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# Measurement of the CKM angle $\beta$ at BaBar

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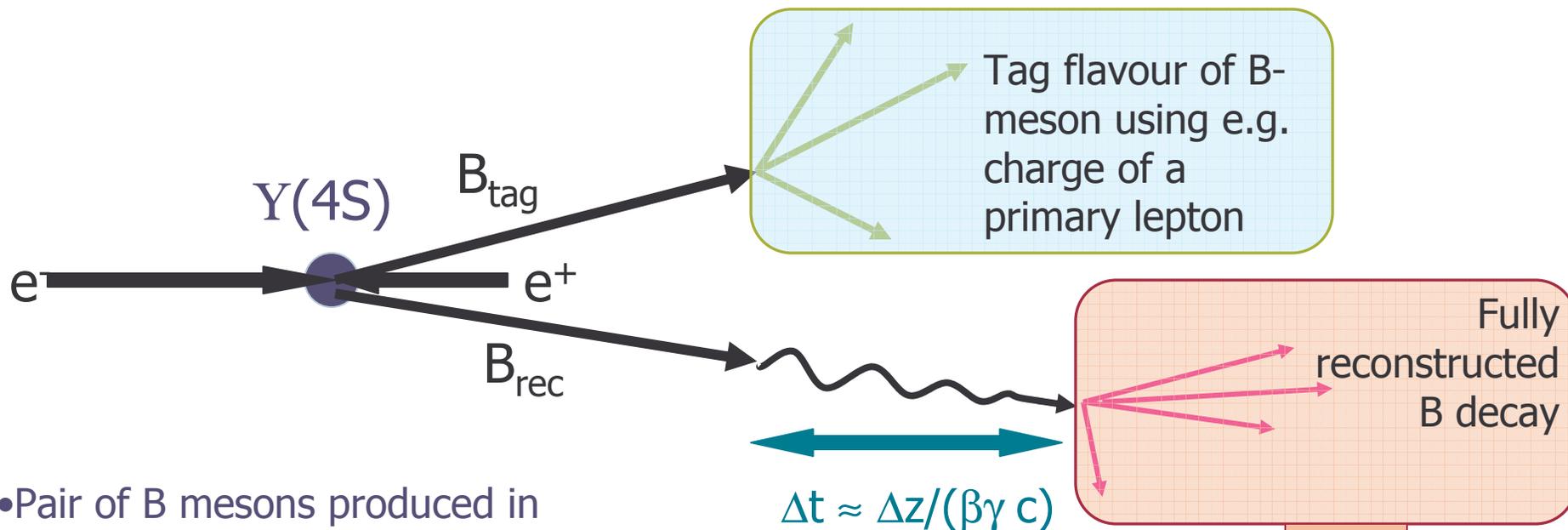
5th Rencontres du Vietnam  
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# Measuring time-dependent asymmetry



- Pair of B mesons produced in coherent  $L=1$  state, boosted ( $\beta\gamma=0.55$ ) wrt lab frame
- At exact time that  $B_{tag}$  decays,  $B_{rec}$  is known to have opposite flavour
- $B_{rec}$  may mix during the time  $\Delta t$  between the two B decays

Use 2 nearly uncorrelated variables to help distinguish signal from background:

$$m_{ES} = [(s/2 + \mathbf{p}_i \cdot \mathbf{p}_B)^2 / E_i - \mathbf{p}_B^2]^{1/2}$$

$$\Delta E = (E_i E_B - \mathbf{p}_i \cdot \mathbf{p}_B - s/2) / \sqrt{s}$$

# Measuring time-dependent asymmetry

$$a_{f_{CP}}(t) = \frac{\Gamma(\bar{B}_{\text{phys}}^0(t) \rightarrow f_{CP}) - \Gamma(B_{\text{phys}}^0(t) \rightarrow f_{CP})}{\Gamma(\bar{B}_{\text{phys}}^0(t) \rightarrow f_{CP}) + \Gamma(B_{\text{phys}}^0(t) \rightarrow f_{CP})} = -C_{f_{CP}} \cos(\Delta m t) + S_{f_{CP}} \sin(\Delta m t)$$

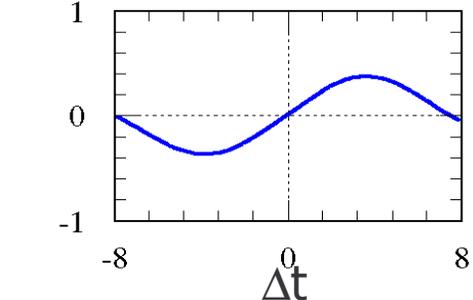
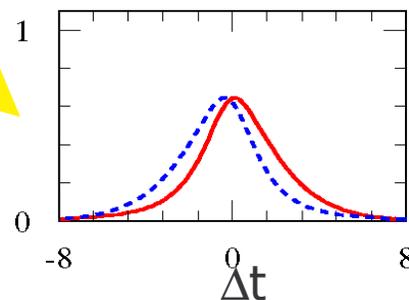
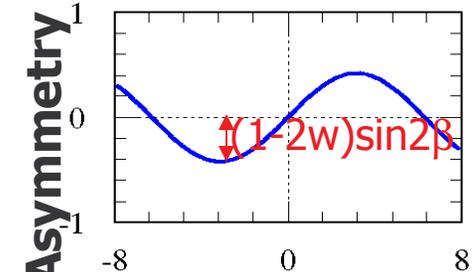
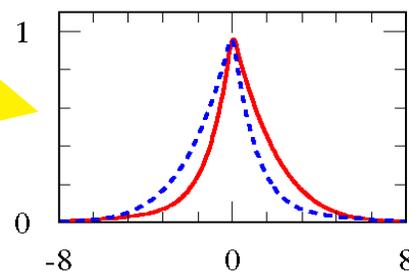
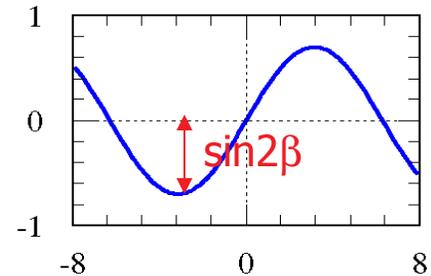
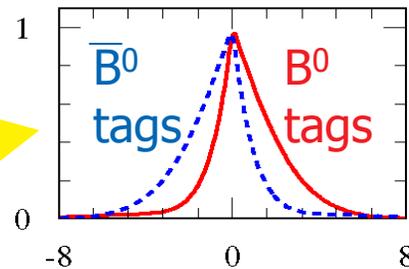
e.g. For  $B \rightarrow J/\psi K_S$   $C=0$ ,  $S=\sin 2\beta$

Perfect  $\Delta t$  resolution,  
perfect tagging

Perfect  $\Delta t$  resolution,  
wrong tag fraction  $w$

Realistic  $\Delta t$  resolution,  
wrong tag fraction  $w$

- Measure **mistag fraction** and  **$\Delta t$  resolution function** by fitting large sample of reconstructed B mesons of known flavour.



# $\sin 2\beta$ in $b \rightarrow c\bar{c}s$ modes

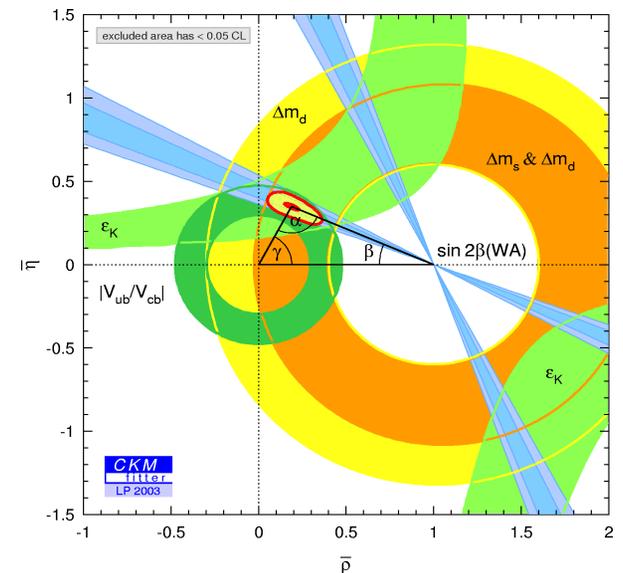
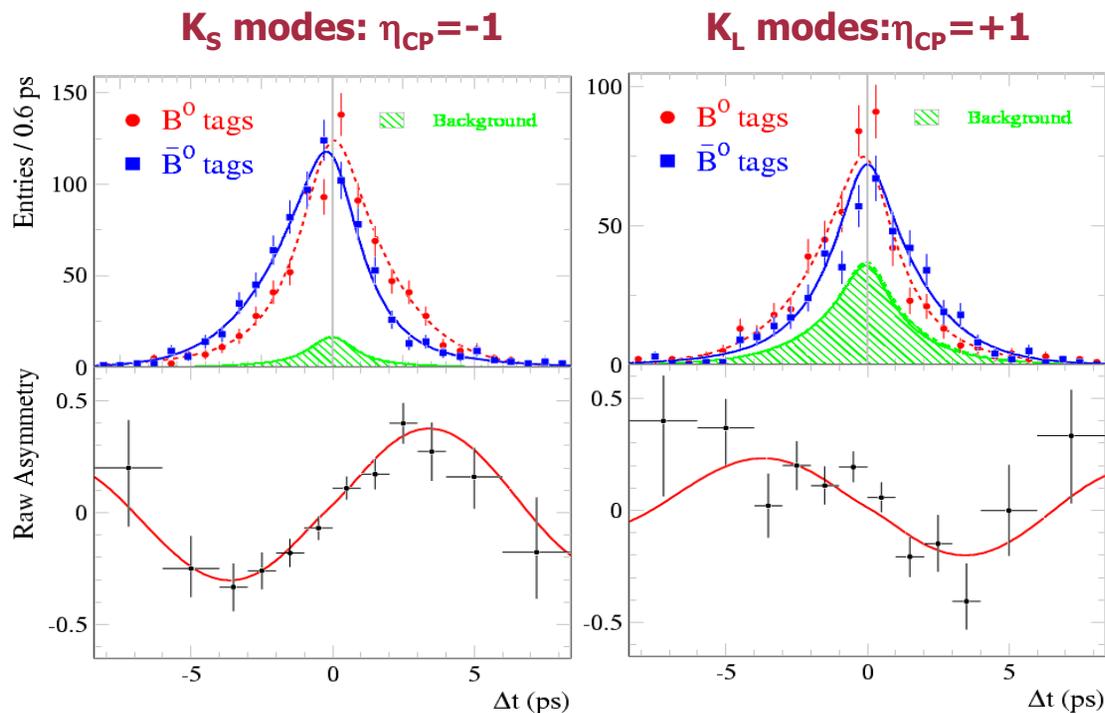
- $\sin 2\beta$  already well measured in  $b \rightarrow c\bar{c}s$  channels by BaBar and Belle
- Small theoretical uncertainty – tree and first order penguin contributions have same phase

*BaBar*:  $80.8 \text{ fb}^{-1}$ :

$$\sin 2\beta = 0.741 \pm 0.067 \pm 0.033$$

*PRL 89, 201802 (2002)*

WA:  $\sin 2\beta = 0.736 \pm 0.049$



Still 4-fold ambiguity in value of  $\beta$

# $\cos 2\beta$ with $B \rightarrow J/\psi K^*$

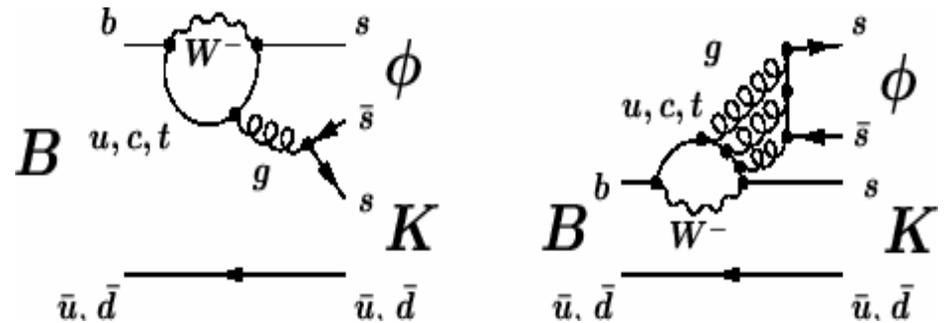
- pseudoscalar  $\rightarrow$  vector vector decay – contains both CP-odd and CP-even components
- Interference between CP-odd and CP-even components gives rise to  $\cos 2\beta$  term in time-dependent angular distributions

$$a(t) = P \cos \Delta mt + \sin \Delta mt (S \sin 2\beta + C \cos 2\beta)$$

- Can measure angular amplitudes to  $\cos 2\beta$  up to a twofold ambiguity
- Use  $K\pi$  S-wave state in  $K^*(892)$  region to resolve this ambiguity by fitting for relative strong phase in bins of  $m(K\pi)$
- If  $\sin 2\beta = 0.736$ , expect  $\cos 2\beta = \pm 0.68$
- Using “toy MC” technique, find the positive solution is more probable  $\Rightarrow$  rule out  $\cos 2\beta < 0$  at 89% CL

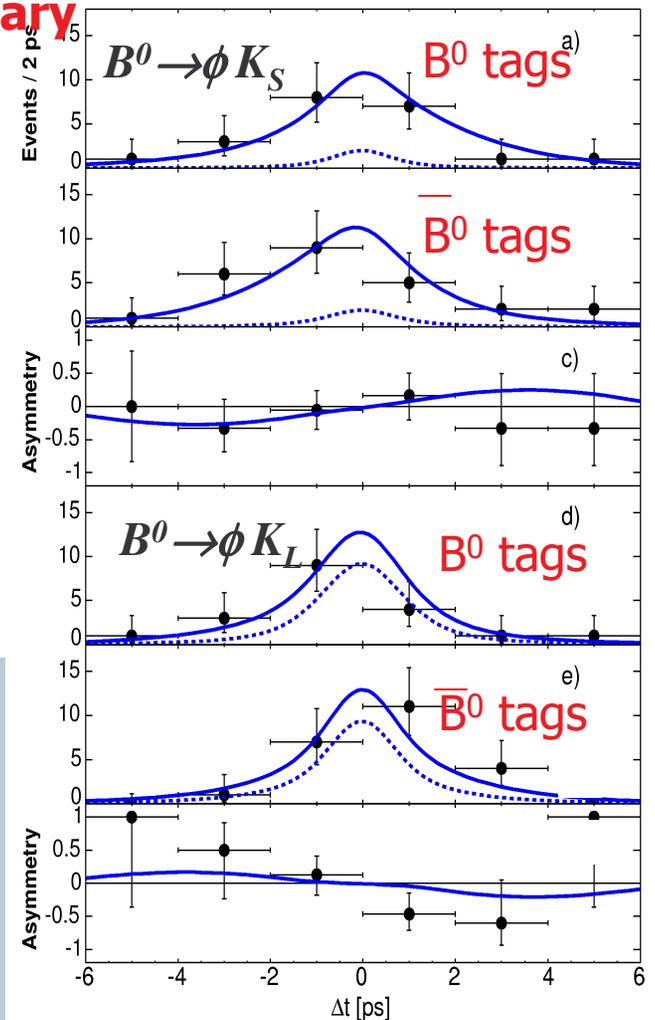
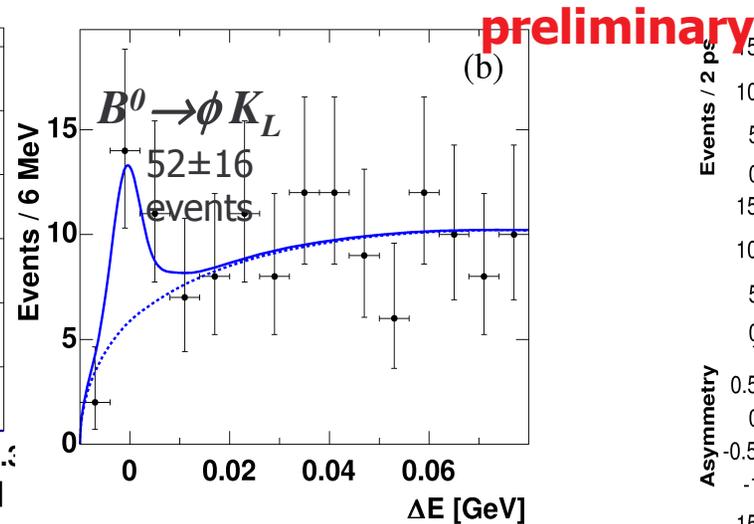
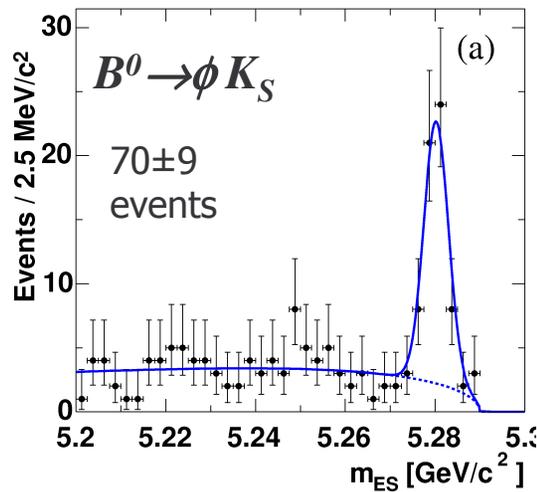
# sin2 $\beta$ from penguin-dominated modes

- In pure  $b \rightarrow s$  penguins (e.g.  $B \rightarrow \phi K^0$ ), measured value of  $\sin 2\beta$  should be the same as for  $b \rightarrow c\bar{c}s$



- Sensitive probe for New Physics: additional loop diagrams can contain heavy non-SM particles and new CP violating phases

# $B \rightarrow \phi K_S$ and $B \rightarrow \phi K_L$



- In SM, pure  $b \rightarrow \bar{s} s s$  penguin, expect
- $S_{\phi K_S} = +\sin 2\beta$ ,  $S_{\phi K_L} = -\sin 2\beta$

*BaBar*:  $113 \text{ fb}^{-1}$

$$S_{\phi K_S} = 0.47 \pm 0.34^{+0.08}_{-0.06}$$

$$C_{\phi K_S} = 0.10 \pm 0.33 \pm 0.10$$

hep-ex/0403026

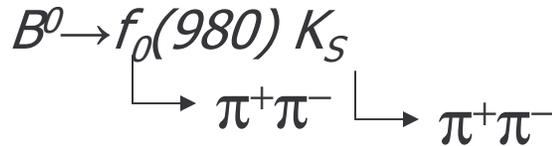
Using  $140 \text{ fb}^{-1}$ , Belle measure

$$S_{\phi K_S} = -0.96 \pm 0.50 \pm 0.10$$

$$C_{\phi K_S} = 0.15 \pm 0.29 \pm 0.07$$

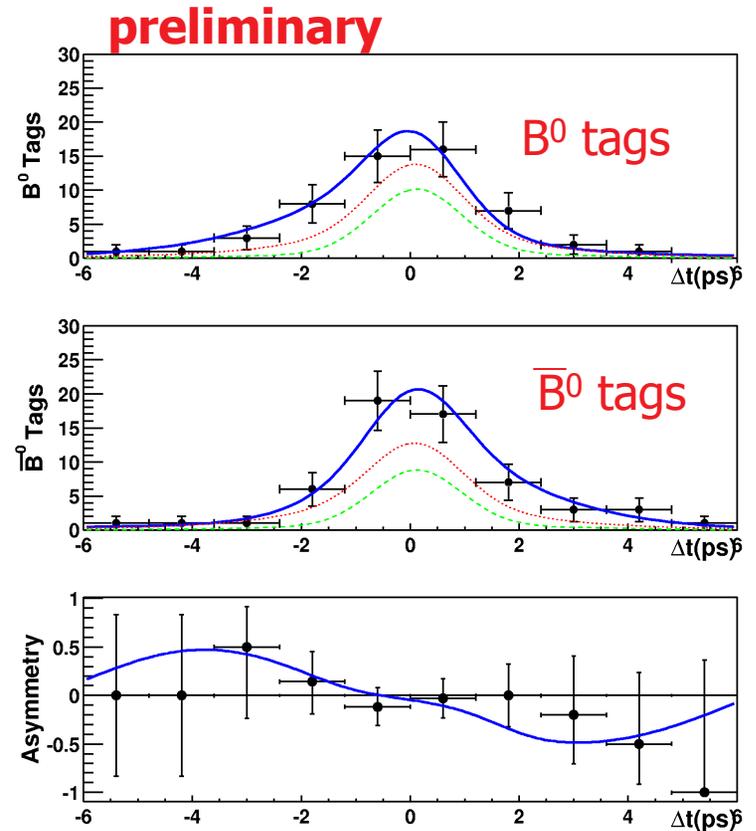
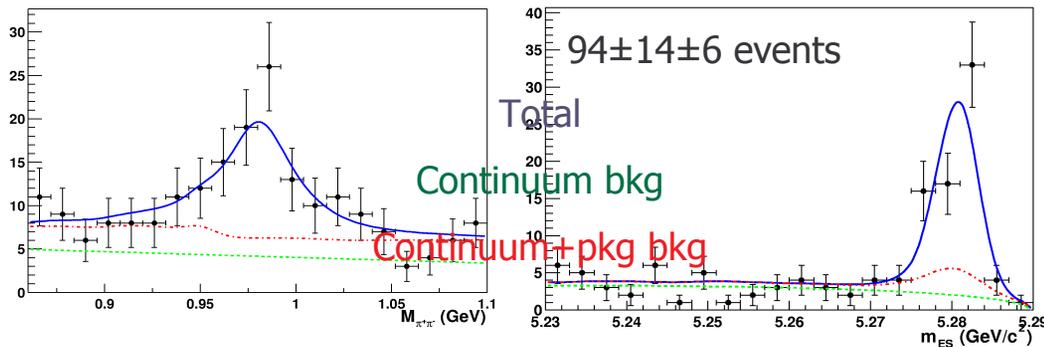
$\Rightarrow 2.3\sigma$  disagreement!

# $B \rightarrow f_0(980) K_S$



- Dominated by  $b \rightarrow s\bar{s}s$  penguin
- Decay to  $\pi\pi$  preferred due to phase space
- “Quasi-two-body” approach – cut on Dalitz plot to reduce contamination from  $\rho$  and  $f_0(1370)$
- Expect  $S_{f_0 K_S} \approx -\sin 2\beta$

*BaBar*. 113fb<sup>-1</sup>



$$S_{f_0 K_S} = -1.62^{+0.56}_{-0.51} \pm 0.10$$

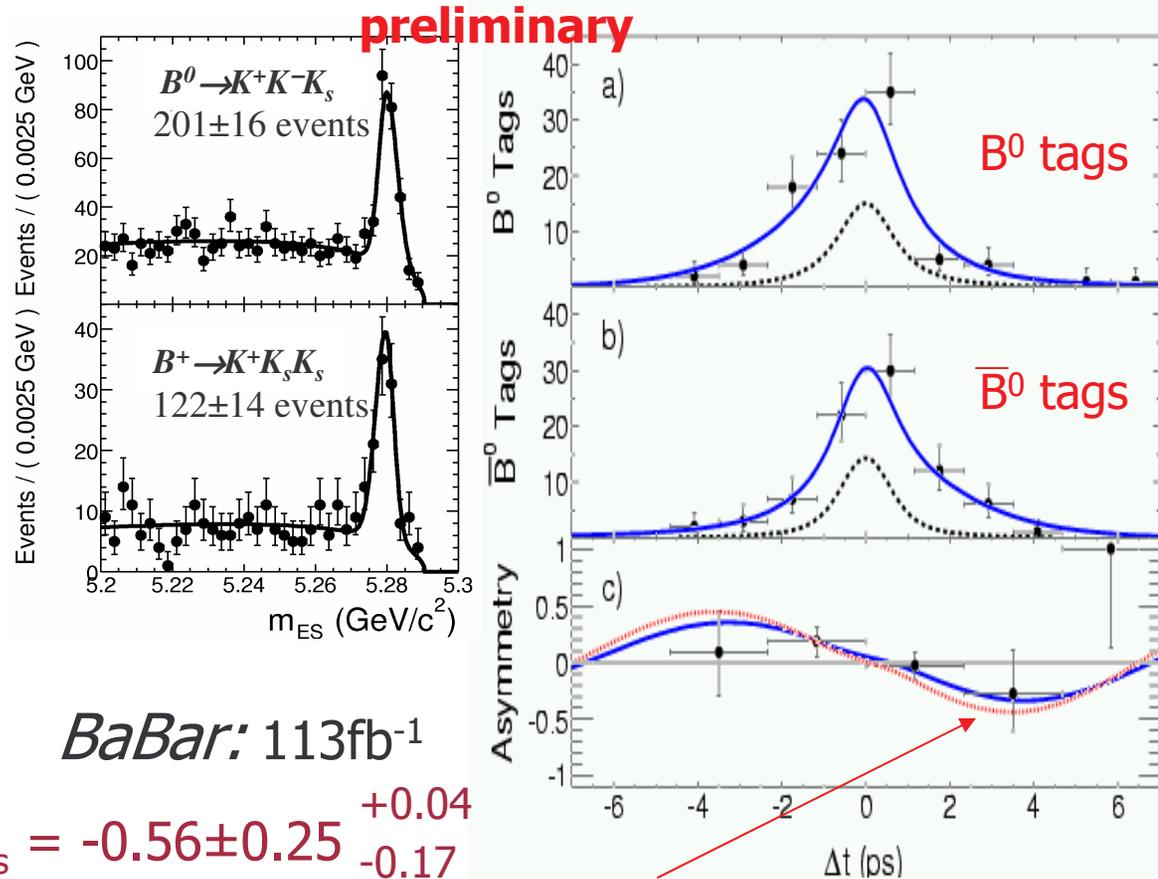
$$C_{f_0 K_S} = 0.27 \pm 0.36 \pm 0.12$$

# $B \rightarrow K^+ K^- K_S$ (excluding $\phi K_S$ )

- Use charged and neutral B decays to determine CP-even fraction using isospin symmetry

$$f_{\text{even}} = \frac{2\Gamma(B^+ \rightarrow K^+ K_S^0 K_S^0)}{\Gamma(B^0 \rightarrow K^+ K^- K^0)} = 0.98 \pm 0.15 \pm 0.04$$

- Expect  $S \approx -\sin 2\beta$



*BaBar*: 113 fb<sup>-1</sup>

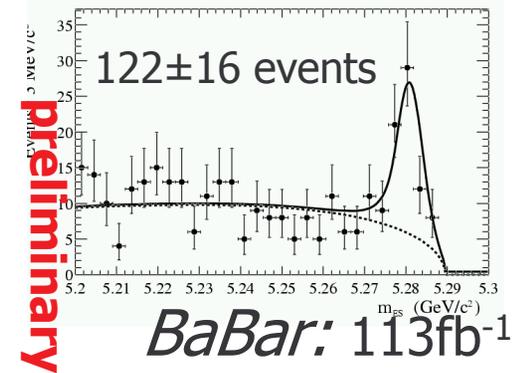
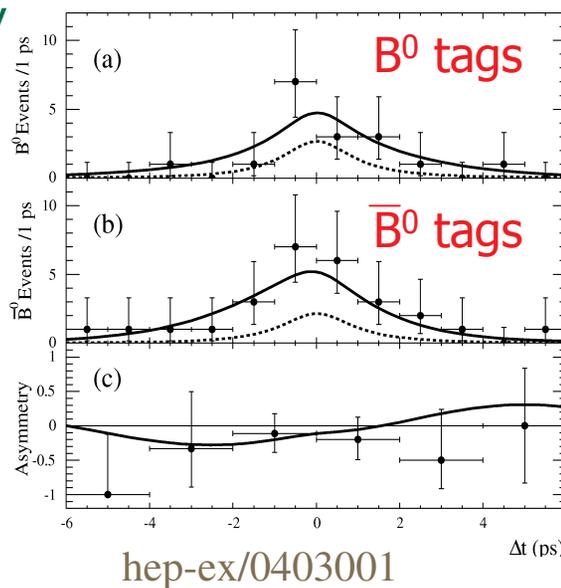
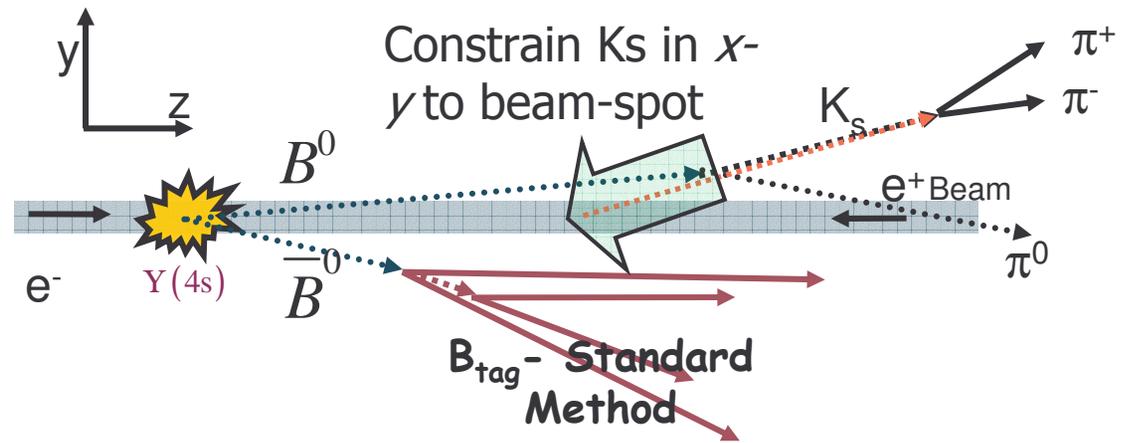
$$S_{K^+ K^- K_S} = -0.56 \pm 0.25^{+0.04}_{-0.17}$$

$$C_{K^+ K^- K_S} = -0.10 \pm 0.19 \pm 0.09$$

hep-ex/0406005

# $B^0 \rightarrow K_S \pi^0$

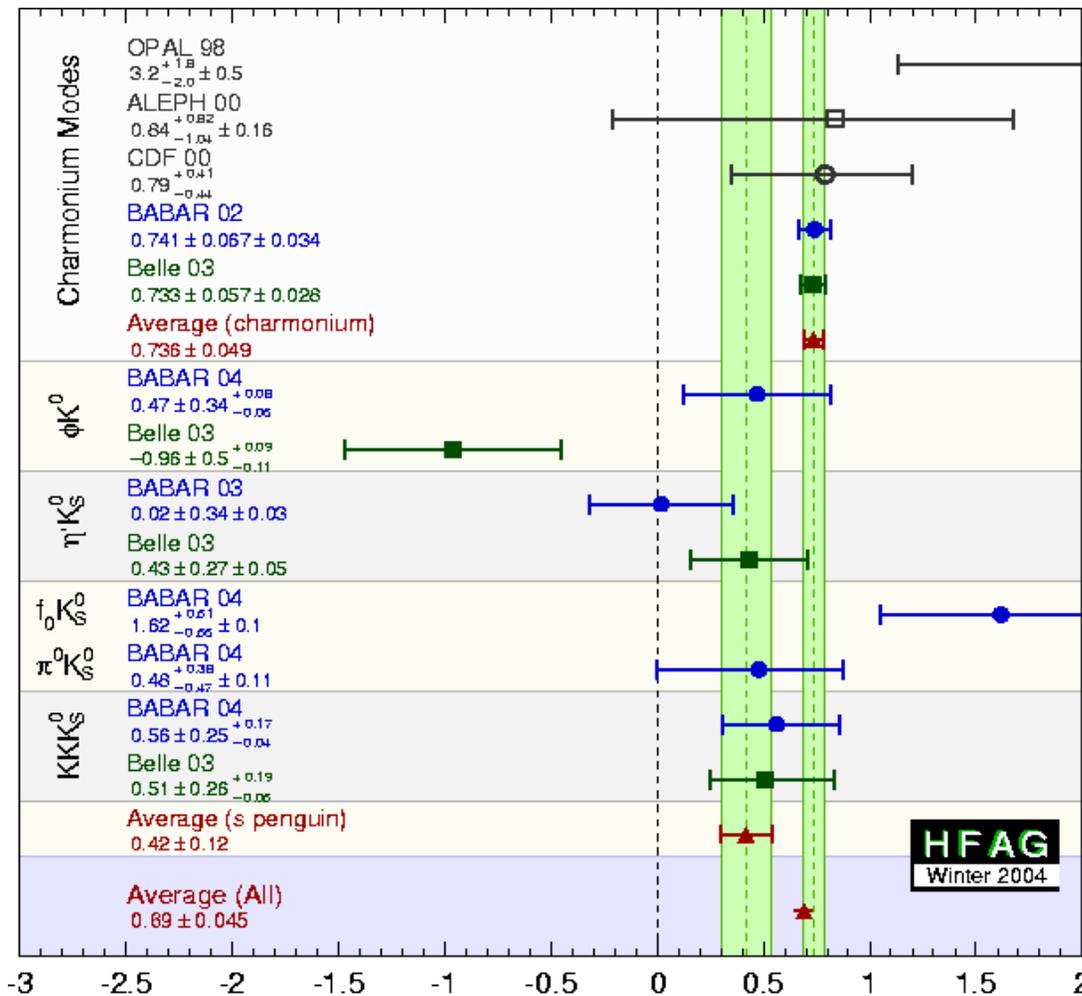
- Experimentally challenging – no charged decay products originating from B decay point
- Use fact that transverse motion of B is small compared to motion in z-direction
- Use intersection of  $K_S$  trajectory and beamspot in x-y plane
- Non-zero tree contribution could lead to  $O(0.1)$  deviation in measured  $\sin 2\beta$  value
- Expect  $S \approx +\sin 2\beta$



$$S_{K_S \pi^0} = 0.48^{+0.38}_{-0.47} \pm 0.11$$

$$C_{K_S \pi^0} = 0.40 \pm 0.28 \pm 0.10$$

# Summary of $\sin 2\beta$ values



- Most results are reasonably consistent with SM, with the exception of Belle  $\phi K_S$
- BaBar-only average for  $b \rightarrow s$  penguins is  $0.63 \pm 0.18$

HFAG  
Winter 2004

# Conclusions

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- $\sin 2\beta$  in  $b \rightarrow c\bar{c}s$  decays already a precision measurement
- Statistics are now large enough that penguin dominated modes are starting to give interesting results
  - $2.3\sigma$  discrepancy between BaBar and Belle in  $B \rightarrow \phi K^0$
  - Situation will be clarified with more data
- First ambiguity-free measurement of sign of  $\cos 2\beta$
- The Standard Model can accommodate all *BaBar* results so far on the angle  $\beta$
- Further updates on several channels with  $205\text{fb}^{-1}$  data coming this summer!

# Backup slides

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# CP violation in the Standard Model

Quark mixing is described by the **CKM matrix**

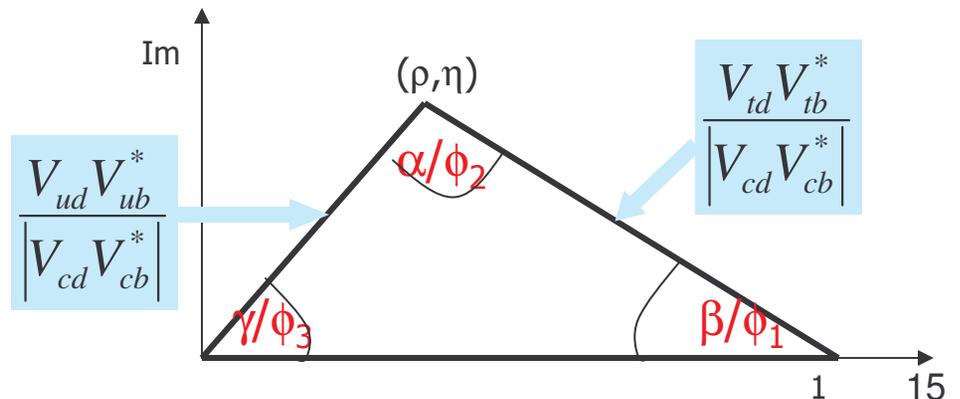
Wolfenstein parametrization

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + O(\lambda^4)$$

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

Matrix is **unitary** – can be represented by triangle on complex plane

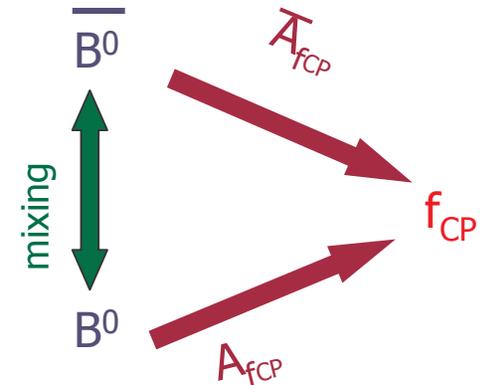
Complex phase  $\rightarrow$  CP violation



# CP violation in the neutral B system

Mass eigenstates  $\rightarrow$   $|B_L\rangle = p|B^0\rangle + q|\bar{B}^0\rangle$ ,  $|B_H\rangle = p|B^0\rangle - q|\bar{B}^0\rangle$ .  $\leftarrow$  Flavour eigenstates

- Consider **time-dependent asymmetry** in decays to a final CP eigenstate  $f_{CP}$ :



$$a_{f_{CP}}(t) = \frac{\Gamma(\bar{B}_{\text{phys}}^0(t) \rightarrow f_{CP}) - \Gamma(B_{\text{phys}}^0(t) \rightarrow f_{CP})}{\Gamma(\bar{B}_{\text{phys}}^0(t) \rightarrow f_{CP}) + \Gamma(B_{\text{phys}}^0(t) \rightarrow f_{CP})} = -C_{f_{CP}} \cos(\Delta m t) + S_{f_{CP}} \sin(\Delta m t)$$

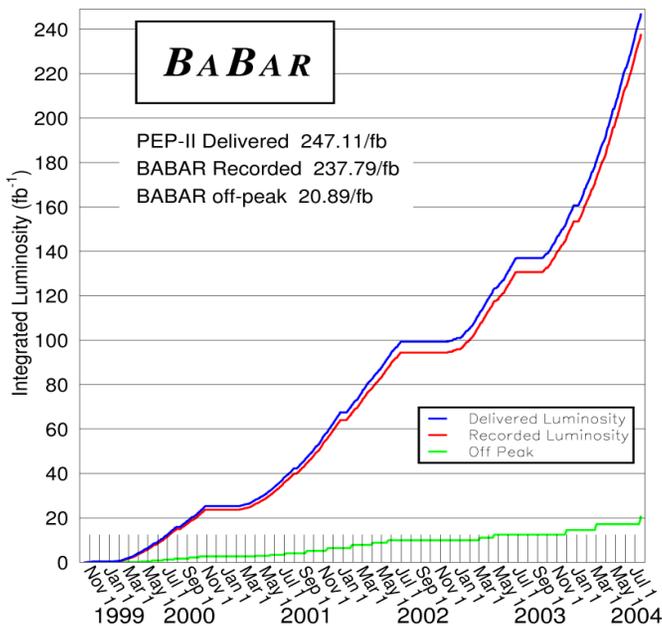
$$C_{f_{CP}} = \frac{1 - |\lambda_{f_{CP}}|^2}{1 + |\lambda_{f_{CP}}|^2}, \quad S_{f_{CP}} = \frac{2\text{Im}\lambda_{f_{CP}}}{1 + |\lambda_{f_{CP}}|^2}, \quad \lambda_{f_{CP}} = \frac{q}{p} \frac{\bar{A}}{A}$$

$\text{Im}(\lambda) \neq 0 \rightarrow$  CPV in interference between mixing and decay  
 $|\bar{A}/A| \neq 1 \rightarrow$  CPV in decay  
 $|q/p| \neq 1 \rightarrow$  CPV in mixing

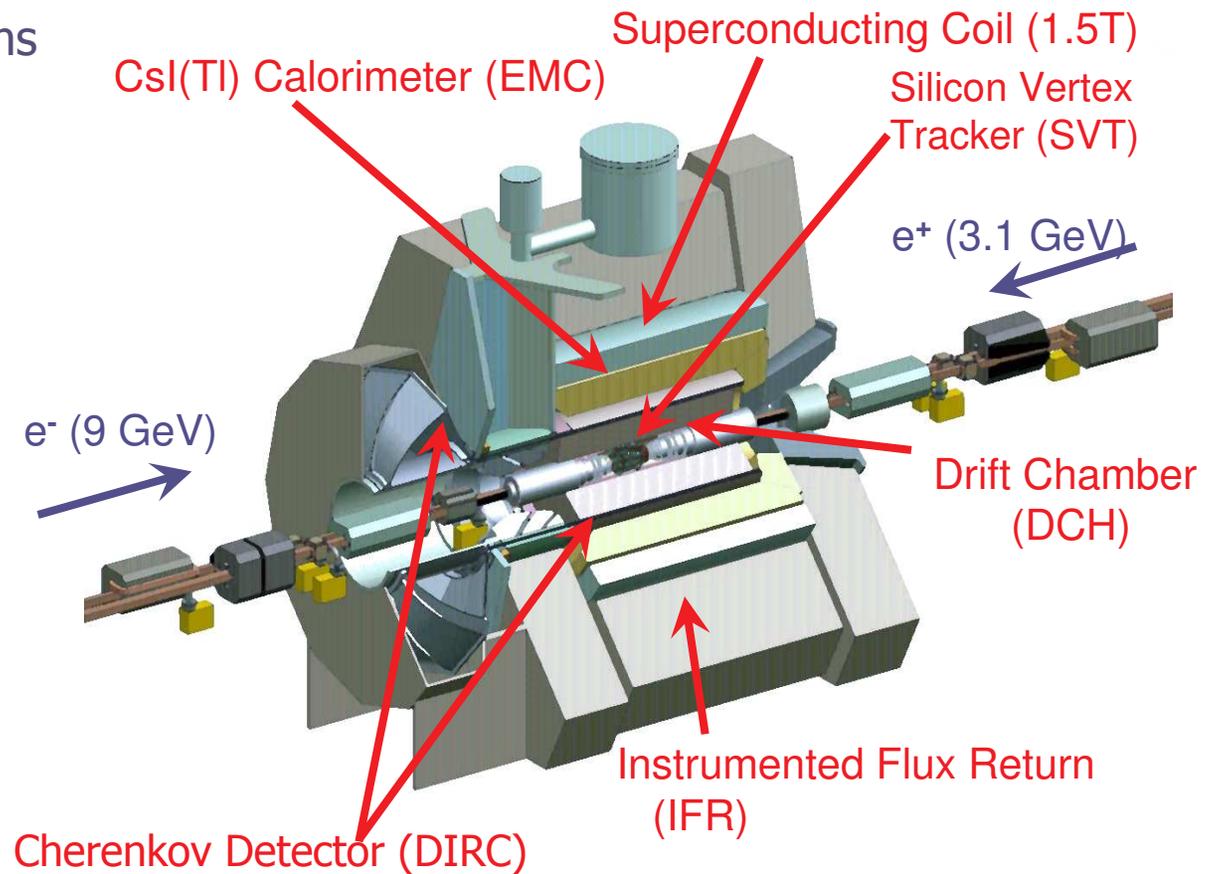
e.g. for  $B \rightarrow J/\psi K_S$ :  $C=0$ ,  $S=\sin 2\beta$

# PEP-II and BaBar

- Located at SLAC, California
- PEP-II collides 9 GeV electrons and 3.1 GeV positrons



Record peak luminosity  
 $= 9.2 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$



# cos2β with B→J/ψ K\*

- B→J/ψ K\* is a scalar→vector vector decay, contains both CP-odd and CP-even components
- cos2β appears in interference between CP-even and CP-odd components in the observables of time-dependent angular distributions

$$a(t) = P \cos \Delta m t + \sin \Delta m t (S \sin 2\beta + C \cos 2\beta)$$

where P, S, C depend on the angular decay amplitudes:

$$A_i = |A_i| e^{i\delta_i}; i = 0, \parallel, \perp$$

and the strong phases:

$$S \propto \cos(\delta_{\parallel} - \delta_0)$$

$$C \propto \cos(\delta_{\perp} - \delta_{\parallel}) \text{ and } \cos(\delta_{\perp} - \delta_0)$$

$$P \propto \sin(\delta_{\perp} - \delta_{\parallel}) \text{ and } \sin(\delta_{\perp} - \delta_0)$$

- Use neutral and charged B→J/ψK\* decays to measure strong phases up to twofold ambiguity

$$\{(\delta_{\parallel} - \delta_0), (\delta_{\perp} - \delta_0)\} \Leftrightarrow \{-(\delta_{\parallel} - \delta_0), \pi - (\delta_{\perp} - \delta_0)\}$$

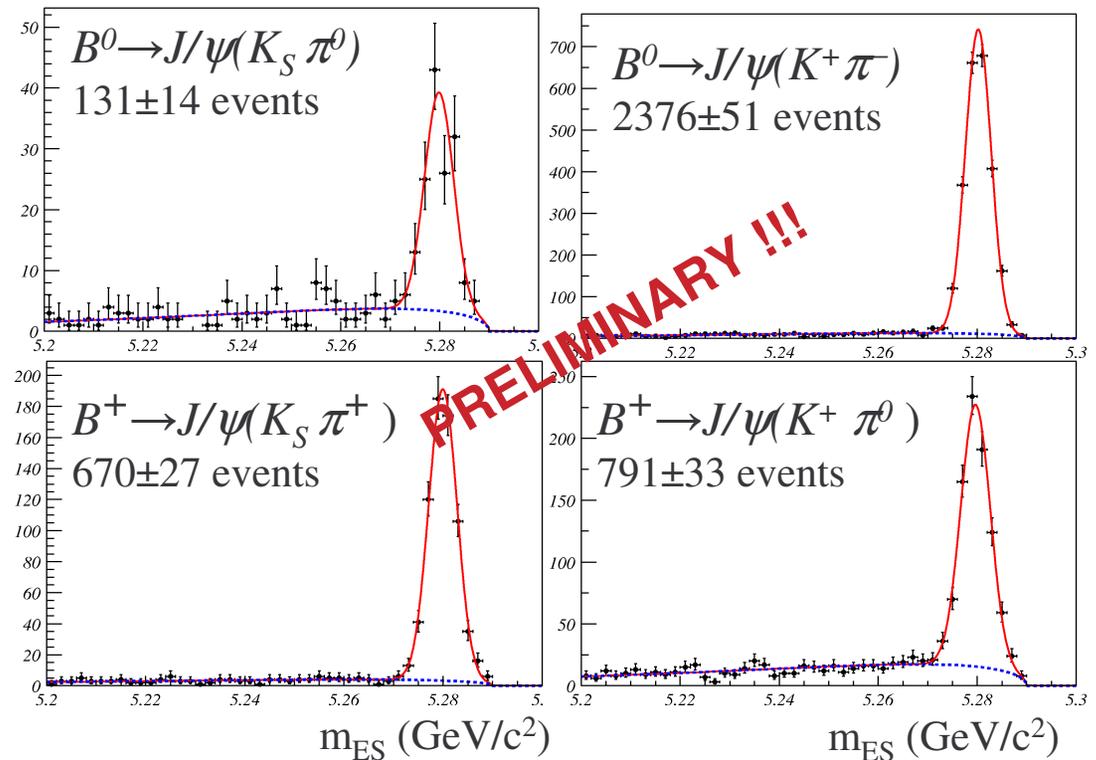
# Measurement of amplitudes

*BABAR* (81 fb<sup>-1</sup>)

Perform angular analysis of:

- $B^0 \rightarrow J/\psi K^{*0}(K^+\pi^-)$
  - $B^+ \rightarrow J/\psi K^{*+}(K_S\pi^+)$
  - $B^+ \rightarrow J/\psi K^{*+}(K^+\pi^0)$
- } +C.C.

	value	stat.	syst.
$ A_0 ^2$	$= 0.566$	$\pm 0.012$	$\pm 0.005$
$ A_{  } ^2$	$= 0.204$	$\pm 0.015$	$\pm 0.005$
$ A_{\perp} ^2$	$= 0.230$	$\pm 0.015$	$\pm 0.004$



Solution 1

$$\delta_{||} - \delta_0 = 2.729 \pm 0.101 \pm 0.052$$

$$\delta_{\perp} - \delta_0 = 0.184 \pm 0.070 \pm 0.046$$

Solution 2

$$\delta_{||} - \delta_0 = 3.554 \pm 0.101 \pm 0.052$$

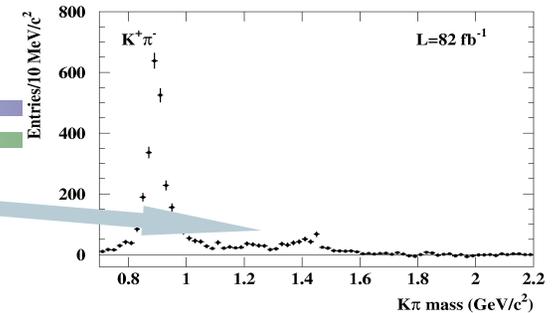
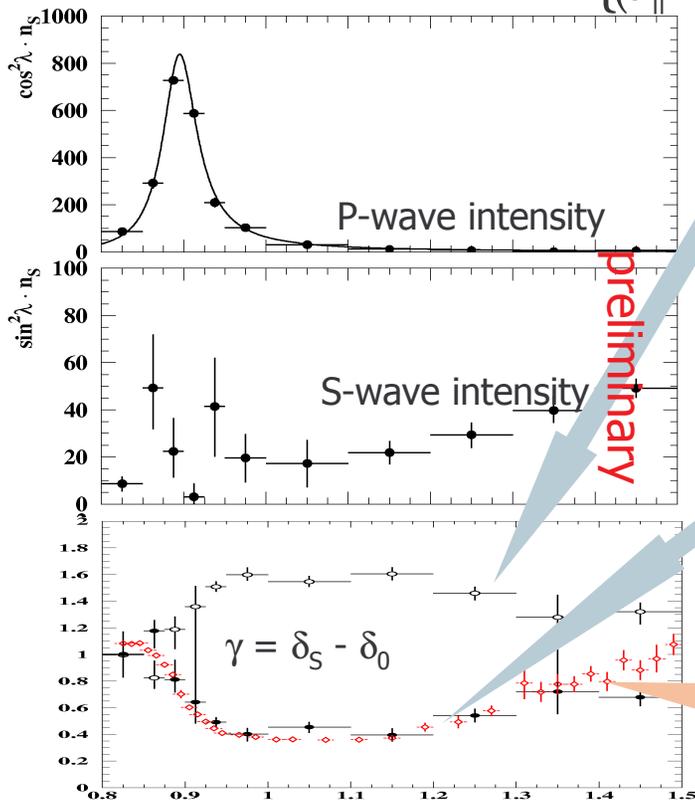
$$\delta_{\perp} - \delta_0 = 2.958 \pm 0.070 \pm 0.046$$

# Resolving the strong phase ambiguity

- Broad  $K\pi$  S-wave is known to lie in  $K^*(892)$  region
- Introduce new amplitude and new relative phase  $\gamma = (\delta_S - \delta_0)$ :

- Ambiguity becomes:

$$\{(\delta_{\parallel} - \delta_0), (\delta_{\perp} - \delta_0), \gamma\} \quad \{-(\delta_{\parallel} - \delta_0), \pi - (\delta_{\perp} - \delta_0), -\gamma\}$$



- Strong phase rotates counter-clockwise with increasing invariant mass
- In  $K^*$  region, S-wave phase rotates slowly, P-wave rotates quickly, therefore  $\gamma$  rotates clockwise
- Fit in bins of  $M(K\pi)$  P- and S- wave intensities, and  $\gamma$ , fixing to the two possible solutions in turn
- Physical behaviour observed for solution 2
- Also agrees well with LASS data for  $Kp \rightarrow K\pi(n)$  scattering..

# Determining sign of $\cos 2\beta$

Perform time-dependent fit to  $B^0 \rightarrow J/\psi K^{*0}(K_S \pi^0)$  sample:

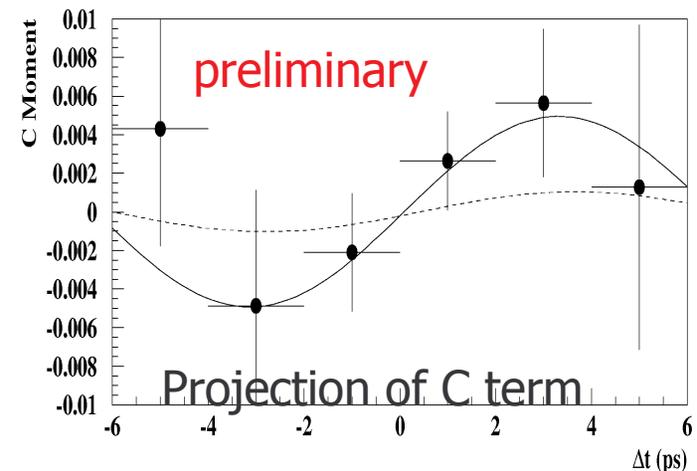
- With  $\sin 2\beta$  floating:

$$\cos 2\beta = +3.32^{+0.76}_{-0.96} \pm 0.27$$

$$\sin 2\beta = -0.10 \pm 0.57$$

- With  $\sin 2\beta$  fixed to 0.731:

$$\cos 2\beta = +2.72^{+0.50}_{-0.79} \pm 0.27$$



- If  $\sin 2\beta$  and  $\cos 2\beta$  come from the same angle, expect  $\cos 2\beta = \pm 0.68$
- Generate toy MC using both solutions:
  - Find probability for solution  $-0.68$  is  $(8.1 \pm 3.1)\%$
  - Therefore  $\cos 2\beta > 0$  at 89% CL

# cos2β contour plot

