



The large scale structure of the Universe as seen by Planck

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On behalf of the Planck Collaboration

XVII. Gravitational lensing by large scale structure

XVI. Cosmological parameters

XVIII. Gravitational lensing - infrared background correlation

XIX. The integrated Sachs-Wolfe effect

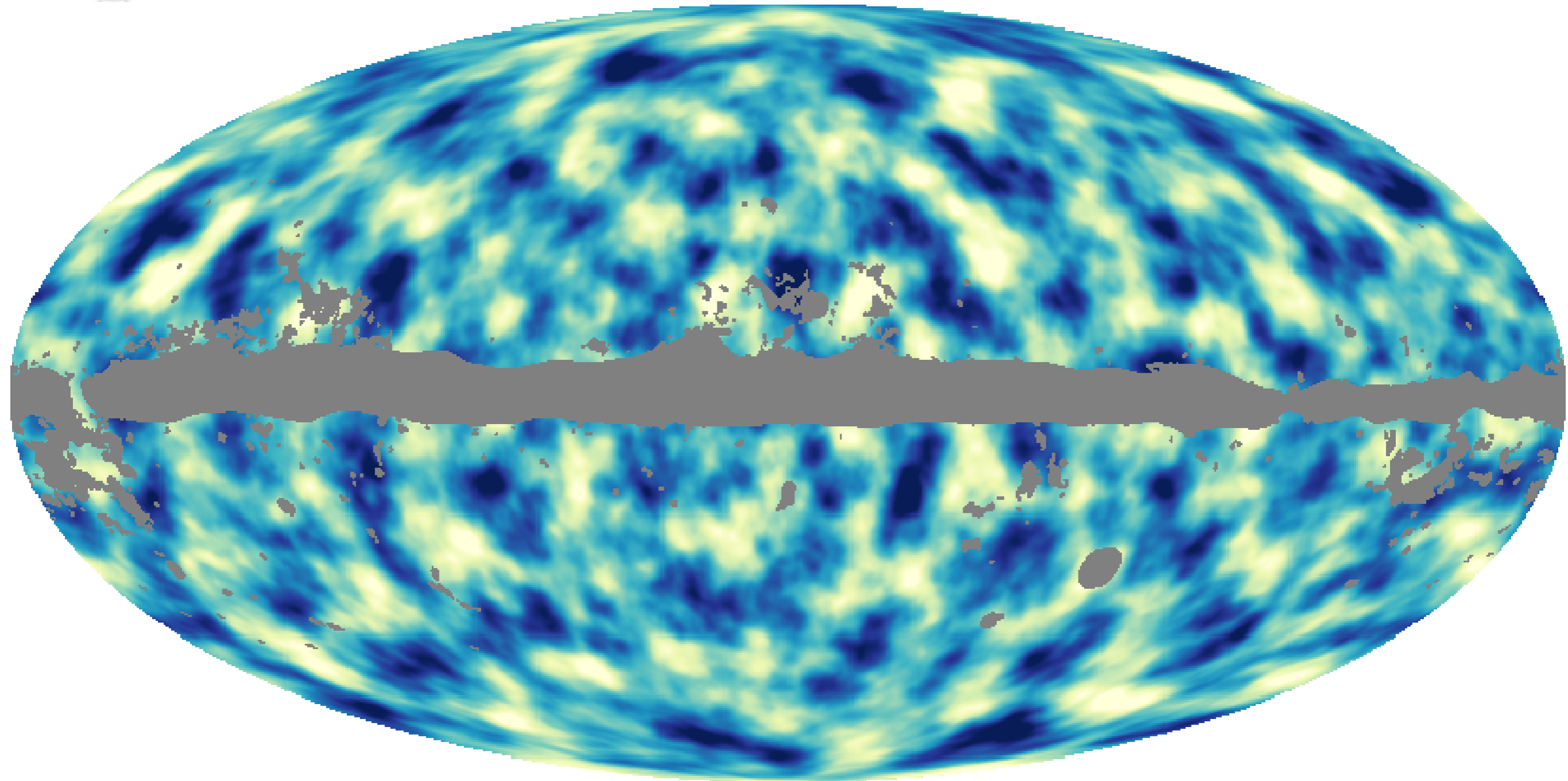
The scientific results that we present today are a product of the Planck Collaboration, including individuals from more than 100 scientific institutes in Europe, the USA and Canada



Planck is a project of the European Space Agency, with instruments provided by two scientific Consortia funded by ESA member states (in particular the lead countries: France and Italy) with contributions from NASA (USA), and telescope reflectors provided in a collaboration between ESA and a scientific Consortium led and funded by Denmark.



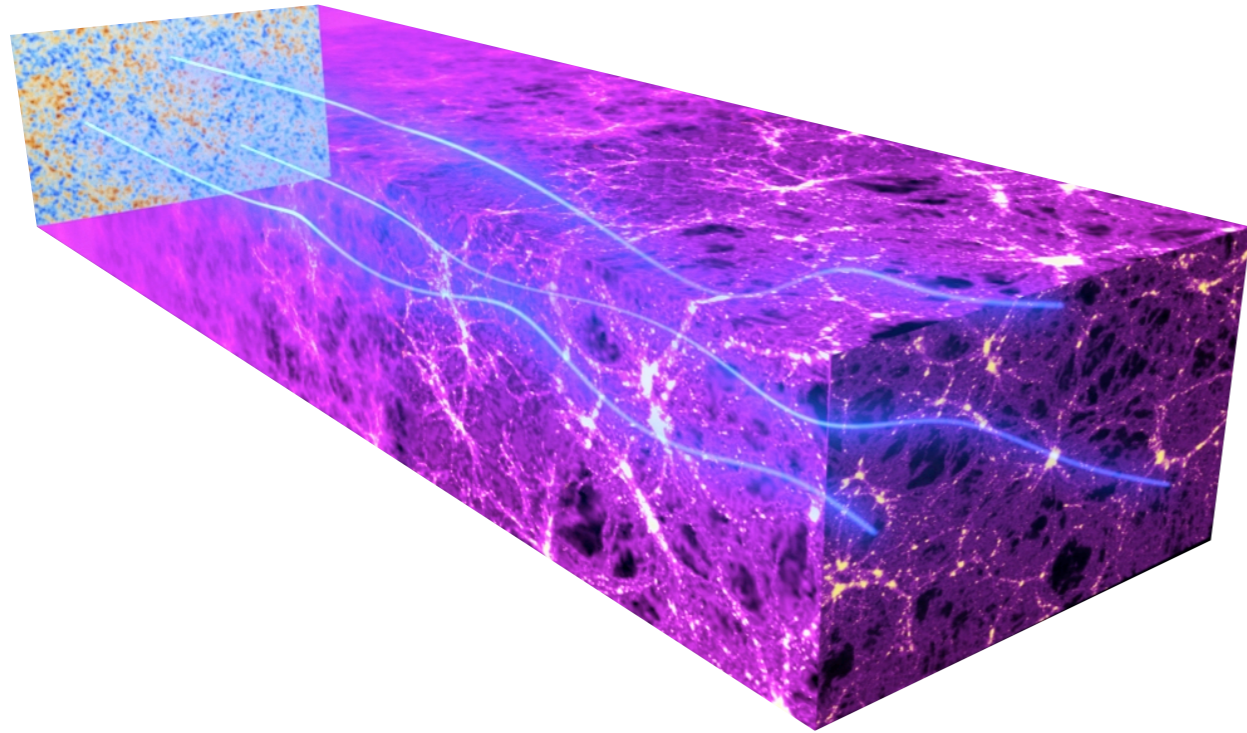
The matter in the Universe



Planck picture of the matter distribution at $z \sim 2$



CMB lensing



Typical deflection $\delta\beta$ sourced by potential Ψ

$$\Psi \sim 2 \cdot 10^{-5} \quad \delta\beta \sim 10^{-4}$$

Photons encounter ~ 50 potential wells

r.m.s deflection
 $50^{1/2} * 10^{-4} \sim 2$ arcmin

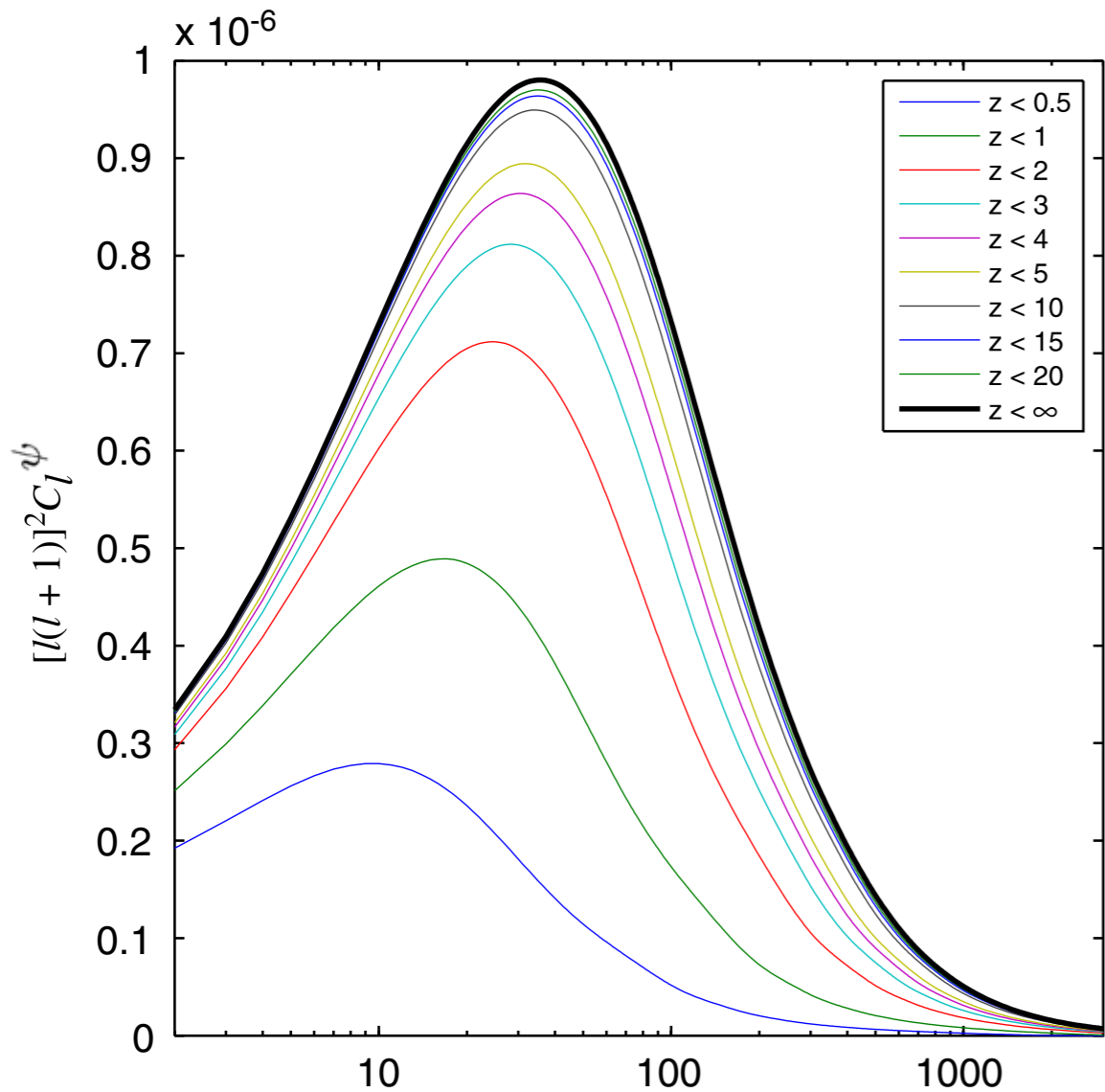
$$\Theta[\hat{\mathbf{n}}] = \tilde{\Theta}[\hat{\mathbf{n}} + \nabla\phi(\hat{\mathbf{n}})] \approx \tilde{\Theta}[\hat{\mathbf{n}}] + \nabla\phi[\hat{\mathbf{n}}] \nabla\tilde{\Theta}[\hat{\mathbf{n}}] + \dots$$

$$\phi(\hat{\mathbf{n}}) = -2 \int_0^{\chi_*} d\chi \frac{f_K(\chi_* - \chi)}{f_K(\chi_*)f_K(\chi)} \Psi(\chi\hat{\mathbf{n}}; \eta_0 - \chi).$$

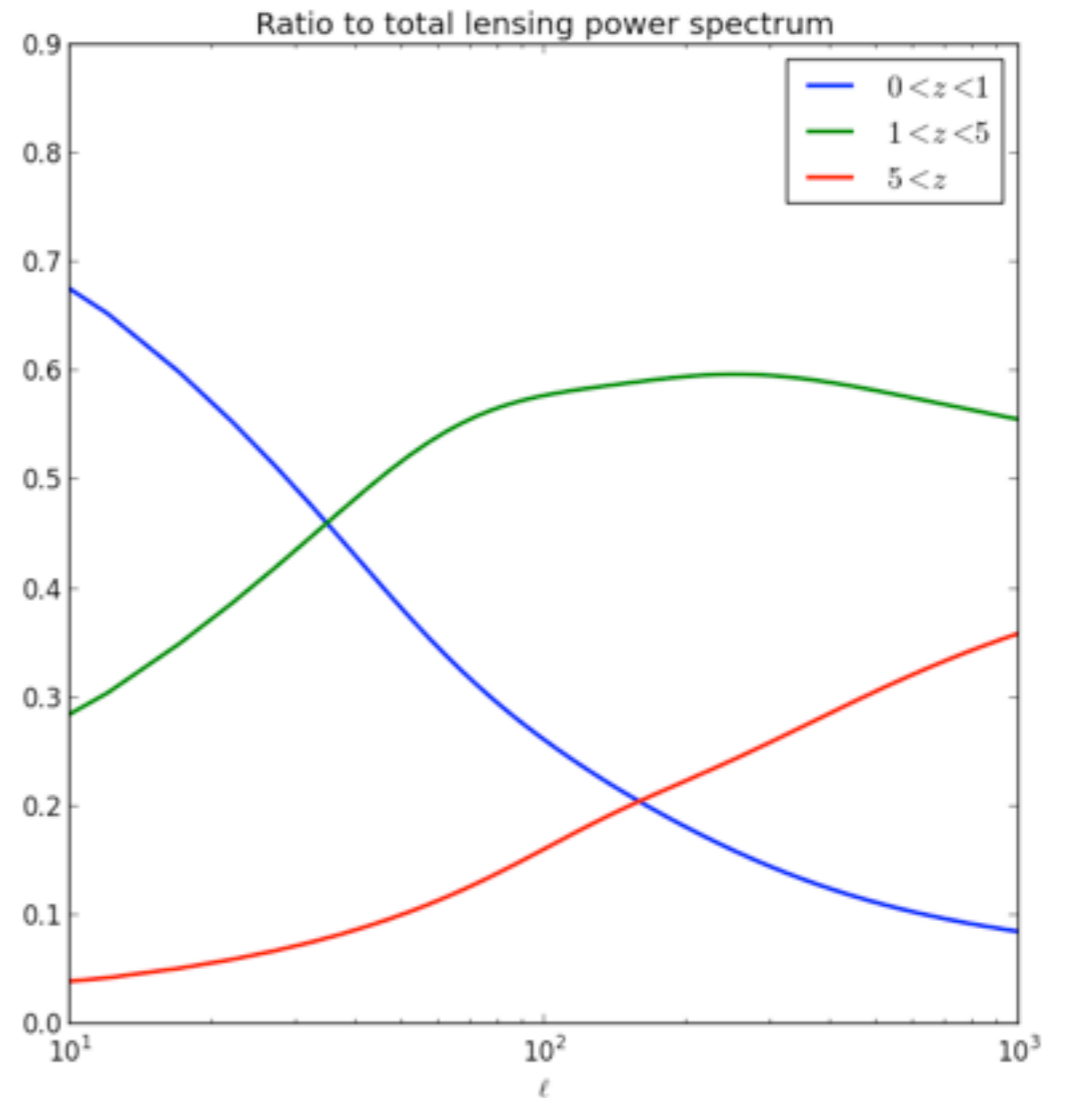


The lensing potential

$$\phi(\hat{n}) = -2 \int_0^{\chi_*} d\chi \frac{f_K(\chi_* - \chi)}{f_K(\chi_*)f_K(\chi)} \Psi(\chi \hat{n}; \eta_0 - \chi).$$



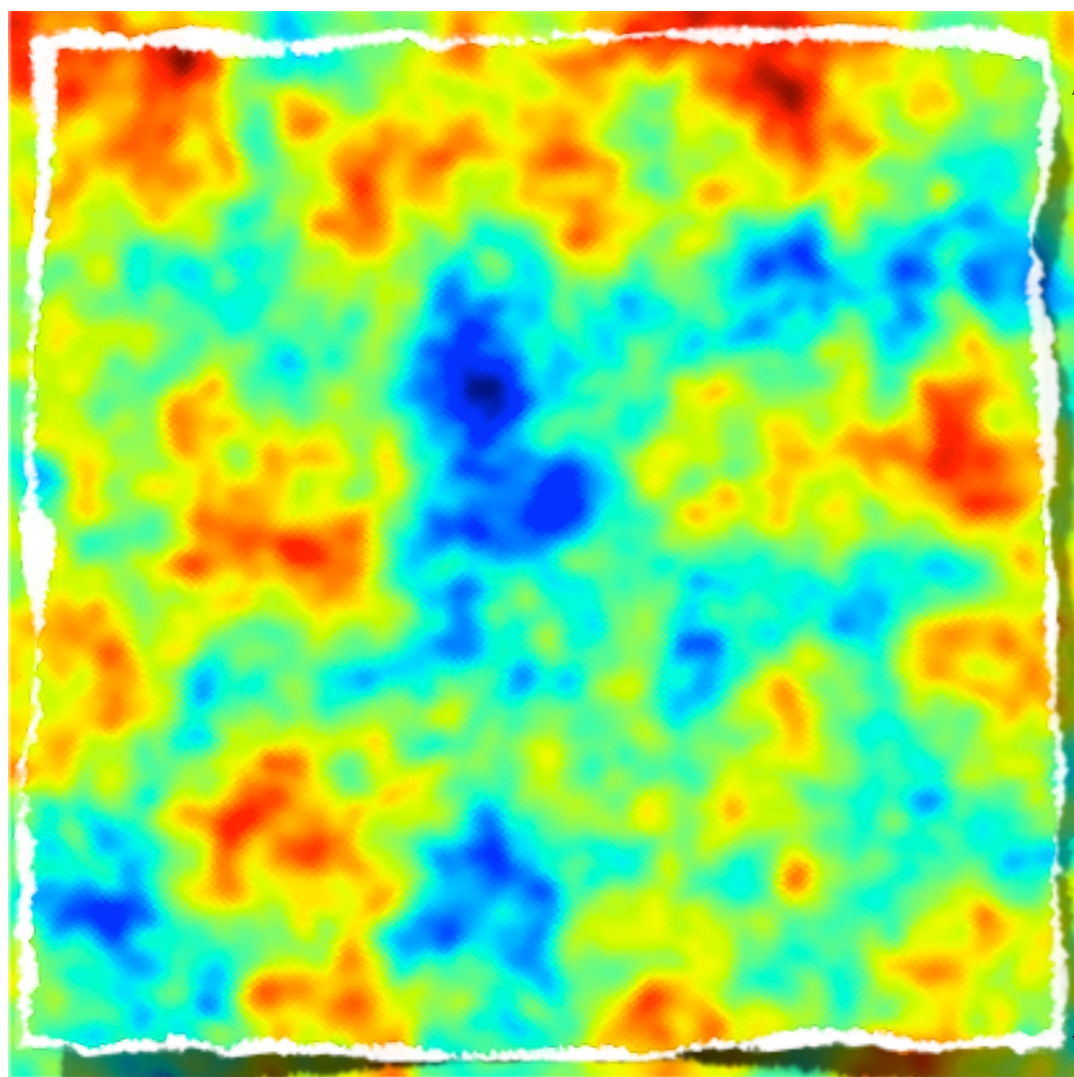
Lewis & Challinor, 2006





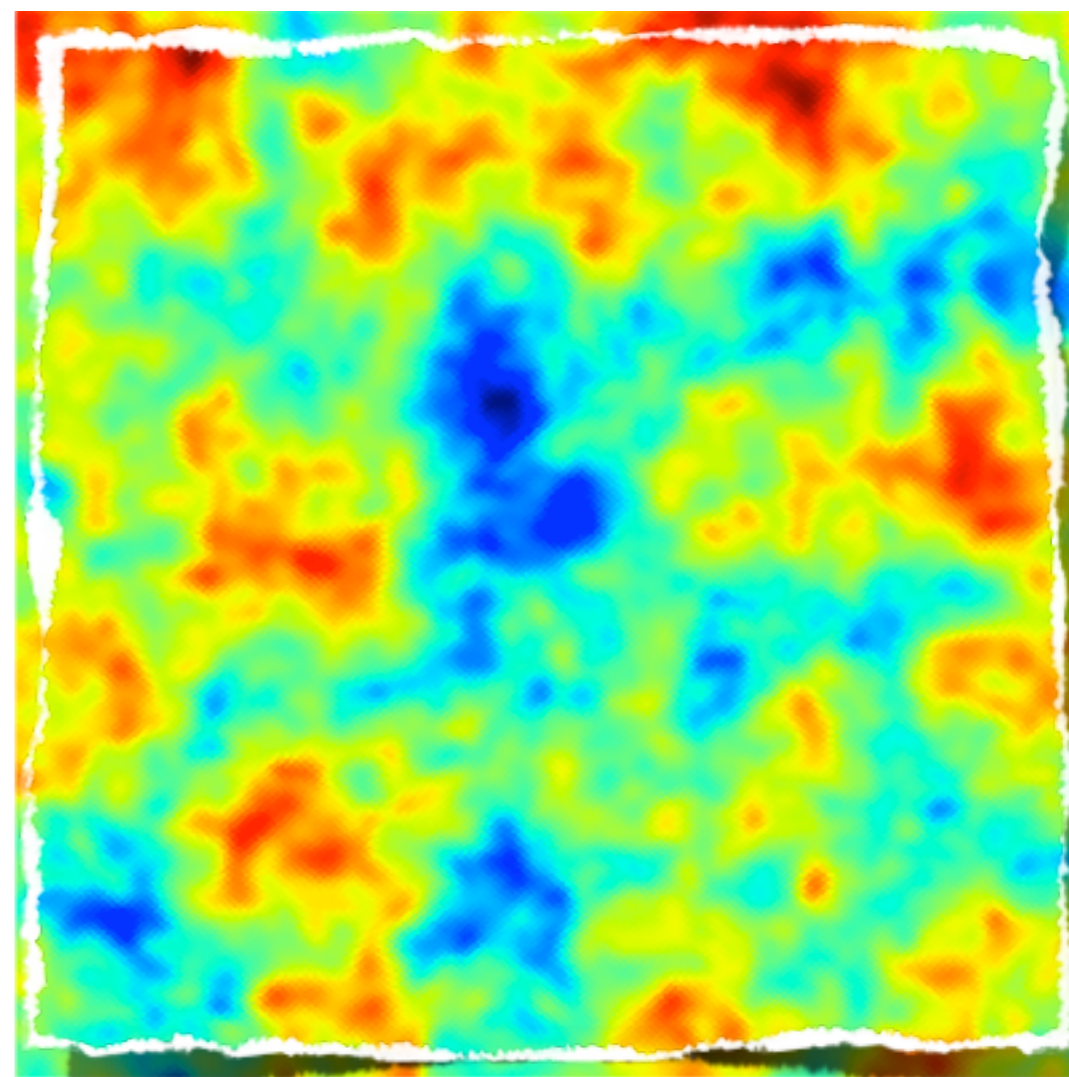
CMB lensing

Deflections are about 2 arcmin



Unlensed

6°

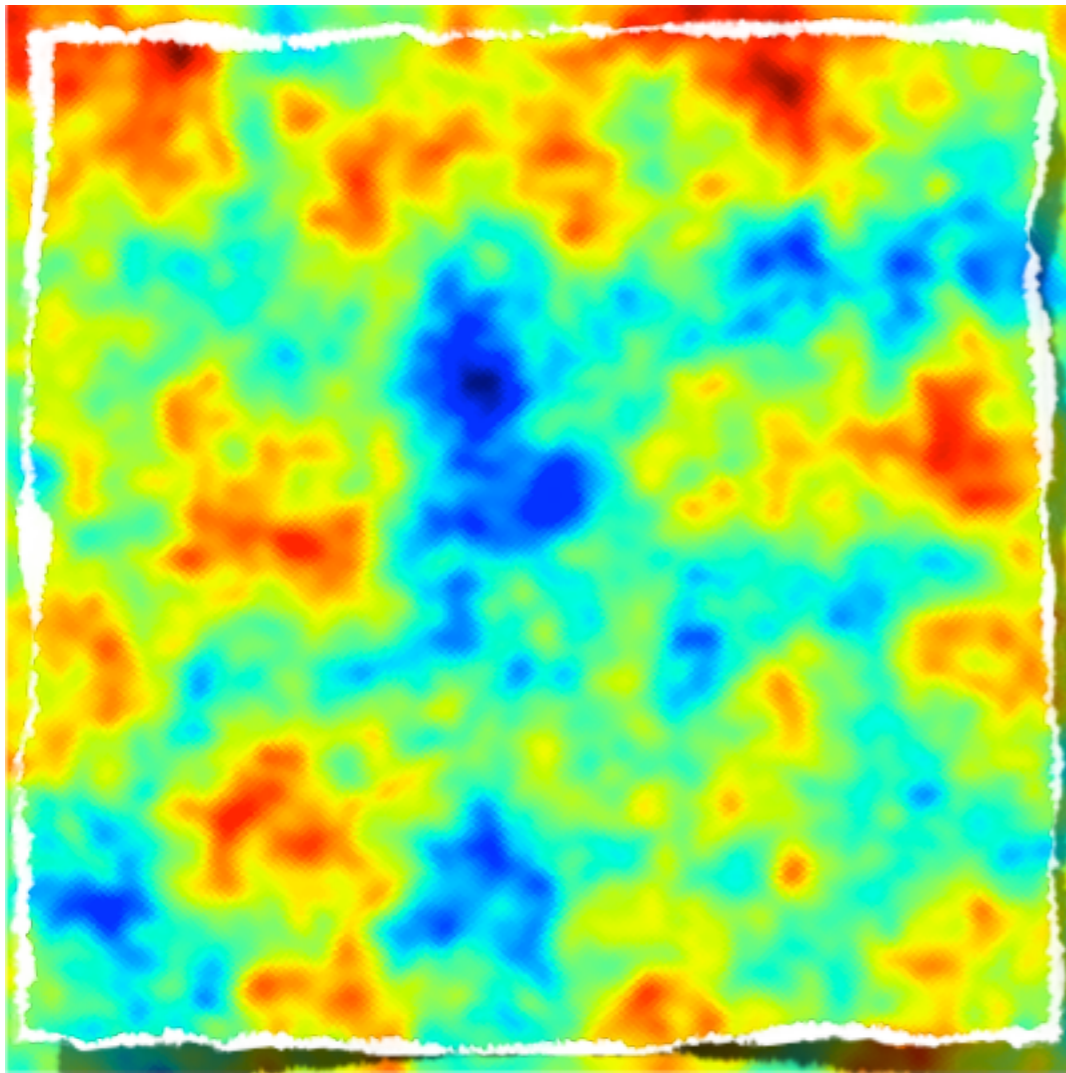


Lensed



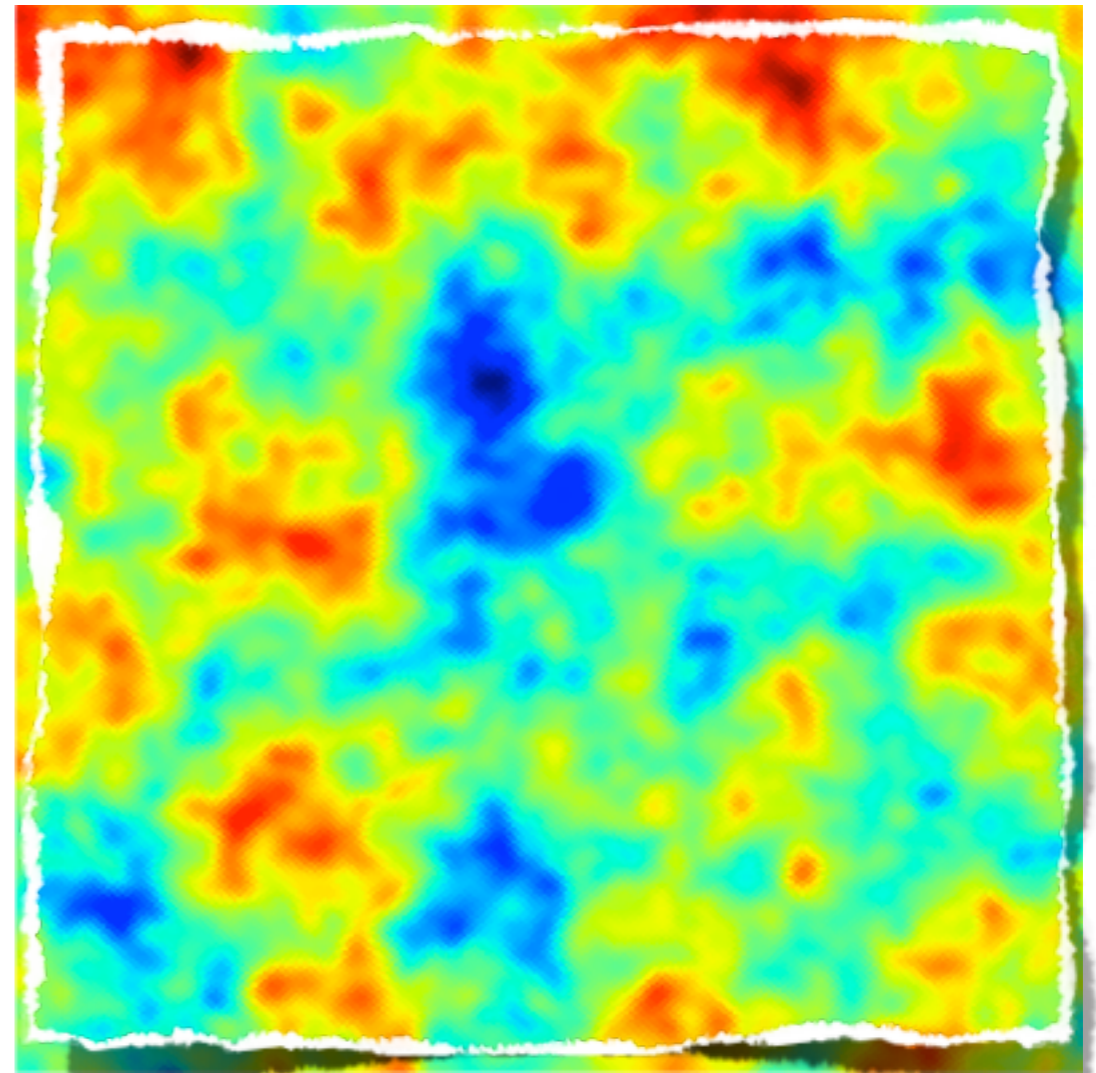
CMB lensing

Deflections are about 2 arcmin



Unlensed

6°

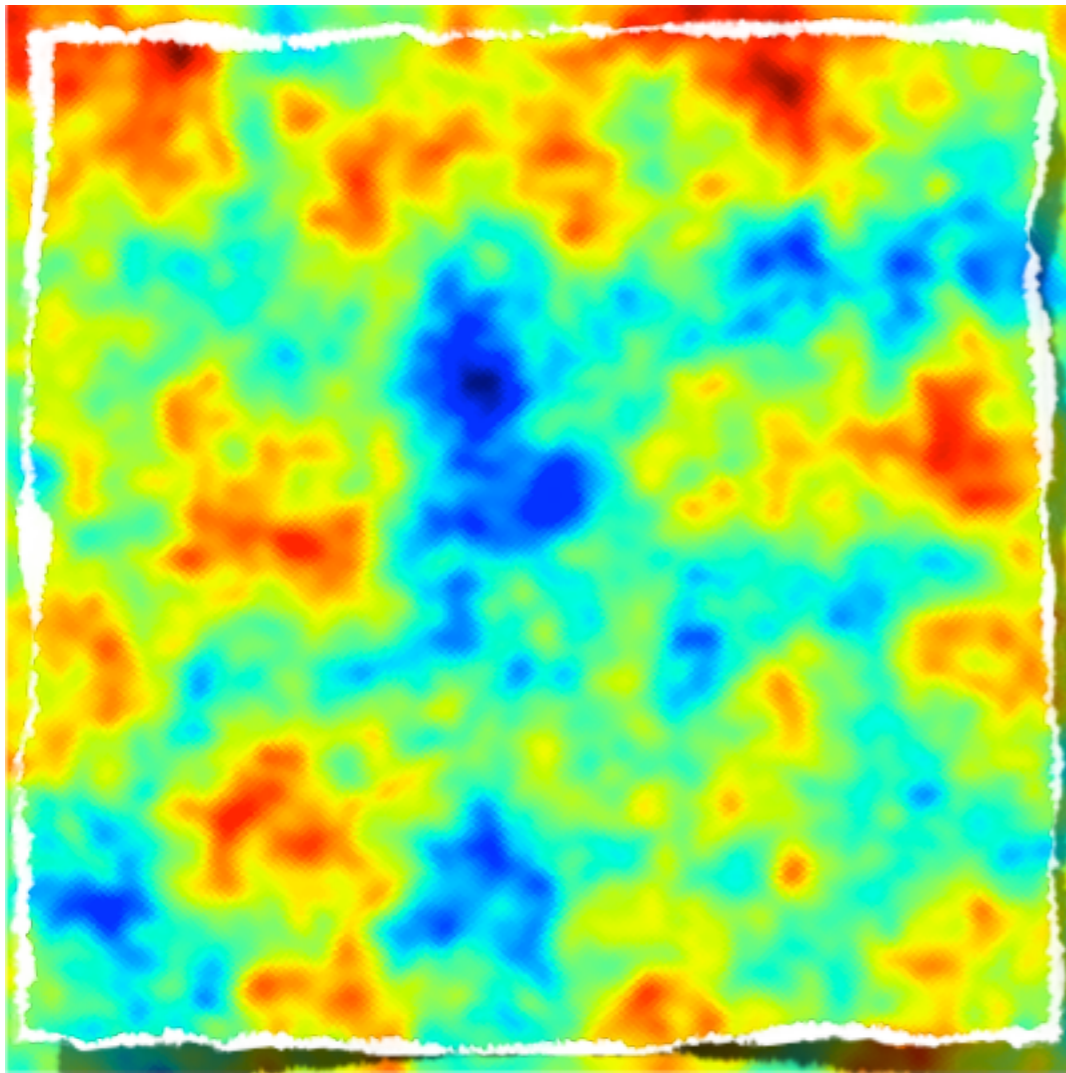


Unlensed



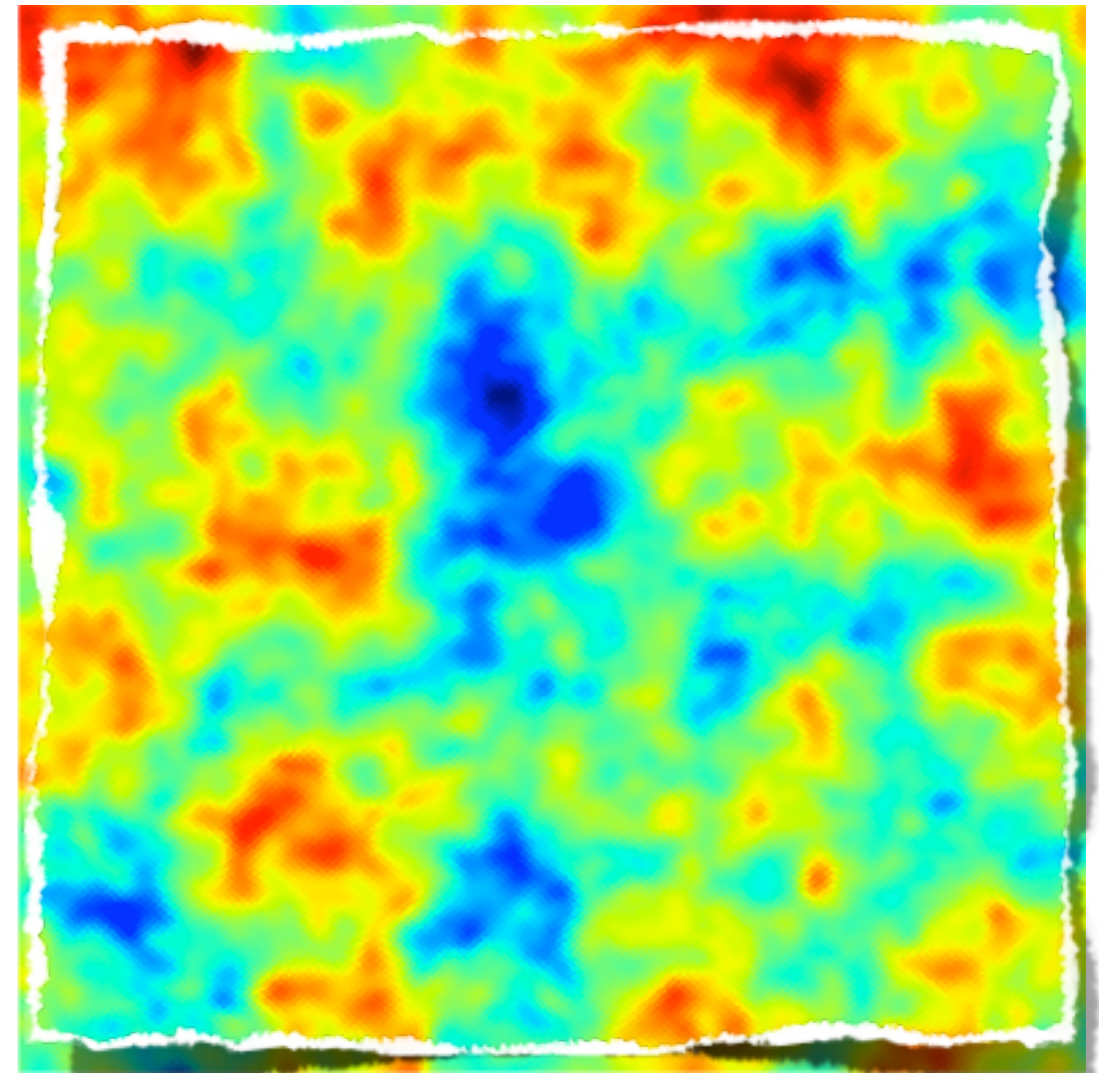
CMB lensing

Deflections are about 2 arcmin



Unlensed

6°

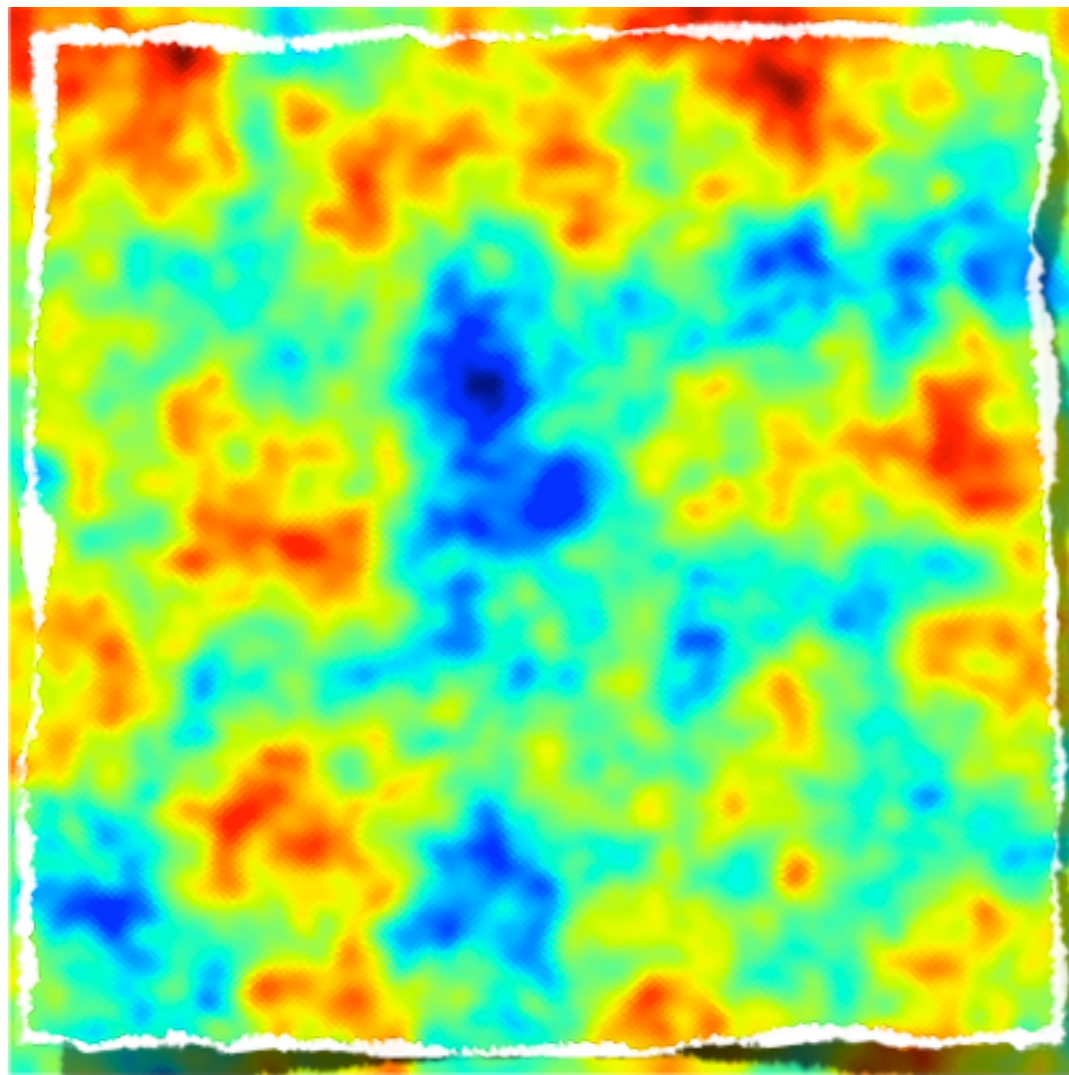


Lensed



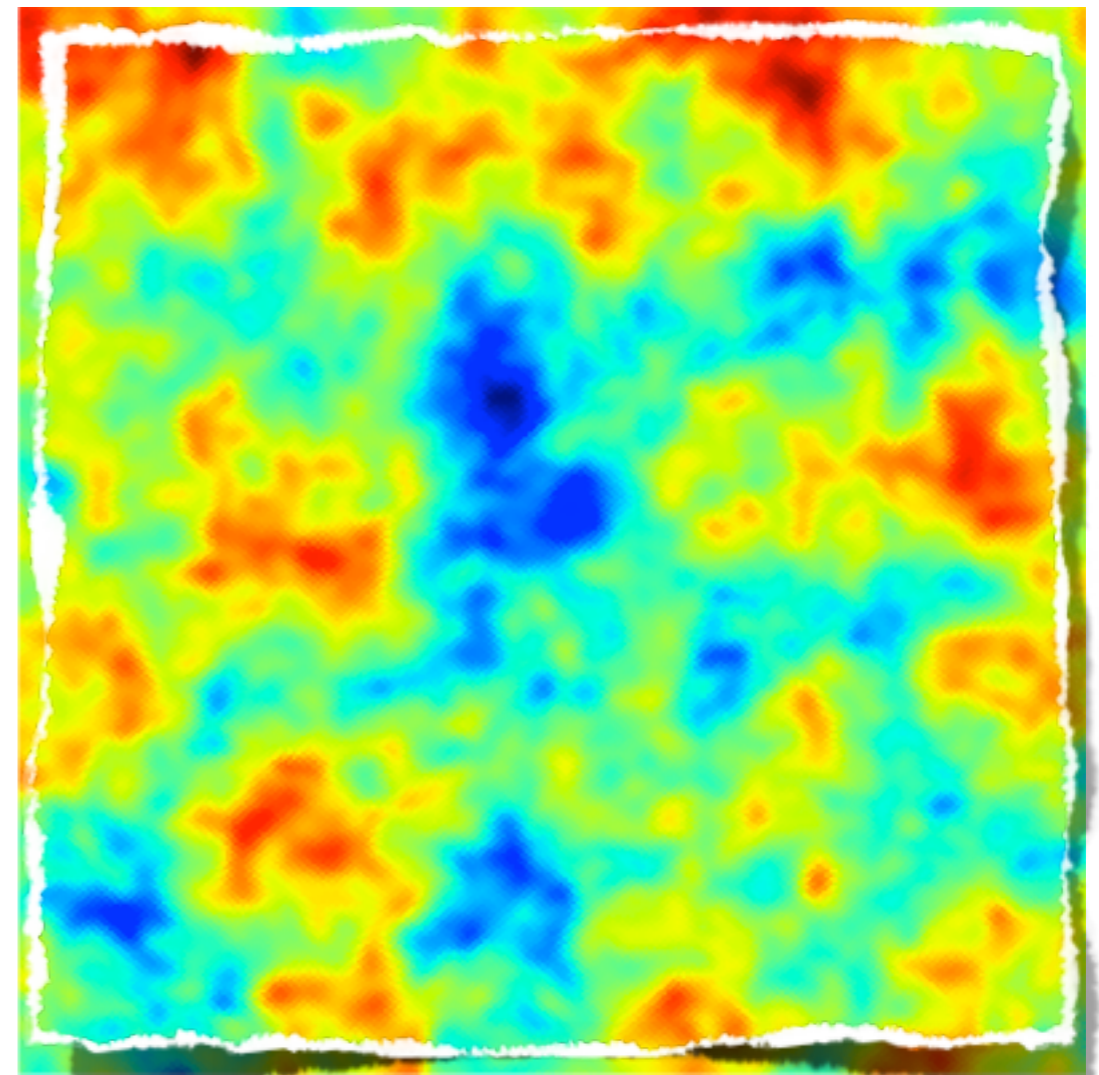
CMB lensing

Deflections are about 2 arcmin



Unlensed

6°



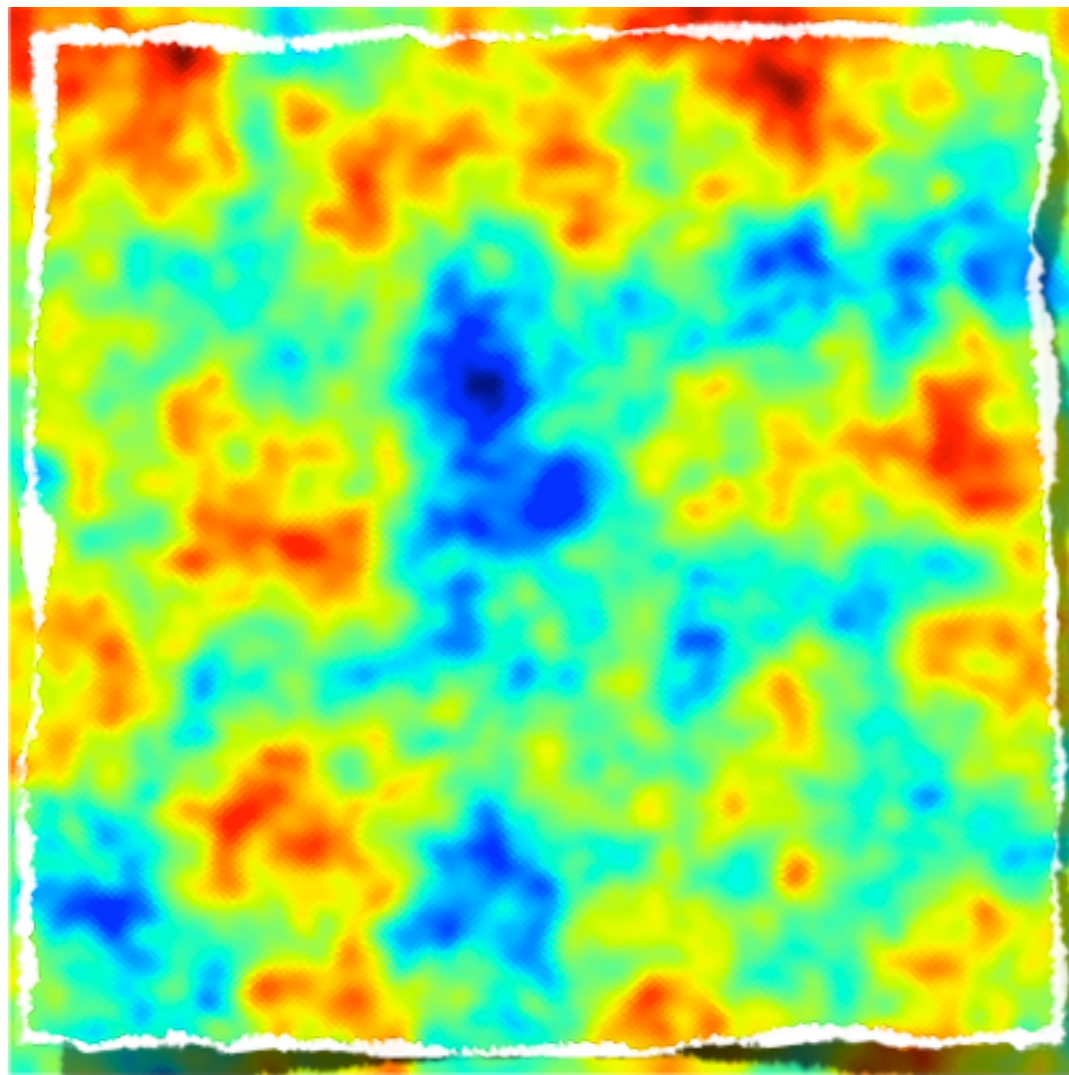
Lensed

Deflections are correlated on the degree scale



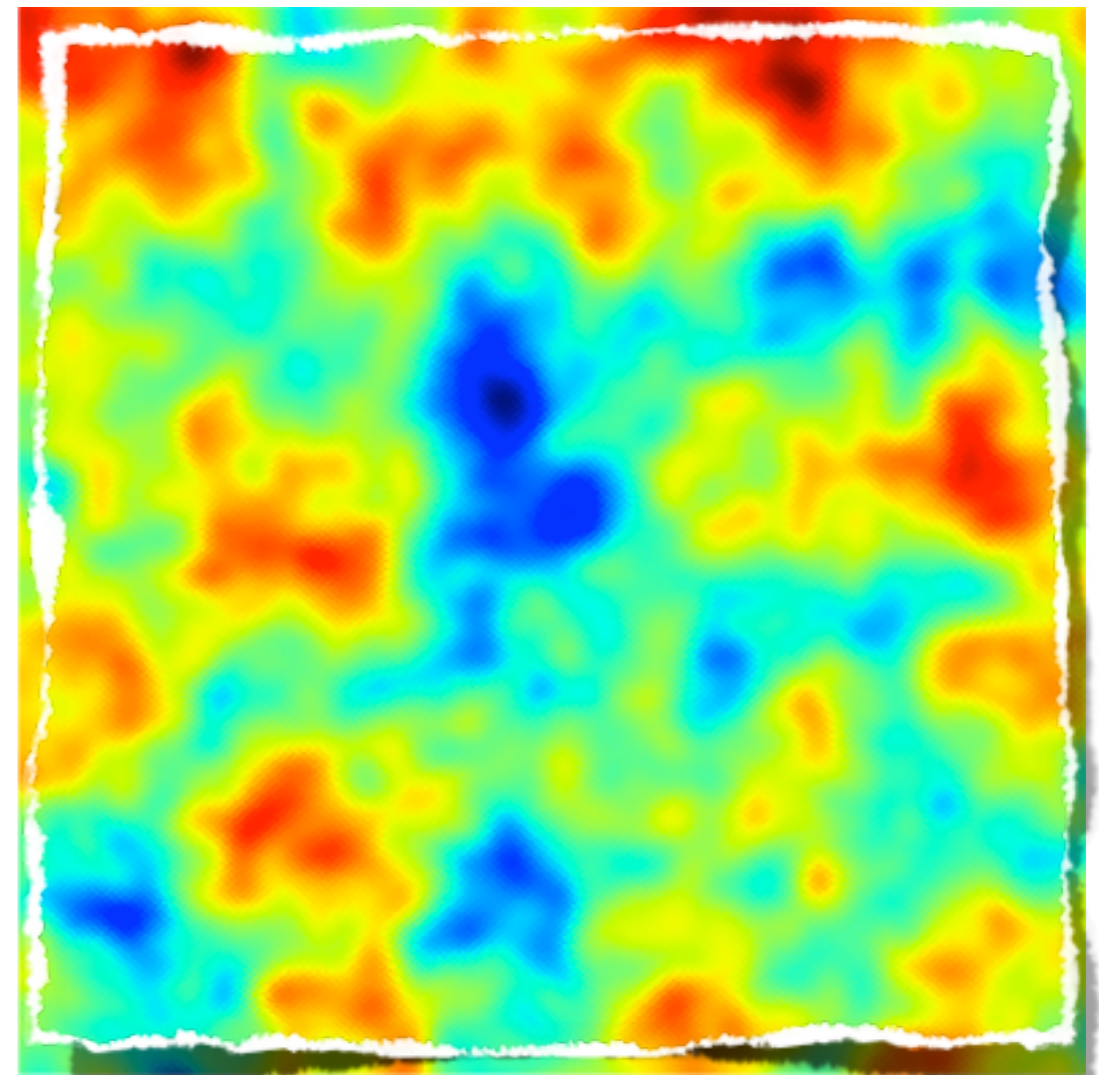
CMB lensing

Deflections are about 2 arcmin



Unlensed

6°



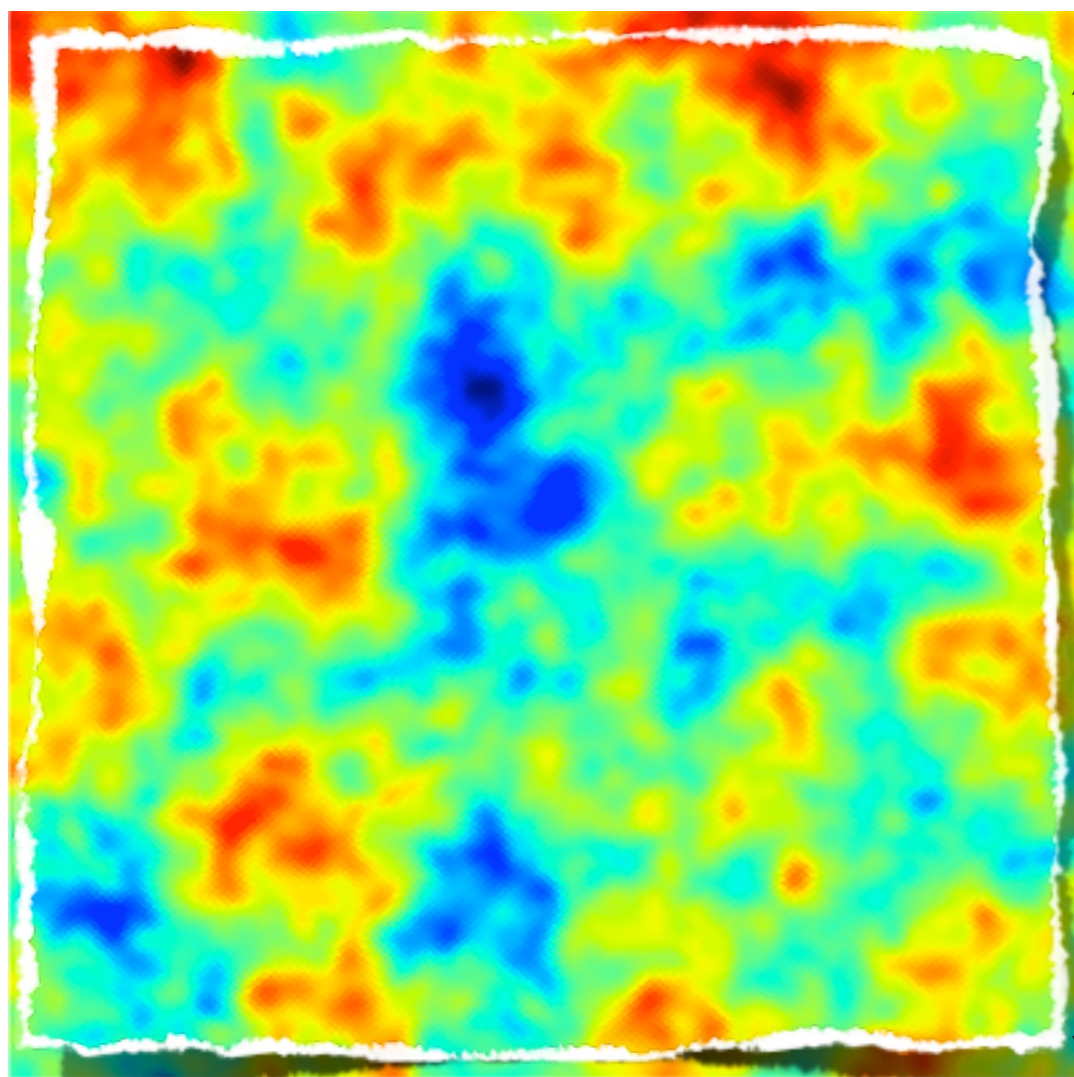
Lensed,
beamed

Deflections are correlated on the degree scale

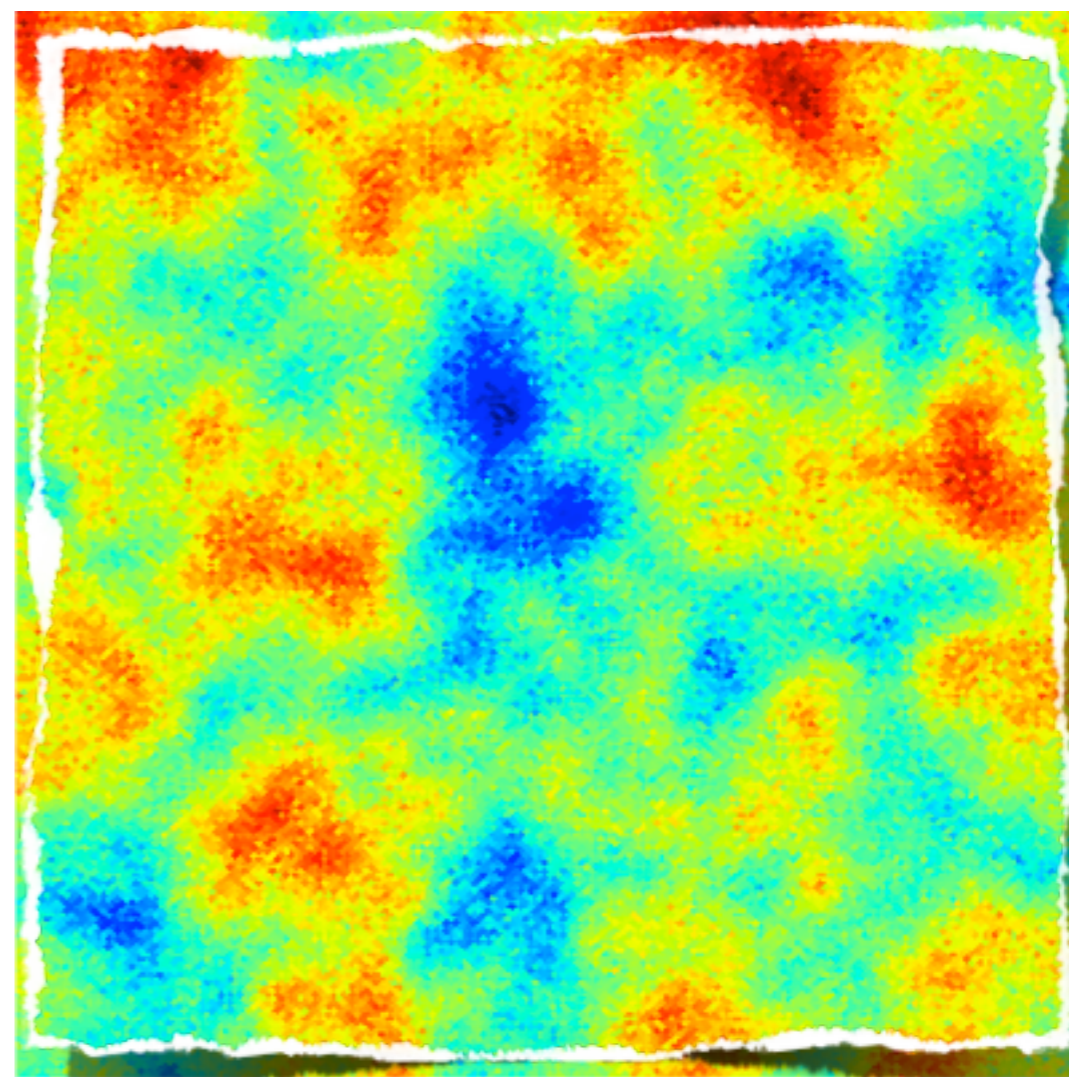


CMB lensing

Deflections are about 2 arcmin



Unlensed



Lensed,
beamed, noised

Deflections are correlated on the degree scale



Impact on CMB

- CMB lensing induces statistical anisotropies

$$\Delta \langle T_{\ell_1 m_1} T_{\ell_2 m_2} \rangle = \sum_{LM} \sum_{\ell_1 m_1, \ell_2 m_2} (-1)^M \begin{pmatrix} \ell_1 & \ell_2 & L \\ m_1 & m_2 & -M \end{pmatrix} W_{\ell_1 \ell_2 L}^\phi \phi_{LM},$$

**Lensing can also be detected in TT
~10 sigma with Planck2013**

- Quadratic estimator (Hu & Okamoto)

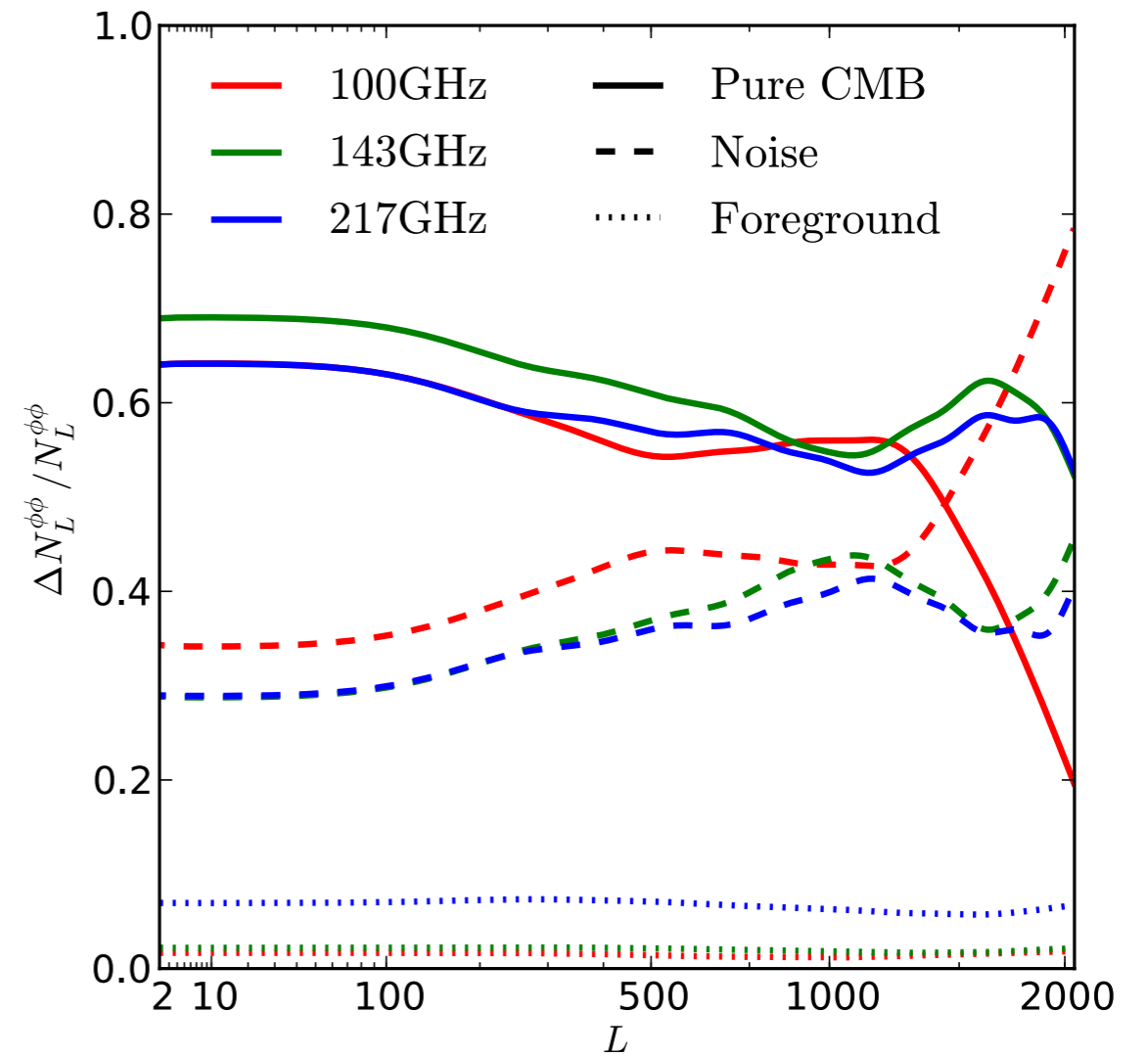
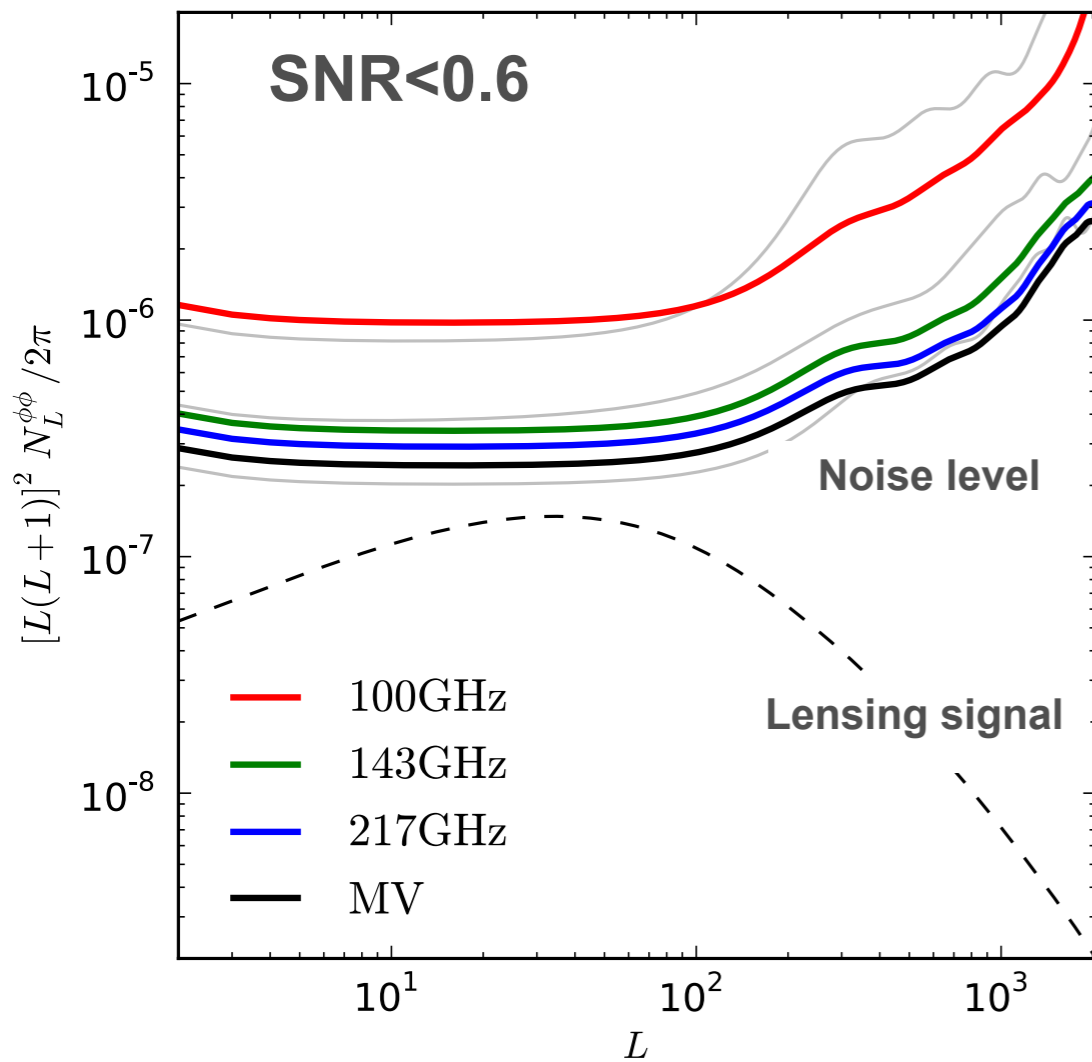
$$\bar{x}_{LM} = \frac{1}{2} \sum_{\ell_1 m_1, \ell_2 m_2} (-1)^M \begin{pmatrix} \ell_1 & \ell_2 & L \\ m_1 & m_2 & -M \end{pmatrix} W_{\ell_1 \ell_2 L}^x \bar{T}_{\ell_1 m_1}^{(1)} \bar{T}_{\ell_2 m_2}^{(2)}.$$

$$W_{\ell_1 \ell_2 L}^\phi = -\sqrt{\frac{(2\ell_1 + 1)(2\ell_2 + 1)(2L + 1)}{4\pi}} \sqrt{L(L + 1)\ell_1(\ell_1 + 1)} \\ \times C_{\ell_1}^{TT} \left(\frac{1 + (-1)^{\ell_1 + \ell_2 + L}}{2} \right) \begin{pmatrix} \ell_1 & \ell_2 & L \\ 1 & 0 & -1 \end{pmatrix} + (\ell_1 \leftrightarrow \ell_2). \quad (6)$$



CMB lensing reconstruction

■ Ideal Planck case

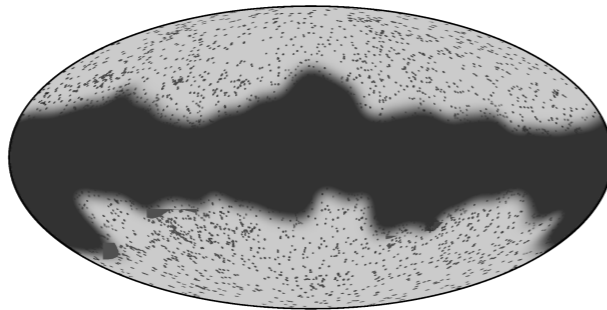




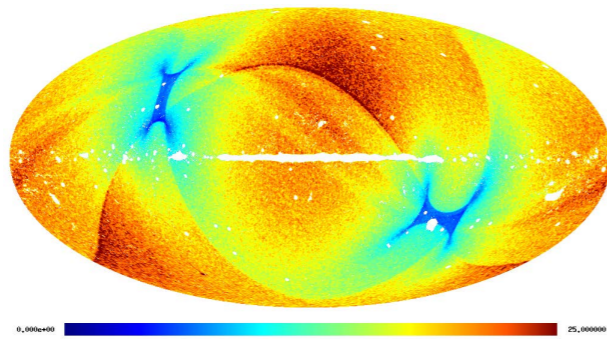
CMB lensing reconstruction

- Other sources of statistical anisotropies

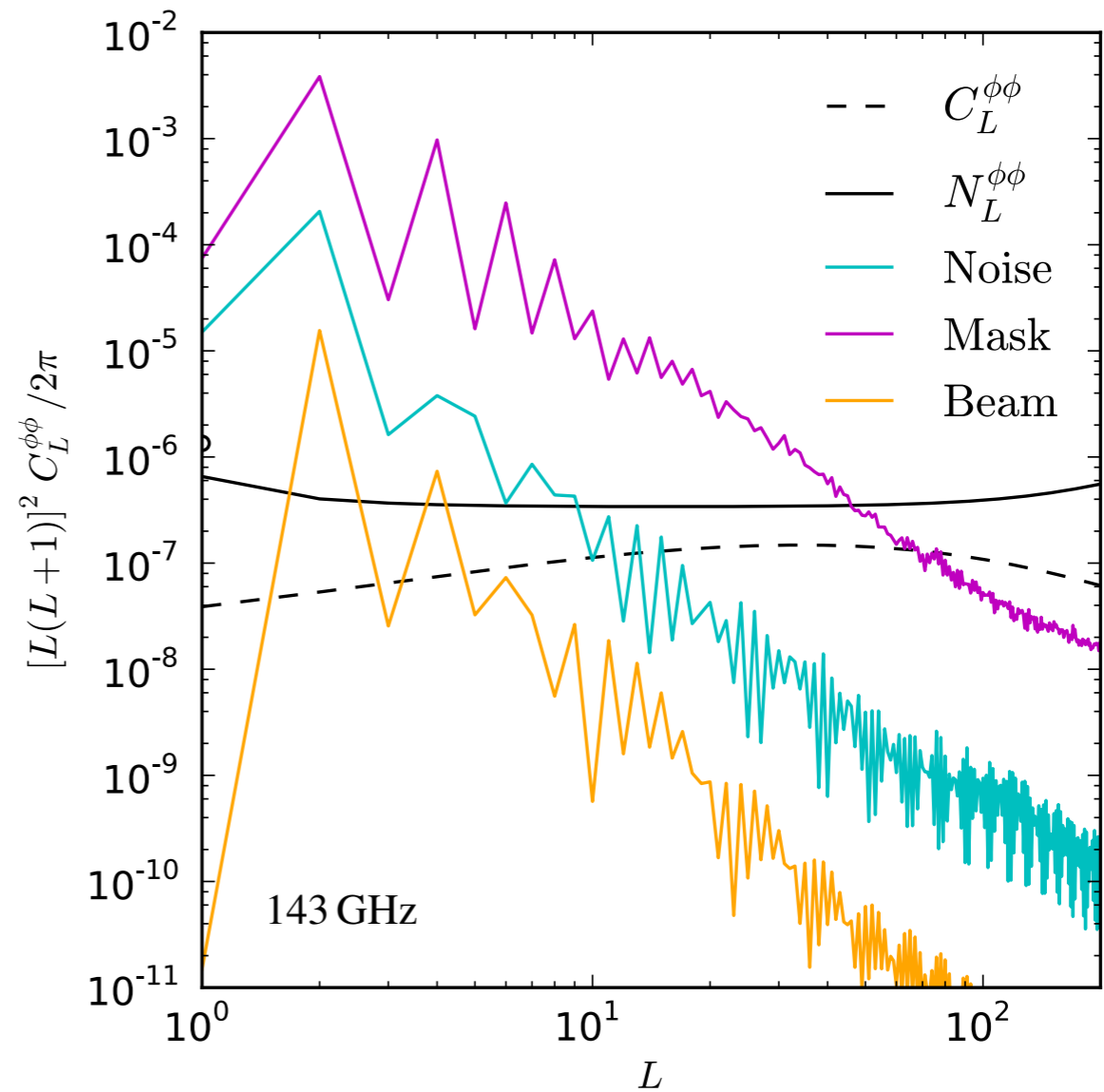
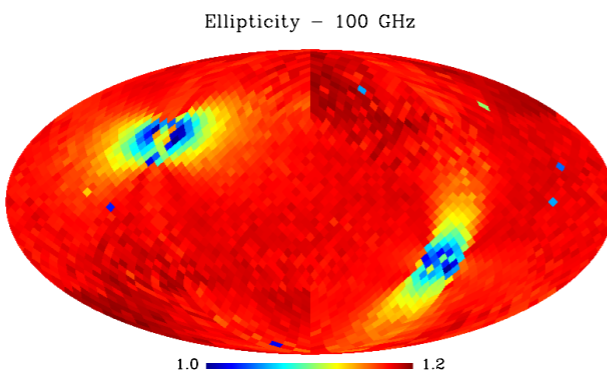
Galactic + PS mask



Inh. noise



Beam ellipticity





CMB lensing reconstruction

$$\hat{\phi}_{LM}^x = \frac{1}{\mathcal{R}_L^{x\phi}} \left(\bar{x}_{LM} - \bar{x}_{LM}^{MF} \right).$$

$$\bar{x}_{LM} = \frac{1}{2} \sum_{\ell_1 m_1, \ell_2 m_2} (-1)^M \begin{pmatrix} \ell_1 & \ell_2 & L \\ m_1 & m_2 & -M \end{pmatrix} W_{\ell_1 \ell_2 L}^x \langle \bar{T}_{\ell_1 m_1}^{(1)} \bar{T}_{\ell_2 m_2}^{(2)} \rangle.$$

$$\bar{\phi}_{\ell m} = [(C^{-1}T)\nabla(SC^{-1}T)]_{\ell m}$$

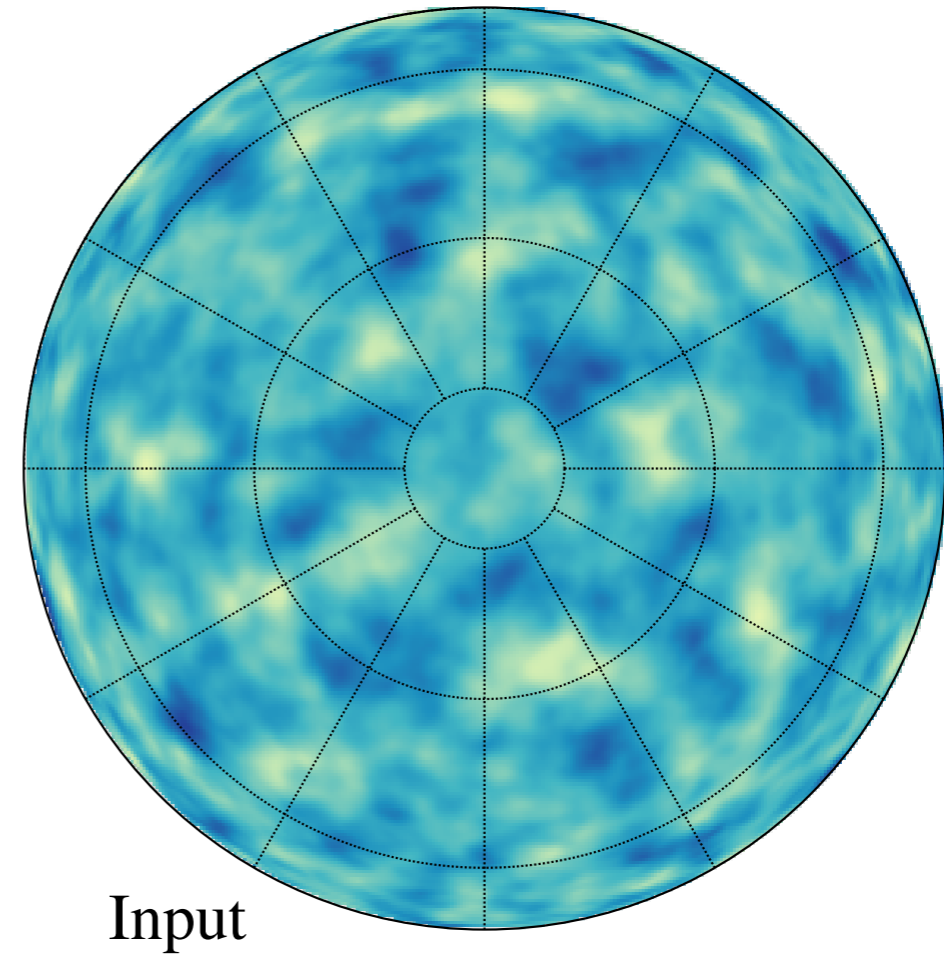
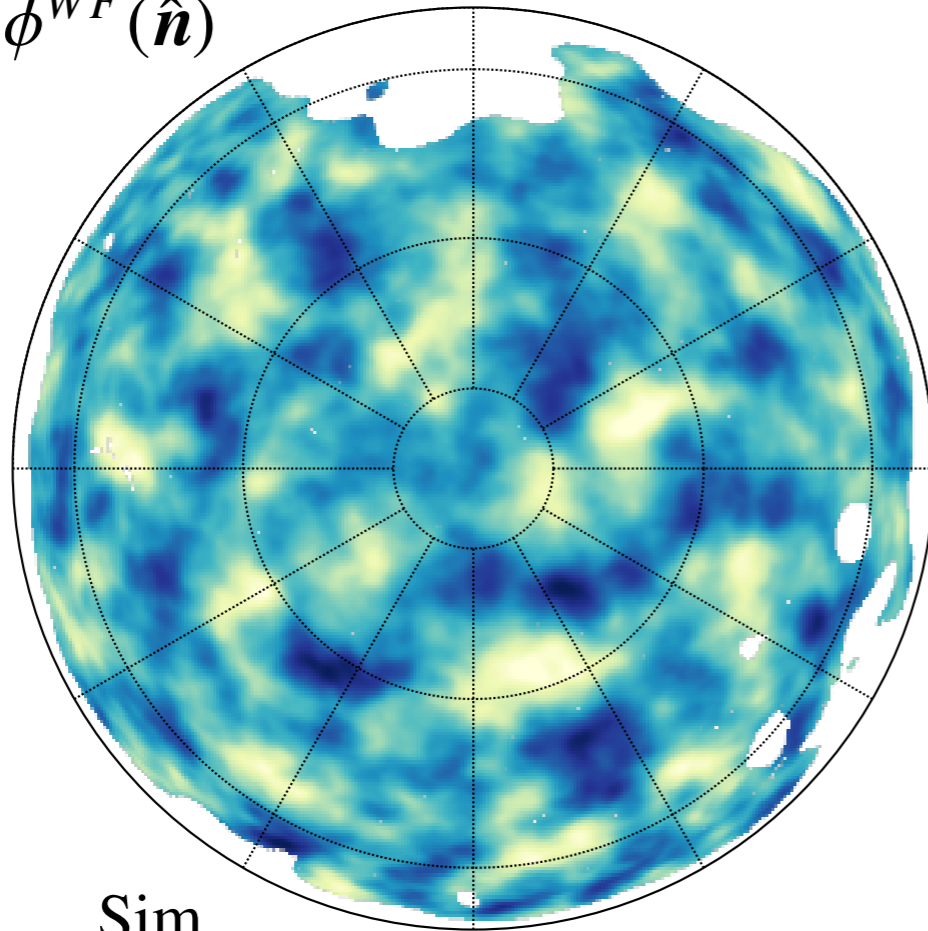
$$\bar{T}_{\ell m} = [S + N]^{-1} T_{\ell m} \approx [C_{\ell}^{TT} + C_{\ell}^{NN}]^{-1} T_{\ell m} = F_{\ell} T_{\ell m} \quad \mathcal{R}_L^{x\phi} = \frac{1}{(2L+1)} \sum_{\ell_1 \ell_2} \frac{1}{2} W_{\ell_1 \ell_2 L}^x W_{\ell_1 \ell_2 L}^{\phi} F_{\ell_1}^{(1)} F_{\ell_2}^{(2)}.$$

- Take two temperature maps and inverse-variance filter them
- Multiply one by the temperature power spectrum and differentiate it
- Multiply it with the first filtered map
- Do the same on a set of realistic simulations
- Take the difference and normalize to get unbiased estimator



CMB lensing reconstruction

$$\phi^{WF}(\hat{n})$$

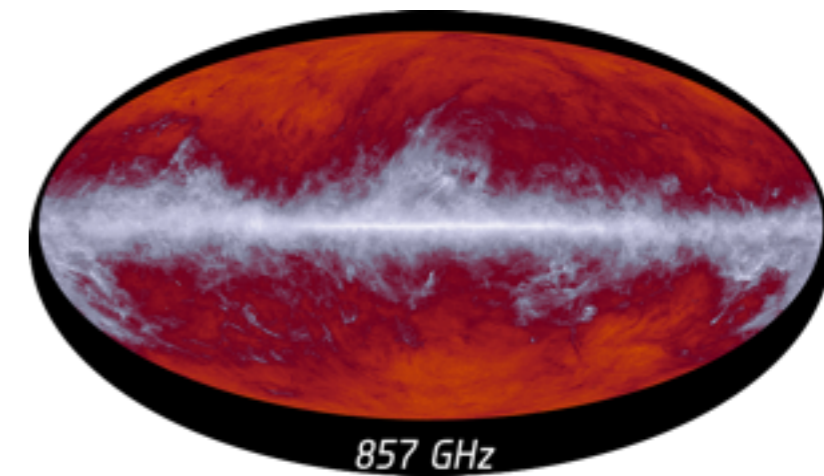
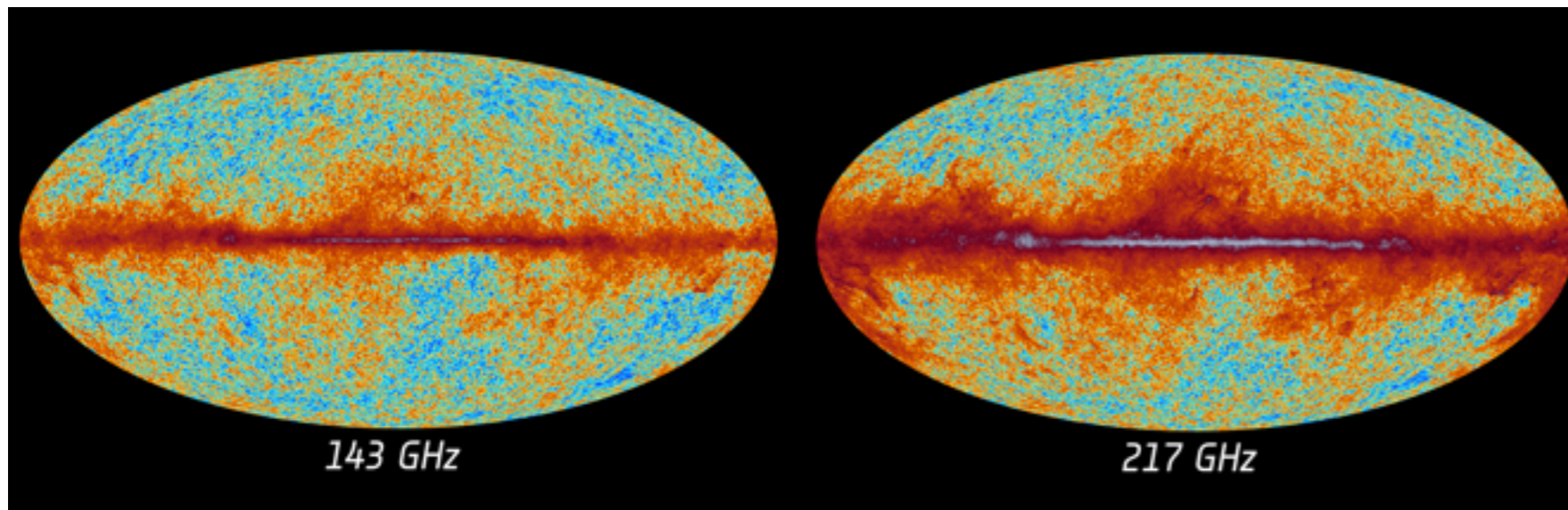


Reconstruction on a realistic Planck simulation



Best reconstruction

- Minimum-variance combination of 143GHz & 217 GHz

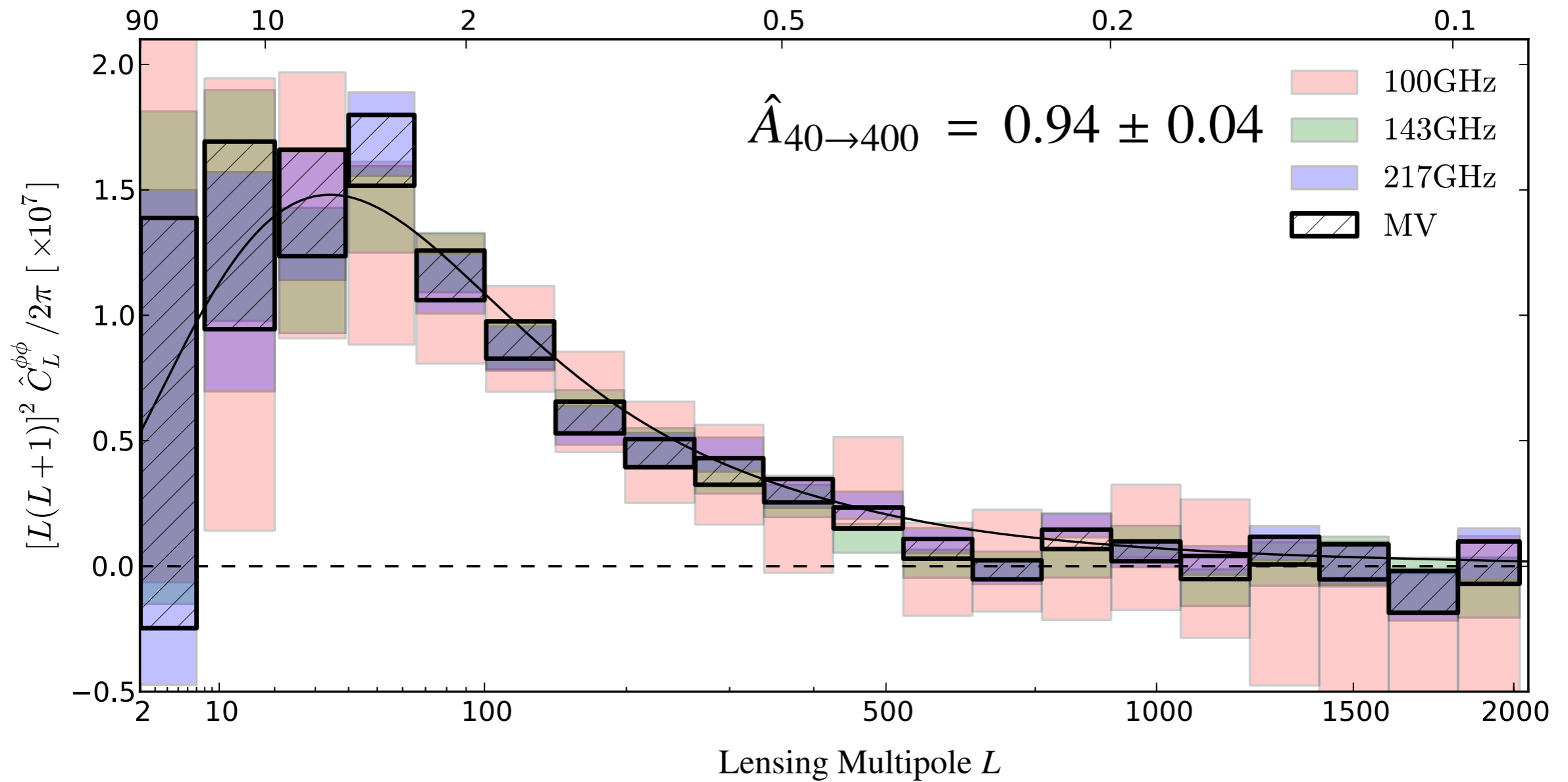


- 857 GHz map used as a template for dust cleaning
- 30 % Galactic mask +CO+ point sources
- 5° apodization (for lensing power spectrum estimation)



Best reconstruction

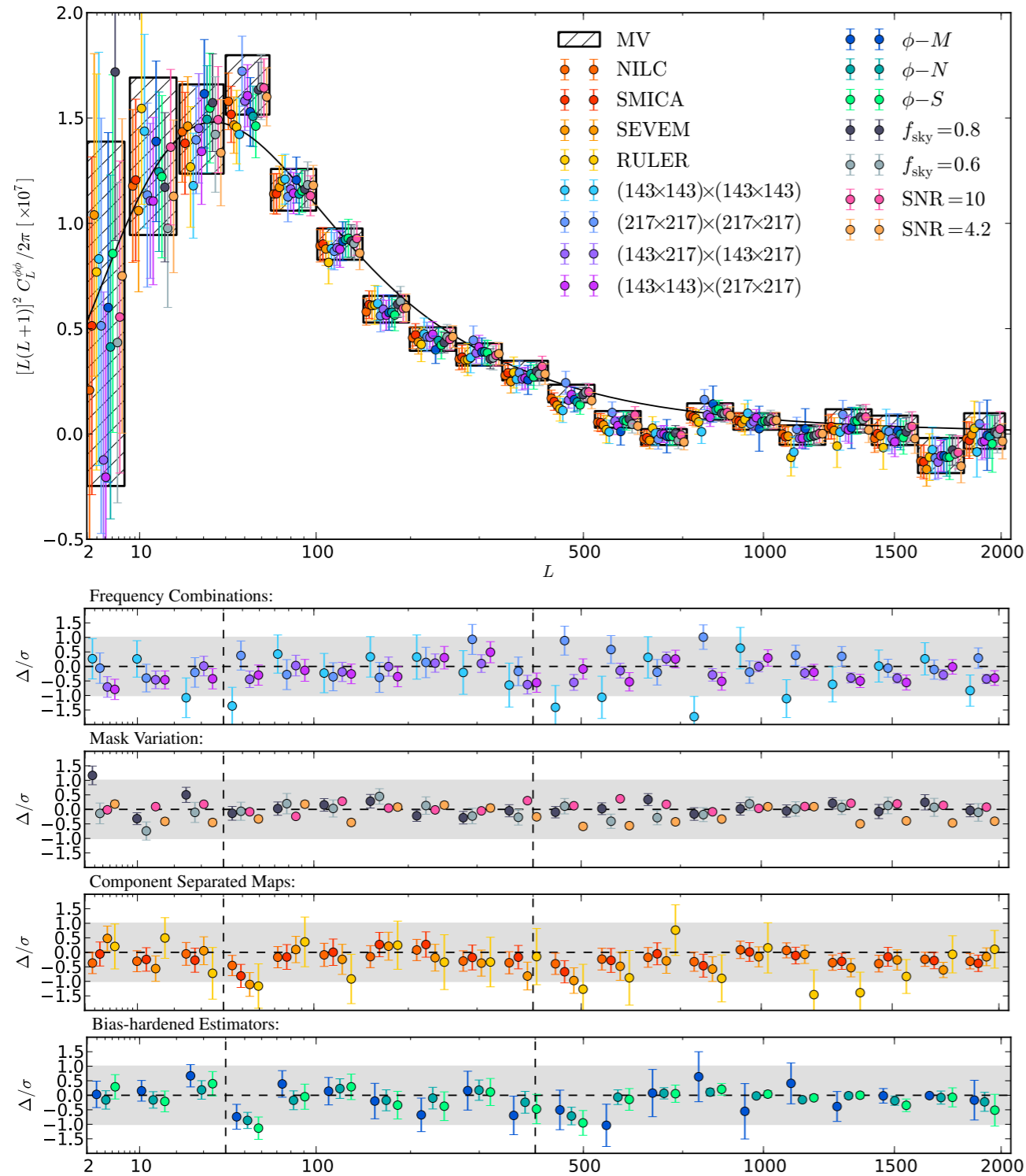
Angular Scale [deg.]



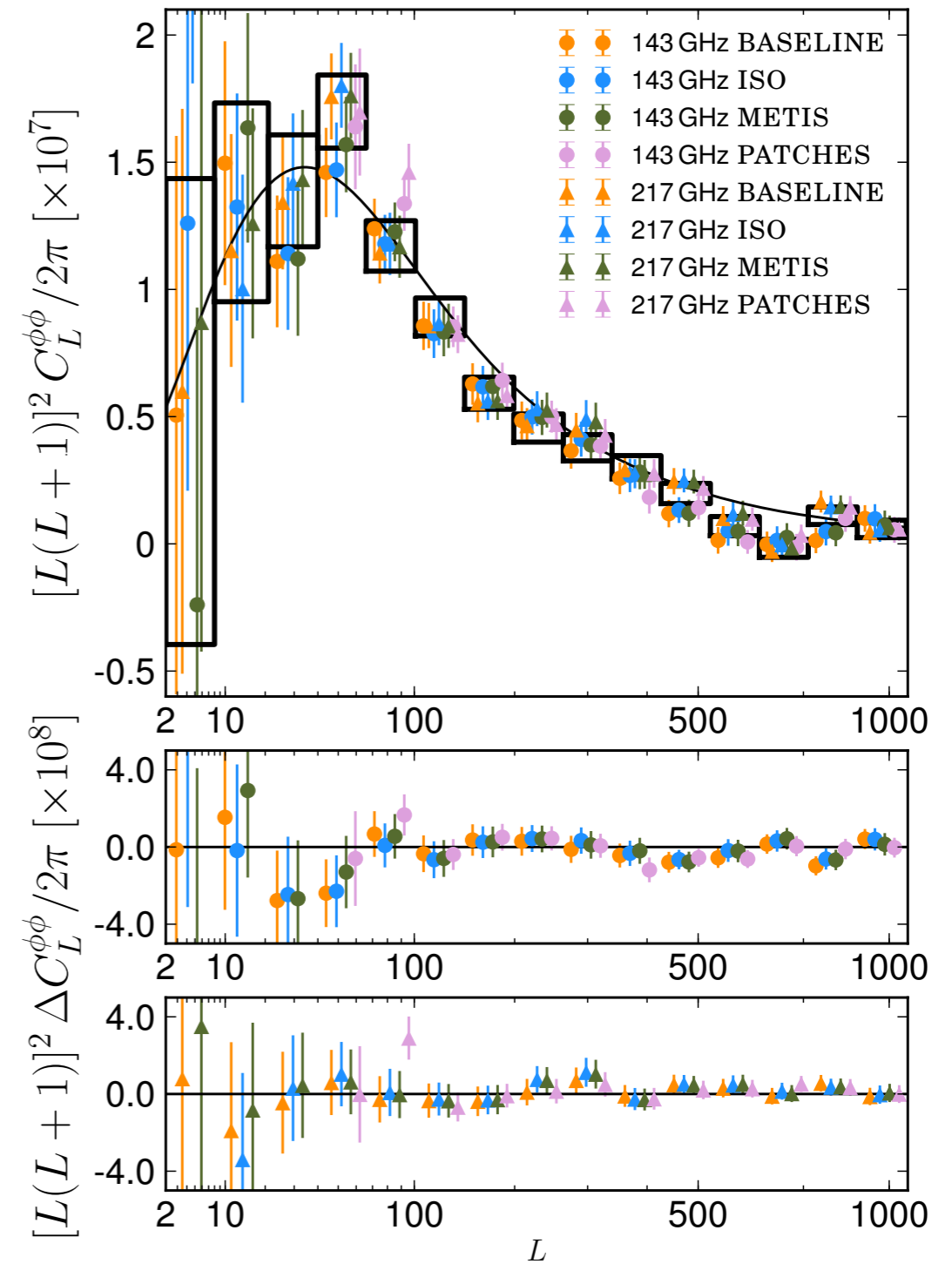


Tests

Testing foreground contamination

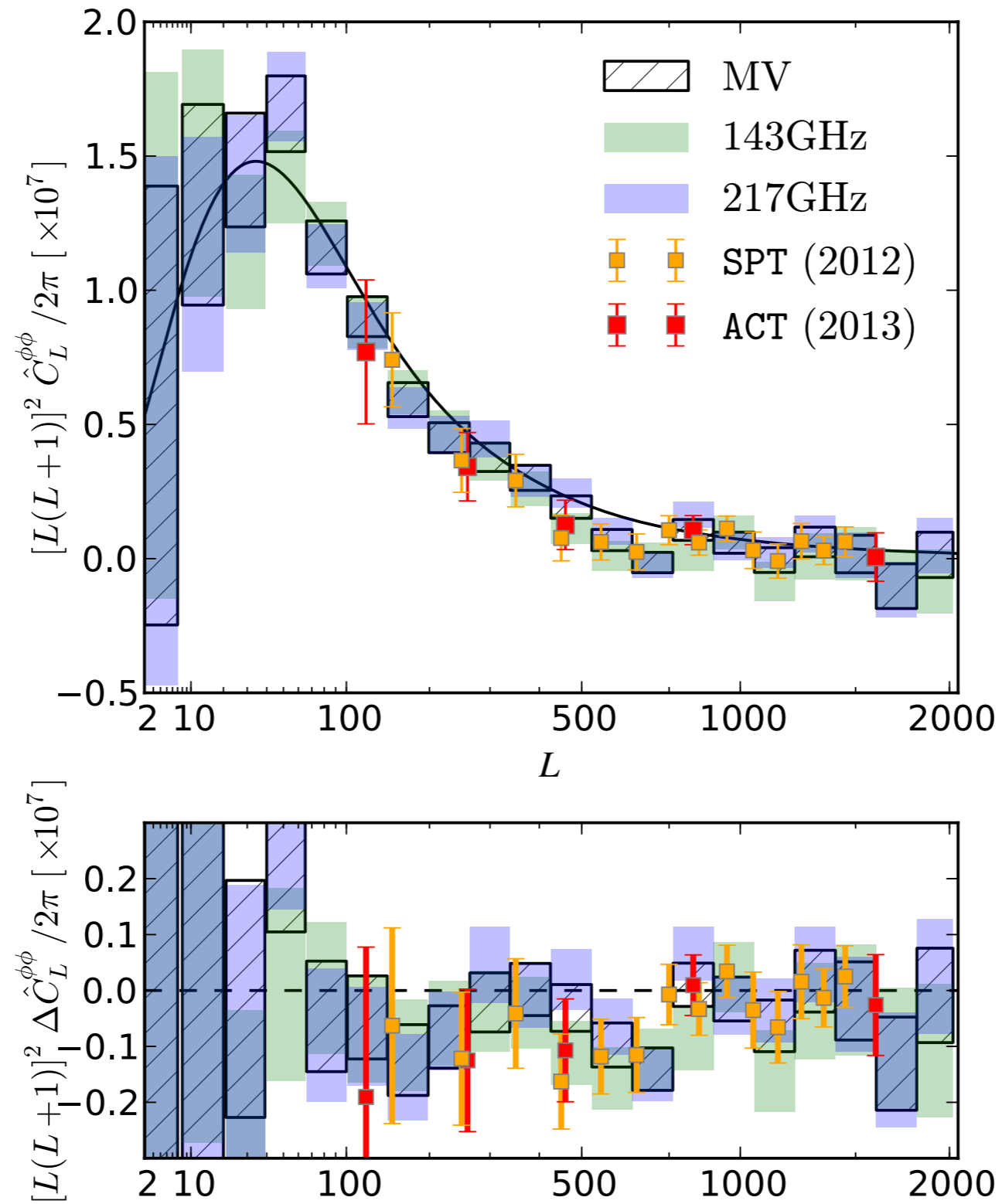


Testing the filter & implementation



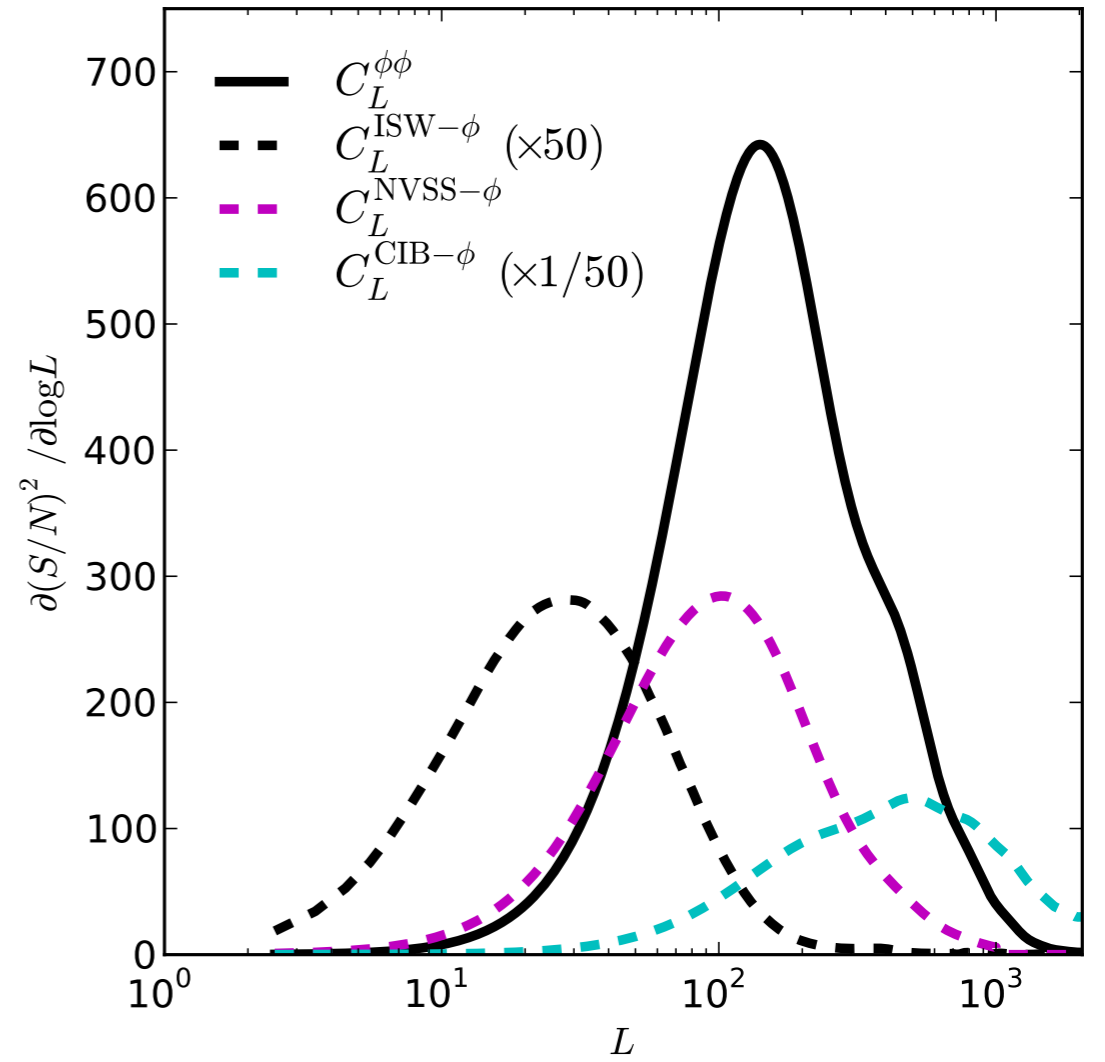
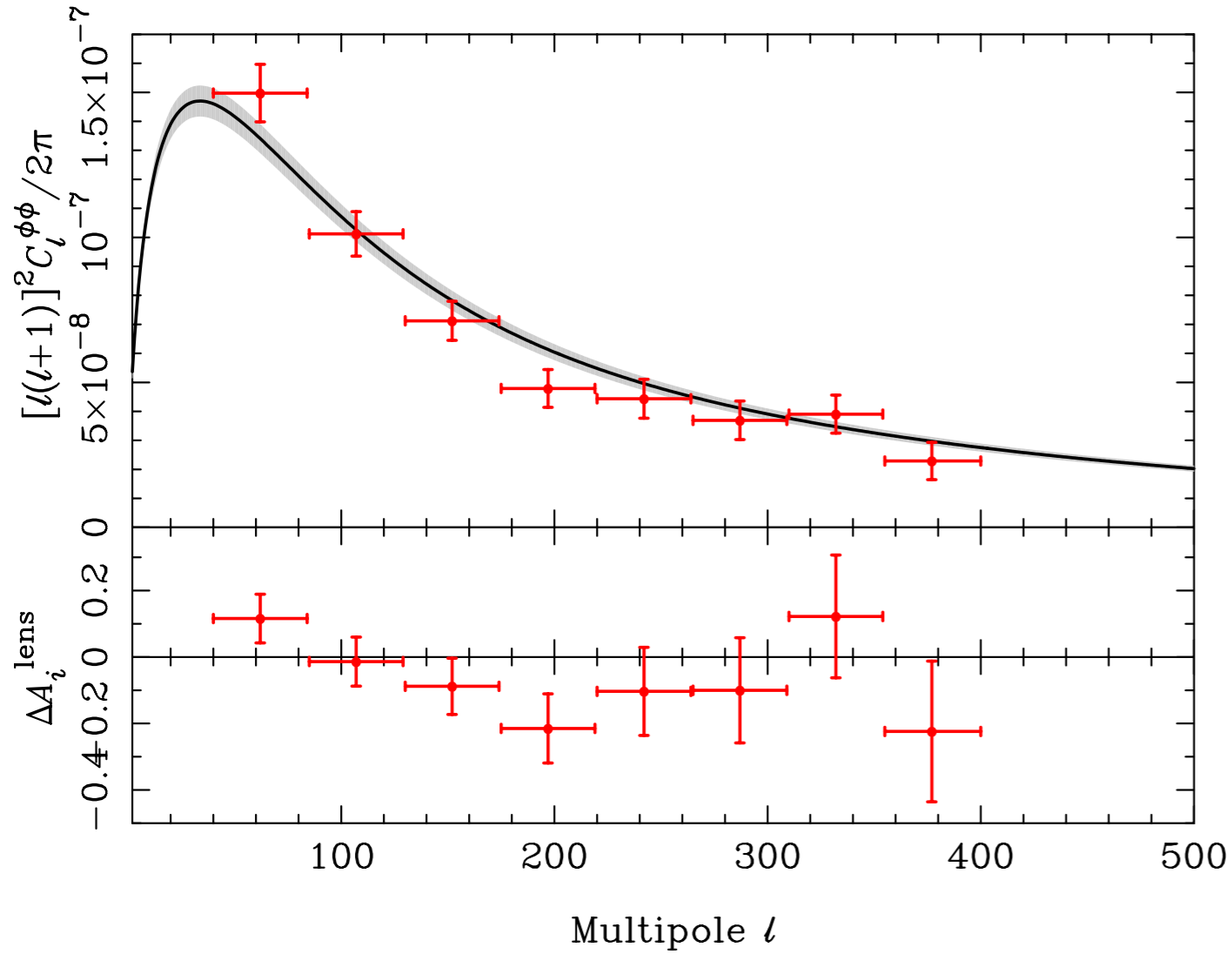


Comparison to other surveys



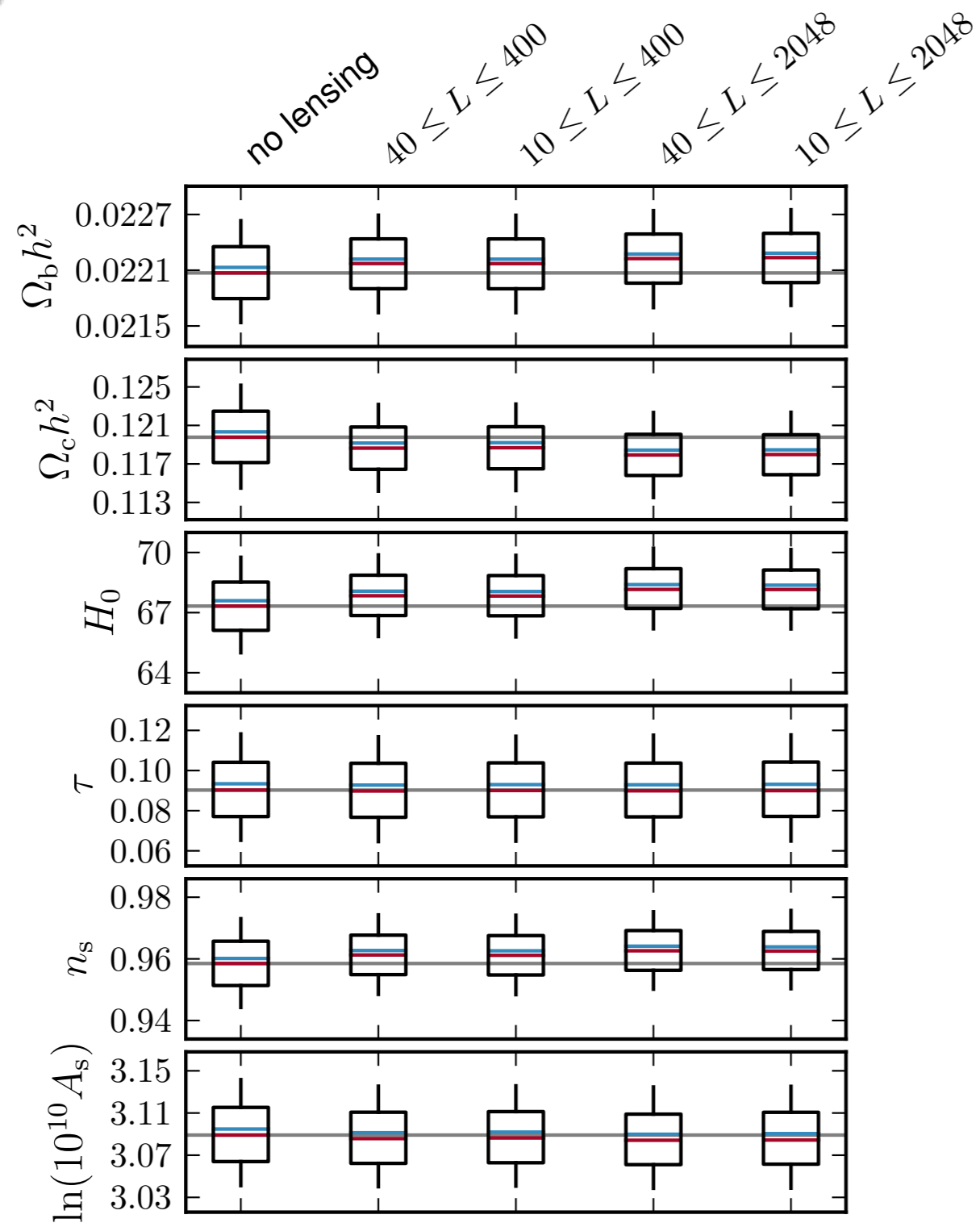


Cosmology





Cosmology



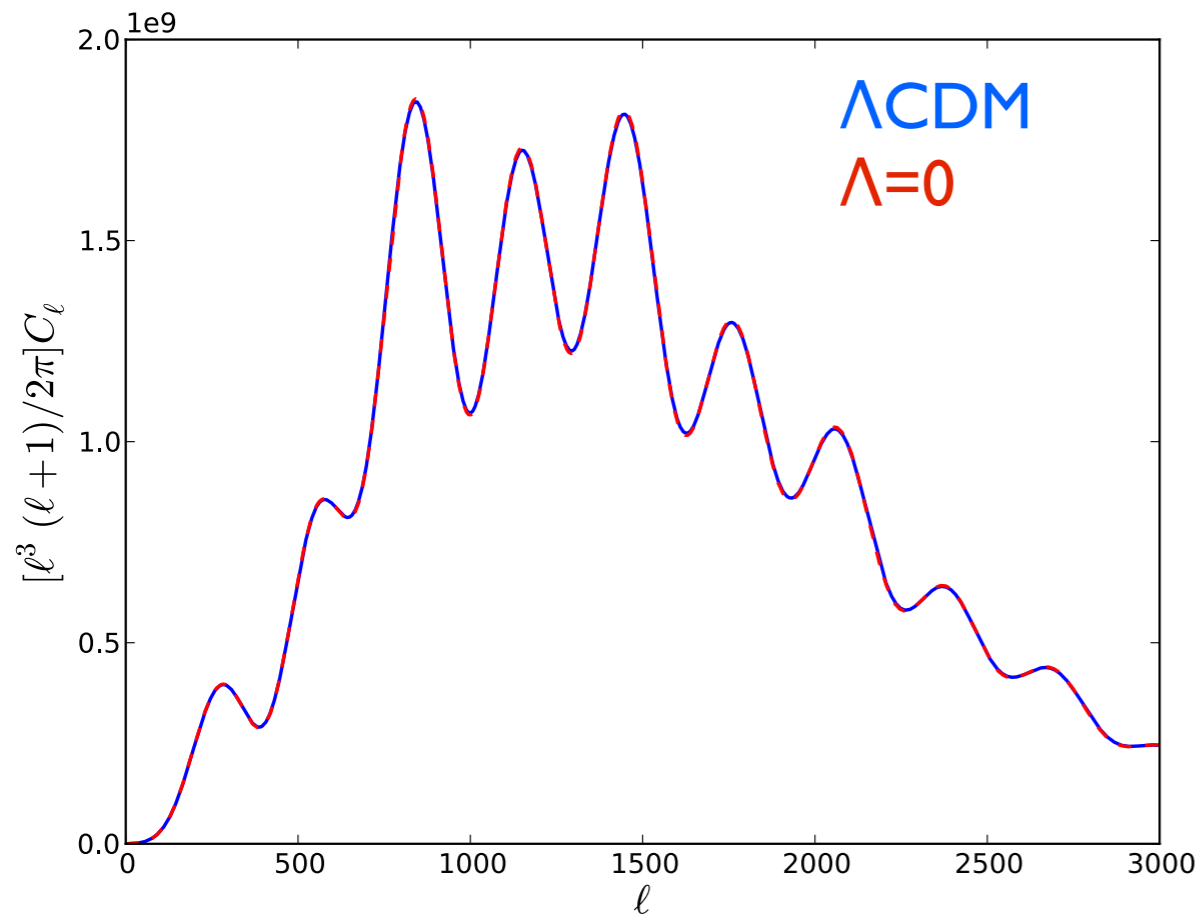
**Adding lensing reconstruction brings
~20% improvement on some parameters**

**Adding low-L and high-L lensing
information does not improve precision
but slightly shift central values**

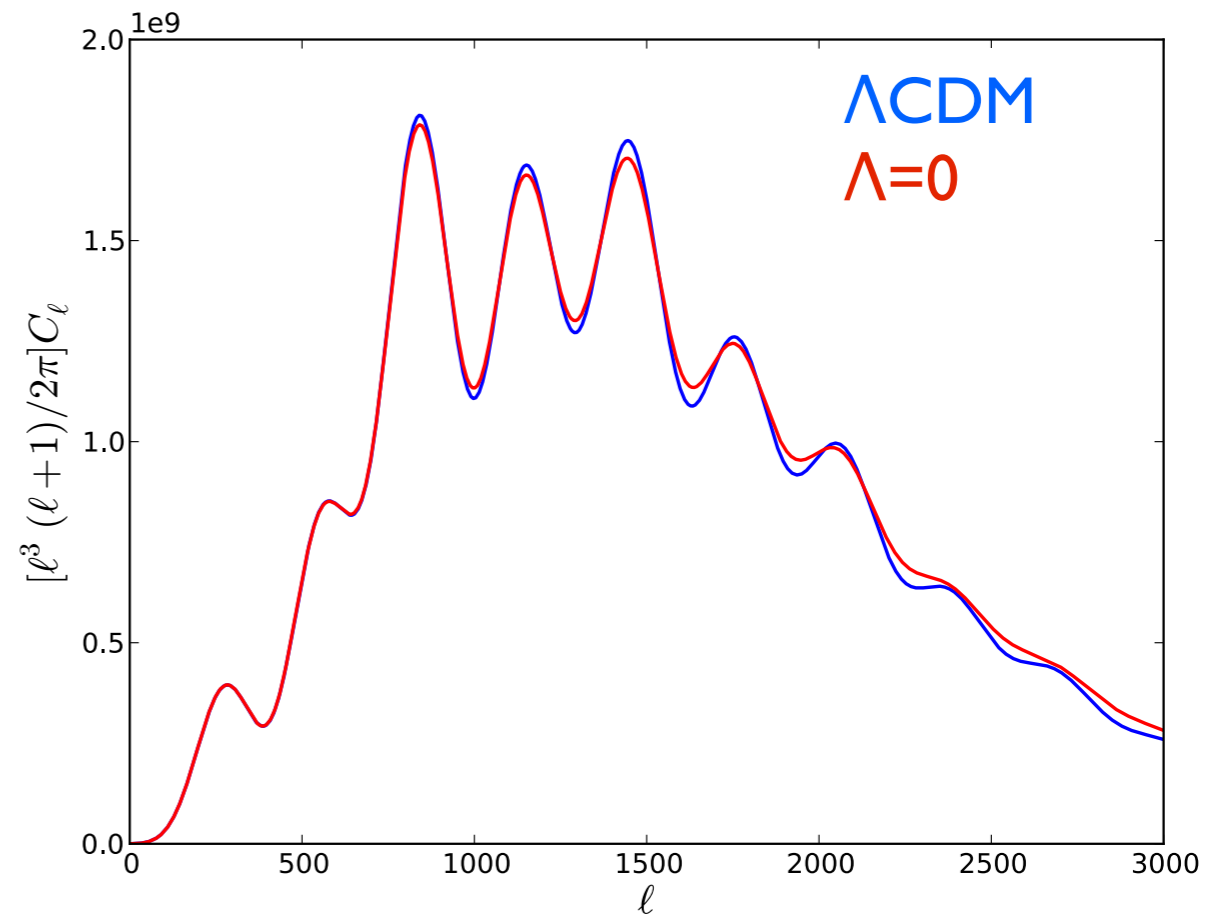


Cosmology

- CMB lensing break the angular diameter degeneracy



Unlensed TT



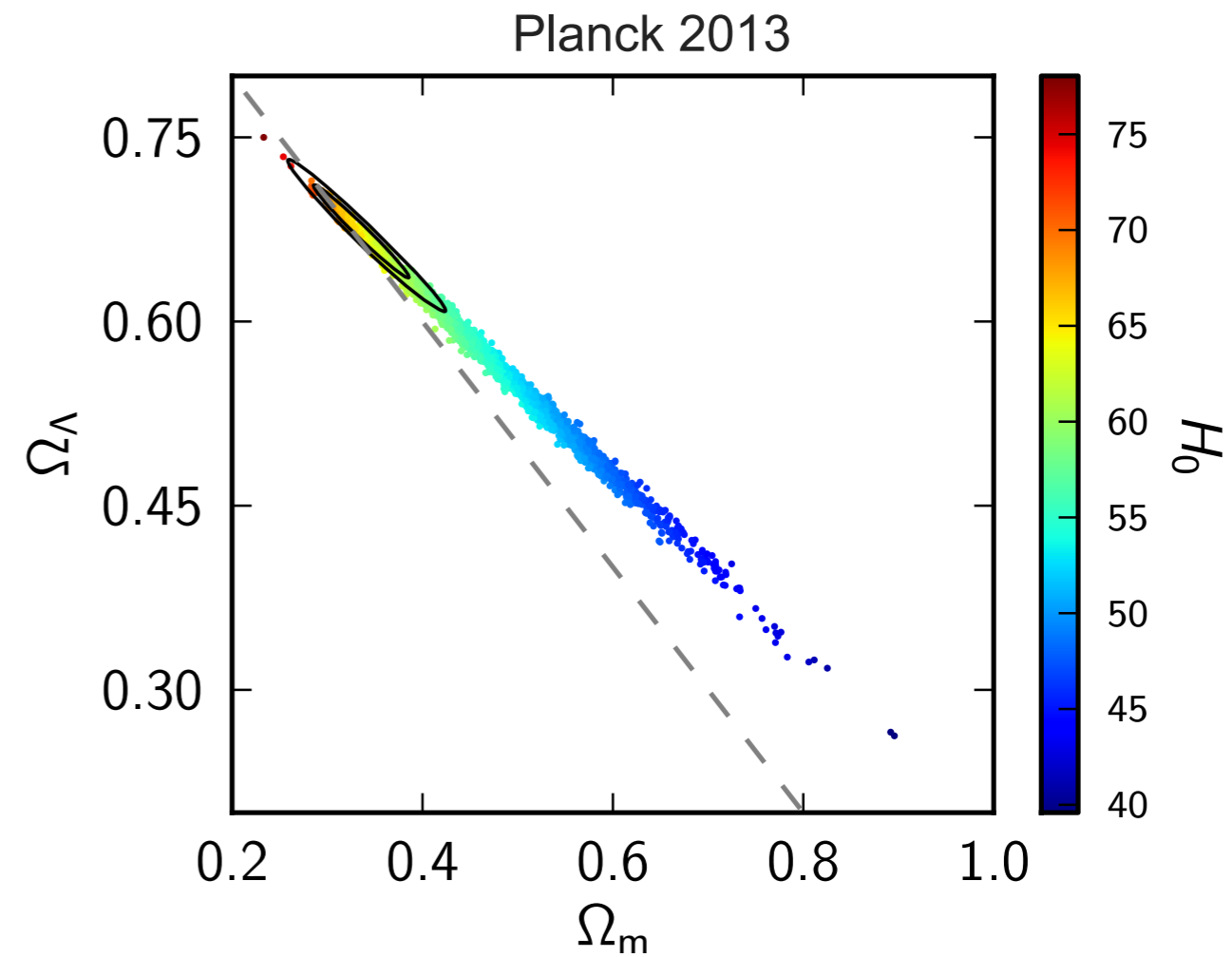
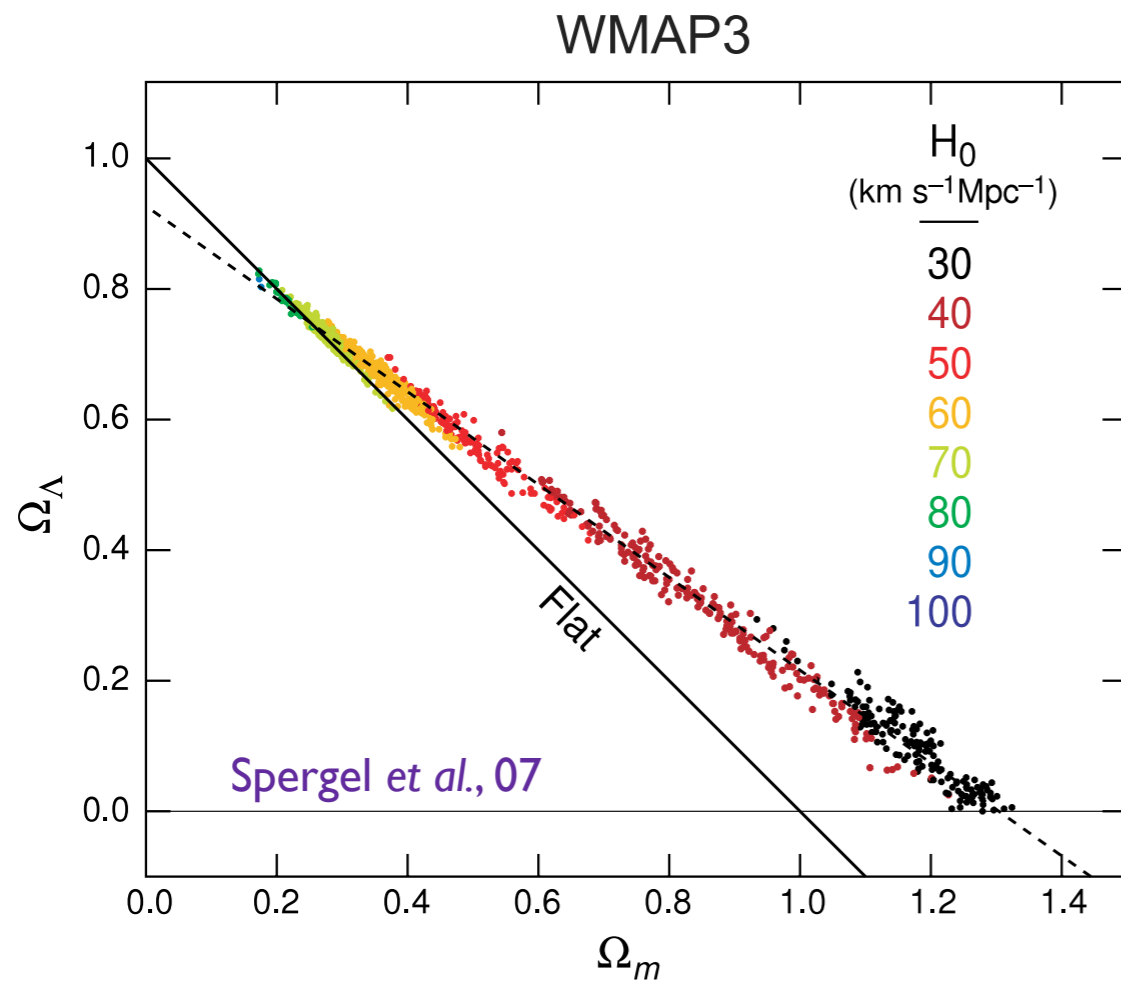
Lensed TT

See also [Sherwin *et al.*, 11 \(ACT\)](#)



Cosmology

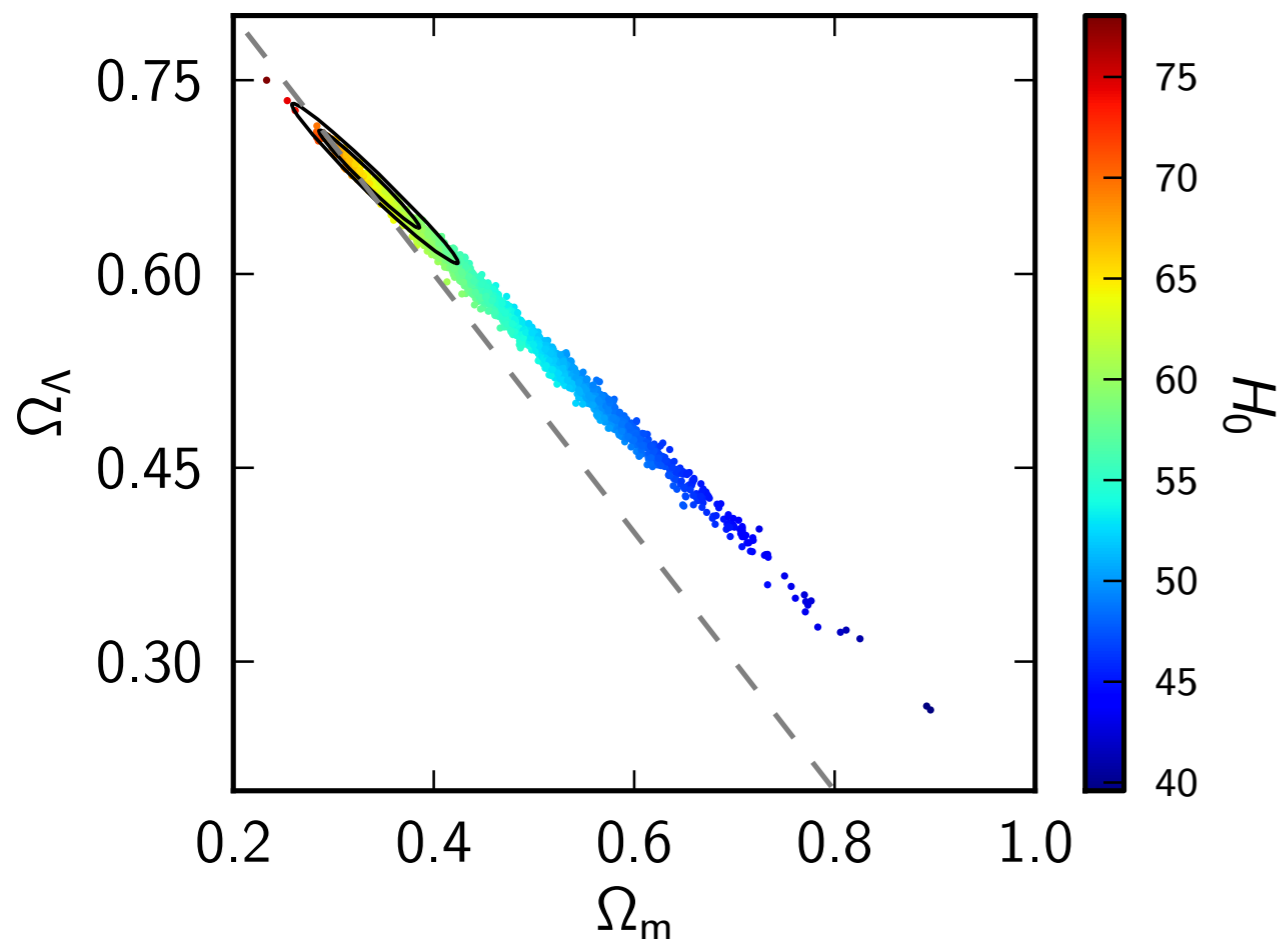
- CMB lensing break the angular diameter degeneracy



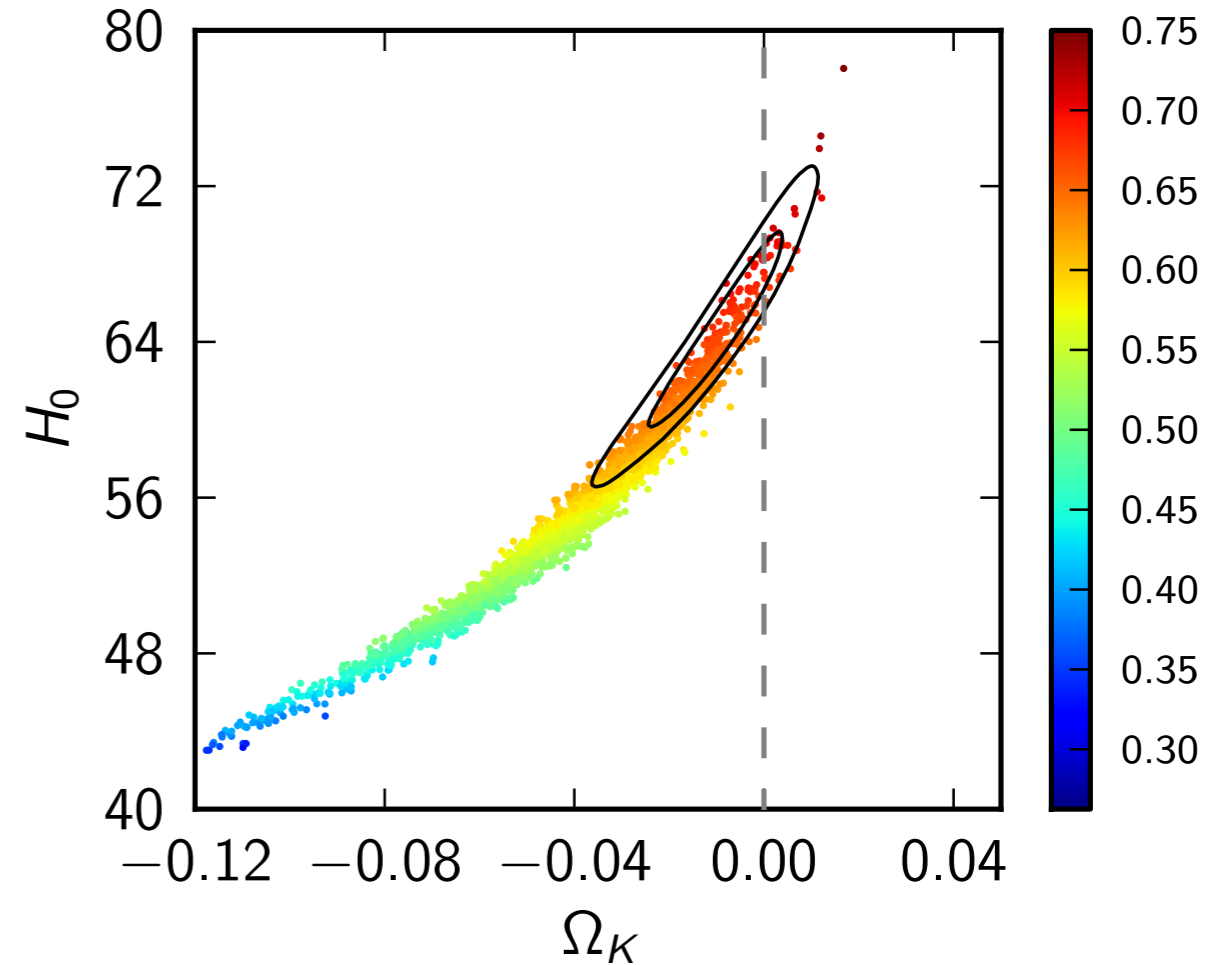


Cosmology

- CMB lensing break the angular diameter degeneracy



$$\Omega_\Lambda = 0.57^{+0.073}_{-0.055} \quad (68\%; \text{Planck+WP+highL})$$
$$\Omega_\Lambda = 0.67^{+0.027}_{-0.023} \quad (68\%; \text{Planck+lensing+WP+highL}).$$



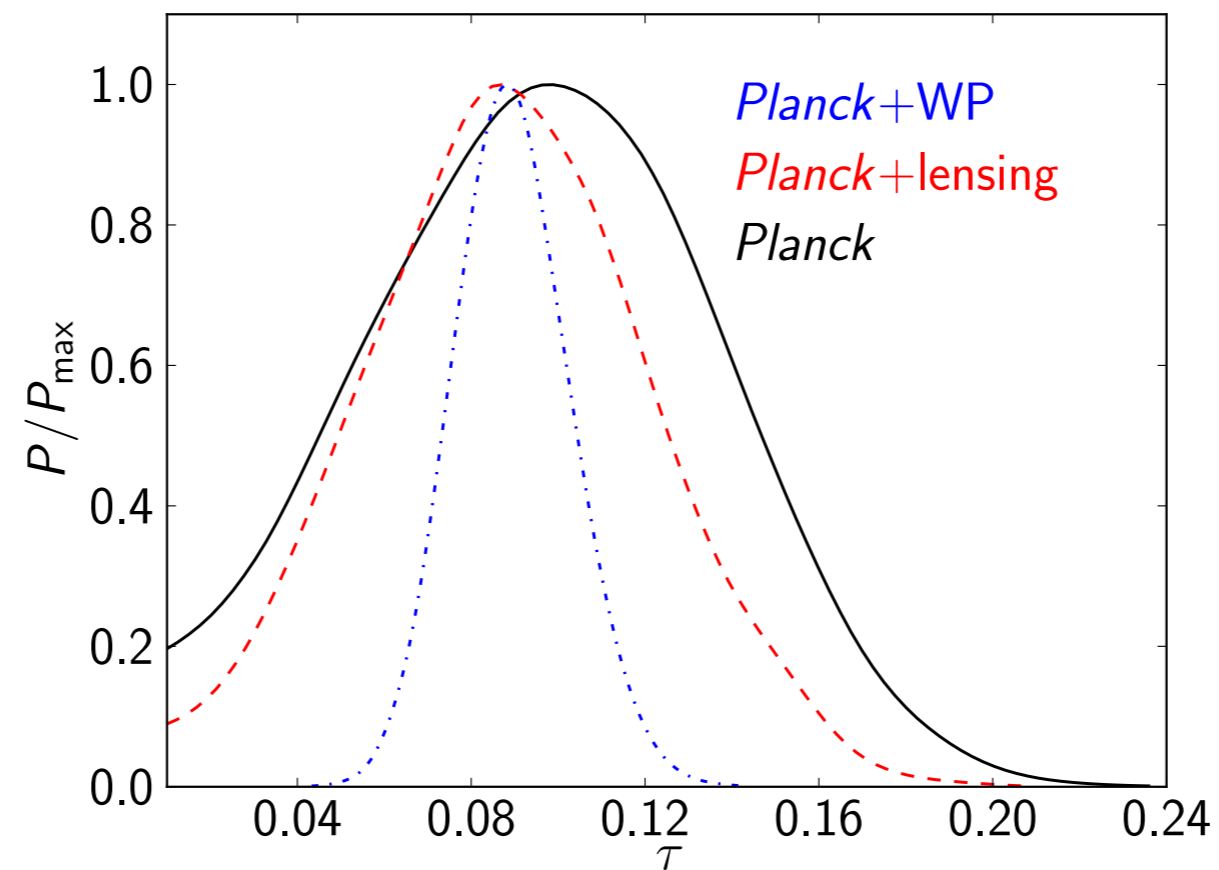
$$100\Omega_K = -4.2^{+4.3}_{-4.8} \quad (95\%; \text{Planck+WP+highL});$$
$$100\Omega_K = -1.0^{+1.8}_{-1.9} \quad (95\%; \text{Planck+lensing} \\ + \text{WP+highL}).$$



Cosmology

■ Reionization

Optical depth - Amplitude degeneracy $A_s e^{-2\tau}$



$$\tau = 0.097 \pm 0.038 \quad (68\%; \textit{Planck})$$

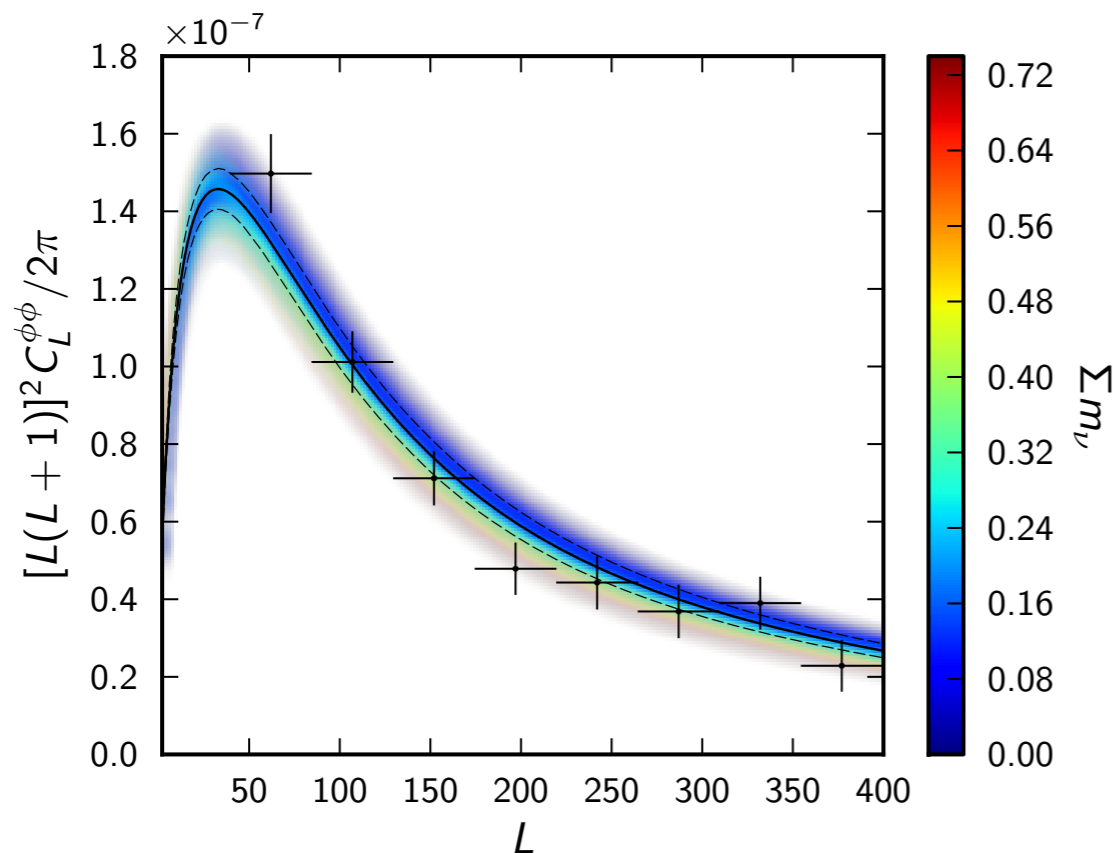
$$\tau = 0.089 \pm 0.032 \quad (68\%; \textit{Planck+lensing}).$$



Cosmology

■ Sum of neutrinos masses

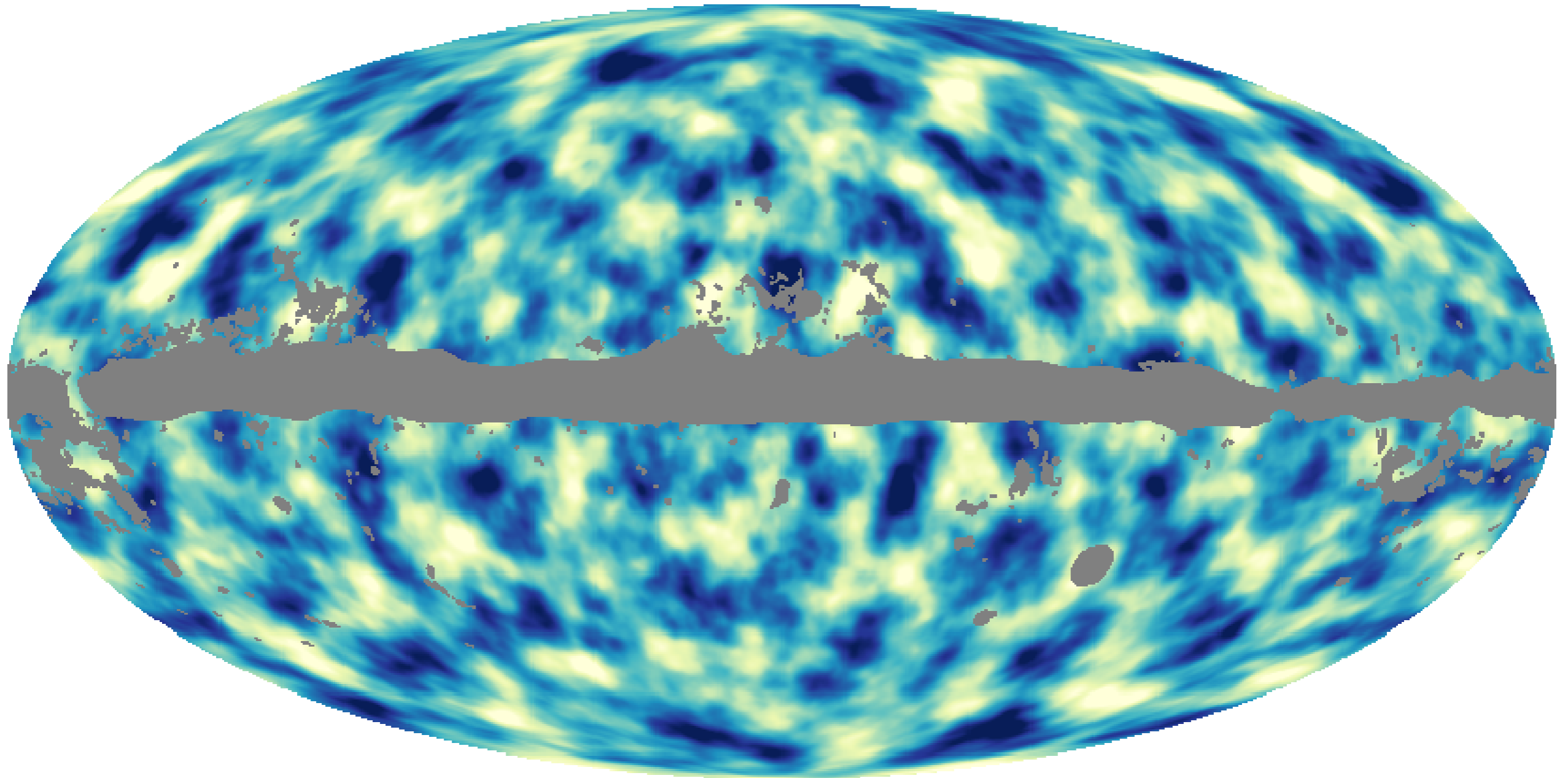
- Mild tension : constraint weaker than expected!
- Temperature power spectra: more lensing = smaller mass
- Reconstruction: less lensing = larger mass



$$\sum m_\nu < 0.66 \text{ eV}, \quad (95\%; \text{Planck}+\text{WP}+\text{highL}),$$
$$\sum m_\nu < 0.85 \text{ eV}, \quad (95\%; \text{Planck}+\text{lensing}+\text{WP}+\text{highL}),$$



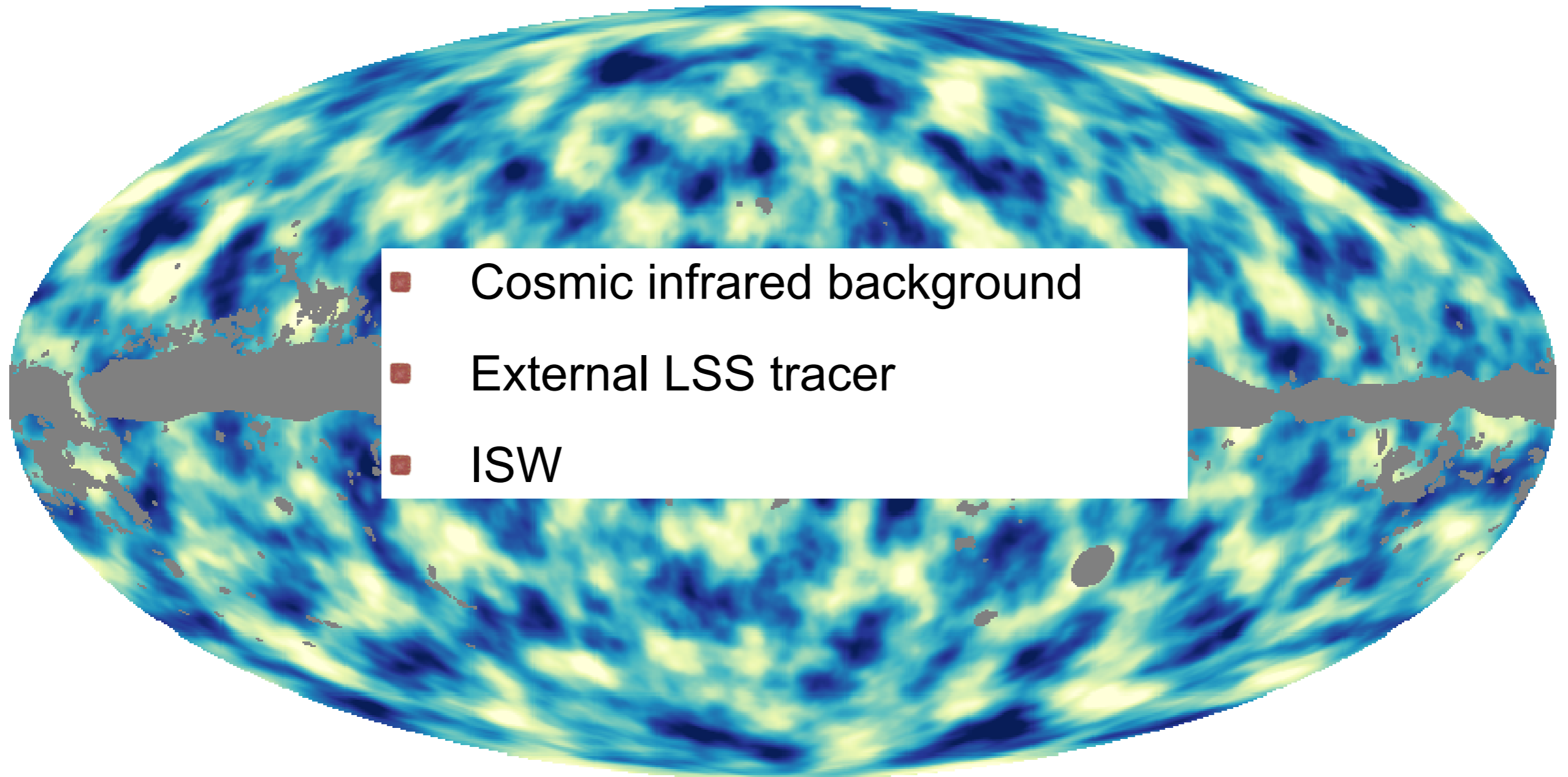
Cross-correlations



The lensing map traces the matter distribution up to the last scattering surface



Cross-correlations

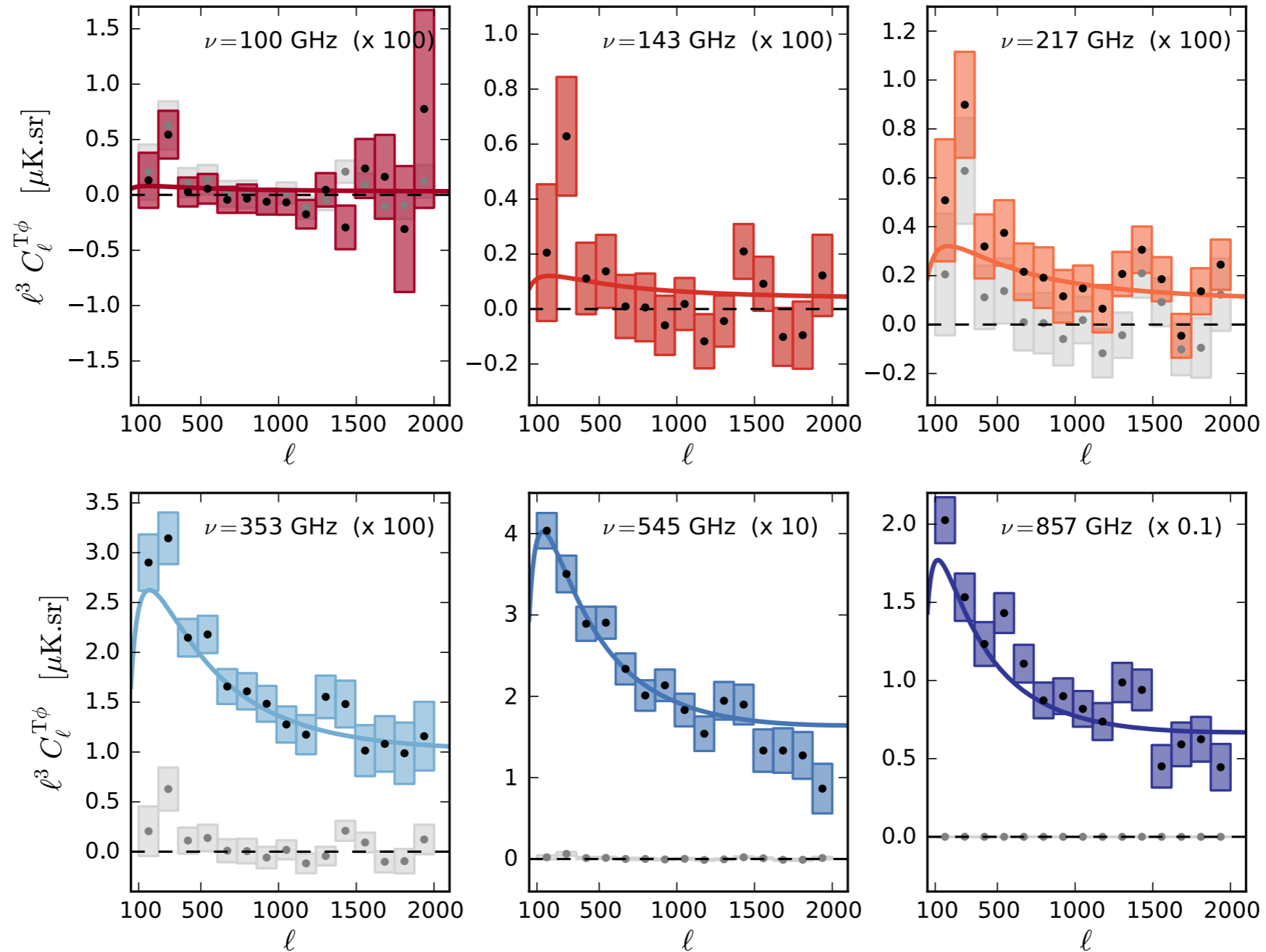


The lensing map traces the matter distribution up to the last scattering surface



CMB lensing - CIB

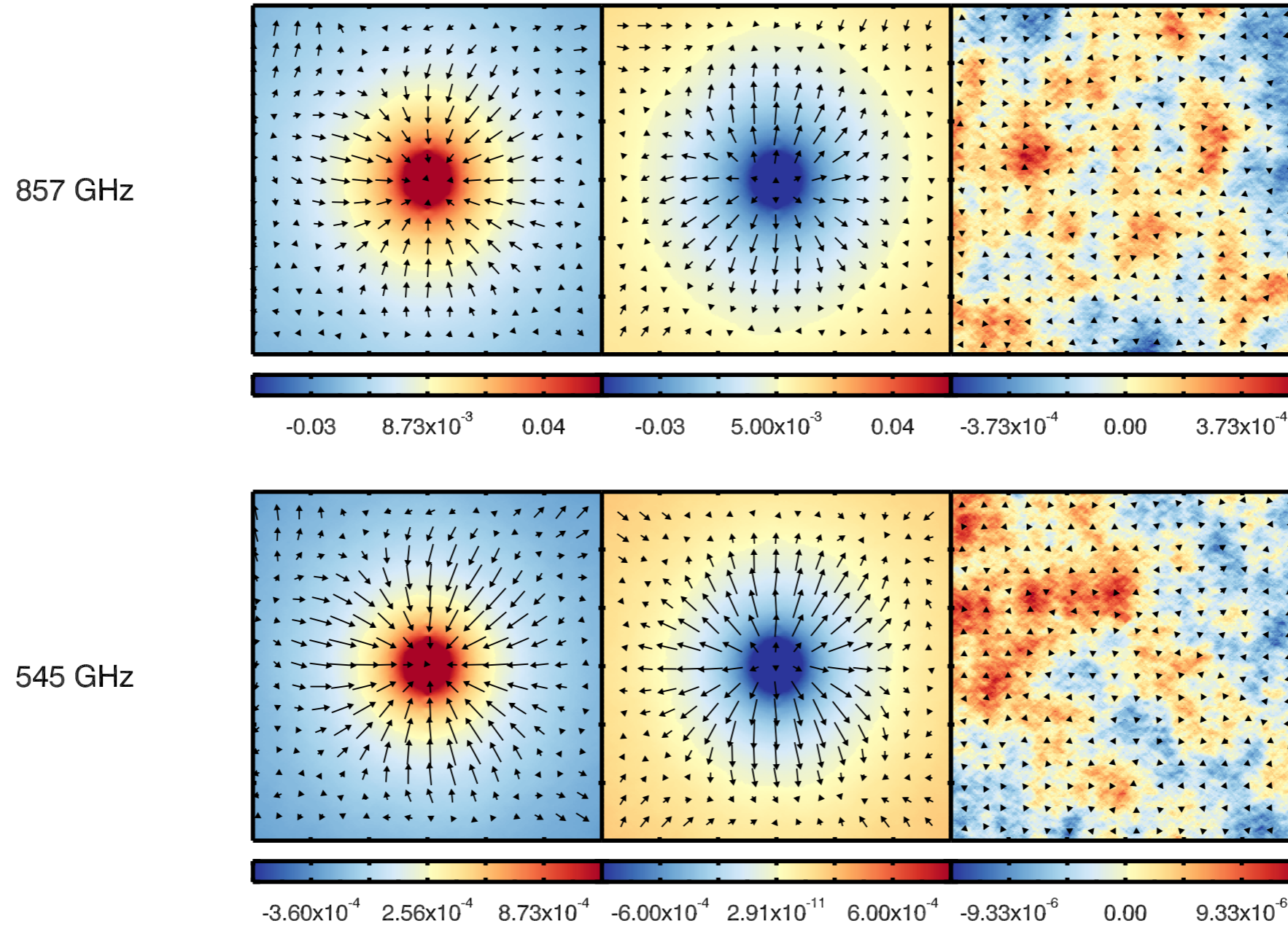
- Lensing potential correlated with HFI temperature maps





CMB lensing - CIB

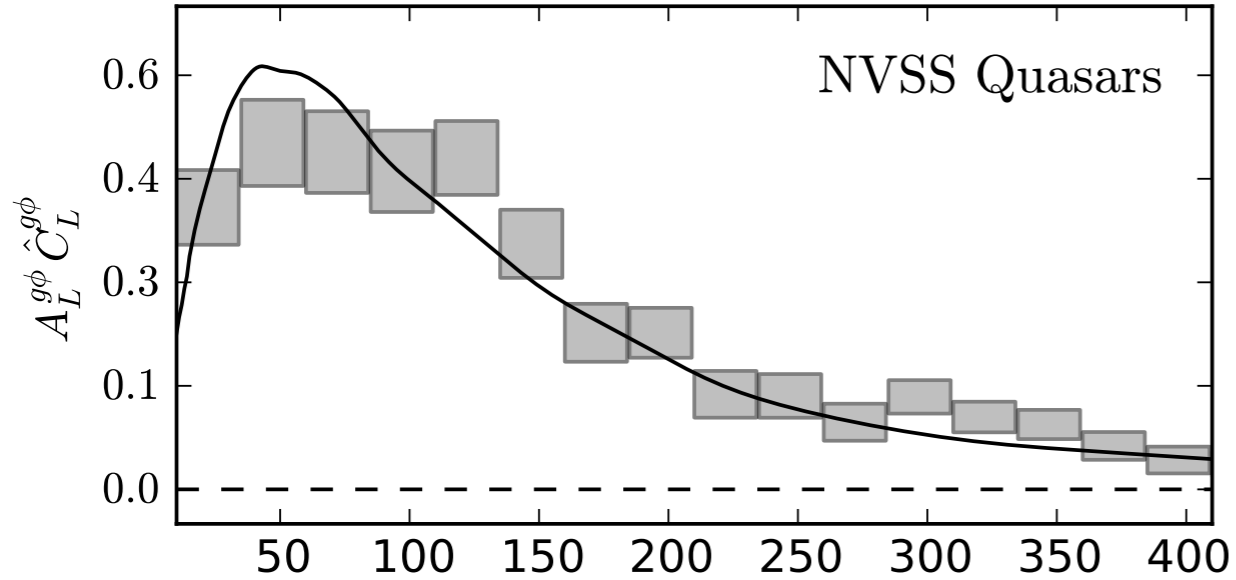
- Deflection stacked on 20.000 temperature extrema



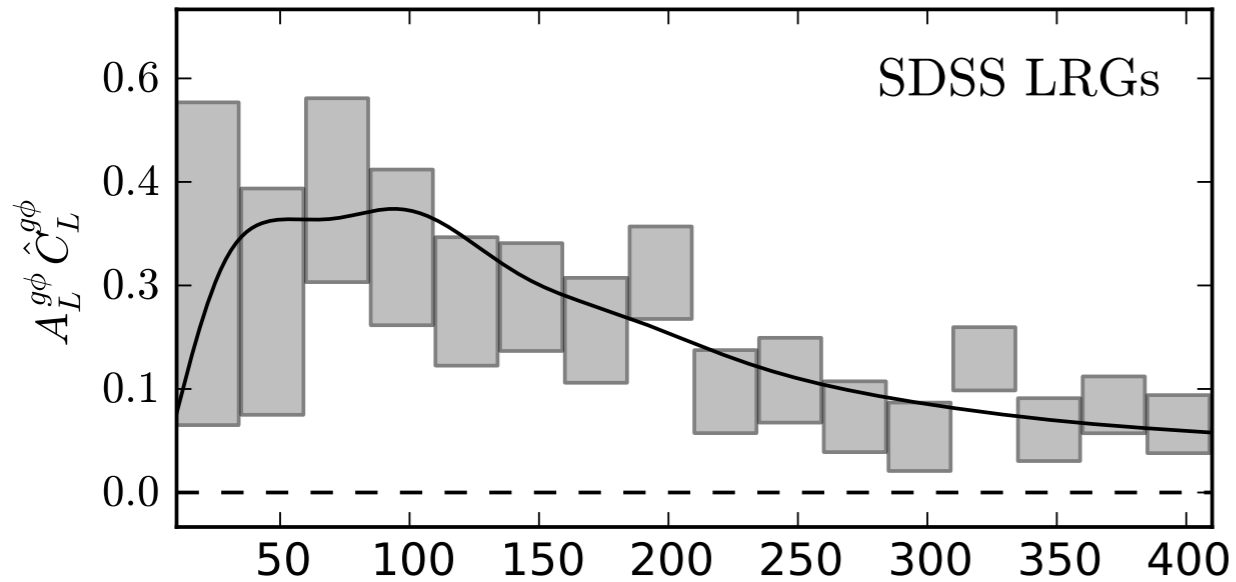
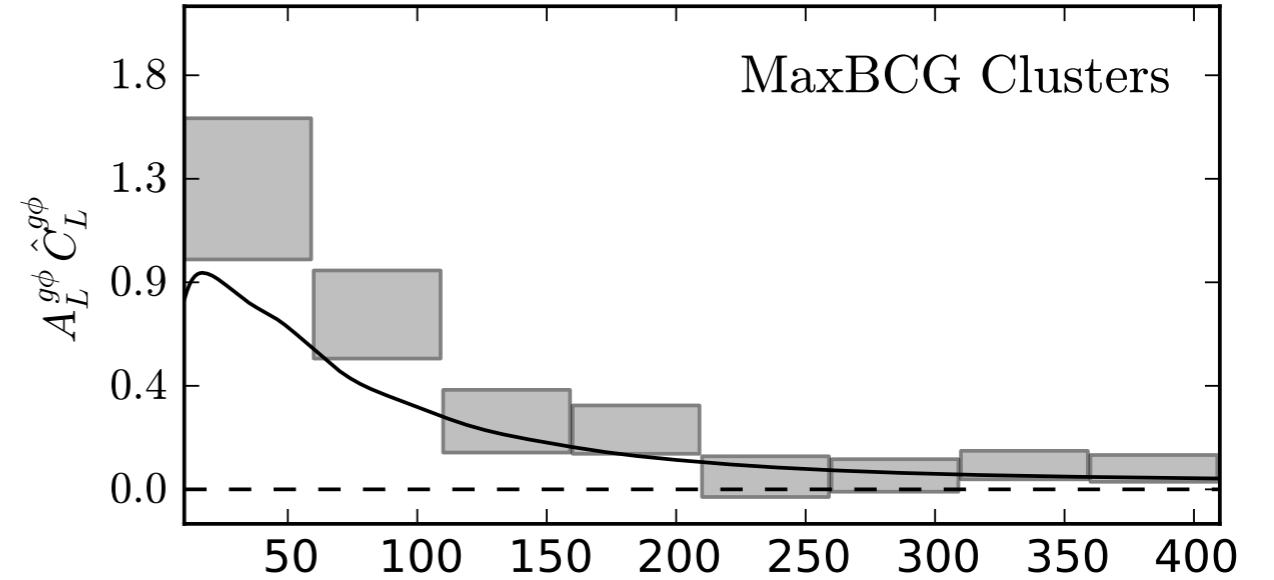


CMB lensing - External tracers

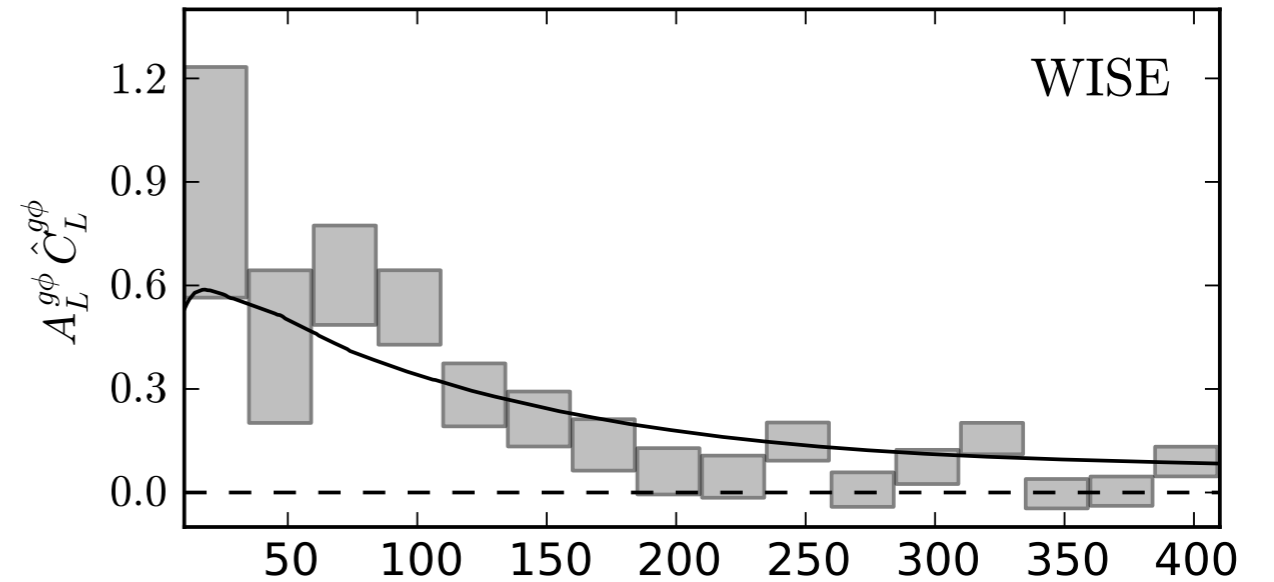
$$b(z) = 1.7 \rightarrow \hat{A}_{\text{NVSS}}^{g\phi} = 1.03 \pm 0.05 (\approx 20\sigma)$$



$$b(z) = 3 \rightarrow \hat{A}_{\text{MaxBCG}}^{g\phi} = 1.54 \pm 0.21 (\approx 7\sigma)$$



$$b(z) = 2 \rightarrow \hat{A}_{\text{LRGs}}^{g\phi} = 0.96 \pm 0.10 (\approx 10\sigma)$$

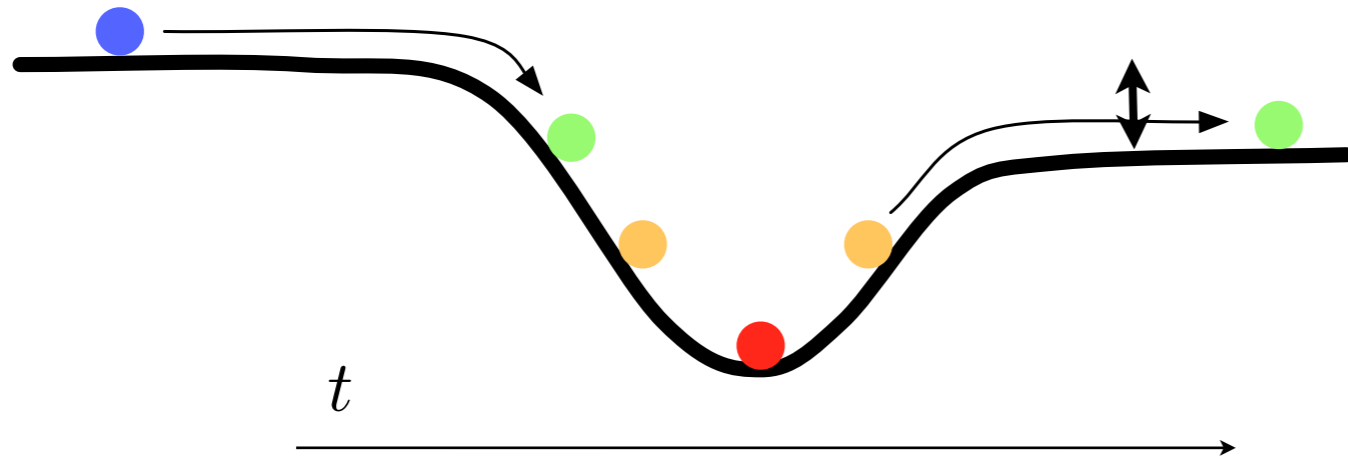


$$b(z) = 1 \rightarrow \hat{A}_{\text{WISE}}^{g\phi} = 0.97 \pm 0.13 (\approx 7\sigma)$$



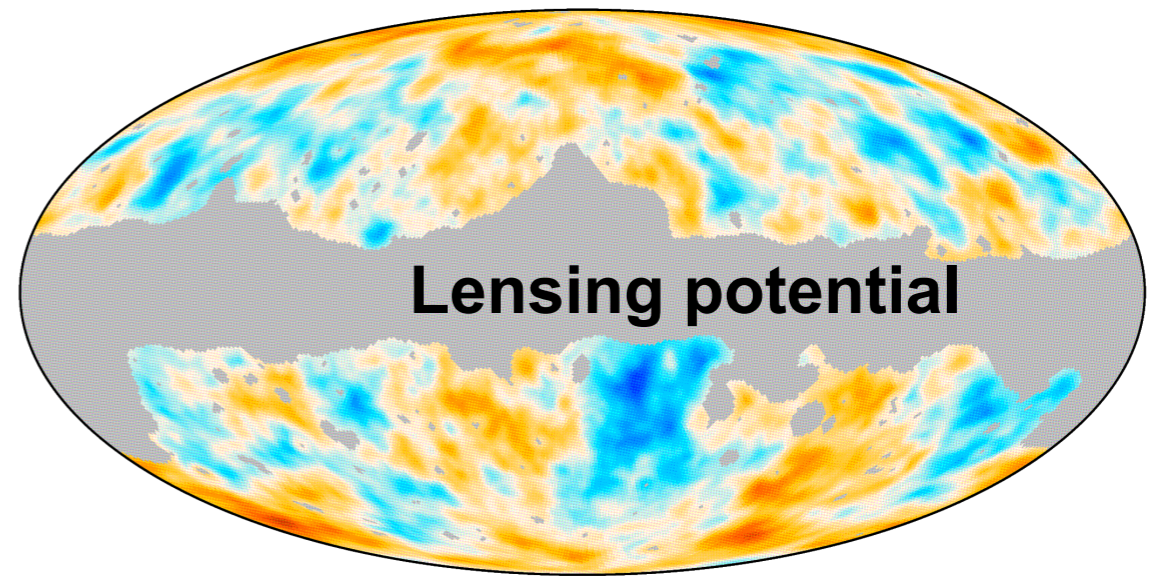
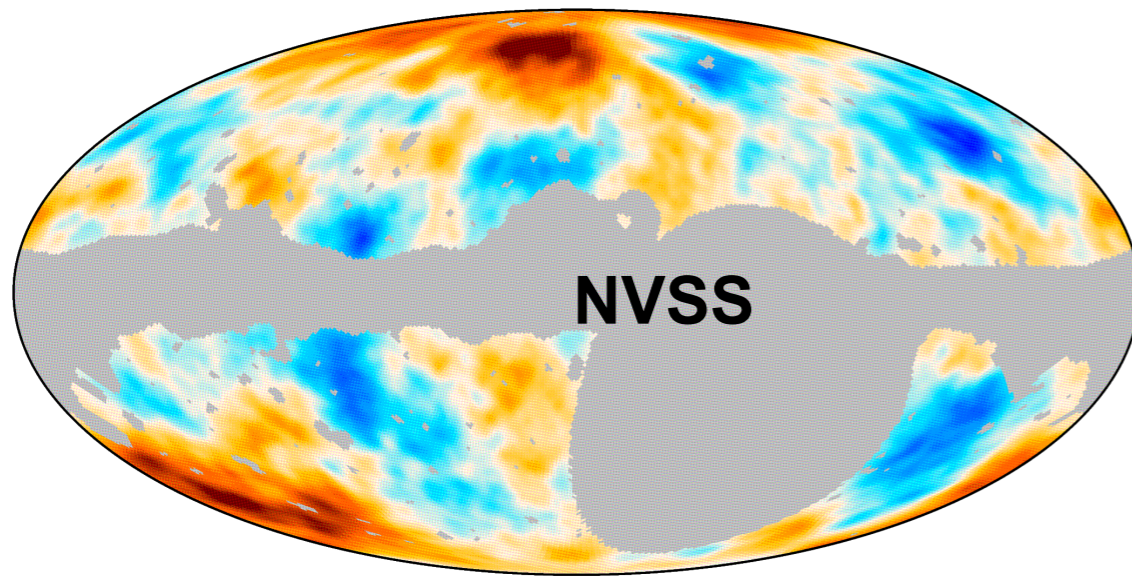
ISW

Shallowing of the potential due to expansion driven by dark energy



$$\frac{\Delta T}{T} = \frac{2}{c^3} \int_{\eta^*}^{\eta_0} d\eta \frac{\partial \Phi}{\partial \eta}$$

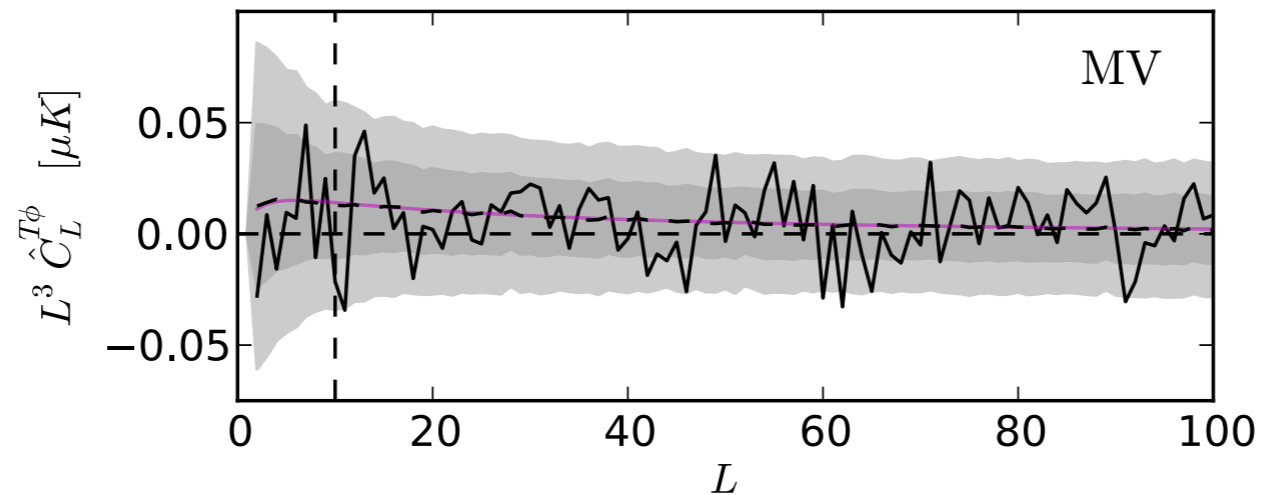
Courtesy: K. Benabed



Planck ISW maps



ISW - Lensing correlation

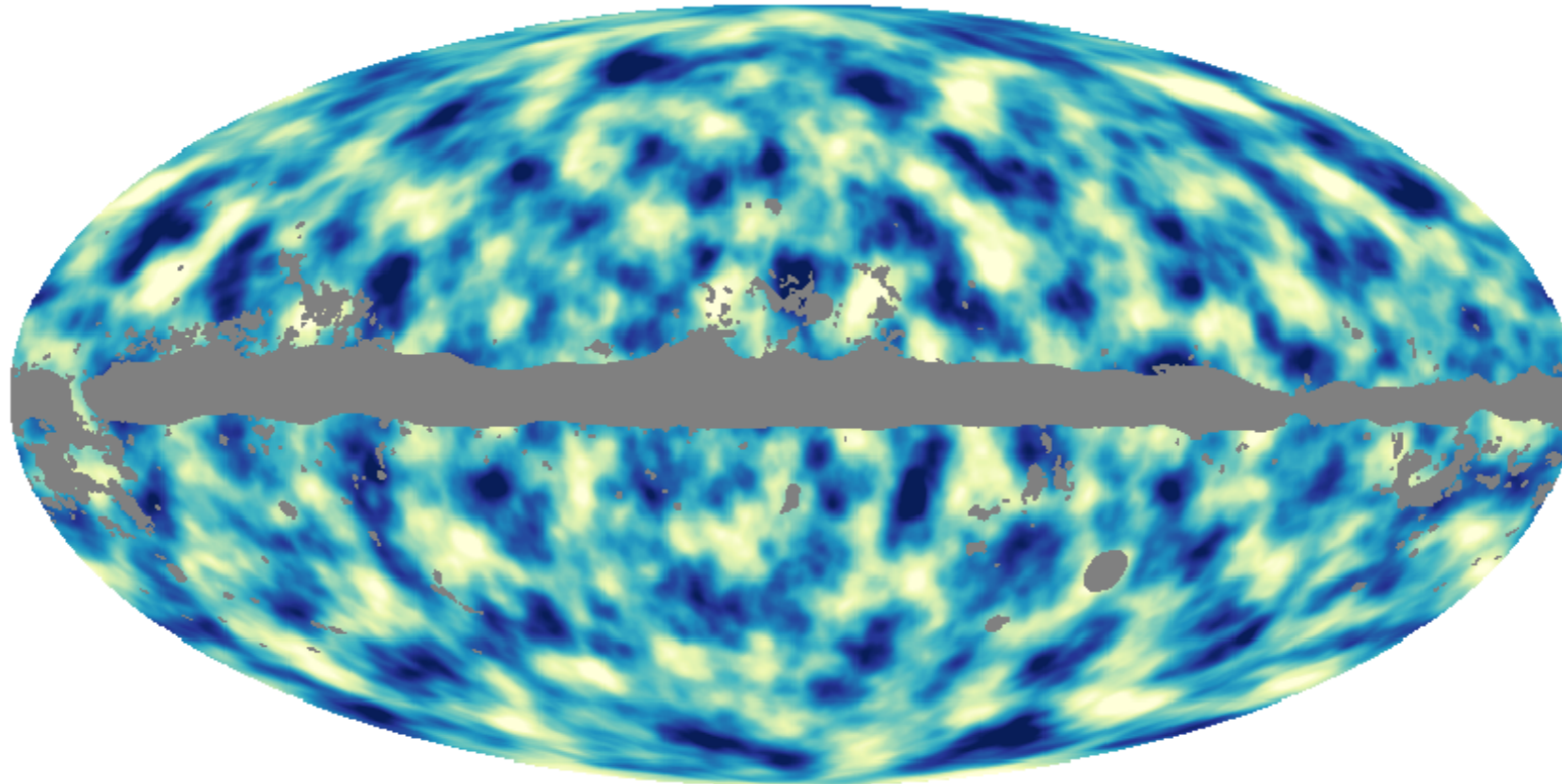


Estimator		C-R	σ	NILC	σ	SEVEM	σ	SMICA	σ	MV	
$T\phi$	$\ell \geq 10$	0.52 ± 0.33	1.5	0.72 ± 0.30	2.4	0.58 ± 0.31	1.9	0.68 ± 0.30	2.3	0.78 ± 0.32	2.4
	$\ell \geq 2$	0.52 ± 0.32	1.6	0.75 ± 0.28	2.7	0.62 ± 0.29	2.1	0.70 ± 0.28	2.5		
KSW		0.75 ± 0.32	2.3	0.85 ± 0.32	2.7	0.68 ± 0.32	2.1	0.81 ± 0.31	2.6		
binned		0.80 ± 0.40	2.0	1.03 ± 0.37	2.8	0.83 ± 0.39	2.1	0.91 ± 0.37	2.5		
modal		0.68 ± 0.39	1.7	0.93 ± 0.37	2.5	0.60 ± 0.37	1.6	0.77 ± 0.37	2.1		

- First 2.5sigma detection. Robust against dataset and estimator
- Links Λ and CDM



The Planck lensing map



- (Almost) Full-sky map of the large scale structure at $z \sim 2$
- Will be used for the next 10-20 years (DES, Euclid, LSST, ...)
- Available on the PLA