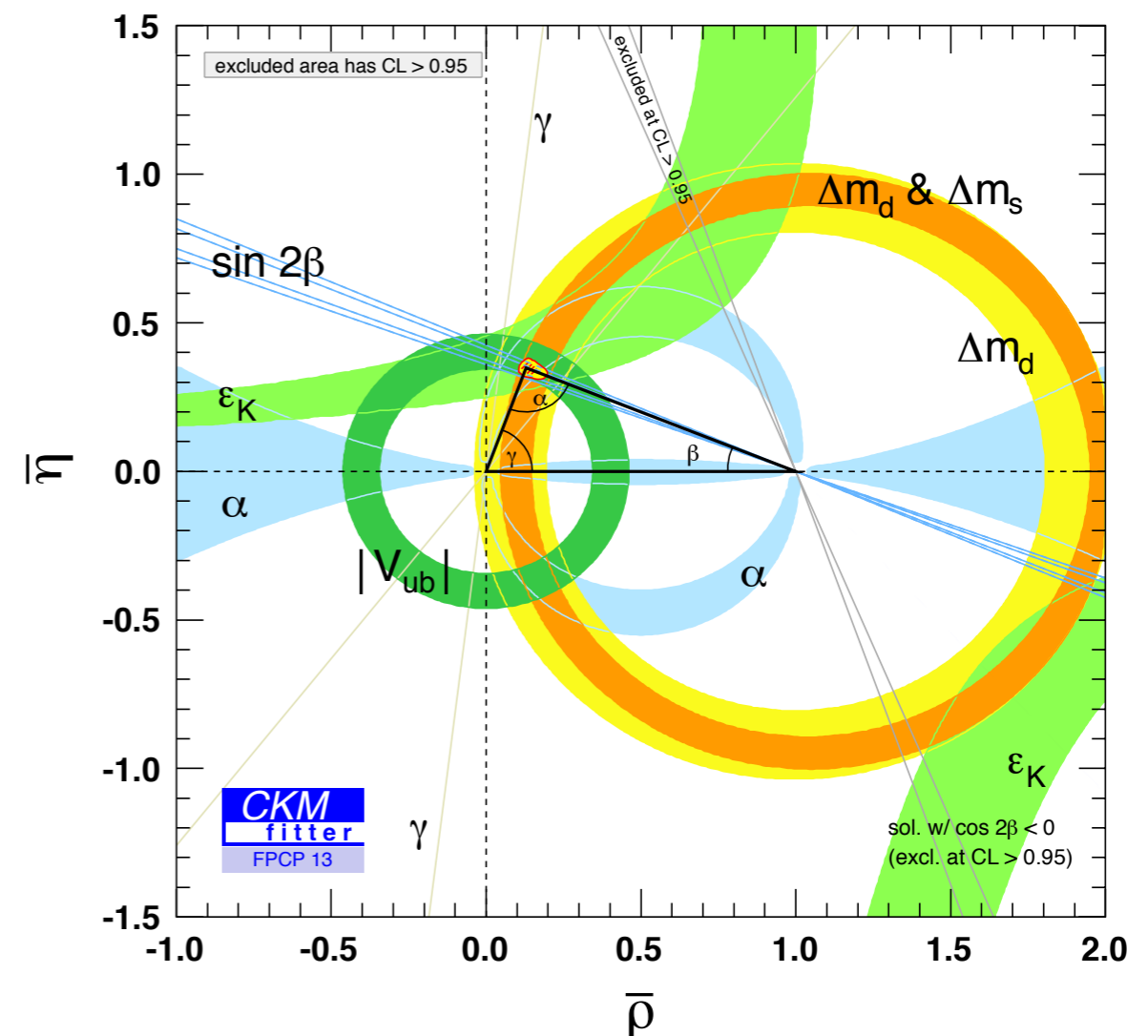
- particles and antiparticles behave differently
- well established in Standard Model (CKM matrix → unitarity triangles)

▶ Why CP violation?

- tiny matter-antimatter asymmetry resulted in matter-dominated universe
- CPV required to explain asymmetry
- CPV in SM not enough

▶ Why measure CP violation?

- test SM by over-constraining CKM parameters
- find contributions of Physics Beyond the Standard Model (BSM)

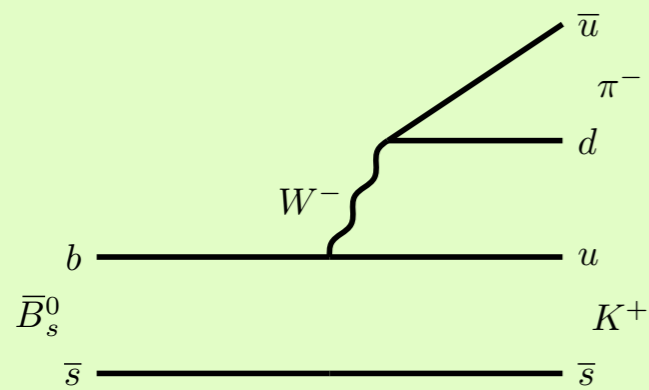


$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

Sources of CP violation

DIRECT CPV

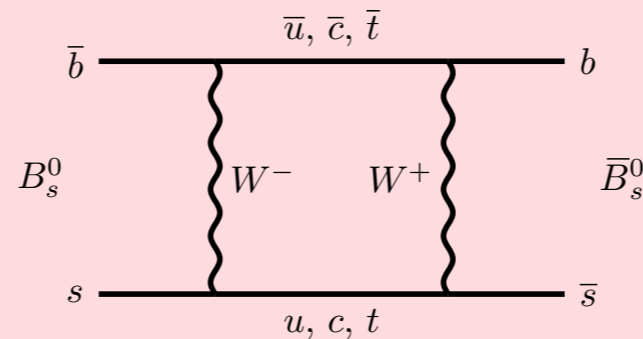


different decay rates for

$$\Gamma(B \rightarrow X) \neq \Gamma(\bar{B} \rightarrow \bar{X})$$

- ▶ $B_{(s)} \rightarrow K\pi$
- ▶ γ in $B^\pm \rightarrow Dh^\pm$

MIXING CPV

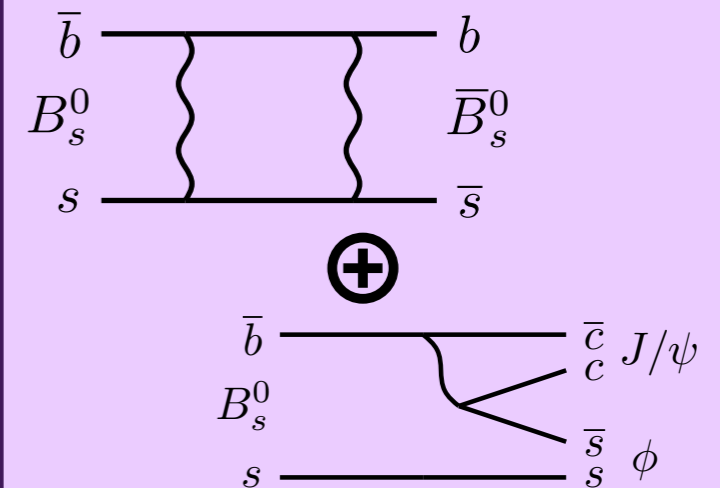


difference in mixing

$$\Gamma(B(t) \rightarrow \bar{X}) \neq \Gamma(\bar{B}(t) \rightarrow X)$$

- ▶ flavour-specific asymmetry a_{sl}

INTERFERENCE CPV

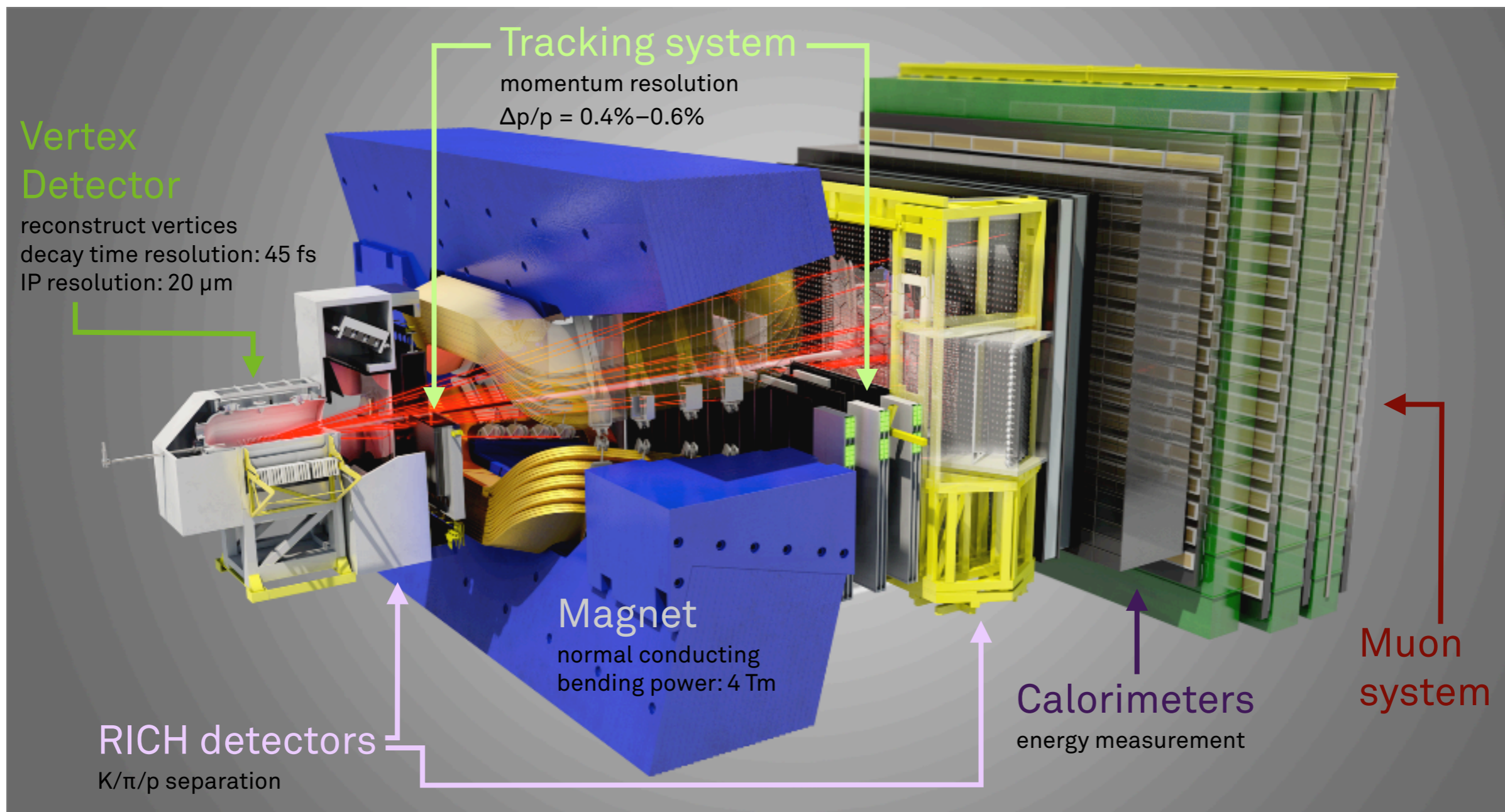


interference in mixing and decay

$$\Gamma(B(t) \rightarrow X_{CP}) \neq \Gamma(\bar{B}(t) \rightarrow X_{CP})$$

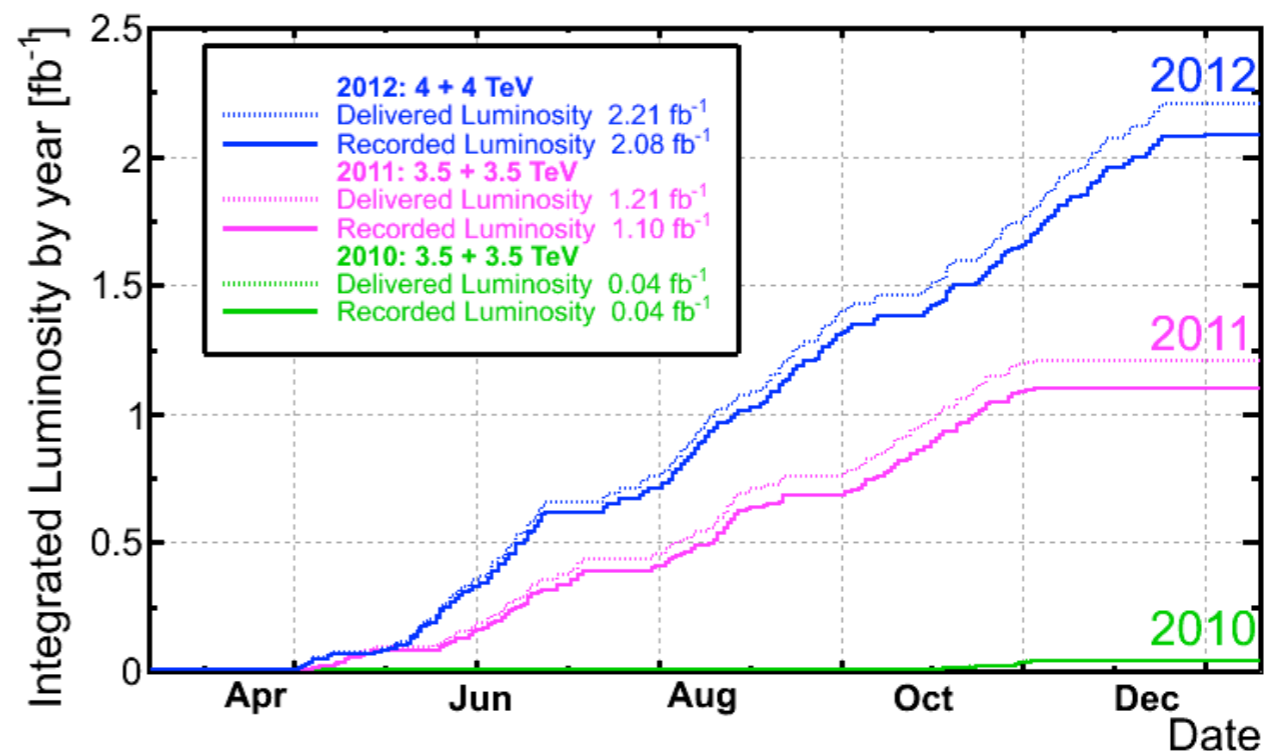
- ▶ $B_d \rightarrow J/\psi K_S$
- ▶ $B_s \rightarrow J/\psi K K / J/\psi \pi \pi$

The LHCb detector



LHCb performance

- ▶ Total luminosity:
 - $L_{\text{int}} \approx 3 \text{ fb}^{-1}$
- ▶ Data taking efficiency: 93%
- ▶ Trigger:
 - reducing 20 MHz collision rate to 5 kHz output rate





Direct CPV

$B_{(s)} \rightarrow K\pi$

γ in $B^{\pm} \rightarrow Dh^{\pm}$

Direct CP violation in $B_{(s)} \rightarrow K\pi$, 1 fb^{-1}

► measure CP asymmetries:

$$A_{CP}(B^0 \rightarrow K^+\pi^-) = \frac{\Gamma(\bar{B}^0 \rightarrow K^-\pi^+) - \Gamma(B^0 \rightarrow K^+\pi^-)}{\Gamma(\bar{B}^0 \rightarrow K^-\pi^+) + \Gamma(B^0 \rightarrow K^+\pi^-)}$$

$$A_{CP}(B_s^0 \rightarrow K^-\pi^+) = \frac{\Gamma(\bar{B}_s^0 \rightarrow K^+\pi^-) - \Gamma(B_s^0 \rightarrow K^-\pi^+)}{\Gamma(\bar{B}_s^0 \rightarrow K^+\pi^-) + \Gamma(B_s^0 \rightarrow K^-\pi^+)}$$

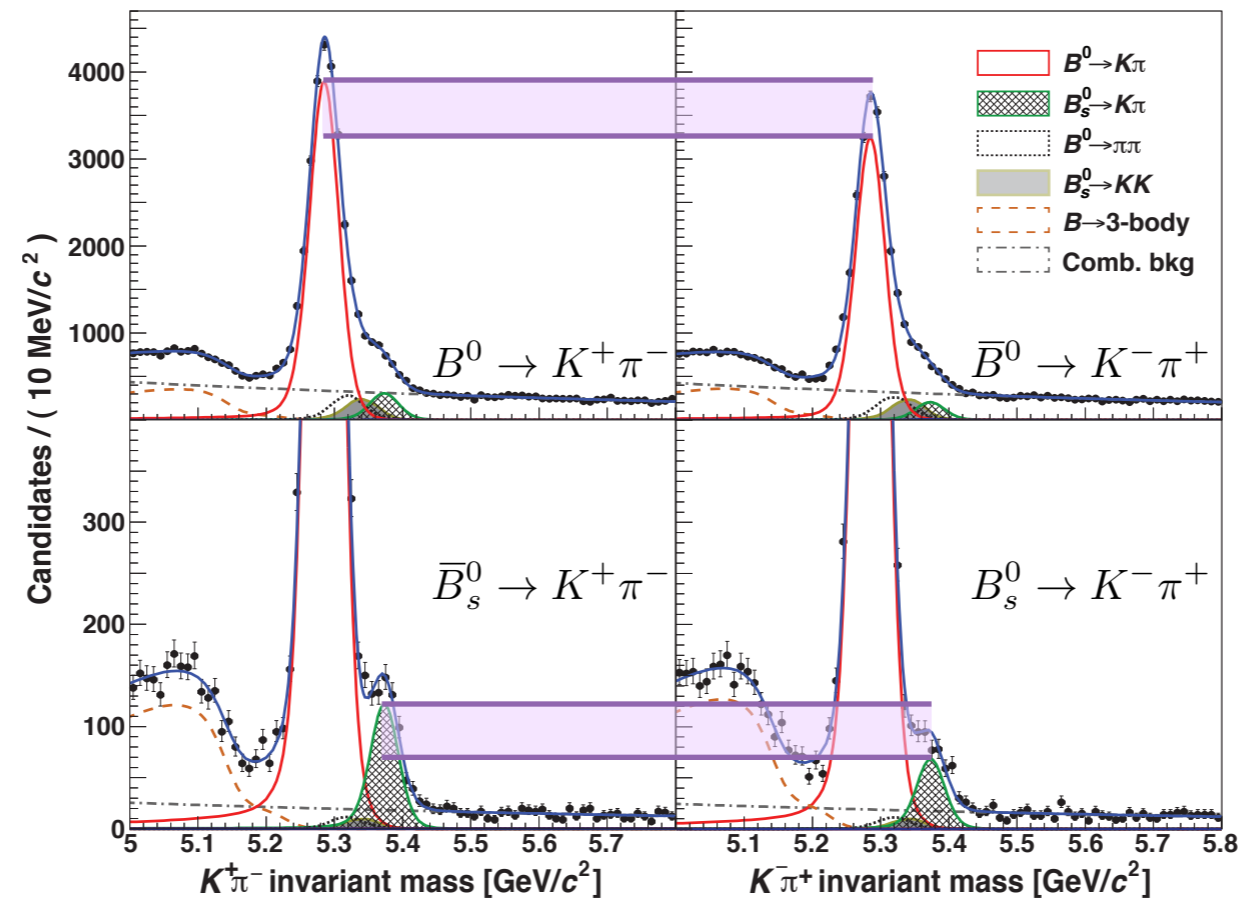
► CPV through interference between tree and penguin contributions

Phys. Rev. Lett.
110 (2013) 221601

► measurement:

- measure raw asymmetries from mass distribution fit
- correct raw asymmetries for instrumental and production asymmetries

Direct CP violation in $B_{(s)} \rightarrow K\pi$, 1 fb^{-1}



Phys. Rev. Lett.
110 (2013) 221601

most precise!

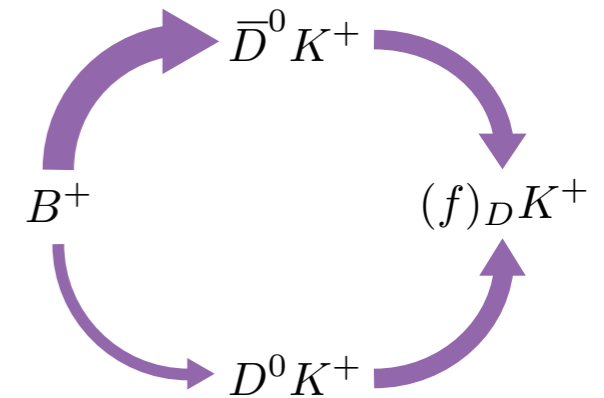
$$A_{CP}(B^0 \rightarrow K^+ \pi^-) = -0.080 \pm 0.007 \text{ (stat)} \pm 0.003 \text{ (syst)}$$

$$A_{CP}(B_s^0 \rightarrow K^- \pi^+) = 0.27 \pm 0.04 \text{ (stat)} \pm 0.01 \text{ (syst)}$$

first CPV in B_s
(6.5σ)

γ in $B^\pm \rightarrow Dh^\pm$

- ▶ determination of γ from tree level diagrams in $B^\pm \rightarrow Dh^\pm$
- ▶ combine various single measurements (not covered):
 - LHCb γ : GLW ($D \rightarrow KK/\pi\pi$), ADS ($D \rightarrow K\pi/K\pi\pi\pi$), GGSZ ($D \rightarrow K_S\pi\pi/K_S KK$)
 - additional LHCb/CLEO/HFAG inputs on D parameters (mixing, hadronic parameters, CP violation)
 - total of max. 38 observables (γ , phases, ratios, ...)
- ▶ use frequentist plugin approach:
 - combine all measurements into single likelihood
 - for nearly all observables: treat stat. + syst. fluctuations as Gaussian
 - correct for undercoverage



γ in $B^\pm \rightarrow Dh^\pm$

▶ using $B^\pm \rightarrow DK^\pm$ only, with 2012 data:

- GLW/ADS with 1 fb^{-1} + GGSZ with 3 fb^{-1}
- no D mixing

LHCb-CONF-2013-006

most
precise!

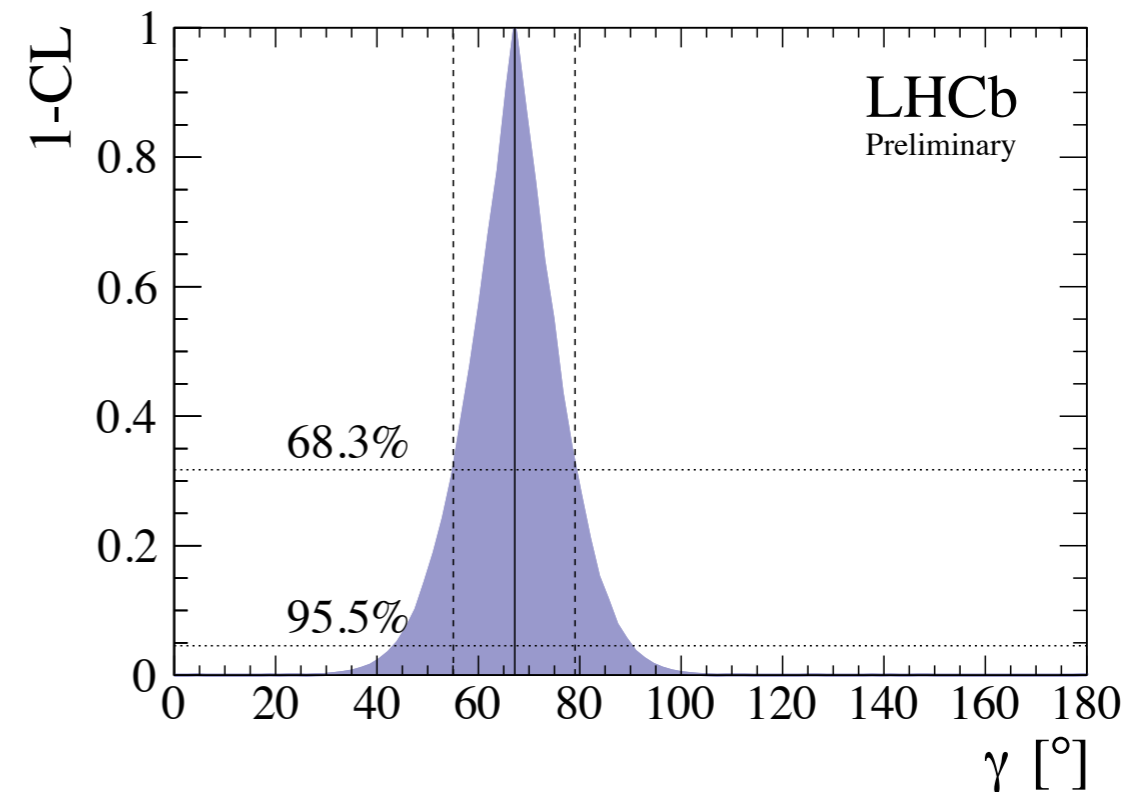
$$\gamma = (67 \pm 12)^\circ$$

▶ combining $B^\pm \rightarrow DK^\pm$ and $B^\pm \rightarrow D\pi^\pm$:

- GLW/ADS/GGSZ with 1 fb^{-1}
- incl. D mixing

$$\gamma = (72.6^{+9.7}_{-17.2})^\circ$$

arXiv:1305.2050





Mixing CPV

Flavour-specific asymmetry a_{sl} in B_s

Flavour-specific asymmetry a_{sl} in B_s

► flavour-specific asymmetry:

$$a_{sl}^s = \frac{\Gamma(\bar{B}_s^0(t) \rightarrow f) - \Gamma(B_s^0(t) \rightarrow \bar{f})}{\Gamma(\bar{B}_s^0(t) \rightarrow f) + \Gamma(B_s^0(t) \rightarrow \bar{f})} \quad \text{with } f : D_s^- X \mu^+ \nu_\mu$$



NEW!

- $B_s(t)$: time evolution of particle produced as B_s at $t=0$
- f : flavour-specific final state only B_s can decay into
- decays only possible via B mixing

arXiv:1308.1048

► measured quantity (time-integrated):

$$A_{\text{meas}} = \frac{\Gamma(D_s^- \mu^+) - \Gamma(D_s^+ \mu^-)}{\Gamma(D_s^- \mu^+) + \Gamma(D_s^+ \mu^-)} = \frac{a_{sl}^s}{2}$$

- corrected for reconstruction and background asymmetries

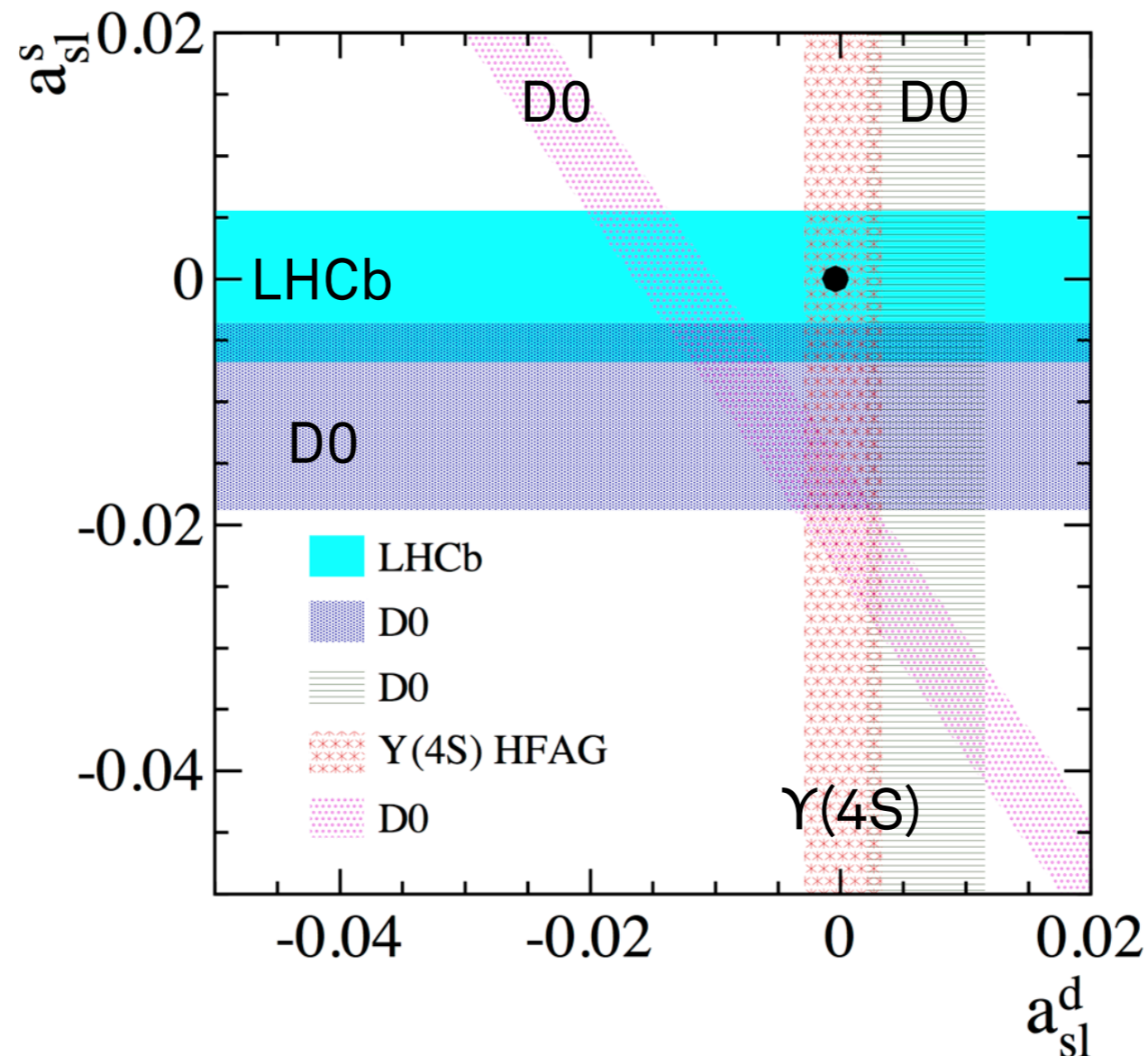
► measurement on 1 fb^{-1}

Flavour-specific asymmetry a_{sl} in B_s

$$a_{sl}^s = (-0.06 \pm 0.50 (\text{stat}) \pm 0.36 (\text{syst}))\%$$

most precise!

NEW!



arXiv:1308.1048



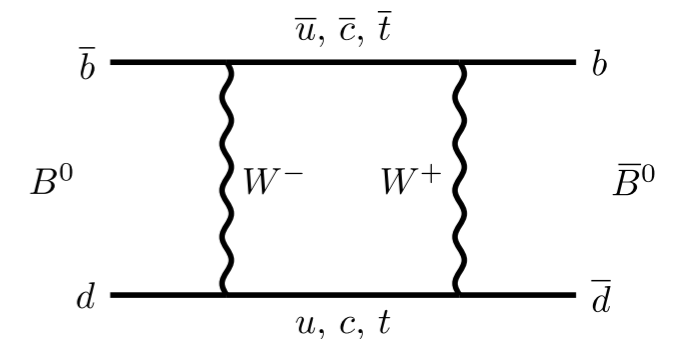
Interference CPV

$B_d \rightarrow J/\psi K_S$

$B_s \rightarrow J/\psi K K / J/\psi \pi \pi$

CP violation in interference between mixing and decay

- ▶ neutral B mesons mix through box diagrams
- ▶ light and heavy mass eigenstate: B_L, B_H
 - mass difference $\Delta m_{s,d} \Rightarrow$ oscillation frequency
 - decay width difference $\Delta \Gamma_{s,d}$
- ▶ interference CPV:
 - both flavour eigenstates (B/\bar{B}) can decay into common final state f
 - measure time-dependent asymmetry



$$A_{CP}(t) = \frac{\Gamma(\bar{B}(t) \rightarrow f) - \Gamma(B(t) \rightarrow f)}{\Gamma(\bar{B}(t) \rightarrow f) + \Gamma(B(t) \rightarrow f)}$$

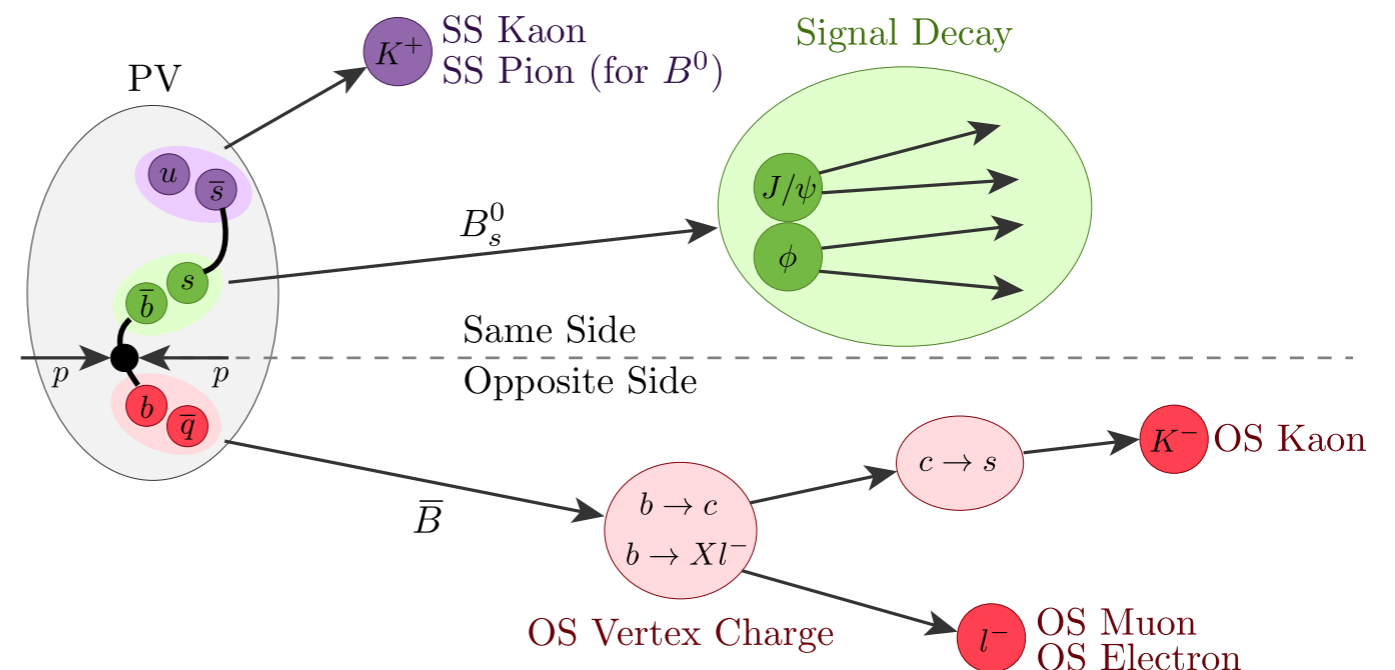
- $B(t)$: time evolution of particle produced as B at $t=0$

CP violation in interference between mixing and decay

► ingredients to measure interference CPV:

- B production flavour \Rightarrow Flavour Tagging
- B decay time
- wrong-tag rate
- decay time resolution

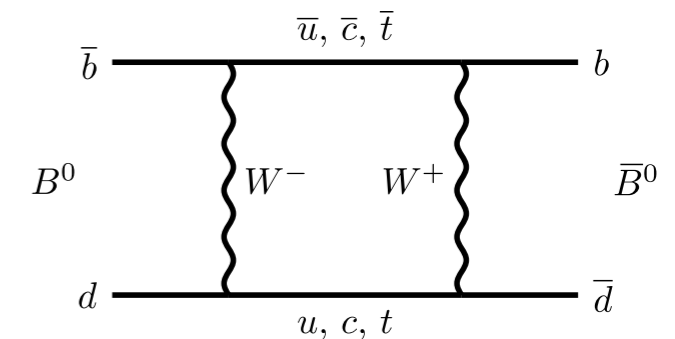
$$A_{CP}(t) = \frac{\Gamma(\bar{B}(t) \rightarrow f) - \Gamma(B(t) \rightarrow f)}{\Gamma(\bar{B}(t) \rightarrow f) + \Gamma(B(t) \rightarrow f)}$$



CP asymmetry in $B_d \rightarrow J/\psi K_S$

- ▶ measurement of time-dependent asymmetry:

$$\begin{aligned}
 A_{J/\psi K_S^0}(t) &= \frac{\Gamma(\bar{B}^0(t) \rightarrow J/\psi K_S^0) - \Gamma(B^0(t) \rightarrow J/\psi K_S^0)}{\Gamma(\bar{B}^0(t) \rightarrow J/\psi K_S^0) + \Gamma(B^0(t) \rightarrow J/\psi K_S^0)} \\
 &= S_{J/\psi K_S^0} \sin(\Delta m_d t) - C_{J/\psi K_S^0} \cos(\Delta m_d t)
 \end{aligned}$$



- ▶ in SM: direct and mixing CPV negligible:

$$C_{J/\psi K_S^0} \approx 0 \Rightarrow S_{J/\psi K_S^0} = \sin 2\beta$$

- ▶ “golden mode” for $\sin 2\beta$, world averages:

$$S_{J/\psi K_S^0} = 0.665 \pm 0.024 \quad C_{J/\psi K_S^0} = 0.024 \pm 0.026$$

CP asymmetry in $B_d \rightarrow J/\psi K_S$

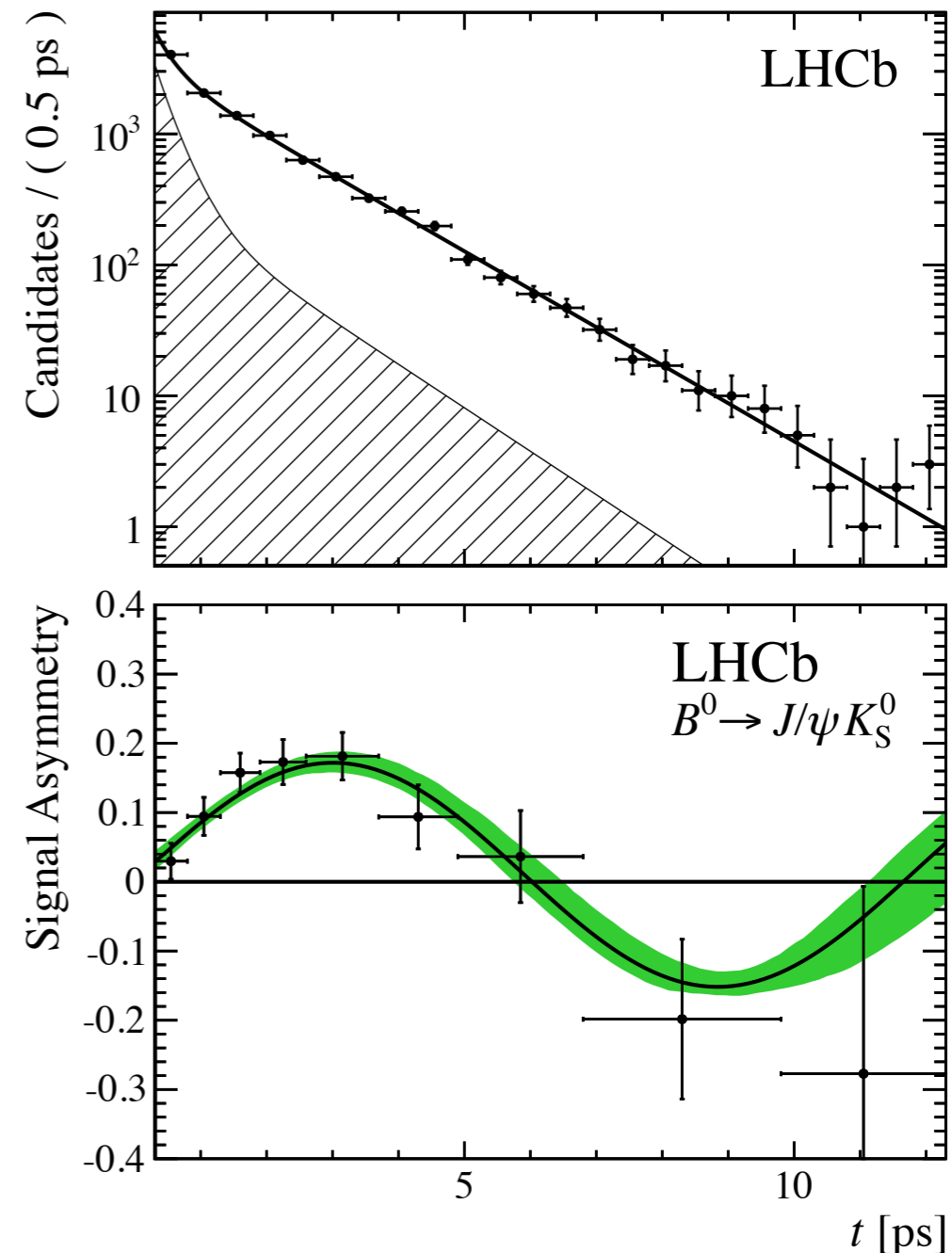
- ▶ result on 1 fb^{-1} data:

$$S_{J/\psi K_S^0} = 0.73 \pm 0.07 \text{ (stat)} \pm 0.04 \text{ (syst)}$$

$$C_{J/\psi K_S^0} = 0.03 \pm 0.09 \text{ (stat)} \pm 0.01 \text{ (syst)}$$

- ▶ first significant CPV measurement in $B_d \rightarrow J/\psi K_S$ at hadron collider
- ▶ only OS tagging used

Phys. Lett. B 721 (2013) 24-31



CP violation in $B_s \rightarrow J/\psi K^+ K^- / J/\psi \pi^+ \pi^-$

- ▶ CP violating phase ϕ_s , standard model prediction:

$$\phi_s^{\text{SM}} = -0.036 \pm 0.002 \text{ rad}$$

- ▶ possible new physics (NP) in box diagrams:

$$\phi_s = \phi_s^{\text{SM}} + \phi_s^{\text{NP}}$$

- ▶ challenges:

- $\Delta m_s = 17.8 \text{ ps}^{-1}$ ($\Delta m_d = 0.510 \text{ ps}^{-1}$)
- LHCb decay time resolution: 45 fs
- precise resolution description essential
- $K^+ K^-$ via P-wave ($\phi(1020)$) or non-resonant S-wave
- disentanglement via angular analysis



CP violation in $B_s \rightarrow J/\psi K^+ K^- / J/\psi \pi^+ \pi^-$

- ▶ using only $B_s \rightarrow J/\psi K^+ K^-$, 1 fb^{-1} :

$$\phi_s = 0.07 \pm 0.09 \text{ (stat)} \pm 0.01 \text{ (syst) rad}$$

$$\Gamma_s = 0.663 \pm 0.005 \text{ (stat)} \pm 0.006 \text{ (syst) ps}^{-1}$$

$$\Delta\Gamma_s = 0.100 \pm 0.016 \text{ (stat)} \pm 0.003 \text{ (syst) ps}^{-1}$$

- ▶ $B_s \rightarrow J/\psi K^+ K^- + B_s \rightarrow J/\psi \pi^+ \pi^-$, 1 fb^{-1} :

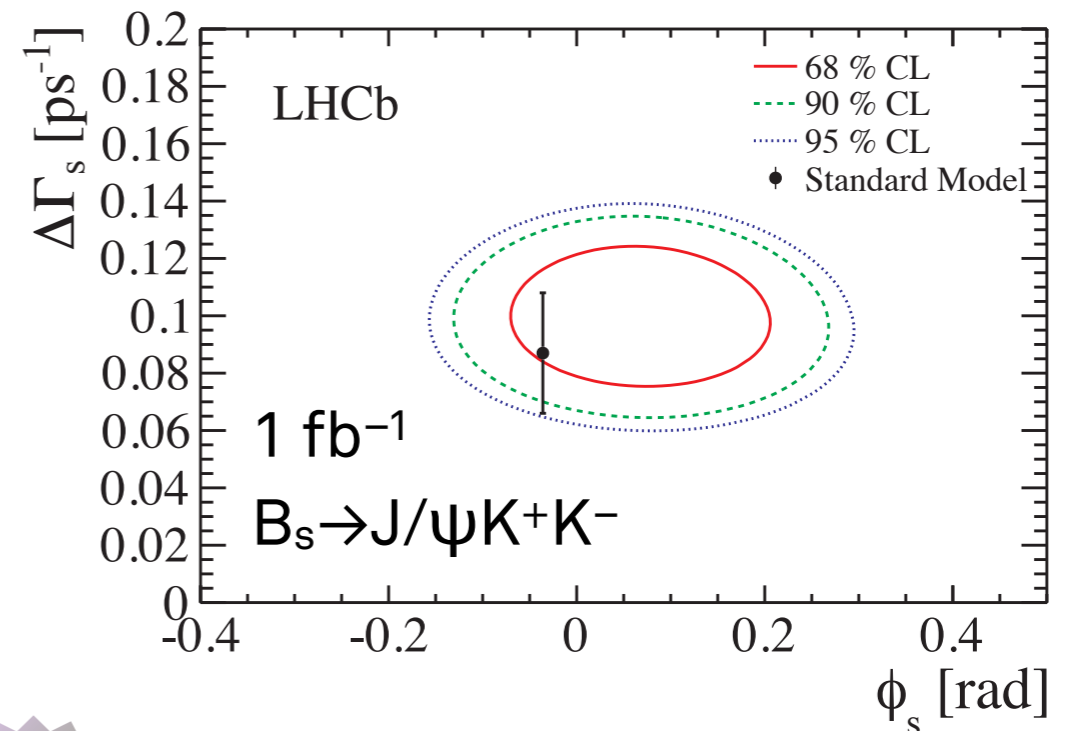
$$\phi_s = 0.01 \pm 0.07 \text{ (stat)} \pm 0.01 \text{ (syst) rad}$$

$$\Gamma_s = 0.661 \pm 0.004 \text{ (stat)} \pm 0.006 \text{ (syst) ps}^{-1}$$

$$\Delta\Gamma_s = 0.106 \pm 0.011 \text{ (stat)} \pm 0.007 \text{ (syst) ps}^{-1}$$

most
precise!

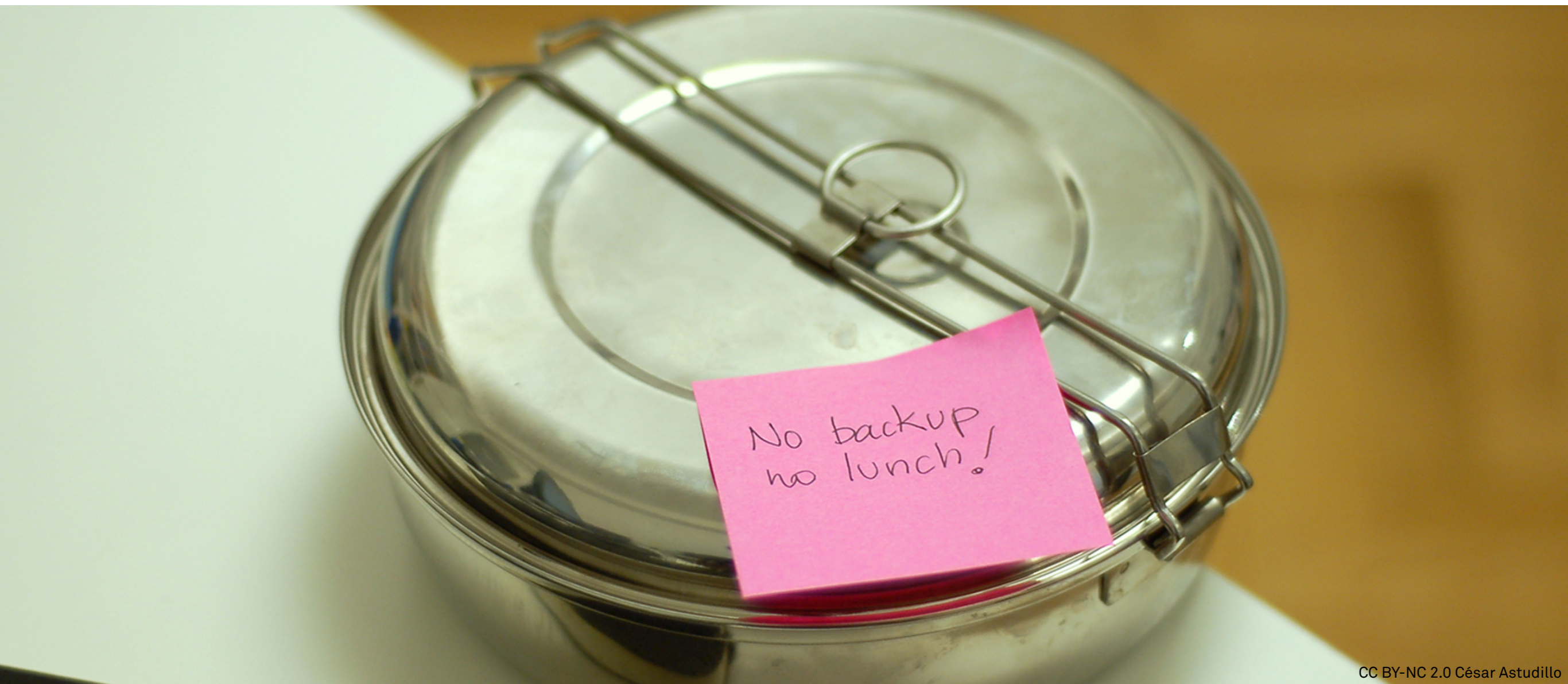
- ▶ combining OS+SS tagging
- ▶ data split in six bins of invariant $K^+ K^-$ mass
 - higher statistical precision
 - resolve ambiguity in ϕ_s and $\Delta\Gamma_s$



Phys. Rev. D 87, 112010 (2013)

Conclusions

- ▶ with 1 fb^{-1} of data:
 - $\phi_s, \Delta\Gamma_s, \Gamma_s$: most precise single measurement
 - $S_{J/\psi K_S}, C_{J/\psi K_S}$: most precise and first significant CP violation at a hadron collider
 - γ : LHCb competitive
 - $B_{(s)} \rightarrow K\pi$: first observation of CP violation in B_s decays
- ▶ new analyses with 3 fb^{-1} expected soon:
 - Standard Model tests and searches for new physics ongoing



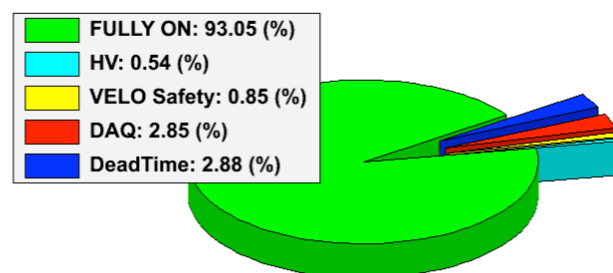
Backup

LHCb facts

Integrated luminosity

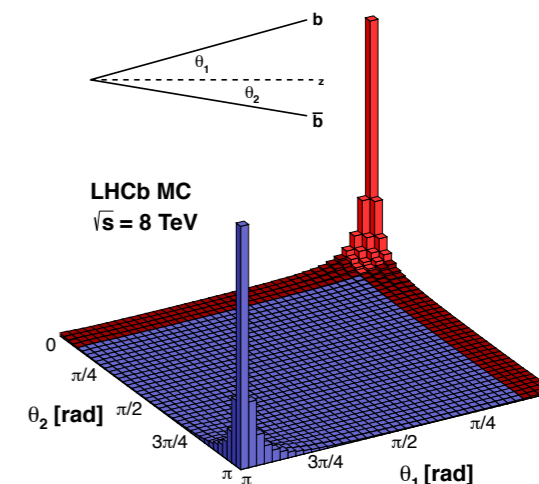
2010: 37 pb⁻¹
 2011: 1.0 fb⁻¹
 2012: 2 fb⁻¹ (note number of digits)

LHCb Efficiency breakdown pp collisions 2010-2012



Acceptance

pseudorapidity:
 $2 < \eta < 5$



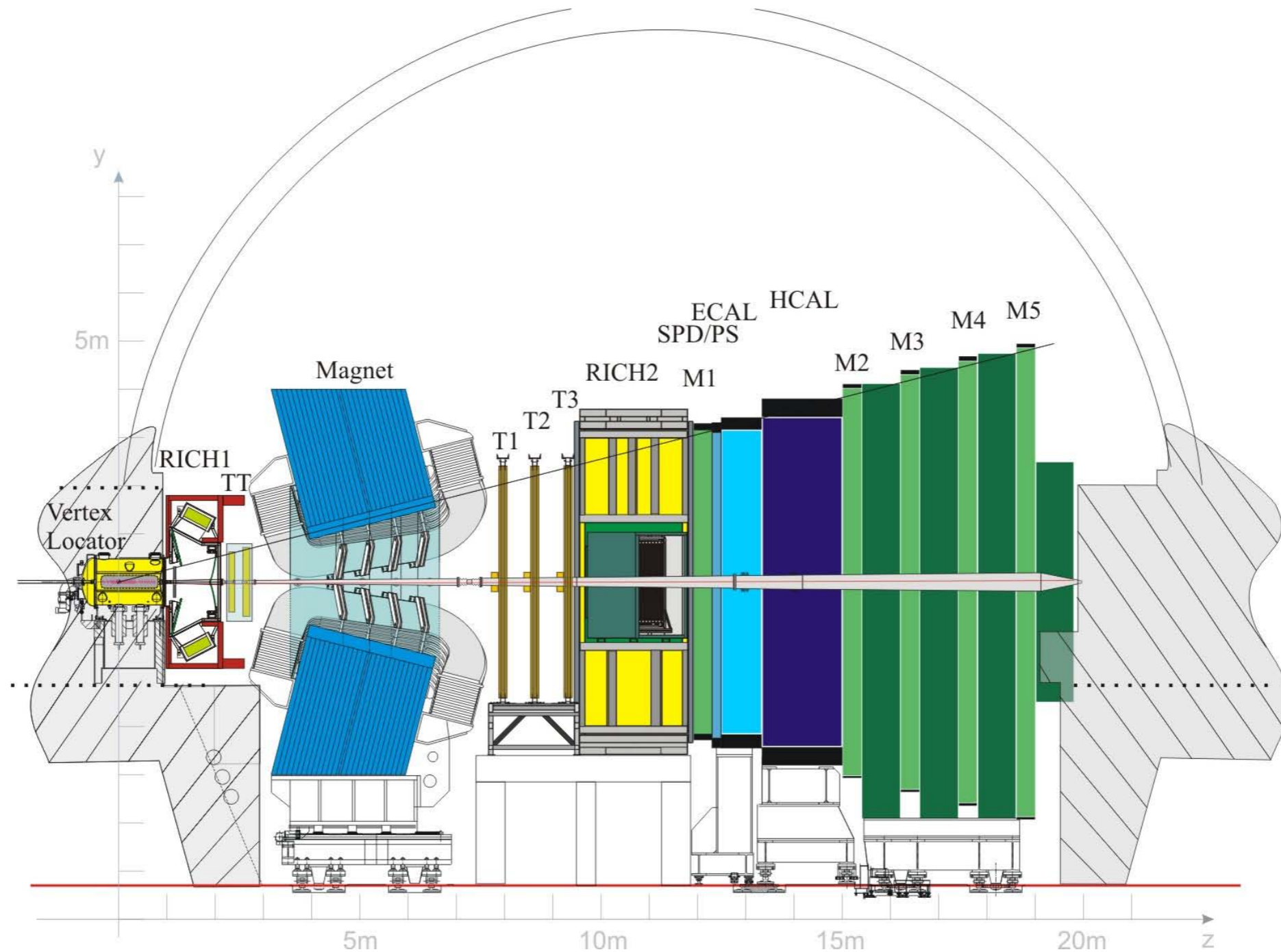
Resolutions

momentum resolution:
 $\Delta p / p = 0.4 \% \text{ at } 5 \text{ GeV}/c \text{ to } 0.6 \% \text{ at } 100 \text{ GeV}/c$
 ECAL resolution (nominal):
 $1 \% + 10 \% / \sqrt{E[\text{GeV}]}$
 impact parameter resolution:
 20 μm for high-pT tracks
 invariant mass resolution:
 $\sim 8 \text{ MeV}/c^2$ for $B \rightarrow J/\psi X$ decays with constraint on J/ψ mass
 $\sim 22 \text{ MeV}/c^2$ for two-body B decays
 $\sim 100 \text{ MeV}/c^2$ for $B_S \rightarrow \varphi \gamma$, dominated by photon contribution
 decay time resolution:
 45 fs for $B_S \rightarrow J/\psi \varphi$ and for $B_S \rightarrow D_S \pi$

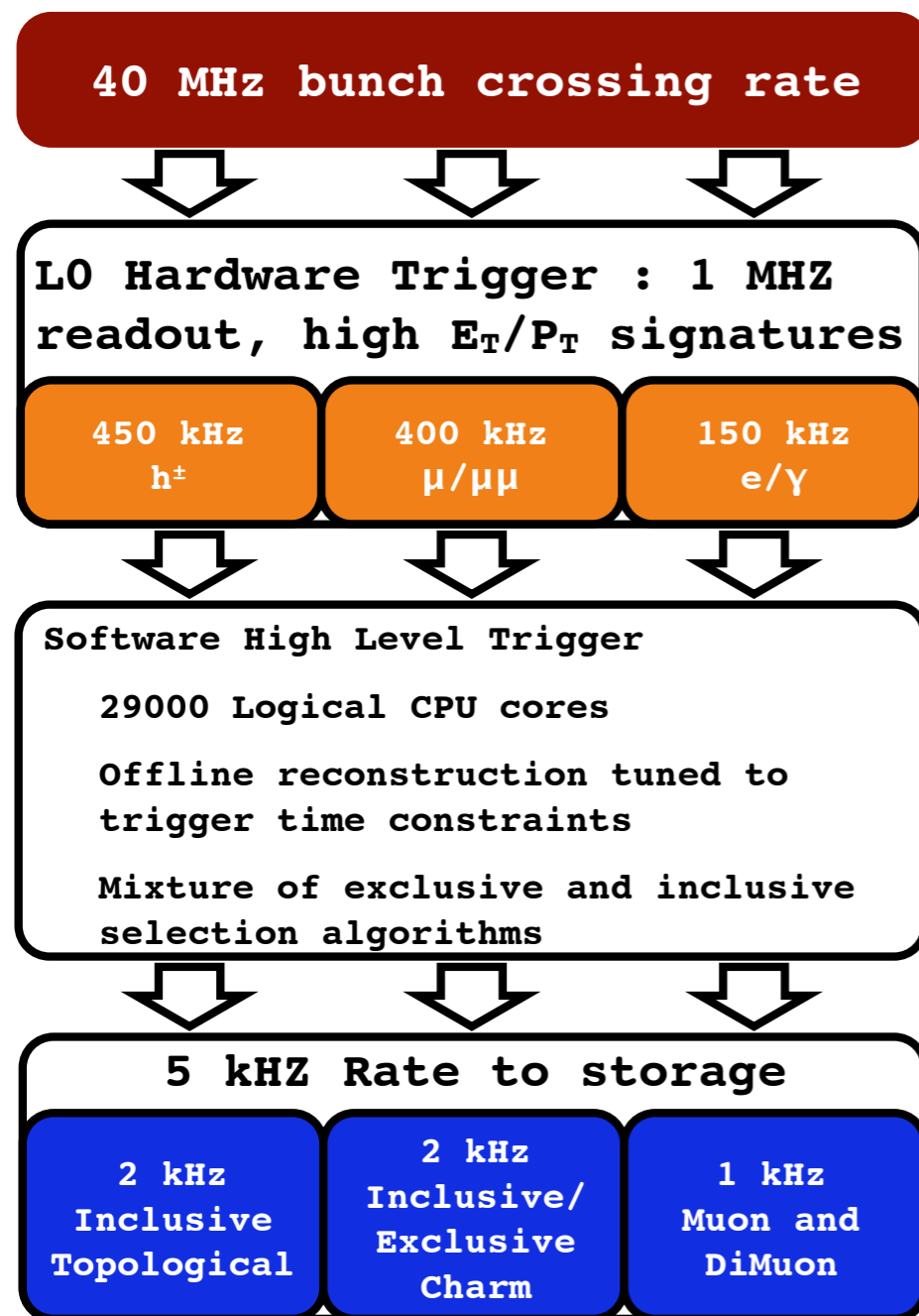
Efficiencies

percentage of working detector channels:
 $\sim 99 \%$ for all sub-detectors
 data taking efficiency:
 $> 90 \%$
 data good for analyses:
 $> 99 \%$
 trigger efficiencies:
 $\sim 90 \%$ for dimuon channels
 $\sim 30 \%$ for multi-body hadronic final states
 track reconstruction efficiency:
 $> 96 \%$ for long tracks
 electron ID efficiency:
 $\sim 90 \%$ for $\sim 5 \% e \rightarrow h$ mis-id probability
 kaon ID efficiency:
 $\sim 95 \%$ for $\sim 5 \% \pi \rightarrow K$ mis-id probability
 muon ID efficiency:
 $\sim 97 \%$ for 1-3 $\% \pi \rightarrow \mu$ mis-id probability

LHCb schematics



LHCb Trigger



▶ two stage trigger

- L0 Trigger (Hardware)
- High Level Trigger (Software)

Direct CPV in $B_{(s)} \rightarrow K\pi$: Correction

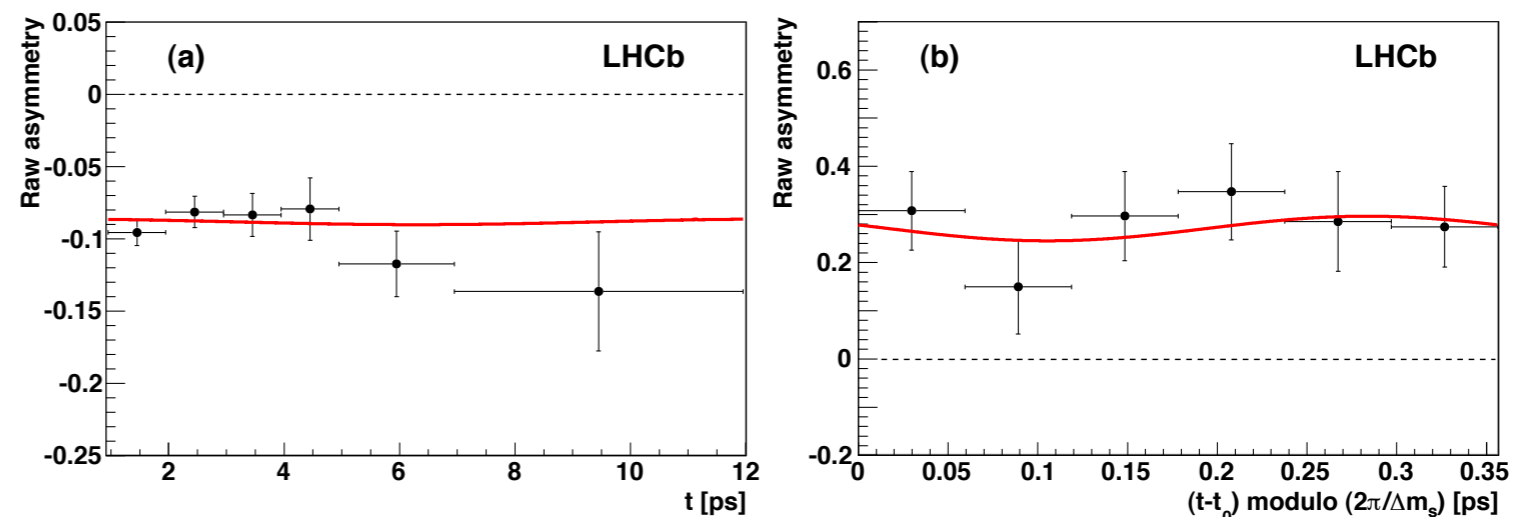
- ▶ Correction from raw to CP asymmetry:

$$A_{CP} = A_{\text{raw}} - \zeta_{d(s)} A_D(K\pi) + \kappa_{d(s)} A_P(B_{(s)}^0)$$

$\zeta_d=+1, \zeta_s=-1$ instrumental asymmetry mixing dilution production asymmetry

- ▶ A_D : measured with $D^{*+} \rightarrow D^0(K-\pi^+)\pi^+ / D^0(K-K^+)\pi^+$ decays (incl. $D^0 \rightarrow K-K^+$ CP asymmetry)
- ▶ A_P : measured from time-dependent raw asymmetries

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a_{sl} in B_s : systematics

Table 3: Sources of systematic uncertainty on A_{meas} .

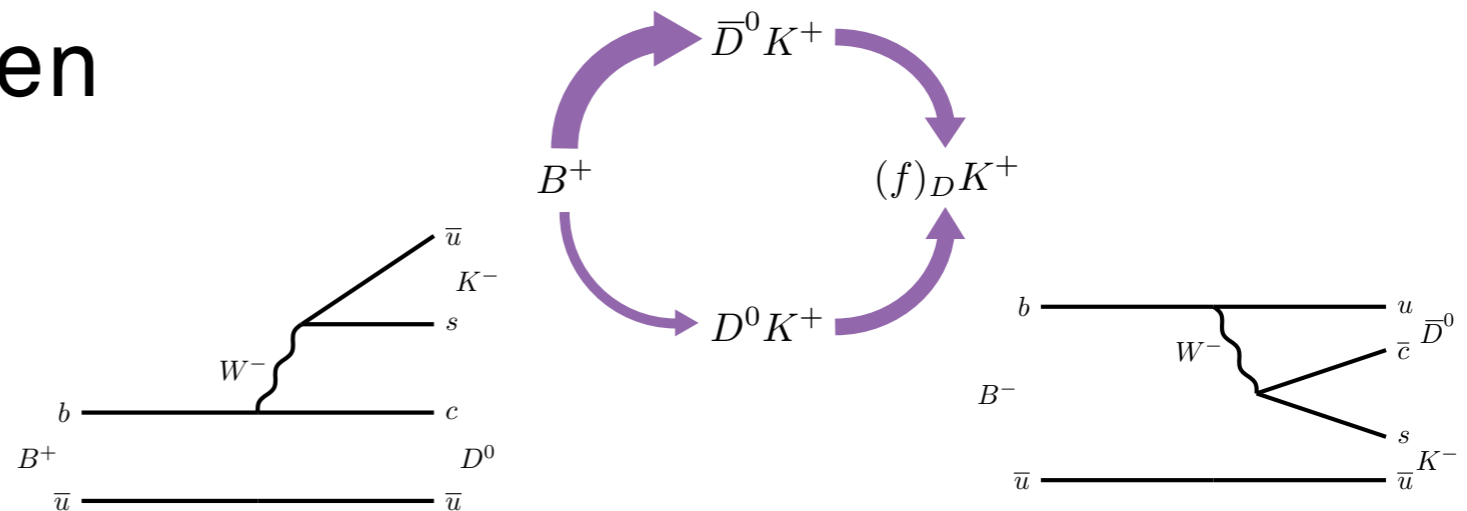
Source	$\sigma(A_{\text{meas}})[\%]$
Signal modelling and muon correction	0.07
Statistical uncertainty on the efficiency ratios	0.08
Background asymmetry	0.05
Asymmetry in track reconstruction	0.13
Field-up and field-down run conditions	0.01
Software trigger bias (topological trigger)	0.05
Total	0.18

Table 2: Muon efficiency ratio corrected asymmetry A_{μ}^c . The errors account for the statistical uncertainties in the B_s^0 signal yields.

A_{μ}^c [%]	KS muon correction		MS muon correction		Average
	$p_x p_y$	$p_T \phi$	$p_x p_y$	$p_T \phi$	
Up	$+0.38 \pm 0.38$	$+0.30 \pm 0.38$	$+0.64 \pm 0.37$	$+0.63 \pm 0.37$	$+0.49 \pm 0.38$
Down	-0.17 ± 0.32	-0.25 ± 0.32	-0.60 ± 0.32	-0.62 ± 0.32	-0.41 ± 0.32
Avg.	$+0.11 \pm 0.25$	$+0.02 \pm 0.25$	$+0.02 \pm 0.24$	$+0.01 \pm 0.24$	$+0.04 \pm 0.25$

γ in $B^\pm \rightarrow Dh^\pm$

- ▶ interference between two tree diagrams
- ▶ methods differ in D decay products



- ▶ measure charge asymmetries and yield ratios (GLW/ADS):

$$A_h^f = \frac{\Gamma(B^- \rightarrow D[\rightarrow f]h^-) - \Gamma(B^+ \rightarrow D[\rightarrow \bar{f}]h^+)}{\Gamma(B^- \rightarrow D[\rightarrow f]h^-) + \Gamma(B^+ \rightarrow D[\rightarrow \bar{f}]h^+)}$$

$$R_{K/\pi}^f = \frac{\Gamma(B^- \rightarrow D[\rightarrow f]K^-) + \Gamma(B^+ \rightarrow D[\rightarrow \bar{f}]K^+)}{\Gamma(B^- \rightarrow D[\rightarrow f]\pi^-) + \Gamma(B^+ \rightarrow D[\rightarrow \bar{f}]\pi^+)}$$

$$R_h^\pm = \frac{\Gamma(B^\pm \rightarrow D[\rightarrow f_{\text{sup}}]h^\pm)}{\Gamma(B^\pm \rightarrow D[\rightarrow f]h^\pm)}$$

- ▶ cartesian coordinates from Dalitz plane (GGSZ)

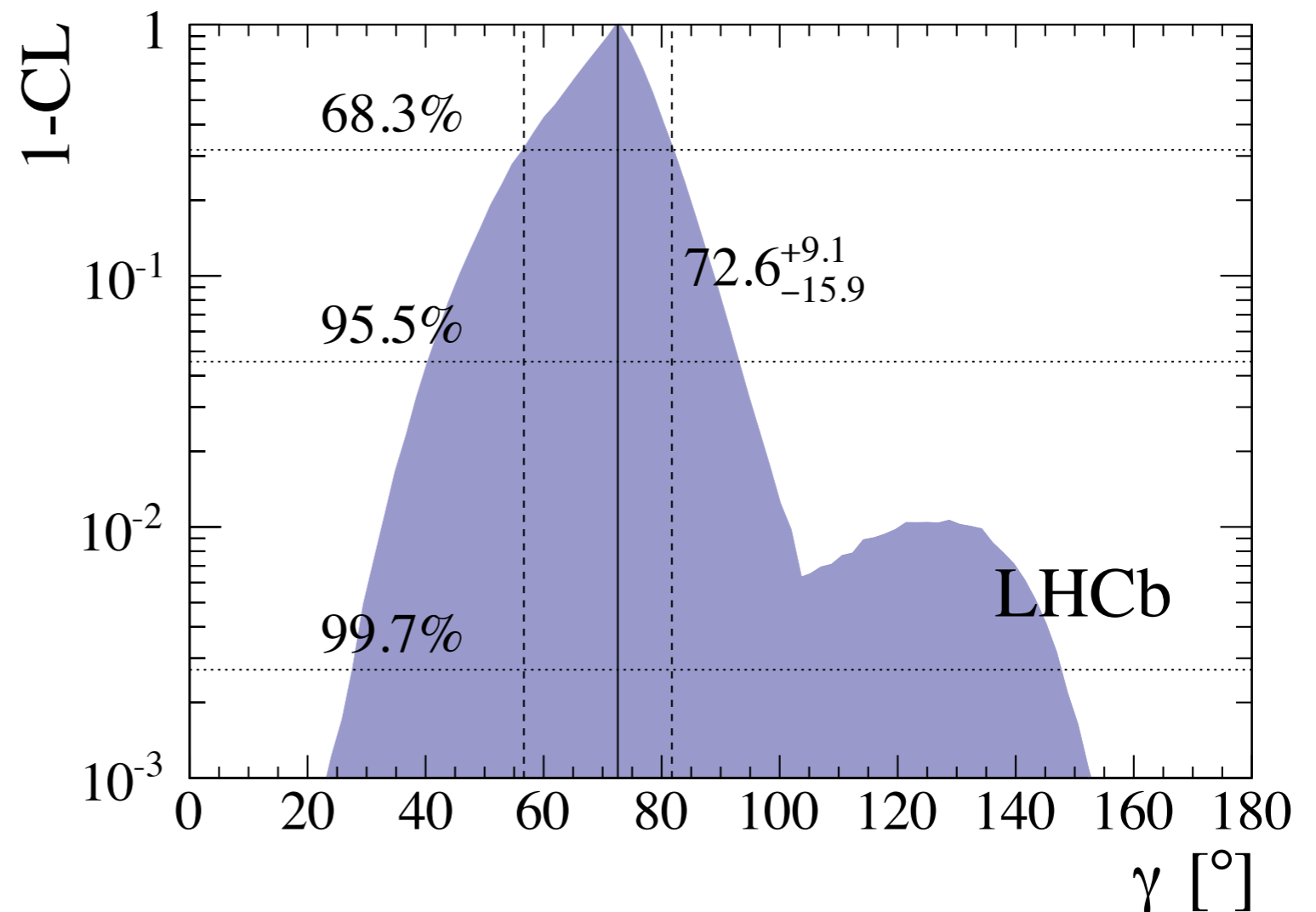
γ in $B^\pm \rightarrow Dh^\pm$, 1 fb^{-1}

► Combining $B^\pm \rightarrow DK^\pm$ and $B^\pm \rightarrow D\pi^\pm$:

arXiv:1305.2050

- GLW/ADS/GGSZ with 1 fb^{-1}
- incl. D mixing

$$\gamma = (72.6^{+9.7}_{-17.2})^\circ$$



γ in $B^\pm \rightarrow Dh^\pm$: plugin method

► plugin method similar to Feldman-Cousins:

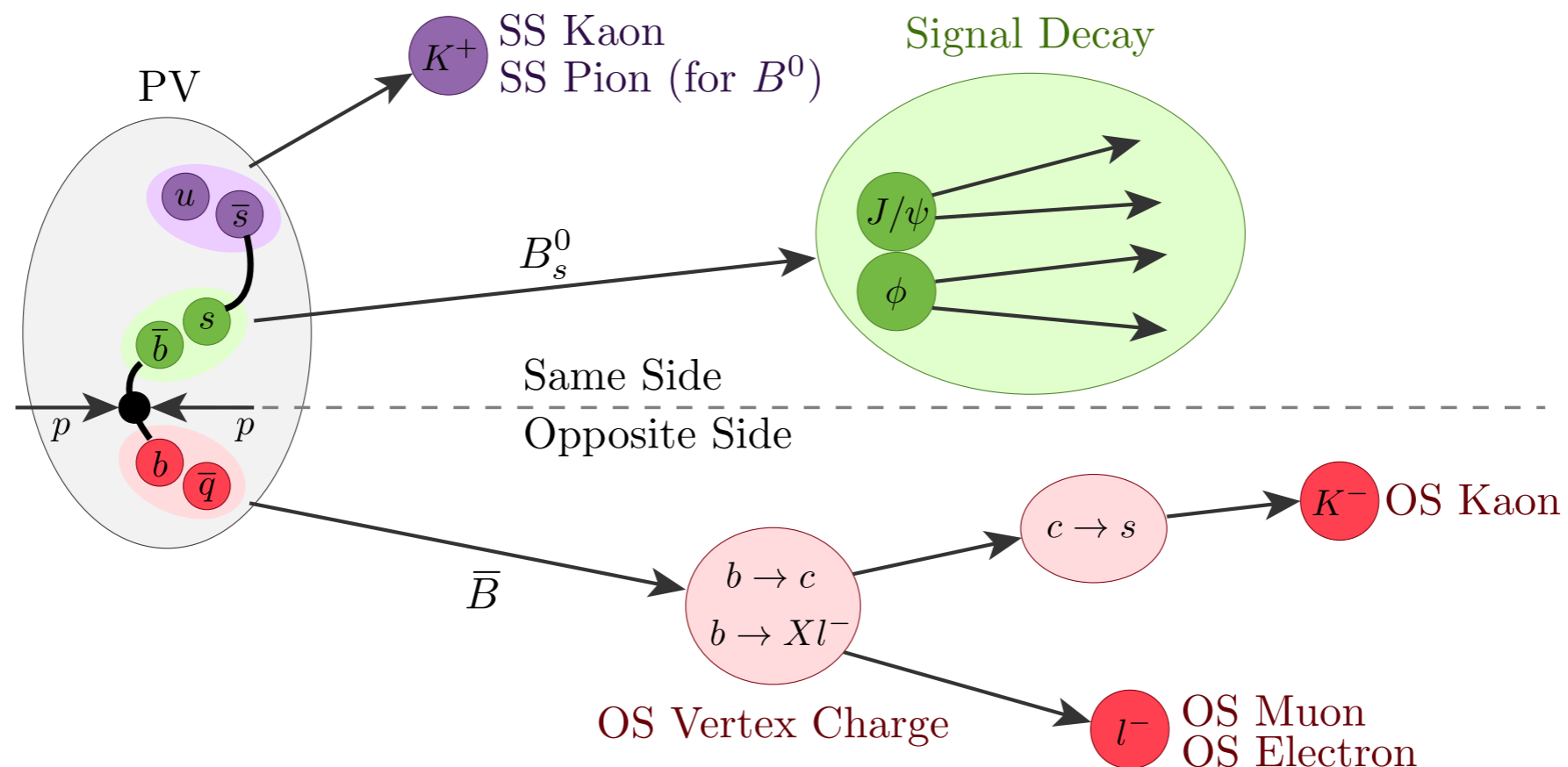
The evaluation of this combination follows a frequentist approach. A χ^2 -function is defined as $\chi^2(\vec{\alpha}) = -2 \ln \mathcal{L}(\vec{\alpha})$, where $\mathcal{L}(\vec{\alpha})$ is defined in Eq. 1. The best-fit point is given by the global minimum of the χ^2 -function, $\chi^2(\vec{\alpha}_{\min})$. To evaluate the confidence level for a given value of a certain parameter, say $\gamma = \gamma_0$ in the following, the value of the χ^2 -function at the new minimum is considered, $\chi^2(\vec{\alpha}'_{\min}(\gamma_0))$. This also defines the profile likelihood function $\hat{\mathcal{L}}(\gamma_0) = \exp(-\chi^2(\vec{\alpha}'_{\min})/2)$. Then a test statistic is defined as $\Delta\chi^2 = \chi^2(\vec{\alpha}'_{\min}) - \chi^2(\vec{\alpha}_{\min})$. The p -value, or $1 - \text{CL}$, is calculated by means of a Monte Carlo procedure, described in Ref. [29] and briefly recapitulated here. For each value of γ_0 :

1. $\Delta\chi^2$ is calculated;
2. a set of pseudoexperiments \vec{A}_j is generated using Eq. 1 with parameters $\vec{\alpha}$ set to $\vec{\alpha}'_{\min}$ as the PDF;
3. $\Delta\chi^{2'}$ of the pseudoexperiment is calculated by replacing $\vec{A}_{\text{obs}} \rightarrow \vec{A}_j$ and minimising with respect to $\vec{\alpha}$, once with γ as a free parameter, and once with γ fixed to γ_0 ;
4. $1 - \text{CL}$ is calculated as the fraction of pseudoexperiments which perform worse ($\Delta\chi^2 < \Delta\chi^{2'}$) than the measured data.

This method is sometimes known as the “ $\hat{\mu}$ ”, or the “plug-in” method. Its coverage cannot be guaranteed [29] for the full parameter space, but is verified for the best-fit point. The reason is, that at each point γ_0 , the nuisance parameters, *i.e.* the components of $\vec{\alpha}$ other than the parameter of interest, are set to their best-fit values for this point, as opposed to computing an n -dimensional confidence belt, which is computationally very demanding.

Flavour Tagging

- ▶ infer B production flavour
- ▶ **Opposite Side algorithms:**
charge of leptons/hadrons of other B meson
- ▶ **Same Side algorithms:**
Kaon/Pion charge from fragmentation
- ▶ mistag probability ω
 - dilution $D=(1-2\omega)$ of CP asymmetry
- ▶ calibration of taggers necessary

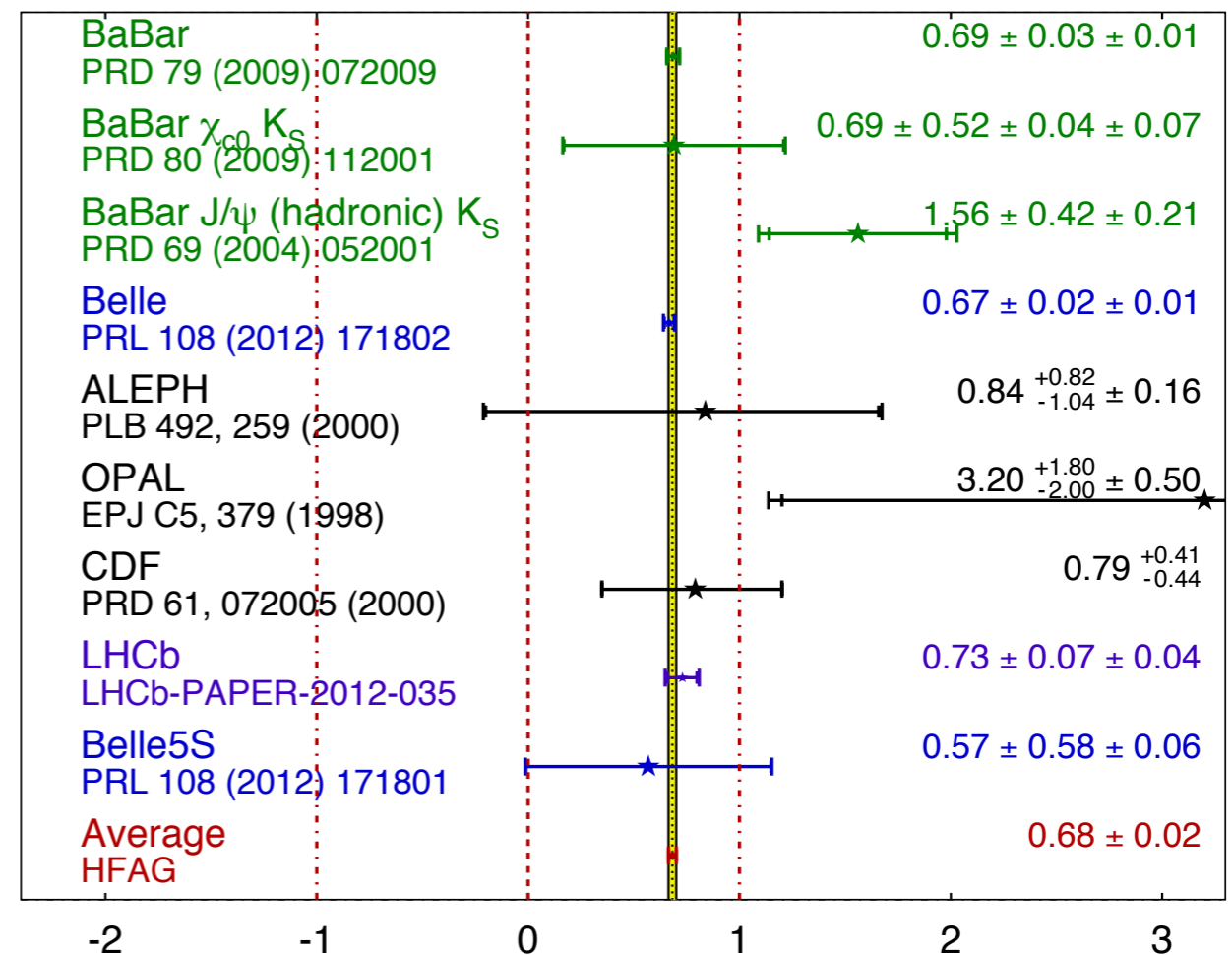


CPV in $B_d \rightarrow J/\psi K_S$: comparison

- ▶ LHCb not yet competitive with B factories
- ▶ measurement on 3 fb^{-1} data expected soon

$$\sin(2\beta) \equiv \sin(2\phi_1)$$

HFAG
 CKM 2012
 PRELIMINARY



CPV in $B_d \rightarrow J/\psi K_S$: systematics/tagging

Table 1

Summary of systematic uncertainties on the CP parameters.

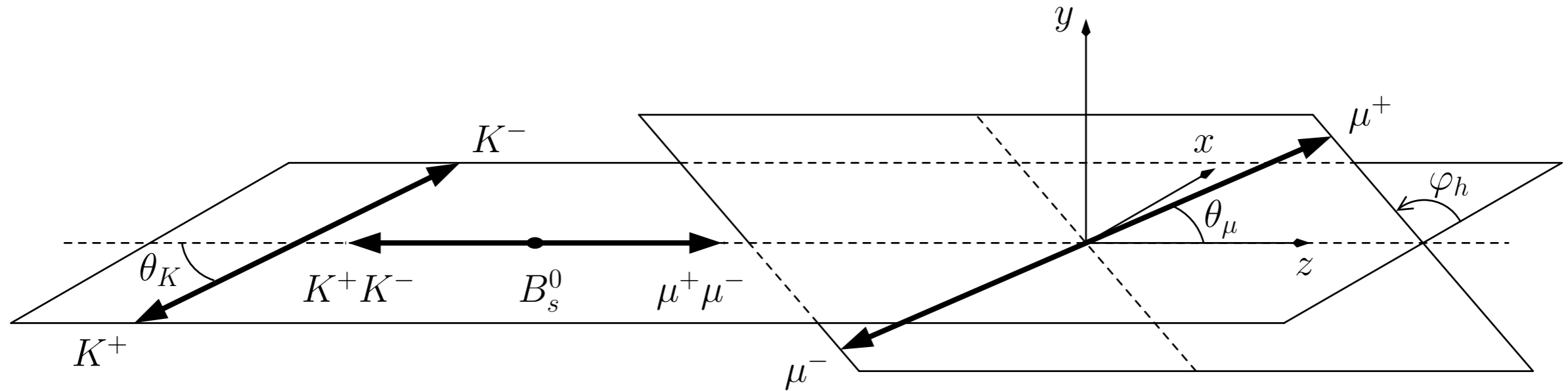
Origin	$\sigma(S_{J/\psi K_S^0})$	$\sigma(C_{J/\psi K_S^0})$
Tagging calibration	0.034	0.001
Tagging efficiency difference	0.002	0.002
Decay time resolution	0.001	0.002
Decay time acceptance	0.002	0.006
Background model	0.012	0.009
Fit bias	0.004	0.005
Total	0.036	0.012

$$\varepsilon_{\text{tag}} \mathcal{D}^2 = (2.38 \pm 0.27)\%$$

$$\varepsilon_{\text{tag}} = (32.65 \pm 0.31)\%$$

$$\omega = (36.5 \pm 0.8)\%$$

CPV $B_s \rightarrow J/\psi K^+ K^- / J/\psi \pi^+ \pi^-$: angles

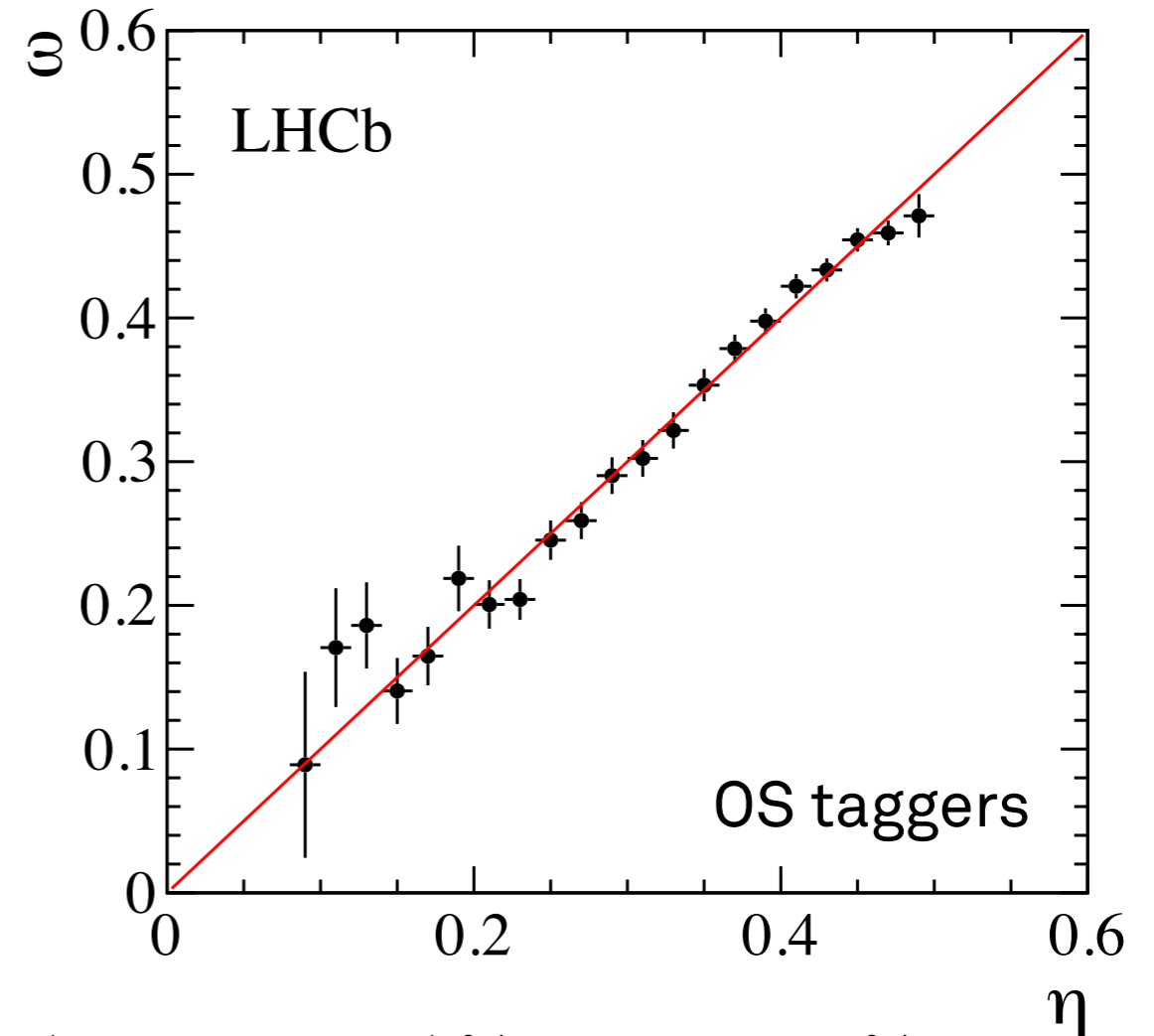


Flavour Tagging calibration

- predicted wrong-tag probability η transformed:

$$\omega(\eta) = p_0 \pm \frac{\Delta p_0}{2} + p_1(\eta - \langle \eta \rangle)$$

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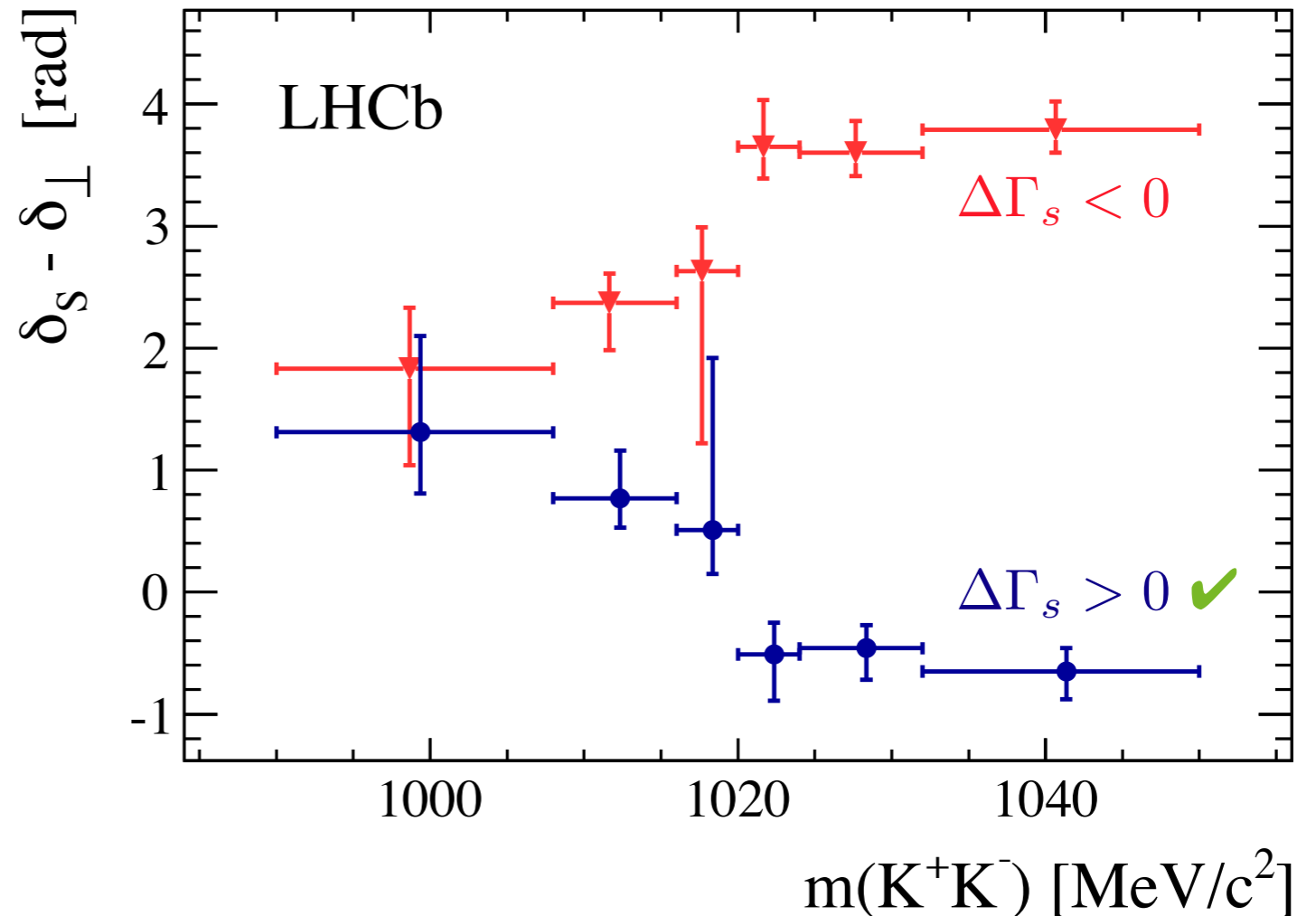


$$\varepsilon_{\text{tag}} \mathcal{D}^2 = (3.13 \pm 0.12 \pm 0.20)\% \quad \varepsilon_{\text{tag}} = (39.36 \pm 0.32)\% \quad \omega = 35.9\%$$

Calibration	p_0	p_1	$\langle \eta \rangle$	Δp_0
OS	$0.392 \pm 0.002 \pm 0.008$	$1.000 \pm 0.020 \pm 0.012$	0.392	0.011 ± 0.003
SSK	$0.350 \pm 0.015 \pm 0.007$	$1.000 \pm 0.160 \pm 0.020$	0.350	-0.019 ± 0.005

CPV $B_s \rightarrow J/\psi K^+ K^- / J/\psi \pi^+ \pi^-$: ambiguity tu

- ▶ measure phase difference between S- and P-wave amplitudes
- ▶ physical solution:
 - decreasing trend with $m(K^+ K^-)$



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CPV $B_s \rightarrow J/\psi K^+ K^- / J/\psi \pi^+ \pi^-$: systematics

Table 9: Statistical and systematic uncertainties.

Source	Γ_s [ps ⁻¹]	$\Delta\Gamma_s$ [ps ⁻¹]	$ A_\perp ^2$	$ A_0 ^2$	δ_\parallel [rad]	δ_\perp [rad]	ϕ_s [rad]	$ \lambda $
Stat. uncertainty	0.0048	0.016	0.0086	0.0061	^{+0.13} _{-0.21}	0.22	0.091	0.031
Background subtraction	0.0041	0.002	–	0.0031	0.03	0.02	0.003	0.003
$B^0 \rightarrow J/\psi K^{*0}$ background	–	0.001	0.0030	0.0001	0.01	0.02	0.004	0.005
Ang. acc. reweighting	0.0007	–	0.0052	0.0091	0.07	0.05	0.003	0.020
Ang. acc. statistical	0.0002	–	0.0020	0.0010	0.03	0.04	0.007	0.006
Lower decay time acc. model	0.0023	0.002	–	–	–	–	–	–
Upper decay time acc. model	0.0040	–	–	–	–	–	–	–
Length and mom. scales	0.0002	–	–	–	–	–	–	–
Fit bias	–	–	0.0010	–	–	–	–	–
Decay time resolution offset	–	–	–	–	–	0.04	0.006	–
Quadratic sum of syst.	0.0063	0.003	0.0064	0.0097	0.08	0.08	0.011	0.022
Total uncertainties	0.0079	0.016	0.0107	0.0114	^{+0.15} _{-0.23}	0.23	0.092	0.038

Table 10: Statistical and systematic uncertainties for S-wave fractions in bins of $m(K^+ K^-)$.

Source	bin 1 F_S	bin 2 F_S	bin 3 F_S	bin 4 F_S	bin 5 F_S	bin 6 F_S
Stat. uncertainty	^{+0.081} _{-0.073}	^{+0.030} _{-0.027}	^{+0.014} _{-0.007}	^{+0.012} _{-0.009}	^{+0.027} _{-0.025}	^{+0.043} _{-0.042}
Background subtraction	0.014	0.003	0.001	0.002	0.004	0.006
$B^0 \rightarrow J/\psi K^{*0}$ background	0.010	0.006	0.001	0.001	0.002	0.018
Angular acc. reweighting	0.004	0.006	0.004	0.005	0.006	0.007
Angular acc. statistical	0.003	0.003	0.002	0.001	0.003	0.004
Fit bias	0.009	–	0.002	0.002	0.001	0.001
Quadratic sum of syst.	0.020	0.009	0.005	0.006	0.008	0.021
Total uncertainties	^{+0.083} _{-0.076}	^{+0.031} _{-0.029}	^{+0.015} _{-0.009}	^{+0.013} _{-0.011}	^{+0.028} _{-0.026}	^{+0.048} _{-0.047}

CPV $B_s \rightarrow J/\psi K^+ K^- / J/\psi \pi^+ \pi^-$: correlations

Table 6: Results of the maximum likelihood fit for the principal physics parameters. The first uncertainty is statistical and the second is systematic. The value of Δm_s was constrained to the measurement reported in Ref. [38]. The evaluation of the systematic uncertainties is described in Sect. 10.

Parameter	Value
Γ_s [ps ⁻¹]	$0.663 \pm 0.005 \pm 0.006$
$\Delta\Gamma_s$ [ps ⁻¹]	$0.100 \pm 0.016 \pm 0.003$
$ A_\perp ^2$	$0.249 \pm 0.009 \pm 0.006$
$ A_0 ^2$	$0.521 \pm 0.006 \pm 0.010$
δ_\parallel [rad]	$3.30^{+0.13}_{-0.21} \pm 0.08$
δ_\perp [rad]	$3.07 \pm 0.22 \pm 0.08$
ϕ_s [rad]	$0.07 \pm 0.09 \pm 0.01$
$ \lambda $	$0.94 \pm 0.03 \pm 0.02$

Table 7: Correlation matrix for the principal physics parameters.

	Γ_s [ps ⁻¹]	$\Delta\Gamma_s$ [ps ⁻¹]	$ A_\perp ^2$	$ A_0 ^2$	δ_\parallel [rad]	δ_\perp [rad]	ϕ_s [rad]	$ \lambda $
Γ_s [ps ⁻¹]	1.00	-0.39	0.37	-0.27	-0.09	-0.03	0.06	0.03
$\Delta\Gamma_s$ [ps ⁻¹]		1.00	-0.68	0.63	0.03	0.04	-0.04	0.00
$ A_\perp ^2$			1.00	-0.58	-0.28	-0.09	0.08	-0.04
$ A_0 ^2$				1.00	-0.02	-0.00	-0.05	0.02
δ_\parallel [rad]					1.00	0.32	-0.03	0.05
δ_\perp [rad]						1.00	0.28	0.00
ϕ_s [rad]							1.00	0.04
$ \lambda $								1.00